

Package ‘mgcv’

February 8, 2017

Version 1.8-17

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Title Mixed GAM Computation Vehicle with GCV/AIC/REML Smoothness Estimation

Description GAMs, GAMMs and other generalized ridge regression with multiple smoothing parameter estimation by GCV, REML or UBRE/AIC. Includes a gam() function, a wide variety of smoothers, JAGS support and distributions beyond the exponential family.

Priority recommended

Depends R (>= 2.14.0), nlme (>= 3.1-64)

Imports methods, stats, graphics, Matrix

Suggests splines, parallel, survival, MASS

LazyLoad yes

ByteCompile yes

License GPL (>= 2)

NeedsCompilation yes

Repository CRAN

Date/Publication 2017-02-08 21:30:16

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anova.gam	<i>Approximate hypothesis tests related to GAM fits</i>
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Description

Performs hypothesis tests relating to one or more fitted gam objects. For a single fitted gam object, Wald tests of the significance of each parametric and smooth term are performed, so interpretation is analogous to [drop1](#) rather than `anova.lm` (i.e. it's like type III ANOVA, rather than a sequential type I ANOVA). Otherwise the fitted models are compared using an analysis of deviance table: this latter approach should not be use to test the significance of terms which can be penalized to zero. Models to be compared should be fitted to the same data using the same smoothing parameter selection method.

Usage

```
## S3 method for class 'gam'
anova(object, ..., dispersion = NULL, test = NULL,
       freq = FALSE,p.type=0)
## S3 method for class 'anova.gam'
print(x, digits = max(3, getOption("digits") - 3),...)
```

Arguments

<code>object, ...</code>	fitted model objects of class <code>gam</code> as produced by <code>gam()</code> .
<code>x</code>	an <code>anova.gam</code> object produced by a single model call to <code>anova.gam()</code> .
<code>dispersion</code>	a value for the dispersion parameter: not normally used.
<code>test</code>	what sort of test to perform for a multi-model call. One of "Chisq", "F" or "Cp".
<code>freq</code>	whether to use frequentist or Bayesian approximations for parametric term p-values. See summary.gam for details.
<code>p.type</code>	selects exact test statistic to use for single smooth term p-values. See summary.gam for details.
<code>digits</code>	number of digits to use when printing output.

Details

If more than one fitted model is provided than `anova.glm` is used, with the difference in model degrees of freedom being taken as the difference in effective degrees of freedom (when possible this is a smoothing parameter uncertainty corrected version). The p-values resulting from this are only approximate, and must be used with care. The approximation is most accurate when the comparison relates to unpenalized terms, or smoothers with a null space of dimension greater than zero. (Basically we require that the difference terms could be well approximated by unpenalized terms with degrees of freedom approximately the effective degrees of freedom). In simulations the p-values are usually slightly too low. For terms with a zero-dimensional null space (i.e. those which can be penalized to zero) the approximation is often very poor, and significance can be greatly overstated: i.e. p-values are often substantially too low. This case applies to random effect terms.

Note also that in the multi-model call to `anova.gam`, it is quite possible for a model with more terms to end up with lower effective degrees of freedom, but better fit, than the notionally null model with fewer terms. In such cases it is very rare that it makes sense to perform any sort of test, since there is then no basis on which to accept the notional null model.

If only one model is provided then the significance of each model term is assessed using Wald like tests, conditional on the smoothing parameter estimates: see [summary.gam](#) and Wood (2013a,b) for details. The p-values provided here are better justified than in the multi model case, and have close to the correct distribution under the null, unless smoothing parameters are poorly identified. ML or REML smoothing parameter selection leads to the best results in simulations as they tend to avoid occasional severe undersmoothing. In replication of the full simulation study of Scheipl et al. (2008) the tests give almost indistinguishable power to the method recommended there, but slightly too low p-values under the null in their section 3.1.8 test for a smooth interaction (the Scheipl et al. recommendation is not used directly, because it only applies in the Gaussian case, and requires model refits, but it is available in package `RLRsim`).

In the single model case `print.anova.gam` is used as the printing method.

By default the p-values for parametric model terms are also based on Wald tests using the Bayesian covariance matrix for the coefficients. This is appropriate when there are "re" terms present, and is otherwise rather similar to the results using the frequentist covariance matrix (`freq=TRUE`), since the parametric terms themselves are usually unpenalized. Default P-values for parameteric terms that are penalized using the `paraPen` argument will not be good.

Value

In the multi-model case `anova.gam` produces output identical to `anova.glm`, which it in fact uses.

In the single model case an object of class `anova.gam` is produced, which is in fact an object returned from `summary.gam`.

`print.anova.gam` simply produces tabulated output.

WARNING

If models 'a' and 'b' differ only in terms with no un-penalized components (such as random effects) then p values from `anova(a,b)` are unreliable, and usually much too low.

Default P-values will usually be wrong for parametric terms penalized using 'paraPen': use `freq=TRUE` to obtain better p-values when the penalties are full rank and represent conventional random effects.

For a single model, interpretation is similar to `drop1`, not `anova.lm`.

Author(s)

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References

Scheipl, F., Greven, S. and Küchenhoff, H. (2008) Size and power of tests for a zero random effect variance or polynomial regression in additive and linear mixed models. *Comp. Statist. Data Anal.* 52, 3283-3299

Wood, S.N. (2013a) On p-values for smooth components of an extended generalized additive model. *Biometrika* 100:221-228

Wood, S.N. (2013b) A simple test for random effects in regression models. *Biometrika* 100:1005-1010

See Also

[gam](#), [predict.gam](#), [gam.check](#), [summary.gam](#)

Examples

```
library(mgcv)
set.seed(0)
dat <- gamSim(5,n=200,scale=2)

b<-gam(y ~ x0 + s(x1) + s(x2) + s(x3),data=dat)
anova(b)
b1<-gam(y ~ x0 + s(x1) + s(x2),data=dat)
anova(b,b1,test="F")
```

Description

Fits a generalized additive model (GAM) to a very large data set, the term ‘GAM’ being taken to include any quadratically penalized GLM. The degree of smoothness of model terms is estimated as part of fitting. In use the function is much like [gam](#), except that the numerical methods are designed for datasets containing upwards of several tens of thousands of data (see Wood, Goude and Shaw, 2015). The advantage of [bam](#) is much lower memory footprint than [gam](#), but it can also be much faster, for large datasets. [bam](#) can also compute on a cluster set up by the [parallel](#) package.

An alternative fitting approach is provided by the `discrete==TRUE` method. In this case a method based on discretization of covariate values and C code level parallelization (controlled by the `nthreads` argument instead of the `cluster` argument) is used. This extends both the data set and model size usable.

Usage

```
bam(formula, family=gaussian(), data=list(), weights=NULL, subset=NULL,
     na.action=na.omit, offset=NULL, method="fREML", control=list(),
     select=FALSE, scale=0, gamma=1, knots=NULL, sp=NULL, min.sp=NULL,
     paraPen=NULL, chunk.size=10000, rho=0, AR.start=NULL, discrete=FALSE,
     cluster=NULL, nthreads=NA, gc.level=1, use.chol=FALSE, samfrac=1,
     coef=NULL, drop.unused.levels=TRUE, G=NULL, fit=TRUE, drop.intercept=NULL, ...)
```

Arguments

<code>formula</code>	A GAM formula (see formula.gam and also gam.models). This is exactly like the formula for a GLM except that smooth terms, <code>s</code> and <code>te</code> can be added to the right hand side to specify that the linear predictor depends on smooth functions of predictors (or linear functionals of these).
<code>family</code>	This is a family object specifying the distribution and link to use in fitting etc. See glm and family for more details. A negative binomial family is provided: see negbin , but only the known theta case is supported by bam .
<code>data</code>	A data frame or list containing the model response variable and covariates required by the formula. By default the variables are taken from <code>environment(formula)</code> : typically the environment from which gam is called.
<code>weights</code>	prior weights on the contribution of the data to the log likelihood. Note that a weight of 2, for example, is equivalent to having made exactly the same observation twice. If you want to reweight the contributions of each datum without changing the overall magnitude of the log likelihood, then you should normalize the weights (e.g. <code>weights <- weights/mean(weights)</code>).
<code>subset</code>	an optional vector specifying a subset of observations to be used in the fitting process.

na.action	a function which indicates what should happen when the data contain 'NA's. The default is set by the 'na.action' setting of 'options', and is 'na.fail' if that is unset. The "factory-fresh" default is 'na.omit'.
offset	Can be used to supply a model offset for use in fitting. Note that this offset will always be completely ignored when predicting, unlike an offset included in formula (this used to conform to the behaviour of lm and glm).
method	The smoothing parameter estimation method. "GCV.Cp" to use GCV for unknown scale parameter and Mallows' Cp/UBRE/AIC for known scale. "GACV.Cp" is equivalent, but using GACV in place of GCV. "REML" for REML estimation, including of unknown scale, "P-REML" for REML estimation, but using a Pearson estimate of the scale. "ML" and "P-ML" are similar, but using maximum likelihood in place of REML. Default "fREML" uses fast REML computation.
control	A list of fit control parameters to replace defaults returned by <code>gam.control</code> . Any control parameters not supplied stay at their default values.
select	Should selection penalties be added to the smooth effects, so that they can in principle be penalized out of the model? Has the side effect that smooths no longer have a fixed effect component (improper prior from a Bayesian perspective) allowing REML comparison of models with the same fixed effect structure.
scale	If this is positive then it is taken as the known scale parameter. Negative signals that the scale parameter is unknown. 0 signals that the scale parameter is 1 for Poisson and binomial and unknown otherwise. Note that (RE)ML methods can only work with scale parameter 1 for the Poisson and binomial cases.
gamma	It is sometimes useful to inflate the model degrees of freedom in the GCV or UBRE/AIC score by a constant multiplier. This allows such a multiplier to be supplied.
knots	this is an optional list containing user specified knot values to be used for basis construction. For most bases the user simply supplies the knots to be used, which must match up with the k value supplied (note that the number of knots is not always just k). See <code>tp</code> for what happens in the "tp"/"ts" case. Different terms can use different numbers of knots, unless they share a covariate.
sp	A vector of smoothing parameters can be provided here. Smoothing parameters must be supplied in the order that the smooth terms appear in the model formula. Negative elements indicate that the parameter should be estimated, and hence a mixture of fixed and estimated parameters is possible. If smooths share smoothing parameters then <code>length(sp)</code> must correspond to the number of underlying smoothing parameters.
min.sp	Lower bounds can be supplied for the smoothing parameters. Note that if this option is used then the smoothing parameters <code>full.sp</code> , in the returned object, will need to be added to what is supplied here to get the smoothing parameters actually multiplying the penalties. <code>length(min.sp)</code> should always be the same as the total number of penalties (so it may be longer than <code>sp</code> , if smooths share smoothing parameters).
paraPen	optional list specifying any penalties to be applied to parametric model terms. <code>gam.models</code> explains more.
chunk.size	The model matrix is created in chunks of this size, rather than ever being formed whole. Reset to $4*p$ if <code>chunk.size < 4*p</code> where <code>p</code> is the number of coefficients.

<code>rho</code>	An AR1 error model can be used for the residuals (based on dataframe order), of Gaussian-identity link models. This is the AR1 correlation parameter. Standardized residuals (approximately uncorrelated under correct model) returned in <code>std.rsd</code> if non zero.
<code>AR.start</code>	logical variable of same length as data, TRUE at first observation of an independent section of AR1 correlation. Very first observation in data frame does not need this. If NULL then there are no breaks in AR1 correlation.
<code>discrete</code>	with <code>method="FREML"</code> it is possible to discretize covariates for storage and efficiency reasons. If <code>discrete</code> is TRUE, a number or a vector of numbers for each smoother term, then discretization happens. If numbers are supplied they give the number of discretization bins. Experimental at present.
<code>cluster</code>	<code>bam</code> can compute the computationally dominant QR decomposition in parallel using <code>parLapply</code> from the <code>parallel</code> package, if it is supplied with a cluster on which to do this (a cluster here can be some cores of a single machine). See details and example code.
<code>nthreads</code>	Number of threads to use for non-cluster computation (e.g. combining results from cluster nodes). if NA set to <code>max(1, length(cluster))</code> .
<code>gc.level</code>	to keep the memory footprint down, it helps to call the garbage collector often, but this takes a substantial amount of time. Setting this to zero means that garbage collection only happens when R decides it should. Setting to 2 gives frequent garbage collection. 1 is in between.
<code>use.chol</code>	By default <code>bam</code> uses a very stable QR update approach to obtaining the QR decomposition of the model matrix. For well conditioned models an alternative accumulates the crossproduct of the model matrix and then finds its Choleski decomposition, at the end. This is somewhat more efficient, computationally.
<code>samfrac</code>	For very large sample size Generalized additive models the number of iterations needed for the model fit can be reduced by first fitting a model to a random sample of the data, and using the results to supply starting values. This initial fit is run with sloppy convergence tolerances, so is typically very low cost. <code>samfrac</code> is the sampling fraction to use. 0.1 is often reasonable.
<code>coef</code>	initial values for model coefficients
<code>drop.unused.levels</code>	by default unused levels are dropped from factors before fitting. For some smooths involving factor variables you might want to turn this off. Only do so if you know what you are doing.
<code>G</code>	if not NULL then this should be the object returned by a previous call to <code>bam</code> with <code>fit=FALSE</code> . Causes all other arguments to be ignored except <code>chunk.size</code> , <code>gamma</code> , <code>nthreads</code> , <code>cluster</code> , <code>rho</code> , <code>gc.level</code> , <code>samfrac</code> , <code>use.chol</code> and <code>method</code> .
<code>fit</code>	if FALSE then the model is set up for fitting but not estimated, and an object is returned, suitable for passing as the <code>G</code> argument to <code>bam</code> .
<code>drop.intercept</code>	Set to TRUE to force the model to really not have the a constant in the parametric model part, even with factor variables present.
<code>...</code>	further arguments for passing on e.g. to <code>gam.fit</code> (such as <code>mustart</code>).

Details

When `discrete=FALSE`, `bam` operates by first setting up the basis characteristics for the smooths, using a representative subsample of the data. Then the model matrix is constructed in blocks using `predict.gam`. For each block the factor R , from the QR decomposition of the whole model matrix is updated, along with $Q'y$ and the sum of squares of y . At the end of block processing, fitting takes place, without the need to ever form the whole model matrix.

In the generalized case, the same trick is used with the weighted model matrix and weighted pseudodata, at each step of the PIRLS. Smoothness selection is performed on the working model at each stage (performance oriented iteration), to maintain the small memory footprint. This is trivial to justify in the case of GCV or C_p /UBRE/AIC based model selection, and for REML/ML is justified via the asymptotic multivariate normality of $Q'z$ where z is the IRLS pseudodata.

For full method details see Wood, Goude and Shaw (2015).

Note that POI is not as stable as the default nested iteration used with `gam`, but that for very large, information rich, datasets, this is unlikely to matter much.

Note also that it is possible to spend most of the computational time on basis evaluation, if an expensive basis is used. In practice this means that the default "tp" basis should be avoided: almost any other basis (e.g. "cr" or "ps") can be used in the 1D case, and tensor product smooths (te) are typically much less costly in the multi-dimensional case.

If `cluster` is provided as a cluster set up using `makeCluster` (or `makeForkCluster`) from the `parallel` package, then the rate limiting QR decomposition of the model matrix is performed in parallel using this cluster. Note that the speed ups are often not that great. On a multi-core machine it is usually best to set the cluster size to the number of physical cores, which is often less than what is reported by `detectCores`. Using more than the number of physical cores can result in no speed up at all (or even a slow down). Note that a highly parallel BLAS may negate all advantage from using a cluster of cores. Computing in parallel of course requires more memory than computing in series. See examples.

When `discrete=TRUE` the covariate data are first discretized. Discretization takes place on a smooth by smooth basis, or in the case of tensor product smooths (or any smooth that can be represented as such, such as random effects), separately for each marginal smooth. The required spline bases are then evaluated at the discrete values, and stored, along with index vectors indicating which original observation they relate to. Fitting is by a version of performance oriented iteration/PQL using REML smoothing parameter selection on each iterative working model (as for the default method). The iteration is based on the derivatives of the REML score, without computing the score itself, allowing the expensive computations to be reduced to one parallel block Cholesky decomposition per iteration (plus two basic operations of equal cost, but easily parallelized). Unlike standard POI/PQL, only one step of the smoothing parameter update for the working model is taken at each step (rather than iterating to the optimal set of smoothing parameters for each working model). At each step a weighted model matrix crossproduct of the model matrix is required - this is efficiently computed from the pre-computed basis functions evaluated at the discretized covariate values. Efficient computation with tensor product terms means that some terms within a tensor product may be re-ordered for maximum efficiency. Parallel computation is controlled using the `nthreads` argument. For this method no cluster computation is used, and the `parallel` package is not required.

Value

An object of class "gam" as described in `gamObject`.

WARNINGS

The routine will be slow if the default "tp" basis is used.

Unless discrete=TRUE, you must have more unique combinations of covariates than the model has total parameters. (Total parameters is sum of basis dimensions plus sum of non-spline terms less the number of spline terms).

This routine is less stable than 'gam' for the same dataset.

The negbin family is only supported for the *known theta* case.

Author(s)

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References

Wood, S.N., Goude, Y. & Shaw S. (2015) Generalized additive models for large datasets. Journal of the Royal Statistical Society, Series C 64(1): 139-155.

Wood, S.N., Li, Z., Shaddick, G. & Augustin N.H. (2016) Generalized additive models for gigadata: modelling the UK black smoke network daily data. Journal of the American Statistical Association.

See Also

[mgcv.parallel](#), [mgcv-package](#), [gamObject](#), [gam.models](#), [smooth.terms](#), [linear.functional.terms](#), [s](#), [te.predict.gam](#), [plot.gam](#), [summary.gam](#), [gam.side](#), [gam.selection](#), [gam.control.gam.check](#), [linear.functional.terms.negbin](#), [magic](#), [vis.gam](#)

Examples

```
library(mgcv)
## See help("mgcv-parallel") for using bam in parallel

## Some examples are marked 'Not run' purely to keep
## checking load on CRAN down. Sample sizes are small for
## the same reason.

set.seed(3)
dat <- gamSim(1, n=25000, dist="normal", scale=20)
bs <- "cr"; k <- 12
b <- bam(y ~ s(x0, bs=bs) + s(x1, bs=bs) + s(x2, bs=bs, k=k) +
         s(x3, bs=bs), data=dat)
summary(b)
plot(b, pages=1, rug=FALSE) ## plot smooths, but not rug
plot(b, pages=1, rug=FALSE, seWithMean=TRUE) ## `with intercept' CIs

## Not run:
ba <- bam(y ~ s(x0, bs=bs, k=k) + s(x1, bs=bs, k=k) + s(x2, bs=bs, k=k) +
         s(x3, bs=bs, k=k), data=dat, method="GCV.Cp") ## use GCV
summary(ba)
## End(Not run)
```

```
## A Poisson example...

k <- 15
dat <- gamSim(1,n=21000,dist="poisson",scale=.1)

system.time(b1 <- bam(y ~ s(x0,bs=bs)+s(x1,bs=bs)+s(x2,bs=bs,k=k),
                    data=dat,family=poisson()))
b1

## Sparse smoother example (deprecated)...
## Not run:
dat <- gamSim(1,n=10000,dist="poisson",scale=.1)
system.time( b3 <- bam(y ~ te(x0,x1,bs="ps",k=10,np=FALSE)+
                    s(x2,bs="ps",k=30)+s(x3,bs="ps",k=30),data=dat,
                    method="REML",family=poisson(),sparse=TRUE))
b3
## End(Not run)
```

bam.update

Update a strictly additive bam model for new data.

Description

Gaussian with identity link models fitted by `bam` can be efficiently updated as new data becomes available, by simply updating the QR decomposition on which estimation is based, and re-optimizing the smoothing parameters, starting from the previous estimates. This routine implements this.

