

Package ‘gptk’

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Title Gaussian Processes Tool-Kit

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Depends R (>= 2.8.0), fields, Matrix

Imports

Suggests spam

Description The gptk package implements a general-purpose toolkit for
Gaussian process regression with a variety of covariance
functions (e.g. RBF, Mattern, polynomial, etc). Based on a
MATLAB implementation by Neil D. Lawrence. See inst/doc/index.html for more details.

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R topics documented:

basePlot	3
cmpndKernParamInit	3
cmpndNoiseParamInit	4
demAutoOptimiseGp	5
demGpCov2D	5

demGpSample	6
demInterpolation	6
demOptimiseGp	7
demRegression	8
expTransform	8
gaussianNoiseOut	9
gaussianNoiseParamInit	10
gaussSamp	10
gpBlockIndices	11
gpComputeAlpha	12
gpComputeM	12
gpCovGrads	13
gpCovGradsTest	14
gpCreate	14
gpDataIndices	15
gpExpandParam	16
gpExtractParam	16
gpGradient	17
gpLogLikeGradients	18
gpLogLikelihood	19
gpMeanFunctionGradient	19
gpObjective	20
gpOptimise	21
gpOptions	21
gpOut	22
gpPlot	23
gpPosteriorMeanVar	23
gpPosteriorSample	24
gpSample	25
gpScaleBiasGradient	25
gpTest	26
gpUpdateAD	27
gpUpdateKernels	27
kernCompute	28
kernCreate	29
kernDiagGradient	30
kernDiagGradX	31
kernGradient	31
kernParamInit	32
kernTest	33
modelDisplay	34
modelExpandParam	34
modelExtractParam	35
modelGradient	35
modelGradientCheck	36
modelOut	37
modelOutputGrad	37
multiKernParamInit	38

basePlot 3

noiseCreate	39
noiseOut	39
noiseParamInit	40
optimiDefaultConstraint	41
rbfKernDiagGradX	41
rbfKernGradX	42
rbfKernParamInit	43
SCGoptim	43
whiteKernDiagGradX	44
whiteKernGradX	45
whiteKernParamInit	46
zeroAxes	46

Index 47

basePlot *Plot a contour of the 2D Gaussian distribution with covariance matrix K.*

Description

Creates the basic plot as an ellipse with major and minor radii as the square roots of the two eigenvalues of K.

Usage

`basePlot(K)`

Arguments

K the covariance matrix.

See Also

[zeroAxes](#).

cmpndKernParamInit *CMPND kernel parameter initialisation.*

Description

initialises the compound kernel structure with some default parameters.

Usage

`cmpndKernParamInit(kern)`

Arguments

kern the kernel structure which requires initialisation.

Value

kern the kernel structure with the default parameters placed in.

See Also

[kernCreate](#), [kernParamInit](#).

Examples

```
## missing
```

cmpndNoiseParamInit *CMPND noise parameter initialisation.*

Description

initialises the compound noise structure with some default parameters.

Usage

```
cmpndNoiseParamInit(noise,y)
```

Arguments

noise the noise structure which requires initialisation.

y the data design matrix.

Value

noise the noise structure with the default parameters placed in.

See Also

[noiseCreate](#), [noiseParamInit](#).

Examples

```
## missing
```

demAutoOptimiseGp *Gaussian Process Optimisation Demo*

Description

Shows that by varying the length scale, an artificial data set has different likelihoods, yet there is an optimum for which the likelihood is maximised. This demo is similar to demOptimiseGp, only here, it is demonstrated how the length scale hyperparameter is optimised automatically through SCG (scaled conjugate gradients) numerical optimisation. Run multiple times to understand the effect of optimisation on randomly generated datasets.

Usage

```
demAutoOptimiseGp(path=getwd(), filename='demAutoOptimiseGp', png=FALSE, gif=FALSE)
```

Arguments

path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.
gif	save series of images as animated gif.

See Also

[gpOptions](#), [kernCreate](#), [gaussSamp](#), [gpCreate](#), [gpExpandParam](#), [gpLogLikelihood](#), [gpPosteriorMeanVar](#), [gpOptimise](#), [gpPlot](#).

demGpCov2D *Gaussian Process 2D Covariance Demo*

Description

Gives the joint distribution for f1 and f2, two values of a function sampled from a Gaussian process. The plots show the joint distributions as well as the conditional for f2 given f1.

Usage

```
demGpCov2D(ind=c(1,2), path = getwd(), filename = paste('demGpCov2D', ind[1], '_', ind[2], sep=''), pn
```

Arguments

ind	indices of function values.
path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.
gif	save series of images as animated gif.

See Also

[demGpSample](#), [basePlot](#), [zeroAxes](#).

demGpSample

Gaussian Process Sampling Demo

Description

This example shows how points which look like they come from a function to be sampled from a Gaussian distribution. The sample is 25 dimensional and is from a Gaussian with a particular covariance.

Usage

```
demGpSample(bw=FALSE, path=getwd(), filename='gpSample', png=FALSE)
```

Arguments

bw	greyscale plots.
path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.

See Also

[kernCreate](#), [kernCompute](#), [gaussSamp](#), [demGpSample](#), [basePlot](#), [zeroAxes](#).

demInterpolation

Gaussian Process Interpolation Demo

Description

Plots, consecutively, an increasing number of data points, followed by an interpolated fit through the data points using a Gaussian process. This is a noiseless system, and the data is sampled from a GP with a known covariance function. The curve is then recovered with minimal uncertainty after only nine data points are included.

Usage

```
demInterpolation(path=getwd(), filename='demInterpolation', png=FALSE, gif=FALSE)
```

Arguments

path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.
gif	save series of images as animated gif.

See Also

[gpOptions](#), [kernCreate](#), [kernCompute](#), [gaussSamp](#), [kernDiagCompute](#), [gpCreate](#), [gpPlot](#).

demOptimiseGp

Gaussian Process Optimisation Demo

Description

Shows a series of plots of a Gaussian process with different length scales fitted to six data points. For each plot there is a corresponding plot of the log likelihood. The log likelihood peaks for a length scale close to 1. This was the length scale used to generate the data.

Usage

```
demOptimiseGp(path=getwd(), filename='demOptimiseGp', png=FALSE, gif=FALSE)
```

Arguments

path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.
gif	save series of images as animated gif.

See Also

[gpOptions](#), [kernCreate](#), [kernCompute](#), [gaussSamp](#), [kernDiagCompute](#), [gpCreate](#), [gpExpandParam](#), [gpLogLikelihood](#), [gpPosteriorMeanVar](#), [gpPlot](#).

demRegression	<i>Gaussian Process Regression Demo</i>
---------------	---

Description

The regression demo very much follows the format of the interpolation demo. Here the difference is that the data is sampled with noise. Fitting a model with noise means that the regression will not necessarily pass right through each data point.

