

Package ‘CeroliOutlierDetection’

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Type Package

Title Outlier Detection Using the Iterated RMCD Method of Cerioli (2010)

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Depends R (>= 3.0.0)

Imports robustbase (>= 0.91-1)

Description Implements the iterated RMCD method of Cerioli (2010) for multivariate outlier detection via robust Mahalanobis distances. Also provides the finite-sample RMCD method discussed in the paper, as well as the methods provided in Hardin and Rocke (2005) and Green and Martin (2014).

License GPL (>= 2)

Suggests rrcov, robust, mvtnorm, alr3

URL <http://christophergreen.github.io/CeroliOutlierDetection/>

NeedsCompilation no

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 cerioli2010.fsracd.test

Finite-Sample Reweighted MCD Outlier Detection Test of Cerioli (2010)

Description

Given a set of observations, this function tests whether there are outliers in the data set and identifies outlying points. Outlier testing/identification is done using the Mahalanobis-distances based on the MCD dispersion estimate. The finite-sample reweighted MCD method of Cerioli (2010) is used to test for unusually large distances, which indicate possible outliers.

Usage

```
cerioli2010.fsracd.test(datamat,
  mcd.alpha = max.bdp.mcd.alpha(n,v),
  signif.alpha = 0.05, nsamp = 500,
  nmini = 300, trace = FALSE,
  delta = 0.025, hrdf.method=c("GM14", "HR05"))
```

Arguments

datamat	(Data Frame or Matrix) Data set to test for outliers (rows = observations, columns = variables). datamat cannot have missing values; please deal with them prior to calling this function. datamat will be converted to a matrix.
mcd.alpha	(Numeric) Value to control the fraction of observations used to compute the covariance matrices in the MCD calculation. Default value is corresponds to the maximum breakpoint case of the MCD; valid values are between 0.5 and 1. See the covMcd documentation in the robustbase library for further details.
signif.alpha	(Numeric) Desired nominal size α of the <i>individual</i> outlier test (default value is 0.05). Equivalently, significance level at which to test individual observations for outlyingness. (This is the α parameter in Cerioli (2010).) To test the intersection hypothesis of no outliers in the data, specify

$$\alpha = 1 - (1 - \gamma)^{(1/n)},$$

where γ is the nominal size of the intersection test and n is the number of observations.

nsamp	(Integer) Number of subsamples to use in computing the MCD. See the covMcd documentation in the robustbase library.
nmini	(Integer) See the covMcd documentation in the robustbase library.
trace	(Logical) See the covMcd documentation in the robustbase library.
delta	(Numeric) False-positive rate to use in the reweighting step (Step 2). Defaults to 0.025 as used in Cerioli (2010). When the ratio n/ν of sample size to dimension is very small, using a smaller delta can improve the accuracy of the method.

`hrdf.method` (String) Method to use for computing degrees of freedom and cutoff values for the non-MCD subset. The original method of Hardin and Rocke (2005) and the expanded method of Green and Martin (2014) are available as the options “HR05” and “GM14”, respectively. “GM14” is the default, as it is more accurate across a wider range of `mcd.alpha` values.

Value

`mu.hat` Location estimate from the MCD calculation

`sigma.hat` Dispersion estimate from the MCD calculation

`mahdist` Mahalanobis distances calculated using the MCD estimate

`DD` Hardin-Rocke or Green-Martin critical values for testing MCD distances. Used to produce weights for reweighted MCD. See Equation (16) in Cerioli (2010).

`weights` Weights used in the reweighted MCD. See Equation (16) in Cerioli (2010).

`mu.hat.rw` Location estimate from the reweighted MCD calculation

`sigma.hat.rw` Dispersion estimate from the reweighted MCD calculation

`mahdist.rw` a matrix of dimension `nrow(datamat)` by `length(signif.alpha)` of Mahalanobis distances computed using the finite-sample reweighted MCD methodology in Cerioli (2010). Even though the distances do not depend on `signif.alpha`, there is one column per entry in `signif.alpha` for user convenience.

`critvalfcn` Function to compute critical values for Mahalanobis distances based on the reweighted MCD; see Equations (18) and (19) in Cerioli (2010). The function takes a significance level as its only argument, and provides a critical value for each of the original observations (though there will only be two unique values, one for points included in the reweighted MCD (`weights == 1`) and one for points excluded from the reweighted MCD (`weights == 0`)).