Usage

```
bam.update(b,data,chunk.size=10000)
```

Arguments

<code>b</code>	A gam object fitted by <code>bam</code> and representing a strictly additive model (i.e. gaussian errors, identity link).
<code>data</code>	Extra data to augment the original data used to obtain <code>b</code> . Must include a <code>weights</code> column if the original fit was weighted and a <code>AR.start</code> column if <code>AR.start</code> was non NULL in original fit.
<code>chunk.size</code>	size of subsets of data to process in one go when getting fitted values.

Details

`bam.update` updates the QR decomposition of the (weighted) model matrix of the GAM represented by `b` to take account of the new data. The orthogonal factor multiplied by the response vector is also updated. Given these updates the model and smoothing parameters can be re-estimated, as if the whole dataset (original and the new data) had been fitted in one go. The function will use the

same AR1 model for the residuals as that employed in the original model fit (see rho parameter of `bam`).

Note that there may be small numerical differences in fit between fitting the data all at once, and fitting in stages by updating, if the smoothing bases used have any of their details set with reference to the data (e.g. default knot locations).

Value

An object of class "gam" as described in `gamObject`.

WARNINGS

AIC computation does not currently take account of AR model, if used.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

`mgcv-package`, `bam`

Examples

```
library(mgcv)
## following is not *very* large, for obvious reasons...
set.seed(8)
n <- 5000
dat <- gamSim(1,n=n,dist="normal",scale=5)
dat[c(50,13,3000,3005,3100),]<- NA
dat1 <- dat[(n-999):n,]
dat0 <- dat[1:(n-1000),]
bs <- "ps";k <- 20
method <- "GCV.Cp"
b <- bam(y ~ s(x0,bs=bs,k=k)+s(x1,bs=bs,k=k)+s(x2,bs=bs,k=k)+
         s(x3,bs=bs,k=k),data=dat0,method=method)

b1 <- bam.update(b,dat1)

b2 <- bam.update(bam.update(b,dat1[1:500,]),dat1[501:1000,])

b3 <- bam(y ~ s(x0,bs=bs,k=k)+s(x1,bs=bs,k=k)+s(x2,bs=bs,k=k)+
         s(x3,bs=bs,k=k),data=dat,method=method)
b1;b2;b3

## example with AR1 errors...
```

```

e <- rnorm(n)
for (i in 2:n) e[i] <- e[i-1]*.7 + e[i]
dat$y <- dat$f + e*3
dat[c(50,13,3000,3005,3100),]<- NA
dat1 <- dat[(n-999):n,]
dat0 <- dat[1:(n-1000),]
method <- "ML"

b <- bam(y ~ s(x0,bs=bs,k=k)+s(x1,bs=bs,k=k)+s(x2,bs=bs,k=k)+
         s(x3,bs=bs,k=k),data=dat0,method=method,rho=0.7)

b1 <- bam.update(b,dat1)

summary(b1);summary(b2);summary(b3)

```

bandchol

Choleski decomposition of a band diagonal matrix

Description

Computes Choleski decomposition of a (symmetric positive definite) band-diagonal matrix, A.

Usage

```
bandchol(B)
```

Arguments

B An n by k matrix containing the diagonals of the matrix A to be decomposed. First row is leading diagonal, next is first sub-diagonal, etc. sub-diagonals are zero padded at the end. Alternatively gives A directly, i.e. a square matrix with 2k-1 non zero diagonals (those from the lower triangle are not accessed).

Details

Calls `dpbtrf` from LAPACK. The point of this is that it has $O(k^2n)$ computational cost, rather than the $O(n^3)$ required by dense matrix methods.

Value

Let R be the factor such that $t(R) \%*\% R = A$. R is upper triangular and if the rows of B contained the diagonals of A on entry, then what is returned is an n by k matrix containing the diagonals of R, packed as B was packed on entry. If B was square on entry, then R is returned directly. See examples.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Anderson, E., Bai, Z., Bischof, C., Blackford, S., Dongarra, J., Du Croz, J., Greenbaum, A., Hammarling, S., McKenney, A. and Sorensen, D., 1999. LAPACK Users' guide (Vol. 9). Siam.

Examples

```
require(mgcv)
## simulate a banded diagonal matrix
n <- 7;set.seed(8)
A <- matrix(0,n,n)
sdiag(A) <- runif(n);sdiag(A,1) <- runif(n-1)
sdiag(A,2) <- runif(n-2)
A <- crossprod(A)

## full matrix form...
bandchol(A)
chol(A) ## for comparison

## compact storage form...
B <- matrix(0,3,n)
B[1,] <- sdiag(A);B[2,1:(n-1)] <- sdiag(A,1)
B[3,1:(n-2)] <- sdiag(A,2)
bandchol(B)
```

 betar

GAM beta regression family

Description

Family for use with `gam`, implementing regression for beta distributed data on (0,1). A linear predictor controls the mean, μ of the beta distribution, while the variance is then $\mu(1 - \mu)/(1 + \phi)$, with parameter ϕ being estimated during fitting, alongside the smoothing parameters.

Usage

```
betar(theta = NULL, link = "logit", eps=.Machine$double.eps*100)
```

Arguments

theta	the extra parameter (ϕ above).
link	The link function: one of "logit", "probit", "cloglog" and "cauchit".
eps	the response variable will be truncated to the interval $[\text{eps}, 1-\text{eps}]$ if there are values outside this range. This truncation is not entirely benign, but too small a value of eps will cause stability problems if there are zeroes or ones in the response.

Details

These models are useful for proportions data which can not be modelled as binomial. Note the assumption that data are in (0,1), despite the fact that for some parameter values 0 and 1 are perfectly legitimate observations. The restriction is needed to keep the log likelihood bounded for all parameter values. Any data exactly at 0 or 1 are reset to be just above 0 or just below 1 using the eps argument (in fact any observation $< \text{eps}$ is reset to eps and any observation $> 1 - \text{eps}$ is reset to $1 - \text{eps}$). Note the effect of this resetting. If $\mu\phi > 1$ then impossible 0s are replaced with highly improbable eps values. If the inequality is reversed then 0s with infinite probability density are replaced with eps values having high finite probability density. The equivalent condition for 1s is $(1 - \mu)\phi > 1$. Clearly all types of resetting are somewhat unsatisfactory, and care is needed if data contain 0s or 1s (often it makes sense to manually reset the 0s and 1s in a manner that somehow reflects the sampling setup).

Value

An object of class `extended.family`.

WARNINGS

Do read the details section if your data contain 0s and or 1s.

Author(s)

Natalya Pya (nyp20@bath.ac.uk) and Simon Wood (s.wood@r-project.org)

Examples

```
library(mgcv)
## Simulate some beta data...
set.seed(3);n<-400
dat <- gamSim(1,n=n)
mu <- binomial()$linkinv(dat$f/4-2)
phi <- .5
a <- mu*phi;b <- phi - a;
dat$y <- rbeta(n,a,b)

bm <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=betar(link="logit"),data=dat)

bm
plot(bm,pages=1)
```


Description

mgcv works largely because many people have reported bugs over the years. If you find something that looks like a bug, please report it, so that the package can be improved. mgcv does not have a large development budget, so it is a big help if bug reports follow the following guidelines.

The ideal report consists of an email to <simon.wood@r-project.org> with a subject line including mgcv somewhere, containing

1. The results of running `sessionInfo` in the R session where the problem occurs. This provides platform details, R and package version numbers, etc.
2. A brief description of the problem.
3. Short cut and paste-able code that produces the problem, including the code for loading/generating the data (using standard R functions like `load`, `read.table` etc).
4. Any required data files. If you send real data it will only be used for the purposes of debugging.

Of course if you have dug deeper and have an idea of what is causing the problem, that is also helpful to know, as is any suggested code fix. (Don't send a fixed package .tar.gz file, however - I can't use this).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

choose.k

Basis dimension choice for smooths

Description

Choosing the basis dimension, and checking the choice, when using penalized regression smoothers.

Penalized regression smoothers gain computational efficiency by virtue of being defined using a basis of relatively modest size, k . When setting up models in the mgcv package, using `s` or `te` terms in a model formula, k must be chosen: the defaults are essentially arbitrary.

In practice $k-1$ (or k) sets the upper limit on the degrees of freedom associated with an `s` smooth (1 degree of freedom is usually lost to the identifiability constraint on the smooth). For `te` smooths the upper limit of the degrees of freedom is given by the product of the k values provided for each marginal smooth less one, for the constraint. However the actual effective degrees of freedom are controlled by the degree of penalization selected during fitting, by GCV, AIC, REML or whatever is specified. The exception to this is if a smooth is specified using the `fx=TRUE` option, in which case it is unpenalized.

So, exact choice of k is not generally critical: it should be chosen to be large enough that you are reasonably sure of having enough degrees of freedom to represent the underlying 'truth' reasonably well, but small enough to maintain reasonable computational efficiency. Clearly 'large' and 'small' are dependent on the particular problem being addressed.

As with all model assumptions, it is useful to be able to check the choice of k informally. If the effective degrees of freedom for a model term are estimated to be much less than $k-1$ then this is

unlikely to be very worthwhile, but as the EDF approach $k-1$, checking can be important. A useful general purpose approach goes as follows: (i) fit your model and extract the deviance residuals; (ii) for each smooth term in your model, fit an equivalent, single, smooth to the residuals, using a substantially increased k to see if there is pattern in the residuals that could potentially be explained by increasing k . Examples are provided below.

The obvious, but more costly, alternative is simply to increase the suspect k and refit the original model. If there are no statistically important changes as a result of doing this, then k was large enough. (Change in the smoothness selection criterion, and/or the effective degrees of freedom, when k is increased, provide the obvious numerical measures for whether the fit has changed substantially.)

`gam.check` runs a simple simulation based check on the basis dimensions, which can help to flag up terms for which k is too low. Grossly too small k will also be visible from partial residuals available with `plot.gam`.

One scenario that can cause confusion is this: a model is fitted with $k=10$ for a smooth term, and the EDF for the term is estimated as 7.6, some way below the maximum of 9. The model is then refitted with $k=20$ and the EDF increases to 8.7 - what is happening - how come the EDF was not 8.7 the first time around? The explanation is that the function space with $k=20$ contains a larger subspace of functions with EDF 8.7 than did the function space with $k=10$: one of the functions in this larger subspace fits the data a little better than did any function in the smaller subspace. These subtleties seldom have much impact on the statistical conclusions to be drawn from a model fit, however.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) Generalized Additive Models: An Introduction with R. CRC.
<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
## Simulate some data ....
library(mgcv)
set.seed(1)
dat <- gamSim(1,n=400,scale=2)

## fit a GAM with quite low `k`
b<-gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=6)+s(x3,k=6),data=dat)
plot(b,pages=1,residuals=TRUE) ## hint of a problem in s(x2)

## the following suggests a problem with s(x2)
gam.check(b)

## Another approach (see below for more obvious method)...
## check for residual pattern, removeable by increasing `k`
## typically `k`, below, should be substantially larger than
## the original, `k` but certainly less than n/2.
## Note use of cheap "cs" shrinkage smoothers, and gamma=1.4
```

```

## to reduce chance of overfitting...
rsd <- residuals(b)
gam(rsd~s(x0,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~s(x1,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~s(x2,k=40,bs="cs"),gamma=1.4,data=dat) ## `k' too low
gam(rsd~s(x3,k=40,bs="cs"),gamma=1.4,data=dat) ## fine

## refit...
b <- gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=20)+s(x3,k=6),data=dat)
gam.check(b) ## better

## similar example with multi-dimensional smooth
b1 <- gam(y~s(x0)+s(x1,x2,k=15)+s(x3),data=dat)
rsd <- residuals(b1)
gam(rsd~s(x0,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~s(x1,x2,k=100,bs="ts"),gamma=1.4,data=dat) ## `k' too low
gam(rsd~s(x3,k=40,bs="cs"),gamma=1.4,data=dat) ## fine

gam.check(b1) ## shows same problem

## and a `te' example
b2 <- gam(y~s(x0)+te(x1,x2,k=4)+s(x3),data=dat)
rsd <- residuals(b2)
gam(rsd~s(x0,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~te(x1,x2,k=10,bs="cs"),gamma=1.4,data=dat) ## `k' too low
gam(rsd~s(x3,k=40,bs="cs"),gamma=1.4,data=dat) ## fine

gam.check(b2) ## shows same problem

## same approach works with other families in the original model
dat <- gamSim(1,n=400,scale=.25,dist="poisson")
bp<-gam(y~s(x0,k=5)+s(x1,k=5)+s(x2,k=5)+s(x3,k=5),
        family=poisson,data=dat,method="ML")

gam.check(bp)

rsd <- residuals(bp)
gam(rsd~s(x0,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~s(x1,k=40,bs="cs"),gamma=1.4,data=dat) ## fine
gam(rsd~s(x2,k=40,bs="cs"),gamma=1.4,data=dat) ## `k' too low
gam(rsd~s(x3,k=40,bs="cs"),gamma=1.4,data=dat) ## fine

rm(dat)

## More obvious, but more expensive tactic... Just increase
## suspicious k until fit is stable.

set.seed(0)
dat <- gamSim(1,n=400,scale=2)
## fit a GAM with quite low `k'
b <- gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=6)+s(x3,k=6),
        data=dat,method="REML")
b

```

```

## edf for 3rd smooth is highest as proportion of k -- increase k
b <- gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=12)+s(x3,k=6),
        data=dat,method="REML")
b
## edf substantially up, -ve REML substantially down
b <- gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=24)+s(x3,k=6),
        data=dat,method="REML")
b
## slight edf increase and -ve REML change
b <- gam(y~s(x0,k=6)+s(x1,k=6)+s(x2,k=40)+s(x3,k=6),
        data=dat,method="REML")
b
## definitely stabilized (but really k around 20 would have been fine)

```

columb

Reduced version of Columbus OH crime data

Description

By district crime data from Columbus OH, together with polygons describing district shape. Useful for illustrating use of simple Markov Random Field smoothers.

Usage

```

data(columb)
data(columb.polys)

```

Format

columb is a 49 row data frame with the following columns

area land area of district

home.value housing value in 1000USD.

income household income in 1000USD.

crime residential burglaries and auto thefts per 1000 households.

open.space measure of open space in district.

district code identifying district, and matching names(columb.polys).

columb.polys contains the polygons defining the areas in the format described below.

Details

The data frame columb relates to the districts whose boundaries are coded in columb.polys. columb.polys[[i]] is a 2 column matrix, containing the vertices of the polygons defining the boundary of the ith district. columb.polys[[2]] has an artificial hole inserted to illustrate how holes in districts can be specified. Different polygons defining the boundary of a district are separated by NA rows in columb.polys[[1]], and a polygon enclosed within another is treated as a hole in that region (a hole should never come first). names(columb.polys) matches columb\$district (order unimportant).

Source

The data are adapted from the columbus example in the spdep package, where the original source is given as:

Anselin, Luc. 1988. Spatial econometrics: methods and models. Dordrecht: Kluwer Academic, Table 12.1 p. 189.

Examples

```
## see ?mrf help files
```

concurvity

GAM concurvity measures

Description

Produces summary measures of concurvity between [gam](#) components.

Usage

```
concurvity(b, full=TRUE)
```

Arguments

b	An object inheriting from class "gam".
full	If TRUE then concurvity of each term with the whole of the rest of the model is considered. If FALSE then pairwise concurvity measures between each smooth term (as well as the parametric component) are considered.

Details

Concurvity occurs when some smooth term in a model could be approximated by one or more of the other smooth terms in the model. This is often the case when a smooth of space is included in a model, along with smooths of other covariates that also vary more or less smoothly in space. Similarly it tends to be an issue in models including a smooth of time, along with smooths of other time varying covariates.

Concurvity can be viewed as a generalization of co-linearity, and causes similar problems of interpretation. It can also make estimates somewhat unstable (so that they become sensitive to apparently innocuous modelling details, for example).

This routine computes three related indices of concurvity, all bounded between 0 and 1, with 0 indicating no problem, and 1 indicating total lack of identifiability. The three indices are all based on the idea that a smooth term, f , in the model can be decomposed into a part, g , that lies entirely in the space of one or more other terms in the model, and a remainder part that is completely within the term's own space. If g makes up a large part of f then there is a concurvity problem. The indices used are all based on the square of $\|g\|/\|f\|$, that is the ratio of the squared Euclidean norms of the vectors of f and g evaluated at the observed covariate values.

The three measures are as follows

worst This is the largest value that the square of $\|g\|/\|f\|$ could take for any coefficient vector. This is a fairly pessimistic measure, as it looks at the worst case irrespective of data. This is the only measure that is symmetric.

observed This just returns the value of the square of $\|g\|/\|f\|$ according to the estimated coefficients. This could be a bit over-optimistic about the potential for a problem in some cases.

estimate This is the squared F-norm of the basis for g divided by the F-norm of the basis for f . It is a measure of the extent to which the f basis can be explained by the g basis. It does not suffer from the pessimism or potential for over-optimism of the previous two measures, but is less easy to understand.

Value

If `full=TRUE` a matrix with one column for each term and one row for each of the 3 concurvity measures detailed below. If `full=FALSE` a list of 3 matrices, one for each of the three concurvity measures detailed below. Each row of the matrix relates to how the model terms depend on the model term supplying that rows name.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
library(mgcv)
## simulate data with concurvity...
set.seed(8);n<- 200
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
      (10 * x)^3 * (1 - x)^10
t <- sort(runif(n)) ## first covariate
## make covariate x a smooth function of t + noise...
x <- f2(t) + rnorm(n)*3
## simulate response dependent on t and x...
y <- sin(4*pi*t) + exp(x/20) + rnorm(n)*.3

## fit model...
b <- gam(y ~ s(t,k=15) + s(x,k=15),method="REML")

## assess concurvity between each term and `rest of model'...
concurvity(b)

## ... and now look at pairwise concurvity between terms...
concurvity(b,full=FALSE)
```

Description

The `cox.ph` family implements the Cox Proportional Hazards model with Peto's correction for ties, and estimation by penalized partial likelihood maximization, for use with `gam`. In the model formula, event time is the response. The `weights` vector provides the censoring information (0 for censoring, 1 for event). Deals with the case in which each subject has one event/censoring time and one row of covariate values. When each subject has several time dependent covariates see `cox.pht`.

Usage

```
cox.ph(link="identity")
```

Arguments

`link` currently (and possibly for ever) only "identity" supported.

Details

Used with `gam` to fit Cox Proportional Hazards models to survival data. The model formula will have event/censoring times on the left hand side and the linear predictor specification on the right hand side. Censoring information is provided by the `weights` argument to `gam`, with 1 indicating an event and 0 indicating censoring.

Prediction from the fitted model object (using the `predict` method) with `type="response"` will predict on the survivor function scale. See example code below for extracting the cumulative baseline hazard/survival directly. Martingale or deviance residuals can be extracted. The `fitted.values` stored in the model object are survival function estimates for each subject at their event/censoring time.

Estimation of model coefficients is by maximising the log-partial likelihood penalized by the smoothing penalties. See e.g. Hastie and Tibshirani, 1990, section 8.3. for the partial likelihood used (with Peto's approximation for ties), but note that optimization of the partial likelihood does not follow Hastie and Tibshirani. See Klein and Moeschberger (2003) for estimation of residuals, the cumulative baseline hazard, survival function and associated standard errors (the survival standard error expression has a typo).

The percentage deviance explained reported for Cox PH models is based on the sum of squares of the deviance residuals, as the model deviance, and the sum of squares of the deviance residuals when the covariate effects are set to zero, as the null deviance. The same baseline hazard estimate is used for both.

This family deals efficiently with the case in which each subject has one event/censoring time and one row of covariate values. For studies in which there are multiple time varying covariate measures for each subject then the equivalent Poisson model should be fitted to suitable pseudodata using `bam(..., discrete=TRUE)`.

Value

An object inheriting from class `general.family`.

References

Hastie and Tibshirani (1990) *Generalized Additive Models*, Chapman and Hall.

Klein, J.P and Moeschberger, M.L. (2003) *Survival Analysis: Techniques for Censored and Truncated Data* (2nd ed.) Springer.

