Package 'lrstat'

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Type Package

Title Power and Sample Size Calculation for Non-Proportional Hazards and Beyond

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Description Performs power and sample size calculation for non-proportional hazards model using the Fleming-Harrington family of weighted log-rank tests. The sequentially calculated log-rank test score statistics are assumed to have independent increments as characterized in Anastasios A. Tsiatis (1982) <doi:10.1080/01621459.1982.10477898>. The mean and variance of log-rank test score statistics are calculated based on Kaifeng Lu (2021) <doi:10.1002/pst.2069>. The boundary crossing probabilities are calculated using the recursive integration algorithm described in Christopher Jennison and Bruce W. Turnbull (2000, ISBN:0849303168). The package can also be used for continuous, binary, and count data. For continuous data, it can handle missing data through mixed-model for repeated measures (MMRM). In crossover designs, it can estimate direct treatment effects while accounting for carryover effects. For binary data, it can design Simon's 2-stage, modified toxicity probability-2 (mTPI-2), and Bayesian optimal interval (BOIN) trials. For count data, it can design group sequential trials for negative binomial endpoints with censoring. Additionally, it facilitates group sequential equivalence trials for all supported data types. Moreover, it can design adaptive group sequential trials for changes in sample size, error spending function, number and spacing or future looks. Finally, it offers various options for adjusted p-values, including graphical and gatekeeping procedures.

License GPL (>= 2)

Imports Rcpp (>= 1.0.9), mvtnorm (>= 1.1-3), lpSolve (>= 5.6.1), shiny (>= 1.7.1)

LinkingTo Rcpp

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R topics documented:

accrual 4
adaptDesign 5
BOINTable 9
caltime 11
ClopperPearsonCI 13
errorSpent 14
exitprob 15
fadjpbon 16
fadjpdun 17
fadjpsim 18
fmodmix 19
fseqbon 20
fstdmix 22
fstp2seq 24
ftrunc 25
fwgtmat 26
getAccrualDurationFromN 26
getADCI 27
getADRCI 31
getBound 34
getCI 35
getCP 37
getDesign 42
getDesignAgreement 45
getDesignANOVA 47
getDesignANOVAContrast 49
getDesignEquiv 51
getDesignFisherExact 56
getDesignLogistic 57
getDesignMeanDiff 60
getDesignMeanDiffCarryover 64
getDesignMeanDiffEquiv 67
getDesignMeanDiffMMRM 70
getDesignMeanDiffXO 72
getDesignMeanDiffXOEquiv 76
getDesignMeanRatio 79

getDesignMeanRatioEquiv . . . 82
getDesignMeanRatioXO . . . 85
getDesignMeanRatioXOEquiv . . . 89
getDesignOddsRatio . . . 92
getDesignOddsRatioEquiv . . . 95
getDesignOneMean . . . 98
getDesignOneMultinom . . . 102
getDesignOneProportion . . . 103
getDesignOneRateExact . . . 107
getDesignOneSlope . . . 108
getDesignOrderedBinom . . . 112
getDesignPairedMeanDiff . . . 113
getDesignPairedMeanDiffEquiv . . . 117
getDesignPairedMeanRatio . . . 119
getDesignPairedMeanRatioEquiv . . . 123
getDesignPairedPropMcNemar . . . 126
getDesignRepeatedANOVA . . . 129
getDesignRepeatedANOVAContrast . . . 131
getDesignRiskDiff . . . 133
getDesignRiskDiffEquiv . . . 136
getDesignRiskDiffExact . . . 139
getDesignRiskDiffExactEquiv . . . 141
getDesignRiskRatio . . . 142
getDesignRiskRatioEquiv . . . 146
getDesignRiskRatioExact . . . 149
getDesignRiskRatioExactEquiv . . . 150
getDesignRiskRatioFM . . . 152
getDesignSlopeDiff . . . 155
getDesignSlopeDiffMMRM . . . 159
getDesignTwoMultinom . . . 162
getDesignTwoOrdinal . . . 163
getDesignTwoWayANOVA . . . 165
getDesignUnorderedBinom . . . 166
getDesignUnorderedMultinom . . . 168
getDesignWilcoxon . . . 169
getDurationFromNevents . . . 173
getNeventsFromHazardRatio . . . 175
getRCI . . . 177
hedgesg . . . 179
kmest . . . 181
lrpower . . . 183
lrsamplesize . . . 188
lrsim . . . 192
lrsim2e . . . 197
lrsim2e3a . . . 201
lrsim3a . . . 206
lrstat . . . 210
mnOddsRatioCI . . . 213

mnRateDiffCI . . . 214
mnRateRatioCI . . . 215
mnRiskDiffCI . . . 217
mnRiskRatioCI . . . 218
mTPI2Table . . . 219
nbpower . . . 220
nbpower1s . . . 225
nbpowerequiv . . . 229
nbsamplesize . . . 233
nbsamplesize1s . . . 237
nbsamplesizeequiv . . . 240
nbstat . . . 243
ptpwexp . . . 248
qtpwexp . . . 249
remlOddsRatio . . . 250
remlRateDiff . . . 250
remlRateRatio . . . 251
remlRiskDiff . . . 252
remlRiskRatio . . . 253
repeatedPValue . . . 253
rtpwexp . . . 255
runShinyApp . . . 256
simon2stage . . . 256
survQuantile . . . 257
updateGraph . . . 258

Index **260**

`accrual` *Number of enrolled subjects*

Description

Obtains the number of subjects enrolled by given calendar times.

Usage

```
accrual(
  time = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  accrualDuration = NA_real_
)
```

Arguments

time	A vector of calendar times at which to calculate the number of enrolled subjects.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
accrualDuration	Duration of the enrollment period.

Value

A vector of total number of subjects enrolled by the specified calendar times.

Author(s)

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Examples

```
# Example 1: Uniform enrollment with 20 patients per month for 12 months.

accrual(time = 3, accrualTime = 0, accrualIntensity = 20,
        accrualDuration = 12)


# Example 2: Piecewise accrual, 10 patients per month for the first
# 3 months, and 20 patients per month thereafter. Patient recruitment
# ends at 12 months for the study.

accrual(time = c(2, 9), accrualTime = c(0, 3),
        accrualIntensity = c(10, 20), accrualDuration = 12)
```

---

adaptDesign *Adaptive design at an interim look*

Description

Obtains the conditional power for specified incremental information given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks. Conversely, obtains the incremental information needed to attain a specified conditional power given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks.

Usage

```
adaptDesign(
  betaNew = NA_real_,
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  spendingTime = NA_real_,
  MullerSchafer = 0L,
  kNew = NA_integer_,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  futilityStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  typeBetaSpendingNew = "none",
  parameterBetaSpendingNew = NA_real_,
  userBetaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_,
  varianceRatio = 1
)
```

Arguments

betaNew	The type II error for the secondary trial.
INew	The maximum information of the secondary trial. Either betaNew or INew should be provided while the other one should be missing.
L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
theta	The parameter value.
IMax	The maximum information of the primary trial. Must be provided if futilityBounds is missing and typeBetaSpending is not equal to "none", or if conditional power calculation is desired.
kMax	The maximum number of stages of the primary trial.

`informationRates`
: The information rates of the primary trial.

`efficacyStopping`
: Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

`futilityStopping`
: Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

`criticalValues`
: The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

`alpha`
: The significance level of the primary trial. Defaults to 0.025.

`typeAlphaSpending`
: The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
: The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
: The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.

`futilityBounds`
: The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
: The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
: The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`spendingTime`
: The error spending time of the primary trial. Defaults to missing, in which case, it is the same as `informationRates`.

`MullerSchafer`
: Whether to use the Muller and Schafer (2001) method for trial adaptation.

`kNew`
: The number of looks of the secondary trial.

`informationRatesNew`
: The spacing of looks of the secondary trial.

`efficacyStoppingNew`
: The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

`futilityStoppingNew`
: The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

`typeAlphaSpendingNew`
: The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpendingNew`
: The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`typeBetaSpendingNew`
: The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpendingNew`
: The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpendingNew`
: The user defined cumulative beta spending. Cumulative beta spent up to each stage of the secondary trial.

`spendingTimeNew`
: The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as `informationRatesNew`.

`varianceRatio`
: The ratio of the variance under H0 to the variance under H1.

Value

An `adaptDesign` object with two list components:

- `primaryTrial`: A list of selected information for the primary trial, including `L`, `zL`, `theta`, `kMax`, `informationRates`, `efficacyBounds`, `futilityBounds`, and `MullerSchafer`.
- `secondaryTrial`: A `design` object for the secondary trial.

Author(s)

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References

Lu Chi, H. M. James Hung, and Sue-Jane Wang. Modification of sample size in group sequential clinical trials. Biometrics 1999;55:853-857.

Hans-Helge Muller and Helmut Schafer. Adaptive group sequential designs for clinical trials: Combining the advantages of adaptive and of classical group sequential approaches. Biometrics 2001;57:886-891.

See Also

getDesign

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# conditional power with sample size increase
(des2 = adaptDesign(
  betaNew = NA, INew = 420/(4*sigma1^2),
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# Muller & Schafer (2001) method to design the secondary trial:
# 3-look gamma(-2) spending with 84% power at delta = 4.5 and sigma = 20
(des2 = adaptDesign(
  betaNew = 0.16, INew = NA,
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))

# incremental sample size for sigma = 20
(nNew = 4*sigma1^2*des2$secondaryTrial$overallResults$information)
```

BOINTable *BOIN decision table*

Description

Obtains the decision table for the Bayesian optimal interval (BOIN) design.

Usage

```
BOINTable(
  nMax = NA_integer_,
  pT = 0.3,
  phi1 = 0.6 * pT,
  phi2 = 1.4 * pT,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

Arguments

nMax	The maximum number of subjects in a dose cohort.
pT	The target toxicity probability. Defaults to 0.3.
phi1	The lower equivalence limit for target toxicity probability.
phi2	The upper equivalence limit for target toxicity probability.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if Prob(p > pT | Data) > pExcessTox, then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

Value

An S3 class BOINTable object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - phi1: The lower equivalence limit for target toxicity probability.
  - phi2: The upper equivalence limit for target toxicity probability.
  - lambda1: The lower decision boundary for observed toxicity probability.
  - lambda2: The upper decision boundary for observed toxicity probability.
  - a: The prior toxicity parameter for the beta prior.
  - b: The prior non-toxicity parameter for the beta prior.
  - pExcessTox: The threshold for excessive toxicity.
- decisionDataFrame: The decision data frame for the BOIN design. It includes the following variables:
  - n: The sample size.

  - y: The number of toxicities.
  - decision: The dosing decision.
- decisionMatrix: The decision matrix corresponding to the decision data frame.

Author(s)

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Examples

```
BOINTable(nMax = 18, pT = 0.3, phi = 0.6*0.3, phi2 = 1.4*0.3)
```

---

caltime *Calendar times for target number of events*

Description

Obtains the calendar times needed to reach the target number of subjects experiencing an event.

Usage

```
caltime(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

Arguments

nevents	A vector of target number of events.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

`accrualTime` A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

`accrualIntensity` A vector of accrual intensities. One for each accrual time interval.

`piecewiseSurvivalTime` A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

`stratumFraction` A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

`lambda1` A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

`lambda2` A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

`gamma1` The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

`gamma2` The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

`accrualDuration` Duration of the enrollment period.

`followupTime` Follow-up time for the last enrolled subject.

`fixedFollowup` Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

Value

A vector of calendar times expected to yield the target number of events.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

caltime(nevents = c(24, 80), allocationRatioPlanned = 1,
        accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
```

```
gamma2 = -log(1-0.05)/12,
accrualDuration = 22,
followupTime = 18, fixedFollowup = FALSE)
```

ClopperPearsonCI *Clopper-Pearson confidence interval for one-sample proportion*

Description

Obtains the Clopper-Pearson exact confidence interval for a one-sample proportion.

Usage

```
ClopperPearsonCI(n, y, cilevel = 0.95)
```

Arguments

n	The sample size.
y	The number of responses.
cilevel	The confidence interval level.

Value

A data frame with the following variables:

- n: The sample size.
- y: The number of responses.
- phat: The observed proportion of responses.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
ClopperPearsonCI(20, 3)
```

errorSpent *Error spending*

Description

Obtains the error spent at given spending times for the specified error spending function.

Usage

```
errorSpent(t, error, sf = "sfOF", sfpar = NA)
```

Arguments

t	A vector of spending times, typically equal to information fractions.
error	The total error to spend.
sf	The spending function. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, and "sfHSD" for Hwang, Shi & DeCani spending function. Defaults to "sfOF".
sfpar	The parameter for the spending function. Corresponds to rho for "sfKD" and gamma for "sfHSD".

Value

A vector of errors spent up to the interim look.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
errorSpent(t = 0.5, error = 0.025, sf = "sfOF")
errorSpent(t = c(0.5, 0.75, 1), error = 0.025, sf = "sfHSD", sfpar = -4)
```

exitprob *Stagewise exit probabilities*

Description

Obtains the stagewise exit probabilities for both efficacy and futility stopping.

Usage

```
exitprob(b, a = NA, theta = 0, I = NA)
```

Arguments

b	Upper boundaries on the z-test statistic scale.
a	Lower boundaries on the z-test statistic scale. Defaults to `c(rep(-6.0, kMax-1), b[kMax])` if left unspecified, where `kMax = length(b)`.
theta	Stagewise parameter of interest, e.g., `-U/V` for weighted log-rank test, where `U` is the mean and `V` is the variance of the weighted log-rank test score statistic at each stage. For proportional hazards and conventional log-rank test, use the scalar input, `theta = -log(HR)`. Defaults to 0 corresponding to the null hypothesis.
I	Stagewise cumulative information, e.g., `V`, the variance of the weighted log-rank test score statistic at each stage. For conventional log-rank test, information can be approximated by `phi*(1-phi)*D`, where `phi` is the probability of being allocated to the active arm, and `D` is the total number of events at each stage. Defaults to `seq(1, kMax)` if left unspecified.

Value

A list of stagewise exit probabilities:

- `exitProbUpper`: The vector of efficacy stopping probabilities
- `exitProbLower`: The vector of futility stopping probabilities.

Author(s)

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Examples

```
exitprob(b = c(3.471, 2.454, 2.004), theta = -log(0.6),
         I = c(50, 100, 150)/4)

exitprob(b = c(2.963, 2.359, 2.014),
         a = c(-0.264, 0.599, 2.014),
         theta = c(0.141, 0.204, 0.289),
         I = c(81, 121, 160))
```

fadjpbon *Adjusted p-values for Bonferroni-based graphical approaches*

Description

Obtains the adjusted p-values for graphical approaches using weighted Bonferroni tests.

Usage

```
fadjpbon(w, G, p)
```

Arguments

w	The vector of initial weights for elementary hypotheses.
G	The initial transition matrix.
p	The raw p-values for elementary hypotheses.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Frank Bretz, Willi Maurer, Werner Brannath and Martin Posch. A graphical approach to sequentially rejective multiple test procedures. Statistics in Medicine. 2009; 28:586-604.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
fadjpbon(w, g, pvalues)
```

fadjpdun *Adjusted p-values for Dunnett-based graphical approaches*

Description

Obtains the adjusted p-values for graphical approaches using weighted Dunnett tests.

Usage

```
fadjpdun(wgtmat, p, family = NULL, corr = NULL)
```

Arguments

wgtmat	The weight matrix for intersection hypotheses.
p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for elementary hypotheses.
corr	The correlation matrix that should be used for the parametric test. Can contain NAs for unknown correlations between families.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
corr = matrix(c(1,0.5,NA,NA, 0.5,1,NA,NA,
                NA,NA,1,0.5, NA,NA,0.5,1),
              nrow = 4, byrow = TRUE)
fadjpdun(wgtmat, pvalues, family, corr)
```

fadjpsim *Adjusted p-values for Simes-based graphical approaches*

Description

Obtains the adjusted p-values for graphical approaches using weighted Simes tests.

Usage

```
fadjpsim(wgtmat, p, family = NULL)
```

Arguments

wgtmat	The weight matrix for intersection hypotheses.
p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for elementary hypotheses.

Value

A matrix of adjusted p-values.

Author(s)

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References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

Kaifeng Lu. Graphical approaches using a Bonferroni mixture of weighted Simes tests. Statistics in Medicine. 2016; 35:4041-4055.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
fadjpsim(wgtmat, pvalues, family)
```

`fmodmix` *Adjusted p-values for modified mixture gatekeeping procedures*

Description

Obtains the adjusted p-values for the modified gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

Usage

```
fmodmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = 1
)
```

Arguments

`p`	The raw p-values for elementary hypotheses.
`family`	The matrix of family indicators for the hypotheses.
`serial`	The matrix of serial rejection set for the hypotheses.
`parallel`	The matrix of parallel rejection set for the hypotheses.
`gamma`	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
`test`	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
`exhaust`	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko, George Kordzakhia, and Thomas Brechenmacher. Mixture-based gatekeeping procedures for multiplicity problems with multiple sequences of hypotheses. Journal of Biopharmaceutical Statistics. 2016; 26(4):758–780.

George Kordzakhia, Thomas Brechenmacher, Eiji Ishida, Alex Dmitrienko, Winston Wenxiang Zheng, and David Fuyuan Li. An enhanced mixture method for constructing gatekeeping procedures in clinical trials. Journal of Biopharmaceutical Statistics. 2018; 28(1):113–128.

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 1, 0, 0,
                  0, 0, 0, 0, 0, 0, 1, 1),
                nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0,
                  0, 0, 0, 0, 0, 0, 0, 0,
                  1, 0, 0, 0, 0, 0, 0, 0,
                  0, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 0, 0, 0, 0, 0,
                  0, 0, 0, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 0, 0, 0,
                  0, 0, 0, 0, 0, 1, 0, 0),
                nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fmodmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 1)
```

`fseqbon` *Group sequential trials using Bonferroni-based graphical approaches*

Description

Obtains the test results for group sequential trials using graphical approaches based on weighted Bonferroni tests.

Usage

```
fseqbon(
  w,
  G,
  alpha = 0.025,
  kMax,
```

```
  typeAlphaSpending = NULL,
  parameterAlphaSpending = NULL,
  incidenceMatrix = NULL,
  maxInformation = NULL,
  p,
  information,
  spendingTime = NULL
)
```

Arguments

w	The vector of initial weights for elementary hypotheses.
G	The initial transition matrix.
alpha	The significance level. Defaults to 0.025.
kMax	The maximum number of stages.
typeAlphaSpending	The vector of alpha spending functions. Each element is one of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF" if not provided.
parameterAlphaSpending	The vector of parameter values for the alpha spending functions. Each element corresponds to the value of Delta for "WT", rho for "sfKD", or gamma for "sfHSD". Defaults to missing if not provided.
incidenceMatrix	The incidence matrix indicating whether the specific hypothesis will be tested at the given look. The number of columns of incidenceMatrix must be equal to the maximum number of study looks (kMax). If not provided, defaults to testing each hypothesis at all study looks.
maxInformation	The vector of target maximum information for each hypothesis. Defaults to a vector of 1s if not provided.
p	The matrix of raw p-values for each hypothesis by study look.
information	The matrix of observed information for each hypothesis by study look.
spendingTime	The spending time for alpha spending by study look. If not provided, it is the same as informationRates calculated from information and maxInformation.

Value

A vector to indicate the first look the specific hypothesis is rejected (0 if the hypothesis is not rejected).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Willi Maurer and Frank Bretz. Multiple testing in group sequential trials using graphical approaches. Statistics in Biopharmaceutical Research. 2013; 5:311-320.