Usage

```
demRegression(path=getwd(), filename='demRegression', png=FALSE, gif=FALSE)
```

Arguments

path	path where the plot images are saved.
filename	name of saved images.
png	save image as png.
gif	save series of images as animated gif.

See Also

[gpOptions](#), [kernCreate](#), [kernCompute](#), [gaussSamp](#), [kernDiagCompute](#), [gpCreate](#), [gpPlot](#), [demInterpolation](#).

expTransform	<i>Constrains a parameter.</i>
--------------	--------------------------------

Description

contains commands to constrain parameters to be positive via exponentiation or within a fixed interval via the sigmoid function.

Usage

```
expTransform(x, transform)
sigmoidTransform(x, transform)
boundedTransform(x, transform, bounds)
```

Arguments

x	input argument.
transform	type of transform, 'atox' maps a value into the transformed space (i.e. makes it positive). 'xtoa' maps the parameter back from transformed space to the original space. 'gradfact' gives the factor needed to correct gradients with respect to the transformed parameter.
bounds	a 2-vector of bounds of allowed values in boundedTransform

Value

Return value as selected by tranform

See Also

[modelOptimise](#)

Examples

```
# Transform unconstrained parameter -4 to a positive value
expTransform(-4, 'atox')
```

```
# Transform a bounded parameter in (1,3) to an unconstrained one
boundedTransform(2, 'xtoa', c(1, 3))
```

gaussianNoiseOut	<i>Compute the output of the GAUSSIAN noise given the input mean and variance.</i>
------------------	--

Description

computes the ouptut for the Gaussian noise given input mean and variances.

Usage

```
gaussianNoiseOut(noise, mu, varSigma)
```

Arguments

noise	the noise structure for which the output is computed.
mu	the input mean values.
varSigma	the input variance values.

Value

y	the output from the noise model.
---	----------------------------------

See Also

[gaussianNoiseParamInit](#), [noiseOut](#), [noiseCreate](#).

Examples

```
## missing
```

 gaussianNoiseParamInit

GAUSSIAN noise parameter initialisation.

Description

initialises the Gaussian noise structure with some default parameters.

Usage

```
gaussianNoiseParamInit(noise,y)
```

Arguments

noise	the noise structure which requires initialisation.
y	the data design matrix.

Value

noise	the noise structure with the default parameters placed in.
-------	--

See Also

[noiseCreate](#), [noiseParamInit](#).

Examples

```
## missing
```

 gaussSamp

Sample from a Gaussian with a given covariance.

Description

samples a given number of samples from a Gaussian with a given covariance matrix.

Usage

```
gaussSamp(mu=matrix(0,nrow=dim(Sigma)[1]), Sigma, numSamps)
```

Arguments

mu	the mean of the Gaussian to sample from.
Sigma	the covariance of the Gaussian to sample from.
numSamps	the number of samples to take from the Gaussian.

Value

y the samples from the Gaussian

See Also

[rnorm](#), [eigen](#).

Examples

```
## missing
```

gpBlockIndices	<i>Return indices of given block.</i>
----------------	---------------------------------------

Description

returns the indices of a given block for the PITC approximation.

Usage

```
gpBlockIndices(model, blockNo)
```

Arguments

model the model for which the indices are being computed.
blockNo the block number for which the indices are required.

Value

indices the data indices associated with given block.

See Also

[gpComputeAlpha](#), [gpCovGrads](#), [gpLogLikeGradients](#), [gpLogLikelihood](#), [gpUpdateAD](#).

Examples

```
## missing
```

gpComputeAlpha *Update the vector 'alpha' for computing posterior mean quickly.*

Description

updates the vectors that are known as 'alpha' in the support vector machine, in other words $\text{invK} * y$, where y is the target values.

Usage

```
gpComputeAlpha(model, m)
```

Arguments

model the model for which the alphas are going to be updated.
 m the values of m for which the updates will be made.

Value

model the model with the updated alphas.

See Also

[gpCreate](#), [gpUpdateAD](#), [gpUpdateKernels](#).

Examples

```
## missing
```

gpComputeM *Compute the matrix m given the model.*

Description

computes the matrix m (the scaled, bias and mean function removed matrix of the targets), given the model.

Usage

```
gpComputeM(model)
```

Arguments

model the model for which the values are to be computed.

Value

m the scaled, bias and mean function removed values.

See Also

[gpCreate](#), [gpComputeAlpha](#), [gpUpdateAD](#).

Examples

```
## missing
```

gpCovGrads	<i>Sparse objective function gradients wrt Covariance functions for inducing variables.</i>
------------	---

Description

gives the gradients of the log likelihood with respect to the components of the sparse covariance (or the full covariance for the ftc case).

Usage

```
gpCovGrads(model, M)
```

Arguments

model the model for which the gradients are to be computed.
M The training data for which the computation is to be made

Value

gK_uu the gradient of the likelihood with respect to the elements of K_uu (or in the case of the 'ftc' criterion the gradients with respect to the kernel).
gK_uf the gradient of the likelihood with respect to the elements of K_uf.
gLambda the gradient of the likelihood with respect to the diagonal term in the fitc approximation and the blocks of the pitc approximation.
gBeta the gradient with respect to the beta term in the covariance structure.

See Also

[gpCreate](#), [gpLogLikeGradients](#).

Examples

```
## missing
```

gpCovGradsTest	<i>Test the gradients of the likelihood wrt the covariance.</i>
----------------	---

Description

tests the gradients of the covariance to ensure they are correct.

Usage

```
gpCovGradsTest(model)
```

Arguments

model	the model to be tested.
-------	-------------------------

Value

model	the model that was tested.
-------	----------------------------

See Also

[gpCreate](#), [gpCovGrads](#).

Examples

```
## missing
```

gpCreate	<i>Create a GP model with inducing variables/pseudo-inputs.</i>
----------	---

Description

Creates a Gaussian process model structure with default parameter settings as specified by the options vector.

Usage

```
gpCreate(q, d, X, y, options)
```

Arguments

q	input data dimension.
d	the number of processes (i.e. output data dimension).
X	the input data matrix.
y	the target (output) data.
options	options structure as defined by gpOptions.R.

Value

model model structure containing the Gaussian process.

See Also

[gpOptions.](#)

Examples

```
## missing
```

gpDataIndices	<i>Return indices of present data.</i>
---------------	--

Description

returns the indices of data which is not missing for a given dimension in the GP-LVM and a block number in the PITC approximation.

Usage

```
gpDataIndices(model, dimNo, blockNo)
```

Arguments

model the model for which the indices are being returned.
dimNo the dimension for which the presence of missing data is being looked at.
blockNo the block number in the PITC approximation for which the indices are required.

Value

ind indices of training data along that dimension which isn't missing.

