

Package ‘matchingMarkets’

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VignetteBuilder knitr

Title Analysis of Stable Matchings

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Description Implements structural estimators to correct for the sample selection bias from observed outcomes in matching markets. This includes one-sided matching of agents into groups as well as two-sided matching of students to schools. The package also contains algorithms to find stable matchings in the three most common matching problems: the stable roommates problem, the college admissions problem, and the house allocation problem.

URL <http://matchingMarkets.org>, <http://klein.uk>

BugReports <https://github.com/thiloklein/matchingMarkets/issues>

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R topics documented:

matchingMarkets-package	2
baac00	4
hri	5
hri2	8
iaa	10
khb	11
klein15a	12
klein15b	13
mce	14
plp	16
predict.stabit2	17
sri	18
stabit	19
stabit2	23
stabsim	26
stabsim2	27
ttc	29
Index	30

matchingMarkets-package

An R package for the analysis of stable matchings.

Description

The matchingMarkets package contains R, C++ and Java code for stable matching algorithms and the estimation of structural models that correct for the sample selection bias of observed outcomes in matching markets.

Matching is concerned with who transacts with whom, and how. For example, who works at which job, which students go to which school, who forms a workgroup with whom, and so on.

The empirical analysis of matching markets is naturally subject to sample selection problems. If agents match assortatively on characteristics unobserved to the analyst but correlated with both the exogenous variable and the outcome of interest, regression estimates will generally be biased.

The matchingMarkets package comprises

1. *Bayes estimators.* The estimators implemented in function `stabit` and `stabit2` correct for the selection bias from endogenous matching.
The current package version provides solutions for two commonly observed matching processes: (i) the *group formation problem* with fixed group sizes and (ii) the *college admissions problem*. These processes determine which matches are observed – and which are not – and this is a sample selection problem.
2. *Post-estimation tools.* Setting `mfX=TRUE` in the summary function computes marginal effects from coefficients in binary outcome and selection equations and `khb` implements the Karlson-Holm-Breen test for confounding due to sample selection.

3. *Design matrix generation.* The estimators are based on independent variables for all feasible, i.e., observed and counterfactual, matches in the market. Generating the characteristics of all feasible matches from individual-level data is a combinatorial problem. The package returns design matrices based on pre-specified transformations to generate counterfactual matches.
4. *Algorithms.* The package also contains three matching algorithms that can be used to simulated matching data: `hri`: A constraint model (Posser, 2014) for the **stable marriage** and **college admissions** problem, a.k.a. hospital/residents problem (see Gale and Shapley, 1962). `sri`: A constraint model for the **stable roommates problem** (see Gusfield and Irving, 1989). `ttc`: The top-trading-cycles algorithm for the **housing market problem**. These can be used to obtain stable matchings from simulated or real preference data (see Shapley and Scarf, 1974).
5. *Data.* In addition to the `baac00` dataset from borrowing groups in Thailand's largest agricultural lending program, the package provides functions `stabsim` and `stabsim2` to simulate one's own data from one-sided and two-sided matching markets.

Frequently Asked Questions

- *Why can I not use the classic Heckman correction?*

Estimators such as the Heckman (1979) correction (in package `sampleSelection`) or double selection models are inappropriate for this class of selection problems. To see this, note that a simple first stage discrete choice model assumes that an observed match reveals match partners' preferences over each other. In a matching market, however, agents can only choose from the set of partners who would be willing to form a match with them and we do not observe the players' relevant choice sets.

- *Do I need an instrumental variable to estimate the model?*

Short answer: No. Long answer: The characteristics of other agents in the market serve as the source of exogenous variation necessary to identify the model. The identifying exclusion restriction is that characteristics of all agents in the market affect the matching, i.e., who matches with whom, but it is only the characteristics of the match partners that affect the outcome of a particular match once it is formed. No additional instruments are required for identification (Sorensen, 2007).

- *What are the main assumptions underlying the estimator?*

The approach has certain limitations rooted in its restrictive economic assumptions.

1. The matching models are *complete information* models. That is, agents are assumed to have a complete knowledge of the qualities of other market participants.
2. The models are *static equilibrium* models. This implies that (i) the observed matching must be an equilibrium, i.e., no two agents would prefer to leave their current partners in order to form a new match (definition of pairwise stability), and (ii) the equilibrium must be unique for the likelihood function of the model to be well defined (Bresnahan and Reiss, 1991).
3. Uniqueness results can be obtained in two ways. First, as is common in the industrial organization literature, by imposing suitable *preference restrictions*. A suitable restriction on agents' preferences that guarantees a unique equilibrium is alignment (Pycia, 2012). In a group formation model, (pairwise) preference alignment states that any two agents who belong to the same groups must prefer the same group over the other. Second, by choosing a *market assignment* based on matching algorithms that produce a unique stable matching, such as the well-studied Gale and Shapley (1962) deferred acceptance algorithm.

4. Finally, the models assume *bivariate normality* of the errors in selection and outcome equation. If that assumption fails, the estimator is generally inconsistent and can provide misleading inference in small samples.

How to cite this package

Whenever using this package, please cite as

Klein, T. (2018). `matchingMarkets`: Structural Estimator and Algorithms for the Analysis of Stable Matchings. R package version 0.3-5.

Author(s)

Thilo Klein

References

- Bresnahan, T. and Reiss, P. (1991). Empirical models of discrete games. *Journal of Econometrics*, 48(1-2):57–81.
- Gale, D. and Shapley, L.S. (1962). College admissions and the stability of marriage. *The American Mathematical Monthly*, 69(1):9–15.
- Gusfield, D.M. and R.W. Irving (1989). The stable marriage problem: Structure and algorithms, MIT Press.
- Heckman, J. (1979). Sample selection bias as a specification error. *Econometrica*, 47(1):153–161.
- Prosser, P. (2014). Stable Roommates and Constraint Programming. *Lecture Notes in Computer Science, CPAIOR 2014 Edition*. Springer International Publishing, 8451: 15–28.
- Pycia, M. (2012). Stability and preference alignment in matching and coalition formation. *Econometrica*, 80(1):323–362.
- Shapley, L. and H. Scarf (1974). On cores and indivisibility. *Journal of Mathematical Economics*, 1(1):23–37.
- Sorensen, M. (2007). How smart is smart money? A two-sided matching model of venture capital. *The Journal of Finance*, 62(6):2725–2762.