Examples

```
# Case study from Maurer & Bretz (2013)

fseqbon(
  w = c(0.5, 0.5, 0, 0),
  G = matrix(c(0, 0.5, 0.5, 0,  0.5, 0, 0, 0.5,
               0, 1, 0, 0,  1, 0, 0, 0),
             nrow=4, ncol=4, byrow=TRUE),
  alpha = 0.025,
  kMax = 3,
  typeAlphaSpending = rep("sfOF", 4),
  maxInformation = rep(1, 4),
  p = matrix(c(0.0062, 0.017, 0.009, 0.13,
               0.0002, 0.0035, 0.002, 0.06),
             nrow=4, ncol=2),
  information = matrix(c(rep(1/3, 4), rep(2/3, 4)),
                       nrow=4, ncol=2))
```

---

fstdmix *Adjusted p-values for standard mixture gatekeeping procedures*

Description

Obtains the adjusted p-values for the standard gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

Usage

```
fstdmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = 1
)
```

Arguments

p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for the hypotheses.
serial	The matrix of serial rejection set for the hypotheses.
parallel	The matrix of parallel rejection set for the hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko and Ajit C Tamhane. Mixtures of multiple testing procedures for gatekeeping applications in clinical trials. Statistics in Medicine. 2011; 30(13):1473–1488.

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 1, 0, 0,
                  0, 0, 0, 0, 0, 0, 1, 1),
                nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0,
                  0, 0, 0, 0, 0, 0, 0, 0,
                  1, 0, 0, 0, 0, 0, 0, 0,
                  0, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 0, 0, 0, 0, 0,
                  0, 0, 0, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 0, 0, 0,
                  0, 0, 0, 0, 0, 1, 0, 0),
                nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fstdmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 0)
```

`fstp2seq` *Adjusted p-values for stepwise testing procedures for two sequences*

Description

Obtains the adjusted p-values for the stepwise gatekeeping procedures for multiplicity problems involving two sequences of hypotheses.

Usage

```
fstp2seq(p, gamma, test = "hochberg", retest = TRUE)
```

Arguments

`p`	The raw p-values for elementary hypotheses.
`gamma`	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
`test`	The component multiple testing procedure. It is either "Holm" or "Hochberg", and it defaults to "Hochberg".
`retest`	Whether to allow retesting. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
gamma = c(0.6, 0.6, 0.6, 1)
fstp2seq(p, gamma, test="hochberg", retest=1)
```

ftrunc *Adjusted p-values for Holm, Hochberg, and Hommel procedures*

Description

Obtains the adjusted p-values for possibly truncated Holm, Hochberg, and Hommel procedures.

Usage

```
ftrunc(p, test = "hommel", gamma = 1)
```

Arguments

p	The raw p-values for elementary hypotheses.
test	The test to use, e.g., "holm", "hochberg", or "hommel" (default).
gamma	The value of the truncation parameter. Defaults to 1 for the regular Holm, Hochberg, or Hommel procedure.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko, Ajit C. Tamhane, and Brian L. Wiens. General multistage gatekeeping procedures. Biometrical Journal. 2008; 5:667-677.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
ftrunc(pvalues, "hochberg")
```

fwgtmat *Weight matrix for all intersection hypotheses*

Description

Obtains the weight matrix for all intersection hypotheses.

Usage

```
fwgtmat(w, G)
```

Arguments

w	The vector of weights for elementary hypotheses.
G	The transition matrix.

Value

The weight matrix starting with the global null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
w = c(0.5,0.5,0,0)
g = matrix(c(0,0,1,0, 0,0,0,1, 0,1,0,0, 1,0,0,0),
           nrow=4, ncol=4, byrow=TRUE)
(wgtmat = fwgtmat(w,g))
```

getAccrualDurationFromN *Accrual duration to enroll target number of subjects*

Description

Obtains the accrual duration to enroll the target number of subjects.

Usage

```
getAccrualDurationFromN(
  nsubjects = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_
)
```

Arguments

nsubjects	The vector of target number of subjects.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.

Value

A vector of accrual durations.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getAccrualDurationFromN(nsubjects = c(20, 150), accrualTime = c(0, 3),
                        accrualIntensity = c(10, 20))
```

---

getADCI *Confidence interval after adaptation*

Description

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of an adaptive trial.

Usage

```
getADCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.25,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
```

```
  MullerSchafer = 0L,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_
)
```

Arguments

L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.
L2	The termination look of the secondary trial.
zL2	The z-test statistic at the termination look of the secondary trial.
INew	The maximum information of the secondary trial.
MullerSchafer	Whether to use the Muller and Schafer (2001) method for trial adaptation.
informationRatesNew	The spacing of looks of the secondary trial up to look L2.
efficacyStoppingNew	The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

typeAlphaSpendingNew
: The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew
: The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew
: The error spending time of the secondary trial up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

Value

A data frame with the following variables:

- pvalue: p-value for rejecting the null hypothesis.
- thetahat: Median unbiased point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of confidence interval.
- upper: Upper bound of confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Ping Gao, Lingyun Liu and Cyrus Mehta. Exact inference for adaptive group sequential designs. Stat Med. 2013;32(23):3991-4005.

See Also

adaptDesign

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
```

```
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
 (des2 = adaptDesign(
   INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
   kMax = 3, informationRates = t,
   alpha = 0.05, typeAlphaSpending = "sfHSD",
   parameterAlphaSpending = -4,
   MullerSchafer = TRUE,
   kNew = 3, informationRatesNew = ns/n2,
   typeAlphaSpendingNew = "sfHSD",
   parameterAlphaSpendingNew = -2))

# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# confidence interval
getADCI(L = L, zL = zL,
        IMax = n/(4*sigma1^2), kMax = 3,
        informationRates = t,
        alpha = 0.05, typeAlphaSpending = "sfHSD",
        parameterAlphaSpending = -4,
        L2 = L2, zL2 = zL2,
        INew = n2/(4*sigma2^2),
        MullerSchafer = TRUE,
        informationRatesNew = t2,
        typeAlphaSpendingNew = "sfHSD",
        parameterAlphaSpendingNew = -2)
```

getADRCI *Repeated confidence interval after adaptation*

Description

Obtains the repeated p-value, conservative point estimate, and repeated confidence interval for an adaptive group sequential trial.

Usage

```
getADRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
  MullerSchafer = 0L,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_
)
```

Arguments

L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

alpha The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending
The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.

L2 The look of interest in the secondary trial.

zL2 The z-test statistic at the look of the secondary trial.

INew The maximum information of the secondary trial.

MullerSchafer Whether to use the Muller and Schafer (2001) method for trial adaptation.

informationRatesNew
The spacing of looks of the secondary trial.

efficacyStoppingNew
The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

typeAlphaSpendingNew
The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew
The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew
The error spending time of the secondary trial. up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

Value

A data frame with the following variables:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetahat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Cyrus R. Mehta, Peter Bauer, Martin Posch and Werner Brannath. Repeated confidence intervals for adaptive group sequential trials. Stat Med. 2007;26:5422–5433.

See Also

adaptDesign

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
(des2 = adaptDesign(
  INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, informationRatesNew = ns/n2,
  typeAlphaSpendingNew = "sfHSD",
```

```
  parameterAlphaSpendingNew = -2))

# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# repeated confidence interval
getADRCI(L = L, zL = zL,
         IMax = n/(4*sigma1^2), kMax = 3,
         informationRates = t,
         alpha = 0.05, typeAlphaSpending = "sfHSD",
         parameterAlphaSpending = -4,
         L2 = L2, zL2 = zL2,
         INew = n2/(4*sigma2^2),
         MullerSchafer = TRUE,
         informationRatesNew = t2,
         typeAlphaSpendingNew = "sfHSD",
         parameterAlphaSpendingNew = -2)
```

---

getBound *Efficacy boundaries for group sequential design*

Description

Obtains the efficacy stopping boundaries for a group sequential design.

Usage

```
getBound(
  k = NA,
  informationRates = NA,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  userAlphaSpending = NA,
  spendingTime = NA,
  efficacyStopping = NA
)
```

Arguments

k	Look number for the current analysis.
informationRates	Information rates up to the current look. Must be increasing and less than or equal to 1.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length k for the error spending time at each analysis. Must be increasing and less than or equal to 1. Defaults to missing, in which case, it is the same as informationRates.

efficacyStopping
Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

Details

If typeAlphaSpending is "OF", "P", or "WT", then the boundaries will be based on equally spaced looks.

Value

A numeric vector of critical values up to the current look.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getBound(k = 2, informationRates = c(0.5,1),
         alpha = 0.025, typeAlphaSpending = "sfOF")
```

---

getCI *Confidence interval after trial termination*

Description

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of a group sequential trial.

Usage

```
getCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

L	The termination look.
zL	The z-test statistic at the termination look.
IMax	The maximum information of the trial.
informationRates	The information rates up to look L.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

Value

A data frame with the following components:

- pvalue: p-value for rejecting the null hypothesis.
- thetahat: Median unbiased point estimate of the parameter.

- `cilevel`: Confidence interval level.
- `lower`: Lower bound of confidence interval.
- `upper`: Upper bound of confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Anastasios A. Tsiatis, Gary L. Rosner and Cyrus R. Mehta. Exact confidence intervals following a group sequential test. Biometrics 1984;40:797-803.

Examples

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# crossed the boundary at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

# confidence interval
getCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
      informationRates = c(1/3, 2/3), alpha = 0.05,
      typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

---

getCP *Conditional power allowing for varying parameter values*

Description

Obtains the conditional power for specified incremental information given the interim results, parameter values, and data-dependent changes in the error spending function, as well as the number and spacing of interim looks.

Usage

```
getCP(
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  spendingTime = NA_real_,
  MullerSchafer = 0L,
  kNew = NA_integer_,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  futilityStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  typeBetaSpendingNew = "none",
  parameterBetaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_,
  varianceRatio = 1
)
```

Arguments

INew	The maximum information of the secondary trial.
L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
theta	A scalar or a vector of parameter values of length kMax + kMax - L if MullerSchafer = FALSE or length kMax + kNew if MullerSchafer = TRUE.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

futilityStopping
: Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

criticalValues
: The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

alpha
: The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.

futilityBounds
: The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to `rep(-6, kMax-1)` if left unspecified.

typeBetaSpending
: The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTime
: The error spending time of the primary trial. Defaults to missing, in which case, it is the same as `informationRates`.

MullerSchafer
: Whether to use the Muller and Schafer (2001) method for trial adaptation.

kNew
: The number of looks of the secondary trial.

informationRatesNew
: The spacing of looks of the secondary trial.

efficacyStoppingNew
: The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

futilityStoppingNew
: The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

typeAlphaSpendingNew
: The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang &

Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpendingNew`
: The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`typeBetaSpendingNew`
: The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpendingNew`
: The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`spendingTimeNew`
: The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as `informationRatesNew`.

`varianceRatio` The ratio of the variance under H0 to the variance under H1.

Value

The conditional power given the interim results, parameter values, and data-dependent design changes.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Cyrus R. Mehta and Stuart J. Pocock. Adaptive increase in sample size when interim results are promising: A practical guide with examples. Stat Med. 2011;30:3267–3284.

See Also

`getDesign`

Examples

```
# Conditional power calculation with delayed treatment effect

# Two interim analyses have occurred with 179 and 266 events,
# respectively. The observed hazard ratio at the second interim
# look is 0.81.

trialsdt = as.Date("2020-03-04")                    # trial start date
```

```
iadt = c(as.Date("2022-02-01"), as.Date("2022-11-01")) # interim dates
mo1 = as.numeric(iadt - trialsdt + 1)/30.4375          # interim months

# Assume a piecewise Poisson enrollment process with a 8-month ramp-up
# and 521 patients were enrolled after 17.94 months
N = 521                   # total number of patients
Ta = 17.94                # enrollment duration
Ta1 = 8                   # assumed end of enrollment ramp-up
enrate = N / (Ta - Ta1/2) # enrollment rate after ramp-up

# Assume a median survival of 16.7 months for the control group, a
# 5-month delay in treatment effect, and a hazard ratio of 0.7 after
# the delay
lam1 = log(2)/16.7  # control group hazard of exponential distribution
t1 = 5              # months of delay in treatment effect
hr = 0.7            # hazard ratio after delay
lam2 = hr*lam1      # treatment group hazard after delay

# Assume an annual dropout rate of 5%
gam = -log(1-0.05)/12  # hazard for dropout

# The original target number of events was 298 and the new target is 335
mo2 <- caltime(
  nevents = c(298, 335),
  allocationRatioPlanned = 1,
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000)

# expected number of events and average hazard ratios
(lr1 <- lrstat(
  time = c(mo1, mo2),
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000,
  predictTarget = 3))


hr2 = 0.81                    # observed hazard ratio at interim 2
z2 = (-log(hr2))*sqrt(266/4)  # corresponding z-test statistic value
```

```
# expected mean of -log(HR) at the original looks and the new final look
theta = -log(lr1$HR[c(1,2,3,4)])

# conditional power with sample size increase
getCP(INew = (335 - 266)/4,
      L = 2, zL = z2, theta = theta,
      IMax = 298/4, kMax = 3,
      informationRates = c(179, 266, 298)/298,
      alpha = 0.025, typeAlphaSpending = "sfOF")
```

`getDesign` *Power and sample size for a generic group sequential design*

Description

Obtains the maximum information and stopping boundaries for a generic group sequential design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

Usage

```
getDesign(
  beta = NA_real_,
  IMax = NA_real_,
  theta = NA_real_,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  varianceRatio = 1
)
```

Arguments

`beta`	The type II error.
`IMax`	The maximum information. Either `beta` or `IMax` should be provided while the other one should be missing.

theta The parameter value.

kMax The maximum number of stages.

informationRates
The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping
Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping
Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

varianceRatio The ratio of the variance under H0 to the variance under H1. Defaults to 1.

Value

An S3 class design object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyTheta: The efficacy boundaries on the parameter scale.
  - futilityTheta: The futility boundaries on the parameter scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or IMax.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Christopher Jennison, Bruce W. Turnbull. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall/CRC: Boca Raton, 2000, ISBN:0849303168

Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesign(
  beta = 0.2, theta = -log(0.7),
  kMax = 2, informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: obtain power given the maximum information
(design2 <- getDesign(
  IMax = 72.5, theta = -log(0.7),
  kMax = 3, informationRates = c(0.5, 0.75, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))
```

---

getDesignAgreement *Power and sample size for Cohen's kappa*

Description

Obtains the power given sample size or obtains the sample size given power for Cohen's kappa.

Usage

```
getDesignAgreement(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  kappaH0 = NA_real_,
  kappa = NA_real_,
  p1 = NA_real_,
  p2 = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories.
kappaH0	The kappa coefficient under the null hypothesis.
kappa	The kappa coefficient under the alternative hypothesis.
p1	The marginal probabilities for the first rater.
p2	The marginal probabilities for the second rater. Defaults to be equal to the marginal probabilities for the first rater if not provided.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

The kappa coefficient is defined as

$$\kappa = \frac{\pi_o - \pi_e}{1 - \pi_e},$$

where $\pi_o = \sum_i \pi_{ii}$ is the observed agreement, and $\pi_e = \sum_i \pi_{i.}\pi_{.i}$ is the expected agreement by chance.

By Fleiss et al. (1969), the variance of $\hat{\kappa}$ is given by

$$Var(\hat{\kappa}) = \frac{v_1}{n},$$

where

$$v_1 = \frac{Q_1 + Q_2 - Q3 - Q4}{(1 - \pi_e)^4},$$

$$Q_1 = \pi_o(1 - \pi_e)^2,$$

$$Q_2 = (1 - \pi_o)^2 \sum_i \sum_j \pi_{ij}(\pi_{i.} + \pi_{.j})^2,$$

$$Q_3 = 2(1 - \pi_o)(1 - \pi_e) \sum_i \pi_{ii}(\pi_{i.} + \pi_{.i}),$$

$$Q_4 = (\pi_o\pi_e - 2\pi_e + \pi_o)^2.$$

Given κ and marginals $\{(\pi_{i.}, \pi_{.i}) : i = 1, \ldots, k\}$, we obtain π_o. The only unknowns are the double summation in Q_2 and the single summation in Q_3.

We find the optimal configuration of cell probabilities that yield the maximum variance of $\hat{\kappa}$ by treating the problem as a linear programming problem with constraints to match the given marginal probabilities and the observed agreement and ensure that the cell probabilities are nonnegative. This is an extension of Flack et al. (1988) by allowing unequal marginal probabilities of the two raters.

We perform the optimization under both the null and alternative hypotheses to obtain $\max Var(\hat{\kappa}|\kappa = \kappa_0)$ and $\max Var(\hat{\kappa}|\kappa = \kappa_1)$ for a single subject, and then calculate the sample size or power according to the following equation:

$$\sqrt{n}|\kappa - \kappa_0| = z_{1-\alpha}\sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_0)} + z_{1-\beta}\sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_1)}.$$

Value

An S3 class designAgreement object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The one-sided significance level.
- n: The total sample size.
- ncats: The number of categories.
- kappaH0: The kappa coefficient under the null hypothesis.
- kappa: The kappa coefficient under the alternative hypothesis.
- p1: The marginal probabilities for the first rater.
- p2: The marginal probabilities for the second rater.
- piH0: The cell probabilities that maximize the variance of estimated kappa under H0.
- pi: The cell probabilities that maximize the variance of estimated kappa under H1.
- calculationTarget: The calculation target, beta or n.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

V. F. Flack, A. A. Afifi, and P. A. Lachenbruch. Sample size determinations for the two rater kappa statistic. Psychometrika 1988; 53:321-325.

Examples

```
(design1 <- getDesignAgreement(
  beta = 0.2, n = NA, ncats = 4, kappaH0 = 0.4, kappa = 0.6,
  p1 = c(0.1, 0.2, 0.3, 0.4), p2 = c(0.15, 0.2, 0.24, 0.41),
  rounding = TRUE, alpha = 0.05))
```

---

getDesignANOVA *Power and sample size for one-way ANOVA*

Description

Obtains the power and sample size for one-way analysis of variance.

Usage

```
getDesignANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.
allocationRatioPlanned	Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

Let $\{\mu_i : i = 1, \ldots, k\}$ denote the group means, and $\{r_i : i = 1, \ldots, k\}$ denote the randomization probabilities to the k treatment groups. Let σ denote the common standard deviation, and n denote the total sample size. Then the F-statistic

$$F = \frac{SSR/(k-1)}{SSE/(n-k)} \sim F_{k-1,n-k,\lambda},$$

where

$$\lambda = n \sum_{i=1}^{k} r_i(\mu_i - \bar{\mu})^2/\sigma^2$$

is the noncentrality parameter, and $\bar{\mu} = \sum_{i=1}^{k} r_i\mu_i$.

Value

An S3 class designANOVA object with the following components:

- power: The power to reject the null hypothesis that there is no difference among the treatment groups.

