

# Package ‘corcounts’

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**Type** Package

**Title** Generate correlated count random variables

**Version** 1.4

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**Description** Generate high-dimensional correlated count random variables with a prespecified Pearson correlation.

**License** GPL (>= 3)

**LazyLoad** yes

**Repository** CRAN

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corcounts-package *Generate correlated count random variables*

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### Description

Sample high-dimensional correlated count random variables with approximate prespecified Pearson correlation and exact margins.

### Details

Package: corcounts  
Type: Package  
Version: 1.4  
Date: 2009-11-13  
License: GPL (>= 3)  
LazyLoad: yes

Specify the marginal distributions and parameters and the desired correlation matrix and run `'rcounts()'`.  
In order to allow for regression, i.e. for individual parameters for each cluster, run `'rcounts.reg()'`.

### Author(s)

Maintainer: Vinzenz Erhardt <erhardt@ma.tum.de>

### References

Erhardt, V., Czado, C. (2009) A method for approximately sampling high-dimensional count variables with prespecified Pearson correlation. Submitted for publication.

Czado, C., Erhardt, V., Min, A., Wagner, S. (2007) Zero-inflated generalized Poisson models with regression effects on the mean, dispersion and zero-inflation level applied to patent outsourcing rates. *Statistical Modelling* 7 (2), 125-153.

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c2pc

*Calculate partial correlations from a correlation matrix*

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### Description

`'c2pc'` is used to calculate partial correlations from a correlation matrix.

### Usage

`c2pc(Cin)`

**Arguments**

Cin                    A symmetric positive definite correlation matrix.

**Details**

If you obtain values not in [-1,1], your correlation matrix is not positive definite.

This routine only calculates partial correlations conditional on 1, 12, 123, 1234, etc.. Partial correlations conditional on other margins can be obtained by a permutation of margins.

**Value**

The partial correlations calculated will be

Theta =

```
12.....13.....14.....15.....16
.....23|1.....24|1.....25|1.....26|1
.....34|12.....35|12.....36|12 ...
.....45|123.....46|123
.....56|1234
...
```

**Author(s)**

Vinzenz Erhardt

**See Also**

Package 'corpcor' calculates partial correlations conditional on ALL other margins.

**Examples**

```
# create 8 dimensional symmetric positive correlation matrix with random entries
Cin <- unstructured(8)
Cin

Theta <- c2pc(Cin)
Theta

# transform Theta back to obtain the correlation matrix
pc2c(Theta)

# identical with Cin
pc2c(Theta) - Cin
```

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modified.cvine.alg *Auxiliary function*

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### Description

auxiliary function

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modified.cvine.alg.reg  
*Auxiliary function*

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### Description

auxiliary function

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pc2c *Calculate a corresponding correlation matrix to partial correlations*

---

### Description

'c2pc' is used to calculate the corresponding correlation matrix of dimension T times T out of partial correlations.

### Usage

pc2c(Theta)

### Arguments

Theta            A T times T matrix with partial correlations. See details.

### Details

The partial correlations in Theta have to be specified as

Theta =

```
12.....13.....14.....15.....16
.....23|1.....24|1.....25|1.....26|1
.....34|12.....35|12.....36|12 ...
.....45|123.....46|123
.....56|1234
```

...

and may be NA elsewhere. Theta has to be of dimension T times T.

This routine only calculates partial correlations conditional on 1, 12, 123, 1234, etc.. Partial correlations conditional on other margins can be obtained by a permutation of margins.

**Value**

A symmetric positive definite correlation matrix of dimension T times T.

**Author(s)**

Vinzenz Erhardt

**Examples**

```
# create random uniform(0,1) partial correlations in dimension 8
dimension <- 8
Theta <- matrix(NA,dimension,dimension)
for (i in 2:dimension) {
  for (j in 1:(i-1)) {
    Theta[j,i] <- runif(1,-1,1)
  }
}
Theta

# calculate corresponding correlation matrix
C <- pc2c(Theta)
C

# transform back to partial correlations
c2pc(C)

# equivalence with original Theta
Theta - c2pc(C)
```

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pseudoinv.zigp      *Auxiliary function*

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**Description**

auxiliary function

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R11.AR1      *Auxiliary function*

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**Description**

auxiliary function

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R11.exchangeable    *Auxiliary function*

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### Description

auxiliary function

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rcounts                    *Generate correlated count random variables*

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### Description

'rcounts' is used to sample high-dimensional correlated count random variables with approximate prespecified Pearson correlation and exact margins.

### Usage

```
rcounts(N, margins, mu, phi=rep(NA, length(margins)),
        omega=rep(NA, length(margins)), psi=rep(NA, length(margins)),
        corstr, corpar, conv=0.01)
```

### Arguments

N	number of observations to be generated per margin (should be at least 500).
margins	Vector of margin tokens. Its length T is the dimension. See details.
mu	Vector of length T of means for the Poisson, GP, ZIP, ZIGP and NB margins.
phi	Vector of length T of dispersion parameters for the GP, and ZIGP margins. For Poisson, ZIP and NB margins, an 'NA' can be provided.
omega	Vector of length T of zero-inflation parameters for the ZIP and ZIGP margins. For Poisson, GP and NB margins, an 'NA' can be provided.
psi	Vector of length T of size parameters for the NB margins. For Poisson, GP, ZIP and ZIGP margins, an 'NA' can be provided.
corstr	Correlation structure. Can be 'ex' for exchangeable, 'AR1' for AR(1) and 'unstr' for unstructured.
corpar	Correlation parameter. Scalar correlation for 'ex' and 'AR1' and matrix of dimension TxT for 'unstr'.
conv	Convergence criterion

### Details

The entries in 'margins' can be specified as 'Poi' for Poisson, 'GP' for generalized Poisson, 'ZIP' for zero-inflated Poisson, 'ZIGP' for zero-inflated generalized Poisson and 'NB' for negative-binomial.