See Also

[sampleSelection](#)

baac00

Townsend Thai Project BAAC Annual Resurvey, 2000

Description

The `baac00` data frame contains data of 292 borrowers from Thailand’s largest agricultural lending program. These data are collected as part of the Townsend Thai Project Bank for Agriculture and Agricultural Cooperatives (BAAC) Annual Resurvey (Townsend, 2000). The 292 borrowers are nested within 68 groups and 39 markets. This nestedness makes the dataset particularly relevant for matching applications. A more complete discussion of the data is found in Ahlin (2009), Section 3, and Klein (2015a).

Usage

```
data(baac00)
```

Format

This data frame contains the following columns:

g.id group identifier.

m.id market identifier.

R repayment outcome: BAAC never raised interest rate as a penalty for late repayment.

pi success probability: measure of group members' project success probability.

wst worst year: indicator of economically worst year. 1:last year; 2:year before last year; 101-168:neither.

loan_size loan size: average loan size borrowed by the group.

loan_size2 loan size squared.

ingroup_agei log group age: log of number of years group has existed.

Source

Townsend, R. (2000). Townsend Thai Project Bank for Agriculture and Agricultural Cooperatives (BAAC) Annual Resurvey, 2000. Available at <http://hdl.handle.net/1902.1/12057>, *Murray Research Archive*.

References

Ahlin, C. (2009). Matching for credit: Risk and diversification in Thai microcredit groups. Working Paper 251, *Bureau for Research and Economic Analysis of Development*.

Klein, T. (2015a). *Does Anti-Diversification Pay? A One-Sided Matching Model of Microcredit*. *Cambridge Working Papers in Economics*, #1521.

hri

All stable matchings in the hospital/residents problem with incomplete lists

Description

Finds *all* stable matchings in either the **hospital/residents** problem (a.k.a. college admissions problem) or the related **stable marriage** problem. Dependent on the problem, the results comprise the student and college-optimal or the men and women-optimal matchings. The implementation allows for *incomplete preference lists* (some agents find certain agents unacceptable) and *unbalanced instances* (unequal number of agents on both sides). The function uses the Prosser (2014) constraint encoding based on either given or randomly generated preferences.

Usage

```
hri(nStudents = ncol(s.prefs), nColleges = ncol(c.prefs), nSlots = rep(1,
  nColleges), s.prefs = NULL, c.prefs = NULL, seed = NULL,
  s.range = NULL, c.range = NULL, ...)
```

Arguments

nStudents	integer indicating the number of students (in the college admissions problem) or men (in the stable marriage problem) in the market. Defaults to <code>ncol(s.prefs)</code> .
nColleges	integer indicating the number of colleges (in the college admissions problem) or women (in the stable marriage problem) in the market. Defaults to <code>ncol(c.prefs)</code> .
nSlots	vector of length <code>nColleges</code> indicating the number of places (i.e. quota) of each college. Defaults to <code>rep(1, nColleges)</code> for the marriage problem.
s.prefs	matrix of dimension <code>nColleges</code> x <code>nStudents</code> with the <code>j</code> th column containing student <code>j</code> 's ranking over colleges in decreasing order of preference (i.e. most preferred first).
c.prefs	matrix of dimension <code>nStudents</code> x <code>nColleges</code> with the <code>i</code> th column containing college <code>i</code> 's ranking over students in decreasing order of preference (i.e. most preferred first).
seed	integer setting the state for random number generation.
s.range	range of two integers <code>s.range = c(s.min, s.max)</code> , where <code>s.min < s.max</code> . Produces incomplete preference lists with the length of each student's list randomly sampled from the range <code>[s.min, s.max]</code> . Note: interval is only correct if either <code>c.range</code> or <code>s.range</code> is used.
c.range	range of two integers <code>c.range = c(c.min, c.max)</code> , where <code>c.min < c.max</code> . Produces incomplete preference lists with the length of each college's list randomly sampled from the range <code>[c.min, c.max]</code> . Note: interval is only correct if either <code>c.range</code> or <code>s.range</code> is used.
...	.

Value

`hri` returns a list of the following elements.

<code>s.prefs.smi</code>	student-side preference matrix for the stable marriage problem with incomplete lists (SMI).
<code>c.prefs.smi</code>	college-side preference matrix for the stable marriage problem with incomplete lists (SMI).
<code>s.prefs.hri</code>	student-side preference matrix for the college admissions problem (a.k.a. hospital/residents problem) with incomplete lists (HRI).
<code>c.prefs.hri</code>	college-side preference matrix for the college admissions problem (a.k.a. hospital/residents problem) with incomplete lists (HRI).
<code>matchings</code>	edgelist of matched students and colleges, including the number of the match (<code>matching</code>) and two variables that indicate the student-optimal match (<code>sOptimal</code>) and college-optimal match (<code>cOptimal</code>)
.	.

Minimum required arguments

hri requires the following combination of arguments, subject to the matching problem.

nStudents, nColleges Marriage problem with random preferences.

s.prefs, c.prefs Marriage problem with given preferences.

nStudents, nSlots College admissions problem with random preferences.

s.prefs, c.prefs, nSlots College admissions problem with given preferences.

Author(s)

Thilo Klein

References

Gale, D. and L.S. Shapley (1962). College admissions and the stability of marriage. *The American Mathematical Monthly*, 69(1):9–15.

Morizumi, Y., T. Hayashi and Y. Ishida (2011). A network visualization of stable matching in the stable marriage problem. *Artificial Life Robotics*, 16:40–43.

Prosser, P. (2014). Stable Roommates and Constraint Programming. *Lecture Notes in Computer Science, CPAIOR 2014 Edition*. Springer International Publishing, 8451: 15–28.

Examples

```
## -----
## --- Marriage problem

## 3 men, 2 women, random preferences:
hri(nStudents=7, nColleges=6, seed=4)

## 3 men, 2 women, given preferences:
s.prefs <- matrix(c(1,2, 1,2, 1,2), 2,3)
c.prefs <- matrix(c(1,2,3, 1,2,3), 3,2)
hri(s.prefs=s.prefs, c.prefs=c.prefs)

## -----
## --- College admission problem

## 7 students, 2 colleges with 3 slots each, random preferences:
hri(nStudents=7, nSlots=c(3,3), seed=21)

## 7 students, 2 colleges with 3 slots each, given preferences:
s.prefs <- matrix(c(1,2, 1,2, 1,NA, 1,2, 1,2, 1,2, 1,2), 2,7)
c.prefs <- matrix(c(1,2,3,4,5,6,7, 1,2,3,4,5,NA,NA), 7,2)
hri(s.prefs=s.prefs, c.prefs=c.prefs, nSlots=c(3,3))

## 7 students, 3 colleges with 3 slots each, incomplete preferences:
hri(nStudents=7, nSlots=c(3,3,3), seed=21, s.range=c(1,3))

## -----
## --- Summary plots
```

```
## Not run:
## 200 students, 200 colleges with 1 slot each
res <- hri(nStudents=200, nColleges=200, seed=12)
plot(res)
plot(res, energy=TRUE)

## End(Not run)
```

hri2	<i>Resident-optimal matching in the hospital/residents problem with couples</i>
------	---

Description

Implements the Roth Peranson matching algorithm for the **hospital/residents problem with couples** as described in Roth and Peranson (1999). The function is based on a adoption of Fahiem Bacchus's **stable-matching-suite**.