- alpha: The two-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- effectsize: The effect size.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.05))
```

---

getDesignANOVAContrast

Power and sample size for one-way ANOVA contrast

Description

Obtains the power and sample size for a single contrast in one-way analysis of variance.

Usage

```
getDesignANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  contrast = NA_real_,
  meanContrastH0 = 0,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
allocationRatioPlanned	Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Value

An S3 class designANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.
- alpha: The one-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, contrast = c(1, 1, 1, -3)/3,
  allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.025))
```

getDesignEquiv *Power and sample size for a generic group sequential equivalence design*

Description

Obtains the maximum information and stopping boundaries for a generic group sequential equivalence design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

Usage

```
getDesignEquiv(
  beta = NA_real_,
  IMax = NA_real_,
  thetaLower = NA_real_,
  thetaUpper = NA_real_,
  theta = 0,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  varianceRatioH10 = 1,
  varianceRatioH20 = 1,
  varianceRatioH12 = 1,
  varianceRatioH21 = 1
)
```

Arguments

beta	The type II error.
IMax	The maximum information. Either beta or IMax should be provided while the other one should be missing.
thetaLower	The parameter value at the lower equivalence limit.
thetaUpper	The parameter value at the upper equivalence limit.
theta	The parameter value under the alternative hypothesis.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.

`alpha` The significance level for each of the two one-sided tests. Defaults to 0.05.

`typeAlphaSpending`
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
The user defined alpha spending. Cumulative alpha spent up to each stage.

`spendingTime` A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

`varianceRatioH10`
The ratio of the variance under H10 to the variance under H1. Defaults to 1.

`varianceRatioH20`
The ratio of the variance under H20 to the variance under H1. Defaults to 1.

`varianceRatioH12`
The ratio of the variance under H10 to the variance under H20. Defaults to 1.

`varianceRatioH21`
The ratio of the variance under H20 to the variance under H10. Defaults to 1.

Details

Consider the equivalence design with two one-sided hypotheses:

$$H_{10} : \theta \leq \theta_{10},$$

$$H_{20} : \theta \geq \theta_{20}.$$

We reject H_{10} at or before look k if

$$Z_{1j} = (\hat{\theta}_j - \theta_{10})\sqrt{\frac{n_j}{v_{10}}} \geq b_j$$

for some $j = 1, \ldots, k$, where $\{b_j : j = 1, \ldots, K\}$ are the critical values associated with the specified alpha-spending function, and v_{10} is the null variance of $\hat{\theta}$ based on the restricted maximum likelihood (reml) estimate of model parameters subject to the constraint imposed by H_{10} for one sampling unit drawn from H_1. For example, for estimating the risk difference $\theta = \pi_1 - \pi_2$, the asymptotic limits of the reml estimates of π_1 and π_2 subject to the constraint imposed by H_{10} are given by

$$(\tilde{\pi}_1, \tilde{\pi}_2) = f(\theta_{10}, r, r\pi_1, 1 - r, (1 - r)\pi_2),$$

where $f(\theta_0, n_1, y_1, n_2, y_2)$ is the function to obtain the reml of π_1 and π_2 subject to the constraint that $\pi_1 - \pi_2 = \theta_0$ with observed data (n_1, y_1, n_2, y_2) for the number of subjects and number of responses in the active treatment and control groups, r is the randomization probability for the active treatment group, and

$$v_{10} = \frac{\tilde{\pi}_1(1 - \tilde{\pi}_1)}{r} + \frac{\tilde{\pi}_2(1 - \tilde{\pi}_2)}{1 - r}.$$

Let $I_j = n_j/v_1$ denote the information for θ at the jth look, where

$$v_1 = \frac{\pi_1(1-\pi_1)}{r} + \frac{\pi_2(1-\pi_2)}{1-r}$$

denotes the variance of $\hat{\theta}$ under H_1 for one sampling unit. It follows that

$$(Z_{1j} \geq b_j) = (Z_j \geq w_{10} b_j + (\theta_{10} - \theta)\sqrt{I_j}),$$

where $Z_j = (\hat{\theta}_j - \theta)\sqrt{I_j}$, and $w_{10} = \sqrt{v_{10}/v_1}$.

Similarly, we reject H_{20} at or before look k if

$$Z_{2j} = (\hat{\theta}_j - \theta_{20})\sqrt{\frac{n_j}{v_{20}}} \leq -b_j$$

for some $j = 1, \ldots, k$, where v_{20} is the null variance of $\hat{\theta}$ based on the reml estimate of model parameters subject to the constraint imposed by H_{20} for one sampling unit drawn from H_1. We have

$$(Z_{2j} \leq -b_j) = (Z_j \leq -w_{20} b_j + (\theta_{20} - \theta)\sqrt{I_j}),$$

where $w_{20} = \sqrt{v_{20}/v_1}$.

Let $l_j = w_{10} b_j + (\theta_{10} - \theta)\sqrt{I_j}$, and $u_j = -w_{20} b_j + (\theta_{20} - \theta)\sqrt{I_j}$. The cumulative probability to reject $H_0 = H_{10} \cup H_{20}$ at or before look k under the alternative hypothesis H_1 is given by

$$P_\theta\left(\cup_{j=1}^k (Z_{1j} \geq b_j) \cap \cup_{j=1}^k (Z_{2j} \leq -b_j)\right) = p_1 + p_2 + p_{12},$$

where

$$p_1 = P_\theta\left(\cup_{j=1}^k (Z_{1j} \geq b_j)\right) = P_\theta\left(\cup_{j=1}^k (Z_j \geq l_j)\right),$$
$$p_2 = P_\theta\left(\cup_{j=1}^k (Z_{2j} \leq -b_j)\right) = P_\theta\left(\cup_{j=1}^k (Z_j \leq u_j)\right),$$

and

$$p_{12} = P_\theta\left(\cup_{j=1}^k \{(Z_j \geq l_j) \cup (Z_j \leq u_j)\}\right).$$

Of note, both p_1 and p_2 can be evaluated using one-sided exit probabilities for group sequential designs. If there exists $j \leq k$ such that $l_j \leq u_j$, then $p_{12} = 1$. Otherwise, p_{12} can be evaluated using two-sided exit probabilities for group sequential designs.

To evaluate the type I error of the equivalence trial under H_{10}, we first match the information under H_{10} with the information under H_1. For example, for estimating the risk difference for two independent samples, the sample size n_{10} under H_{10} must satisfy

$$\frac{1}{n_{10}}\left(\frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1-\pi_2)}{1-r}\right) = \frac{1}{n}\left(\frac{\pi_1(1-\pi_1)}{r} + \frac{\pi_2(1-\pi_2)}{1-r}\right).$$

Then we obtain the reml estimates of π_1 and π_2 subject to the constraint imposed by H_{20} for one sampling unit drawn from H_{10},

$$(\tilde{\pi}_{10}, \tilde{\pi}_{20}) = f(\theta_{20}, r, r(\pi_2 + \theta_{10}), 1 - r, (1-r)\pi_2).$$

Let t_j denote the information fraction at look j. Define

$$\tilde{v}_1 = \frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1-\pi_2)}{1-r},$$

and

$$\tilde{v}_{20} = \frac{\tilde{\pi}_{10}(1-\tilde{\pi}_{10})}{r} + \frac{\tilde{\pi}_{20}(1-\tilde{\pi}_{20})}{1-r}.$$

The cumulative rejection probability under H_{10} at or before look k is given by

$$P_{\theta_{10}}\left(\cup_{j=1}^{k}\{(\hat{\theta}_j-\theta_{10})\sqrt{n_{10}t_j/\tilde{v}_1}\geq b_j\}\cap\cup_{j=1}^{k}\{(\hat{\theta}_j-\theta_{20})\sqrt{n_{10}t_j/\tilde{v}_{20}}\leq -b_j\}\right) = q_1+q_2+q_{12},$$

where

$$q_1 = P_{\theta_{10}}\left(\cup_{j=1}^{k}\{(\hat{\theta}_j-\theta_{10})\sqrt{n_{10}t_j/\tilde{v}_1}\geq b_j\}\right) = P_{\theta_{10}}\left(\cup_{j=1}^{k}(Z_j\geq b_j)\right),$$

$$q_2 = P_{\theta_{10}}\left(\cup_{j=1}^{k}\{(\hat{\theta}_j-\theta_{20})\sqrt{n_{10}t_j/\tilde{v}_{20}}\leq -b_j\}\right) = P_{\theta_{10}}\left(\cup_{j=1}^{k}(Z_j\leq -b_jw_{21}+(\theta_{20}-\theta_{10})\sqrt{I_j})\right),$$

and

$$q_{12} = P_{\theta_{10}}\left(\cup_{j=1}^{k}\{(Z_j\geq b_j)\cup(Z_j\leq -w_{21}b_j+(\theta_{20}-\theta_{10})\sqrt{I_j})\}\right).$$

Here $Z_j = (\hat{\theta}_j-\theta_{10})\sqrt{I_j}$, and $w_{21} = \sqrt{\tilde{v}_{20}/\tilde{v}_1}$. Of note, q_1, q_2, and q_{12} can be evaluated using group sequential exit probabilities. Similarly, we can define $\tilde{v}_2$, $\tilde{v}_{10}$, and $w_{12} = \sqrt{\tilde{v}_{10}/\tilde{v}_2}$, and evaluate the type I error under H_{20}.

The variance ratios correspond to

$$\text{varianceRatioH10} = v_{10}/v_1,$$

$$\text{varianceRatioH20} = v_{20}/v_1,$$

$$\text{varianceRatioH12} = \tilde{v}_{10}/\tilde{v}_2,$$

$$\text{varianceRatioH21} = \tilde{v}_{20}/\tilde{v}_1.$$

If the alternative variance is used, then the variance ratios are all equal to 1.

Value

An S3 class `designEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `kMax`: The number of stages.
  - `thetaLower`: The parameter value at the lower equivalence limit.
  - `thetaUpper`: The parameter value at the upper equivalence limit.
  - `theta`: The parameter value under the alternative hypothesis.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH10`: The expected information under H10.

  - expectedInformationH20: The expected information under H20.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative probability for efficacy stopping under H10.
  - cumulativeAttainedAlphaH20: The cumulative probability for efficacy stopping under H20.
  - efficacyThetaLower: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyThetaUpper: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following components:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - calculationTarget: The calculation target, beta or IMax.

Author(s)

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Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesignEquiv(
  beta = 0.2, thetaLower = log(0.8), thetaUpper = log(1.25),
  kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))


# Example 2: obtain power given the maximum information
(design2 <- getDesignEquiv(
  IMax = 72.5, thetaLower = log(0.7), thetaUpper = -log(0.7),
```

```
  kMax = 3, informationRates = c(0.5, 0.75, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))
```

`getDesignFisherExact` *Power and sample size for Fisher's exact test for two proportions*

Description

Obtains the power given sample size or obtains the sample size given power for Fisher's exact test for two proportions.

Usage

```
getDesignFisherExact(
  beta = NA_real_,
  n = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`pi1`	The assumed probability for the active treatment group.
`pi2`	The assumed probability for the control group.
`allocationRatioPlanned`	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
`alpha`	The two-sided significance level. Defaults to 0.05.

Value

A data frame with the following variables:

- `alpha`: The two-sided significance level.
- `power`: The power.
- `n`: The sample size.
- `pi1`: The assumed probability for the active treatment group.
- `pi2`: The assumed probability for the control group.
- `calculationTarget`: The calculation target, `beta` or `n`.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignFisherExact(
  beta = 0.2, pi1 = 0.5, pi2 = 0.2, alpha = 0.05))
```

---

getDesignLogistic *Power and sample size for logistic regression*

Description

Obtains the power given sample size or obtains the sample size given power for logistic regression of a binary response given the covariate of interest and other covariates.

Usage

```
getDesignLogistic(
  beta = NA_real_,
  n = NA_real_,
  ncovariates = NA_integer_,
  nconfigs = NA_integer_,
  x = NA_real_,
  pconfigs = NA_real_,
  corr = 0,
  oddsratios = NA_real_,
  responseprob = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncovariates	The number of covariates.
nconfigs	The number of configurations of discretized covariate values.
x	The matrix of covariate values.
pconfigs	The vector of probabilities for the configurations.
corr	The multiple correlation between the predictor and other covariates. Defaults to 0.
oddsratios	The odds ratios for one unit increase in the covariates.

responseprob	The response probability in the full model when all predictor variables are equal to their means.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

We consider the logistic regression of a binary response variable Y on a set of predictor variables $x = (x_1, \ldots, x_K)^T$ with x_1 being the covariate of interest: $\log \frac{P(Y_i=1)}{1-P(Y_i=1)} = \psi_0 + x_i^T \psi$, where $\psi = (\psi_1, \ldots, \psi_K)^T$. Similar to Self et al (1992), we assume that all covariates are either inherently discrete or discretized from continuous distributions (e.g. using the quantiles). Let m denote the total number of configurations of the covariate values. Let

$$\pi_i = P(x = x_i), i = 1, \ldots, m$$

denote the probabilities for the configurations of the covariates under independence. The likelihood ratio test statistic for testing $H_0 : \psi_1 = 0$ can be approximated by a noncentral chi-square distribution with one degree of freedom and noncentrality parameter

$$\Delta = 2 \sum_{i=1}^{m} \pi_i [b'(\theta_i)(\theta_i - \theta_i^*) - \{b(\theta_i) - b(\theta_i^*)\}],$$

where

$$\theta_i = \psi_0 + \sum_{j=1}^{k} \psi_j x_{ij},$$

$$\theta_i^* = \psi_0^* + \sum_{j=2}^{k} \psi_j^* x_{ij},$$

for $\psi_0^* = \psi_0 + \psi_1 \mu_1$, and $\psi_j^* = \psi_j$ for $j = 2, \ldots, K$. Here μ_1 is the mean of x_1, e.g., $\mu_1 = \sum_i \pi_i x_{i1}$. In addition, by formulating the logistic regression in the framework of generalized linear models,

$$b(\theta) = \log(1 + \exp(\theta)),$$

and

$$b'(\theta) = \frac{\exp(\theta)}{1 + \exp(\theta)}.$$

The regression coefficients ψ can be obtained by taking the log of the odds ratios for the covariates. The intercept ψ_0 can be derived as

$$\psi_0 = \log(\bar{\mu}/(1 - \bar{\mu})) - \sum_{j=1}^{K} \psi_j \mu_j,$$

where $\bar{\mu}$ denotes the response probability when all predictor variables are equal to their means.

Finally, let ρ denote the multiple correlation between the predictor and other covariates. The noncentrality parameter of the chi-square test is adjusted downward by multiplying by $1 - \rho^2$.

Value

An S3 class `designLogistic` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The total sample size.
- `ncovariates`: The number of covariates.
- `nconfigs`: The number of configurations of discretized covariate values.
- `x`: The matrix of covariate values.
- `pconfigs`: The vector of probabilities for the configurations.
- `corr`: The multiple correlation between the predictor and other covariates.
- `oddsratios`: The odds ratios for one unit increase in the covariates.
- `responseprob`: The response probability in the full model when all predictor variables are equal to their means.
- `effectsize`: The effect size for the chi-square test.
- `calculationTarget`: The calculation target, `beta` or `n`.
- `rounding`: Whether to round up sample size.

Author(s)

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References

Steven G. Self, Robert H. Mauritsen and Jill Ohara. Power calculations for likelihood ratio tests in generalized linear models. Biometrics 1992; 48:31-39.

Examples

```
# two ordinal covariates
x1 = c(5, 10, 15, 20)
px1 = c(0.2, 0.3, 0.3, 0.2)

x2 = c(2, 4, 6)
px2 = c(0.4, 0.4, 0.2)

# discretizing a normal distribution with mean 4 and standard deviation 2
nbins = 10
x3 = qnorm(((1:nbins) - 0.5)/nbins)*2 + 4
px3 = rep(1/nbins, nbins)

# combination of covariate values
nconfigs = length(x1)*length(x2)*length(x3)
x = expand.grid(x3 = x3, x2 = x2, x1 = x1)
x = as.matrix(x[, ncol(x):1])
```

```
# probabilities for the covariate configurations under independence
pconfigs = as.numeric(px1 %x% px2 %x% px3)

# convert the odds ratio for the predictor variable in 5-unit change
# to the odds ratio in 1-unit change
(design1 <- getDesignLogistic(
  beta = 0.1, ncovariates = 3,
  nconfigs = nconfigs,
  x = x,
  pconfigs = pconfigs,
  oddsratios = c(1.2^(1/5), 1.4, 1.3),
  responseprob = 0.25,
  alpha = 0.1))
```

`getDesignMeanDiff` *Group sequential design for two-sample mean difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference.

Usage

```
getDesignMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for

Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpending`
: The user defined beta spending. Cumulative beta spent up to each stage.

`spendingTime`
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designMeanDiff` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanDiffH0`: The mean difference under the null hypothesis.
  - `meanDiff`: The mean difference under the alternative hypothesis.
  - `stDev`: The standard deviation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.

  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - futilityMeanDiff: The futility boundaries on the mean difference scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

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Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiff(
  beta = NA, n = 456, meanDiff = 9, stDev = 32,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for two-sample t-test
(design2 <- getDesignMeanDiff(
  beta = 0.1, n = NA, meanDiff = 0.3, stDev = 1,
  normalApproximation = FALSE, alpha = 0.025))
```

`getDesignMeanDiffCarryover` *Power and sample size for direct treatment effects in crossover trials accounting for carryover effects*

Description

Obtains the power and sample size for direct treatment effects in crossover trials accounting for carryover effects.

Usage

```
getDesignMeanDiffCarryover(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  corr = 0.5,
  design = NA_real_,
  cumdrop = NA_real_,
  allocationRatioPlanned = NA_real_,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanDiffH0`	The mean difference at the last time point under the null hypothesis. Defaults to 0.
`meanDiff`	The mean difference at the last time point under the alternative hypothesis.
`stDev`	The standard deviation for within-subject random error.
`corr`	The intra-subject correlation due to subject random effect.
`design`	The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
`cumdrop`	The cumulative dropout rate over periods.
`allocationRatioPlanned`	Allocation ratio for the sequences. Defaults to equal randomization if not provided.
`normalApproximation`	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.

rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

The linear mixed-effects model to assess the direct treatment effect in the presence of carryover treatment effect is given by

$$y_{ijk} = \mu + \alpha_i + b_{ij} + \gamma_k + \tau_{d(i,k)} + \lambda_{c(i,k-1)} + e_{ijk},$$

$$i = 1, \ldots, n; j = 1, \ldots, r_i; k = 1, \ldots, p; d, c = 1, \ldots, t,$$

where μ is the general mean, α_i is the effect of the ith treatment sequence, b_{ij} is the random effect with variance σ_b^2 for the $j$the subject of the ith treatment sequence, γ_k is the period effect, and e_{ijk} is the random error with variance σ^2 for the subject in period k. The direct effect of the treatment administered in period k of sequence i is $\tau_{d(i,k)}$, and $\lambda_{c(i,k-1)}$ is the carryover effect of the treatment administered in period $k-1$ of sequence i. The value of the carryover effect for the observed response in the first period is $\lambda_{c(i,0)} = 0$ since there is no carryover effect in the first period. The intra-subject correlation due to the subject random effect is

$$\rho = \frac{\sigma_b^2}{\sigma_b^2 + sigma^2}.$$

By constructing the design matrix X for the linear model with a compound symmetry covariance matrix for the response vector of a subject, we can obtain

$$Var(\hat{\beta}) = (X'V^{-1}X)^{-1}.$$

The covariance matrix for the direct treatment effects and the carryover treatment effects can be extracted from the appropriate sub-matrices. The covariance matrix for the direct treatment effects without accounting for the carryover treatment effects can be obtained by omitting the carryover effect terms from the model.

The power and relative efficiency are for the direct treatment effect comparing the first treatment to the last treatment accounting for carryover effects.

The degrees of freedom for the t-test can be calculated as the total number of observations minus the number of subjects minus $p-1$ minus $2(t-1)$ to account for the subject effect, period effect, and direct and carryover treatment effects.

Value

An S3 class `designMeanDiffCarryover` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `meanDiffH0`: The mean difference under the null hypothesis.
- `meanDiff`: The mean difference under the alternative hypothesis.
- `stDev`: The standard deviation for within-subject random error.

- corr: The intra-subject correlation due to subject random effect.
- design: The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
- nseq: The number of sequences.
- nprd: The number of periods.
- ntrt: The number of treatments.
- cumdrop: The cumulative dropout rate over periods.
- V_direct_only: The covariance matrix for direct treatment effects without accounting for carryover effects.
- V_direct_carry: The covariance matrix for direct and carryover treatment effects.
- v_direct_only: The variance of direct treatment effects without accounting for carryover effects.
- v_direct: The variance of direct treatment effects accounting for carryover effects.
- v_carry: The variance of carryover treatment effects.
- releff_direct: The relative efficiency of the design for estimating direct treatment effects after accounting for carryover effects with respect to that without accounting for carryover effects. This is equal to v_direct_only/v_direct.
- releff_carry: The relative efficiency of the design for estimating carryover effects. This is equal to v_direct_only/v_carry.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the sequences.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Robert O. Kuehl. Design of Experiments: Statistical Principles of Research Design and Analysis. Brooks/Cole: Pacific Grove, CA. 2000.