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

Examples

```
library(mgcv)
library(survival) ## for data
col1 <- colon[colon$type==1,] ## concentrate on single event
col1$differ <- as.factor(col1$differ)
col1$sex <- as.factor(col1$sex)

b <- gam(time~s(age,by=sex)+sex+s(nodes)+perfor+rx+obstruct+adhere,
         family=cox.ph(),data=col1,weights=status)

summary(b)

plot(b,pages=1,all.terms=TRUE) ## plot effects

plot(b$linear.predictors,residuals(b))

## plot survival function for patient j...

np <- 300;j <- 6
newd <- data.frame(time=seq(0,3000,length=np))
dname <- names(col1)
for (n in dname) newd[[n]] <- rep(col1[[n]][j],np)
newd$time <- seq(0,3000,length=np)
fv <- predict(b,newdata=newd,type="response",se=TRUE)
plot(newd$time,fv$fit,type="l",ylim=c(0,1),xlab="time",ylab="survival")
lines(newd$time,fv$fit+2*fv$se.fit,col=2)
lines(newd$time,fv$fit-2*fv$se.fit,col=2)

## crude plot of baseline survival...

plot(b$family$data$tr,exp(-b$family$data$h),type="l",ylim=c(0,1),
     xlab="time",ylab="survival")
lines(b$family$data$tr,exp(-b$family$data$h + 2*b$family$data$q^.5),col=2)
lines(b$family$data$tr,exp(-b$family$data$h - 2*b$family$data$q^.5),col=2)
lines(b$family$data$tr,exp(-b$family$data$km),lty=2) ## Kaplan Meier

## Simple simulated known truth example...
ph.weibull.sim <- function(eta,gamma=1,h0=.01,t1=100) {
```



```

lambda <- h0*exp(eta)
n <- length(eta)
U <- runif(n)
t <- (-log(U)/lambda)^(1/gamma)
d <- as.numeric(t <= t1)
t[!d] <- t1
list(t=t,d=d)
}
n <- 500;set.seed(2)
x0 <- runif(n, 0, 1);x1 <- runif(n, 0, 1)
x2 <- runif(n, 0, 1);x3 <- runif(n, 0, 1)
f0 <- function(x) 2 * sin(pi * x)
f1 <- function(x) exp(2 * x)
f2 <- function(x) 0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10
f3 <- function(x) 0*x
f <- f0(x0) + f1(x1) + f2(x2)
g <- (f-mean(f))/5
surv <- ph.weibull.sim(g)
surv$x0 <- x0;surv$x1 <- x1;surv$x2 <- x2;surv$x3 <- x3

b <- gam(t~s(x0)+s(x1)+s(x2,k=15)+s(x3),family=cox.ph,weights=d,data=surv)

plot(b,pages=1)

```

Description

The `cox.ph` family only allows one set of covariate values per subject. If each subject has several time varying covariate measurements then it is still possible to fit a proportional hazards regression model, via an equivalent Poisson model. The recipe is provided by Whitehead (1980) and is equally valid in the smooth additive case. Its drawback is that the equivalent Poisson dataset can be quite large.

The trick is to generate an artificial Poisson observation for each subject in the risk set at each non-censored event time. The corresponding covariate values for each subject are whatever they are at the event time, while the Poisson response is zero for all subjects except those experiencing the event at that time (this corresponds to Peto's correction for ties). The linear predictor for the model must include an intercept for each event time (the cumulative sum of the exponential of these is the Breslow estimate of the baseline hazard).

Below is some example code employing this trick for the `pbcsseq` data from the `survival` package. It uses `bam` for fitting with the `discrete=TRUE` option for efficiency: there is some approximation involved in doing this, and the exact equivalent to what is done in `cox.ph` is rather obtained by using `gam` with `method="REML"` (taking some 14 times the computational time for the example below).

The function `tdpois` in the example code uses crude piecewise constant interpolation for the covariates, in which the covariate value at an event time is taken to be whatever it was the previous time that it was measured. Obviously more sophisticated interpolation schemes might be preferable.

References

Whitehead (1980) Fitting Cox's regression model to survival data using GLIM. *Applied Statistics* 29(3):268-275

Examples

```
require(mgcv);require(survival)

## First define functions for producing Poisson model data frame

app <- function(x,t,to) {
  ## wrapper to approx for calling from apply...
  y <- if (sum(!is.na(x))<1) rep(NA,length(to)) else
    approx(t,x,to,method="constant",rule=2)$y
  if (is.factor(x)) factor(levels(x)[y],levels=levels(x)) else y
} ## app

tdpois <- function(dat,event="z",et="fuptime",t="day",status="status1",
                  id="id") {
  ## dat is data frame. id is patient id; et is event time; t is
  ## observation time; status is 1 for death 0 otherwise;
  ## event is name for Poisson response.
  if (event %in% names(dat)) warning("event name in use")
  require(utils) ## for progress bar
  te <- sort(unique(dat[[et]][dat[[status]]==1])) ## event times
  sid <- unique(dat[[id]])
  prg <- txtProgressBar(min = 0, max = length(sid), initial = 0,
    char = "=",width = NA, title="Progress", style = 3)
  ## create dataframe for poisson model data
  dat[[event]] <- 0; start <- 1
  dap <- dat[rep(1:length(sid),length(te)),]
  for (i in 1:length(sid)) { ## work through patients
    di <- dat[dat[[id]]==sid[i],] ## ith patient's data
    tr <- te[te <= di[[et]][1]] ## times required for this patient
    ## Now do the interpolation of covariates to event times...
    um <- data.frame(lapply(X=di,FUN=app,t=di[[t]],to=tr))
    ## Mark the actual event...
    if (um[[et]][1]==max(tr)&&um[[status]]==1) um[[event]][nrow(um)] <- 1
    um[[et]] <- tr ## reset time to relevant event times
    dap[start:(start-1+nrow(um)),] <- um ## copy to dap
    start <- start + nrow(um)
    setTxtProgressBar(prg, i)
  }
  close(prg)
  dap[1:(start-1),]
} ## tdpois

## The following takes too long for CRAN checking
## (but typically takes a minute or less).
## Not run:
## Convert pbcseq to equivalent Poisson form...
pbcseq$status1 <- as.numeric(pbcseq$status==2) ## death indicator
```

```

pb <- tdpois(pbcseq) ## conversion
pb$tf <- factor(pb$futime) ## add factor for event time

## Fit Poisson model...
b <- bam(z ~ tf - 1 + sex + trt + s(sqrt(protime)) + s(platelet)+ s(age)+
s(bili)+s(albumin), family=poisson,data=pb,discrete=TRUE,nthreads=2)

par(mfrow=c(2,3))
plot(b,scale=0)

## compute residuals...
chaz <- tapply(fitted(b),pb$id,sum) ## cum haz by subject
d <- tapply(pb$z,pb$id,sum) ## censoring indicator
mrtd <- d - chaz ## Martingale
drsd <- sign(mrtd)*sqrt(-2*(mrtd + d*log(chaz))) ## deviance

## plot survivor function and s.e. band for subject 25
te <- sort(unique(pb$futime)) ## event times
di <- pbcseq[pbcseq$id==25,] ## data for subject 25
pd <- data.frame(lapply(X=di,FUN=app,t=di$day,to=te)) ## interpolate to te
pd$tf <- factor(te)
X <- predict(b,newdata=pd,type="lpmatrix")
eta <- drop(X%%coef(b)); H <- cumsum(exp(eta))
J <- apply(exp(eta)*X,2,cumsum)
se <- diag(J%%vcov(b)%%t(J))^0.5
plot(stepfun(te,c(1,exp(-H))),do.points=FALSE,ylim=c(0.7,1),
      ylab="S(t)",xlab="t (days)",main="",lwd=2)
lines(stepfun(te,c(1,exp(-H+se))),do.points=FALSE)
lines(stepfun(te,c(1,exp(-H-se))),do.points=FALSE)
rug(pbcseq$day[pbcseq$id==25]) ## measurement times

## End(Not run)

```

cSplineDes

Evaluate cyclic B spline basis

Description

Uses splineDesign to set up the model matrix for a cyclic B-spline basis.

Usage

```
cSplineDes(x, knots, ord = 4, derivs=0)
```

Arguments

x	covariate values for smooth.
knots	The knot locations: the range of these must include all the data.
ord	order of the basis. 4 is a cubic spline basis. Must be >1.

derivs order of derivative of the spline to evaluate, between 0 and ord-1. Recycled to length of x.

Details

The routine is a wrapper that sets up a B-spline basis, where the basis functions wrap at the first and last knot locations.

Value

A matrix with `length(x)` rows and `length(knots)-1` columns.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[cyclic.p.spline](#)

Examples

```
require(mgcv)
## create some x's and knots...
n <- 200
x <- 0:(n-1)/(n-1);k<- 0:5/5
X <- cSplineDes(x,k) ## cyclic spline design matrix
## plot evaluated basis functions...
plot(x,X[,1],type="l"); for (i in 2:5) lines(x,X[,i],col=i)
## check that the ends match up...
ee <- X[1,]-X[n,];ee
tol <- .Machine$double.eps^.75
if (all.equal(ee,ee*0,tolerance=tol)!=TRUE)
  stop("cyclic spline ends don't match!")

## similar with uneven data spacing...
x <- sort(runif(n)) + 1 ## sorting just makes end checking easy
k <- seq(min(x),max(x),length=8) ## create knots
X <- cSplineDes(x,k) ## get cyclic spline model matrix
plot(x,X[,1],type="l"); for (i in 2:ncol(X)) lines(x,X[,i],col=i)
ee <- X[1,]-X[n,];ee ## do ends match??
tol <- .Machine$double.eps^.75
if (all.equal(ee,ee*0,tolerance=tol)!=TRUE)
  stop("cyclic spline ends don't match!")
```

exclude.too.far	<i>Exclude prediction grid points too far from data</i>
-----------------	---

Description

Takes two arrays defining the nodes of a grid over a 2D covariate space and two arrays defining the location of data in that space, and returns a logical vector with elements TRUE if the corresponding node is too far from data and FALSE otherwise. Basically a service routine for `vis.gam` and `plot.gam`.

Usage

```
exclude.too.far(g1,g2,d1,d2,dist)
```

Arguments

<code>g1</code>	co-ordinates of grid relative to first axis.
<code>g2</code>	co-ordinates of grid relative to second axis.
<code>d1</code>	co-ordinates of data relative to first axis.
<code>d2</code>	co-ordinates of data relative to second axis.
<code>dist</code>	how far away counts as too far. Grid and data are first scaled so that the grid lies exactly in the unit square, and <code>dist</code> is a distance within this unit square.

Details

Linear scalings of the axes are first determined so that the grid defined by the nodes in `g1` and `g2` lies exactly in the unit square (i.e. on $[0,1]$ by $[0,1]$). These scalings are applied to `g1`, `g2`, `d1` and `d2`. The minimum Euclidean distance from each node to a datum is then determined and if it is greater than `dist` the corresponding entry in the returned array is set to TRUE (otherwise to FALSE). The distance calculations are performed in compiled code for speed without storage overheads.

Value

A logical array with TRUE indicating a node in the grid defined by `g1`, `g2` that is 'too far' from any datum.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[vis.gam](#)

Examples

```
library(mgcv)
x<-rnorm(100);y<-rnorm(100) # some "data"
n<-40 # generate a grid...
mx<-seq(min(x),max(x),length=n)
my<-seq(min(y),max(y),length=n)
gx<-rep(mx,n);gy<-rep(my,rep(n,n))
tf<-exclude.too.far(gx,gy,x,y,0.1)
plot(gx[!tf],gy[!tf],pch=".");points(x,y,col=2)
```

extract.lme.cov

Extract the data covariance matrix from an lme object

Description

This is a service routine for [gamm](#). Extracts the estimated covariance matrix of the data from an `lme` object, allowing the user control about which levels of random effects to include in this calculation. `extract.lme.cov` forms the full matrix explicitly: `extract.lme.cov2` tries to be more economical than this.

Usage

```
extract.lme.cov(b,data,start.level=1)
extract.lme.cov2(b,data,start.level=1)
```

Arguments

<code>b</code>	A fitted model object returned by a call to lme .
<code>data</code>	The data frame/ model frame that was supplied to lme .
<code>start.level</code>	The level of nesting at which to start including random effects in the calculation. This is used to allow smooth terms to be estimated as random effects, but treated like fixed effects for variance calculations.

Details

The random effects, correlation structure and variance structure used for a linear mixed model combine to imply a covariance matrix for the response data being modelled. These routines extract that covariance matrix. The process is slightly complicated, because different components of the fitted model object are stored in different orders (see function code for details!).

The `extract.lme.cov` calculation is not optimally efficient, since it forms the full matrix, which may in fact be sparse. `extract.lme.cov2` is more efficient. If the covariance matrix is diagonal, then only the leading diagonal is returned; if it can be written as a block diagonal matrix (under some permutation of the original data) then a list of matrices defining the non-zero blocks is returned along with an index indicating which row of the original data each row/column of the block diagonal matrix relates to. The block sizes are defined by the coarsest level of grouping in the random effect structure.

[gamm](#) uses `extract.lme.cov2`.

`extract.lme.cov` does not currently deal with the situation in which the grouping factors for a correlation structure are finer than those for the random effects. `extract.lme.cov2` does deal with this situation.

Value

For `extract.lme.cov` an estimated covariance matrix.

For `extract.lme.cov2` a list containing the estimated covariance matrix and an indexing array. The covariance matrix is stored as the elements on the leading diagonal, a list of the matrices defining a block diagonal matrix, or a full matrix if the previous two options are not possible.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

For `lme` see:

Pinheiro J.C. and Bates, D.M. (2000) *Mixed effects Models in S and S-PLUS*. Springer

For details of how GAMMs are set up here for estimation using `lme` see:

Wood, S.N. (2006) Low rank scale invariant tensor product smooths for Generalized Additive Mixed Models. *Biometrics* 62(4):1025-1036

or

Wood S.N. (2006) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gamm](#), [formXtViX](#)

Examples

```
## see also ?formXtViX for use of extract.lme.cov2
require(mgcv)
library(nlme)
data(Rail)
b <- lme(travel~1,Rail,~1|Rail)
extract.lme.cov(b,Rail)
```

Description

As well as the standard families documented in `family` (see also `glm`) which can be used with functions `gam`, `bam` and `gamm`, `mgcv` also supplies some extra families, most of which are currently only usable with `gam`. These are described here.

Details

The following families are in the exponential family given the value of a single parameter. They are usable with all modelling functions.

- `Tweedie` An exponential family distribution for which the variance of the response is given by the mean response to the power p . p is in $(1,2)$ and must be supplied. See `tw` to estimate p .
- `negbin` The negative binomial. See `nb` to estimate the θ parameter of the negative binomial.

The following families are for regression type models dependent on a single linear predictor, and with a log likelihood which is a sum of independent terms, each corresponding to a single response observation. Usable only with `gam`, with smoothing parameter estimation by "REML" or "ML" (the latter does not integrate the unpenalized and parametric effects out of the marginal likelihood optimized for the smoothing parameters).

- `ocat` for ordered categorical data.
- `tw` for Tweedie distributed data, when the power parameter relating the variance to the mean is to be estimated.
- `nb` for negative binomial data when the θ parameter is to be estimated.
- `betar` for proportions data on $(0,1)$ when the binomial is not appropriate.
- `scat` scaled t for heavy tailed data that would otherwise be modelled as Gaussian.
- `zip` for zero inflated Poisson data, when the zero inflation rate depends simply on the Poisson mean.

The following families implement more general model classes. Usable only with `gam` and only with REML smoothing parameter estimation.

- `cox.ph` the Cox Proportional Hazards model for survival data.
- `gaulss` a Gaussian location-scale model where the mean and the standard deviation are both modelled using smooth linear predictors.
- `gevlss` a generalized extreme value (GEV) model where the location, scale and shape parameters are each modelled using a linear predictor.
- `ziplss` a 'two-stage' zero inflated Poisson model, in which 'potential-presence' is modelled with one linear predictor, and Poisson mean abundance given potential presence is modelled with a second linear predictor.
- `mvn`: multivariate normal additive models.
- `multinom`: multinomial logistic regression, for unordered categorical responses.

Author(s)

Simon N. Wood (s.wood@r-project.org) & Natalya Pya

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. Journal of the American Statistical Association. <http://arxiv.org/abs/1511.03864>

fix.family.link

Modify families for use in GAM fitting and checking

Description

Generalized Additive Model fitting by ‘outer’ iteration, requires extra derivatives of the variance and link functions to be added to family objects. The first 3 functions add what is needed. Model checking can be aided by adding quantile and random deviate generating functions to the family. The final two functions do this.

Usage

```
fix.family.link(fam)
fix.family.var(fam)
fix.family.ls(fam)
fix.family.qf(fam)
fix.family.rd(fam)
```

Arguments

fam A family.

Details

Consider the first 3 function first.

Outer iteration GAM estimation requires derivatives of the GCV, UBRE/gAIC, GACV, REML or ML score, which are obtained by finding the derivatives of the model coefficients w.r.t. the log smoothing parameters, using the implicit function theorem. The expressions for the derivatives require the second and third derivatives of the link w.r.t. the mean (and the 4th derivatives if Fisher scoring is not used). Also required are the first and second derivatives of the variance function w.r.t. the mean (plus the third derivative if Fisher scoring is not used). Finally REML or ML estimation of smoothing parameters requires the log saturated likelihood and its first two derivatives w.r.t. the scale parameter. These functions add functions evaluating these quantities to a family.

If the family already has functions dvar, d2var, d3var, d2link, d3link, d4link and for RE/ML ls, then these functions simply return the family unmodified: this allows non-standard links to be used with `gam` when using outer iteration (performance iteration operates with unmodified families). Note that if you only need Fisher scoring then d4link and d3var can be dummy, as they are ignored. Similarly ls is only needed for RE/ML.

The `dvar` function is a function of a mean vector, `mu`, and returns a vector of corresponding first derivatives of the family variance function. The `d2link` function is also a function of a vector of mean values, `mu`: it returns a vector of second derivatives of the link, evaluated at `mu`. Higher derivatives are defined similarly.

If modifying your own family, note that you can often get away with supplying only a `dvar` and `d2var`, function if your family only requires links that occur in one of the standard families.

The second two functions are useful for investigating the distribution of residuals and are used by [qq.gam](#). If possible the functions add quantile (`qf`) or random deviate (`rd`) generating functions to the family. If a family already has `qf` or `rd` functions then it is left unmodified. `qf` functions are only available for some families, and for quasi families neither type of function is available.

Value

A family object with extra component functions `dvar`, `d2var`, `d2link`, `d3link`, `d4link`, `ls`, and possibly `qf` and `rd`, depending on which functions are called.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam.fit3](#), [qq.gam](#)

fixDependence

Detect linear dependencies of one matrix on another

Description

Identifies columns of a matrix `X2` which are linearly dependent on columns of a matrix `X1`. Primarily of use in setting up identifiability constraints for nested GAMs.

Usage

```
fixDependence(X1, X2, tol=.Machine$double.eps^.5, rank.def=0, strict=FALSE)
```

Arguments

<code>X1</code>	A matrix.
<code>X2</code>	A matrix, the columns of which may be partially linearly dependent on the columns of <code>X1</code> .
<code>tol</code>	The tolerance to use when assessing linear dependence.
<code>rank.def</code>	If the degree of rank deficiency in <code>X2</code> , given <code>X1</code> , is known, then it can be supplied here, and <code>tol</code> is then ignored. Unused unless positive and not greater than the number of columns in <code>X2</code> .
<code>strict</code>	if TRUE then only columns individually dependent on <code>X1</code> are detected, if FALSE then enough columns to make the reduced <code>X2</code> full rank and independent of <code>X1</code> are detected.

Details

The algorithm uses a simple approach based on QR decomposition: see Wood (2006, section 4.10.2) for details.