Usage

```
hri2(nStudents = ncol(s.prefs), nColleges = ncol(c.prefs), nSlots = rep(1,
  nColleges), nCouples = ncol(co.prefs), s.prefs = NULL, c.prefs = NULL,
  co.prefs = NULL, seed = NULL, ...)
```

Arguments

nStudents	integer indicating the number of students (in the college admissions problem) or men (in the stable marriage problem) in the market. Defaults to <code>ncol(s.prefs)</code> .
nColleges	integer indicating the number of colleges (in the college admissions problem) or women (in the stable marriage problem) in the market. Defaults to <code>ncol(c.prefs)</code> .
nSlots	vector of length <code>nColleges</code> indicating the number of places (i.e. quota) of each college. Defaults to <code>rep(1, nColleges)</code> for the marriage problem.
nCouples	integer indicating the number of couples (in the college admissions problem) or men (in the stable marriage problem) in the market. Defaults to <code>ncol(co.prefs)</code> .
s.prefs	matrix of dimension <code>nColleges x nStudents</code> with the <code>j</code> th column containing student <code>j</code> 's ranking over colleges in decreasing order of preference (i.e. most preferred first).
c.prefs	matrix of dimension <code>nStudents x nColleges</code> with the <code>i</code> th column containing college <code>i</code> 's ranking over students in decreasing order of preference (i.e. most preferred first).
co.prefs	matrix of dimension <code>4 x nCouples</code> in long format with the 1th and 2th columns containing student couple id's; 3th and 4th is a 2-tuple ranking over college preference for the couple (<code>coupleStudent1.pref</code> , <code>coupleStudent2.pref</code>) in decreasing order of preference by rows (i.e. most preferred first).
seed	integer setting the state for random number generation.
...	.

Value

hri2 returns a list of the following elements:

matchings	list of matched students and colleges.
summary	detailed report of the matching result, including further information on ranks. See function: summary.hrci(x)

Minimum required arguments

hri2 requires the following combination of arguments, subject to the matching problem.

nStudents, nColleges Residence hospital problem without couples and random preferences

nStudents, nColleges, nCouples, nSlots Residence hospital problem with couples and random preferences.

s.prefs, c.prefs, co.prefs, nSlots Residence hospital problem with couples and given preferences.

Author(s)

Sven Giegerich, Thilo Klein

References

Gale, D. and L.S. Shapley (1962). College admissions and the stability of marriage. *The American Mathematical Monthly*, 69(1):9–15.

Roth, A. E., & Peranson, E. (1999). The redesign of the matching market for American physicians: Some engineering aspects of economic design. *American economic review*, 89(4), 748-780.

Kojima, F., Pathak, P. A., & Roth, A. E. (2013). Matching with couples: Stability and incentives in large markets. *The Quarterly Journal of Economics*, 128(4), 1585-1632.

Examples

```
## Example with given preferences
s.prefs <- matrix(c(4,2,3,5,1, 2,1,3,4,5, 1,2,3,4,5), 5,3)
c.prefs <- matrix(c(1,2,3, 1,2,3, 1,2,3, 1,2,3, 1,2,3), 3,5)
co.prefs <- matrix(c(4,4,4,4,4,4,4,5,5,5,5,5,5,5, 1,2,1,2,3,3,4,3, 1,1,2,2,2,3,3,4), 8,4)
res <- hri2(s.prefs=s.prefs, c.prefs=c.prefs, co.prefs=co.prefs, nSlots=c(1,1,1,1))
res$matchings
# summary(res)

## Example with random preferences
nStudents <- 50
nColleges <- 30
nCouples <- 4
nSlots <- sample(1:nStudents, nColleges)
res <- hri2(nStudents=nStudents, nColleges=nColleges, nCouples=nCouples, nSlots=nSlots)
res$matchings
# summary(res)
```

iaa	<i>Immediate Acceptance Algorithm (a.k.a. Boston mechanism) for two-sided matching markets</i>
-----	--

Description

Finds the optimal assignment of students to colleges in the **college admissions** problem based on the Boston mechanism. The option `acceptance="deferred"` instead uses the Gale-Shapley (1962) Deferred Acceptance Algorithm with male offer. The function works with either given or randomly generated preferences.

Usage

```
iaa(nStudents = ncol(s.prefs), nColleges = ncol(c.prefs), nSlots = rep(1,
  nColleges), s.prefs = NULL, c.prefs = NULL, acceptance = "immediate")
```

Arguments

<code>nStudents</code>	integer indicating the number of students (in the college admissions problem) or men (in the stable marriage problem) in the market. Defaults to <code>ncol(s.prefs)</code> .
<code>nColleges</code>	integer indicating the number of colleges (in the college admissions problem) or women (in the stable marriage problem) in the market. Defaults to <code>ncol(c.prefs)</code> .
<code>nSlots</code>	vector of length <code>nColleges</code> indicating the number of places (i.e. quota) of each college. Defaults to <code>rep(1, nColleges)</code> for the marriage problem.
<code>s.prefs</code>	matrix of dimension <code>nColleges x nStudents</code> with the <code>j</code> th column containing student <code>j</code> 's ranking over colleges in decreasing order of preference (i.e. most preferred first).
<code>c.prefs</code>	matrix of dimension <code>nStudents x nColleges</code> with the <code>i</code> th column containing college <code>i</code> 's ranking over students in decreasing order of preference (i.e. most preferred first).
<code>acceptance</code>	if <code>acceptance="deferred"</code> returns the solution found by the student-proposing Gale-Shapley deferred acceptance algorithm; if <code>acceptance="immediate"</code> (the default) returns the solution found by the Boston mechanism.

Value

`iaa` returns a list with the following elements.

<code>s.prefs</code>	student-side preference matrix.
<code>c.prefs</code>	college-side preference matrix.
<code>iterations</code>	number of iterations required to find the stable matching.
<code>matchings</code>	edgelist of matches
<code>singles</code>	identifier of single (or unmatched) students/men.

Minimum required arguments

iaa requires the following combination of arguments, subject to the matching problem.

nStudents, nColleges Marriage problem with random preferences.

s.prefs, c.prefs Marriage problem with given preferences.

nStudents, nSlots College admissions problem with random preferences.

s.prefs, c.prefs, nSlots College admissions problem with given preferences.