Examples

```
# Williams design for 4 treatments

(design1 = getDesignMeanDiffCarryover(
  beta = 0.2, n = NA,
  meanDiff = 0.5, stDev = 1,
  design = matrix(c(1, 4, 2, 3,
                    2, 1, 3, 4,
                    3, 2, 4, 1,
```

```
                  4, 3, 1, 2),
                4, 4, byrow = TRUE),
    alpha = 0.025))
```

`getDesignMeanDiffEquiv` *Group sequential design for equivalence in two-sample mean difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean difference.

Usage

```
getDesignMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanDiffLower`	The lower equivalence limit of mean difference.
`meanDiffUpper`	The upper equivalence limit of mean difference.
`meanDiff`	The mean difference under the alternative hypothesis.
`stDev`	The standard deviation.
`allocationRatioPlanned`	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation
: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding
: Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax
: The maximum number of stages.

informationRates
: The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha
: The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffLower: The lower equivalence limit of mean difference.
  - meanDiffUpper: The upper equivalence limit of mean difference.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:

  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

`getDesignMeanDiffMMRM` *Power and sample size for two-sample mean difference at the last time point from the MMRM model*

Description

Obtains the power and sample size for two-sample mean difference at the last time point from the mixed-model for repeated measures (MMRM) model.

Usage

```
getDesignMeanDiffMMRM(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  k = 1,
  covar1 = diag(k),
  covar2 = NA_real_,
  cumdrop1 = rep(0, k),
  cumdrop2 = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanDiffH0`	The mean difference at the last time point under the null hypothesis. Defaults to 0.
`meanDiff`	The mean difference at the last time point under the alternative hypothesis.
`k`	The number of postbaseline time points.
`covar1`	The covariance matrix for the repeated measures given baseline for the active treatment group.
`covar2`	The covariance matrix for the repeated measures given baseline for the control group. If missing, it will be set equal to the covariance matrix for the active treatment group.
`cumdrop1`	The cumulative dropout rate at the postbaseline time points for the active treatment group.
`cumdrop2`	The cumulative dropout rate at the postbaseline time points for the control group. If missing, it will be set equal to the cumulative dropout rate for the active treatment group.

`allocationRatioPlanned`
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

`normalApproximation`
: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution is the total effective sample size minus 2.

`rounding`
: Whether to round up sample size. Defaults to 1 for sample size rounding.

`alpha`
: The one-sided significance level. Defaults to 0.025.

Value

An S3 class `designMeanDiffMMRM` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `meanDiffH0`: The mean difference under the null hypothesis.
- `meanDiff`: The mean difference under the alternative hypothesis.
- `k`: The number of postbaseline time points.
- `covar1`: The covariance matrix for the repeated measures given baseline for the active treatment group.
- `covar2`: The covariance matrix for the repeated measures given baseline for the control group.
- `cumdrop1`: The cumulative dropout rate at the postbaseline time points for the active treatment group.
- `cumdrop2`: The cumulative dropout rate at the postbaseline time points for the control group.
- `inflation1`: The variance inflation factor for the active treatment group.
- `inflation2`: The variance inflation factor for the control group.
- `calculationTarget`: The calculation target, `beta` or `n`.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
- `normalApproximation`: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# function to generate the AR(1) correlation matrix
ar1_cor <- function(n, corr) {
  exponent <- abs(matrix(1:n - 1, n, n, byrow = TRUE) - (1:n - 1))
  corr^exponent
}

# function to generate the cumulative dropout rate
exp_drop <- function(n, dropprob) {
  1 - (1 - dropprob)^((1:n)/n)
}

(design1 <- getDesignMeanDiffMMRM(
  beta = 0.2,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  k = 4,
  covar1 = ar1_cor(4, 0.7),
  cumdrop1 = exp_drop(4, 0.10),
  allocationRatioPlanned = 1,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025))
```

---

getDesignMeanDiffXO *Group sequential design for mean difference in 2x2 crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference in 2x2 crossover.

Usage

```
getDesignMeanDiffXO(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
```

```
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.
allocationRatioPlanned	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,

Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
: The user defined alpha spending. Cumulative alpha spent up to each stage.

`futilityBounds` Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpending`
: The user defined beta spending. Cumulative beta spent up to each stage.

`spendingTime` A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designMeanDiffXO` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanDiffH0`: The mean difference under the null hypothesis.
  - `meanDiff`: The mean difference under the alternative hypothesis.
  - `stDev`: The standard deviation for within-subject random error.

- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - futilityMeanDiff: The futility boundaries on the mean difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanDiffXO(
  beta = 0.2, n = NA, meanDiff = 75, stDev = 150,
  normalApproximation = FALSE, alpha = 0.05))
```

`getDesignMeanDiffXOEquiv` *Group sequential design for equivalence in mean difference in 2x2 crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in mean difference in 2x2 crossover.

Usage

```
getDesignMeanDiffXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanDiffLower`	The lower equivalence limit of mean difference.
`meanDiffUpper`	The upper equivalence limit of mean difference.
`meanDiff`	The mean difference under the alternative hypothesis.
`stDev`	The standard deviation for within-subject random error.
`allocationRatioPlanned`	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
`normalApproximation`	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates
The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiffXOEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffLower: The lower equivalence limit of mean difference.
  - meanDiffUpper: The upper equivalence limit of mean difference.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

getDesignMeanRatio *Group sequential design for two-sample mean ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio.

Usage

```
getDesignMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to `sqrt(log(1 + CV^2))`.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation
: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding
: Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax
: The maximum number of stages.

informationRates
: The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping
: Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping
: Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues
: Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha
: The significance level. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class `designMeanRatio` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioH0`: The mean ratio under the null hypothesis.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
  - `numberOfSubjects`: The number of subjects.
  - `efficacyMeanRatio`: The efficacy boundaries on the mean ratio scale.
  - `futilityMeanRatio`: The futility boundaries on the mean ratio scale.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanRatio(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

---

getDesignMeanRatioEquiv

Group sequential design for equivalence in two-sample mean ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean ratio.

Usage

```
getDesignMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
```

```
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioLower	The lower equivalence limit of mean ratio.
meanRatioUpper	The upper equivalence limit of mean ratio.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class `designMeanRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlpha`: The attained significance level.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioLower`: The lower equivalence limit of mean ratio.
  - `meanRatioUpper`: The upper equivalence limit of mean ratio.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlpha`: The cumulative probability for efficacy stopping under H0.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `numberOfSubjects`: The number of subjects.
  - `efficacyMeanRatioLower`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - `efficacyMeanRatioUpper`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `spendingTime`: The error spending time at each analysis.
  - `calculationTarget`: The calculation target, `beta` or `n`.
  - `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
  - `normalApproximation`: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanRatioXO *Group sequential design for mean ratio in 2x2 crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio in 2x2 crossover.

Usage

```
getDesignMeanRatioXO(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
```

```
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to sqrt(log(1 + CV^2)).
allocationRatioPlanned	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanRatioXO object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioH0: The mean ratio under the null hypothesis.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.

  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
  - futilityMeanRatio: The futility boundaries on the mean ratio scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanRatioXO(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

`getDesignMeanRatioXOEquiv` *Group sequential design for equivalence in mean ratio in 2x2 crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence mean ratio in 2x2 crossover.

Usage

```
getDesignMeanRatioXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanRatioLower`	The lower equivalence limit of mean ratio.
`meanRatioUpper`	The upper equivalence limit of mean ratio.
`meanRatio`	The mean ratio under the alternative hypothesis.
`CV`	The coefficient of variation.
`allocationRatioPlanned`	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
`normalApproximation`	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates
The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioLower: The lower equivalence limit of mean ratio.
  - meanRatioUpper: The upper equivalence limit of mean ratio.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanRatioLower: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanRatioUpper: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

`getDesignOddsRatio` *Group sequential design for two-sample odds ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample odds ratio.

Usage

```
getDesignOddsRatio(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`oddsRatioH0`	The odds ratio under the null hypothesis. Defaults to 1.
`pi1`	The assumed probability for the active treatment group.
`pi2`	The assumed probability for the control group.
`nullVariance`	Whether to use the variance under the null or the empirical variance under the alternative.

`allocationRatioPlanned`
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

`rounding`
: Whether to round up sample size. Defaults to 1 for sample size rounding.

`kMax`
: The maximum number of stages.

`informationRates`
: The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

`efficacyStopping`
: Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

`futilityStopping`
: Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

`criticalValues`
: Upper boundaries on the z-test statistic scale for stopping for efficacy.

`alpha`
: The significance level. Defaults to 0.025.

`typeAlphaSpending`
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
: The user defined alpha spending. Cumulative alpha spent up to each stage.

`futilityBounds`
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpending`
: The user defined beta spending. Cumulative beta spent up to each stage.

`spendingTime`
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designOddsRatio` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `oddsRatioH0`: The odds ratio under the null hypothesis.
  - `pi1`: The assumed probability for the active treatment group.
  - `pi2`: The assumed probability for the control group.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
  - `efficacyOdddsRatio`: The efficacy boundaries on the odds ratio scale.
  - `futilityOddsRatio`: The futility boundaries on the odds ratio scale.
  - `numberOfSubjects`: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOddsRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

getDesignOddsRatioEquiv

Group sequential design for equivalence in two-sample odds ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample odds ratio.

Usage

```
getDesignOddsRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioLower = NA_real_,
  oddsRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
```

```
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
oddsRatioLower	The lower equivalence limit of odds ratio.
oddsRatioUpper	The upper equivalence limit of odds ratio.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class designOddsRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - oddsRatioLower: The lower equivalence limit of odds ratio.
  - oddsRatioUpper: The upper equivalence limit of odds ratio.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyOddsRatioLower: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyOddsRatioUpper: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.

- `calculationTarget`: The calculation target, `beta` or `n`.
- `nullVariance`: Whether to use the variance under the null or the empirical variance under the alternative.
- `varianceRatioH10`: The ratio of the variance under H10 to the variance under H1.
- `varianceRatioH20`: The ratio of the variance under H20 to the variance under H1.
- `varianceRatioH12`: The ratio of the variance under H10 to the variance under H20.
- `varianceRatioH21`: The ratio of the variance under H20 to the variance under H10.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
- `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOddsRatioEquiv(
  beta = 0.2, n = NA, oddsRatioLower = 0.8,
  oddsRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignOneMean *Group sequential design for one-sample mean*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample mean.

Usage

```
getDesignOneMean(
  beta = NA_real_,
  n = NA_real_,
  meanH0 = 0,
  mean = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
```

```
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanH0	The mean under the null hypothesis. Defaults to 0.
mean	The mean under the alternative hypothesis.
stDev	The standard deviation.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneMean object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanH0: The mean under the null hypothesis.
  - mean: The mean under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.

  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMean: The efficacy boundaries on the mean scale.
  - futilityMean: The futility boundaries on the mean scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignOneMean(
```

```
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  normalApproximation = FALSE, alpha = 0.025))
```

`getDesignOneMultinom` *Power and sample for one-sample multinomial response*

Description

Obtains the power given sample size or obtains the sample size given power for one-sample multinomial response.

Usage

```
getDesignOneMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  piH0 = NA_real_,
  pi = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`ncats`	The number of categories of the multinomial response.
`piH0`	The prevalence of each category under the null hypothesis. Only need to provide the values for the first `ncats-1` categories.
`pi`	The prevalence of each category. Only need to provide the values for the first `ncats-1` categories.
`rounding`	Whether to round up sample size. Defaults to 1 for sample size rounding.
`alpha`	The two-sided significance level. Defaults to 0.05.

Value

An S3 class `designOneMultinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ncats`: The number of categories of the multinomial response.
- `piH0`: The prevalence of each category under the null hypothesis.

- pi: The prevalence of each category.
- effectsize: The effect size for the chi-square test.
- calculationTarget: The calculation target, beta or n.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOneMultinom(
  beta = 0.1, ncats = 3, piH0 = c(0.25, 0.25),
  pi = c(0.3, 0.4), alpha = 0.05))
```

---

getDesignOneProportion

Group sequential design for one-sample proportion

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample proportion.

Usage

```
getDesignOneProportion(
  beta = NA_real_,
  n = NA_real_,
  piH0 = 0.1,
  pi = 0.2,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
```

```
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
piH0	The response probability under the null hypothesis.
pi	The response probability under the alternative hypothesis.
normalApproximation	The type of computation of the p-values. If TRUE, the normal approximation will be used, otherwise the calculations are performed with the binomial distribution. The exact calculation using the binomial distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for

Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneProportion object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping as well as for the binomial exact test in a fixed design.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - piH0: The response probability under the null hypothesis.
  - pi: The response probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.

  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyResponses: The efficacy boundaries on the number of responses scale.
  - futilityResponses: The futility boundaries on the number of responses scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the binomial distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample binomial exact test
(design2 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  normalApproximation = FALSE, alpha = 0.05))
```

`getDesignOneRateExact` *Power and sample size for one-sample Poisson rate exact test*

Description

Obtains the power given sample size or obtains the sample size given power for one-sample Poisson rate.

Usage

```
getDesignOneRateExact(
  beta = NA_real_,
  n = NA_real_,
  lambdaH0 = NA_real_,
  lambda = NA_real_,
  D = 1,
  alpha = 0.025
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`lambdaH0`	The Poisson rate under the null hypothesis.
`lambda`	The Poisson rate under the alternative hypothesis.
`D`	The average exposure per subject.
`alpha`	The one-sided significance level. Defaults to 0.025.

Value

A data frame containing the following variables:

- `alpha`: The specified significance level.
- `attainedAlpha`: The attained type I error of the exact test.
- `power`: The actual power of the exact test.
- `n`: The sample size.
- `lambdaH0`: The Poisson rate under the null hypothesis.
- `lambda`: The Poisson rate under the alternative hypothesis.
- `D`: The average exposure per subject.
- `r`: The critical value of the number of events for rejecting the null hypothesis. Reject H0 if `Y >= r` for upper-tailed test, and reject H0 if `Y <= r` for lower-tailed test.
- `calculationTarget`: The calculation target, `beta` or `n`.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: power calculation
(design1 <- getDesignOneRateExact(
  n = 525, lambdaH0 = 0.049, lambda = 0.012,
  D = 0.5, alpha = 0.025))

# Example 2: sample size calculation
(design2 <- getDesignOneRateExact(
  beta = 0.2, lambdaH0 = 0.2, lambda = 0.3,
  D = 1, alpha = 0.05))
```

---

getDesignOneSlope *Group sequential design for one-sample slope*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample slope.

Usage

```
getDesignOneSlope(
  beta = NA_real_,
  n = NA_real_,
  slopeH0 = 0,
  slope = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
```

```
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
slopeH0	The slope under the null hypothesis. Defaults to 0.
slope	The slope under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneSlope object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - slopeH0: The slope under the null hypothesis.
  - slope: The slope under the alternative hypothesis.
  - stDev: The standard deviation of the residual.
  - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacySlope: The efficacy boundaries on the slope scale.
  - futilitySlope: The futility boundaries on the slope scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOneSlope(
  beta = 0.1, n = NA, slope = 0.5,
  stDev = 15, stDevCovariate = 9,
  normalApproximation = FALSE,
  alpha = 0.025))
```

getDesignOrderedBinom *Power and sample size for Cochran-Armitage trend test for ordered multi-sample binomial response*

Description

Obtains the power given sample size or obtains the sample size given power for the Cochran-Armitage trend test for ordered multi-sample binomial response.

Usage

```
getDesignOrderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  w = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
pi	The response probabilities for the treatment groups.
w	The scores assigned to the treatment groups. This should reflect the ordinal nature of the treatment groups, e.g. dose levels. Defaults to equally spaced scores.
allocationRatioPlanned	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designOrderedBinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.

- pi: The response probabilities for the treatment groups.
- w: The scores assigned to the treatment groups.
- trendstat: The Cochran-Armitage trend test statistic.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOrderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

---

getDesignPairedMeanDiff

Group sequential design for paired mean difference

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean difference.

Usage

```
getDesignPairedMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffH0 = 0,
  pairedDiff = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
```

```
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedDiffH0	The paired difference under the null hypothesis. Defaults to 0.
pairedDiff	The paired difference under the alternative hypothesis.
stDev	The standard deviation for paired difference.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffH0: The paired difference under the null hypothesis.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPairedDiff: The efficacy boundaries on the paired difference scale.
  - futilityPairedDiff: The futility boundaries on the paired difference scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  normalApproximation = FALSE, alpha = 0.025))
```

`getDesignPairedMeanDiffEquiv` *Group sequential design for equivalence in paired mean difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean difference.

Usage

```
getDesignPairedMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffLower = NA_real_,
  pairedDiffUpper = NA_real_,
  pairedDiff = 0,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`pairedDiffLower`	The lower equivalence limit of paired difference.
`pairedDiffUpper`	The upper equivalence limit of paired difference.
`pairedDiff`	The paired difference under the alternative hypothesis.
`stDev`	The standard deviation for paired difference.
`normalApproximation`	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
`rounding`	Whether to round up sample size. Defaults to 1 for sample size rounding.
`kMax`	The maximum number of stages.

informationRates
: The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha
: The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level under H0.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffLower: The lower equivalence limit of paired difference.
  - pairedDiffUpper: The upper equivalence limit of paired difference.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyPairedDiffLower: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyPairedDiffUpper: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedMeanRatio

Group sequential design for paired mean ratio

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean ratio.

Usage

```
getDesignPairedMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioH0 = 1,
  pairedRatio = 1.2,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`pairedRatioH0`	The paired ratio under the null hypothesis.
`pairedRatio`	The paired ratio under the alternative hypothesis.
`CV`	The coefficient of variation for paired ratio.
`normalApproximation`	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
`rounding`	Whether to round up sample size. Defaults to 1 for sample size rounding.
`kMax`	The maximum number of stages.
`informationRates`	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

efficacyStopping
: Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping
: Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues
: Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha
: The significance level. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.

  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedRatioH0: The paired ratio under the null hypothesis.
  - pairedRatio: The paired ratio under the alternative hypothesis.
  - CV: The coefficient of variation for paired ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - numberOfSubjects: The number of subjects.
  - efficacyPairedRatio: The efficacy boundaries on the paired ratio scale.
  - futilityPairedRatio: The futility boundaries on the paired ratio scale.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.

- calculationTarget: The calculation target, beta or n.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedMeanRatioEquiv

Group sequential design for equivalence in paired mean ratio

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean ratio.

Usage

```
getDesignPairedMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioLower = NA_real_,
  pairedRatioUpper = NA_real_,
  pairedRatio = 1,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
```

```
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedRatioLower	The lower equivalence limit of paired ratio.
pairedRatioUpper	The upper equivalence limit of paired ratio.
pairedRatio	The paired ratio under the alternative hypothesis.
CV	The coefficient of variation for paired ratio.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.

  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level under H0.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedRatioLower: The lower equivalence limit of paired ratio.
  - pairedRatioUpper: The upper equivalence limit of paired ratio.
  - pairedRatio: The paired ratio under the alternative hypothesis.
  - CV: The coefficient of variation for paired ratios.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative alpha attained under H0.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
  - efficacyPairedRatioLower: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyPairedRatioUpper: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedPropMcNemar

Group sequential design for McNemar's test for paired proportions

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for McNemar's test for paired proportions.

Usage

```
getDesignPairedPropMcNemar(
  beta = NA_real_,
  n = NA_real_,
  pDiscordant = NA_real_,
  riskDiff = NA_real_,
  nullVariance = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pDiscordant	The proportion of discordant pairs (xi = pi01 + pi10).
riskDiff	The risk difference between the active and control treatments (delta = pi_t - pi_c = pi01 - pi10)
nullVariance	Whether to use the variance under the null or the variance under the alternative.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedPropMcNemar object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pDiscordant: The proportion of discordant pairs (xi = pi01 + pi10).
  - riskDiff: The risk difference between the active and control treatments (delta = pi_t - pi_c = pi01 - pi10)
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.

  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - futilityRiskDiff: The futility boundaries on the risk difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or n.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: fixed design
(design1 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025, kMax = 3, typeAlphaSpending = "sfOF"))
```

---

getDesignRepeatedANOVA

Power and sample size for repeated-measures ANOVA

Description

Obtains the power and sample size for one-way repeated measures analysis of variance. Each subject takes all treatments in the longitudinal study.

