

# Package ‘Copula.Markov’

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**Type** Package

**Title** Copula-Based Estimation and Statistical Process Control for  
Serially Correlated Time Series

**Version** 2.4

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**Author** Takeshi Emura, Xinwei Huang, Weiru Chen, Ting-Hsuan Long

**Maintainer** Takeshi Emura <takeshiemura@gmail.com>

**Description** Estimation and statistical process control are performed under  
copula-based time-series models.

Available are statistical methods in Long and Emura (2014 JCSA),  
Emura et al. (2017 Commun Stat-Simul) <DOI:10.1080/03610918.2015.1073303>,  
Huang and Emura(2019, in revision) and Huang, Chen and Emura (2019-, in revision).

**License** GPL-2

**NeedsCompilation** no

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Copula.Markov-package *Copula-Based Estimation and Statistical Process Control for Serially Correlated Time Series*

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### Description

Copulas are applied to model a Markov dependence for serially correlated time series. The Clayton and Joe copulas are available to specify the dependence structure. The normal and binomial distributions are available for the marginal model. Maximum likelihood estimation is implemented for estimating parameters, and a Shewhart control chart is drawn for performing statistical process control.

### Details

Package:	Copula.Markov
Type:	Package
Version:	2.4
Date:	2019-03-24
License:	GPL-2

### Author(s)

Emura T, Chen WR, Long TH, Huang X. Maintainer: Takeshi Emura <takeshiemura@gmail.com>

### References

Chen W (2018) Copula-based Markov chain model with binomial data, NCU Library

Huang XW, Chen W, Emura T (2019-), A control chart using a copula-based Markov chain for attribute data, revision

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TH and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

Huang XW, Emura T (2019-), Model diagnostic procedures for copula-based Markov chain models for statistical process control, in revision

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Clayton.Markov.DATA    *Generating Time Series Data Under a Copula-Based Markov Chain Model with the Clayton Copula*

---

**Description**

Time-series datasets are generated under a copula-based Markov chain model with the Clayton copula.

**Usage**

```
Clayton.Markov.DATA(n, mu, sigma, alpha)
```

**Arguments**

n	sample size
mu	mean
sigma	standard deviation
alpha	association parameter

**Details**

$-1 < \alpha < 0$  for negative association;  $\alpha > 0$  for positive association

**Value**

time series data

**Author(s)**

Takeshi Emura

**References**

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TH and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

**Examples**

```
set.seed(1)
Y=Clayton.Markov.DATA(n=1000,mu=0,sigma=1,alpha=8)
Clayton.Markov.MLE(Y,plot=TRUE)
```

---

Clayton.Markov.DATA.binom

*Generating Time Series Data Under a Copula-Based Markov Chain Model with the Clayton Copula and Binomial Margin.*

---

## Description

Time-series datasets are generated under a copula-based Markov chain model with the Clayton copula and binomial margin.

## Usage

```
Clayton.Markov.DATA.binom(n, size, prob, alpha)
```

## Arguments

n	number of observations
size	number of binomial trials
prob	binomial probability; $0 < p < 1$
alpha	association parameter

## Details

$-1 < \alpha < 0$  for negative association;  $\alpha > 0$  for positive association

## Value

time series data

## Author(s)

Huang XW, Chen W, Emura T

## References

Chen W (2018) Copula-based Markov chain model with binomial data, NCU Library

Huang XW, Chen W, Emura T (2019) A control chart using a copula-based Markov chain for attribute data, in revision.

## Examples

```
size=50
prob=0.5
alpha=2
set.seed(1)
Y=Clayton.Markov.DATA.binom(n=500,size,prob,alpha)
### sample mean and SD ###
```

```
mean(Y)
sd(Y)
### true mean and SD ###
size*prob
sqrt(size*prob*(1-prob))
```

---

Clayton.Markov.GOF      *Goodness-of-fit test*

---

### Description

Perform a parametric bootstrap test.

### Usage

```
Clayton.Markov.GOF(Y, k = 3, D = 1, B = 200, GOF.plot=FALSE)
```

### Arguments

Y	vector of datasets
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
D	diameter for U(-D, D) used in randomized Newton-Raphson
B	the number of Bootstrap replications
GOF.plot	if TRUE, show the model diagnostic plots for B bootstrap replications

### Value

CM	Cramer-von Mises test
KS	Kolmogorov-Smirnov test

### Author(s)

Takeshi Emura

### References

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TH and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

Huang XW, Emura T (2019-), Model diagnostic procedures for copula-based Markov chain models for statistical process control, in revision

**Examples**

```
set.seed(1)
Y=Clayton.Markov.DATA(n=1000,mu=0,sigma=1,alpha=2)
Clayton.Markov.GOF(Y,B=5,GOF.plot=TRUE)
```

---

```
Clayton.Markov.GOF.binom
```

*Goodness-of-fit test*

---

**Description**

Perform a parametric bootstrap test.