See Also

[gpCreate.](#)

Examples

```
## missing
```

gpExpandParam	<i>Expand a parameter vector into a GP model.</i>
---------------	---

Description

takes the given vector of parameters and places them in the model structure, it then updates any stored representations that are dependent on those parameters, for example kernel matrices etc..

Usage

```
gpExpandParam(model, params)
```

Arguments

model	the model structure for which parameters are to be updated.
params	a vector of parameters for placing in the model structure.

Value

model	a returned model structure containing the updated parameters.
-------	---

See Also

[gpCreate](#), [gpExtractParam](#), [modelExtractParam](#), [gpUpdateKernels](#).

Examples

```
## missing
```

gpExtractParam	<i>Extract a parameter vector from a GP model.</i>
----------------	--

Description

does the same as above, but also returns parameter names.

Usage

```
gpExtractParam(model, only.values=TRUE, ...)
```

Arguments

model	the model structure containing the information about the model.
only.values	(logical) do not return parameter names.
...	optional additional arguments.

Value

params a vector of parameters from the model.
names cell array of parameter names.

See Also

[gpCreate](#), [gpExpandParam](#), [modelExtractParam](#).

Examples

```
## missing
```

gpGradient	<i>Gradient wrapper for a GP model.</i>
------------	---

Description

wraps the log likelihood gradient function to return the gradient of the negative of the log likelihood. This can then be used in, for example, NETLAB, minimisation tools.

Usage

```
gpGradient(params, model)
```

Arguments

params the parameters of the model.
model the model for which gradients will be computed.

Value

g the returned gradient of the negative log likelihood for the given parameters.

See Also

[gpCreate](#), [gpGradient](#), [gpLogLikeGradients](#), [gpOptimise](#).

Examples

```
## missing
```

gpLogLikeGradients *Compute the gradients for the parameters and X.*

Description

computes the gradients of the Gaussian process log likelihood with respect to the model parameters (and optionally, as above with respect to inducing variables and input data) given the target data, input data and inducing variable locations.

Usage

```
gpLogLikeGradients(model, X=model$X, M, X_u, gX_u.return=FALSE, gX.return=FALSE, g_beta.return=FALSE)
```

Arguments

model	the model structure for which gradients are computed.
X	the input data locations for which gradients are computed.
M	the scaled and bias removed target data for which the gradients are computed.
X_u	the inducing variable locations for which gradients are computed.
gX_u.return	(logical) return the gradient of the log likelihood with respect to the inducing variables. If inducing variables aren't being used this returns zero.
gX.return	(logical) return the gradient of the log likelihood with respect to the input data locations.
g_beta.return	(logical) to return the gradient of the log likelihood with respect to beta.

Value

gParam	contains the gradient of the log likelihood with respect to the model parameters (including any gradients with respect to beta).
--------	--

See Also

[gpLogLikelihood](#).

Examples

```
## missing
```

gpLogLikelihood *Compute the log likelihood of a GP.*

Description

computes the log likelihood of a data set given a GP model.

Usage

```
gpLogLikelihood(model)
```

Arguments

model the GP model for which log likelihood is to be computed.

Value

ll the log likelihood of the data in the GP model.

See Also

[gpCreate](#), [gpLogLikeGradients](#), [modelLogLikelihood](#).

Examples

```
## missing
```

gpMeanFunctionGradient *Compute the log likelihood gradient wrt the scales.*

Description

computes the gradient of the log likelihood with respect to the scales. In the future the gradients with respect to the biases may also be included.

Usage

```
gpMeanFunctionGradient(model)
```

Arguments

model the model for which the gradients are to be computed.

Value

g the gradients of the likelihood with respect to the mean function's parameters.

See Also

[gpCreate](#), [gpScaleBiasGradient](#), [gpLogLikeGradients](#), [gpLogLikelihood](#).

Examples

```
## missing
```

gpObjective	<i>Wrapper function for GP objective.</i>
-------------	---

Description

returns the negative log likelihood of a Gaussian process model given the model structure and a vector of parameters. This allows the use of NETLAB minimisation functions to find the model parameters.

Usage

```
gpObjective(params, model)
```

Arguments

params	the parameters of the model for which the objective will be evaluated.
model	the model structure for which the objective will be evaluated.

Value

f	the negative log likelihood of the GP model.
---	--

See Also

[gpCreate](#), [gpGradient](#), [gpLogLikelihood](#), [gpOptimise](#).

Examples

```
## missing
```

gpOptimise	<i>Optimise the inducing variable based kernel.</i>
------------	---

Description

optimises the Gaussian process model for a given number of iterations.

Usage

```
gpOptimise(model, display, iters, gradcheck)
```

Arguments

model	the model to be optimised.
display	whether or not to display while optimisation proceeds, set to 2 for the most verbose and 0 for the least verbose.
iters	number of iterations for the optimisation.
gradcheck	(logical) do a gradient check.

Value

model	the optimised model.
-------	----------------------

See Also

[gpCreate](#), [gpGradient](#), [gpObjective](#).

Examples

```
## missing
```

gpOptions	<i>Return default options for GP model.</i>
-----------	---

Description

returns the default options in a structure for a GP model.

Usage

```
gpOptions(approx)
```

Arguments

approx approximation type, either 'ftc' (no approximation), 'dtevar' (variational sparse approximation) 'dte' (deterministic training conditional), 'fite' (fully independent training conditional) or 'pite' (partially independent training conditional).

Value

options structure containing the default options for the given approximation type.

See Also

[gpCreate](#).

Examples

```
## missing
```

gpOut

Evaluate the output of an Gaussian process model.

Description

evaluates the output of a given Gaussian process model.

Usage

```
gpOut(model, x)
```

Arguments

model the model for which the output is being evaluated.
 x the input position for which the output is required.

Value

y the output of the GP model. The function checks if there is a noise model associated with the GP, if there is, it is used, otherwise the mean of gpPosteriorMeanVar is returned.

See Also

[gpCreate](#), [gpPosteriorMeanVar](#).

Examples

```
## missing
```

gpPlot *Gaussian Process Plotter*

Description

Plots the GP mean and variance.

Usage

```
gpPlot(model, Xstar, mu, S, simpose=NULL, xlim=NULL, ylim=NULL, xlab='', ylab='', col='blue', title='')
```

Arguments

model	the model structure for which GP mean and variance are to be plotted.
Xstar	the input positions for which the mean and variance will be plotted.
mu	the precomputed GP posterior mean vector.
S	the precomputed GP posterior variance vector.
simpose	vector of datapoints to be superimposed on the plot with added white noise.
xlim	x-axis plotting limits.
ylim	y-axis plotting limits.
xlab	x-axis label.
ylab	y-axis label.
col	color for plotting the GP mean and variance.
title	plot title.

See Also

[gpPosteriorMeanVar](#), [polygon](#), [zeroAxes](#).

gpPosteriorMeanVar *Mean and variances of the posterior at points given by X.*

Description

returns the posterior mean and variance for a given set of points.