`signif.alpha` Significance levels used in testing.

`mcd.alpha` Fraction of the observations used to compute the MCD estimate

`outliers` A matrix of dimension `nrow(datamat)` by `length(signif.alpha)` indicating whether each row of `datamat` is an outlier. The *i*-th column corresponds to the result of testing observations for outlyingness at significance level `signif.alpha[i]`.

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

Andrea Cerioli. Multivariate outlier detection with high-breakdown estimators. *Journal of the American Statistical Association*, 105(489):147-156, 2010.

Andrea Cerioli, Marco Riani, and Anthony C. Atkinson. Controlling the size of multivariate outlier tests with the MCD estimator of scatter. *Statistical Computing*, 19:341-353, 2009.

See Also

[cerioli2010.irmcd.test](#)

Examples

```

require(mvtnorm, quiet=TRUE)

#####
# dimension v, number of observations n
v <- 5
n <- 200
simdata <- array( rmvnorm(n*v, mean=rep(0,v),
  sigma = diag(rep(1,v))), c(n,v) )
#
# detect outliers with nominal sizes
# c(0.05,0.01,0.001)
#
sa <- 1. - ((1. - c(0.05,0.01,0.001))^(1./n))
results <- cerioli2010.fsrncd.test( simdata,
  signif.alpha=sa )
# count number of outliers detected for each
# significance level
colSums( results$outliers )

#####
# add some contamination to illustrate how to
# detect outliers using the fsrncd test
# 10/200 = 5% contamination
simdata[ sample(n,10), ] <- array(
  rmvnorm( 10*v, mean=rep(2,v), sigma = diag(rep(1,v))),
  c(10,v)
)
results <- cerioli2010.fsrncd.test( simdata,
  signif.alpha=sa )
colMeans( results$outliers )

## Not run:
#####
# example of how to ensure the size of the intersection test is correct

n.sim <- 5000
simdata <- array(
  rmvnorm(n*v*n.sim, mean=rep(0,v), sigma=diag(rep(1,v))),
  c(n,v,n.sim)
)
# in practice we'd do this using one of the parallel processing
# methods out there
sa <- 1. - ((1. - 0.01)^(1./n))
results <- apply( simdata, 3, function(dm) {
  z <- cerioli2010.fsrncd.test( dm,
    signif.alpha=sa )
  # true if outliers were detected in the data, false otherwise
  any(z$outliers[,1,drop=TRUE])
}

```

```

    })
    # count the percentage of samples where outliers were detected;
    # should be close to the significance level value used (0.01) in these
    # samples for the intersection test.
    mean(results)

## End(Not run)

```

```
cerioli2010.irmcd.test
```

Iterated RMCD test of Cerioli (2010)

Description

Given a set of observations, this function tests whether there are outliers in the data set and identifies outlying points. Outlier testing/identification is done using the Mahalanobis-distances based on the MCD dispersion estimate. The iterated reweighted MCD method of Cerioli (2010) is used to ensure the intersection test has the specified nominal size (Type I error rate).

Usage

```

cerioli2010.irmcd.test(datamat,
  mcd.alpha = max.bdp.mcd.alpha(n,v),
  signif.gamma = 0.05, nsamp = 500,
  nmini = 300, trace = FALSE,
  delta = 0.025, hrdf.method=c("GM14", "HR05"))

```

Arguments

datamat	(Data Frame or Matrix) Data set to test for outliers (rows = observations, columns = variables). datamat cannot have missing values; please deal with them prior to calling this function. datamat will be converted to a matrix.
mcd.alpha	(Numeric) Value to control the fraction of observations used to compute the covariance matrices in the MCD calculation. Default value is corresponds to the maximum breakpoint case of the MCD; valid values are between 0.5 and 1. See the covMcd documentation in the robustbase library for further details.
signif.gamma	(Numeric) Desired nominal size of the <i>intersection</i> outlier test (e.g., 0.05), i.e., a test that there are no outliers in the data. (This is the γ parameter in Cerioli (2010).) The corresponding α parameter for testing individual observations for outlyingness will be calculated from γ as

$$\alpha = 1 - (1 - \gamma)^{(1/n)}.$$

nsamp	(Integer) Number of subsamples to use in computing the MCD. See the covMcd documentation in the robustbase library.
nmini	(Integer) See the covMcd documentation in the robustbase library.