Author(s)

Thilo Klein

References

Gale, D. and Shapley, L.S. (1962). College admissions and the stability of marriage. *The American Mathematical Monthly*, 69(1):9–15.

Kojima, F. and M.U. Unver (2014). The "Boston" school-choice mechanism. *Economic Theory*, 55(3): 515–544.

Examples

```
## -----
## --- College admission problem

## Boston mechanism for 7 students, 2 colleges with 3 slots each
set.seed(123)
iaa(nStudents=7, nSlots=c(3,3))

## Gale-Shapley algorithm
set.seed(123)
iaa(nStudents=7, nSlots=c(3,3), acceptance="deferred")

## Same results for the Gale-Shapley algorithm with hri() function
set.seed(123)
hri(nStudents=7, nSlots=c(3,3))

## 7 students, 2 colleges with 3 slots each, given preferences:
s.prefs <- matrix(c(1,2, 1,2, 1,2, 1,2, 1,2, 1,2, 1,2), 2,7)
c.prefs <- matrix(c(1,2,3,4,5,6,7, 1,2,3,4,5,6,7), 7,2)
iaa(s.prefs=s.prefs, c.prefs=c.prefs, nSlots=c(3,3))
```

Description

Significance test for confounding; that is, the difference between regression coefficients from same-sample nested logit and probit models. The test procedure follows Karlson et al (2012), Section 3.4.

Usage

```
khb(X, y, z)
```

Arguments

X data frame comprising independent variables including confounding variable.
y vector of dependent variable.
z character string giving the name of the confounding variable in X.

Author(s)

Thilo Klein

References

Karlson, K.B., A. Holm and R. Breen (2012). Comparing regression coefficients between same-sample nested models using logit and probit: A new method. *Sociological Methodology*, 42(1):286–313.

Examples

```
## 1. load results from Klein (2015a)
data(klein15a)

## 2. apply KHB method
with(klein15a$variables, khb(X=X, y=Y, z="eta"))
```

klein15a	<i>MCMC results in Klein (2015a)</i>
----------	--------------------------------------

Description

MCMC results in Klein (2015a).

Usage

```
data(klein15a)
```

Format

A list containing the following elements:

model.list .
coefs .

References

Klein, T. (2015a). *Does Anti-Diversification Pay? A One-Sided Matching Model of Microcredit*. *Cambridge Working Papers in Economics*, #1521.

klein15b

Results of Monte Carlo Simulations in Klein (2015b)

Description

Results of Monte Carlo Simulations in Klein (2015b) for 40 two-group markets.

Usage

```
data(klein15b)
```

Format

A list containing the following elements:

exp.5.5.ols Benchmark study, OLS: coefficient estimates for 40 markets with groups of 5. Data for all 5 group members is observed.

exp.5.5.ntu Benchmark study, structural model.

exp.6.5.ols Experiment 1, OLS: coefficient estimates for 40 markets with groups of 6. Only Data for 5 group members is observed.

exp.6.5.ntu Experiment 1, structural model.

exp.6.6.ols Experiment 2, OLS: coefficient estimates for 40 markets with groups of 6. Data for all 6 group members is observed but only a random sample of 250 of the 922 counterfactual groups is used in the analysis.

exp.6.6.ntu Experiment 2, structural model.

References

Klein, T. (2015a). *Does Anti-Diversification Pay? A One-Sided Matching Model of Microcredit*. *Cambridge Working Papers in Economics*, #1521.

Klein, T. (2015b). *Analysis of stable matchings in R: Package matchingMarkets*. *Vignette to R package matchingMarkets*, The Comprehensive R Archive Network.

Examples

```
## Plot of posterior distributions

data(klein15b)

tpe <- c(rep("Benchmark",2), rep("Experiment 1",2), rep("Experiment 2",2))

for(i in seq(1,length(klein15b)-1,2)){
  ntu <- klein15b[[i]]
  ols <- klein15b[[i+1]]

  ntu <- ntu[,colnames(ntu) == "beta.wst.ieq"]
  ols <- ols[,colnames(ols) == "beta.wst.ieq"]
}
```

```

if(i == 1){
  draws <- data.frame(Structural=ntu, OLS=ols, type=tpe[i]) #, stringsAsFactors=FALSE
} else{
  draws <- rbind(draws, data.frame(Structural=ntu, OLS=ols, type=tpe[i]))
}
}

library(lattice)
lattice.options(default.theme = standard.theme(color = FALSE))
keys <- list(text=c("Structural model","OLS"), space="top", columns=2, lines=TRUE)
densityplot( ~ Structural + OLS | type, plot.points=FALSE, auto.key=keys,
  data = draws, xlab = "coefficient draws", ylab = "density", type = "l",
  panel = function(x,...) {
    panel.densityplot(x,...)
    panel.abline(v=-1, lty=3)
  })

## Not run:
## Modes of posterior distributions

## load data
data(klein15b)

## define function to obtain the mode
mode <- function(x){
  d <- density(x,bw="SJ")
  formatC(round(d$x[which.max(d$y)], 3), format='f', digits=3)
}

## Benchmark study
apply(klein15b$exp.5.5.ntu, 2, mode)
apply(klein15b$exp.5.5.ols, 2, mode)

## Experiment 1
apply(klein15b$exp.6.5.ntu, 2, mode)
apply(klein15b$exp.6.5.ols, 2, mode)

## Experiment 2
apply(klein15b$exp.6.6.ntu, 2, mode)
apply(klein15b$exp.6.6.ols, 2, mode)

## End(Not run)

```

Description

MC Experiments

Usage

```
mce(seed, niter, N, n, m, type, method)
```

Arguments

seed	seed value for Monte Carlo Experiment
niter	number of draws in estimation
N	group size (population)
n	group size (sample)
m	number of markets
type	type of the MC Experiment. Either <code>group.members</code> for randomly sampled group members or <code>counterfactual.groups</code> for randomly sampled number of counterfactual (or feasible) groups in selection equation (capped at limit <code>max.combs=250</code>)
method	either <code>group.members</code> or <code>counterfactual.groups</code>

Author(s)