Usage

```
gpPosteriorMeanVar(model, X, varsigma.return=FALSE)
```

Arguments

`model` the model for which the posterior will be computed.
`X` the input positions for which the posterior will be computed.
`varsigma.return` (logical) compute variances.

Value

`mu` the mean of the posterior distribution.
`sigma` the variances of the posterior distributions.

See Also

[gpCreate.](#)

Examples

```
## missing
```

`gpPosteriorSample` *Plot Samples from a GP Posterior.*

Description

Gaussian processes are non-parametric models. They are specified by their covariance function and a mean function. When combined with data observations a posterior Gaussian process is induced. This function samples from that posterior.

Usage

```
gpPosteriorSample(kernType, numSamps=10, params=NULL, lims=c(-3,3), path=getwd(), png=FALSE)
```

Arguments

`kernType` the type of kernel to sample from.
`numSamps` the number of samples to take.
`params` parameter vector for the kernel.
`lims` limits of the x axis.
`path` path where the plot images are saved.
`png` save image as png.

See Also

[gpOptions](#), [kernCreate](#), [kernCompute](#), [gaussSamp](#), [zeroAxes](#).

gpSample	<i>Plot Samples from a GP.</i>
----------	--------------------------------

Description

creates a plot of samples from a kernel with the given parameters and variance.

Usage

```
gpSample(kernType, numSamps=10, params=NULL, lims=c(-3,3), path=getwd(), png=FALSE)
```

Arguments

kernType	the type of kernel to sample from.
numSamps	the number of samples to take.
params	parameter vector for the kernel.
lims	limits of the x axis.
path	path where the plot images are saved.
png	save image as png.

See Also

[gpOptions](#).

gpScaleBiasGradient	<i>Compute the log likelihood gradient wrt the scales.</i>
---------------------	--

Description

computes the gradient of the log likelihood with respect to the scales. In the future the gradients with respect to the biases may also be included.

Usage

```
gpScaleBiasGradient(model)
```

Arguments

model	the model for which the gradients are to be computed.
-------	---

Value

g	the gradients of the likelihood with respect to the scales.
---	---

See Also

[gpCreate](#), [gpLogLikeGradients](#), [gpLogLikelihood](#).

Examples

```
## missing
```

gpTest

Test the gradients of the gpCovGrads function and the gp models.

Description

runs some tests on the GP code to test that it is working.

Usage

```
gpTest(q=2, d=3, N=10, k=5)
```

Arguments

q	input data dimension.
d	the number of processes (i.e. output data dimension).
N	the number of datapoints.
k	the number of inducing variables.

Value

model	a cell array of models used for testing.
-------	--

Examples

```
## missing
```

gpUpdateAD	<i>Update the representations of A and D associated with the model.</i>
------------	---

Description

updates the representations of A and D in the model when called by gpUpdateKernels.

Usage

```
gpUpdateAD(model, X)
```

Arguments

model	the model for which the representations are being updated.
X	the X values for which the representations are being computed.

Value

model	the model with the A and D representations updated.
-------	---

See Also

[gpUpdateKernels](#), [gpExpandParam](#).

Examples

```
## missing
```

gpUpdateKernels	<i>Update the kernels that are needed.</i>
-----------------	--

Description

updates any representations of the kernel in the model structure, such as invK, logDetK or K.

Usage

```
gpUpdateKernels(model, X, X_u)
```

Arguments

model	the model structure for which kernels are being updated.
X	the input locations for update of kernels.
X_u	the inducing input locations.

Value

model the model structure with the kernels updated.

See Also

[gpExpandParam](#), [gpCreate](#).

Examples

```
## missing
```

kernCompute	<i>Compute the kernel given the parameters and X.</i>
-------------	---

Description

Compute the kernel given the parameters and X.

Usage

```
kernCompute(kern, x, x2)
kernDiagCompute(kern, x)
```

Arguments

kern	kernel structure to be computed.
x	depending on the number of inputs, x can be the input data matrix (rows are data points) to the kernel computation, or the first input matrix to the kernel computation (forms the rows of the kernel).
x2	second input matrix to the kernel computation (forms the columns of the kernel).

Details

$K \leftarrow \text{kernCompute}(\text{kern}, x)$ computes a kernel matrix for the given kernel type given an input data matrix.

$K \leftarrow \text{kernCompute}(\text{kern}, x1, x2)$ computes a kernel matrix for the given kernel type given two input data matrices, one for the rows and one for the columns.

$K \leftarrow \text{kernDiagCompute}(\text{kern}, x)$ computes the diagonal of a kernel matrix for the given kernel.

$K \leftarrow *X*\text{kernCompute}(\text{kern1}, \text{kern2}, x)$ $K \leftarrow *X*\text{kernCompute}(\text{kern1}, \text{kern2}, x1, x2)$ same as above, but for cross combinations of two kernels, kern1 and kern2.

Value

K	computed elements of the kernel structure.
Kd	vector containing computed diagonal elements of the kernel structure.

See Also[kernCreate](#)**Examples**

```
kern <- kernCreate(1, 'rbf')
K <- kernCompute(kern, as.matrix(3:8))
```

kernCreate	<i>Initialise a kernel structure.</i>
------------	---------------------------------------

Description

Initialise a kernel structure.

Usage

```
kernCreate(x, kernType, kernOptions=NULL)
```

Arguments

x	Input data values (from which kernel will later be computed).
kernType	Type of kernel to be created, some standard types are 'lin', 'rbf', 'white', 'bias' and 'rbfard'. If a cell of the form 'cmpnd', 'rbf', 'lin', 'white' is used a compound kernel based on the sum of the individual kernels will be created. The 'cmpnd' element at the start of the sequence is optional. Furthermore, 'tensor', 'rbf', 'lin' can be used to give a tensor product kernel, whose elements are the formed from the products of the two individual kernel's elements and 'multi', 'rbf', ... can be used to create a block structured kernel for use with multiple outputs. Finally the form 'parametric', struct('opt1', val1), 'rbf' can be used to pass options to other kernels.
kernOptions	the kernel options.

Details

kern <- kernCreate(x, kernType) input points and a kernel type.

kern <- kernCreate(dim, kernType) creates a kernel matrix structure given the dimensions of the design matrix and the kernel type.

Value

kern	The kernel structure.
------	-----------------------

See Also[kernParamInit](#).

Examples

```
## missing
```

kernDiagGradient	<i>Compute the gradient of the kernel's parameters for the diagonal.</i>
------------------	--

Description

computes the gradient of functions of the diagonal of the kernel matrix with respect to the parameters of the kernel. The parameters' gradients are returned in the order given by the `kernExtractParam` command.

Usage

```
kernDiagGradient(kern, x, covDiag)
```

Arguments

kern	the kernel structure for which the gradients are computed.
x	the input data for which the gradient is being computed.
covDiag	partial derivatives of the function of interest with respect to the diagonal elements of the kernel matrix.