trace	(Logical) See the <code>covMcd</code> documentation in the <code>robustbase</code> library.
delta	(Numeric) False-positive rate to use in the reweighting step (Step 2). Defaults to 0.025 as used in Cerioli (2010). When the ratio n/ν of sample size to dimension is very small, using a smaller delta can improve the accuracy of the method.
hrdf.method	(String) Method to use for computing degrees of freedom and cutoff values for the non-MCD subset. The original method of Hardin and Rocke (2005) and the expanded method of Green and Martin (2014) are available as the options “HR05” and “GM14”, respectively. “GM14” is the default, as it is more accurate across a wider range of <code>mcd.alpha</code> values.

Details

Calls the finite-sample reweighted MCD (FSRMCD) outlier detection function `cerioli2010.fsracd.test` first to test for the existence of any outliers in the data. If the FSRMCD method rejects the null hypothesis of no outliers in the data, individual observations are then tested for outlyingness using the critical value function returned by `cerioli2010.fsracd.test` with significance γ .

Value

outliers	A matrix of dimension <code>nrow(datamat)</code> by <code>length(signif.gamma)</code> indicating whether each row of <code>datamat</code> is an outlier. The i -th column corresponds to the result of testing observations for outlyingness at significance level <code>signif.gamma[i]</code> .
mahdist.rw	a matrix of dimension <code>nrow(datamat)</code> by <code>length(signif.gamma)</code> of Mahalanobis distances computed using the finite-sample reweighted MCD methodology in Cerioli (2010). Even though the distances do not depend on <code>signif.gamma</code> , there is one column per entry in <code>signif.gamma</code> for user convenience.

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

Andrea Cerioli. Multivariate outlier detection with high-breakdown estimators. *Journal of the American Statistical Association*, 105(489):147-156, 2010.

Andrea Cerioli, Marco Riani, and Anthony C. Atkinson. Controlling the size of multivariate outlier tests with the MCD estimator of scatter. *Statistical Computing*, 19:341-353, 2009.

See Also

[cerioli2010.fsracd.test](#)

Examples

```
require(mvtnorm, quiet=TRUE)

#####
# dimension v, number of observations n
v <- 5
```

```

n <- 200
simdata <- array( rmvnorm(n*v, mean=rep(0,v),
  sigma = diag(rep(1,v))), c(n,v) )
# detect outliers
results <- cerioli2010.irmcd.test( simdata,
  signif.gamma=c(0.05,0.01,0.001) )
# count number of outliers detected for each
# significance level
colSums( results$outliers )

#####
# add some contamination to illustrate how to
# detect outliers using the irmcd test
# 10/200 = 5% contamination
simdata[ sample(n,10), ] <- array(
  rmvnorm( 10*v, mean=rep(2,v), sigma = diag(rep(1,v))),
  c(10,v)
)
results <- cerioli2010.irmcd.test( simdata,
  signif.gamma=0.01 )
mean( results$outliers[,1,drop=TRUE] )

#####
# banknote example from Cerioli (2010)
## Not run:

require(rrcov) # for CovMcd
require(alr3) # banknote data set lives here
data(banknote, package="alr3")
# length, width of left edge, width of right edge,
# width of bottom edge, width of top edge, length
# of image diagonal, counterfeit (1=counterfeit)

bnk.gamma <- 0.01
# genuine banknotes
# classical mean and covariance
banknote.real <- banknote[ banknote[, "Y"]==0, 1:6 ]
cov.cls <- CovClassic( banknote.real )
# 1 - (1 - 0.01)^(1/100) quantile of scaled-Beta distribution
# with m=100 and v=6
bnk.m <- nrow( banknote.real )
bnk.v <- ncol( banknote.real )
bnk.alpha <- 1. - ((1. - bnk.gamma)^(1./bnk.m))
cutoff.cls <- (bnk.m-1.)*(bnk.m-1.)*qbeta( 1. - bnk.alpha, bnk.v/2.,
(bnk.m - bnk.v - 1.)/2.)/bnk.m
# Figure 4 (left) in Cerioli (2010)
plot( getDistance( cov.cls ), xlab="Index number",
ylab="Squared Mahalanobis Distance", type="p",
ylim=c(0,45)
)
abline( h=cutoff.cls )