Thilo Klein

Examples

```
## Not run:
## 1. Set parameters
mciter <- 2 #500
niter <- 10 #400000
nodes <- 4

## 2. Setup parallel backend to use 4 processors
library(foreach); library(doSNOW)
cl <- makeCluster(4); registerDoSNOW(cl)

## 3. Define foreach loop function
mce.add <- function(mciter, niter, N, n, m, type, method){
  h <- foreach(i=1:mciter) %dopar% {
    library(matchingMarkets)
    mce(seed=i,niter, N, n, m, type, method)
  }
  do.call(rbind, h)
}

## 4. Run simulations:

## 4-a. Benchmark study
exp.5.5.ols <- mce.add(mciter=mciter, niter=niter, N=5, n=5, m=40,
  type="group.members", method="outcome")
exp.5.5.ntu <- mce.add(mciter=mciter, niter=niter, N=5, n=5, m=40,
  type="group.members", method="NTU")

## 4-b. Experiment 1: randomly sampled group members
```

```

exp.6.5.ols <- mce.add(mciter=mciter, niter=niter, N=6, n=5, m=40,
                      type="group.members", method="outcome")
exp.6.5.ntu <- mce.add(mciter=mciter, niter=niter, N=6, n=5, m=40,
                      type="group.members", method="NTU")

## 4-c. Experiment 2: randomly sampled counterfactual groups
exp.6.6.ols <- mce.add(mciter=mciter, niter=niter, N=6, n=6, m=40,
                      type="counterfactual.groups", method="outcome")
exp.6.6.ntu <- mce.add(mciter=mciter, niter=niter, N=6, n=6, m=40,
                      type="counterfactual.groups", method="NTU")

## 5. Stop parallel backend
stopCluster(cl)

## End(Not run)

```

 plp

Partitioning Linear Programme for the stable roommates problem

Description

Finds the stable matching in the **stable roommates problem** with transferable utility. Uses the Partitioning Linear Programme formulated in Quint (1991).

Usage

```
plp(V = NULL, N = NULL)
```

Arguments

V	valuation matrix of dimension $N \times N$ that gives row-players valuation over column players (or vice versa).
N	integer (divisible by 2) that gives the number of players in the market.

Value

plp returns a list with the following items.

Valuation.matrix	input values of V.
Assignment.matrix	upper triangular matrix of dimension $N \times N$ with entries of 1 for equilibrium pairs and 0 otherwise.
Equilibrium.groups	matrix that gives the $N/2$ equilibrium pairs and equilibrium partners' mutual valuations.

Author(s)

Thilo Klein

References

Quint, T. (1991). Necessary and sufficient conditions for balancedness in partitioning games. *Mathematical Social Sciences*, 22(1):87–91.

Examples

```
## Roommate problem with 10 players, transferable utility and random preferences:
plp(N=10)

## Roommate problem with 10 players, transferable utility and given preferences:
V <- matrix(rep(1:10, 10), 10, 10)
plp(V=V)
```

predict.stabit2 *Predict method for fitted matching models*

Description

Calculate predicted values for matching models fitted with functions `stabit` and `stabit2`.

Usage

```
## S3 method for class 'stabit2'
predict(object, newdata = NULL, ...)
```

Arguments

<code>object</code>	a fitted object of class <code>stabit</code>
<code>newdata</code>	optionally, a data frame in which to look for variables with which to predict. If omitted, the fitted linear predictors or the fitted response values are returned.
<code>...</code>	.

Author(s)

Thilo Klein

References

Klein, T. (2015a). [Does Anti-Diversification Pay? A One-Sided Matching Model of Microcredit](#). *Cambridge Working Papers in Economics*, #1521.

Examples

```
## load the results from Klein (2015) paper
data(klein15a)

## predict the latent outcome variable
predict(klein15a)
```

sri	<i>All stable matchings in the stable roommates problem with incomplete lists</i>
-----	---

Description

Finds all stable matchings (if one exists) in the **stable roommates problem** with incomplete lists using the Prosser (2014) constraint encoding based on either given or randomly generated preferences.

Usage

```
sri(prefs = NULL, nAgents = NULL, seed = NULL, p.range = NULL)
```

Arguments

prefs	valuation matrix of dimension $nAgents \times nAgents$ that gives column-players' ranking over other players in decreasing order of preference (i.e. most preferred first).
nAgents	integer that gives the number of players in the market.
seed	integer setting the state for random number generation.
p.range	range of two integers $p.range = c(p.min, p.max)$, where $p.min < p.max$. Produces incomplete preference lists with the length of each player's list randomly sampled from the range $[p.min, p.max]$. Note: interval is always too small because non-permissible matches are automatically deleted.

Value

sri returns a list with the following items.

prefs	agents' preference list.
matching	edgelist of matched pairs, including the number of the match (matching).

Author(s)

Thilo Klein

References

- Gusfield, D.M. and R.W. Irving (1989). *The Stable Marriage Problem: Structure and Algorithms*, MIT Press.
- Prosser, P. (2014). *Stable Roommates and Constraint Programming. Lecture Notes in Computer Science, CPAIOR 2014 Edition*. Springer International Publishing, 8451: 15–28.
- Irving, R.W. and S. Scott (2007). The stable fixtures problem: A many-to-many extension of stable roommates. *Discrete Applied Mathematics*, 155: 2118–2129.

Examples

```
## Roommate problem with 10 players, given preferences:
prefs <- matrix(rep(1:10, 10), 10, 10)
sri(prefs=prefs)

## Roommate problem with 10 players, random preferences:
sri(nAgents=10, seed=1)

## Roommate problem with no equilibrium matching:
sri(nAgents=10, seed=2)

## Roommate problem with 3 equilibria:
sri(nAgents=10, seed=3)
```

stabit

Matching model and selection correction for group formation

Description

The function provides a Gibbs sampler for a structural matching model that estimates preferences and corrects for sample selection bias when the selection process is a one-sided matching game; that is, group/coalition formation.

The input is individual-level data of all group members from one-sided matching markets; that is, from group/coalition formation games.

In a first step, the function generates a model matrix with characteristics of *all feasible* groups of the same size as the observed groups in the market.

For example, in the stable roommates problem with $n = 4$ students $\{1, 2, 3, 4\}$ sorting into groups of 2, we have $\binom{4}{2} = 6$ feasible groups: (1,2)(3,4) (1,3)(2,4) (1,4)(2,3).

In the group formation problem with $n = 6$ students $\{1, 2, 3, 4, 5, 6\}$ sorting into groups of 3, we have $\binom{6}{3} = 20$ feasible groups. For the same students sorting into groups of sizes 2 and 4, we have $\binom{6}{2} + \binom{6}{4} = 30$ feasible groups.