Value

g	gradients of the relevant function with respect to each of the parameters. Ordering should match the ordering given in <code>kernExtractParam</code> .
---	--

See Also

[kernDiagGradient](#), [kernExtractParam](#), [kernGradient](#).

Examples

```
## missing
```

kernDiagGradX	<i>Compute the gradient of the kernel wrt X.</i>
---------------	--

Description

computes the gradient of the (diagonal of the) kernel matrix with respect to the elements of the design matrix given in X.

Usage

```
kernDiagGradX(kern, x)
kernGradX(kern, x1, x2)
```

Arguments

kern	the kernel structure for which gradients are being computed.
x	the input data in the form of a design matrix.
x1	row locations against which gradients are being computed.
x2	column locations against which gradients are being computed.

Value

gX	the gradients of the diagonal with respect to each element of X. The returned matrix has the same dimensions as X.
gX2	the returned gradients. The gradients are returned in a matrix which is numData x numInputs x numData. Where numData is the number of data points and numInputs is the number of input dimensions in X.

See Also

[kernGradient](#)

kernGradient	<i>Compute the gradient wrt the kernel parameters.</i>
--------------	--

Description

Compute the gradient wrt the kernel parameters.

Usage

```
kernGradient(kern, x, ...)
## kernGradient(kern, x, partial)
## kernGradient(kern, x, x1, x2, partial_)
```

Arguments

kern	the kernel structure for which the gradients are being computed.
x	the input locations for which the gradients are being computed.
...	other arguments such as: 'partial', a matrix of partial derivatives of the function of interest with respect to the kernel matrix. The argument takes the form of a square matrix of dimension numData, where numData is the number of rows in X, 'x1', the input locations associated with the rows of the kernel matrix, 'x2', the input locations associated with the columns of the kernel matrix, 'partial_', matrix of partial derivatives of the function of interest with respect to the kernel matrix. The matrix should have the same number of rows as X1 and the same number of columns as X2 has rows.

Details

`g <- kernGradient(kern, x, partial)` `g <- *kernGradient(kern, x, partial)` computes the gradient of functions with respect to the kernel parameters. As well as the kernel structure and the input positions, the user provides a matrix PARTIAL which gives the partial derivatives of the function with respect to the relevant elements of the kernel matrix.

`g <- kernGradient(kern, x1, x2, partial_)` `g <- *kernGradient(kern, x1, x2, partial_)` computes the derivatives as above, but input locations are now provided in two matrices associated with rows and columns of the kernel matrix.

`g <- *X*kernGradient(kern1, kern2, x, partial)` `g <- *X*kernGradient(kern1, kern2, x1, x2, partial_)` same as above, but for cross combinations of two kernels, kern1 and kern2.

Value

g	gradients of the function of interest with respect to the kernel parameters. The ordering of the vector should match that provided by the function kernExtractParam.
---	--

See Also

[kernCompute](#), [kernExtractParam](#).

Examples

```
kern <- kernCreate(1, 'rbf')
g <- kernGradient(kern, as.matrix(c(1, 4)), array(1, c(2, 2)))
```

kernParamInit

Kernel parameter initialisation.

Description

initialises the parameters of a kernel.

Usage

```
kernParamInit(kern)
```

Arguments

kern the kernel structure for which the parameters will be initialised.

Value

kern the kernel structure with the parameters initialised.

See Also

[kernCreate.](#)

Examples

```
## missing
```

kernTest	<i>Run some tests on the specified kernel.</i>
----------	--

Description

runs some tests on a given kernel structure to ensure it is correctly implemented.

Usage

```
kernTest(kernType, numIn=4, tieParamNames=list(), testindex=NULL)
```

Arguments

kernType type of kernel to test. For example, 'rbf' or 'cmpnd', 'rbf', 'lin', 'white'.
 numIn the number of input dimensions (default is 4).
 tieParamNames list of regular expressions for parameter names that should be tied (default is none).
 testindex indices of the covariance gradient to test for.

Value

kern the kernel as it was used in the tests.

See Also

[kernCreate.](#)

Examples

```
## missing
```

modelDisplay	<i>Display a model.</i>
--------------	-------------------------

Description

displays the parameters of the model/kernel and the model/kernel type to the console.

Usage

```
modelDisplay(model, ...)
```

Arguments

model	the model/kernel structure to be displayed.
...	optional additional arguments.

See Also

[modelExtractParam](#)

modelExpandParam	<i>Update a model structure with new parameters or update the posterior processes.</i>
------------------	--

Description

Update a model structure or component with new parameters, or update the posterior processes.

Usage

```
modelExpandParam(model, params)
modelUpdateProcesses(model, predt=NULL)
```

Arguments

model	the model structure to be updated.
params	vector of parameters.
predt	.

Details

`model <- modelExpandParam(model, param)` returns a model structure filled with the parameters in the given vector. This is used as a helper function to enable parameters to be optimised in, for example, the optimisation functions.

`model <- modelUpdateProcesses(model)` updates posterior processes of the given model.

Value

model updated model structure.

See Also

[modelExtractParam](#)

modelExtractParam *Extract the parameters of a model.*

Description

Extract parameters from the model into a vector of parameters for optimisation.

Usage

```
modelExtractParam(model, only.values=TRUE, untransformed.values=FALSE)
```

Arguments

model the model structure containing the parameters to be extracted.
 only.values include parameter names in the returned vector.
 untransformed.values return actual values, not transformed values used by the optimisers.

Value

param vector of parameters extracted from the model.

See Also

[modelExpandParam](#)

modelGradient *Model log-likelihood/objective error function and its gradient.*

Description

modelGradient gives the gradient of the objective function for a model. By default the objective function (modelObjective) is a negative log likelihood (modelLogLikelihood).

Usage

```
modelObjective(params, model, ...)
modelLogLikelihood(model)
modelGradient(params, model, ...)
```

Arguments

params	parameter vector to evaluate at.
model	model structure.
...	optional additional arguments.

Value

g	the gradient of the error function to be minimised.
v	the objective function value (lower is better).
ll	the log-likelihood value.

See Also

[modelOptimise](#).

modelGradientCheck	<i>Check gradients of given model.</i>
--------------------	--

Description

checks the supplied gradient function and the supplied objective function to ensure that the numerical gradients (as computed with the objective function) match the analytically computed gradients.

Usage

```
modelGradientCheck(model, ...)
```

Arguments

model	the model for which gradients are to be checked.
...	additional arguments that are passed to the objective and gradient functions (after the parameter vector which is always assumed to be the first argument passed).

See Also

[modelObjective](#), [modelGradient](#).

modelOut	<i>Give the output of a model for given X.</i>
----------	--

Description

Give the output of a model for given X.

