

Package ‘fracdiff’

June 9, 2009

Version 1.3-2

Title Fractionally differenced ARIMA aka ARFIMA(p,d,q) models

Date 2009-.-.-.

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Description Maximum likelihood estimation of the parameters of a fractionally differenced ARIMA(p,d,q) model (Haslett and Raftery, Appl.Statistics, 1989).

Enhances longmemo

LazyData yes

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Repository CRAN

Date/Publication 2009-06-09 10:02:37

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confint.fracdiff *Confidence Intervals for Fracdiff Model Parameters*

Description

Computes confidence intervals for one or more parameters in a fitted fracdiff model, see [fracdiff](#).

Usage

```
## S3 method for class 'fracdiff':
confint(object, parm, level = 0.95, ...)
```

Arguments

object	an object of class <code>fracdiff</code> , typically result of fracdiff (...).
parm	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
level	the confidence level required.
...	additional argument(s) for methods.

Value

A matrix (or vector) with columns giving lower and upper confidence limits for each parameter. These will be labelled as $(1-\text{level})/2$ and $1 - (1-\text{level})/2$ in % (by default 2.5% and 97.5%).

Author(s)

Spencer Graves posted the initial version to R-help.

See Also

the generic [confint](#); [fracdiff](#) model fitting.

Examples

```
set.seed(101)
ts2 <- fracdiff.sim(5000, ar = .2, ma = -.4, d = .3)
mFD <- fracdiff(ts2$series, nar = length(ts2$ar), nma = length(ts2$ma))
coef(mFD)
confint(mFD)
```

`diffseries`*Fractionally Differentiate Data*

Description

Differentiates the time series data using the approximated binomial expression of the long-memory filter and an estimate of the memory parameter in the ARFIMA(p,d,q) model.

Usage

```
diffseries(x, d)
```

Arguments

x	numeric vector or univariate time series
d	number specifying the fractional difference order.

Value

the fractionally differenced series x.

Author(s)

Valderio A. Reisen (valderio@cce.ufes.br) and Artur J. Lemonte

References

See those in [fdSperio](#); additionally

Reisen, V. A. and Lopes, S. (1999) Some simulations and applications of forecasting long-memory time series models; *Journal of Statistical Planning and Inference* **80**, 269–287.

Reisen, V. A. Cribari-Neto, F. and Jensen, M.J. (2003) Long Memory Inflationary Dynamics. The case of Brazil. *Studies in Nonlinear Dynamics and Econometrics* **7**(3), 1–16.

See Also

[fracdiff.sim](#)

Examples

```
memory.long <- fracdiff.sim(80, d = 0.3)
mGPH <- fdGPH(memory.long$series)
r <- diffseries(memory.long$series, d = mGPH$d)
#acf(r) # shouldn't show structure - ideally
```

fdGPH

*Geweke and Porter-Hudak Estimator for ARFIMA(p,d,q)***Description**

Estimate the fractional (or “memory”) parameter d in the ARFIMA(p,d,q) model by the method of Geweke and Porter-Hudak (GPH). The GPH estimator is based on the regression equation using the periodogram function as an estimate of the spectral density.

Usage

```
fdGPH(x, bandw.exp = 0.5)
```

Arguments

x	univariate time series
bandw.exp	the bandwidth used in the regression equation

Details

The function also provides the asymptotic standard deviation and the standard error deviation of the fractional estimator.

The bandwidth is $bw = \text{trunc}(n \wedge \text{bandw.exp})$, where $0 < \text{bandw.exp} < 1$ and n is the sample size. Default $\text{bandw.exp} = 0.5$.

Value

d	GPH estimate
sd.as	asymptotic standard deviation
sd.reg	standard error deviation

Author(s)

Valderio A. Reisen and Artur J. Lemonte

References

see those in [fdSperio](#).

See Also

[fdSperio](#), [fracdiff](#)

Examples

```
memory.long <- fracdiff.sim(1500, d = 0.3)
fdGPH(memory.long$series)
```

`fdSperio`*Sperio Estimate for 'd' in ARFIMA(p,d,q)*

Description

This function makes use Reisen (1994) estimator to estimate the memory parameter d in the ARFIMA(p,d,q) model. It is based on the regression equation using the smoothed periodogram function as an estimate of the spectral density.

Usage

```
fdSperio(x, bandw.exp = 0.5, beta = 0.9)
```

Arguments

<code>x</code>	univariate time series data.
<code>bandw.exp</code>	numeric: exponent of the bandwidth used in the regression equation.
<code>beta</code>	numeric: exponent of the bandwidth used in the lag Parzen window.

Details

The function also provides the asymptotic standard deviation and the standard error deviation of the fractional estimator.

The bandwidths are $bw = \text{trunc}(n^{\wedge} \text{bandw.exp})$, where $0 < \text{bandw.exp} < 1$ and n is the sample size. Default `bandw.exp = 0.5`; and $bw2 = \text{trunc}(n^{\wedge} \text{beta})$, where $0 < \text{beta} < 1$ and n is the sample size. Default `beta = 0.9`.