Usage

```
getDesignRepeatedANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

Let y_{ij} denote the measurement under treatment condition $j(j = 1, \ldots, k)$ for subject $i(i = 1, \ldots, n)$. Then

$$y_{ij} = \alpha + \beta_j + b_i + e_{ij},$$

where b_i denotes the subject random effect, $b_i \sim N(0, \sigma_b^2)$, and $e_{ij} \sim N(0, \sigma_e^2)$ denotes the within-subject residual. If we set $\beta_k = 0$, then α is the mean of the last treatment (control), and β_j is the difference in mean between the jth treatment and the control for $j = 1, \ldots, k-1$.

The repeated measures have a compound symmetry covariance structure. Let $\sigma^2 = \sigma_b^2 + \sigma_e^2$, and $\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma_e^2}$. Then $Var(y_i) = \sigma^2\{(1-\rho)I_k + \rho 1_k 1_k^T\}$. Let X_i denote the design matrix for subject i. Let $\theta = (\alpha, \beta_1, \ldots, \beta_{k-1})^T$. It follows that

$$Var(\hat{\theta}) = \left(\sum_{i=1}^{n} X_i^T V_i^{-1} X_i\right)^{-1}.$$

It can be shown that

$$Var(\hat{\beta}) = \frac{\sigma^2(1-\rho)}{n}(I_{k-1} + 1_{k-1}1_{k-1}^T).$$

It follows that $\hat{\beta}^T \hat{V}_{\hat{\beta}}^{-1} \hat{\beta} \sim F_{k-1,(n-1)(k-1),\lambda}$, where the noncentrality parameter for the F distribution is

$$\lambda = \beta^T V_{\hat{\beta}}^{-1} \beta = \frac{n \sum_{j=1}^{k} (\mu_j - \bar{\mu})^2}{\sigma^2(1-\rho)}.$$

Value

An S3 class designRepeatedANOVA object with the following components:

- power: The power to reject the null hypothesis that there is no difference among the treatment groups.
- alpha: The two-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The total standard deviation.
- corr: The correlation among the repeated measures.
- effectsize: The effect size.
- calculationTarget: The calculation target, beta or n.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRepeatedANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, alpha = 0.05))
```

---

getDesignRepeatedANOVAContrast

Power and sample size for one-way repeated measures ANOVA contrast

---

Description

Obtains the power and sample size for a single contrast in one-way repeated measures analysis of variance.

Usage

```
getDesignRepeatedANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
```

```
  corr = 0,
  contrast = NA_real_,
  meanContrastH0 = 0,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Value

An S3 class designRepeatedANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.
- alpha: The one-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The total standard deviation.
- corr: The correlation among the repeated measures.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- calculationTarget: The calculation target, beta or n.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRepeatedANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, contrast = c(1, 1, 1, -3)/3,
  alpha = 0.025))
```

---

getDesignRiskDiff *Group sequential design for two-sample risk difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk difference.

Usage

```
getDesignRiskDiff(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.

`riskDiffH0` The risk difference under the null hypothesis. Defaults to 0.

`pi1` The assumed probability for the active treatment group.

`pi2` The assumed probability for the control group.

`nullVariance` Whether to use the variance under the null or the empirical variance under the alternative.

`allocationRatioPlanned`
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

`rounding` Whether to round up sample size. Defaults to 1 for sample size rounding.

`kMax` The maximum number of stages.

`informationRates`
The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

`efficacyStopping`
Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

`futilityStopping`
Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

`criticalValues` Upper boundaries on the z-test statistic scale for stopping for efficacy.

`alpha` The significance level. Defaults to 0.025.

`typeAlphaSpending`
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
The user defined alpha spending. Cumulative alpha spent up to each stage.

`futilityBounds` Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskDiffH0: The risk difference under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - futilityRiskDiff: The futility boundaries on the risk difference scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.

  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskDiff(
  beta = 0.2, n = NA, pi1 = 0.1, pi2 = 0.15,
  kMax = 3, alpha = 0.025, typeAlphaSpending = "sfOF",
  nullVariance = 0))
```

---

getDesignRiskDiffEquiv

Group sequential design for equivalence in two-sample risk difference

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk difference.

Usage

```
getDesignRiskDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,

"sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
: The user defined alpha spending. Cumulative alpha spent up to each stage.

`spendingTime`
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designRiskDiffEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH10`: The expected information under H10.
  - `expectedInformationH20`: The expected information under H20.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH10`: The expected number of subjects under H10.
  - `expectedNumberOfSubjectsH20`: The expected number of subjects under H20.
  - `riskDiffLower`: The lower equivalence limit of risk difference.
  - `riskDiffUpper`: The upper equivalence limit of risk difference.
  - `pi1`: The assumed probability for the active treatment group.
  - `pi2`: The assumed probability for the control group.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlphaH10`: The cumulative alpha attained under H10.
  - `cumulativeAttainedAlphaH20`: The cumulative alpha attained under H20.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.

  - information: The cumulative information.
  - efficacyRiskDiffLower: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyRiskDiffUpper: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskDiffEquiv(
  beta = 0.2, n = NA, riskDiffLower = -0.1,
  riskDiffUpper = 0.1, pi1 = 0.12, pi2 = 0.12,
  nullVariance = 1,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignRiskDiffExact

Power and sample size for exact unconditional test for risk difference

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk difference.

Usage

```
getDesignRiskDiffExact(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskDiffH0: The risk difference under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffBound: The critical value on the scale of score test statistic for risk difference.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.
- calculationTarget: The calculation target, beta or n.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Superiority test

getDesignRiskDiffExact(n = 50, pi1 = 0.6, pi2 = 0.25, alpha = 0.025)


# Non-inferiority test

getDesignRiskDiffExact(beta = 0.1, riskDiffH0 = -0.2,
                       pi1 = 0.8, pi2 = 0.8, alpha = 0.025)
```

---

getDesignRiskDiffExactEquiv

Power and sample size for exact unconditional test for equivalence in risk difference

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk difference.

Usage

```
getDesignRiskDiffExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.

allocationRatioPlanned
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

alpha
: The significance level for each of the two one-sided tests. Defaults to 0.05.

Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.
- riskDiffLower: The lower equivalence limit of risk difference.
- riskDiffUpper: The upper equivalence limit of risk difference.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskDiffUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.
- calculationTarget: The calculation target, beta or n.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getDesignRiskDiffExactEquiv(
  n = 200, riskDiffLower = -0.2, riskDiffUpper = 0.2,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatio *Group sequential design for two-sample risk ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio.

Usage

```
getDesignRiskRatio(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping
: Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues
: Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha
: The significance level. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.

  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskRatioH0: The risk ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskRatio: The efficacy boundaries on the risk ratio scale.
  - futilityRiskRatio: The futility boundaries on the risk ratio scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

getDesignRiskRatioEquiv

Group sequential design for equivalence in two-sample risk ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk ratio.

Usage

```
getDesignRiskRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioLower	The lower equivalence limit of risk ratio.

riskRatioUpper The upper equivalence limit of risk ratio.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

nullVariance Whether to use the variance under the null or the empirical variance under the alternative.

allocationRatioPlanned
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates
The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.

  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - riskRatioLower: The lower equivalence limit of risk ratio.
  - riskRatioUpper: The upper equivalence limit of risk ratio.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyRiskRatioLower: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyRiskRatioUpper: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatioEquiv(
  beta = 0.2, n = NA, riskRatioLower = 0.8,
  riskRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignRiskRatioExact

Power and sample size for exact unconditional test for risk ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk ratio.

Usage

```
getDesignRiskRatioExact(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskRatioH0: The risk ratio under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioBound: The critical value on the scale of score test statistic for risk ratio.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.
- calculationTarget: The calculation target, beta or n.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Non-inferiority test

getDesignRiskRatioExact(beta = 0.1, riskRatioH0 = 0.833,
                        pi1 = 0.9, pi2 = 0.9, alpha = 0.025)
```

---

getDesignRiskRatioExactEquiv

Power and sample size for exact unconditional test for equivalence in risk ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk ratio.

Usage

```
getDesignRiskRatioExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioLower	The lower equivalence limit of risk ratio.
riskRatioUpper	The upper equivalence limit of risk ratio.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.

Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.
- riskRatioLower: The lower equivalence limit of risk ratio.
- riskRatioUpper: The upper equivalence limit of risk ratio.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskRatioUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.
- calculationTarget: The calculation target, beta or n.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getDesignRiskRatioExactEquiv(
  n = 200, riskRatioLower = 0.8, riskRatioUpper = 1.25,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatioFM *Group sequential design for two-sample risk ratio based on the Farrington-Manning score test*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio based on the Farrington-Manning score test

Usage

```
getDesignRiskRatioFM(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatioFM object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskRatioH0: The risk ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.

  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskRatioScore: The efficacy boundaries on the score test pi1 - riskRatioH0*pi2 score.
  - futilityRiskRatioScore: The futility boundaries on the score test pi1 - riskRatioH0*pi2 scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - calculationTarget: The calculation target, beta or n.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatioFM(
  beta = 0.2, riskRatioH0 = 1.3, pi1 = 0.125, pi2 = 0.125,
  alpha = 0.05))
```

---

getDesignSlopeDiff *Group sequential design for two-sample slope difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample slope difference.

Usage

```
getDesignSlopeDiff(
  beta = NA_real_,
  n = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

`efficacyStopping`
: Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

`futilityStopping`
: Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

`criticalValues`
: Upper boundaries on the z-test statistic scale for stopping for efficacy.

`alpha`
: The significance level. Defaults to 0.025.

`typeAlphaSpending`
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

`parameterAlphaSpending`
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

`userAlphaSpending`
: The user defined alpha spending. Cumulative alpha spent up to each stage.

`futilityBounds`
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpending`
: The user defined beta spending. Cumulative beta spent up to each stage.

`spendingTime`
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designSlopeDiff` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.

  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - slopeDiffH0: The slope difference under the null hypothesis.
  - slopeDiff: The slope difference under the alternative hypothesis.
  - stDev: The standard deviation of the residual.
  - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
  - futilitySlopeDiff: The futility boundaries on the slope difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.

- spendingTime: The error spending time at each analysis.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignSlopeDiff(
  beta = 0.1, n = NA, slopeDiff = -0.5,
  stDev = 10, stDevCovariate = 6,
  normalApproximation = FALSE, alpha = 0.025))
```

---

getDesignSlopeDiffMMRM

Power and sample for two-sample slope difference from the MMRM model

---

Description

Obtains the power given sample size or obtains the sample size given power for two-sample slope difference from the growth curve MMRM model.

Usage

```
getDesignSlopeDiffMMRM(
  beta = NA_real_,
  n = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
  stDevIntercept = 1,
  stDevSlope = 1,
  corrInterceptSlope = 0.5,
  k = NA_integer_,
  t = NA_real_,
  cumdrop1 = rep(0, k),
  cumdrop2 = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
```

```
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevIntercept	The standard deviation of the random intercept.
stDevSlope	The standard deviation of the random slope.
corrInterceptSlope	The correlation between the random intercept and random slope.
k	The number of time points including the baseline.
t	The time points. It should have k elements, start with 0 corresponding to the baseline time point, and be increasing.
cumdrop1	The cumulative dropout rate at the given time points for the active treatment group.
cumdrop2	The cumulative dropout rate at the given time points for the control group. If missing, it will be set equal to the cumulative dropout rate for the active treatment group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

We use the following random-effects model to compare two slopes:

$$y_{ij} = \alpha + (\beta + \gamma x_i)t_j + a_i + b_i t_j + e_{ij},$$

where

- α: overall intercept common across treatment groups due to randomization
- β: slope for the control group
- γ: difference in slope between the active treatment and control groups
- x_i: treatment indicator for subject i, 1 for the active treatment and 0 for the control

- t_j: time point j for repeated measurements, $t_1 = 0 < t_2 < \ldots < t_k$
- (a_i, b_i): random intercept and random slope for subject i, $Var(a_i) = \sigma_a^2$, $Var(b_i) = \sigma_b^2$, $Corr(a_i, b_i) = \rho$
- e_{ij}: within-subject residual with variance σ_e^2

By accounting for randomization, we improve the efficiency for estimating the difference in slope. We also allow for non-equal spacing of the time points and missing data due to dropouts.

Value

An S3 class `designSlopeDiffMMRM` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `slopeDiffH0`: The slope difference under the null hypothesis.
- `slopeDiff`: The slope difference under the alternative hypothesis.
- `stDev`: The standard deviation of the residual.
- `stDevIntercept`: The standard deviation of the random intercept.
- `stDevSlope`: The standard deviation of the random slope.
- `corrInterceptSlope`: The correlation between the random intercept and random slope.
- `k`: The number of time points including the baseline.
- `t`: The time points.
- `cumdrop1`: The cumulative dropout rate at the given time points for the active treatment group.
- `cumdrop2`: The cumulative dropout rate at the given time points for the control group.
- `calculationTarget`: The calculation target, `beta` or `n`.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
- `normalApproximation`: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignSlopeDiffMMRM(
  beta = 0.1, n = NA, slopeDiff = -1,
  stDev = 4, stDevIntercept = 10,
  stDevSlope = 6, corrInterceptSlope = 0.5,
  k = 7, t = seq(0, 6),
  normalApproximation = TRUE, alpha = 0.025))
```

getDesignTwoMultinom *Power and sample for difference in two-sample multinomial response*

Description

Obtains the power given sample size or obtains the sample size given power for difference in two-sample multinomial response.

Usage

```
getDesignTwoMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designTwoMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the multinomial response.

- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- effectsize: The effect size for the chi-square test.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoMultinom(
  beta = 0.1, ncats = 3, pi1 = c(0.3, 0.35),
  pi2 = c(0.2, 0.3), alpha = 0.05))
```

---

getDesignTwoOrdinal *Power and sample size for the Wilcoxon test for two-sample ordinal response*

Description

Obtains the power given sample size or obtains the sample size given power for the Wilcoxon test for two-sample ordinal response.

Usage

```
getDesignTwoOrdinal(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the ordinal response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The significance level. Defaults to 0.025.

Value

An S3 class designTwoOrdinal object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the ordinal response.
- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- meanscore1: The mean midrank score for the treatment group.
- meanscore2: The mean midrank score for the control group.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoOrdinal(
  beta = 0.1, ncats = 4, pi1 = c(0.55, 0.3, 0.1),
  pi2 = c(0.214, 0.344, 0.251), alpha = 0.025))
```

`getDesignTwoWayANOVA` *Power and sample size for two-way ANOVA*

Description

Obtains the power and sample size for two-way analysis of variance.

Usage

```
getDesignTwoWayANOVA(
  beta = NA_real_,
  n = NA_real_,
  nlevelsA = 2,
  nlevelsB = 2,
  means = NA_real_,
  stDev = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`nlevelsA`	The number of groups for Factor A.
`nlevelsB`	The number of levels for Factor B.
`means`	The matrix of treatment means for Factors A and B combination.
`stDev`	The common standard deviation.
`rounding`	Whether to round up sample size. Defaults to 1 for sample size rounding.
`alpha`	The two-sided significance level. Defaults to 0.05.

Value

An S3 class `designTwoWayANOVA` object with the following components:

- `alpha`: The two-sided significance level.
- `nlevelsA`: The number of levels for Factor A.
- `nlevelsB`: The number of levels for Factor B.
- `means`: The matrix of treatment group means.
- `stDev`: The common standard deviation.
- `effectsizeA`: The effect size for Factor A.
- `effectsizeB`: The effect size for Factor B.
- `effectsizeAB`: The effect size for Factor A and Factor B interaction.

- calculationTarget: The calculation target, beta or n.
- rounding: Whether to round up sample size.
- powerdf: The data frame containing the power and sample size results. It has the following variables:
  - n: The sample size.
  - powerA: The power to reject the null hypothesis that there is no difference among Factor A levels.
  - powerB: The power to reject the null hypothesis that there is no difference among Factor B levels.
  - powerAB: The power to reject the null hypothesis that there is no interaction between Factor A and Factor B.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoWayANOVA(
  beta = 0.1, nlevelsA = 2, nlevelsB = 2,
  means = matrix(c(0.5, 4.7, 0.4, 6.9), 2, 2, byrow = TRUE),
  stDev = 2, alpha = 0.05))
```

---

getDesignUnorderedBinom

Power and sample size for unordered multi-sample binomial response

---

Description

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample binomial response.

Usage

```
getDesignUnorderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
pi	The response probabilities for the treatment groups.
allocationRatioPlanned	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designUnorderedBinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignUnorderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

getDesignUnorderedMultinom *Power and sample size for unordered multi-sample multinomial response*

Description

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample multinomial response.

Usage

```
getDesignUnorderedMultinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  ncats = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
ncats	The number of categories of the multinomial response.
pi	The matrix of response probabilities for the treatment groups. It should have ngroups rows and ncats-1 or ncats columns.
allocationRatioPlanned	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designUnorderedMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.

- ncats: The number of categories of the multinomial response.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- calculationTarget: The calculation target, beta or n.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignUnorderedMultinom(
  beta = 0.1, ngroups = 3, ncats = 4,
  pi = matrix(c(0.230, 0.320, 0.272,
                0.358, 0.442, 0.154,
                0.142, 0.036, 0.039),
              3, 3, byrow = TRUE),
  allocationRatioPlanned = c(2, 2, 1),
  alpha = 0.05))
```

---

getDesignWilcoxon *Group sequential design for two-sample Wilcoxon test*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample Wilcoxon test.

Usage

```
getDesignWilcoxon(
  beta = NA_real_,
  n = NA_real_,
  pLarger = 0.6,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
```

```
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pLarger	The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designWilcoxon object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping..
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pLarger: The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.

  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPLarger: The efficacy boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
  - futilityPLarger: The futility boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - calculationTarget: The calculation target, beta or n.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: fixed design
(design1 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025,
  kMax = 3, typeAlphaSpending = "sfOF"))
```

`getDurationFromNevents` *Range of accrual duration for target number of events*

Description

Obtains a range of accrual duration to reach the target number of events.

Usage

```
getDurationFromNevents(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  followupTime = 18,
  fixedFollowup = 0L,
  npoints = 23L,
  interval = as.numeric(c(0.001, 240))
)
```

Arguments

`nevents`	The target number of events.
`allocationRatioPlanned`	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
`accrualTime`	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
`accrualIntensity`	A vector of accrual intensities. One for each accrual time interval.
`piecewiseSurvivalTime`	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`stratumFraction`	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
`lambda1`	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
npoints	The number of accrual duration time points. Defaults to 23.
interval	The interval to search for the solution of accrualDuration. Defaults to c(0.001, 240).

Value

A data frame of the following variables:

- nevents: The target number of events.
- fixedFollowup: Whether a fixed follow-up design is used.
- accrualDuration: The accrual duration.
- subjects: The total number of subjects.
- studyDuration: The study duration.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

getDurationFromNevents(
  nevents = 80, allocationRatioPlanned = 1,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12,
  fixedFollowup = FALSE)
```

`getNeventsFromHazardRatio` *Get the required number of events given hazard ratio*

Description

Obtains the required number of events given the hazard ratios under the null and alternative hypotheses for a group sequential design.

Usage

```
getNeventsFromHazardRatio(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  hazardRatioH0 = 1,
  hazardRatio = 0.5,
  allocationRatioPlanned = 1,
  rounding = 1L
)
```

Arguments

`beta`	Type II error. Defaults to 0.2.
`kMax`	The maximum number of stages.
`informationRates`	The information rates in terms of number of events. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

hazardRatio Hazard ratio under the alternative hypothesis for the active treatment versus control. Defaults to 0.5.

allocationRatioPlanned
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding Whether to round up the number of events. Defaults to 1 for rounding.

Value

The required number of events.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getNeventsFromHazardRatio(
  beta = 0.2, kMax = 2,
  informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP",
  hazardRatio = 0.673)
```

---

getRCI *Repeated confidence interval for group sequential design*

Description

Obtains the repeated confidence interval for a group sequential trial.