Value

A vector of the columns of X2 which are linearly dependent on columns of X1 (or which need to be deleted to achieve independence and full rank if `strict==FALSE`). NULL if the two matrices are independent.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

Examples

```
library(mgcv)
n<-20;c1<-4;c2<-7
X1<-matrix(runif(n*c1),n,c1)
X2<-matrix(runif(n*c2),n,c2)
X2[,3]<-X1[,2]+X2[,4]*.1
X2[,5]<-X1[,1]*.2+X1[,2]*.04
fixDependence(X1,X2)
fixDependence(X1,X2,strict=TRUE)
```

formula.gam

GAM formula

Description

Description of [gam](#) formula (see Details), and how to extract it from a fitted gam object.

Usage

```
## S3 method for class 'gam'
formula(x,...)
```

Arguments

x fitted model objects of class gam (see [gamObject](#)) as produced by gam().
 ... un-used in this case

Details

`gam` will accept a formula or, with some families, a list of formulae. Other mgcv modelling functions will not accept a list. The list form provides a mechanism for specifying several linear predictors, and allows these to share terms: see below.

The formulae supplied to `gam` are exactly like those supplied to `glm` except that smooth terms, `s`, `te`, `ti` and `t2` can be added to the right hand side (and `.` is not supported in `gam` formulae).

Smooth terms are specified by expressions of the form:

```
s(x1, x2, ..., k=12, fx=FALSE, bs="tp", by=z, id=1)
```

where `x1`, `x2`, etc. are the covariates which the smooth is a function of, and `k` is the dimension of the basis used to represent the smooth term. If `k` is not specified then basis specific defaults are used. Note that these defaults are essentially arbitrary, and it is important to check that they are not so small that they cause oversmoothing (too large just slows down computation). Sometimes the modelling context suggests sensible values for `k`, but if not informal checking is easy: see `choose.k` and `gam.check`.

`fx` is used to indicate whether or not this term should be unpenalized, and therefore have a fixed number of degrees of freedom set by `k` (almost always `k-1`). `bs` indicates the basis to use for the smooth: the built in options are described in `smooth.terms`, and user defined smooths can be added (see `user.defined.smooth`). If `bs` is not supplied then the default "tp" (`tprs`) basis is used. `by` can be used to specify a variable by which the smooth should be multiplied. For example `gam(y~s(x, by=z))` would specify a model $E(y) = f(x)z$ where $f(\cdot)$ is a smooth function. The `by` option is particularly useful for models in which different functions of the same variable are required for each level of a factor and for 'varying coefficient models': see `gam.models`. `id` is used to give smooths identities: smooths with the same identity have the same basis, penalty and smoothing parameter (but different coefficients, so they are different functions).

An alternative for specifying smooths of more than one covariate is e.g.:

```
te(x, z, bs=c("tp", "tp"), m=c(2, 3), k=c(5, 10))
```

which would specify a tensor product smooth of the two covariates `x` and `z` constructed from marginal t.p.r.s. bases of dimension 5 and 10 with marginal penalties of order 2 and 3. Any combination of basis types is possible, as is any number of covariates. `te` provides further information. `ti` terms are a variant designed to be used as interaction terms when the main effects (and any lower order interactions) are present. `t2` produces tensor product smooths that are the natural low rank analogue of smoothing spline anova models.

`s`, `te`, `ti` and `t2` terms accept an `sp` argument of supplied smoothing parameters: positive values are taken as fixed values to be used, negative to indicate that the parameter should be estimated. If `sp` is supplied then it over-rides whatever is in the `sp` argument to `gam`, if it is not supplied then it defaults to all negative, but does not over-ride the `sp` argument to `gam`.

Formulae can involve nested or "overlapping" terms such as

```
y~s(x)+s(z)+s(x, z) or y~s(x, z)+s(z, v)
```

but nested models should really be set up using `ti` terms: see `gam.side` for further details and examples.

Smooth terms in a `gam` formula will accept matrix arguments as covariates (and corresponding by variable), in which case a 'summation convention' is invoked. Consider the example of `s(X, Z, by=L)` where `X`, `Z` and `L` are `n` by `m` matrices. Let `F` be the `n` by `m` matrix that results from evaluating the smooth at the values in `X` and `Z`. Then the contribution to the linear predictor from the term will be `rowSums(F*L)` (note the element-wise multiplication). This convention allows the linear predictor of the GAM to depend on (a discrete approximation to) any linear functional of a smooth:

see [linear.functional.terms](#) for more information and examples (including functional linear models/signal regression).

Note that `gam` allows any term in the model formula to be penalized (possibly by multiple penalties), via the `paraPen` argument. See [gam.models](#) for details and example code.

When several formulae are provided in a list, then they can be used to specify multiple linear predictors for families for which this makes sense (e.g. `mvn`). The first formula in the list must include a response variable, but later formulae need not (depending on the requirements of the family). Let the linear predictors be indexed, 1 to `d` where `d` is the number of linear predictors, and the indexing is in the order in which the formulae appear in the list. It is possible to supply extra formulae specifying that several linear predictors should share some terms. To do this a formula is supplied in which the response is replaced by numbers specifying the indices of the linear predictors which will share the terms specified on the r.h.s. For example `1+3~s(x)+z-1` specifies that linear predictors 1 and 3 will share the terms `s(x)` and `z` (but we don't want an extra intercept, as this would usually be unidentifiable). Note that it is possible that a linear predictor only includes shared terms: it must still have its own formula, but the r.h.s. would simply be `-1` (e.g. `y ~ -1` or `~ -1`).

Value

Returns the model formula, `x$formula`. Provided so that `anova` methods print an appropriate description of the model.

WARNING

A `codegam` formula should not refer to variables using e.g. `dat[["x"]]`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam](#)

formXtViX

Form component of GAMM covariance matrix

Description

This is a service routine for [gamm](#). Given, V , an estimated covariance matrix obtained using [extract.lme.cov2](#) this routine forms a matrix square root of $X^T V^{-1} X$ as efficiently as possible, given the structure of V (usually sparse).

Usage

```
formXtViX(V,X)
```

Arguments

V	A data covariance matrix list returned from <code>extract.lme.cov2</code>
X	A model matrix.

Details

The covariance matrix returned by `extract.lme.cov2` may be in a packed and re-ordered format, since it is usually sparse. Hence a special service routine is required to form the required products involving this matrix.

Value

A matrix, R such that `crossprod(R)` gives $X^T V^{-1} X$.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

For lme see:

Pinheiro J.C. and Bates, D.M. (2000) Mixed effects Models in S and S-PLUS. Springer

For details of how GAMMs are set up for estimation using lme see:

Wood, S.N. (2006) Low rank scale invariant tensor product smooths for Generalized Additive Mixed Models. *Biometrics* 62(4):1025-1036

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gamm](#), [extract.lme.cov2](#)

Examples

```
require(mgcv)
library(nlme)
data(ergoStool)
b <- lme(effort ~ Type, data=ergoStool, random=~1|Subject)
V1 <- extract.lme.cov(b, ergoStool)
V2 <- extract.lme.cov2(b, ergoStool)
X <- model.matrix(b, data=ergoStool)
crossprod(formXtViX(V2, X))
t(X)
```

fs.test	<i>FELSPLINE test function</i>
---------	--------------------------------

Description

Implements a finite area test function based on one proposed by Tim Ramsay (2002).

Usage

```
fs.test(x,y,r0=.1,r=.5,l=3,b=1,exclude=TRUE)
fs.boundary(r0=.1,r=.5,l=3,n.theta=20)
```

Arguments

x,y	Points at which to evaluate the test function.
r0	The test domain is a sort of bent sausage. This is the radius of the inner bend
r	The radius of the curve at the centre of the sausage.
l	The length of an arm of the sausage.
b	The rate at which the function increases per unit increase in distance along the centre line of the sausage.
exclude	Should exterior points be set to NA?
n.theta	How many points to use in a piecewise linear representation of a quarter of a circle, when generating the boundary curve.

Details

The function details are not given in the source article: but this is pretty close. The function is modified from Ramsay (2002), in that it bulges, rather than being flat: this makes a better test of the smoother.

Value

fs.test returns function evaluations, or NAs for points outside the boundary. fs.boundary returns a list of x,y points to be jointed up in order to define/draw the boundary.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Tim Ramsay (2002) "Spline smoothing over difficult regions" J.R.Statist. Soc. B 64(2):307-319

Examples

```

require(mgcv)
## plot the function, and its boundary...
fsb <- fs.boundary()
m<-300;n<-150
xm <- seq(-1,4,length=m);yn<-seq(-1,1,length=n)
xx <- rep(xm,n);yy<-rep(yn,rep(m,n))
tru <- matrix(fs.test(xx,yy),m,n) ## truth
image(xm,yn,tru,col=heat.colors(100),xlab="x",ylab="y")
lines(fsb$x,fsb$y,lwd=3)
contour(xm,yn,tru,levels=seq(-5,5,by=.25),add=TRUE)

```

full.score

GCV/UBRE score for use within nlm

Description

Evaluates GCV/UBRE score for a GAM, given smoothing parameters. The routine calls `gam.fit` to fit the model, and is usually called by `nlm` to optimize the smoothing parameters.

This is basically a service routine for `gam`, and is not usually called directly by users. It is only used in this context for GAMs fitted by outer iteration (see `gam.outer`) when the the outer method is "nlm.fd" (see `gam` argument optimizer).

Usage

```
full.score(sp,G,family,control,gamma,...)
```

Arguments

sp	The logs of the smoothing parameters
G	a list returned by <code>mgcv::gam.setup</code>
family	The family object for the GAM.
control	a list returned by <code>gam.control</code>
gamma	the degrees of freedom inflation factor (usually 1).
...	other arguments, typically for passing on to <code>gam.fit</code> .

Value

The value of the GCV/UBRE score, with attribute "full.gam.object" which is the full object returned by `gam.fit`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Description

Fits a generalized additive model (GAM) to data, the term ‘GAM’ being taken to include any quadratically penalized GLM and a variety of other models estimated by a quadratically penalised likelihood type approach (see [family.mgcv](#)). The degree of smoothness of model terms is estimated as part of fitting. `gam` can also fit any GLM subject to multiple quadratic penalties (including estimation of degree of penalization). Confidence/credible intervals are readily available for any quantity predicted using a fitted model.

Smooth terms are represented using penalized regression splines (or similar smoothers) with smoothing parameters selected by GCV/UBRE/AIC/REML or by regression splines with fixed degrees of freedom (mixtures of the two are permitted). Multi-dimensional smooths are available using penalized thin plate regression splines (isotropic) or tensor product splines (when an isotropic smooth is inappropriate), and users can add smooths. Linear functionals of smooths can also be included in models. For an overview of the smooths available see [smooth.terms](#). For more on specifying models see [gam.models](#), [random.effects](#) and [linear.functional.terms](#). For more on model selection see [gam.selection](#). Do read [gam.check](#) and [choose.k](#).

See [gam](#) from package `gam`, for GAMs via the original Hastie and Tibshirani approach (see details for differences to this implementation).

For very large datasets see [bam](#), for mixed GAM see [gamm](#) and [random.effects](#).

Usage

```
gam(formula, family=gaussian(), data=list(), weights=NULL, subset=NULL,
    na.action, offset=NULL, method="GCV.Cp",
    optimizer=c("outer", "newton"), control=list(), scale=0,
    select=FALSE, knots=NULL, sp=NULL, min.sp=NULL, H=NULL, gamma=1,
    fit=TRUE, paraPen=NULL, G=NULL, in.out, drop.unused.levels=TRUE,
    drop.intercept=NULL, ...)
```

Arguments

formula	A GAM formula, or a list of formulae (see formula.gam and also gam.models). These are exactly like the formula for a GLM except that smooth terms, <code>s</code> , <code>te</code> , <code>ti</code> and <code>t2</code> , can be added to the right hand side to specify that the linear predictor depends on smooth functions of predictors (or linear functionals of these).
family	This is a family object specifying the distribution and link to use in fitting etc (see <code>glm</code> and family). See family.mgcv for a full list of what is available, which goes well beyond exponential family. Note that quasi families actually result in the use of extended quasi-likelihood if <code>method</code> is set to a RE/ML method (McCullagh and Nelder, 1989, 9.6).

data	A data frame or list containing the model response variable and covariates required by the formula. By default the variables are taken from <code>environment(formula)</code> : typically the environment from which <code>gam</code> is called.
weights	prior weights on the contribution of the data to the log likelihood. Note that a weight of 2, for example, is equivalent to having made exactly the same observation twice. If you want to reweight the contributions of each datum without changing the overall magnitude of the log likelihood, then you should normalize the weights (e.g. <code>weights <- weights/mean(weights)</code>).
subset	an optional vector specifying a subset of observations to be used in the fitting process.
na.action	a function which indicates what should happen when the data contain 'NA's. The default is set by the 'na.action' setting of 'options', and is 'na.fail' if that is unset. The "factory-fresh" default is 'na.omit'.
offset	Can be used to supply a model offset for use in fitting. Note that this offset will always be completely ignored when predicting, unlike an offset included in <code>formula</code> (this used to conform to the behaviour of <code>lm</code> and <code>glm</code>).
control	A list of fit control parameters to replace defaults returned by <code>gam.control</code> . Values not set assume default values.
method	The smoothing parameter estimation method. "GCV.Cp" to use GCV for unknown scale parameter and Mallows' Cp/UBRE/AIC for known scale. "GACV.Cp" is equivalent, but using GACV in place of GCV. "REML" for REML estimation, including of unknown scale, "P-REML" for REML estimation, but using a Pearson estimate of the scale. "ML" and "P-ML" are similar, but using maximum likelihood in place of REML. Beyond the exponential family "REML" is the default, and the only other option is "ML".
optimizer	An array specifying the numerical optimization method to use to optimize the smoothing parameter estimation criterion (given by <code>method</code>). "perf" for performance iteration. "outer" for the more stable direct approach. "outer" can use several alternative optimizers, specified in the second element of <code>optimizer</code> : "newton" (default), "bfgs", "optim", "nlm" and "nlm.fd" (the latter is based entirely on finite differenced derivatives and is very slow). "efs" for the extended Fellner Schall method - only currently available for general families.
scale	If this is positive then it is taken as the known scale parameter. Negative signals that the scale parameter is unknown. 0 signals that the scale parameter is 1 for Poisson and binomial and unknown otherwise. Note that (RE)ML methods can only work with scale parameter 1 for the Poisson and binomial cases.
select	If this is TRUE then <code>gam</code> can add an extra penalty to each term so that it can be penalized to zero. This means that the smoothing parameter estimation that is part of fitting can completely remove terms from the model. If the corresponding smoothing parameter is estimated as zero then the extra penalty has no effect.
knots	this is an optional list containing user specified knot values to be used for basis construction. For most bases the user simply supplies the knots to be used, which must match up with the <code>k</code> value supplied (note that the number of knots is not always just <code>k</code>). See tprs for what happens in the "tp"/"ts" case. Different terms can use different numbers of knots, unless they share a covariate.

sp	A vector of smoothing parameters can be provided here. Smoothing parameters must be supplied in the order that the smooth terms appear in the model formula. Negative elements indicate that the parameter should be estimated, and hence a mixture of fixed and estimated parameters is possible. If smooths share smoothing parameters then <code>length(sp)</code> must correspond to the number of underlying smoothing parameters.
min.sp	Lower bounds can be supplied for the smoothing parameters. Note that if this option is used then the smoothing parameters <code>full.sp</code> , in the returned object, will need to be added to what is supplied here to get the smoothing parameters actually multiplying the penalties. <code>length(min.sp)</code> should always be the same as the total number of penalties (so it may be longer than <code>sp</code> , if smooths share smoothing parameters).
H	A user supplied fixed quadratic penalty on the parameters of the GAM can be supplied, with this as its coefficient matrix. A common use of this term is to add a ridge penalty to the parameters of the GAM in circumstances in which the model is close to un-identifiable on the scale of the linear predictor, but perfectly well defined on the response scale.
gamma	It is sometimes useful to inflate the model degrees of freedom in the GCV or UBRE/AIC score by a constant multiplier. This allows such a multiplier to be supplied.
fit	If this argument is TRUE then <code>gam</code> sets up the model and fits it, but if it is FALSE then the model is set up and an object <code>G</code> containing what would be required to fit is returned. See argument <code>G</code> .
paraPen	optional list specifying any penalties to be applied to parametric model terms. gam.models explains more.
G	Usually NULL, but may contain the object returned by a previous call to <code>gam</code> with <code>fit=FALSE</code> , in which case all other arguments are ignored except for <code>gamma</code> , <code>in.out</code> , <code>scale</code> , <code>control</code> , <code>method</code> optimizer and <code>fit</code> .
in.out	optional list for initializing outer iteration. If supplied then this must contain two elements: <code>sp</code> should be an array of initialization values for all smoothing parameters (there must be a value for all smoothing parameters, whether fixed or to be estimated, but those for fixed s.p.s are not used); <code>scale</code> is the typical scale of the GCV/UBRE function, for passing to the outer optimizer, or the the initial value of the scale parameter, if this is to be estimated by RE/ML.
drop.unused.levels	by default unused levels are dropped from factors before fitting. For some smooths involving factor variables you might want to turn this off. Only do so if you know what you are doing.
drop.intercept	Set to TRUE to force the model to really not have the a constant in the parametric model part, even with factor variables present. Can be vector when formula is a list.
...	further arguments for passing on e.g. to <code>gam.fit</code> (such as <code>mustart</code>).

Details

A generalized additive model (GAM) is a generalized linear model (GLM) in which the linear predictor is given by a user specified sum of smooth functions of the covariates plus a conventional

parametric component of the linear predictor. A simple example is:

$$\log(E(y_i)) = \alpha + f_1(x_{1i}) + f_2(x_{2i})$$

where the (independent) response variables $y_i \sim \text{Poi}$, and f_1 and f_2 are smooth functions of covariates x_1 and x_2 . The log is an example of a link function. Note that to be identifiable the model requires constraints on the smooth functions. By default these are imposed automatically and require that the function sums to zero over the observed covariate values (the presence of a metric by variable is the only case which usually suppresses this).

If absolutely any smooth functions were allowed in model fitting then maximum likelihood estimation of such models would invariably result in complex overfitting estimates of f_1 and f_2 . For this reason the models are usually fit by penalized likelihood maximization, in which the model (negative log) likelihood is modified by the addition of a penalty for each smooth function, penalizing its ‘wiggleness’. To control the tradeoff between penalizing wiggleness and penalizing badness of fit each penalty is multiplied by an associated smoothing parameter: how to estimate these parameters, and how to practically represent the smooth functions are the main statistical questions introduced by moving from GLMs to GAMs.

The `mgcv` implementation of `gam` represents the smooth functions using penalized regression splines, and by default uses basis functions for these splines that are designed to be optimal, given the number basis functions used. The smooth terms can be functions of any number of covariates and the user has some control over how smoothness of the functions is measured.

`gam` in `mgcv` solves the smoothing parameter estimation problem by using the Generalized Cross Validation (GCV) criterion

$$nD/(n - DoF)^2$$

or an Un-Biased Risk Estimator (UBRE) criterion

$$D/n + 2sDoF/n - s$$

where D is the deviance, n the number of data, s the scale parameter and DoF the effective degrees of freedom of the model. Notice that UBRE is effectively just AIC rescaled, but is only used when s is known.

Alternatives are GACV, or a Laplace approximation to REML. There is some evidence that the latter may actually be the most effective choice. The main computational challenge solved by the `mgcv` package is to optimize the smoothness selection criteria efficiently and reliably. Various alternative numerical methods are provided which can be set by argument `optimizer`.