Value

a list with components

<code>d</code>	Sperio estimate
<code>sd.as</code>	asymptotic standard deviation
<code>sd.reg</code>	standard error deviation

Author(s)

Valderio A. Reisen (valderio@cce.ufes.br) and Artur J. Lemonte

References

- Geweke, J. and Porter-Hudak, S. (1983) The estimation and application of long memory time series models. *Journal of Time Series Analysis* **4**(4), 221–238.
- Reisen, V. A. (1994) Estimation of the fractional difference parameter in the ARFIMA(p,d,q) model using the smoothed periodogram. *Journal Time Series Analysis*, **15**(1), 335–350.
- Reisen, V. A., B. Abraham, and E. M. M. Toscano (2001) Parametric and semiparametric estimations of stationary univariate ARFIMA model. *Brazilian Journal of Probability and Statistics* **14**, 185–206.

See Also

`fdGPH`, `fracdiff`

Examples

```
memory.long <- fracdiff.sim(1500, d = 0.3)
spm <- fdSperio(memory.long$series)
str(spm, digits=6)
```

`fracdiff`

ML Estimates for Fractionally-Differenced ARIMA (p,d,q) models

Description

Calculates the maximum likelihood estimators of the parameters of a fractionally-differenced ARIMA (p,d,q) model, together (if possible) with their estimated covariance and correlation matrices and standard errors, as well as the value of the maximized likelihood. The likelihood is approximated using the fast and accurate method of Haslett and Raftery (1989).

Usage

```
fracdiff(x, nar = 0, nma = 0,
         ar = rep(NA, max(nar, 1)), ma = rep(NA, max(nma, 1)),
         dtol = NULL, drange = c(0, 0.5), h, M = 100)
```

Arguments

<code>x</code>	time series (numeric vector) for the ARIMA model
<code>nar</code>	number of autoregressive parameters p .
<code>nma</code>	number of moving average parameters q .
<code>ar</code>	initial autoregressive parameters
<code>ma</code>	initial moving average parameters
<code>dtol</code>	interval of uncertainty for d . If <code>dtol</code> is negative or <code>NULL</code> , the fourth root of machine precision will be used. <code>dtol</code> will be altered if necessary by the program.

drange	interval over which the likelihood function is to be maximized as a function of d .
h	size of finite difference interval for numerical derivatives. By default (or if negative), $h = \min(0.1, \text{eps}.5 * (1 + \text{abs}(\text{cllf})))$, where $\text{cllf} := \log. \text{max.likelihood}(\text{as returned})$ and $\text{eps}.5 := \text{sqrt}(\text{.Machine}\$\text{double.neg.eps})$ (typically 1.05e-8). This is used to compute a finite difference approximation to the Hessian, and hence only influences the cov, cor, and std.error computations; see also fracdiff.var .
M	number of terms in the likelihood approximation (see Haslett and Raftery 1989).

Value

an object of S3 class "fracdiff", which is a list with components:

log.likelihood	logarithm of the maximum likelihood
d	optimal fractional-differencing parameter
ar	vector of optimal autoregressive parameters
ma	vector of optimal moving average parameters
covariance.dpq	covariance matrix of the parameter estimates (order : d, ar, ma).
stderror.dpq	standard errors of the parameter estimates c(d, ar, ma).
correlation.dpq	correlation matrix of the parameter estimates (order : d, ar, ma).
h	interval used for numerical derivatives, see h argument.
dtol	interval of uncertainty for d; possibly altered from input dtol.
M	as input.
hessian.dpq	the approximate Hessian matrix H of 2nd order partial derivatives of the likelihood with respect to the parameters; this is (internally) used to compute <code>covariance.dpq</code> , the approximate asymptotic covariance matrix as $C = (-H)^{-1}$.

Method

The optimization is carried out in two levels:

an outer univariate unimodal optimization in d over the interval `drange` (typically [0,.5]), using Brent's `fmin` algorithm), and

an inner nonlinear least-squares optimization in the AR and MA parameters to minimize white noise variance (uses the MINPACK subroutine `lmDER`). written by Chris Fraley (March 1991).

Note

Ordinarily, `nar` and `nma` should not be too large (say < 10) to avoid degeneracy in the model. The function `fracdiff.sim` is available for generating test problems.

References

J. Haslett and A. E. Raftery (1989) Space-time Modelling with Long-memory Dependence: Assessing Ireland's Wind Power Resource (with Discussion); *Applied Statistics* **38**, 1–50.

R. Brent (1973) *Algorithms for Minimization without Derivatives*, Prentice-Hall

J. J. More, B. S. Garbow, and K. E. Hillstom (1980) *Users Guide for MINPACK-1*, Technical Report ANL-80-74, Applied Mathematics Division, Argonne National Laboratory.

See Also

`coef.fracdiff` and other methods for "fracdiff" objects; `fracdiff.sim`

Examples

```
ts.test <- fracdiff.sim( 5000, ar = .2, ma = -.4, d = .3)
fracdiff( ts.test$series, nar = length(ts.test$ar), nma = length(ts.test$ma)
```

fracdiff-methods *Many Methods for "fracdiff" Objects*

Description

Many “accessor” methods for `fracdiff` objects, notably `summary`, `coef`, `vcov`, and `logLik`; further `print()` methods were needed.