Usage

```
getRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

L	The look of interest.
zL	The z-test statistic at the look.
IMax	The maximum information of the trial.
informationRates	The information rates up to look L.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime
: The error spending time up to look `L`. Defaults to missing, in which case, it is the same as `informationRates`.

Value

A data frame with the following components:

- `pvalue`: Repeated p-value for rejecting the null hypothesis.
- `thetahat`: Point estimate of the parameter.
- `cilevel`: Confidence interval level.
- `lower`: Lower bound of repeated confidence interval.
- `upper`: Upper bound of repeated confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Christopher Jennison and Bruce W. Turnbull. Interim analyses: the repeated confidence interval approach (with discussion). J R Stat Soc Series B. 1989;51:305-361.

Examples

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# results at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)
```

```
# repeated confidence interval
getRCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
       informationRates = c(1/3, 2/3), alpha = 0.05,
       typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

`hedgesg` *Hedges' g effect size*

Description

Obtains Hedges' g estimate and confidence interval of effect size.

Usage

```
hedgesg(tstat, m, ntilde, cilevel = 0.95)
```

Arguments

`tstat`	The value of the t-test statistic for comparing two treatment conditions.
`m`	The degrees of freedom for the t-test.
`ntilde`	The normalizing sample size to convert the standardized treatment difference to the t-test statistic, i.e., `tstat = sqrt(ntilde)*meanDiff/stDev`.
`cilevel`	The confidence interval level. Defaults to 0.95.

Details

Hedges' g is an effect size measure commonly used in meta-analysis to quantify the difference between two groups. It's an improvement over Cohen's d, particularly when dealing with small sample sizes.

The formula for Hedges' g is

$$g = c(m)d,$$

where d is Cohen's d effect size estimate, and $c(m)$ is the bias correction factor,

$$d = (\hat{\mu}_1 - \hat{\mu}_2)/\hat{\sigma},$$

$$c(m) = 1 - \frac{3}{4m - 1}.$$

Since $c(m) < 1$, Cohen's d overestimates the true effect size. $\delta = (\mu_1 - \mu_2)/\sigma$. Since

$$t = \sqrt{\tilde{n}}d,$$

we have

$$g = \frac{c(m)}{\sqrt{\tilde{n}}}t,$$

where t has a noncentral t distribution with m degrees of freedom and noncentrality parameter $\sqrt{\tilde{n}}\delta$.

The asymptotic variance of g can be approximated by

$$Var(g) = \frac{1}{\tilde{n}} + \frac{g^2}{2m}.$$

The confidence interval for δ can be constructed using normal approximation.

For two-sample mean difference with sample size n_1 for the treatment group and n_2 for the control group, we have $\tilde{n} = \frac{n_1 n_2}{n_1+n_2}$ and $m = n_1 + n_2 - 2$ for pooled variance estimate.

Value

A data frame with the following variables:

- `tstat`: The value of the `t` test statistic.
- `m`: The degrees of freedom for the t-test.
- `ntilde`: The normalizing sample size to convert the standardized treatment difference to the t-test statistic.
- `g`: Hedges' g effect size estimate.
- `varg`: Variance of g.
- `lower`: The lower confidence limit for effect size.
- `upper`: The upper confidence limit for effect size.
- `cilevel`: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Larry V. Hedges. Distribution theory for Glass's estimator of effect size and related estimators. Journal of Educational Statistics 1981; 6:107-128.

Examples

```
n1 = 7
n2 = 8
meanDiff = 0.444
stDev = 1.201
m = n1+n2-2
ntilde = n1*n2/(n1+n2)
tstat = sqrt(ntilde)*meanDiff/stDev

hedgesg(tstat, m, ntilde)
```

kmest *Stratified difference in milestone survival*

Description

Obtains the stratified Kaplan-Meier estimate of milestone survival probabilities and difference in milestone survival at given calendar times and milestone time.

Usage

```
kmest(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  numSubintervals = 300L
)
```

Arguments

time	A vector of calendar times at which to calculate the milestone survival.
milestone	The milestone time at which to calculate the Kaplan-Meier estimate of survival probability.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

`stratumFraction`
: A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

`lambda1`
: A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

`lambda2`
: A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

`gamma1`
: The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

`gamma2`
: The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

`accrualDuration`
: Duration of the enrollment period.

`followupTime`
: Follow-up time for the last enrolled subject.

`fixedFollowup`
: Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

`numSubintervals`
: Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.

Value

A data frame containing the following variables:

- `time`: The calendar time at which to calculate the milestone survival.
- `subjects`: The enrolled number of subjects.
- `milestone`: The milestone time relative to randomization.
- `surv1`: The milestone survival probability for the treatment group.
- `surv2`: The milestone survival probability for the control group.
- `vsurv1`: The variance for `surv1`.
- `vsurv2`: The variance for `surv2`.
- `survdiff`: The difference in milestone survival probabilities, i.e., `surv1 - surv2`.
- `vsurvdiff`: The variance for `survdiff`.
- `survdiffZ`: The Z-statistic value, i.e., `survdiff/sqrt(vsurvdiff)`.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

kmest(time = c(22, 40),
      milestone = 18,
      allocationRatioPlanned = 1,
      accrualTime = seq(0, 8),
      accrualIntensity = 26/9*seq(1, 9),
      piecewiseSurvivalTime = c(0, 6),
      stratumFraction = c(0.2, 0.8),
      lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
      lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
      gamma1 = -log(1-0.05)/12,
      gamma2 = -log(1-0.05)/12,
      accrualDuration = 22,
      followupTime = 18, fixedFollowup = FALSE)
```

---

lrpower *Log-rank test power*

Description

Estimates the power, stopping probabilities, and expected sample size in a two-group survival design.

Usage

```
lrpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 20L,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
```

```
  lambda1 = 0.0309,
  lambda2 = 0.0533,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = 11.6,
  followupTime = 18,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax	The maximum number of stages.
informationRates	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

hazardRatioH0
: Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime
: A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
: A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
: A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1
: A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2
: A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1
: The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2
: The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration
: Duration of the enrollment period.

followupTime
: Follow-up time for the last enrolled subject.

fixedFollowup
: Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1
: The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2
: The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

numSubintervals
: Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.

estimateHazardRatio
: Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.

typeOfComputation
: The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration
: Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class lrpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - rho1: The first parameter of the Fleming-Harrington family of weighted log-rank test.
  - rho2: The second parameter of the Fleming-Harrington family of weighted log-rank test.
  - kMax: The number of stages.
  - hazardRatioH0: The hazard ratio under the null hypothesis.
  - typeOfComputation: The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method.
- byStageResults: A data frame containing the following variables:

  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyHR: The efficacy boundaries on the hazard ratio scale if estimateHazardRatio.
  - futilityHR: The futility boundaries on the hazard ratio scale if estimateHazardRatio.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - HR: The average hazard ratio.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, estimateHazardRatio, and spendingTime.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

Author(s)

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Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

lrpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

lrsamplesize *Log-rank test sample size*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a two-group survival design.

Usage

```
lrsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 20L,
  piecewiseSurvivalTime = 0L,
```

```
  stratumFraction = 1L,
  lambda1 = 0.0309,
  lambda2 = 0.0533,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

`beta`	Type II error. Defaults to 0.2.
`kMax`	The maximum number of stages.
`informationRates`	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
`criticalValues`	Upper boundaries on the z-test statistic scale for stopping for efficacy.
`alpha`	The significance level. Defaults to 0.025.
`typeAlphaSpending`	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
`parameterAlphaSpending`	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
`userAlphaSpending`	The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
The user defined beta spending. Cumulative beta spent up to each stage.

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration
Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

numSubintervals
Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.

estimateHazardRatio
Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.

typeOfComputation
The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

interval The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`. Adjustment may be needed for non-monotone relationship with study power.

spendingTime A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

rounding Whether to round up sample size and events. Defaults to 1 for sample size rounding.

Value

A list of two components:

- `resultsUnderH1`: An S3 class `lrpower` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `lrpower` object under the null hypothesis.

Author(s)

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See Also

`lrpower`

Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

# Example 1: Obtains accrual duration given power and follow-up duration

lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
```

```
              accrualTime = seq(0, 8),
              accrualIntensity = 26/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
              stratumFraction = c(0.2, 0.8),
              lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
              lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
              gamma1 = -log(1-0.05)/12,
              gamma2 = -log(1-0.05)/12,
              accrualDuration = NA,
              followupTime = 18, fixedFollowup = FALSE)


  # Example 2: Obtains follow-up duration given power and accrual duration

  lrsamplesize(beta = 0.2, kMax = 2,
              informationRates = c(0.8, 1),
              alpha = 0.025, typeAlphaSpending = "sfOF",
              accrualTime = seq(0, 8),
              accrualIntensity = 26/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
              stratumFraction = c(0.2, 0.8),
              lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
              lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
              gamma1 = -log(1-0.05)/12,
              gamma2 = -log(1-0.05)/12,
              accrualDuration = 22,
              followupTime = NA, fixedFollowup = FALSE)


  # Example 3: Obtains absolute accrual intensity given power,
  # accrual duration, follow-up duration, and relative accrual intensity

  lrsamplesize(beta = 0.2, kMax = 2,
              informationRates = c(0.8, 1),
              alpha = 0.025, typeAlphaSpending = "sfOF",
              accrualTime = seq(0, 8),
              accrualIntensity = 26/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
              stratumFraction = c(0.2, 0.8),
              lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
              lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
              gamma1 = -log(1-0.05)/12,
              gamma2 = -log(1-0.05)/12,
              accrualDuration = 22,
              followupTime = 18, fixedFollowup = FALSE)
```

---

lrsim *Log-rank test simulation*

Description

Performs simulation for two-arm group sequential trials based on weighted log-rank test.

Usage

```
lrsim(
  kMax = NA_integer_,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  futilityBounds = NA_real_,
  hazardRatioH0 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

kMax	The maximum number of stages.
informationRates	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Fixed prior to the trial. If left unspecified, it defaults to plannedEvents / plannedEvents[kMax] when plannedEvents is provided and to plannedTime / plannedTime[kMax] otherwise.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocation1 Number of subjects in the active treatment group in a randomization block. Defaults to 1 for equal randomization.

allocation2 Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration
Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of events at each stage.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses, `plannedEvents` should be missing.

maxNumberOfIterations
The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage
The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

Value

An S3 class `lrsim` object with 3 components:

- `overview`: A list containing the following information:
  - `rejectPerStage`: The efficacy stopping probability by stage.
  - `futilityPerStage`: The futility stopping probability by stage.
  - `cumulativeRejection`: Cumulative efficacy stopping probability by stage.
  - `cumulativeFutility`: The cumulative futility stopping probability by stage.
  - `numberOfEvents`: The average number of events by stage.
  - `numberOfDropouts`: The average number of dropouts by stage.
  - `numberOfSubjects`: The average number of subjects by stage.
  - `analysisTime`: The average analysis time by stage.
  - `overallReject`: The overall rejection probability.
  - `expectedNumberOfEvents`: The expected number of events for the overall study.
  - `expectedNumberOfDropouts`: The expected number of dropouts for the overall study.
  - `expectedNumberOfSubjects`: The expected number of subjects for the overall study.
  - `expectedStudyDuration`: The expected study duration.
  - `hazardRatioH0`: Hazard ratio under the null hypothesis for the active treatment versus control.
  - `useEvents`: whether the analyses are planned based on the number of events or calendar time.
  - `accrualDuration`: Duration of the enrollment period.
  - `fixedFollowup`: Whether a fixed follow-up design is used.
  - `rho1`: The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
  - `rho2`: The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
  - `kMax`: The maximum number of stages.
- `sumdata`: A data frame of summary data by iteration and stage:
  - `iterationNumber`: The iteration number.
  - `stopStage`: The stage at which the trial stops.
  - `eventsNotAchieved`: Whether the target number of events is not achieved for the iteration.
  - `stageNumber`: The stage number, covering all stages even if the trial stops at an interim look.
  - `analysisTime`: The time for the stage since trial start.
  - `accruals1`: The number of subjects enrolled at the stage for the treatment group.
  - `accruals2`: The number of subjects enrolled at the stage for the control group.
  - `totalAccruals`: The total number of subjects enrolled at the stage.
  - `events1`: The number of events at the stage for the treatment group.
  - `events2`: The number of events at the stage for the control group.
  - `totalEvents`: The total number of events at the stage.
  - `dropouts1`: The number of dropouts at the stage for the treatment group.

  - dropouts2: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - uscore: The numerator of the log-rank test statistic.
  - vscore: The variance of the log-rank test statistic.
  - logRankStatistic: The log-rank test Z-statistic.
  - rejectPerStage: Whether to reject the null hypothesis at the stage.
  - futilityPerStage: Whether to stop the trial for futility at the stage.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stopStage: The stage at which the trial stops.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1 or 2) for the subject.
  - survivalTime: The underlying survival time for the subject.
  - dropoutTime: The underlying dropout time for the subject.
  - timeUnderObservation: The time under observation since randomization.
  - event: Whether the subject experienced the event.
  - dropoutEvent: Whether the subject dropped out.

Author(s)

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Examples

```
# Example 1: analyses based on number of events

sim1 = lrsim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedEvents = c(60, 120),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)

# summary statistics
sim1

# summary for each simulated data set
head(sim1$sumdata)

# raw data for selected replication
```

```
head(sim1$rawdata)


# Example 2: analyses based on calendar time have similar power

sim2 = lrsim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedTime = c(31.9, 113.2),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)

# summary statistics
sim2

# summary for each simulated data set
head(sim2$sumdata)
```

---

lrsim2e *Log-rank test simulation for two endpoints*

Description

Performs simulation for two-endpoint two-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in two arms combined, and the subsequent looks are driven by the total number of OS events in two arms combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim2e(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH0e1 = 1,
  hazardRatioH0e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda1e2 = NA_real_,
```

```
  lambda2e2 = NA_real_,
  gamma1e1 = 0L,
  gamma2e1 = 0L,
  gamma1e2 = 0L,
  gamma2e2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

kMax	The maximum number of stages.
kMaxe1	Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.
hazardRatioH0e1	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH0e2	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 2 (OS). Defaults to 1 for superiority test.
allocation1	Number of subjects in the treatment group in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
rho	The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.

lambda1e1 A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).

lambda2e1 A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 1 (PFS).

lambda1e2 A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).

lambda2e2 A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 2 (OS).

gamma1e1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).

gamma2e1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 1 (PFS).

gamma1e2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).

gamma2e2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 2 (OS).

accrualDuration
Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.

maxNumberOfIterations
The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage
The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the treatment group.
  - accruals2: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - endpoint: The endpoint (1 or 2) under consideration.
  - events1: The number of events at the stage for the treatment group.
  - events2: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the treatment group.
  - dropouts2: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic: The log-rank test Z-statistic for the endpoint.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1 or 2) for the subject.
  - survivalTime1: The underlying survival time for event endpoint 1 for the subject.
  - dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
  - timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
  - event1: Whether the subject experienced event endpoint 1.
  - dropoutEvent1: Whether the subject dropped out for endpoint 1.
  - survivalTime2: The underlying survival time for event endpoint 2 for the subject.
  - dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
  - timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
  - event2: Whether the subject experienced event endpoint 2.
  - dropoutEvent2: Whether the subject dropped out for endpoint 2.

Author(s)

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Examples

```
sim1 = lrsim2e(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30,
  accrualDuration = 20.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrsim2e3a *Log-rank test simulation for two endpoints and three arms*

Description

Performs simulation for two-endpoint three-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in Arm A and Arm C combined, and the subsequent looks are driven by the total number of OS events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim2e3a(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH013e1 = 1,
  hazardRatioH023e1 = 1,
  hazardRatioH012e1 = 1,
  hazardRatioH013e2 = 1,
  hazardRatioH023e2 = 1,
```

```
  hazardRatioH012e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  allocation3 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda3e1 = NA_real_,
  lambda1e2 = NA_real_,
  lambda2e2 = NA_real_,
  lambda3e2 = NA_real_,
  gamma1e1 = 0L,
  gamma2e1 = 0L,
  gamma3e1 = 0L,
  gamma1e2 = 0L,
  gamma2e2 = 0L,
  gamma3e2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

kMax	The maximum number of stages.
kMaxe1	Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.
hazardRatioH013e1	Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH023e1	Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH012e1	Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH013e2
: Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH023e2
: Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH012e2
: Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 2 (OS). Defaults to 1 for superiority test.

allocation1
: Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.

allocation2
: Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.

allocation3
: Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.

accrualTime
: A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
: A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
: A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

rho
: The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.

lambda1e1
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).

lambda2e1
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).

lambda3e1
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).

lambda1e2
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).

lambda2e2
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).

lambda3e2
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).

gamma1e1
: The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).

gamma2e1 The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).

gamma3e1 The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).

gamma1e2 The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).

gamma2e2 The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).

gamma3e2 The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).

accrualDuration
Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 for Arms A and C combined and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax for Arms A and C combined.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.

maxNumberOfIterations
The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage
The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.

  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
  - accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
  - accruals3: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - endpoint: The endpoint (1 or 2) under consideration.
  - events1: The number of events at the stage for the active treatment 1 group.
  - events2: The number of events at the stage for the active treatment 2 group.
  - events3: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the active treatment 1 group.
  - dropouts2: The number of dropouts at the stage for the active treatment 2 group.
  - dropouts3: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control for the endpoint.
  - logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control for the endpoint.
  - logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2 for the endpoint.

- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1, 2, or 3) for the subject.
  - survivalTime1: The underlying survival time for event endpoint 1 for the subject.
  - dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
  - timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
  - event1: Whether the subject experienced event endpoint 1.
  - dropoutEvent1: Whether the subject dropped out for endpoint 1.
  - survivalTime2: The underlying survival time for event endpoint 2 for the subject.
  - dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
  - timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
  - event2: Whether the subject experienced event endpoint 2.
  - dropoutEvent2: Whether the subject dropped out for endpoint 2.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
sim1 = lrsim2e3a(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12*0.70,
  lambda3e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30*0.75,
  lambda3e2 = log(2)/30,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrsim3a *Log-rank test simulation for three arms*

Description

Performs simulation for three-arm group sequential trials based on weighted log-rank test. The looks are driven by the total number of events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim3a(
  kMax = NA_integer_,
  hazardRatioH013 = 1,
  hazardRatioH023 = 1,
  hazardRatioH012 = 1,
  allocation1 = 1L,
```

```
  allocation2 = 1L,
  allocation3 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  lambda3 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  gamma3 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

kMax	The maximum number of stages.
hazardRatioH013	Hazard ratio under the null hypothesis for arm 1 versus arm 3. Defaults to 1 for superiority test.
hazardRatioH023	Hazard ratio under the null hypothesis for arm 2 versus arm 3. Defaults to 1 for superiority test.
hazardRatioH012	Hazard ratio under the null hypothesis for arm 1 versus arm 2. Defaults to 1 for superiority test.
allocation1	Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.
allocation3	Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
: A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 1.

lambda2
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 2.

lambda3
: A vector of hazard rates for the event in each analysis time interval by stratum for arm 3.

gamma1
: The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1.

gamma2
: The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2.

gamma3
: The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3.

accrualDuration
: Duration of the enrollment period.

followupTime
: Follow-up time for the last enrolled subject.

fixedFollowup
: Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1
: The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2
: The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents
: The planned cumulative total number of events at Look 1 to Look `kMax` for Arms A and C combined.

plannedTime
: The calendar times for the analyses. To use calendar time to plan the analyses, `plannedEvents` should be missing.

maxNumberOfIterations
: The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage
: The number of raw datasets per stage to extract. Defaults to 1.

seed
: The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

Value

A list with 2 components:

- `sumdata`: A data frame of summary data by iteration and stage:

  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
  - accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
  - accruals3: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - events1: The number of events at the stage for the active treatment 1 group.
  - events2: The number of events at the stage for the active treatment 2 group.
  - events3: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the active treatment 1 group.
  - dropouts2: The number of dropouts at the stage for the active treatment 2 group.
  - dropouts3: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control.
  - logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control.
  - logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2.

- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1, 2, or 3) for the subject.
  - survivalTime: The underlying survival time for the subject.
  - dropoutTime: The underlying dropout time for the subject.
  - timeUnderObservation: The time under observation since randomization for the subject.
  - event: Whether the subject experienced the event.
  - dropoutEvent: Whether the subject dropped out.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
sim1 = lrsim3a(
  kMax = 3,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  lambda1 = log(2)/12*0.60,
  lambda2 = log(2)/12*0.70,
  lambda3 = log(2)/12,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 295),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrstat *Number of subjects having an event and log-rank statistics*

Description

Obtains the number of subjects accrued, number of events, number of dropouts, and number of subjects reaching the maximum follow-up in each group, mean and variance of weighted log-rank score statistic, estimated hazard ratio from weighted Cox regression and variance of log hazard ratio estimate at given calendar times.

Usage