Broadly `gam` works by first constructing basis functions and one or more quadratic penalty coefficient matrices for each smooth term in the model formula, obtaining a model matrix for the strictly parametric part of the model formula, and combining these to obtain a complete model matrix (/design matrix) and a set of penalty matrices for the smooth terms. The linear identifiability constraints are also obtained at this point. The model is fit using `gam.fit`, `gam.fit3` or variants, which are modifications of `glm.fit`. The GAM penalized likelihood maximization problem is solved by Penalized Iteratively Reweighted Least Squares (P-IRLS) (see e.g. Wood 2000). Smoothing parameter selection is integrated in one of two ways. (i) ‘Performance iteration’ uses the fact that at each P-IRLS iteration a penalized weighted least squares problem is solved, and the smoothing parameters of that problem can be estimated by GCV or UBRE. Eventually, in most cases, both model parameter estimates and smoothing parameter estimates converge. (ii) Alternatively the P-IRLS scheme is iterated to convergence for each trial set of smoothing parameters, and GCV, UBRE or

REML scores are only evaluated on convergence - optimization is then ‘outer’ to the P-IRLS loop: in this case the P-IRLS iteration has to be differentiated, to facilitate optimization, and `gam.fit3` or one of its variants is used in place of `gam.fit`. The default is the second method, outer iteration.

Several alternative basis-penalty types are built in for representing model smooths, but alternatives can easily be added (see `smooth.terms` for an overview and `smooth.construct` for how to add smooth classes). The choice of the basis dimension (k in the `s`, `te`, `ti` and `t2` terms) is something that should be considered carefully (the exact value is not critical, but it is important not to make it restrictively small, nor very large and computationally costly). The basis should be chosen to be larger than is believed to be necessary to approximate the smooth function concerned. The effective degrees of freedom for the smooth will then be controlled by the smoothing penalty on the term, and (usually) selected automatically (with an upper limit set by $k-1$ or occasionally k). Of course the k should not be made too large, or computation will be slow (or in extreme cases there will be more coefficients to estimate than there are data).

Note that `gam` assumes a very inclusive definition of what counts as a GAM: basically any penalized GLM can be used: to this end `gam` allows the non smooth model components to be penalized via argument `paraPen` and allows the linear predictor to depend on general linear functionals of smooths, via the summation convention mechanism described in `linear.functional.terms`. `link{family.mgcv}` details what is available beyond GLMs and the exponential family.

Details of the default underlying fitting methods are given in Wood (2011 and 2004). Some alternative methods are discussed in Wood (2000 and 2006).

`gam()` is not a clone of Trevor Hastie’s original (as supplied in S-PLUS or package `gam`). The major differences are (i) that by default estimation of the degree of smoothness of model terms is part of model fitting, (ii) a Bayesian approach to variance estimation is employed that makes for easier confidence interval calculation (with good coverage probabilities), (iii) that the model can depend on any (bounded) linear functional of smooth terms, (iv) the parametric part of the model can be penalized, (v) simple random effects can be incorporated, and (vi) the facilities for incorporating smooths of more than one variable are different: specifically there are no `lo` smooths, but instead (a) `s` terms can have more than one argument, implying an isotropic smooth and (b) `te`, `ti` or `t2` smooths are provided as an effective means for modelling smooth interactions of any number of variables via scale invariant tensor product smooths. Splines on the sphere, Duchon splines and Gaussian Markov Random Fields are also available. (vii) Models beyond the exponential family are available. See `gam` from package `gam`, for GAMs via the original Hastie and Tibshirani approach.

Value

If `fit=FALSE` the function returns a list `G` of items needed to fit a GAM, but doesn’t actually fit it.

Otherwise the function returns an object of class “`gam`” as described in `gamObject`.

WARNINGS

The default basis dimensions used for smooth terms are essentially arbitrary, and it should be checked that they are not too small. See `choose.k` and `gam.check`.

You must have more unique combinations of covariates than the model has total parameters. (Total parameters is sum of basis dimensions plus sum of non-spline terms less the number of spline terms).

Automatic smoothing parameter selection is not likely to work well when fitting models to very few response data.

For data with many zeroes clustered together in the covariate space it is quite easy to set up GAMs which suffer from identifiability problems, particularly when using Poisson or binomial families. The problem is that with e.g. log or logit links, mean value zero corresponds to an infinite range on the linear predictor scale.

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Front end design inspired by the S function of the same name based on the work of Hastie and Tibshirani (1990). Underlying methods owe much to the work of Wahba (e.g. 1990) and Gu (e.g. 2002).

References

Key References on this implementation:

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

Wood, S.N. (2004) Stable and efficient multiple smoothing parameter estimation for generalized additive models. *J. Amer. Statist. Ass.* 99:673-686. [Default method for additive case by GCV (but no longer for generalized)]

Wood, S.N. (2003) Thin plate regression splines. *J.R.Statist.Soc.B* 65(1):95-114

Wood, S.N. (2006a) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

Wood S.N. (2006b) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.

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Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. *Scandinavian Journal of Statistics*, 39(1), 53-74.

Key Reference on GAMs and related models:

Hastie (1993) in Chambers and Hastie (1993) *Statistical Models in S*. Chapman and Hall.

Hastie and Tibshirani (1990) *Generalized Additive Models*. Chapman and Hall.

Wahba (1990) *Spline Models of Observational Data*. SIAM

Wood, S.N. (2000) Modelling and Smoothing Parameter Estimation with Multiple Quadratic Penalties. *J.R.Statist.Soc.B* 62(2):413-428 [The original mgcv paper, but no longer the default methods.]

Background References:

Green and Silverman (1994) *Nonparametric Regression and Generalized Linear Models*. Chapman and Hall.

Gu and Wahba (1991) Minimizing GCV/GML scores with multiple smoothing parameters via the Newton method. *SIAM J. Sci. Statist. Comput.* 12:383-398

Gu (2002) *Smoothing Spline ANOVA Models*, Springer.

McCullagh and Nelder (1989) *Generalized Linear Models* 2nd ed. Chapman & Hall.

O'Sullivan, Yandall and Raynor (1986) Automatic smoothing of regression functions in generalized linear models. *J. Am. Statist.Ass.* 81:96-103

Wood (2001) mgcv:GAMs and Generalized Ridge Regression for R. *R News* 1(2):20-25

Wood and Augustin (2002) GAMs with integrated model selection using penalized regression splines and applications to environmental modelling. *Ecological Modelling* 157:157-177

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[mgcv-package](#), [gamObject](#), [gam.models](#), [smooth.terms](#), [linear.functional.terms](#), [s](#), [te](#) [predict.gam](#), [plot.gam](#), [summary.gam](#), [gam.side](#), [gam.selection](#), [gam.control](#) [gam.check](#), [linear.functional.terms](#) [negbin](#), [magic](#), [vis.gam](#)

Examples

```
## see also examples in ?gam.models (e.g. 'by' variables,
## random effects and tricks for large binary datasets)

library(mgcv)
set.seed(2) ## simulate some data..
dat <- gamSim(1,n=400,dist="normal",scale=2)
b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat)
summary(b)
plot(b,pages=1,residuals=TRUE) ## show partial residuals
plot(b,pages=1,seWithMean=TRUE) ## `with intercept' CIs
## run some basic model checks, including checking
## smoothing basis dimensions...
gam.check(b)

## same fit in two parts ....
G <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),fit=FALSE,data=dat)
b <- gam(G=G)
print(b)

## 2 part fit enabling manipulation of smoothing parameters...
G <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),fit=FALSE,data=dat,sp=b$sp)
G$sp0 <- log(b$sp*10) ## provide log of required sp vec
gam(G=G) ## it's smoother

## change the smoothness selection method to REML
b0 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="REML")
## use alternative plotting scheme, and way intervals include
## smoothing parameter uncertainty...
plot(b0,pages=1,scheme=1,unconditional=TRUE)

## Would a smooth interaction of x0 and x1 be better?
## Use tensor product smooth of x0 and x1, basis
## dimension 49 (see ?te for details, also ?t2).
bt <- gam(y~te(x0,x1,k=7)+s(x2)+s(x3),data=dat,
          method="REML")
plot(bt,pages=1)
```

```

plot(bt,pages=1,scheme=2) ## alternative visualization
AIC(b0,bt) ## interaction worse than additive

## Alternative: test for interaction with a smooth ANOVA
## decomposition (this time between x2 and x1)
bt <- gam(y~s(x0)+s(x1)+s(x2)+s(x3)+ti(x1,x2,k=6),
          data=dat,method="REML")
summary(bt)

## If it is believed that x0 and x1 are naturally on
## the same scale, and should be treated isotropically
## then could try...
bs <- gam(y~s(x0,x1,k=40)+s(x2)+s(x3),data=dat,
          method="REML")
plot(bs,pages=1)
AIC(b0,bt,bs) ## additive still better.

## Now do automatic terms selection as well
b1 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,
          method="REML",select=TRUE)
plot(b1,pages=1)

## set the smoothing parameter for the first term, estimate rest ...
bp <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),sp=c(0.01,-1,-1,-1),data=dat)
plot(bp,pages=1,scheme=1)
## alternatively...
bp <- gam(y~s(x0,sp=.01)+s(x1)+s(x2)+s(x3),data=dat)

# set lower bounds on smoothing parameters ....
bp<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),
        min.sp=c(0.001,0.01,0,10),data=dat)
print(b);print(bp)

# same with REML
bp<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),
        min.sp=c(0.1,0.1,0,10),data=dat,method="REML")
print(b0);print(bp)

## now a GAM with 3df regression spline term & 2 penalized terms

b0 <- gam(y~s(x0,k=4,fx=TRUE,bs="tp")+s(x1,k=12)+s(x2,k=15),data=dat)
plot(b0,pages=1)

## now simulate poisson data...
dat <- gamSim(1,n=2000,dist="poisson",scale=.1)

## use "cr" basis to save time, with 2000 data...
b2<-gam(y~s(x0,bs="cr")+s(x1,bs="cr")+s(x2,bs="cr")+
        s(x3,bs="cr"),family=poisson,data=dat,method="REML")
plot(b2,pages=1)

```



```

## drop x3, but initialize sp's from previous fit, to
## save more time...

b2a<-gam(y~s(x0,bs="cr")+s(x1,bs="cr")+s(x2,bs="cr"),
        family=poisson,data=dat,method="REML",
        in.out=list(sp=b2$sp[1:3],scale=1))
par(mfrow=c(2,2))
plot(b2a)

par(mfrow=c(1,1))
## similar example using performance iteration
dat <- gamSim(1,n=400,dist="poisson",scale=.25)

b3<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=poisson,
        data=dat,optimizer="perf")
plot(b3,pages=1)

## repeat using GACV as in Wood 2008...

b4<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=poisson,
        data=dat,method="GACV.Cp",scale=-1)
plot(b4,pages=1)

## repeat using REML as in Wood 2011...

b5<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=poisson,
        data=dat,method="REML")
plot(b5,pages=1)

## a binary example (see ?gam.models for large dataset version)...

dat <- gamSim(1,n=400,dist="binary",scale=.33)

lr.fit <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=binomial,
            data=dat,method="REML")

## plot model components with truth overlaid in red
op <- par(mfrow=c(2,2))
fn <- c("f0","f1","f2","f3");xn <- c("x0","x1","x2","x3")
for (k in 1:4) {
  plot(lr.fit,residuals=TRUE,select=k)
  ff <- dat[[fn[k]]];xx <- dat[[xn[k]]]
  ind <- sort.int(xx,index.return=TRUE)$ix
  lines(xx[ind],(ff-mean(ff))[ind]*.33,col=2)
}
par(op)
anova(lr.fit)
lr.fit1 <- gam(y~s(x0)+s(x1)+s(x2),family=binomial,
            data=dat,method="REML")
lr.fit2 <- gam(y~s(x1)+s(x2),family=binomial,
            data=dat,method="REML")

```

```

AIC(lr.fit,lr.fit1,lr.fit2)

## For a Gamma example, see ?summary.gam...

## For inverse Gaussian, see ?rig

## now 2D smoothing...

eg <- gamSim(2,n=500,scale=.1)
attach(eg)

op <- par(mfrow=c(2,2),mar=c(4,4,1,1))

contour(truth$x,truth$z,truth$f) ## contour truth
b4 <- gam(y~s(x,z),data=data) ## fit model
fit1 <- matrix(predict.gam(b4,pr,se=FALSE),40,40)
contour(truth$x,truth$z,fit1) ## contour fit
persp(truth$x,truth$z,truth$f) ## persp truth
vis.gam(b4) ## persp fit
detach(eg)
par(op)

## Not run:
#####
## largish dataset example with user defined knots
#####

par(mfrow=c(2,2))
n <- 5000
eg <- gamSim(2,n=n,scale=.5)
attach(eg)

ind<-sample(1:n,200,replace=FALSE)
b5<-gam(y~s(x,z,k=40),data=data,
        knots=list(x=data$x[ind],z=data$z[ind]))
## various visualizations
vis.gam(b5,theta=30,phi=30)
plot(b5)
plot(b5,scheme=1,theta=50,phi=20)
plot(b5,scheme=2)

par(mfrow=c(1,1))
## and a pure "knot based" spline of the same data
b6<-gam(y~s(x,z,k=64),data=data,knots=list(x= rep((1:8-0.5)/8,8),
        z=rep((1:8-0.5)/8,rep(8,8))))
vis.gam(b6,color="heat",theta=30,phi=30)

## varying the default large dataset behaviour via `xt`
b7 <- gam(y~s(x,z,k=40,xt=list(max.knots=500,seed=2)),data=data)
vis.gam(b7,theta=30,phi=30)
detach(eg)

## End(Not run)

```

gam.check

*Some diagnostics for a fitted gam model***Description**

Takes a fitted gam object produced by `gam()` and produces some diagnostic information about the fitting procedure and results. The default is to produce 4 residual plots, some information about the convergence of the smoothness selection optimization, and to run diagnostic tests of whether the basis dimension choices are adequate.

Usage

```
gam.check(b, old.style=FALSE,
          type=c("deviance", "pearson", "response"),
          k.sample=5000, k.rep=200,
          rep=0, level=.9, rl.col=2, rep.col="gray80", ...)
```

Arguments

<code>b</code>	a fitted gam object as produced by <code>gam()</code> .
<code>old.style</code>	If you want old fashioned plots, exactly as in Wood, 2006, set to TRUE.
<code>type</code>	type of residuals, see <code>residuals.gam</code> , used in all plots.
<code>k.sample</code>	Above this k testing uses a random sub-sample of data.
<code>k.rep</code>	how many re-shuffles to do to get p-value for k testing.
<code>rep, level, rl.col, rep.col</code>	arguments passed to <code>qq.gam()</code> when <code>old.style</code> is false, see there.
<code>...</code>	extra graphics parameters to pass to plotting functions.

Details

Checking a fitted gam is like checking a fitted glm, with two main differences. Firstly, the basis dimensions used for smooth terms need to be checked, to ensure that they are not so small that they force oversmoothing: the defaults are arbitrary. `choose.k` provides more detail, but the diagnostic tests described below and reported by this function may also help. Secondly, fitting may not always be as robust to violation of the distributional assumptions as would be the case for a regular GLM, so slightly more care may be needed here. In particular, the theory of quasi-likelihood implies that if the mean variance relationship is OK for a GLM, then other departures from the assumed distribution are not problematic: GAMs can sometimes be more sensitive. For example, un-modelled overdispersion will typically lead to overfit, as the smoothness selection criterion tries to reduce the scale parameter to the one specified. Similarly, it is not clear how sensitive REML and ML smoothness selection will be to deviations from the assumed response distribution. For these reasons this routine uses an enhanced residual QQ plot.

This function plots 4 standard diagnostic plots, some smoothing parameter estimation convergence information and the results of tests which may indicate if the smoothing basis dimension for a term is too low.

Usually the 4 plots are various residual plots. For the default optimization methods the convergence information is summarized in a readable way, but for other optimization methods, whatever is returned by way of convergence diagnostics is simply printed.

The test of whether the basis dimension for a smooth is adequate is based on computing an estimate of the residual variance based on differencing residuals that are near neighbours according to the (numeric) covariates of the smooth. This estimate divided by the residual variance is the k -index reported. The further below 1 this is, the more likely it is that there is missed pattern left in the residuals. The p -value is computed by simulation: the residuals are randomly re-shuffled k .rep times to obtain the null distribution of the differencing variance estimator, if there is no pattern in the residuals. For models fitted to more than k .sample data, the tests are based of k .sample randomly sampled data. Low p -values may indicate that the basis dimension, k , has been set too low, especially if the reported edf is close to $k \setminus$, the maximum possible EDF for the term. Note the disconcerting fact that if the test statistic itself is based on random resampling and the null is true, then the associated p -values will of course vary widely from one replicate to the next. Currently smooths of factor variables are not supported and will give an NA p -value.

Doubling a suspect k and re-fitting is sensible: if the reported edf increases substantially then you may have been missing something in the first fit. Of course p -values can be low for reasons other than a too low k . See [choose.k](#) for fuller discussion.

The QQ plot produced is usually created by a call to [qq.gam](#), and plots deviance residuals against approximate theoretical quantiles of the deviance residual distribution, according to the fitted model. If this looks odd then investigate further using [qq.gam](#). Note that residuals for models fitted to binary data contain very little information useful for model checking (it is necessary to find some way of aggregating them first), so the QQ plot is unlikely to be useful in this case.

Value

A vector of reference quantiles for the residual distribution, if these can be computed.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

N.H. Augustin, E-A Sauleaub, S.N. Wood (2012) On quantile quantile plots for generalized linear models. Computational Statistics & Data Analysis. 56(8), 2404-3409.

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[choose.k](#), [gam](#), [magic](#)

Examples

```
library(mgcv)
set.seed(0)
```

```

dat <- gamSim(1,n=200)
b<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat)
plot(b,pages=1)
gam.check(b,pch=19,cex=.3)

```

gam.control

*Setting GAM fitting defaults***Description**

This is an internal function of package `mgcv` which allows control of the numerical options for fitting a GAM. Typically users will want to modify the defaults if model fitting fails to converge, or if the warnings are generated which suggest a loss of numerical stability during fitting. To change the default choice of fitting method, see `gam` arguments `method` and `optimizer`.

Usage

```

gam.control(nthreads=1,irls.reg=0.0,epsilon = 1e-07, maxit = 200,
           mgcv.tol=1e-7,mgcv.half=15, trace = FALSE,
           rank.tol=.Machine$double.eps^0.5,
           nlm=list(),optim=list(),newton=list(),
           outerPIsteps=0,idLinksBases=TRUE,scalePenalty=TRUE,
           keepData=FALSE,scale.est="fletcher",edge.correct=FALSE)

```

Arguments

<code>nthreads</code>	Some parts of some smoothing parameter selection methods (e.g. REML) can use some parallelization in the C code if your R installation supports openMP, and <code>nthreads</code> is set to more than 1. Note that it is usually better to use the number of physical cores here, rather than the number of hyper-threading cores.
<code>irls.reg</code>	For most models this should be 0. The iteratively re-weighted least squares method by which GAMs are fitted can fail to converge in some circumstances. For example, data with many zeroes can cause problems in a model with a log link, because a mean of zero corresponds to an infinite range of linear predictor values. Such convergence problems are caused by a fundamental lack of identifiability, but do not show up as lack of identifiability in the penalized linear model problems that have to be solved at each stage of iteration. In such circumstances it is possible to apply a ridge regression penalty to the model to impose identifiability, and <code>irls.reg</code> is the size of the penalty.
<code>epsilon</code>	This is used for judging conversion of the GLM IRLS loop in <code>gam.fit</code> or <code>gam.fit3</code> .
<code>maxit</code>	Maximum number of IRLS iterations to perform.
<code>mgcv.tol</code>	The convergence tolerance parameter to use in GCV/UBRE optimization.
<code>mgcv.half</code>	If a step of the GCV/UBRE optimization method leads to a worse GCV/UBRE score, then the step length is halved. This is the number of halvings to try before giving up.