Usage

```
modelOut(model, X, Phi.return=FALSE, ...)
```

Arguments

model	structure specifying the model.
X	input location(s) for which output is to be computed.
Phi.return	(logical) return the basis function(s) as well.
...	optional additional arguments.

Details

`Y <- modelOut(model, X)` gives the output of the model for a given input X. For latent variable models it gives a position in data space given a position in latent space.

`Phi, Y <- modelOut(model, X)` gives the output of the model for a given input X. For latent variable models it gives a position in data space given a position in latent space.

Value

Y	output location(s) corresponding to given input locations.
Phi	output basis function(s) corresponding to given input

Examples

```
## missing
```

modelOutputGrad	<i>Compute derivatives with respect to params of model outputs.</i>
-----------------	---

Description

Compute derivatives with respect to params of model outputs.

Usage

```
modelOutputGrad(model, X, dim)
```

Arguments

model	the model structure for which gradients are computed.
X	input locations where gradients are to be computed.
dim	the dimension of the model for which gradients are required.

Details

`g <- modelOutputGrad(model, X)` gives the gradients of the outputs from the model with respect to the parameters for a given set of inputs.

`g <- modelOutputGrad(model, X, dim)` gives the gradients of the outputs from the model with respect to the parameters for a given set of inputs.

Value

g	gradients of the model output with respect to the model parameters for the given input locations. The size of the returned matrix is of dimension number of data x number of parameters x number of model outputs (which maintains compatibility with NETLAB).
---	--

See Also

[modelLogLikelihood](#).

Examples

```
## missing
```

multiKernParamInit *MULTI kernel parameter initialisation.*

Description

initialises the multiple output block kernel structure with some default parameters.

Usage

```
multiKernParamInit(kern)
```

Arguments

kern	the kernel structure which requires initialisation.
------	---

Value

kern	the kernel structure with the default parameters placed in.
------	---

See Also

[kernCreate](#), [kernParamInit](#).

Examples

```
## missing
```

noiseCreate	<i>Initialise a noise structure.</i>
-------------	--------------------------------------

Description

takes a noise type and a target vector and initialises a noise structure from it. The parameters of the noise structure are the set by calling noiseParamInit.

Usage

```
noiseCreate(noiseType, y)
```

Arguments

noiseType	the type of noise to be created (e.g. 'gaussian', 'probit', 'ncnm').
y	the target vector.

See Also

[noiseParamInit](#).

Examples

```
## missing
```

noiseOut	<i>Give the output of the noise model given the mean and variance.</i>
----------	--

Description

computes the output for the given noise given input mean and variances.

Usage

```
noiseOut(noise, mu, varsigma)
```

Arguments

noise	the noise structure for which the output is computed.
mu	the input mean values.
varsigma	the input variance values.

Value

y	the output from the noise model.
---	----------------------------------

See Also

[noiseParamInit](#), [noiseCreate](#).

Examples

```
## missing
```

noiseParamInit	<i>Noise model's parameter initialisation.</i>
----------------	--

Description

initialises the noise structure with some default parameters.

Usage

```
noiseParamInit(noise,y)
```

Arguments

noise	the noise structure which requires initialisation.
y	the data design matrix.

Value

noise	the noise structure with the default parameters placed in.
-------	--

See Also

[noiseCreate](#).

Examples

```
## missing
```

`optimiDefaultConstraint`*Returns function for parameter constraint.*

Description

returns the current default function for constraining a parameter.

Usage

```
optimiDefaultConstraint(constraint)
```

Arguments

`constraint` the type of constraint you want to place on the parameter, options include 'positive' (gives an 'exp' constraint) and 'zeroone' (gives a 'sigmoid' constraint).

Value

`val` a list with two components: 'func' for the name of function used to apply the constraint, and 'hasArgs' for a boolean flag if the function requires additional arguments.

See Also

[expTransform](#), [sigmoidTransform](#).

Examples

```
optimiDefaultConstraint('positive')  
optimiDefaultConstraint('bounded')
```

`rbfKernDiagGradX`*Gradient of RBF kernel's diagonal with respect to X.*

Description

computes the gradient of the diagonal of the radial basis function kernel matrix with respect to the elements of the design matrix given in X.

Usage

```
rbfKernDiagGradX(kern, X)
```

Arguments

kern	the kernel structure for which gradients are being computed.
X	the input data in the form of a design matrix.

Value

gX	the gradients of the diagonal with respect to each element of X. The returned matrix has the same dimensions as X.
----	--

See Also

[rbfKernParamInit](#), [kernDiagGradX](#), [rbfKernGradX](#).

Examples

```
## missing
```

rbfKernGradX	<i>Gradient of RBF kernel with respect to input locations.</i>
--------------	--

Description

computes the gradient of the radial basis function kernel with respect to the input positions where both the row positions and column positions are provided separately.

Usage

```
rbfKernGradX(kern, x1, x2)
```

Arguments

kern	kernel structure for which gradients are being computed.
x1	row locations against which gradients are being computed.
x2	column locations against which gradients are being computed.

Value

g	the returned gradients. The gradients are returned in a matrix which is numData2 x numInputs x numData1. Where numData1 is the number of data points in X1, numData2 is the number of data points in X2 and numInputs is the number of input dimensions in X.
---	---

See Also

[rbfKernParamInit](#), [kernGradX](#), [rbfKernDiagGradX](#).

Examples

```
## missing
```

rbfKernParamInit	<i>RBF kernel parameter initialisation.</i>
------------------	---

Description

initialises the radial basis function kernel structure with some default parameters.

Usage

```
rbfKernParamInit(kern)
```

Arguments

kern	the kernel structure which requires initialisation.
------	---

Value

kern	the kernel structure with the default parameters placed in.
------	---

See Also

[kernCreate](#), [kernParamInit](#).

Examples

```
## missing
```

SCGoptim	<i>Optimise the given function using (scaled) conjugate gradients.</i>
----------	--

Description

Optimise the given function using (scaled) conjugate gradients.

Usage

```
## options <- optimiDefaultOptions()
SCGoptim(x, fn, grad, options, ...)
CGoptim(x, fn, grad, options, ...)
modelOptimise(model, options, ...)
```

Arguments

model	the model to be optimised.
x	initial parameter values.
fn	objective function to minimise
grad	gradient function of the objective
options	options structure like one returned by <code>optimiDefaultOptions</code> . The fields are interpreted as <code>\ option[1]</code> : number of iterations <code>\ option[2]</code> : interval for the line search <code>\ option[3]</code> : tolerance for x to terminate the loop <code>\ option[4]</code> : tolerance for fn to terminate the loop <code>\ option\$display</code> : option of showing the details of optimisation
...	extra arguments to pass to fn and grad

Value

options	an options structure
newParams	optimised parameter values
model	the optimised model.