```

```

# reweighted MCD, maximum breakdown point case
cov.rob <- CovMcd( banknote.real,
alpha=floor((bnk.m + bnk.v + 1.)/2.)/bnk.m, nsamp="best" )
# cutoff using chi-squared individually
cutoff.rmcdind <- qchisq(1. - bnk.gamma, df=bnk.v)
# cutoff using simultaneous chi-square
cutoff.rmcdsim <- qchisq(1. - bnk.alpha, df=bnk.v)
# scaled-F cutoff using FSRMCD
# cutoff value is returned by critvalfcn for observations
# with weight=0
tmp.fsrncd <- cerioli2010.fsrncd.test( banknote.real,
signif.alpha=bnk.alpha )
cutoff.fsrncd <- unique(tmp.fsrncd$critvalfcn( bnk.alpha )[tmp.fsrncd$weights==0])
# Figure 4 (right)
plot( getDistance( cov.rob ), xlab="Index number",
ylab="Squared Robust Reweighted Distance", type="p",
ylim=c(0,45)
)
abline( h=cutoff.rmcdind, lty="dotted" )
abline( h=cutoff.rmcdsim, lty="dashed" )
abline( h=cutoff.fsrncd, lty="solid" )
legend( "topright", c("RMCD_ind","RMCD","FSRMCD"),
lty=c("dotted","dashed","solid") )

# forged banknotes
# classical mean and covariance
banknote.fake <- banknote[ banknote[,"Y"]==1, 1:6 ]
cov.cls <- CovClassic( banknote.fake )
# 1 - (1 - 0.01)^(1/100) quantile of scaled-Beta distribution
# with m=100 and v=6
bnk.m <- nrow( banknote.fake )
bnk.v <- ncol( banknote.fake )
bnk.alpha <- 1. - ((1. - bnk.gamma)^(1./bnk.m))
cutoff.cls <- (bnk.m-1.)*(bnk.m-1.)*qbeta( 1. - bnk.alpha, bnk.v/2.,
(bnk.m - bnk.v - 1.)/2.)/bnk.m
# Figure 5 (left) in Cerioli (2010)
plot( getDistance( cov.cls ), xlab="Index number",
ylab="Squared Mahalanobis Distance", type="p",
ylim=c(0,45)
)
abline( h=cutoff.cls )

# reweighted MCD, maximum breakdown point case
cov.rob <- CovMcd( banknote.fake,
alpha=floor((bnk.m + bnk.v + 1.)/2.)/bnk.m, nsamp="best" )
# cutoff using chi-squared individually
cutoff.rmcdind <- qchisq(1. - bnk.gamma, df=bnk.v)
# scaled-F cutoff using FSRMCD
# cutoff value is returned by critvalfcn for observations
# with weight=0
tmp.fsrncd <- cerioli2010.fsrncd.test( banknote.fake,
signif.alpha=bnk.alpha )

```



```

cutoff.fsrncd <- unique(tmp.fsrncd$critvalfcn( bnk.alpha )[tmp.fsrncd$weights==0])
cutoff.irmcd <- unique(tmp.fsrncd$critvalfcn( bnk.gamma )[tmp.fsrncd$weights==0])
# Figure 5 (right) in Cerioli (2010)
plot( getDistance( cov.rob ), xlab="Index number",
      ylab="Squared robust reweighted Distance", type="p",
      ylim=c(0,150)
    )
abline( h=cutoff.rmcdind, lty="dotted" )
abline( h=cutoff.fsrncd, lty="dashed" )
abline( h=cutoff.irmcd, lty="solid" )
legend( "topright", c("RMCD_ind","FSRNCd","IRMCD"),
      lty=c("dotted","dashed","solid" )
    )

## End(Not run)

#####
# example of how to ensure the size of the intersection test is correct
## Not run:
n.sim <- 5000
simdata <- array(
  rmvnorm(n*v*n.sim, mean=rep(0,v), sigma=diag(rep(1,v))),
  c(n,v,n.sim)
)
# in practice we'd do this using one of the parallel processing
# methods out there
results <- apply( simdata, 3, function(dm) {
  z <- cerioli2010.irmcd.test( dm,
    signif.gamma=0.01 )
  # true if outliers were detected in the data, false otherwise
  any(z$outliers[,1,drop=TRUE])
})
# count the percentage of samples where outliers were detected;
# should be close to the significance level value used (0.01) in these
# samples for the intersection test
mean(results)

## End(Not run)

```

CerioliOutlierDetection

*CerioliOutlierDetection: package for implementing the Iterated
Reweighted MCD outlier detection method of Cerioli (2010)*

Description

Implements the outlier detection methodology of Cerioli (2010) based on Mahalanobis distances and the minimum covariance determinant (MCD) estimate of dispersion. Also provides critical values for testing outlyingness of MCD-based Mahalanobis distances using the distribution approximations developed by Hardin and Rocke (2005) and Green and Martin (2014).