Usage

```
## S3 method for class 'fracdiff':
coef(object, ...)
## S3 method for class 'fracdiff':
logLik(object, ...)
## S3 method for class 'fracdiff':
print(x, digits = getOption("digits"), ...)
## S3 method for class 'fracdiff':
summary(object, symbolic.cor = FALSE, ...)
## S3 method for class 'summary.fracdiff':
print(x, digits = max(3, getOption("digits") - 3),
      correlation = FALSE, symbolic.cor = x$symbolic.cor,
      signif.stars = getOption("show.signif.stars"), ...)
## S3 method for class 'fracdiff':
vcov(object, ...)
```

Arguments

<code>x</code> , object	object of class <code>fracdiff</code> .
<code>digits</code>	the number of significant digits to use when printing.
...	further arguments passed from and to methods.

- `correlation` logical; if TRUE, the correlation matrix of the estimated parameters is returned and printed.
- `symbolic.cor` logical. If TRUE, print the correlations in a symbolic form (see [symnum](#)) rather than as numbers.
- `signif.stars` logical. If TRUE, “significance stars” are printed for each coefficient.

Author(s)

Martin Maechler

See Also

[fracdiff](#) to get "fracdiff" objects, [confint.fracdiff](#) for the [confint](#) method; further, [fracdiff.var](#).

Examples

```
set.seed(7)
ts4 <- fracdiff.sim(10000, ar = c(0.6, -.05, -0.2), ma = -0.4, d = 0.2)
modFD <- fracdiff(ts4$series, nar = length(ts4$ar), nma = length(ts4$ma))
## -> warning (singular Hessian)
coef(modFD) # the estimated parameters
vcov(modFD)
smFD <- summary(modFD)
smFD
coef(smFD) # gives the whole table
AIC(modFD) # AIC works because of the logLik() method
```

fracdiff.sim

Simulate fractional ARIMA Time Series

Description

Generates simulated long-memory time series data from the fractional ARIMA(p,d,q) model. This is a test problem generator for [fracdiff](#).

Usage

```
fracdiff.sim(n, ar = NULL, ma = NULL, d,
             rand.gen = rnorm, innov = rand.gen(n+q, ...),
             n.start = NA, allow.0.nstart = FALSE, ..., mu = 0.)
```

Arguments

n	length of the time series.
ar	vector of autoregressive parameters; empty by default.
ma	vector of moving average parameters; empty by default.
d	fractional differencing parameter.
rand.gen	a function to generate the innovations; the default, <code>rnorm</code> generates white $N(0,1)$ noise.
innov	an optional times series of innovations. If not provided, <code>rand.gen()</code> is used.
n.start	length of “burn-in” period. If NA, the default, the same value as in <code>arima.sim</code> is computed.
allow.0.nstart	logical indicating if <code>n.start = 0</code> should be allowed even when $p + q > 0$. This not recommended unless for producing the same series as with older versions of <code>fracdiff.sim</code> .
...	additional arguments for <code>rand.gen()</code> . Most usefully, the standard deviation of the innovations generated by <code>rnorm</code> can be specified by <code>sd</code> .
mu	time series mean (added at the end).

Value

a list containing the following elements :

series	time series
ar, ma, d, mu, n.start	same as input

See Also

`fracdiff`, also for references; `arima.sim`

Examples

```
## Pretty (too) short to "see" the long memory
fracdiff.sim(100, ar = .2, ma = .4, d = .3)

## longer with "extreme" ar:
r <- fracdiff.sim(n=1500, ar=-0.9, d= 0.3)
plot(as.ts(r$series))
```

fracdiff.var	<i>Recompute Covariance Estimate for fracdiff</i>
--------------	---

Description

Allows the finite-difference interval to be altered for recomputation of the covariance estimate for fracdiff.

Usage

```
fracdiff.var(x, fracdiff.out, h)
```

Arguments

`x` a univariate time series or a vector. Missing values (NAs) are not allowed.

`fracdiff.out` output from `fracdiff` for time series `x`.

`h` finite-difference interval for approximating partial derivatives with respect to the `d` parameter.

Value

an object of S3 class "fracdiff", i.e., basically a list with the same elements as the result from `fracdiff`, but with possibly different values for the hessian, covariance, and correlation matrices and for standard error, as well as for `h`.

See Also

`fracdiff`, also for references.

Examples

```
## Generate a fractionally-differenced ARIMA(1,d,1) model :
ts.test <- fracdiff.sim(10000, ar = .2, ma = .4, d = .3)
## estimate the parameters in an ARIMA(1,d,1) model for the simulated series
fd.out <- fracdiff(ts.test$ser, nar= 1, nma = 1)

## Modify the covariance estimate by changing the finite-difference interval
(fd.o2 <- fracdiff.var(ts.test$series, fd.out, h = .0001))
## looks identical as print(fd.out),
## however these (e.g.) differ :
vcov(fd.out)
vcov(fd.o2)
```

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