**Usage**

```
Clayton.Markov.GOF.binom(Y, k = 3, size, B = 200,GOF.plot=FALSE)
```

**Arguments**

Y	vector of datasets
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
size	number of binomial trials
B	the number of Bootstrap replications
GOF.plot	if TRUE, show the model diagnostic plots for B bootstrap replications

**Value**

CM	Cramer-von Mises test
KS	Kolmogorov-Smirnov test

**Author(s)**

Huang XW, Emura T

**References**

Huang XW, Chen W, Emura T (2019) A control chart using a copula-based Markov chain for attribute data, in revision.

**Examples**

```
size=50
prob=0.5
alpha=2
set.seed(1)
Y=Clayton.Markov.DATA.binom(n=500,size,prob,alpha)
Clayton.Markov.GOF.binom(Y,size=size,B=5,k=3,GOF.plot=TRUE) ## B=5 to save time
```

---

Clayton.Markov.MLE      *Maximum Likelihood Estimation and Statistical Process Control Under the Clayton Copula*

---

### Description

The maximum likelihood estimates are produced and the Shewhart control chart is drawn with k-sigma control limits (e.g., 3-sigma). The dependence model follows the Clayton copula and the marginal (stationary) distribution follows the normal distribution.

### Usage

```
Clayton.Markov.MLE(Y, k = 3, D = 1, plot = TRUE, GOF=FALSE)
```

### Arguments

Y	vector of datasets
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
D	diameter for U(-D, D) used in randomized Newton-Raphson
plot	show the control chart if TRUE
GOF	show the model diagnostic plot if TRUE

### Value

estimates	estimates
out_of_control	IDs for out-of-control points
Gradient	gradients (must be zero)
Hessian	Hessian matrix
Mineigenvalue_Hessian	Minimum eigenvalue for the Hessian matrix
CM.test	Cramer-von Mises test statistics
KS.test	Kolmogorov-Smirnov test statistics

### Author(s)

Takeshi Emura

### References

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TH and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

**Examples**

```
set.seed(1)
Y=Clayton.Markov.DATA(n=1000,mu=0,sigma=1,alpha=2)
Clayton.Markov.MLE(Y,plot=TRUE)
```

---

Clayton.Markov.MLE.binom

*Maximum Likelihood Estimation and Statistical Process Control Under the Clayton Copula*

---

**Description**

The maximum likelihood estimates are produced and the Shewhart control chart is drawn with k-sigma control limits (e.g., 3-sigma). The dependence model follows the Clayton copula and the marginal (stationary) distribution follows the normal distribution.

**Usage**

```
Clayton.Markov.MLE.binom(Y, size, k = 3, method="nlm", plot = TRUE, GOF=FALSE)
```

**Arguments**

Y	vector of observations
size	numbe of binomial trials
method	nlm or Newton
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
plot	show the control chart if TRUE
GOF	show the model diagnostic plot if TRUE

**Value**

p	estimate, SE, and 95CI
alpha	estimate, SE, and 95CI
out_of_control	IDs for out-of-control points
Gradient	gradients (must be zero)
Hessian	Hessian matrix
Mineigenvalue_Hessian	Minimum eigenvalue for the Hessian matrix

**Author(s)**

Huang XW, Emura T



## References

Chen W (2018) Copula-based Markov chain model with binomial data, NCU Library

Huang XW, Chen W, Emura T (2019) A control chart using a copula-based Markov chain for attribute data, in revision.

## Examples

```
size=50
prob=0.5
alpha=2
set.seed(1)
Y=Clayton.Markov.DATA.binom(n=500,size,prob,alpha)
Clayton.Markov.MLE.binom(Y,size=size,k=3,plot=TRUE)
```

---

Clayton.Markov2.DATA *Generating Time Series Data Under a Copula-Based 2nd-order Markov Chain Model with the Clayton Copula*

---

## Description

Time-series datasets are generated under a copula-based 2nd order Markov chain model with the Clayton copula.

## Usage

```
Clayton.Markov2.DATA(n, mu, sigma, alpha)
```

## Arguments

n	sample size
mu	mean
sigma	standard deviation
alpha	association parameter

## Details

-1<alpha<0 for negative association; alpha>0 for positive association

## Value

time series data

## Author(s)

Xinwei Huang and Takeshi Emura

**References**

Huang XW, Emura T (2019-), Model diagnostic procedures for copula-based Markov chain models for statistical process control, in revision

**Examples**

```
Clayton.Markov2.DATA(n = 100, mu = 0, sigma = 1, alpha = 2)
```

---

Clayton.Markov2.MLE     *Maximum Likelihood Estimation and Statistical Process Control Under the Clayton Copula with a 2nd order Markov chain.*

---

**Description**

The maximum likelihood estimates are produced and the Shewhart control chart is drawn with k-sigma control limits (e.g., 3-sigma). The dependence model follows the Clayton copula and the marginal (stationary) distribution follows the normal distribution.