<code>trace</code>	Set this to TRUE to turn on diagnostic output.
<code>rank.tol</code>	The tolerance used to estimate the rank of the fitting problem.
<code>n1m</code>	list of control parameters to pass to <code>n1m</code> if this is used for outer estimation of smoothing parameters (not default). See details.
<code>optim</code>	list of control parameters to pass to <code>optim</code> if this is used for outer estimation of smoothing parameters (not default). See details.
<code>newton</code>	list of control parameters to pass to default Newton optimizer used for outer estimation of log smoothing parameters. See details.
<code>outerPIsteps</code>	The number of performance iteration steps used to initialize outer iteration.
<code>idLinksBases</code>	If smooth terms have their smoothing parameters linked via the <code>id</code> mechanism (see <code>s</code>), should they also have the same bases. Set this to FALSE only if you are sure you know what you are doing (you should almost surely set <code>scalePenalty</code> to FALSE as well in this case).
<code>scalePenalty</code>	<code>gamm</code> is somewhat sensitive to the absolute scaling of the penalty matrices of a smooth relative to its model matrix. This option rescales the penalty matrices to accomodate this problem. Probably should be set to FALSE if you are linking smoothing parameters but have set <code>idLinkBases</code> to FALSE.
<code>keepData</code>	Should a copy of the original data argument be kept in the gam object? Strict compatibility with class <code>glm</code> would keep it, but it wastes space to do so.
<code>scale.est</code>	How to estimate the scale parameter for exponential family models estimated by outer iteration. See <code>gam.scale</code> .
<code>edge.correct</code>	With RE/ML smoothing parameter selection in gam using the default Newton RE/ML optimizer, it is possible to improve inference at the ‘completely smooth’ edge of the smoothing parameter space, by decreasing smoothing parameters until there is a small increase in the negative RE/ML (e.g. 0.02). Set to TRUE or to a number representing the target increase to use. Only changes the corrected smoothing parameter matrix, V_c .

Details

Outer iteration using `newton` is controlled by the list `newton` with the following elements: `conv.tol` (default $1e-6$) is the relative convergence tolerance; `maxNstep` is the maximum length allowed for an element of the Newton search direction (default 5); `maxSstep` is the maximum length allowed for an element of the steepest descent direction (only used if Newton fails - default 2); `maxHalf` is the maximum number of step halvings to permit before giving up (default 30).

If outer iteration using `n1m` is used for fitting, then the control list `n1m` stores control arguments for calls to routine `n1m`. The list has the following named elements: (i) `ndigit` is the number of significant digits in the GCV/UBRE score - by default this is worked out from `epsilon`; (ii) `gradtol` is the tolerance used to judge convergence of the gradient of the GCV/UBRE score to zero - by default set to $10 * \epsilon$; (iii) `stepmax` is the maximum allowable log smoothing parameter step - defaults to 2; (iv) `steptol` is the minimum allowable step length - defaults to $1e-4$; (v) `iterlim` is the maximum number of optimization steps allowed - defaults to 200; (vi) `check.analyticals` indicates whether the built in exact derivative calculations should be checked numerically - defaults to FALSE. Any of these which are not supplied and named in the list are set to their default values.

Outer iteration using `optim` is controlled using list `optim`, which currently has one element: `factr` which takes default value $1e7$.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

Wood, S.N. (2004) Stable and efficient multiple smoothing parameter estimation for generalized additive models. *J. Amer. Statist. Ass.* 99:673-686.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam](#), [gam.fit](#), [glm.control](#)

gam.convergence

GAM convergence and performance issues

Description

When fitting GAMs there is a tradeoff between speed of fitting and probability of fit convergence. The default fitting options, specified by `gam` arguments `method` and `optimizer`, opt for certainty of convergence over speed of fit. In the Generalized Additive Model case it means using ‘outer’ iteration in preference to ‘performance iteration’: see [gam.outer](#) for details.

It is possible for the default ‘outer’ iteration to fail when finding initial smoothing parameters using a few steps of performance iteration (if you get a convergence failure message from `magic` when outer iterating, then this is what has happened): lower `outerPIsteps` in [gam.control](#) to fix this.

There are three things that you can try to speed up GAM fitting. (i) if you have large numbers of smoothing parameters in the generalized case, then try the “bfgs” method option in `gam` argument `optimizer`: this can be faster than the default. (ii) Change the `optimizer` argument to `gam` so that ‘performance iteration’ is used in place of the default outer iteration. Usually performance iteration converges well and it can sometimes be quicker than the default outer iteration. (iii) For large datasets it may be worth changing the smoothing basis to use `bs="cr"` (see [s](#) for details) for 1-d smooths, and to use `te` smooths in place of `s` smooths for smooths of more than one variable. This is because the default thin plate regression spline basis “tp” is costly to set up for large datasets (much over 1000 data, say). (iv) consider using [bam](#).

If the GAM estimation process fails to converge when using performance iteration, then switch to outer iteration via the `optimizer` argument of `gam`. If it still fails, try increasing the number of IRLS iterations (see [gam.control](#)) or perhaps experiment with the convergence tolerance.

If you still have problems, it’s worth noting that a GAM is just a (penalized) GLM and the IRLS scheme used to estimate GLMs is not guaranteed to converge. Hence non convergence of a GAM may relate to a lack of stability in the basic IRLS scheme. Therefore it is worth trying to establish whether the IRLS iterations are capable of converging. To do this fit the problematic GAM with all smooth terms specified with `fx=TRUE` so that the smoothing parameters are all fixed at zero. If this ‘largest’ model can converge then, then the maintainer would quite like to know about your

problem! If it doesn't converge, then its likely that your model is just too flexible for the IRLS process itself. Having tried increasing `maxit` in `gam.control`, there are several other possibilities for stabilizing the iteration. It is possible to try (i) setting lower bounds on the smoothing parameters using the `min.sp` argument of `gam`: this may or may not change the model being fitted; (ii) reducing the flexibility of the model by reducing the basis dimensions `k` in the specification of `s` and `te` model terms: this obviously changes the model being fitted somewhat; (iii) introduce a small regularization term into the fitting via the `irls.reg` argument of `gam.control`: this option obviously changes the nature of the fit somewhat, since parameter estimates are pulled towards zero by doing this.

Usually, a major contributor to fitting difficulties is that the model is a very poor description of the data.

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gam.fit

GAM P-IRLS estimation with GCV/UBRE smoothness estimation

Description

This is an internal function of package `mgcv`. It is a modification of the function `glm.fit`, designed to be called from `gam` when performance iteration is selected (not the default). The major modification is that rather than solving a weighted least squares problem at each IRLS step, a weighted, penalized least squares problem is solved at each IRLS step with smoothing parameters associated with each penalty chosen by GCV or UBRE, using routine `magic`. For further information on usage see code for `gam`. Some regularization of the IRLS weights is also permitted as a way of addressing identifiability related problems (see `gam.control`). Negative binomial parameter estimation is supported.

The basic idea of estimating smoothing parameters at each step of the P-IRLS is due to Gu (1992), and is termed 'performance iteration' or 'performance oriented iteration'.

Usage

```
gam.fit(G, start = NULL, etastart = NULL,
        mustart = NULL, family = gaussian(),
        control = gam.control(), gamma=1,
        fixedSteps=(control$maxit+1),...)
```

Arguments

<code>G</code>	An object of the type returned by <code>gam</code> when <code>fit=FALSE</code> .
<code>start</code>	Initial values for the model coefficients.
<code>etastart</code>	Initial values for the linear predictor.

mustart	Initial values for the expected response.
family	The family object, specifying the distribution and link to use.
control	Control option list as returned by gam.control .
gamma	Parameter which can be increased to up the cost of each effective degree of freedom in the GCV or AIC/UBRE objective.
fixedSteps	How many steps to take: useful when only using this routine to get rough starting values for other methods.
...	Other arguments: ignored.

Value

A list of fit information.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

- Gu (1992) Cross-validating non-Gaussian data. *J. Comput. Graph. Statist.* 1:169-179
- Gu and Wahba (1991) Minimizing GCV/GML scores with multiple smoothing parameters via the Newton method. *SIAM J. Sci. Statist. Comput.* 12:383-398
- Wood, S.N. (2000) Modelling and Smoothing Parameter Estimation with Multiple Quadratic Penalties. *J.R.Statist.Soc.B* 62(2):413-428
- Wood, S.N. (2004) Stable and efficient multiple smoothing parameter estimation for generalized additive models. *J. Amer. Statist. Ass.* 99:637-686

See Also

[gam.fit3](#), [gam](#), [magic](#)

gam.fit3	<i>P-IRLS GAM estimation with GCV & UBRE/AIC or RE/ML derivative calculation</i>
----------	--

Description

Estimation of GAM smoothing parameters is most stable if optimization of the UBRE/AIC, GCV, GACV, REML or ML score is outer to the penalized iteratively re-weighted least squares scheme used to estimate the model given smoothing parameters.

This routine estimates a GAM (any quadratically penalized GLM) given log smoothing parameters, and evaluates derivatives of the smoothness selection scores of the model with respect to the log smoothing parameters. Calculation of exact derivatives is generally faster than approximating them by finite differencing, as well as generally improving the reliability of GCV/UBRE/AIC/REML score minimization.

The approach is to run the P-IRLS to convergence, and only then to iterate for first and second derivatives.

Not normally called directly, but rather service routines for [gam](#).

Usage

```
gam.fit3(x, y, sp, Eb, UrS=list(),
        weights = rep(1, nobs), start = NULL, etastart = NULL,
        mustart = NULL, offset = rep(0, nobs), U1 = diag(ncol(x)),
        Mp = -1, family = gaussian(), control = gam.control(),
        intercept = TRUE, deriv=2, gamma=1, scale=1,
        printWarn=TRUE, scoreType="REML", null.coef=rep(0, ncol(x)),
        pearson.extra=0, dev.extra=0, n.true=-1, S1=NULL, ...)
```

Arguments

x	The model matrix for the GAM (or any penalized GLM).
y	The response variable.
sp	The log smoothing parameters.
Eb	A balanced version of the total penalty matrix: used for numerical rank determination.
UrS	List of square root penalties premultiplied by transpose of orthogonal basis for the total penalty.
weights	prior weights for fitting.
start	optional starting parameter guesses.
etastart	optional starting values for the linear predictor.
mustart	optional starting values for the mean.
offset	the model offset
U1	An orthogonal basis for the range space of the penalty — required for ML smoothness estimation only.
Mp	The dimension of the total penalty null space — required for ML smoothness estimation only.
family	the family - actually this routine would never be called with <code>gaussian()</code>
control	control list as returned from glm.control
intercept	does the model have an intercept, TRUE or FALSE
deriv	Should derivatives of the GCV and UBRE/AIC scores be calculated? 0, 1 or 2, indicating the maximum order of differentiation to apply.
gamma	The weight given to each degree of freedom in the GCV and UBRE scores can be varied (usually increased) using this parameter.
scale	The scale parameter - needed for the UBRE/AIC score.
printWarn	Set to FALSE to suppress some warnings. Useful in order to ensure that some warnings are only printed if they apply to the final fitted model, rather than an intermediate used in optimization.

scoreType	specifies smoothing parameter selection criterion to use.
null.coef	coefficients for a model which gives some sort of upper bound on deviance. This allows immediate divergence problems to be controlled.
pearson.extra	Extra component to add to numerator of pearson statistic in P-REML/P-ML smoothness selection criteria.
dev.extra	Extra component to add to deviance for REML/ML type smoothness selection criteria.
n.true	Number of data to assume in smoothness selection criteria. <=0 indicates that it should be the number of rows of X.
S1	A smooth list suitable for passing to gam.fit5.
...	Other arguments: ignored.

Details

This routine is basically `glm.fit` with some modifications to allow (i) for quadratic penalties on the log likelihood; (ii) derivatives of the model coefficients with respect to log smoothing parameters to be obtained by use of the implicit function theorem and (iii) derivatives of the GAM GCV, UBRE/AIC, REML or ML scores to be evaluated at convergence.

In addition the routines apply step halving to any step that increases the penalized deviance substantially.

The most costly parts of the calculations are performed by calls to compiled C code (which in turn calls LAPACK routines) in place of the compiled code that would usually perform least squares estimation on the working model in the IRLS iteration.

Estimation of smoothing parameters by optimizing GCV scores obtained at convergence of the P-IRLS iteration was proposed by O'Sullivan et al. (1986), and is here termed 'outer' iteration.

Note that use of non-standard families with this routine requires modification of the families as described in [fix.family.link](#).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

The routine has been modified from `glm.fit` in R 2.0.1, written by the R core (see `glm.fit` for further credits).

References

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

O'Sullivan, Yandall & Raynor (1986) Automatic smoothing of regression functions in generalized linear models. *J. Amer. Statist. Assoc.* 81:96-103.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam.fit](#), [gam](#), [magic](#)

Description

This page is intended to provide some more information on how to specify GAMs. A GAM is a GLM in which the linear predictor depends, in part, on a sum of smooth functions of predictors and (possibly) linear functionals of smooth functions of (possibly dummy) predictors.

Specifically let y_i denote an independent random variable with mean μ_i and an exponential family distribution, or failing that a known mean variance relationship suitable for use of quasi-likelihood methods. Then the the linear predictor of a GAM has a structure something like

$$g(\mu_i) = \mathbf{X}_i\beta + f_1(x_{1i}, x_{2i}) + f_2(x_{3i}) + L_i f_3(x_4) + \dots$$

where g is a known smooth monotonic ‘link’ function, $\mathbf{X}_i\beta$ is the parametric part of the linear predictor, the x_j are predictor variables, the f_j are smooth functions and L_i is some linear functional of f_3 . There may of course be multiple linear functional terms, or none.

The key idea here is that the dependence of the response on the predictors can be represented as a parametric sub-model plus the sum of some (functionals of) smooth functions of one or more of the predictor variables. Thus the model is quite flexible relative to strictly parametric linear or generalized linear models, but still has much more structure than the completely general model that says that the response is just some smooth function of all the covariates.

Note one important point. In order for the model to be identifiable the smooth functions usually have to be constrained to have zero mean (usually taken over the set of covariate values). The constraint is needed if the term involving the smooth includes a constant function in its span. `gam` always applies such constraints unless there is a `by` variable present, in which case an assessment is made of whether the constraint is needed or not (see below).

The following sections discuss specifying model structures for `gam`. Specification of the distribution and link function is done using the `family` argument to `gam` and works in the same way as for `glm`. This page therefore concentrates on the model formula for `gam`.

Models with simple smooth terms

Consider the example model.

$$g(\mu_i) = \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} + f_1(x_{3i}) + f_2(x_{4i}, x_{5i})$$

where the response variables y_i has expectation μ_i and g is a link function.

The `gam` formula for this would be

$$y \sim x1 + x2 + s(x3) + s(x4, x5).$$

This would use the default basis for the smooths (a thin plate regression spline basis for each), with automatic selection of the effective degrees of freedom for both smooths. The dimension of the smoothing basis is given a default value as well (the dimension of the basis sets an upper limit on the maximum possible degrees of freedom for the basis - the limit is typically one less than basis dimension). Full details of how to control smooths are given in `s` and `te`, and further discussion of

basis dimension choice can be found in [choose.k](#). For the moment suppose that we would like to change the basis of the first smooth to a cubic regression spline basis with a dimension of 20, while fixing the second term at 25 degrees of freedom. The appropriate formula would be:

```
y ~ x1 + x2 + s(x3,bs="cr",k=20) + s(x4,x5,k=26,fx=TRUE).
```

The above assumes that x_4 and x_5 are naturally on similar scales (e.g. they might be co-ordinates), so that isotropic smoothing is appropriate. If this assumption is false then tensor product smoothing might be better (see [te](#)).

```
y ~ x1 + x2 + s(x3) + te(x4,x5)
```

would generate a tensor product smooth of x_4 and x_5 . By default this smooth would have basis dimension 25 and use cubic regression spline marginals. Varying the defaults is easy. For example

```
y ~ x1 + x2 + s(x3) + te(x4,x5,bs=c("cr","ps"),k=c(6,7))
```

specifies that the tensor product should use a rank 6 cubic regression spline marginal and a rank 7 P-spline marginal to create a smooth with basis dimension 42.

Nested terms/functional ANOVA

Sometimes it is interesting to specify smooth models with a main effects + interaction structure such as

$$E(y_i) = f_1(x_i) + f_2(z_i) + f_3(x_i, z_i)$$

or

$$E(y_i) = f_1(x_i) + f_2(z_i) + f_3(v_i) + f_4(x_i, z_i) + f_5(z_i, v_i) + f_6(z_i, v_i) + f_7(x_i, z_i, v_i)$$

for example. Such models should be set up using [ti](#) terms in the model formula. For example:

```
y ~ ti(x) + ti(z) + ti(x,z), or
```

```
y ~ ti(x) + ti(z) + ti(v) + ti(x,z) + ti(x,v) + ti(z,v)+ti(x,z,v).
```

The [ti](#) terms produce interactions with the component main effects excluded appropriately. (There is in fact no need to use [ti](#) terms for the main effects here, [s](#) terms could also be used.)

[gam](#) allows nesting (or ‘overlap’) of [te](#) and [s](#) smooths, and automatically generates side conditions to make such models identifiable, but the resulting models are much less stable and interpretable than those constructed using [ti](#) terms.

‘by’ variables

by variables are the means for constructing ‘varying-coefficient models’ (geographic regression models) and for letting smooths ‘interact’ with factors or parametric terms. They are also the key to specifying general linear functionals of smooths.

The [s](#) and [te](#) terms used to specify smooths accept an argument `by`, which is a numeric or factor variable of the same dimension as the covariates of the smooth. If a `by` variable is numeric, then its i^{th} element multiplies the i^{th} row of the model matrix corresponding to the smooth term concerned.

Factor smooth interactions (see also [factor.smooth.interaction](#)). If a `by` variable is a [factor](#) then it generates an indicator vector for each level of the factor, unless it is an [ordered](#) factor. In the non-ordered case, the model matrix for the smooth term is then replicated for each factor level, and each copy has its rows multiplied by the corresponding rows of its indicator variable. The smoothness penalties are also duplicated for each factor level. In short a different smooth is generated for each factor level (the `id` argument to [s](#) and [te](#) can be used to force all such smooths to have the same smoothing parameter). [ordered](#) by variables are handled in the same way, except that no smooth is generated for the first level of the ordered factor (see [b3](#) example below). This is

useful for setting up identifiable models when the same smooth occurs more than once in a model, with different factor by variables.

As an example, consider the model

$$E(y_i) = \beta_0 + f(x_i)z_i$$

where f is a smooth function, and z_i is a numeric variable. The appropriate formula is:

`y ~ s(x, by=z)`

- the `by` argument ensures that the smooth function gets multiplied by covariate z . Note that when using `factor by variables`, centering constraints are applied to the smooths, which usually means that the `by` variable should be included as a parametric term, as well.

The example code below also illustrates the use of `factor by variables`.

`by variables` may be supplied as numeric matrices as part of specifying general linear functional terms.

If a `by variable` is present and numeric (rather than a factor) then the corresponding smooth is only subjected to an identifiability constraint if (i) the `by variable` is a constant vector, or, (ii) for a matrix `by variable`, L , if `L%%rep(1, ncol(L))` is constant or (iii) if a user defined smooth constructor supplies an identifiability constraint explicitly, and that constraint has an attribute `"always.apply"`.

Linking smooths with 'id'

It is sometimes desirable to insist that different smooth terms have the same degree of smoothness. This can be done by using the `id` argument to `s` or `te` terms. Smooths which share an `id` will have the same smoothing parameter. Really this only makes sense if the smooths use the same basis functions, and the default behaviour is to force this to happen: all smooths sharing an `id` have the same basis functions as the first smooth occurring with that `id`. Note that if you want exactly the same function for each smooth, then this is best achieved by making use of the summation convention covered under 'linear functional terms'.

As an example suppose that $E(y_i) \equiv \mu_i$ and

$$g(\mu_i) = f_1(x_{1i}) + f_2(x_{2i}, x_{3i}) + f_3(x_{4i})$$

but that f_1 and f_3 should have the same smoothing parameters (and x_2 and x_3 are on different scales). Then the `gam` formula

`y ~ s(x1, id=1) + te(x_2, x3) + s(x4, id=1)`

would achieve the desired result. `id` can be numbers or character strings. Giving an `id` to a term with a `factor by variable` causes the smooths at each level of the factor to have the same smoothing parameter.

Smooth term `ids` are not supported by `gamm`.