See Also

[modelObjective](#), [modelGradient](#)

Examples

```
## Not run to speed up package checks
# model <- GPLearn(..., dontOptimise=TRUE)
# options <- optimiDefaultOptions()
# model <- modelOptimise(model, options)
```

whiteKernDiagGradX *Gradient of WHITE kernel's diagonal with respect to X.*

Description

computes the gradient of the diagonal of the white noise kernel matrix with respect to the elements of the design matrix given in X.

Usage

```
whiteKernDiagGradX(kern, X)
```

Arguments

kern	the kernel structure for which gradients are being computed.
X	the input data in the form of a design matrix.

Value

`gX` the gradients of the diagonal with respect to each element of `X`. The returned matrix has the same dimensions as `X`.

See Also

[whiteKernParamInit](#), [kernDiagGradX](#), [whiteKernGradX](#).

Examples

```
## missing
```

<code>whiteKernGradX</code>	<i>Gradient of WHITE kernel with respect to input locations.</i>
-----------------------------	--

Description

computes the gradient of the white noise kernel with respect to the input positions where both the row positions and column positions are provided separately.

Usage

```
whiteKernGradX(kern, x1, x2)
```

Arguments

<code>kern</code>	kernel structure for which gradients are being computed.
<code>x1</code>	row locations against which gradients are being computed.
<code>x2</code>	column locations against which gradients are being computed.

Value

`g` the returned gradients. The gradients are returned in a matrix which is `numData2 x numInputs x numData1`. Where `numData1` is the number of data points in `X1`, `numData2` is the number of data points in `X2` and `numInputs` is the number of input dimensions in `X`.

Examples

```
## missing
```

whiteKernParamInit	<i>WHITE kernel parameter initialisation.</i>
--------------------	---

Description

initialises the white noise kernel structure with some default parameters.

Usage

```
whiteKernParamInit(kern)
```

Arguments

kern	the kernel structure which requires initialisation.
------	---

Value

kern	the kernel structure with the default parameters placed in.
------	---

See Also

[kernCreate](#), [kernParamInit](#).

Examples

```
## missing
```

zeroAxes	<i>A function to move the axes crossing point to the origin.</i>
----------	--

Description

moves the crossing point of the axes to the origin.

Usage

```
zeroAxes(col='blue')
```

Arguments

col	color of the axes..
-----	---------------------

See Also

[plot](#).

Examples

```
## missing
```

Index

*Topic **model**

- basePlot, [3](#)
- cmpndKernParamInit, [3](#)
- cmpndNoiseParamInit, [4](#)
- demAutoOptimiseGp, [5](#)
- demGpCov2D, [5](#)
- demGpSample, [6](#)
- demInterpolation, [6](#)
- demOptimiseGp, [7](#)
- demRegression, [8](#)
- expTransform, [8](#)
- gaussianNoiseOut, [9](#)
- gaussianNoiseParamInit, [10](#)
- gaussSamp, [10](#)
- gpBlockIndices, [11](#)
- gpComputeAlpha, [12](#)
- gpComputeM, [12](#)
- gpCovGrads, [13](#)
- gpCovGradsTest, [14](#)
- gpCreate, [14](#)
- gpDataIndices, [15](#)
- gpExpandParam, [16](#)
- gpExtractParam, [16](#)
- gpGradient, [17](#)
- gpLogLikeGradients, [18](#)
- gpLogLikelihood, [19](#)
- gpMeanFunctionGradient, [19](#)
- gpObjective, [20](#)
- gpOptimise, [21](#)
- gpOptions, [21](#)
- gpOut, [22](#)
- gpPlot, [23](#)
- gpPosteriorMeanVar, [23](#)
- gpScaleBiasGradient, [25](#)
- gpTest, [26](#)
- gpUpdateAD, [27](#)
- gpUpdateKernels, [27](#)
- kernCompute, [28](#)
- kernCreate, [29](#)
- kernDiagGradient, [30](#)
- kernDiagGradX, [31](#)
- kernGradient, [31](#)
- kernParamInit, [32](#)
- kernTest, [33](#)
- modelDisplay, [34](#)
- modelExpandParam, [34](#)
- modelExtractParam, [35](#)
- modelGradient, [35](#)
- modelGradientCheck, [36](#)
- modelOut, [37](#)
- modelOutputGrad, [37](#)
- multiKernParamInit, [38](#)
- noiseCreate, [39](#)
- noiseOut, [39](#)
- noiseParamInit, [40](#)
- optimiDefaultConstraint, [41](#)
- rbfKernDiagGradX, [41](#)
- rbfKernGradX, [42](#)
- rbfKernParamInit, [43](#)
- SCGoptim, [43](#)
- whiteKernDiagGradX, [44](#)
- whiteKernGradX, [45](#)
- whiteKernParamInit, [46](#)
- zeroAxes, [46](#)

- basePlot, [3](#), [6](#)
- boundedTransform (expTransform), [8](#)

- CGoptim (SCGoptim), [43](#)
- cgpdisimExpandParam (modelExpandParam), [34](#)
- cgpdisimExtractParam (modelExtractParam), [35](#)
- cgpdisimGradient (modelGradient), [35](#)
- cgpdisimLogLikeGradients (modelGradient), [35](#)
- cgpdisimLogLikelihood (modelGradient), [35](#)
- cgpdisimObjective (modelGradient), [35](#)

- cgpdismUpdateProcesses
 - (modelExpandParam), 34
- cgpsimExpandParam (modelExpandParam), 34
- cgpsimExtractParam (modelExtractParam), 35
- cgpsimGradient (modelGradient), 35
- cgpsimLogLikeGradients (modelGradient), 35
- cgpsimLogLikelihood (modelGradient), 35
- cgpsimObjective (modelGradient), 35
- cgpsimOptimise (SCGoptim), 43
- cgpsimUpdateProcesses
 - (modelExpandParam), 34
- cmpndKernCompute (kernCompute), 28
- cmpndKernDiagCompute (kernCompute), 28
- cmpndKernDiagGradX (kernDiagGradX), 31
- cmpndKernDisplay (modelDisplay), 34
- cmpndKernExpandParam
 - (modelExpandParam), 34
- cmpndKernExtractParam
 - (modelExtractParam), 35
- cmpndKernGradient (kernGradient), 31
- cmpndKernGradX (kernDiagGradX), 31
- cmpndKernParamInit, 3
- cmpndNoiseParamInit, 4

- demAutoOptimiseGp, 5
- demGpCov2D, 5
- demGpSample, 6, 6
- demInterpolation, 6, 8
- demOptimiseGp, 7
- demRegression, 8
- disimKernCompute (kernCompute), 28
- disimKernDiagCompute (kernCompute), 28
- disimKernDisplay (modelDisplay), 34
- disimKernExpandParam
 - (modelExpandParam), 34
- disimKernExtractParam
 - (modelExtractParam), 35
- disimKernGradient (kernGradient), 31
- disimXdisimKernCompute (kernCompute), 28
- disimXdisimKernGradient (kernGradient), 31
- disimXrbfKernCompute (kernCompute), 28
- disimXrbfKernGradient (kernGradient), 31
- disimXsimKernCompute (kernCompute), 28
- disimXsimKernGradient (kernGradient), 31