```
lrstat(
  time = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
```

```
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  predictTarget = 2L
)
```

Arguments

time	A vector of calendar times at which to calculate the number of events and the mean and variance of log-rank test score statistic.
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

numSubintervals Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.

predictTarget The target of prediction. Set predictTarget = 1 to predict the number of events only. Set predictTarget = 2 (default) to predict the number of events and log-rank score statistic mean and variance. Set predictTarget = 3 to predict the number of events, log-rank score statistic mean and variance, and hazard ratio and variance of log hazard ratio.

Value

A data frame containing the following variables if predictTarget = 1:

- time: The analysis time since trial start.
- subjects: The number of enrolled subjects.
- nevents: The total number of events.
- nevents1: The number of events in the active treatment group.
- nevents2: The number of events in the control group.
- ndropouts: The total number of dropouts.
- ndropouts1: The number of dropouts in the active treatment group.
- ndropouts2: The number of dropouts in the control group.
- nfmax: The total number of subjects reaching maximum follow-up.
- nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
- nfmax2: The number of subjects reaching maximum follow-up in the control group.

If predictTarget = 2, the following variables will also be included:

- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank score test statistic.
- logRankZ: The log-rank test statistic on the Z-scale.
- hazardRatioH0: The hazard ratio under the null hypothesis.

Furthermore, if predictTarget = 3, the following additional variables will also be included:

- HR: The average hazard ratio from weighted Cox regression.
- vlogHR: The variance of log hazard ratio.
- zlogHR: The Z-statistic for log hazard ratio.

Author(s)

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Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

lrstat(time = c(22, 40), allocationRatioPlanned = 1,
       accrualTime = seq(0, 8),
       accrualIntensity = 26/9*seq(1, 9),
       piecewiseSurvivalTime = c(0, 6),
       stratumFraction = c(0.2, 0.8),
       lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
       lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
       gamma1 = -log(1-0.05)/12,
       gamma2 = -log(1-0.05)/12,
       accrualDuration = 22,
       followupTime = 18, fixedFollowup = FALSE)
```

---

mnOddsRatioCI *Miettinen-Nurminen score confidence interval for two-sample odds ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample odds ratio possibly with stratification.

Usage

```
mnOddsRatioCI(n1, y1, n2, y2, cilevel = 0.95)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for odds ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnOddsRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRateDiffCI *Miettinen-Nurminen score confidence interval for two-sample rate difference*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate difference possibly with stratification.

Usage

```
mnRateDiffCI(t1, y1, t2, y2, cilevel = 0.95)
```

Arguments

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

A list with two components:

- `data` A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - `t1`: The exposure for the active treatment group.
  - `y1`: The number of events for the active treatment group.
  - `t2`: The exposure for the control group.
  - `y2`: The number of events for the control group.
- `estimates`: A data frame containing the point estimate and confidence interval for rate difference. It has the following variables:
  - `scale`: The scale of treatment effect.
  - `estimate`: The point estimate.
  - `lower`: The lower limit of the confidence interval.
  - `upper`: The upper limit of the confidence interval.
  - `cilevel`: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRateDiffCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

---

mnRateRatioCI *Miettinen-Nurminen score confidence interval for two-sample rate ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate ratio possibly with stratification.

Usage

```
mnRateRatioCI(t1, y1, t2, y2, cilevel = 0.95)
```

Arguments

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - t1: The exposure for the active treatment group.
  - y1: The number of events for the active treatment group.
  - t2: The exposure for the control group.
  - y2: The number of events for the control group.
- estimates: A data frame containing the point estimate and confidence interval for rate ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRateRatioCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

`mnRiskDiffCI` *Miettinen-Nurminen score confidence interval for two-sample risk difference*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk difference possibly with stratification.

Usage

```
mnRiskDiffCI(n1, y1, n2, y2, cilevel = 0.95)
```

Arguments

`n1`	The sample size for the active treatment group.
`y1`	The number of responses for the active treatment group.
`n2`	The sample size for the control group.
`y2`	The number of responses for the control group.
`cilevel`	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- `data` A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - `n1`: The sample size for the active treatment group.
  - `y1`: The number of responses for the active treatment group.
  - `n2`: The sample size for the control group.
  - `y2`: The number of responses for the control group.
- `estimates`: A data frame containing the point estimate and confidence interval for risk difference. It has the following variables:
  - `scale`: The scale of treatment effect.
  - `estimate`: The point estimate.
  - `lower`: The lower limit of the confidence interval.
  - `upper`: The upper limit of the confidence interval.
  - `cilevel`: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRiskDiffCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRiskRatioCI *Miettinen-Nurminen score confidence interval for two-sample risk ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk ratio possibly with stratification.

Usage

```
mnRiskRatioCI(n1, y1, n2, y2, cilevel = 0.95)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for risk ratio. It has the following variables:

- `scale`: The scale of treatment effect.
- `estimate`: The point estimate.
- `lower`: The lower limit of the confidence interval.
- `upper`: The upper limit of the confidence interval.
- `cilevel`: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRiskRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

`mTPI2Table` *mTPI-2 decision table*

Description

Obtains the decision table for the modified toxicity probability interval-2 (mTPI-2) design.

Usage

```
mTPI2Table(
  nMax = NA_integer_,
  pT = 0.3,
  epsilon1 = 0.05,
  epsilon2 = 0.05,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

Arguments

`nMax`	The maximum number of subjects in a dose cohort.
`pT`	The target toxicity probability. Defaults to 0.3.
`epsilon1`	The lower equivalence margin from the target. Defaults to 0.05.
`epsilon2`	The upper equivalence margin from the target. Defaults to 0.05.
`a`	The prior toxicity parameter for the beta prior.
`b`	The prior non-toxicity parameter for the beta prior.
`pExcessTox`	The threshold for excessive toxicity, i.e., if Prob(p > pT | Data) > pExcessTox, then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

Value

An S3 class `mTPI2Table` object with the following components:

- `settings`: The input settings data frame with the following variables:
  - `nMax`: The maximum number of subjects in a dose cohort.
  - `pT`: The target toxicity probability.
  - `epsilon1`: The lower equivalence margin from the target.
  - `epsilon2`: The upper equivalence margin from the target.
  - `a`: The prior toxicity parameter for the beta prior.
  - `b`: The prior non-toxicity parameter for the beta prior.
  - `pExcessTox`: The threshold for excessive toxicity.
- `subintervals`: The subintervals of equal length in the mTPI-2 design. It includes the following variables:
  - `lower`: The lower bound of the subinterval.
  - `upper`: The upper bound of the subinterval.
  - `decision`: The dosing decision for the subinterval.
- `decisionDataFrame`: The decision data frame for the mTPI-2 design. It includes the following variables:
  - `n`: The sample size.
  - `y`: The number of toxicities.
  - `decision`: The dosing decision.
- `decisionMatrix`: The decision matrix corresponding to the decision data frame.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mTPI2Table(nMax = 18, pT = 0.3, epsilon1 = 0.05, epsilon2 = 0.05)
```

---

nbpower *Negative binomial rate ratio power*

Description

Estimates the power for negative binomial rate ratio test.

Usage

```
nbpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa1 = 5,
  kappa2 = 5,
  lambda1 = 0.0875,
  lambda2 = 0.125,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = 1.25,
  followupTime = 2.75,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_,
  nullVariance = 0L
)
```

Arguments

`kMax`	The maximum number of stages.
`informationRates`	The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
`criticalValues`	Upper boundaries on the z-test statistic scale for stopping for efficacy.
`alpha`	The significance level. Defaults to 0.025.

typeAlphaSpending
: The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

rateRatioH0
: Rate ratio under the null hypothesis.

allocationRatioPlanned
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime
: A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
: A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

kappa1
: The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group.

kappa2
: The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group.

lambda1
: The rate parameter of the negative binomial distribution for the active treatment group.

lambda2
: The rate parameter of the negative binomial distribution for the control group.

gamma1
: The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group. Defaults to 0 for no dropout.

gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

An S3 class nbpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - exposure: The total exposure.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedExposure: The expected exposure.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - kMax: The number of stages.
  - rateRatioH0: The rate ratio under the null hypothesis.
  - rateRatio: The rate ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRateRatio: The efficacy boundaries on the rate ratio scale.
  - futilityRateRatio: The futility boundaries on the rate ratio scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, accrualDuration, followupTime, fixedFollowup, spendingTime, and nullVariance.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - exposure2: The exposure by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedExposure1: The expected exposure for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.
  - expectedExposure2: The expected exposure for the control group.

Author(s)

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See Also

nbstat

Examples

```
# Example 1: Variable follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 1956/1.25,
        kappa1 = 5, kappa2 = 5,
        lambda1 = 0.0875, lambda2 = 0.125,
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.25,
        followupTime = 2.75, fixedFollowup = FALSE,
        nullVariance = 1)

# Example 2: Fixed follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 220/1.5,
        kappa1 = 3, kappa2 = 3,
        lambda1 = 0.5*8.4, lambda2 = 8.4,
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.5,
        followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbpower1s *One-sample negative binomial rate power*

Description

Estimates the power, stopping probabilities, and expected sample size in a one-group negative binomial design.

Usage

```
nbpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
```

```
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa = 5,
  lambdaH0 = 0.125,
  lambda = 0.0875,
  gamma = 0L,
  accrualDuration = 1.25,
  followupTime = 2.75,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax	The maximum number of stages.
informationRates	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

accrualTime
: A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
: A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

kappa
: The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution.

lambdaH0
: The rate parameter of the negative binomial distribution under the null hypothesis.

lambda
: The rate parameter of the negative binomial distribution under the alternative hypothesis.

gamma
: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration
: Duration of the enrollment period.

followupTime
: Follow-up time for the last enrolled subject.

fixedFollowup
: Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

studyDuration
: Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of `accrualDuration` and `followupTime`. If provided, the value is allowed to be less than the sum of `accrualDuration` and `followupTime`.

Value

An S3 class `nbpower1s` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `numberOfEvents`: The total number of events.
  - `numberOfDropouts`: The total number of dropouts.
  - `numbeOfSubjects`: The total number of subjects.
  - `exposure`: The total exposure.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.

  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedExposure: The expected exposure.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - kMax: The number of stages.

- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRate: The efficacy boundaries on the rate scale.
  - futilityRate: The futility boundaries on the rate scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, kappa, lambdaH0, lambda, gamma, accrualDuration, followupTime, fixedFollowup, and spendingTime.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbstat

Examples

```
# Example 1: Variable follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          accrualIntensity = 500,
          kappa = 5, lambdaH0 = 0.125, lambda = 0.0875,
          gamma = 0, accrualDuration = 1.25,
          followupTime = 2.75, fixedFollowup = FALSE)

# Example 2: Fixed follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          accrualIntensity = 40,
          kappa = 3, lambdaH0 = 8.4, lambda = 0.5*8.4,
          gamma = 0, accrualDuration = 1.5,
          followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbpowerequiv *Power for equivalence in negative binomial rate ratio*

Description

Obtains the power for equivalence in negative binomial rate ratio.

Usage

```
nbpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa1 = 5,
  kappa2 = 5,
  lambda1 = 0.125,
  lambda2 = 0.125,
  gamma1 = 0L,
```

```
  gamma2 = 0L,
  accrualDuration = 1.25,
  followupTime = 2.75,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_,
  nullVariance = 0L
)
```

Arguments

kMax	The maximum number of stages.
informationRates	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
rateRatioLower	The lower equivalence limit of rate ratio.
rateRatioUpper	The upper equivalence limit of rate ratio.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group.

lambda1	The rate parameter of the negative binomial distribution for the active treatment group.
lambda2	The rate parameter of the negative binomial distribution for the control group.
gamma1	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group. Defaults to 0 for no dropout.
gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

An S3 class nbpowerequiv object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - exposure: The total exposure.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedExposure: The expected exposure.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - kMax: The number of stages.
  - rateRatioLower: The lower equivalence limit of rate ratio.
  - rateRatioUpper: The upper equivalence limit of rate ratio.

  - rateRatio: The rate ratio.

- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRateRatioLower: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyRateRatioUpper: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, accrualDuration, followupTime, fixedFollowup, spendingTime, nullVariance, and varianceRatios. The varianceRatios is a data frame with the following variables:
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.//'
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - exposure2: The exposure by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.

- expectedExposure1: The expected exposure for the treatment group.
- expectedNumberOfEvents2: The expected number of events for control group.
- expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- expectedNumberOfSubjects2: The expected number of subjects for the control group.
- expectedExposure2: The expected exposure for the control group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbstat

Examples

```
# Example 1: Variable follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 2/3, rateRatioUpper = 3/2,
             accrualIntensity = 1956/1.25,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.125, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = 2.75, fixedFollowup = FALSE,
             nullVariance = 1)

# Example 2: Fixed follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 0.5, rateRatioUpper = 2,
             accrualIntensity = 220/1.5,
             kappa1 = 3, kappa2 = 3,
             lambda1 = 8.4, lambda2 = 8.4,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.5,
             followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesize *Negative binomial rate ratio sample size*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a two-group negative binomial design.

Usage

```
nbsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa1 = 5,
  kappa2 = 5,
  lambda1 = 0.0875,
  lambda2 = 0.125,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
  nullVariance = 0L
)
```

Arguments

`beta`	Type II error. Defaults to 0.2.
`kMax`	The maximum number of stages.
`informationRates`	The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
The user defined beta spending. Cumulative beta spent up to each stage.

rateRatioH0 Rate ratio under the null hypothesis.

allocationRatioPlanned
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group.

lambda1	The rate parameter of the negative binomial distribution for the active treatment group.
lambda2	The rate parameter of the negative binomial distribution for the control group.
gamma1	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group. Defaults to 0 for no dropout.
gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`. Adjustment may be needed for non-monotone relationship with study power.
spendingTime	A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

A list of two components:

- `resultsUnderH1`: An S3 class `nbpower` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `nbpower` object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbpower

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 1956/1.25,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.0875, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
```

```
             followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.0875, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = 2.25, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 1667,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.0875, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = NA,
             followupTime = 0.5, fixedFollowup = TRUE)
```

`nbsamplesize1s` *One-sample negative binomial rate sample size*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group negative binomial design.

Usage

```
nbsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
```

```
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa = 5,
  lambdaH0 = 0.125,
  lambda = 0.0875,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

`beta`	Type II error. Defaults to 0.2.
`kMax`	The maximum number of stages.
`informationRates`	The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
`criticalValues`	Upper boundaries on the z-test statistic scale for stopping for efficacy.
`alpha`	The significance level. Defaults to 0.025.
`typeAlphaSpending`	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
`parameterAlphaSpending`	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
`userAlphaSpending`	The user defined alpha spending. Cumulative alpha spent up to each stage.

`futilityBounds` Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified.

`typeBetaSpending`
The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

`parameterBetaSpending`
The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

`userBetaSpending`
The user defined beta spending. Cumulative beta spent up to each stage.

`accrualTime` A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

`accrualIntensity`
A vector of accrual intensities. One for each accrual time interval.

`piecewiseSurvivalTime`
A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

`kappa` The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution.

`lambdaH0` The rate parameter of the negative binomial distribution under the null hypothesis.

`lambda` The rate parameter of the negative binomial distribution under the alternative hypothesis.

`gamma` The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

`accrualDuration`
Duration of the enrollment period.

`followupTime` Follow-up time for the last enrolled subject.

`fixedFollowup` Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

`interval` The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`. Adjustment may be needed for non-monotone relationship with study power.

`spendingTime` A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

`rounding` Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- `resultsUnderH1`: An S3 class `nbpower1s` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `nbpower1s` object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbpower1s

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               accrualIntensity = 500,
               kappa = 5, lambdaH0 = 0.125, lambda = 0.0875,
               gamma = 0, accrualDuration = 1.25,
               followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               kappa = 5, lambdaH0 = 0.125, lambda = 0.0875,
               gamma = 0, accrualDuration = 1.25,
               followupTime = 2.25, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               accrualIntensity = 40,
               kappa = 3, lambdaH0 = 8.4, lambda = 4.2,
               gamma = 0, accrualDuration = NA,
               followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesizeequiv *Sample size for equivalence in negative binomial rate ratio*

Description

Obtains the sample size for equivalence in negative binomial rate ratio.