Linear functional terms

General linear functional terms have a long history in the spline literature including in the penalized GLM context (see e.g. Wahba 1990). Such terms encompass varying coefficient models/ geographic regression, functional GLMs (i.e. GLMs with functional predictors), GLASS models, etc, and allow smoothing with respect to aggregated covariate values, for example.

Such terms are implemented in `mgcv` using a simple 'summation convention' for smooth terms: If the covariates of a smooth are supplied as matrices, then summation of the evaluated smooth over

the columns of the matrices is implied. Each covariate matrix and any by variable matrix must be of the same dimension. Consider, for example the term

`s(X, Z, by=L)`

where X , Z and L are $n \times p$ matrices. Let f denote the thin plate regression spline specified. The resulting contribution to the i^{th} element of the linear predictor is

$$\sum_{j=1}^p L_{ij} f(X_{ij}, Z_{ij})$$

If no L is supplied then all its elements are taken as 1. In R code terms, let F denote the $n \times p$ matrix obtained by evaluating the smooth at the values in X and Z . Then the contribution of the term to the linear predictor is `rowSums(L*F)` (note that it's element by element multiplication here!).

The summation convention applies to `te` terms as well as `s` terms. More details and examples are provided in [linear.functional.terms](#).

Random effects

Random effects can be added to gam models using `s(..., bs="re")` terms (see [smooth.construct.re.smooth.spec](#)), or the `paraPen` argument to `gam` covered below. See [gam.vcomp](#), [random.effects](#) and [smooth.construct.re.smooth.spec](#) for further details. An alternative is to use the approach of [gamm](#).

Penalizing the parametric terms

In case the ability to add smooth classes, smooth identities, by variables and the summation convention are still not sufficient to implement exactly the penalized GLM that you require, `gam` also allows you to penalize the parametric terms in the model formula. This is mostly useful in allowing one or more matrix terms to be included in the formula, along with a sequence of quadratic penalty matrices for each.

Suppose that you have set up a model matrix \mathbf{X} , and want to penalize the corresponding coefficients, β with two penalties $\beta^T \mathbf{S}_1 \beta$ and $\beta^T \mathbf{S}_2 \beta$. Then something like the following would be appropriate: `gam(y ~ X - 1, paraPen=list(X=list(S1, S2)))`

The `paraPen` argument should be a list with elements having names corresponding to the terms being penalized. Each element of `paraPen` is itself a list, with optional elements `L`, `rank` and `sp`: all other elements must be penalty matrices. If present, `rank` is a vector giving the rank of each penalty matrix (if absent this is determined numerically). `L` is a matrix that maps underlying log smoothing parameters to the log smoothing parameters that actually multiply the individual quadratic penalties: taken as the identity if not supplied. `sp` is a vector of (underlying) smoothing parameter values: positive values are taken as fixed, negative to signal that the smoothing parameter should be estimated. Taken as all negative if not supplied.

An obvious application of `paraPen` is to incorporate random effects, and an example of this is provided below. In this case the supplied penalty matrices will be (generalized) inverse covariance matrices for the random effects — i.e. precision matrices. The final estimate of the covariance matrix corresponding to one of these penalties is given by the (generalized) inverse of the penalty matrix multiplied by the estimated scale parameter and divided by the estimated smoothing parameter for the penalty. For example, if you use an identity matrix to penalize some coefficients that are to be viewed as i.i.d. Gaussian random effects, then their estimated variance will be the estimated scale parameter divided by the estimate of the smoothing parameter, for this penalty. See the 'rail' example below.

P-values for penalized parametric terms should be treated with caution. If you must have them, then use the option `freq=TRUE` in `anova.gam` and `summary.gam`, which will tend to give reasonable results for random effects implemented this way, but not for terms with a rank deficient penalty (or penalties with a wide eigen-spectrum).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wahba (1990) Spline Models of Observational Data SIAM.

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

Examples

```
require(mgcv)
set.seed(10)
## simulate data from  $y = f(x_2) * x_1 + \text{error}$ 
dat <- gamSim(3, n=400)

b <- gam(y ~ s(x2, by=x1), data=dat)
plot(b, pages=1)
summary(b)

## Factor 'by' variable example (with a spurious covariate  $x_0$ )
## simulate data...

dat <- gamSim(4)

## fit model...
b <- gam(y ~ fac+s(x2, by=fac)+s(x0), data=dat)
plot(b, pages=1)
summary(b)

## note that the preceding fit is the same as...
b1 <- gam(y ~ s(x2, by=as.numeric(fac==1))+s(x2, by=as.numeric(fac==2))+
          s(x2, by=as.numeric(fac==3))+s(x0)-1, data=dat)
## ... the '-1' is because the intercept is confounded with the
## *uncentred* smooths here.
plot(b1, pages=1)
summary(b1)

## repeat forcing all s(x2) terms to have the same smoothing param
## (not a very good idea for these data!)
b2 <- gam(y ~ fac+s(x2, by=fac, id=1)+s(x0), data=dat)
plot(b2, pages=1)
summary(b2)

## now repeat with a single reference level smooth, and
## two 'difference' smooths...
```



```

dat$fac <- ordered(dat$fac)
b3 <- gam(y ~ fac+s(x2)+s(x2,by=fac)+s(x0),data=dat,method="REML")
plot(b3,pages=1)
summary(b3)

rm(dat)

## An example of a simple random effects term implemented via
## penalization of the parametric part of the model...

dat <- gamSim(1,n=400,scale=2) ## simulate 4 term additive truth
## Now add some random effects to the simulation. Response is
## grouped into one of 20 groups by `fac` and each groups has a
## random effect added....
fac <- as.factor(sample(1:20,400,replace=TRUE))
dat$X <- model.matrix(~fac-1)
b <- rnorm(20)*.5
dat$y <- dat$y + dat$X%*%b

## now fit appropriate random effect model...
PP <- list(X=list(rank=20,diag(20)))
rm <- gam(y~ X+s(x0)+s(x1)+s(x2)+s(x3),data=dat,paraPen=PP)
plot(rm,pages=1)
## Get estimated random effects standard deviation...
sig.b <- sqrt(rm$sig2/rm$sp[1]);sig.b

## a much simpler approach uses "re" terms...

rm1 <- gam(y ~ s(fac,bs="re")+s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="ML")
gam.vcomp(rm1)

## Simple comparison with lme, using Rail data.
## See ?random.effects for a simpler method
require(nlme)
b0 <- lme(travel~1,data=Rail,~1|Rail,method="ML")
Z <- model.matrix(~Rail-1,data=Rail,
  contrasts.arg=list(Rail="contr.treatment"))
b <- gam(travel~Z,data=Rail,paraPen=list(Z=list(diag(6))),method="ML")

b0
(b$reml.scale/b$sp)^.5 ## `gam` ML estimate of Rail sd
b$reml.scale^.5      ## `gam` ML estimate of residual sd

b0 <- lme(travel~1,data=Rail,~1|Rail,method="REML")
Z <- model.matrix(~Rail-1,data=Rail,
  contrasts.arg=list(Rail="contr.treatment"))
b <- gam(travel~Z,data=Rail,paraPen=list(Z=list(diag(6))),method="REML")

b0
(b$reml.scale/b$sp)^.5 ## `gam` REML estimate of Rail sd
b$reml.scale^.5      ## `gam` REML estimate of residual sd

```

```
#####
## Approximate large dataset logistic regression for rare events
## based on subsampling the zeroes, and adding an offset to
## approximately allow for this.
## Doing the same thing, but upweighting the sampled zeroes
## leads to problems with smoothness selection, and CIs.
#####
n <- 50000 ## simulate n data
dat <- gamSim(1,n=n,dist="binary",scale=.33)
p <- binomial()$linkinv(dat$f-6) ## make 1's rare
dat$y <- rbinom(p,1,p) ## re-simulate rare response

## Now sample all the 1's but only proportion S of the 0's
S <- 0.02 ## sampling fraction of zeroes
dat <- dat[dat$y==1 | runif(n) < S,] ## sampling

## Create offset based on total sampling fraction
dat$s <- rep(log(nrow(dat)/n),nrow(dat))

lr.fit <- gam(y~s(x0,bs="cr")+s(x1,bs="cr")+s(x2,bs="cr")+s(x3,bs="cr")+
  offset(s),family=binomial,data=dat,method="REML")

## plot model components with truth overlaid in red
op <- par(mfrow=c(2,2))
fn <- c("f0","f1","f2","f3");xn <- c("x0","x1","x2","x3")
for (k in 1:4) {
  plot(lr.fit,select=k,scale=0)
  ff <- dat[[fn[k]]];xx <- dat[[xn[k]]]
  ind <- sort.int(xx,index.return=TRUE)$ix
  lines(xx[ind],(ff-mean(ff))[ind]*.33,col=2)
}
par(op)
rm(dat)

## A Gamma example, by modify `gamSim' output...

dat <- gamSim(1,n=400,dist="normal",scale=1)
dat$f <- dat$f/4 ## true linear predictor
Ey <- exp(dat$f);scale <- .5 ## mean and GLM scale parameter
## Note that `shape' and `scale' in `rgamma' are almost
## opposite terminology to that used with GLM/GAM...
dat$y <- rgamma(Ey*0,shape=1/scale,scale=Ey*scale)
bg <- gam(y~ s(x0)+ s(x1)+s(x2)+s(x3),family=Gamma(link=log),
  data=dat,method="REML")
plot(bg,pages=1,scheme=1)
```

Description

Estimation of GAM smoothing parameters is most stable if optimization of the smoothness selection score (GCV, GACV, UBRE/AIC, REML, ML etc) is outer to the penalized iteratively re-weighted least squares scheme used to estimate the model given smoothing parameters.

This routine optimizes a smoothness selection score in this way. Basically the score is evaluated for each trial set of smoothing parameters by estimating the GAM for those smoothing parameters. The score is minimized w.r.t. the parameters numerically, using `newton` (default), `bfgs`, `optim` or `nlm`. Exact (first and second) derivatives of the score can be used by fitting with `gam.fit3`. This improves efficiency and reliability relative to relying on finite difference derivatives.

Not normally called directly, but rather a service routine for `gam`.

Usage

```
gam.outer(lsp, fscale, family, control, method, optimizer,
          criterion, scale, gamma, G, start=NULL, ...)
```

Arguments

<code>lsp</code>	The log smoothing parameters.
<code>fscale</code>	Typical scale of the GCV or UBRE/AIC score.
<code>family</code>	the model family.
<code>control</code>	control argument to pass to <code>gam.fit</code> if pure finite differencing is being used.
<code>method</code>	method argument to <code>gam</code> defining the smoothness criterion to use (but depending on whether or not <code>scale</code> known).
<code>optimizer</code>	The argument to <code>gam</code> defining the numerical optimization method to use.
<code>criterion</code>	Which smoothness selection criterion to use. One of "UBRE", "GCV", "GACV", "REML" or "P-REML".
<code>scale</code>	Supplied scale parameter. Positive indicates known.
<code>gamma</code>	The degree of freedom inflation factor for the GCV/UBRE/AIC score.
<code>G</code>	List produced by <code>mgcv:::gam.setup</code> , containing most of what's needed to actually fit a GAM.
<code>start</code>	starting parameter values.
<code>...</code>	other arguments, typically for passing on to <code>gam.fit3</code> (ultimately).

Details

See Wood (2008) for full details on 'outer iteration'.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36
<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam.fit3](#), [gam](#), [magic](#)

gam.scale

Scale parameter estimation in GAMs

Description

Scale parameter estimation in [gam](#) depends on the type of family. For extended families then the RE/ML estimate is used. For conventional exponential families, estimated by the default outer iteration, the scale estimator can be controlled using argument `scale.est` in [gam.control](#). The options are "fletcher" (default), "pearson" or "deviance". The Pearson estimator is the (weighted) sum of squares of the pearson residuals, divided by the effective residual degrees of freedom. The Fletcher (2012) estimator is an improved version of the Pearson estimator. The deviance estimator simply substitutes deviance residuals for Pearson residuals.

Usually the Pearson estimator is recommended for GLMs, since it is asymptotically unbiased. However, it can also be unstable at finite sample sizes, if a few Pearson residuals are very large. For example, a very low Poisson mean with a non zero count can give a huge Pearson residual, even though the deviance residual is much more modest. The Fletcher (2012) estimator is designed to reduce these problems.

For performance iteration the Pearson estimator is always used.

[gamm](#) uses the estimate of the scale parameter from the underlying call to `lme`. [bam](#) uses the REML estimator if the method is "fREML". Otherwise the estimator is a Pearson estimator.

Author(s)

Simon N. Wood <simon.wood@r-project.org> with help from Mark Bravington and David Peel

References

Fletcher, David J. (2012) Estimating overdispersion when fitting a generalized linear model to sparse data. *Biometrika* 99(1), 230-237.

See Also

[gam.control](#)

Description

This page is intended to provide some more information on how to select GAMs. In particular, it gives a brief overview of smoothness selection, and then discusses how this can be extended to select inclusion/exclusion of terms. Hypothesis testing approaches to the latter problem are also discussed.

Smoothness selection criteria

Given a model structure specified by a gam model formula, `gam()` attempts to find the appropriate smoothness for each applicable model term using prediction error criteria or likelihood based methods. The prediction error criteria used are Generalized (Approximate) Cross Validation (GCV or GACV) when the scale parameter is unknown or an Un-Biased Risk Estimator (UBRE) when it is known. UBRE is essentially scaled AIC (Generalized case) or Mallows' Cp (additive model case). GCV and UBRE are covered in Craven and Wahba (1979) and Wahba (1990). Alternatively REML of maximum likelihood (ML) may be used for smoothness selection, by viewing the smooth components as random effects (in this case the variance component for each smooth random effect will be given by the scale parameter divided by the smoothing parameter — for smooths with multiple penalties, there will be multiple variance components). The method argument to `gam` selects the smoothness selection criterion.

Automatic smoothness selection is unlikely to be successful with few data, particularly with multiple terms to be selected. In addition GCV and UBRE/AIC score can occasionally display local minima that can trap the minimisation algorithms. GCV/UBRE/AIC scores become constant with changing smoothing parameters at very low or very high smoothing parameters, and on occasion these 'flat' regions can be separated from regions of lower score by a small 'lip'. This seems to be the most common form of local minimum, but is usually avoidable by avoiding extreme smoothing parameters as starting values in optimization, and by avoiding big jumps in smoothing parameters while optimizing. Never the less, if you are suspicious of smoothing parameter estimates, try changing fit method (see `gam` arguments `method` and `optimizer`) and see if the estimates change, or try changing some or all of the smoothing parameters 'manually' (argument `sp` of `gam`, or `sp` arguments to `s` or `te`).

REML and ML are less prone to local minima than the other criteria, and may therefore be preferable.

Automatic term selection

Unmodified smoothness selection by GCV, AIC, REML etc. will not usually remove a smooth from a model. This is because most smoothing penalties view some space of (non-zero) functions as 'completely smooth' and once a term is penalized heavily enough that it is in this space, further penalization does not change it.

However it is straightforward to modify smooths so that under heavy penalization they are penalized to the zero function and thereby 'selected out' of the model. There are two approaches.

The first approach is to modify the smoothing penalty with an additional shrinkage term. Smooth classes `cs.smooth` and `tps.smooth` (specified by `"cs"` and `"ts"` respectively) have smoothness penalties which include a small shrinkage component, so that for large enough smoothing parameters the smooth becomes identically zero. This allows automatic smoothing parameter selection methods to effectively remove the term from the model altogether. The shrinkage component of the penalty is set at a level that usually makes negligible contribution to the penalization of the model, only becoming effective when the term is effectively ‘completely smooth’ according to the conventional penalty.

The second approach leaves the original smoothing penalty unchanged, but constructs an additional penalty for each smooth, which penalizes only functions in the null space of the original penalty (the ‘completely smooth’ functions). Hence, if all the smoothing parameters for a term tend to infinity, the term will be selected out of the model. This latter approach is more expensive computationally, but has the advantage that it can be applied automatically to any smooth term. The `select` argument to `gam` turns on this method.

In fact, as implemented, both approaches operate by eigen-decomposing the original penalty matrix. A new penalty is created on the null space: it is the matrix with the same eigenvectors as the original penalty, but with the originally positive eigenvalues set to zero, and the originally zero eigenvalues set to something positive. The first approach just adds a multiple of this penalty to the original penalty, where the multiple is chosen so that the new penalty can not dominate the original. The second approach treats the new penalty as an extra penalty, with its own smoothing parameter.

Of course, as with all model selection methods, some care must be taken to ensure that the automatic selection is sensible, and a decision about the effective degrees of freedom at which to declare a term ‘negligible’ has to be made.

Interactive term selection

In general the most logically consistent method to use for deciding which terms to include in the model is to compare GCV/UBRE/ML scores for models with and without the term (REML scores should not be used to compare models with different fixed effects structures). When UBRE is the smoothness selection method this will give the same result as comparing by AIC (the AIC in this case uses the model EDF in place of the usual model DF). Similarly, comparison via GCV score and via AIC seldom yields different answers. Note that the negative binomial with estimated theta parameter is a special case: the GCV score is not informative, because of the theta estimation scheme used. More generally the score for the model with a smooth term can be compared to the score for the model with the smooth term replaced by appropriate parametric terms. Candidates for replacement by parametric terms are smooth terms with estimated degrees of freedom close to their minimum possible.

Candidates for removal can also be identified by reference to the approximate p-values provided by `summary.gam`, and by looking at the extent to which the confidence band for an estimated term includes the zero function. It is perfectly possible to perform backwards selection using p-values in the usual way: that is by sequentially dropping the single term with the highest non-significant p-value from the model and re-fitting, until all terms are significant. This suffers from the same problems as stepwise procedures for any GLM/LM, with the additional caveat that the p-values are only approximate. If adopting this approach, it is probably best to use ML smoothness selection.

Note that GCV and UBRE are not appropriate for comparing models using different families: in that case AIC should be used.

Caveats/platitudes

Formal model selection methods are only appropriate for selecting between reasonable models. If formal model selection is attempted starting from a model that simply doesn't fit the data, then it is unlikely to provide meaningful results.

The more thought is given to appropriate model structure up front, the more successful model selection is likely to be. Simply starting with a hugely flexible model with 'everything in' and hoping that automatic selection will find the right structure is not often successful.

Author(s)

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References

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- Craven and Wahba (1979) Smoothing Noisy Data with Spline Functions. *Numer. Math.* 31:377-403
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- Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36
- <http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam](#), [step.gam](#)

Examples

```
## an example of automatic model selection via null space penalization
library(mgcv)
set.seed(3);n<-200
dat <- gamSim(1,n=n,scale=.15,dist="poisson") ## simulate data
dat$x4 <- runif(n, 0, 1);dat$x5 <- runif(n, 0, 1) ## spurious

b<-gam(y~s(x0)+s(x1)+s(x2)+s(x3)+s(x4)+s(x5),data=dat,
      family=poisson,select=TRUE,method="REML")
summary(b)
plot(b,pages=1)
```

gam.side

*Identifiability side conditions for a GAM***Description**

GAM formulae with repeated variables may only correspond to identifiable models given some side conditions. This routine works out appropriate side conditions, based on zeroing redundant parameters. It is called from `mgcv::gam.setup` and is not intended to be called by users.

The method identifies nested and repeated variables by their names, but numerically evaluates which constraints need to be imposed. Constraints are always applied to smooths of more variables in preference to smooths of fewer variables. The numerical approach allows appropriate constraints to be applied to models constructed using any smooths, including user defined smooths.

Usage

```
gam.side(sm, Xp, tol=.Machine$double.eps^.5, with.pen=FALSE)
```

Arguments

<code>sm</code>	A list of smooth objects as returned by <code>smooth.construct</code> .
<code>Xp</code>	The model matrix for the strictly parametric model components.
<code>tol</code>	The tolerance to use when assessing linear dependence of smooths.
<code>with.pen</code>	Should the computation of dependence consider the penalties or not. Doing so will lead to fewer constraints.