**Usage**

```
Clayton.Markov2.MLE(Y, k = 3, D = 1, plot = TRUE, GOF=FALSE)
```

**Arguments**

Y	vector of datasets
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
D	diameter for U(-D, D) used in randomized Newton-Raphson
plot	show the control chart if TRUE
GOF	show the model diagnostic plot if TRUE

**Value**

estimates	estimates
out_of_control	IDs for out-of-control points
Gradient	gradients (must be zero)
Hessian	Hessian matrix
Mineigenvalue_Hessian	Minimum eigenvalue for the Hessian matrix

**Author(s)**

Xinwei Huang and Takeshi Emura

**References**

Huang XW, Emura T (2019-), Model diagnostic procedures for copula-based Markov chain models for statistical process control, in revision

**Examples**

```
Y = c(0.265, 0.256, 0.261, 0.261, 0.260, 0.257, 0.258, 0.263, 0.254, 0.254,
      0.258, 0.256, 0.256, 0.265, 0.270, 0.267, 0.270, 0.267, 0.266, 0.271,
      0.270, 0.264, 0.261, 0.264, 0.266, 0.264, 0.269, 0.268, 0.264, 0.262,
      0.257, 0.255, 0.255, 0.253, 0.251, 0.254, 0.255)
```

```
Clayton.Markov2.MLE(Y, k = 1, D = 1, plot = TRUE)
```

```
Y=Clayton.Markov2.DATA(n=1000,mu=0,sigma=1,alpha=8)
```

```
Clayton.Markov2.MLE(Y, plot=TRUE)
```

---

Joe.Markov.DATA	<i>Generating Time Series Data Under a Copula-Based Markov Chain Model with the Joe Copula</i>
-----------------	--

---

**Description**

Time-series datasets are generated under a copula-based Markov chain model with the Joe copula.

**Usage**

```
Joe.Markov.DATA(n, mu, sigma, alpha)
```

**Arguments**

n	sample size
mu	mean
sigma	standard deviation
alpha	association parameter

**Details**

alpha>=1 for positive association

**Value**

Time series data

**Author(s)**

Takeshi Emura

**References**

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TS and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

**Examples**

```
n=1000
alpha=2.856 ### Kendall's tau =0.5 ###
mu=2
sigma=1
Y=Joe.Markov.DATA(n, mu, sigma, alpha)
mean(Y)
sd(Y)
cor(Y[-1], Y[-n], method="kendall")

Joe.Markov.MLE(Y, k=2)
```

---

Joe.Markov.DATA.binom *Generating Time Series Data Under a Copula-Based Markov Chain Model with the Joe Copula and Binomial Margin.*

---

**Description**

Time-series datasets are generated under a copula-based Markov chain model with the Joe copula and binomial margin.

**Usage**

```
Joe.Markov.DATA.binom(n, size, prob, alpha)
```

**Arguments**

n	number of observations
size	number of binomial trials
prob	binomial probability; $0 < p < 1$
alpha	association parameter

**Details**

alpha  $\geq 1$  for positive association

**Value**

time series data

**Author(s)**

Huang X, Emura T

**References**

Chen W (2018) Copula-based Markov chain model with binomial data, NCU Library

Huang X, Chen W, Emura T (2019-) A control chart using a copula-based Markov chain for attribute data, revision

**Examples**

```

size=50
prob=0.5
alpha=2
set.seed(1)
Y=Joe.Markov.DATA.binom(n=500,size,prob,alpha)
### sample mean and SD ###
mean(Y)
sd(Y)
### true mean and SD ###
size*prob
sqrt(size*prob*(1-prob))

```

Joe.Markov.MLE

---

*Maximum Likelihood Estimation and Statistical Process Control Under the Joe Copula*

---

**Description**

The maximum likelihood estimates are produced and the Shewhart control chart is drawn with k-sigma control limits (e.g., 3-sigma). The dependence model follows the Joe copula and the marginal (stationary) distribution follows the normal distribution.

**Usage**

```
Joe.Markov.MLE(Y, k = 3, D = 1, plot = TRUE, GOF=FALSE)
```

**Arguments**

Y	vector of datasets
k	constant determining the length between LCL and UCL (k=3 corresponds to 3-sigma limit)
D	diameter for U(-D, D) used in randomized Newton-Raphson
plot	show the control chart if TRUE
GOF	show the model diagnostic plot if TRUE

**Value**

estimates	estimates
out_of_control	IDs for out-of-control points
Gradient	gradients (must be zero)
Hessian	Hessian matrix
Mineigenvalue_Hessian	Minimum eigenvalue for the Hessian matrix
CM.test	Cramer-von Mises test statistics
KS.test	Kolmogorov-Smirnov test statistics

**Author(s)**

Takeshi Emura

**References**

Emura T, Long TH, Sun LH (2017), R routines for performing estimation and statistical process control under copula-based time series models, *Communications in Statistics - Simulation and Computation*, 46 (4): 3067-87

Long TH and Emura T (2014), A control chart using copula-based Markov chain models, *Journal of the Chinese Statistical Association* 52 (No.4): 466-96

**Examples**

```
n=1000
alpha=2.856 ### Kendall's tau =0.5 ###
mu=2
sigma=1
Y=Joe.Markov.DATA(n,mu,sigma,alpha)
mean(Y)
sd(Y)
cor(Y[-1],Y[-n],method="kendall")

Joe.Markov.MLE(Y,k=2)
```

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