The structural model consists of a selection and an outcome equation. The *Selection Equation* determines which matches are observed ($D = 1$) and which are not ($D = 0$).

$$\begin{aligned} D &= 1[V \in \Gamma] \\ V &= W\alpha + \eta \end{aligned}$$

Here, V is a vector of latent valuations of *all feasible* matches, ie observed and unobserved, and $1[\cdot]$ is the Iverson bracket. A match is observed if its match valuation is in the set of valuations Γ that satisfy the equilibrium condition (see Klein, 2015a). This condition differs for matching games with transferable and non-transferable utility and can be specified using the method argument. The match valuation V is a linear function of W , a matrix of characteristics for *all feasible* groups, and η , a vector of random errors. α is a parameter vector to be estimated.

The *Outcome Equation* determines the outcome for *observed* matches. The dependent variable can either be continuous or binary, dependent on the value of the binary argument. In the binary case, the dependent variable R is determined by a threshold rule for the latent variable Y .

$$\begin{aligned} R &= 1[Y > c] \\ Y &= X\beta + \epsilon \end{aligned}$$

Here, Y is a linear function of X , a matrix of characteristics for *observed* matches, and ϵ , a vector of random errors. β is a parameter vector to be estimated.

The structural model imposes a linear relationship between the error terms of both equations as $\epsilon = \delta\eta + \xi$, where ξ is a vector of random errors and δ is the covariance parameter to be estimated. If δ were zero, the marginal distributions of ϵ and η would be independent and the selection problem would vanish. That is, the observed outcomes would be a random sample from the population of interest.

Usage

```
stabit(x, m.id = "m.id", g.id = "g.id", R = "R", selection = NULL,
       outcome = NULL, simulation = "none", seed = 123, max.combs = Inf,
       method = "NTU", binary = FALSE, offsetOut = 0, offsetSel = 0,
       marketFE = FALSE, censored = 0, gPrior = FALSE, dropOnes = FALSE,
       interOut = 0, interSel = 0, standardize = 0, niter = 10,
       verbose = FALSE)
```

Arguments

<code>x</code>	data frame with individual-level characteristics of all group members including market- and group-identifiers.
<code>m.id</code>	character string giving the name of the market identifier variable. Defaults to "m.id".
<code>g.id</code>	character string giving the name of the group identifier variable. Defaults to "g.id".
<code>R</code>	dependent variable in outcome equation. Defaults to "R".
<code>selection</code>	list containing variables and pertaining operators in the selection equation. The format is <code>operation = "variable"</code> . See the Details and Examples sections.
<code>outcome</code>	list containing variables and pertaining operators in the outcome equation. The format is <code>operation = "variable"</code> . See the Details and Examples sections.
<code>simulation</code>	should the values of dependent variables in selection and outcome equations be simulated? Options are "none" for no simulation, "NTU" for non-transferable utility matching, "TU" for transferable utility or "random" for random matching of individuals to groups. Simulation settings are (i) all model coefficients set to

	alpha=beta=1; (ii) covariance between error terms $\delta=0.5$; (iii) error terms η and ξ are draws from a standard normal distribution.
seed	integer setting the state for random number generation if <code>simulation=TRUE</code> .
max.combs	integer (divisible by two) giving the maximum number of feasible groups to be used for generating group-level characteristics.
method	estimation method to be used. Either "NTU" or "TU" for selection correction using non-transferable or transferable utility matching as selection rule; "outcome" for estimation of the outcome equation only; or "model.frame" for no estimation.
binary	logical: if TRUE outcome variable is taken to be binary; if FALSE outcome variable is taken to be continuous.
offsetOut	vector of integers indicating the indices of columns in X for which coefficients should be forced to 1. Use 0 for none.
offsetSel	vector of integers indicating the indices of columns in W for which coefficients should be forced to 1. Use 0 for none.
marketFE	logical: if TRUE market-level fixed effects are used in outcome equation; if FALSE no market fixed effects are used.
censored	draws of the δ parameter that estimates the covariation between the error terms in selection and outcome equation are 0:not censored, 1:censored from below, 2:censored from above.
gPrior	logical: if TRUE the g-prior (Zellner, 1986) is used for the variance-covariance matrix.
dropOnes	logical: if TRUE one-group-markets are excluded from estimation.
interOut	two-column matrix indicating the indices of columns in X that should be interacted in estimation. Use 0 for none.
interSel	two-column matrix indicating the indices of columns in W that should be interacted in estimation. Use 0 for none.
standardize	numeric: if <code>standardize>0</code> the independent variables will be standardized by dividing by <code>standardize</code> times their standard deviation. Defaults to no standardization <code>standardize=0</code> .
niter	number of iterations to use for the Gibbs sampler.
verbose	.

Details

Operators for variable transformations in selection and outcome arguments.

`add` sum over all group members and divide by group size.

`int` sum over all possible two-way interactions $x * y$ of group members and divide by the number of those, given by `choose(n, 2)`.

`ieq` sum over all possible two-way equality assertions $1[x = y]$ and divide by the number of those.

`ive` sum over all possible two-way interactions of vectors of variables of group members and divide by number of those.

`inv` ...

`dst` sum over all possible two-way distances between players and divide by number of those, where distance is defined as $e^{-|x-y|}$.

Author(s)

Thilo Klein

References

- Klein, T. (2015a). *Does Anti-Diversification Pay? A One-Sided Matching Model of Microcredit*. *Cambridge Working Papers in Economics*, #1521.
- Zellner, A. (1986). *On assessing prior distributions and Bayesian regression analysis with g-prior distributions*, volume 6, pages 233–243. North-Holland, Amsterdam.

Examples

```
## Not run:
## --- SIMULATED EXAMPLE ---

## 1. Simulate one-sided matching data for 200 markets (m=200) with 2 groups
##   per market (gpm=2) and 5 individuals per group (ind=5). True parameters
##   in selection equation is wst=1, in outcome equation wst=0.

## 1-a. Simulate individual-level, independent variables
idata <- stabsim(m=200, ind=5, seed=123, gpm=2)
head(idata)

## 1-b. Simulate group-level variables
mdata <- stabit(x=idata, simulation="NTU", method="model.frame",
  selection = list(add="wst"), outcome = list(add="wst"), verbose=FALSE)
head(mdata$OUT)
head(mdata$SEL)

## 2. Bias from sorting

## 2-a. Naive OLS estimation
lm(R ~ wst.add, data=mdata$OUT)$coefficients

## 2-b. epsilon is correlated with independent variables
with(mdata$OUT, cor(epsilon, wst.add))

## 2-c. but xi is uncorrelated with independent variables
with(mdata$OUT, cor(xi, wst.add))

## 3. Correction of sorting bias when valuations V are observed

## 3-a. 1st stage: obtain fitted value for eta
lm.sel <- lm(V ~ -1 + wst.add, data=mdata$SEL)
lm.sel$coefficients

eta <- lm.sel$resid[mdata$SEL$D==1]

## 3-b. 2nd stage: control for eta
lm(R ~ wst.add + eta, data=mdata$OUT)$coefficients
```

```

## 4. Run Gibbs sampler
fit1 <- stabit(x=idata, method="NTU", simulation="NTU", censored=1,
              selection = list(add="wst"), outcome = list(add="wst"),
              niter=2000, verbose=FALSE)

## 5. Coefficient table
summary(fit1)

## 6. Plot MCMC draws for coefficients
plot(fit1)

## --- REPLICATION, Klein (2015a) ---

## 1. Load data
data(baac00); head(baac00)

## 2. Run Gibbs sampler
klein15a <- stabit(x=baac00, selection = list(inv="pi",ieq="wst"),
                  outcome = list(add="pi",inv="pi",ieq="wst",
                                add=c("loan_size","loan_size2","lgroup_agei")), offsetOut=1,
                  method="NTU", binary=TRUE, gPrior=TRUE, marketFE=TRUE, niter=800000)

## 3. Marginal effects
summary(klein15a, mfx=TRUE)

## 4. Plot MCMC draws for coefficients
plot(klein15a)

## End(Not run)