**Value**

The function will return a matrix of counts of dimension  $N \times T$ .

**Author(s)**

Vinzenz Erhardt

**Examples**

```

N <- 5000

# high precision in dimension 2
margins <- c("ZIGP", "GP")
mu <- c(10, 15)
phi <- c(1.5, 3.5)
omega <- c(.25, NA)
corstr <- "ex"
corpar <- .5
Y <- rcounts(N=N, margins=margins, mu=mu, phi=phi, omega=omega, corstr=corstr,
             corpar=corpar, conv=0.0001)
cor(Y)

# five-dimensional examples
margins <- c("ZIGP", "GP", "Poi", "NB", "ZIP")
mu <- c(10, 25, 12, 20, 28)
phi <- c(1.5, 2, NA, NA, NA)
omega <- c(.25, NA, NA, NA, .2)
psi <- c(NA, NA, NA, 7, NA)

# Exchangeable structure with correlation of 0.5
corstr <- "ex"
corpar <- .5
Y <- rcounts(N=N, margins=margins, mu=mu, phi=phi, omega=omega, psi=psi,
             corstr=corstr, corpar=corpar)
cor(Y)

# AR(1) structure with correlation of  $\text{corr}(Y(t_1), Y(t_2)) = .8^{|t_1-t_2|}$ 
corstr <- "AR1"
corpar <- .8
Y <- rcounts(N=N, margins=margins, mu=mu, phi=phi, omega=omega, psi=psi,
             corstr=corstr, corpar=corpar)
cor(Y)

# Unstructured correlation. Create random symmetric positive definite
# matrix using function 'unstructured'
corstr <- "unstr"
corpar <- unstructured(5)
corpar
Y <- rcounts(N=N, margins=margins, mu=mu, phi=phi, omega=omega, psi=psi,
             corstr=corstr, corpar=corpar)
cor(Y)

```

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rcounts.reg	<i>Generate correlated count random variables with individual parameters for each cluster</i>
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## Description

'rcounts.reg' is used to sample high-dimensional correlated count random variables with approximate prespecified Pearson correlation and exact margins.

## Usage

```
rcounts.reg(N, margins, mu, phi=matrix(NA,N,length(margins)),
            omega=matrix(NA,N,length(margins)),
            psi=matrix(NA,N,length(margins)), corstr, corpar, conv=0.01)
```

## Arguments

N	number of observations to be generated per margin (should be at least 500).
margins	Vector of margin tokens. Its length T is the dimension. See details.
mu	Matrix of dimension N x T of means for the Poisson, GP, ZIP, ZIGP and NB margins.
phi	Matrix of dimension N x T of dispersion parameters for the GP, and ZIGP margins. For Poisson, ZIP and NB margins, an 'NA' can be provided.
omega	Matrix of dimension N x T of zero-inflation parameters for the ZIP and ZIGP margins. For Poisson, GP and NB margins, an 'NA' can be provided.
psi	Matrix of dimension N x T of size parameters for the NB margins. For Poisson, GP, ZIP and ZIGP margins, an 'NA' can be provided.
corstr	Correlation structure. Can be 'ex' for exchangeable, 'AR1' for AR(1) and 'unstr' for unstructured.
corpar	Correlation parameter. Scalar correlation for 'ex' and 'AR1' and matrix of dimension T x T for 'unstr'.
conv	Convergence criterion

## Details

The entries in 'margins' can be specified as 'Poi' for Poisson, 'GP' for generalized Poisson, 'ZIP' for zero-inflated Poisson, 'ZIGP' for zero-inflated generalized Poisson and 'NB' for negative-binomial.

NOTE: there is a tradeoff between too small N (decreasing accuracy of the resulting correlation) and too high N (dramatically increasing computation time).

## Value

The function will return a matrix of counts of dimension N x T.

**Author(s)**

Vinzenz Erhardt

**Examples**

```
N <- 500

# bivariate example
margins <- c("ZIGP", "GP")
mu <- matrix(runif(N*2, 10, 20), N, 2)
phi <- matrix(runif(N*2, 1, 3), N, 2)
omega <- matrix(c(runif(N, 0, .3), rep(NA, N)), N, 2)
corstr <- "ex"
corpar <- .5
Y <- rcounts.reg(N=N, margins=margins, mu=mu, phi=phi, omega=omega,
                 corstr=corstr, corpar=corpar)

cor(Y)
```

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`unstructured`*Generate random correlation matrix*

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**Description**

'unstructured' generates a random correlation matrix of dimension T with random entries. To ensure positive definiteness, a matrix of partial correlations with random entries uniform on [-0.9, 0.9] will be generated and the corresponding correlation matrix be calculated from it using a bijective recursive relation between them.

**Usage**

```
unstructured(dimension)
```

**Arguments**

`dimension`      Dimension T of the correlation matrix.

**Value**

A correlation matrix of dimension T x T.

**Examples**

```
unstructured(10)
```

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