Details

Package: CerioliOutlierDetection
Type: Package
Version: 1.1.5

The function `cerioli2010.irmcd.test()` provides the outlier detection methodology of Cerioli (2010), and is probably the best place for a new user of this package to start. See the documentation for that function for examples.

This package was also used to produce the results presented in Green and Martin (2014). There is a companion R package, `HardinRockeExtension`, that provides code that can be used to replicate the results of that paper. The package `HardinRockeExtension` is available from Christopher G. Green's GitHub: <https://github.com/christophergreen/HardinRockeExtension>.

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>, with advice and support from Doug Martin.

References

Andrea Cerioli. Multivariate outlier detection with high-breakdown estimators. *Journal of the American Statistical Association*, 105(489):147-156, 2010.

C. G. Green and R. Douglas Martin. An extension of a method of Hardin and Rocke, with an application to multivariate outlier detection via the IRMCD method of Cerioli. Working Paper, 2014. Available from http://students.washington.edu/cggreen/uwstat/papers/cerioli_extension.pdf

J. Hardin and D. M. Rocke. The distribution of robust distances. *Journal of Computational and Graphical Statistics*, 14:928-946, 2005.

ch99AsymptoticDF

Croux and Haesbroeck (1999) asymptotic parameters for the MCD estimate

Description

Computes the asymptotic Wishart degrees of freedom and consistency constant for the MCD robust dispersion estimate (for data with a model normal distribution) as described in Hardin and Rocke (2005) and using the formulas described in Croux and Haesbroeck (1999).

Usage

```
ch99AsymptoticDF(n.obs, p.dim, mcd.alpha)
```

Arguments

n.obs	(Integer) Number of observations
p.dim	(Integer) Dimension of the data, i.e., number of variables.
mcd.alpha	(Numeric) Value that determines the fraction of the sample used to compute the MCD estimate. $1 - mcd.alpha$ will be the fraction of observations that are omitted in computing the MCD estimate. The default value is

$$\lfloor (n.obs + p.dim + 1)/2 \rfloor / n.obs,$$

which yields the MCD estimate with the maximum possible breakdown point.

Details

The consistency factor `c.alpha` is already available in the `robustbase` library as the function `.MCDcons`. (See the code for `covMcd`.) `ch99AsymptoticDF` uses the result of `.MCDcons` for consistency.

The computation of the asymptotic Wishart degrees of freedom parameter `m` follows the Appendix of Hardin and Rocke (2005).

Value

<code>c.alpha</code>	the asymptotic consistency coefficient for the MCD estimate of the dispersion matrix
<code>m.hat.asy</code>	the asymptotic degrees of freedom for the Wishart distribution approximation to the distribution of the MCD dispersion estimate

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

Christopher Croux and Gentiane Haesbroeck. Influence function and efficiency of the minimum covariance determinant scatter matrix estimator. *Journal of Multivariate Analysis*, 71:161-190, 1999.

J. Hardin and D. M. Rocke. The distribution of robust distances. *Journal of Computational and Graphical Statistics*, 14:928-946, 2005.

Examples

```
# compare to table from p941 of Hardin and Rocke (2005)
ch99AsymptoticDF( 50, 5)
ch99AsymptoticDF( 100,10)
ch99AsymptoticDF( 500,10)
ch99AsymptoticDF(1000,20)
```

hr05AdjustedDF	<i>Adjusted Degrees of Freedom for Testing Robust Mahalanobis Distances for Outlyingness</i>
----------------	--

Description

Computes the degrees of freedom for the adjusted F distribution for testing Mahalanobis distances calculated with the minimum covariance determinant (MCD) robust dispersion estimate (for data with a model normal distribution) as described in Hardin and Rocke (2005) or in Green and Martin (2014).