Usage

```
nbsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = 1500L,
  piecewiseSurvivalTime = 0L,
  kappa1 = 5,
  kappa2 = 5,
  lambda1 = 0.125,
  lambda2 = 0.125,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
  nullVariance = 0L
)
```

Arguments

beta	The type II error.
kMax	The maximum number of stages.
informationRates	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
: The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

rateRatioLower
: The lower equivalence limit of rate ratio.

rateRatioUpper
: The upper equivalence limit of rate ratio.

allocationRatioPlanned
: Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime
: A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
: A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

kappa1
: The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group.

kappa2
: The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group.

lambda1
: The rate parameter of the negative binomial distribution for the active treatment group.

lambda2
: The rate parameter of the negative binomial distribution for the control group.

gamma1
: The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group. Defaults to 0 for no dropout.

gamma2
: The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group. Defaults to 0 for no dropout.

accrualDuration
: Duration of the enrollment period.

followupTime
: Follow-up time for the last enrolled subject.

fixedFollowup
: Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval
: The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`. Adjustment may be needed for non-monotone relationship with study power.

spendingTime
: A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

rounding
: Whether to round up sample size. Defaults to 1 for sample size rounding.

nullVariance
: Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

An S3 class `nbpowerequiv` object

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbpowerequiv

Examples

```
# Example 1: Variable follow-up design and solve for follow-up time
nbsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  rateRatioLower = 2/3, rateRatioUpper = 3/2,
                  accrualIntensity = 1956/1.25,
                  kappa1 = 5, kappa2 = 5,
                  lambda1 = 0.125, lambda2 = 0.125,
                  gamma1 = 0, gamma2 = 0,
                  accrualDuration = 1.25,
                  followupTime = NA, fixedFollowup = FALSE,
                  nullVariance = 1)

# Example 2: Fixed follow-up design and solve for accrual duration
nbsamplesizeequiv(beta = 0.2, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  rateRatioLower = 0.5, rateRatioUpper = 2,
                  accrualIntensity = 220/1.5,
                  kappa1 = 3, kappa2 = 3,
                  lambda1 = 8.4, lambda2 = 8.4,
                  gamma1 = 0, gamma2 = 0,
                  accrualDuration = NA,
                  followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbstat *Number of events and information for negative binomial rate ratio*

Description

Obtains the number of subjects accrued, number of events, number of dropouts, number of subjects reaching the maximum follow-up, total exposure, and information for log rate in each group, rate ratio, variance, information, and Wald test statistic of log rate ratio at given calendar times.

Usage

```
nbstat(
  time = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
```

```
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  nullVariance = 0L
)
```

Arguments

`time`	A vector of calendar times at which to calculate the number of events and the Wald test statistic.
`rateRatioH0`	Rate ratio under the null hypothesis.
`allocationRatioPlanned`	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
`accrualTime`	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
`accrualIntensity`	A vector of accrual intensities. One for each accrual time interval.
`piecewiseSurvivalTime`	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`kappa1`	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group.
`kappa2`	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group.
`lambda1`	The rate parameter of the negative binomial distribution for the active treatment group.
`lambda2`	The rate parameter of the negative binomial distribution for the control group.
`gamma1`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group. Defaults to 0 for no dropout.
`gamma2`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group. Defaults to 0 for no dropout.
`accrualDuration`	Duration of the enrollment period.
`followupTime`	Follow-up time for the last enrolled subject.

`fixedFollowup`	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
`nullVariance`	Whether to calculate the variance for log rate ratio under the null hypothesis.

Details

The probability mass function for a negative binomial distribution with dispersion parameter κ_i and rate parameter λ_i is given by

$$P(Y_{ij} = y) = \frac{\Gamma(y + 1/\kappa_i)}{\Gamma(1/\kappa_i)y!} \left(\frac{1}{1 + \kappa_i\lambda_i t_{ij}}\right)^{1/\kappa_i} \left(\frac{\kappa_i\lambda_i t_{ij}}{1 + \kappa_i\lambda_i t_{ij}}\right)^{y},$$

where Y_{ij} is the event count for subject j in treatment group i, and t_{ij} is the exposure time for the subject. If $\kappa_i = 0$, the negative binomial distribution reduces to the Poisson distribution.

For treatment group i, let $\beta_i = \log(\lambda_i)$. The likelihood for $\{(\kappa_i, \beta_i) : i = 1, 2\}$ can be written as

$$l = \sum_{i=1}^{2}\sum_{j=1}^{n_i}\{\log\Gamma(y_{ij}+1/\kappa_i) - \log\Gamma(1/\kappa_i) + y_{ij}(\log(\kappa_i)+\beta_i) - (y_{ij}+1/\kappa_i)\log(1+\kappa_i\exp(\beta_i)t_{ij})\}.$$

It follows that

$$\frac{\partial l}{\partial \beta_i} = \sum_{j=1}^{n_i}\left\{y_{ij} - (y_{ij} + 1/\kappa_i)\frac{\kappa_i\exp(\beta_i)t_{ij}}{1 + \kappa_i\exp(\beta_i)t_{ij}}\right\},$$

and

$$-\frac{\partial^2 l}{\partial \beta_i^2} = \sum_{j=1}^{n_i}(y_{ij} + 1/\kappa_i)\frac{\kappa_i\lambda_i t_{ij}}{(1 + \kappa_i\lambda_i t_{ij})^2}.$$

The Fisher information for β_i is

$$E\left(-\frac{\partial^2 l}{\partial \beta_i^2}\right) = n_i E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i\lambda_i t_{ij}}\right).$$

In addition, we can show that

$$E\left(-\frac{\partial^2 l}{\partial \beta_i \partial \kappa_i}\right) = 0.$$

Therefore, the variance of $\hat{\beta}_i$ is

$$Var(\hat{\beta}_i) = \frac{1}{n_i}\left\{E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i\lambda_i t_{ij}}\right)\right\}^{-1}.$$

To evaluate the integral, we need to obtain the distribution of the exposure time,

$$t_{ij} = \min(\tau - W_{ij}, C_{ij}, T_{fmax}),$$

where τ denotes the calendar time since trial start, W_{ij} denotes the enrollment time for subject j in treatment group i, C_{ij} denotes the time to dropout after enrollment for subject j in treatment group i, and T_{fmax} denotes the maximum follow-up time for all subjects. Therefore,

$$P(t_{ij} \geq t) = P(W_{ij} \leq \tau - t)P(C_{ij} \geq t)I(t \leq T_{fmax}).$$

Let H denote the distribution function of the enrollment time, and G_i denote the survival function of the dropout time for treatment group i. By the change of variables, we have

$$E\left(\frac{\lambda_i t_{ij}}{1+\kappa_i\lambda_i t_{ij}}\right) = \int_0^{\tau\wedge T_{fmax}} \frac{\lambda_i}{(1+\kappa_i\lambda_i t)^2} H(\tau-t)G_i(t)dt.$$

A numerical integration algorithm for a univariate function can be used to evaluate the above integral.

For the restricted maximum likelihood (reml) estimate of (β_1, β_2) subject to the constraint that $\beta_1 - \beta_2 = \Delta$, we express the log-likelihood in terms of $(\beta_2, \Delta, \kappa_1, \kappa_2)$, and takes the derivative of the log-likelihood function with respect to β_2. The resulting score equation has asymptotic limit

$$E\left(\frac{\partial l}{\partial \beta_2}\right) = s_1 + s_2,$$

where

$$s_1 = nrE\left\{\lambda 1_1 t_{1j} - \left(\lambda_1 t_{1j} + \frac{1}{\kappa_1}\right)\frac{\kappa_1 e^{\tilde{\beta}_2+\Delta} t_{1j}}{1+\kappa_1 e^{\tilde{\beta}_2+\Delta} t_{1j}}\right\},$$

and

$$s_2 = n(1-r)E\left\{\lambda_2 t_{2j} - \left(\lambda_2 t_{2j} + \frac{1}{\kappa_2}\right)\frac{\kappa_2 e^{\tilde{\beta}_2} t_{2j}}{1+\kappa_2 e^{\tilde{\beta}_2} t_{2j}}\right\}.$$

Here r is the randomization probability for the active treatment group. The asymptotic limit of the reml of β_2 is the solution $\tilde{\beta}_2$ to $E\left(\frac{\partial l}{\partial \beta_2}\right) = 0$.

Value

A list with two components:

- `resultsUnderH1`: A data frame containing the following variables:
  - `time`: The analysis time since trial start.
  - `subjects`: The number of enrolled subjects.
  - `nevents`: The total number of events.
  - `nevents1`: The number of events in the active treatment group.
  - `nevents2`: The number of events in the control group.
  - `ndropouts`: The total number of dropouts.
  - `ndropouts1`: The number of dropouts in the active treatment group.
  - `ndropouts2`: The number of dropouts in the control group.
  - `nfmax`: The total number of subjects reaching maximum follow-up.
  - `nfmax1`: The number of subjects reaching maximum follow-up in the active treatment group.
  - `nfmax2`: The number of subjects reaching maximum follow-up in the control group.
  - `exposure`: The total exposure time.
  - `exposure1`: The exposure time for the active treatment group.
  - `exposure2`: The exposure time for the control group.
  - `information1`: The Fisher information for the log rate parameter for the active treatment group.

  - information2: The Fisher information for the log rate parameter for the control group.
  - rateRatio: The rate ratio of the active treatment group versus the control group.
  - vlogRR: The variance of log rate ratio.
  - information: The information of log rate ratio.
  - zlogRR: The Z-statistic for log rate ratio.
- resultsUnderH0 when nullVariance = TRUE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - lambda1H0: The restricted maximum likelihood estimate of the event rate for the active treatment group.
  - lambda2H0: The restricted maximum likelihood estimate of the event rate for the control group.
  - information1H0: The Fisher information for the log rate parameter for the active treatment group under H0.
  - information2H0: The Fisher information for the log rate parameter for the control group under H0.
  - vlogRRH0: The variance of log rate ratio under H0.
  - informationH0: The information of log rate ratio under H0.
  - zlogRRH0: The Z-statistic for log rate ratio under H0.
  - varianceRatio: The ratio of the variance under H0 versus the variance under H1.
  - rateRatioH0: The rate ratio under H0.
  - lambda1: The true event rate for the active treatment group.
  - lambda2: The true event rate for the control group.
  - rateRatio: The true rate ratio.
- resultsUnderH0 when nullVariance = FALSE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - varianceRatio: Equal to 1.
  - rateRatioH0: The rate ratio under H0.
  - lambda1: The true event rate for the active treatment group.
  - lambda2: The true event rate for the control group.
  - rateRatio: The true rate ratio.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: Variable follow-up design

nbstat(time = c(1, 1.25, 2, 3, 4),
       accrualIntensity = 1956/1.25,
       kappa1 = 5,
       kappa2 = 5,
       lambda1 = 0.7*0.125,
       lambda2 = 0.125,
```

```
       gamma1 = 0,
       gamma2 = 0,
       accrualDuration = 1.25,
       followupTime = 2.75)

# Example 2: Fixed follow-up design

nbstat(time = c(0.5, 1, 1.5, 2),
       accrualIntensity = 220/1.5,
       kappa1 = 3,
       kappa2 = 3,
       lambda1 = 0.5*8.4,
       lambda2 = 8.4,
       gamma1 = 0,
       gamma2 = 0,
       accrualDuration = 1.5,
       followupTime = 0.5,
       fixedFollowup = 1,
       nullVariance = 1)
```

`ptpwexp` *Distribution function of truncated piecewise exponential distribution*

Description

Obtains the probability of a truncated piecewise exponential distribution.

Usage

```
ptpwexp(q, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

Arguments

`q`	The vector of quantiles.
`piecewiseSurvivalTime`	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`lambda`	A vector of hazard rates for the event. One for each analysis time interval.
`lowerBound`	The left truncation time point for the survival time. Defaults to 0 for no truncation.

Value

The probability p such that P(X > q | X > lowerBound) = 1 - p.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
ptpwexp(q = c(8, 18), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

qtpwexp *Quantile function of truncated piecewise exponential distribution*

Description

Obtains the quantile of a truncated piecewise exponential distribution.

Usage

```
qtpwexp(p, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

Arguments

p	The vector of probabilities.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.
lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.

Value

The quantile q such that P(X > q | X > lowerBound) = 1 - p.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
qtpwexp(p = c(0.205, 0.317), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

remlOddsRatio — *REML estimates of individual proportions with specified odds ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified odds ratio.

Usage

```
remlOddsRatio(oddsRatioH0, n1, y1, n2, y2)
```

Arguments

oddsRatioH0	The specified odds ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlOddsRatio(oddsRatioH0 = 1.25, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

remlRateDiff — *REML estimates of individual rates with specified rate difference*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate difference.

Usage

```
remlRateDiff(rateDiffH0, t1, y1, t2, y2)
```

Arguments

rateDiffH0	The specified rate difference.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRateDiff(rateDiffH0 = 0.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

---

remlRateRatio *REML estimates of individual rates with specified rate ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate ratio.

Usage

```
remlRateRatio(rateRatioH0, t1, y1, t2, y2)
```

Arguments

rateRatioH0	The specified rate ratio.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRateRatio(rateRatioH0 = 1.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

`remlRiskDiff` *REML estimates of individual proportions with specified risk difference*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk difference.

Usage

```
remlRiskDiff(riskDiffH0, n1, y1, n2, y2)
```

Arguments

`riskDiffH0`	The specified risk difference.
`n1`	The sample size for the active treatment group.
`y1`	The number of responses for the active treatment group.
`n2`	The sample size for the control group.
`y2`	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRiskDiff(riskDiffH0 = 0.1, n1 = 10, y1 = 4, n2 = 20, y2 = 0)
```

remlRiskRatio *REML estimates of individual proportions with specified risk ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk ratio.

Usage

```
remlRiskRatio(riskRatioH0, n1, y1, n2, y2)
```

Arguments

riskRatioH0	The specified risk ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRiskRatio(riskRatioH0 = 1.2, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

repeatedPValue *Repeated p-values for group sequential design*

Description

Obtains the repeated p-values for a group sequential design.

Usage

```
repeatedPValue(
  kMax,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  maxInformation = 1,
  p,
  information,
  spendingTime = NULL
)
```

Arguments

kMax	The maximum number of stages.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
maxInformation	The target maximum information. Defaults to 1, in which case, information represents informationRates.
p	The raw p-values at look 1 to look k. It can be a matrix with k columns for k <= kMax.
information	The observed information by look. It can be a matrix with k columns.
spendingTime	The error spending time at each analysis, must be increasing and less than or equal to 1. Defaults to NULL, in which case, it is the same as informationRates derived from information and maxInformation. It can be a matrix with k columns.

Value

The repeated p-values at look 1 to look k.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: informationRates different from spendingTime
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
```

```
                maxInformation = 800,
                p = c(0.2, 0.15, 0.1),
                information = c(529, 700, 800),
                spendingTime = c(0.6271186, 0.8305085, 1))

# Example 2: Maurer & Bretz (2013), current look is not the last look
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
                p = matrix(c(0.0062, 0.017,
                             0.009, 0.13,
                             0.0002, 0.0035,
                             0.002, 0.06),
                           nrow=4, ncol=2),
                information = c(1/3, 2/3))
```

`rtpwexp` *Random number generation function of truncated piecewise exponential distribution*

Description

Obtains random samples from a truncated piecewise exponential distribution.

Usage

```
rtpwexp(n, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

Arguments

`n`	The number of observations.
`piecewiseSurvivalTime`	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`lambda`	A vector of hazard rates for the event. One for each analysis time interval.
`lowerBound`	The left truncation time point for the survival time. Defaults to 0 for no truncation.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
rtpwexp(n = 10, piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

runShinyApp *Run Shiny app*

Description

Runs the log-rank test power and sample size calculation Shiny app.

Usage

```
runShinyApp()
```

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

simon2stage *Simon's two-stage design*

Description

Obtains Simon's two-stage minimax, admissible, and optimal designs.

Usage

```
simon2stage(alpha, beta, piH0, pi, n_max = 110L)
```

Arguments

alpha	Type I error rate (one-sided).
beta	Type II error rate (1-power).
piH0	Response probability under the null hypothesis.
pi	Response probability under the alternative hypothesis.
n_max	Upper limit for sample size, defaults to 110.

Value

A data frame containing the following variables:

- piH0: Response probability under the null hypothesis.
- pi: Response probability under the alternative hypothesis.
- alpha: The specified one-sided significance level.
- beta: The specified type II error.
- n: Total sample size.

- n1: Stage 1 sample size.
- r1: Futility boundary for stage 1.
- r: Futility boundary for stage 2.
- EN0: Expected sample size under the null hypothesis.
- attainedAlpha: Attained type 1 error.
- power: Attained power.
- PET0: Probability of early stopping under the null hypothesis.
- w_lower: Lower bound of the interval for w.
- w_upper: Upper bound of the interval for w.
- design: Description of the design, e.g., minimax, admissible, or optimal.

Here w is the weight in the objective function: w*n + (1-w)*EN0.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
simon2stage(0.05, 0.15, 0.1, 0.3)
```

---

survQuantile *Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data*

Description

Obtains the Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data.

Usage

```
survQuantile(
  time = NA_real_,
  event = NA_real_,
  cilevel = 0.95,
  transform = "loglog",
  probs = c(0.25, 0.5, 0.75)
)
```

Arguments

time	The vector of possibly right-censored survival times.
event	The vector of event indicators.
cilevel	The confidence interval level. Defaults to 0.95.
transform	The transformation of the survival function to use to construct the confidence interval. Options include "linear", "loglog", "log", "asinsqrt", and "logit". Defaults to "loglog".
probs	The vector of probabilities to calculate the quantiles. Defaults to c(0.25, 0.5, 0.75).

Value

A data frame containing the estimated quantile and confidence interval corresponding to each specified probability. It includes the following variables:

- prob: The probability to calculate the quantile.
- quantile: The estimated quantile.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.
- transform: The transformation of the survival function to use to construct the confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
survQuantile(
  time = c(33.7, 3.9, 10.5, 5.4, 19.5, 23.8, 7.9, 16.9, 16.6,
           33.7, 17.1, 7.9, 10.5, 38),
  event = c(0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1),
  probs = c(0.25, 0.5, 0.75))
```

---

updateGraph *Update graph for graphical approaches*

Description

Updates the weights and transition matrix for graphical approaches.

Usage

```
updateGraph(w, G, I, j)
```

Arguments

w	The current vector of weights for elementary hypotheses.
G	The current transition matrix.
I	The set of indices for yet to be rejected hypotheses.
j	The hypothesis to remove from index set I.

Value

A list containing the new vector of weights, the new transition matrix for the graph, and the new set of indices of yet to be rejected hypotheses.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
updateGraph(w = c(0.5, 0.5, 0, 0),
            G = matrix(c(0, 0.5, 0.5, 0,  0.5, 0, 0, 0.5,
                         0, 1, 0, 0,  1, 0, 0, 0),
                       nrow=4, ncol=4, byrow=TRUE),
            I = c(1, 2, 3, 4),
            j = 1)
```

Index

accrual, 4
adaptDesign, 5, *29*, *33*

BOINTable, 9

caltime, 11
ClopperPearsonCI, 13

errorSpent, 14
exitprob, 15

fadjpbon, 16
fadjpdun, 17
fadjpsim, 18
fmodmix, 19
fseqbon, 20
fstdmix, 22
fstp2seq, 24
ftrunc, 25
fwgtmat, 26

getAccrualDurationFromN, 26
getADCI, 27
getADRCI, 31
getBound, 34
getCI, 35
getCP, 37
getDesign, *9*, *40*, 42
getDesignAgreement, 45
getDesignANOVA, 47
getDesignANOVAContrast, 49
getDesignEquiv, 51
getDesignFisherExact, 56
getDesignLogistic, 57
getDesignMeanDiff, 60
getDesignMeanDiffCarryover, 64
getDesignMeanDiffEquiv, 67
getDesignMeanDiffMMRM, 70
getDesignMeanDiffXO, 72
getDesignMeanDiffXOEquiv, 76
getDesignMeanRatio, 79
getDesignMeanRatioEquiv, 82
getDesignMeanRatioXO, 85
getDesignMeanRatioXOEquiv, 89
getDesignOddsRatio, 92
getDesignOddsRatioEquiv, 95
getDesignOneMean, 98
getDesignOneMultinom, 102
getDesignOneProportion, 103
getDesignOneRateExact, 107
getDesignOneSlope, 108
getDesignOrderedBinom, 112
getDesignPairedMeanDiff, 113
getDesignPairedMeanDiffEquiv, 117
getDesignPairedMeanRatio, 119
getDesignPairedMeanRatioEquiv, 123
getDesignPairedPropMcNemar, 126
getDesignRepeatedANOVA, 129
getDesignRepeatedANOVAContrast, 131
getDesignRiskDiff, 133
getDesignRiskDiffEquiv, 136
getDesignRiskDiffExact, 139
getDesignRiskDiffExactEquiv, 141
getDesignRiskRatio, 142
getDesignRiskRatioEquiv, 146
getDesignRiskRatioExact, 149
getDesignRiskRatioExactEquiv, 150
getDesignRiskRatioFM, 152
getDesignSlopeDiff, 155
getDesignSlopeDiffMMRM, 159
getDesignTwoMultinom, 162
getDesignTwoOrdinal, 163
getDesignTwoWayANOVA, 165
getDesignUnorderedBinom, 166
getDesignUnorderedMultinom, 168
getDesignWilcoxon, 169
getDurationFromNevents, 173
getNeventsFromHazardRatio, 175
getRCI, 177

hedgesg, 179

kmest, 181

lrpower, 183, *191*
lrsamplesize, 188
lrsim, 192
lrsim2e, 197
lrsim2e3a, 201
lrsim3a, 206
lrstat, 210

mnOddsRatioCI, 213
mnRateDiffCI, 214
mnRateRatioCI, 215
mnRiskDiffCI, 217
mnRiskRatioCI, 218
mTPI2Table, 219

nbpower, 220, *236*
nbpower1s, 225, *240*
nbpowerequiv, 229, *243*
nbsamplesize, 233
nbsamplesize1s, 237
nbsamplesizeequiv, 240
nbstat, *224*, *228*, *233*, 243

ptpwexp, 248

qtpwexp, 249

remlOddsRatio, 250
remlRateDiff, 250
remlRateRatio, 251
remlRiskDiff, 252
remlRiskRatio, 253
repeatedPValue, 253
rtpwexp, 255
runShinyApp, 256

simon2stage, 256
survQuantile, 257

updateGraph, 258