```

stabit2

Matching model and selection correction for college admissions

Description

The function provides a Gibbs sampler for a structural matching model that estimates preferences and corrects for sample selection bias when the selection process is a two-sided matching game; i.e., a matching of students to colleges.

The structural model consists of a selection and an outcome equation. The *Selection Equation* determines which matches are observed ($D = 1$) and which are not ($D = 0$).

$$\begin{aligned}
 D &= 1[V \in \Gamma] \\
 V &= W\beta + \eta
 \end{aligned}$$

Here, V is a vector of latent valuations of *all feasible* matches, ie observed and unobserved, and $1[.]$ is the Iverson bracket. A match is observed if its match valuation is in the set of valuations Γ that

satisfy the equilibrium condition (see Sorensen, 2007). The match valuation V is a linear function of W , a matrix of characteristics for *all feasible* matches, and η , a vector of random errors. β is a parameter vector to be estimated.

The *Outcome Equation* determines the outcome for *observed* matches. The dependent variable can either be continuous or binary, dependent on the value of the binary argument. In the binary case, the dependent variable R is determined by a threshold rule for the latent variable Y .

$$\begin{aligned} R &= 1[Y > c] \\ Y &= X\alpha + \epsilon \end{aligned}$$

Here, Y is a linear function of X , a matrix of characteristics for *observed* matches, and ϵ , a vector of random errors. α is a parameter vector to be estimated.

The structural model imposes a linear relationship between the error terms of both equations as $\epsilon = \kappa\eta + \nu$, where ν is a vector of random errors and κ is the covariance parameter to be estimated. If κ were zero, the marginal distributions of ϵ and η would be independent and the selection problem would vanish. That is, the observed outcomes would be a random sample from the population of interest.

Usage

```
stabit2(OUT = NULL, SEL = NULL, colleges = NULL, students = NULL,
        outcome = NULL, selection, binary = FALSE, niter, gPrior = FALSE,
        censored = 1, thin = 1, nCores = max(1, detectCores() - 1), ...)
```

Arguments

OUT	data frame with characteristics of all observed matches, including market identifier <code>m.id</code> , college identifier <code>c.id</code> and student identifier <code>s.id</code> .
SEL	optional: data frame with characteristics of all observed and unobserved matches, including market identifier <code>m.id</code> , college identifier <code>c.id</code> and student identifier <code>s.id</code> .
colleges	character vector of variable names for college characteristics. These variables carry the same value for any college.
students	character vector of variable names for student characteristics. These variables carry the same value for any student.
outcome	formula for match outcomes.
selection	formula for match valuations.
binary	logical: if TRUE outcome variable is taken to be binary; if FALSE outcome variable is taken to be continuous.
niter	number of iterations to use for the Gibbs sampler.
gPrior	logical: if TRUE the g-prior (Zellner, 1986) is used for the variance-covariance matrix. (Not yet implemented)
censored	draws of the kappa parameter that estimates the covariation between the error terms in selection and outcome equation are 0:not censored, 1:censored from below, 2:censored from above.


```

thin          integer indicating the level of thinning in the MCMC draws. The default thin=1
              saves every draw, thin=2 every second, etc.

nCores        number of cores to be used in parallel Gibbs sampling.

...          .

```

Author(s)

Thilo Klein

References

Sorensen, M. (2007). How Smart is Smart Money? A Two-Sided Matching Model of Venture Capital. *Journal of Finance*, 62 (6): 2725-2762.

Examples

```

## Not run:
## --- SIMULATED EXAMPLE ---

## 1. Simulate two-sided matching data for 20 markets (m=20) with 100 students
##     (nStudents=100) per market and 20 colleges with quotas of 5 students, each
##     (nSlots=rep(5,20)). True parameters in selection and outcome equations are
##     all equal to 1.

xdata <- stabsim2(m=20, nStudents=100, nSlots=rep(5,20), verbose=FALSE,
  colleges = "c1", students = "s1",
  outcome = ~ c1:s1 + eta + nu,
  selection = ~ -1 + c1:s1 + eta
)
head(xdata$OUT)

## 2. Correction for sorting bias when match valuations V are observed

## 2-a. Bias from sorting
lm1 <- lm(y ~ c1:s1, data=xdata$OUT)
summary(lm1)

## 2-b. Cause of the bias
with(xdata$OUT, cor(c1*s1, eta))

## 2-c. Correction for sorting bias
lm2a <- lm(V ~ -1 + c1:s1, data=xdata$SEL); summary(lm2a)
etahat <- lm2a$residuals[xdata$SEL$D==1]

lm2b <- lm(y ~ c1:s1 + etahat, data=xdata$OUT)
summary(lm2b)

## 3. Correction for sorting bias when match valuations V are unobserved

## 3-a. Run Gibbs sampler (when SEL is given)

```

```

fit2 <- stabit2(OUT = xdata$OUT,
               SEL = xdata$SEL,
               outcome = y ~ c1:s1,
               selection = ~ -1 + c1:s1,
               niter=1000
             )

## 3-b. Alternatively: Run Gibbs sampler (when SEL is not given)
fit2 <- stabit2(OUT = xdata$OUT,
               colleges = "c1",
               students = "s1",
               outcome = y ~ c1:s1,
               selection = ~ -1 + c1:s1,
               niter=1000
             )

## 4. Implemented methods

## 4-a. Get coefficients
fit2

## 4-b. Coefficient table
summary(fit2)

## 4-c. Get marginal effects
summary(fit2, mfx=TRUE)

## 4-d. Also try the following functions
#coef(fit2)
#fitted(fit2)
#residuals(fit2)
#predict(fit2, newdata=NULL)

## 5. Plot MCMC draws for coefficients
plot(fit2)

## End(Not run)

```

stabsim

Simulated data for group formation problem

Description

Simulate individual-level data for one-sided matching markets.