Usage

```
hr05AdjustedDF( n.obs, p.dim, mcd.alpha, m.asy, method = c("HR05", "GM14"))
```

Arguments

n.obs	(Integer) Number of observations
p.dim	(Integer) Dimension of the data, i.e., number of variables.
mcd.alpha	(Numeric) Value that determines the fraction of the sample used to compute the MCD estimate. Default value corresponds to the maximum breakdown point case of the MCD.
m.asy	(Numeric) Asymptotic Wishart degrees of freedom. The default value uses ch99AsymptoticDF to obtain the the asymptotic value, but the user can also provide a pre-computed value.
method	Either "HR05" to use the method of Hardin and Rocke (2005), or "GM14" to use the method of Green and Martin (2014).

Details

Hardin and Rocke (2005) derived an approximate F distribution for testing robust Mahalanobis distances, computed using the MCD estimate of dispersion, for outlyingness. This distribution improves upon the standard χ^2 distribution for identifying outlying points in data set. The method of Hardin and Rocke was designed to work for the maximum breakdown point case of the MCD, where

$$\alpha = \lfloor (n.obs + p.dim + 1)/2 \rfloor / n.obs.$$

Green and Martin (2014) extended this result to $MCD(\alpha)$, where α controls the size of the sample used to compute the MCD estimate, as well as the breakdown point of the estimator.

With argument `method = "HR05"` the function returns m_{pred} as given in Equation 3.4 of Hardin and Rocke (2005). The Hardin and Rocke method is only supported for the maximum breakdown point case; an error will be generated for other values of `mcd.alpha`.

The argument `method = "GM14"` uses the extended methodology described in Green and Martin (2014) and is available for all values of `mcd.alpha`.

Value

Returns the adjusted F degrees of freedom based on the asymptotic value, the dimension of the data, and the sample size.

Note

This function is typically not called directly by users; rather it is used in the construction of other functions.

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

C. G. Green and R. Douglas Martin. An extension of a method of Hardin and Rocke, with an application to multivariate outlier detection via the IRMCD method of Cerioli. Working Paper, 2014. Available from http://students.washington.edu/cggreen/uwstat/papers/cerioli_extension.pdf

J. Hardin and D. M. Rocke. The distribution of robust distances. *Journal of Computational and Graphical Statistics*, 14:928-946, 2005.

See Also

[ch99AsymptoticDF](#)

Examples

```
hr05tester <- function(n,p) {
  a <- floor( (n+p+1)/2 )/n
  hr05AdjustedDF( n, p, a, ch99AsymptoticDF(n,p,a)$m.hat.asy, method="HR05" )
}
# compare to m_pred in table on page 941 of Hardin and Rocke (2005)
hr05tester( 50, 5)
hr05tester( 100,10)
hr05tester( 500,10)
hr05tester(1000,20)

# using default arguments
hr05tester <- function(n,p) {
  hr05AdjustedDF( n, p, method="HR05" )
}
# compare to m_pre in table on page 941 of Hardin and Rocke (2005)
hr05tester( 50, 5)
hr05tester( 100,10)
hr05tester( 500,10)
hr05tester(1000,20)

# Green and Martin (2014) improved method
hr05tester <- function(n,p) {
  hr05AdjustedDF( n, p, method="GM14" )
}
```

```

}
# compare to m_sim in table on page 941 of Hardin and Rocke (2005)
hr05tester( 50, 5)
hr05tester( 100,10)
hr05tester( 500,10)
hr05tester(1000,20)

```

hr05CriticalValue	<i>Hardin and Rocke (2005) Critical Value for Testing MCD-based Mahalanobis Distances</i>
-------------------	---

Description

Hardin and Rocke (2005) provide an approximate F distribution for testing whether Mahalanobis distances calculated using the MCD dispersion estimate are unusually large, and hence, indicative of outliers in the data.

Usage

```
hr05CriticalValue(em, p.dim, signif.alpha)
```

Arguments

em	(Numeric) Degrees of freedom for Wishart distribution approximation to the MCD scatter matrix.
p.dim	(Integer) Dimension of the data, i.e., number of variables.
signif.alpha	(Numeric) Significance level for testing the null hypothesis

Details

Hardin and Rocke (2005) derived an F distributional approximation for the Mahalanobis distances of the observations that were excluded from the MCD calculation; see equation 3.2 on page 938 of the paper.