- eigen, 11

- expTransform, 8, 41

- gaussianNoiseOut, 9
- gaussianNoiseParamInit, 9, 10
- gaussSamp, 5–8, 10, 24
- gpBlockIndices, 11
- gpComputeAlpha, 11, 12, 13
- gpComputeM, 12
- gpCovGrads, 11, 13, 14
- gpCovGradsTest, 14
- gpCreate, 5, 7, 8, 12, 13, 14, 14–17, 19–22, 24, 26, 28
- gpDataIndices, 15
- gpdismDisplay (modelDisplay), 34
- gpdismExpandParam (modelExpandParam), 34
- gpdismExtractParam
 - (modelExtractParam), 35
- gpdismGradient (modelGradient), 35
- gpdismLogLikeGradients
 - (modelGradient), 35
- gpdismLogLikelihood (modelGradient), 35
- gpdismObjective (modelGradient), 35
- gpdismUpdateProcesses
 - (modelExpandParam), 34
- gpExpandParam, 5, 7, 16, 17, 27, 28
- gpExtractParam, 16, 16
- gpGradient, 17, 17, 20, 21
- gpLogLikeGradients, 11, 13, 17, 18, 19, 20, 26
- gpLogLikelihood, 5, 7, 11, 18, 19, 20, 26
- gpMeanFunctionGradient, 19
- gpObjective, 20, 21
- gpOptimise, 5, 17, 20, 21
- gpOptions, 5, 7, 8, 15, 21, 24, 25
- gpOut, 22
- gpPlot, 5, 7, 8, 23
- gpPosteriorMeanVar, 5, 7, 22, 23, 23
- gpPosteriorSample, 24
- gpSample, 25
- gpScaleBiasGradient, 20, 25
- gpsimDisplay (modelDisplay), 34
- gpsimExpandParam (modelExpandParam), 34
- gpsimExtractParam (modelExtractParam), 35
- gpsimGradient (modelGradient), 35
- gpsimLogLikeGradients (modelGradient), 35
- gpsimLogLikelihood (modelGradient), 35

- gpsimObjective (modelGradient), 35
- gpsimUpdateProcesses
 - (modelExpandParam), 34
- gpTest, 26
- gpUpdateAD, 11–13, 27
- gpUpdateKernels, 12, 16, 27, 27

- kernCompute, 6–8, 24, 28, 32
- kernCreate, 4–8, 24, 29, 29, 33, 39, 43, 46
- kernDiagCompute, 7, 8
- kernDiagCompute (kernCompute), 28
- kernDiagGradient, 30, 30
- kernDiagGradX, 31, 42, 45
- kernDisplay (modelDisplay), 34
- kernExpandParam (modelExpandParam), 34
- kernExtractParam, 30, 32
- kernExtractParam (modelExtractParam), 35
- kernGradient, 30, 31, 31
- kernGradX, 42
- kernGradX (kernDiagGradX), 31
- kernParamInit, 4, 29, 32, 39, 43, 46
- kernTest, 33

- localCovarianceGradients
 - (gpLogLikeGradients), 18
- localSCovarianceGradients
 - (gpLogLikeGradients), 18

- mlpKernCompute (kernCompute), 28
- mlpKernDiagGradX (kernDiagGradX), 31
- mlpKernExpandParam (modelExpandParam), 34
- mlpKernExtractParam
 - (modelExtractParam), 35
- mlpKernGradient (kernGradient), 31
- mlpKernGradX (kernDiagGradX), 31
- mlpOptions (gpOptions), 21
- modelDisplay, 34
- modelExpandParam, 34, 35
- modelExtractParam, 16, 17, 34, 35, 35
- modelGradient, 35, 36, 44
- modelGradientCheck, 36
- modelLogLikelihood, 19, 38
- modelLogLikelihood (modelGradient), 35
- modelObjective, 36, 44
- modelObjective (modelGradient), 35
- modelOptimise, 9, 36
- modelOptimise (SCGoptim), 43
- modelOut, 37

- modelOutputGrad, 37
- modelUpdateProcesses
 - (modelExpandParam), 34
- multiKernCompute (kernCompute), 28
- multiKernDiagCompute (kernCompute), 28
- multiKernDisplay (modelDisplay), 34
- multiKernExpandParam
 - (modelExpandParam), 34
- multiKernExtractParam
 - (modelExtractParam), 35
- multiKernGradient (kernGradient), 31
- multiKernParamInit, 38

- noiseCreate, 4, 9, 10, 39, 40
- noiseOut, 9, 39
- noiseParamInit, 4, 10, 39, 40, 40

- optimiDefaultConstraint, 41
- optimiDefaultOptions (SCGoptim), 43

- plot, 46
- polygon, 23

- rbfKernCompute (kernCompute), 28
- rbfKernDiagCompute (kernCompute), 28
- rbfKernDiagGradX, 41, 42
- rbfKernDisplay (modelDisplay), 34
- rbfKernExpandParam (modelExpandParam), 34
- rbfKernExtractParam
 - (modelExtractParam), 35
- rbfKernGradient (kernGradient), 31
- rbfKernGradX, 42, 42
- rbfKernGradXpoint (rbfKernGradX), 42
- rbfKernParamInit, 42, 43
- rnorm, 11

- SCGoptim, 43
- sigmoidTransform, 41
- sigmoidTransform (expTransform), 8
- simKernCompute (kernCompute), 28
- simKernDiagCompute (kernCompute), 28
- simKernDisplay (modelDisplay), 34
- simKernExpandParam (modelExpandParam), 34
- simKernExtractParam
 - (modelExtractParam), 35
- simKernGradient (kernGradient), 31
- simXrbfKernCompute (kernCompute), 28

simXrbfKernGradient (kernGradient), 31
simXsimKernCompute (kernCompute), 28
simXsimKernGradient (kernGradient), 31

translateKernCompute (kernCompute), 28
translateKernDiagCompute (kernCompute),
28
translateKernExpandParam
(modelExpandParam), 34
translateKernExtractParam
(modelExtractParam), 35
translateKernGradient (kernGradient), 31

whiteKernCompute (kernCompute), 28
whiteKernDiagCompute (kernCompute), 28
whiteKernDiagGradX, 44
whiteKernDisplay (modelDisplay), 34
whiteKernExpandParam
(modelExpandParam), 34
whiteKernExtractParam
(modelExtractParam), 35
whiteKernGradient (kernGradient), 31
whiteKernGradX, 45, 45
whiteKernParamInit, 45, 46
whiteXwhiteKernCompute (kernCompute), 28
whiteXwhiteKernGradient (kernGradient),
31

zeroAxes, 3, 6, 23, 24, 46