Usage

```
stabsim(m, ind, seed = 123, singles = NULL, gpm = 2)
```

Arguments

m	integer indicating the number of markets to be simulated.
ind	integer (or vector) indicating the number of individuals per group.
seed	integer setting the state for random number generation. Defaults to <code>set.seed(123)</code> .
singles	integer giving the number of one-group markets.
gpm	integer giving the number of groups per market.

Value

stabsim returns a data frame with the randomly generated variables mimicking those in dataset [baac00](#).

m.id	categorical: market identifier.
g.id	categorical: group identifier.
wst	binary: indicator taking the value 1 if last year was worse than the year before; 0 otherwise.
R	NA: group outcome is not simulated. It can be obtained using the simulation argument in function <code>stabit</code> .

Author(s)

Thilo Klein

Examples

```
## Coalitions [gpm := 2 !]
## Simulate one-sided matching data for 4 markets (m=4) with 2 groups
## per market (gpm=2) and 2 to 4 individuals per group (ind=2:4)
idata <- stabsim(m=4, ind=2:4, seed=124, singles=2, gpm=2)

## Rommmates [ind := 2 !]
## Simulate one-sided matching data for 3 markets (m=3) with 3 groups
## per market (gpm=3) and 2 individuals per group (ind=2)
idata <- stabsim(m=3, ind=2, seed=124, gpm=3)
```

stabsim2

Simulated data for college admissions problem

Description

Simulate data for two-sided matching markets. In the simulation for the Sorensen (2007) model with one selection equation, an equal sharing rule of $\lambda = 0.5$ is used.

Usage

```
stabsim2(m, nStudents, nColleges = length(nSlots), nSlots, colleges, students,
  outcome, selection, binary = FALSE, seed = 123, verbose = TRUE)
```

Arguments

m	integer indicating the number of markets to be simulated.
nStudents	integer indicating the number of students per market.
nColleges	integer indicating the number of colleges per market.
nSlots	vector of length nColleges indicating the number of places at each college, i.e. the college's quota.
colleges	character vector of variable names for college characteristics. These variables carry the same value for any college.
students	character vector of variable names for student characteristics. These variables carry the same value for any student.
outcome	formula for match outcomes.
selection	formula for match valuations.
binary	logical: if TRUE outcome variable is binary; if FALSE outcome variable is continuous.
seed	integer setting the state for random number generation. Defaults to set.seed(123).
verbose	.

Value

stabsim2 returns a list with the following items.

OUT
SEL
SElc
SEls

Author(s)

Thilo Klein

Examples

```
## Simulate two-sided matching data for 2 markets (m=2) with 10 students
## (nStudents=10) per market and 3 colleges (nColleges=3) with quotas of
## 2, 3, and 5 students, respectively.

xdata <- stabsim2(m=2, nStudents=10, nSlots=c(2,3,5), verbose=FALSE,
  colleges = "c1", students = "s1",
  outcome = ~ c1:s1 + eta + nu,
  selection = ~ -1 + c1:s1 + eta
)
head(xdata$OUT)
head(xdata$SEL)
```

ttc *Top-Trading-Cycles Algorithm for the house allocation problem*

Description

Finds the stable matching in the **house allocation problem** with existing tenants. Uses the Top-Trading-Cycles Algorithm proposed in Abdulkadiroglu and Sonmez (1999).

Usage

```
ttc(P = NULL, X = NULL)
```

Arguments

P matrix of individuals' preference rankings (Rank Order Lists) over objects.
 X 2-column-matrix of objects (obj) and their owners (ind).

Value

ttc returns a 2-column matrix of the matching solution for the housing market problem based on the Top-Trading-Cycles algorithm.

Author(s)

Thilo Klein

References

Abdulkadiroglu, A. and Sonmez, T. (1999). House Allocation with Existing Tenants. *Journal of Economic Theory*, 88(2):233–260.
 Shapley, L. and H. Scarf (1974). On Cores and Indivisibility. *Journal of Mathematical Economics*, 1(1):23–37.

Examples

```
## generate matrix of individuals' preference rankings over objects, a.k.a. Rank Order Lists (ROL)
P <- matrix(c(2, 5, 1, 4, 3, # ROL of individual 1
             1, 5, 4, 3, 2, # ind 2
             2, 1, 4, 3, 5, # ind 3
             2, 4, 3, NA, NA, # ind 4
             4, 3, 1, 2, NA), # ind 5
           byrow=FALSE, nrow=5); P

## generate 2-column-matrix of objects ('obj') and their owners ('ind')
X <- data.frame(ind=1:5, obj=5:1); X

## find assignment based on TTC algorithm
ttc(P=P,X=X)
```

Index

- *Topic **algorithms**,
 - [hri2](#), [8](#)
- *Topic **algorithms**
 - [hri](#), [5](#)
 - [iaa](#), [10](#)
 - [plp](#), [16](#)
 - [sri](#), [18](#)
 - [ttc](#), [29](#)
- *Topic **datasets**
 - [baac00](#), [4](#)
 - [klein15a](#), [12](#)
 - [klein15b](#), [13](#)
- *Topic **generate**
 - [stabsim](#), [26](#)
 - [stabsim2](#), [27](#)
- *Topic **matching**
 - [hri2](#), [8](#)
- *Topic **package**
 - [matchingMarkets-package](#), [2](#)
- *Topic **regression**
 - [stabit](#), [19](#)
 - [stabit2](#), [23](#)
- *Topic **summary**
 - [khb](#), [11](#)
 - [predict.stabit2](#), [17](#)

[baac00](#), [3](#), [4](#), [27](#)

[hri](#), [3](#), [5](#)
[hri2](#), [8](#)

[iaa](#), [10](#)

[khb](#), [2](#), [11](#)
[klein15a](#), [12](#)
[klein15b](#), [13](#)

[matchingMarkets](#)
 ([matchingMarkets-package](#)), [2](#)
[matchingMarkets-package](#), [2](#)
[mce](#), [14](#)

[plp](#), [16](#)
[predict.stabit2](#), [17](#)

[sri](#), [3](#), [18](#)
[stabit](#), [2](#), [19](#)
[stabit2](#), [2](#), [23](#)
[stabsim](#), [3](#), [26](#)
[stabsim2](#), [3](#), [27](#)

[ttc](#), [3](#), [29](#)