It is assumed here that the MCD covariance estimate used in the Mahalanobis distance calculation was adjusted by the consistency factor, so it is not included in the calculation here. (If one needs the consistency factor it is returned by the function [ch99AsymptoticDF](#) in this package or by the function `.MCDcons` in the `robustbase` package.)

Value

The appropriate cutoff value (from the F distributional approximation) for testing whether a Mahalanobis distance is unusually large at the specified significance level.

Note

It can happen that one of the F distribution parameters, $m - p + 1$, is non-positive, in which case `qf` will return `NaN`. `hr05CriticalValue` will issue a warning in this case, and return `NA`.

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

J. Hardin and D. M. Rocke. The distribution of robust distances. *Journal of Computational and Graphical Statistics*, 14:928-946, 2005.

See Also

[hr05AdjustedDF](#), [hr05CutoffMvnormal](#)

Examples

```
hr05CriticalValue( hr05AdjustedDF( 1000, 20 ), 20, 0.05 )
```

hr05CutoffMvnormal	<i>Corrected Critical Values for Testing MCD-based Mahalanobis Distances</i>
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Description

Provides critical values for testing for outlyingness using MCD-based Mahalanobis distances and the F distributional approximation developed by Hardin and Rocke (2005) or the enhancement by Green and Martin (2014).

Usage

```
hr05CutoffMvnormal(n.obs, p.dim, mcd.alpha, signif.alpha,  
method = c("GM14", "HR05"), use.consistency.correction = FALSE)
```

Arguments

n.obs	(Integer) Number of observations
p.dim	(Integer) Dimension of the data, i.e., number of variables.
mcd.alpha	(Numeric) Value that determines the fraction of the sample used to compute the MCD estimate. Defaults to the value used in the maximum breakdown point case of the MCD.
signif.alpha	(Numeric) Significance level for testing the null hypothesis. Default value is 0.05.
method	Either "HR05" to use the method of Hardin and Rocke (2005), or "GM14" to use the method of Green and Martin (2014).
use.consistency.correction	(Logical) By default, the method does not multiply the cutoff values by the consistency correction for the MCD, under the assumption that the correction was applied during the calculation of the MCD-based Mahalanobis distances. Specify TRUE to add the correction factor if you need it for your application.

Details

hr05CutoffMvnormal is the typical way in which a user will calculate critical values for testing outlyingness via MCD-based Mahalanobis distances. The critical values come from the F distributional approximation derived by Hardin and Rocke (2005). One can use either the corrected degrees of freedom parameter derived in that paper (which was only shown to work for the maximum breakdown point case of MCD), or the correction derived in Green and Martin (2014) for arbitrary values of `mcd.alpha`.

Value

<code>cutoff.pred</code>	Critical value based on the predicted Wishart degrees of freedom <code>m.pred</code>
<code>cutoff.asy</code>	Critical value based on the asymptotic Wishart degrees of freedom <code>m.asy</code>
<code>c.alpha</code>	The value of the consistency correction factor, c_α
<code>m.asy</code>	Asymptotic Wishart degrees of freedom parameter
<code>m.pred</code>	Predicted Wishart degrees of freedom (using the method specified in <code>method</code>)
<code>n.obs</code>	Number of observations
<code>p.dim</code>	Number of variables

Author(s)

Written and maintained by Christopher G. Green <christopher.g.green@gmail.com>

References

C. G. Green and R. Douglas Martin. An extension of a method of Hardin and Rocke, with an application to multivariate outlier detection via the IRMCD method of Cerioli. Working Paper, 2014. Available from http://students.washington.edu/cggreen/uwstat/papers/cerioli_extension.pdf

J. Hardin and D. M. Rocke. The distribution of robust distances. *Journal of Computational and Graphical Statistics*, 14:928-946, 2005.

See Also

[hr05CriticalValue](#), [hr05AdjustedDF](#)

Examples

```
# examples from page 941 of Hardin and Rocke
hr05CutoffMvnormal(n.obs=50 , p.dim=5 , signif.alpha=0.05)
hr05CutoffMvnormal(n.obs=100 , p.dim=10 , signif.alpha=0.05)
hr05CutoffMvnormal(n.obs=500 , p.dim=10 , signif.alpha=0.05)
hr05CutoffMvnormal(n.obs=1000, p.dim=20, signif.alpha=0.05)
```


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