Details

Models such as $y \sim s(x) + s(z) + s(x, z)$ can be estimated by `gam`, but require identifiability constraints to be applied, to make them identifiable. This routine does this, effectively setting redundant parameters to zero. When the redundancy is between smooths of lower and higher numbers of variables, the constraint is always applied to the smooth of the higher number of variables.

Dependent smooths are identified symbolically, but which constraints are needed to ensure identifiability of these smooths is determined numerically, using `fixDependence`. This makes the routine rather general, and not dependent on any particular basis.

`Xp` is used to check whether there is a constant term in the model (or columns that can be linearly combined to give a constant). This is because centred smooths can appear independent, when they would be dependent if there is a constant in the model, so dependence testing needs to take account of this.

Value

A list of smooths, with model matrices and penalty matrices adjusted to automatically impose the required constraints. Any smooth that has been modified will have an attribute `"del.index"`, listing the columns of its model matrix that were deleted. This index is used in the creation of prediction matrices for the term.

WARNINGS

Much better statistical stability will be obtained by using models like $y \sim s(x) + s(z) + ti(x, z)$ or $y \sim ti(x) + ti(z) + ti(x, z)$ rather than $y \sim s(x) + s(z) + s(x, z)$, since the former are designed not to require further constraint.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[ti](#), [gam.models](#)

Examples

```
## The first two examples here illustrate models that cause
## gam.side to impose constraints, but both are a bad way
## of estimating such models. The 3rd example is the right
## way...
set.seed(7)
require(mgcv)
dat <- gamSim(n=400, scale=2) ## simulate data
## estimate model with redundant smooth interaction (bad idea).
b <- gam(y ~ s(x0) + s(x1) + s(x0, x1) + s(x2), data=dat)
plot(b, pages=1)

## Simulate data with real interaction...
dat <- gamSim(2, n=500, scale=.1)
old.par <- par(mfrow=c(2, 2))

## a fully nested tensor product example (bad idea)
b <- gam(y ~ s(x, bs="cr", k=6) + s(z, bs="cr", k=6) + te(x, z, k=6),
         data=dat$data)
plot(b)

old.par <- par(mfrow=c(2, 2))
## A fully nested tensor product example, done properly,
## so that gam.side is not needed to ensure identifiability.
## ti terms are designed to produce interaction smooths
## suitable for adding to main effects (we could also have
## used s(x) and s(z) without a problem, but not s(z, x)
## or te(z, x)).
b <- gam(y ~ ti(x, k=6) + ti(z, k=6) + ti(x, z, k=6),
         data=dat$data)
plot(b)

par(old.par)
rm(dat)
```

gam.vcomp

*Report gam smoothness estimates as variance components***Description**

GAMs can be viewed as mixed models, where the smoothing parameters are related to variance components. This routine extracts the estimated variance components associated with each smooth term, and if possible returns confidence intervals on the standard deviation scale.

Usage

```
gam.vcomp(x, rescale=TRUE, conf.lev=.95)
```

Arguments

x	a fitted model object of class gam as produced by gam().
rescale	the penalty matrices for smooths are rescaled before fitting, for numerical stability reasons, if TRUE this rescaling is reversed, so that the variance components are on the original scale.
conf.lev	when the smoothing parameters are estimated by REML or ML, then confidence intervals for the variance components can be obtained from large sample likelihood results. This gives the confidence level to work at.

Details

The (pseudo) inverse of the penalty matrix penalizing a term is proportional to the covariance matrix of the term's coefficients, when these are viewed as random. For single penalty smooths, it is possible to compute the variance component for the smooth (which multiplies the inverse penalty matrix to obtain the covariance matrix of the smooth's coefficients). This variance component is given by the scale parameter divided by the smoothing parameter.

This routine computes such variance components, for gam models, and associated confidence intervals, if smoothing parameter estimation was likelihood based. Note that variance components are also returned for tensor product smooths, but that their interpretation is not so straightforward.

The routine is particularly useful for model fitted by gam in which random effects have been incorporated.

Value

Either a vector of variance components for each smooth term (as standard deviations), or a matrix. The first column of the matrix gives standard deviations for each term, while the subsequent columns give lower and upper confidence bounds, on the same scale.

For models in which there are more smoothing parameters than actually estimated (e.g. if some were fixed, or smoothing parameters are linked) then a list is returned. The vc element is as above, the all element is a vector of variance components for all the smoothing parameters (estimated + fixed or replicated).

The routine prints a table of estimated standard deviations and confidence limits, if these can be computed, and reports the numerical rank of the covariance matrix.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2008) Fast stable direct fitting and smoothness selection for generalized additive models. *Journal of the Royal Statistical Society (B)* 70(3):495-518

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

See Also

[smooth.construct.re.smooth.spec](#)

Examples

```
set.seed(3)
require(mgcv)
## simulate some data, consisting of a smooth truth + random effects

dat <- gamSim(1,n=400,dist="normal",scale=2)
a <- factor(sample(1:10,400,replace=TRUE))
b <- factor(sample(1:7,400,replace=TRUE))
Xa <- model.matrix(~a-1) ## random main effects
Xb <- model.matrix(~b-1)
Xab <- model.matrix(~a:b-1) ## random interaction
dat$y <- dat$y + Xa%%rnorm(10)*.5 +
  Xb%%rnorm(7)*.3 + Xab%%rnorm(70)*.7
dat$a <- a;dat$b <- b

## Fit the model using "re" terms, and smoother linkage

mod <- gam(y~s(a,bs="re")+s(b,bs="re")+s(a,b,bs="re")+s(x0,id=1)+s(x1,id=1)+
  s(x2,k=15)+s(x3),data=dat,method="ML")

gam.vcomp(mod)
```

Description

Estimation of GAM smoothing parameters is most stable if optimization of the UBRE/AIC or GCV score is outer to the penalized iteratively re-weighted least squares scheme used to estimate the model given smoothing parameters. These functions evaluate the GCV/UBRE/AIC score of a GAM model, given smoothing parameters, in a manner suitable for use by `optim` or `nlm`. Not normally called directly, but rather service routines for `gam.outer`.

Usage

```
gam2objective(lsp, args, ...)  
gam2derivative(lsp, args, ...)
```

Arguments

lsp	The log smoothing parameters.
args	List of arguments required to call <code>gam.fit3</code> .
...	Other arguments for passing to <code>gam.fit3</code> .

Details

`gam2objective` and `gam2derivative` are functions suitable for calling by `optim`, to evaluate the GCV/UBRE/AIC score and its derivatives w.r.t. log smoothing parameters.

`gam4objective` is an equivalent to `gam2objective`, suitable for optimization by `nlm` - derivatives of the GCV/UBRE/AIC function are calculated and returned as attributes.

The basic idea of optimizing smoothing parameters ‘outer’ to the P-IRLS loop was first proposed in O’Sullivan et al. (1986).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

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<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam.fit3](#), [gam](#), [magic](#)

gamlss.etamu

*Transform derivatives wrt mu to derivatives wrt linear predictor***Description**

Mainly intended for internal use in specifying location scale models. Let $g(\mu) = \eta$, where η is the linear predictor, and g is the link function. Assume that we have calculated the derivatives of the log-likelihood wrt μ . This function uses the chain rule to calculate the derivatives of the log-likelihood wrt η . See [trind.generator](#) for array packing conventions.

Usage

```
gamlss.etamu(l1, l2, l3 = NULL, l4 = NULL, ig1, g2, g3 = NULL,
             g4 = NULL, i2, i3 = NULL, i4 = NULL, deriv = 0)
```

Arguments

l1	array of 1st order derivatives of log-likelihood wrt μ .
l2	array of 2nd order derivatives of log-likelihood wrt μ .
l3	array of 3rd order derivatives of log-likelihood wrt μ .
l4	array of 4th order derivatives of log-likelihood wrt μ .
ig1	reciprocal of the first derivative of the link function wrt the linear predictor.
g2	array containing the 2nd order derivative of the link function wrt the linear predictor.
g3	array containing the 3rd order derivative of the link function wrt the linear predictor.
g4	array containing the 4th order derivative of the link function wrt the linear predictor.
i2	two-dimensional index array, such that $l2[, i2[i, j]]$ contains the partial w.r.t. params indexed by i, j with no restriction on the index values (except that they are in $1, \dots, \text{ncol}(l1)$).
i3	third-dimensional index array, such that $l3[, i3[i, j, k]]$ contains the partial w.r.t. params indexed by i, j, k .
i4	third-dimensional index array, such that $l4[, i4[i, j, k, l]]$ contains the partial w.r.t. params indexed by i, j, k, l .
deriv	if <code>deriv==0</code> only first and second order derivatives will be calculated. If <code>deriv==1</code> the function goes up to 3rd order, and if <code>deriv==2</code> it provides also 4th order derivatives.

Value

A list where the arrays l1, l2, l3, l4 contain the derivatives (up to order four) of the log-likelihood wrt the linear predictor.

Author(s)

Simon N. Wood <simon.wood@r-project.org>.

See Also

[trind.generator](#)

gamlss.gH

Calculating derivatives of log-likelihood wrt regression coefficients

Description

Mainly intended for internal use with location scale model families. Given the derivatives of the log-likelihood wrt the linear predictor, this function obtains the derivatives and Hessian wrt the regression coefficients and derivatives of the Hessian w.r.t. the smoothing parameters. For input derivative array packing conventions see [trind.generator](#).

Usage

```
gamlss.gH(X, jj, l1, l2, i2, l3 = 0, i3 = 0, l4 = 0, i4 = 0, d1b = 0,
          d2b = 0, deriv = 0, fh = NULL, D = NULL)
```

Arguments

X	matrix containing the model matrices of all the linear predictors.
jj	list of index vectors such that $X[, jj[[i]]]$ is the model matrix of the i -th linear predictor.
l1	array of 1st order derivatives of each element of the log-likelihood wrt each parameter.
l2	array of 2nd order derivatives of each element of the log-likelihood wrt each parameter.
i2	two-dimensional index array, such that $l2[, i2[i, j]]$ contains the partial w.r.t. params indexed by i, j with no restriction on the index values (except that they are in $1, \dots, ncol(l1)$).
l3	array of 3rd order derivatives of each element of the log-likelihood wrt each parameter.
i3	third-dimensional index array, such that $l3[, i3[i, j, k]]$ contains the partial w.r.t. params indexed by i, j, k .
l4	array of 4th order derivatives of each element of the log-likelihood wrt each parameter.
i4	third-dimensional index array, such that $l4[, i4[i, j, k, l]]$ contains the partial w.r.t. params indexed by i, j, k, l .
d1b	first derivatives of the regression coefficients wrt the smoothing parameters.
d2b	second derivatives of the regression coefficients wrt the smoothing parameters.

deriv	if <code>deriv==0</code> only first and second order derivatives will be calculated. If <code>deriv==1</code> the function return also the diagonal of the first derivative of the Hessian, if <code>deriv==2</code> it return the full 3rd order derivative and if <code>deriv==3</code> it provides also 4th order derivatives.
fh	eigen-decomposition or Cholesky factor of the penalized Hessian.
D	diagonal matrix, used to provide some scaling.

Value

A list containing `lb` - the grad vector w.r.t. coefs; `lbb` - the Hessian matrix w.r.t. coefs; `d1H` - either a list of the derivatives of the Hessian w.r.t. the smoothing parameters, or a single matrix whose columns are the leading diagonals of these derivative matrices; `trHid2H` - the trace of the inverse Hessian multiplied by the second derivative of the Hessian w.r.t. all combinations of smoothing parameters.

Author(s)

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See Also

[trind.generator](#)

gamm

Generalized Additive Mixed Models

Description

Fits the specified generalized additive mixed model (GAMM) to data, by a call to `lme` in the normal errors identity link case, or by a call to `gammPQL` (a modification of `glmPQL` from the MASS library) otherwise. In the latter case estimates are only approximately MLEs. The routine is typically slower than `gam`, and not quite as numerically robust.

To use `lme4` in place of `nlme` as the underlying fitting engine, see `gamm4` from package `gamm4`.

Smooths are specified as in a call to `gam` as part of the fixed effects model formula, but the wiggly components of the smooth are treated as random effects. The random effects structures and correlation structures available for `lme` are used to specify other random effects and correlations.

It is assumed that the random effects and correlation structures are employed primarily to model residual correlation in the data and that the prime interest is in inference about the terms in the fixed effects model formula including the smooths. For this reason the routine calculates a posterior covariance matrix for the coefficients of all the terms in the fixed effects formula, including the smooths.

To use this function effectively it helps to be quite familiar with the use of `gam` and `lme`.

Usage

```
gamm(formula, random=NULL, correlation=NULL, family=gaussian(),
      data=list(), weights=NULL, subset=NULL, na.action, knots=NULL,
      control=list(niterEM=0, optimMethod="L-BFGS-B"),
      niterPQL=20, verbosePQL=TRUE, method="ML", drop.unused.levels=TRUE, ...)
```

Arguments

formula	A GAM formula (see also formula.gam and gam.models). This is like the formula for a <code>glm</code> except that smooth terms (<code>s</code> and <code>te</code>) can be added to the right hand side of the formula. Note that <code>ids</code> for smooths and fixed smoothing parameters are not supported.
random	The (optional) random effects structure as specified in a call to <code>lme</code> : only the <code>list</code> form is allowed, to facilitate manipulation of the random effects structure within <code>gamm</code> in order to deal with smooth terms. See example below.
correlation	An optional <code>corStruct</code> object (see corClasses) as used to define correlation structures in <code>lme</code> . Any grouping factors in the formula for this object are assumed to be nested within any random effect grouping factors, without the need to make this explicit in the formula (this is slightly different to the behaviour of <code>lme</code>). This is a GEE approach to correlation in the generalized case. See examples below.
family	A family as used in a call to <code>glm</code> or <code>gam</code> . The default <code>gaussian</code> with identity link causes <code>gamm</code> to fit by a direct call to <code>lme</code> provided there is no offset term, otherwise <code>gammPQL</code> is used.
data	A data frame or list containing the model response variable and covariates required by the formula. By default the variables are taken from <code>environment(formula)</code> , typically the environment from which <code>gamm</code> is called.
weights	In the generalized case, weights with the same meaning as <code>glm</code> weights. An <code>lme</code> type weights argument may only be used in the identity link gaussian case, with no offset (see documentation for <code>lme</code> for details of how to use such an argument).
subset	an optional vector specifying a subset of observations to be used in the fitting process.
na.action	a function which indicates what should happen when the data contain 'NA's. The default is set by the 'na.action' setting of 'options', and is 'na.fail' if that is unset. The "factory-fresh" default is 'na.omit'.
knots	this is an optional list containing user specified knot values to be used for basis construction. Different terms can use different numbers of knots, unless they share a covariate.
control	A list of fit control parameters for <code>lme</code> to replace the defaults returned by <code>lmeControl</code> . Note the setting for the number of EM iterations used by <code>lme</code> : smooths are set up using custom <code>pdMat</code> classes, which are currently not supported by the EM iteration code. If you supply a list of control values, it is advisable to include <code>niterEM=0</code> , as well, and only increase from 0 if you want to perturb the starting values used in model fitting (usually to worse values!). The <code>optimMethod</code> option is only used if your version of R does not have the <code>nlsminb</code> optimizer function.

niterPQL	Maximum number of PQL iterations (if any).
verbosePQL	Should PQL report its progress as it goes along?
method	Which of "ML" or "REML" to use in the Gaussian additive mixed model case when lme is called directly. Ignored in the generalized case (or if the model has an offset), in which case gammPQL is used.
drop.unused.levels	by default unused levels are dropped from factors before fitting. For some smooths involving factor variables you might want to turn this off. Only do so if you know what you are doing.
...	further arguments for passing on e.g. to lme

Details

The Bayesian model of spline smoothing introduced by Wahba (1983) and Silverman (1985) opens up the possibility of estimating the degree of smoothness of terms in a generalized additive model as variances of the wiggly components of the smooth terms treated as random effects. Several authors have recognised this (see Wang 1998; Ruppert, Wand and Carroll, 2003) and in the normal errors, identity link case estimation can be performed using general linear mixed effects modelling software such as lme. In the generalized case only approximate inference is so far available, for example using the Penalized Quasi-Likelihood approach of Breslow and Clayton (1993) as implemented in glmmPQL by Venables and Ripley (2002). One advantage of this approach is that it allows correlated errors to be dealt with via random effects or the correlation structures available in the nlme library (using correlation structures beyond the strictly additive case amounts to using a GEE approach to fitting).

Some details of how GAMs are represented as mixed models and estimated using lme or gammPQL in gamm can be found in Wood (2004 ,2006a,b). In addition gamm obtains a posterior covariance matrix for the parameters of all the fixed effects and the smooth terms. The approach is similar to that described in Lin & Zhang (1999) - the covariance matrix of the data (or pseudodata in the generalized case) implied by the weights, correlation and random effects structure is obtained, based on the estimates of the parameters of these terms and this is used to obtain the posterior covariance matrix of the fixed and smooth effects.

The bases used to represent smooth terms are the same as those used in gam, although adaptive smoothing bases are not available. Prediction from the returned gam object is straightforward using predict.gam, but this will set the random effects to zero. If you want to predict with random effects set to their predicted values then you can adapt the prediction code given in the examples below.

In the event of lme convergence failures, consider modifying option(mgcv.vc.logrange): reducing it helps to remove indefiniteness in the likelihood, if that is the problem, but too large a reduction can force over or undersmoothing. See notExp2 for more information on this option. Failing that, you can try increasing the niterEM option in control: this will perturb the starting values used in fitting, but usually to values with lower likelihood! Note that this version of gamm works best with R 2.2.0 or above and nlme, 3.1-62 and above, since these use an improved optimizer.

Value

Returns a list with two items:

gam	an object of class gam, less information relating to GCV/UBRE model selection. At present this contains enough information to use predict, summary and print
-----	--

methods and `vis.gam`, but not to use e.g. the `anova` method function to compare models.

`lme` the fitted model object returned by `lme` or `gammPQL`. Note that the model formulae and grouping structures may appear to be rather bizarre, because of the manner in which the GAMM is split up and the calls to `lme` and `gammPQL` are constructed.

WARNINGS

`gamm` was a somewhat different argument list to `gam`, `gam` arguments such as `gamma` supplied to `gamm` will just be ignored.

`gamm` performs poorly with binary data, since it uses PQL. It is better to use `gam` with `s(..., bs="re")` terms, or `gamm4`.

`gamm` assumes that you know what you are doing! For example, unlike `glmPQL` from MASS it will return the complete `lme` object from the working model at convergence of the PQL iteration, including the 'log likelihood', even though this is not the likelihood of the fitted GAMM.

The routine will be very slow and memory intensive if correlation structures are used for the very large groups of data. e.g. attempting to run the spatial example in the examples section with many 1000's of data is definitely not recommended: often the correlations should only apply within clusters that can be defined by a grouping factor, and provided these clusters do not get too huge then fitting is usually possible.

Models must contain at least one random effect: either a smooth with non-zero smoothing parameter, or a random effect specified in argument `random`.

`gamm` is not as numerically stable as `gam`: an `lme` call will occasionally fail. See details section for suggestions, or try the 'gamm4' package.

`gamm` is usually much slower than `gam`, and on some platforms you may need to increase the memory available to R in order to use it with large data sets (see `memory.limit`).

Note that the weights returned in the fitted GAM object are dummy, and not those used by the PQL iteration: this makes partial residual plots look odd.

Note that the `gam` object part of the returned object is not complete in the sense of having all the elements defined in `gamObject` and does not inherit from `glm`: hence e.g. multi-model `anova` calls will not work.

The parameterization used for the smoothing parameters in `gamm`, bounds them above and below by an effective infinity and effective zero. See `notExp2` for details of how to change this.

Linked smoothing parameters and adaptive smoothing are not supported.

Author(s)

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See Also

[magic](#) for an alternative for correlated data, [te](#), [s](#), [predict.gam](#), [plot.gam](#), [summary.gam](#), [negbin](#), [vis.gam](#), [pdTens](#), [gamm4](#) (<https://cran.r-project.org/package=gamm4>)

Examples

```
library(mgcv)
## simple examples using gamm as alternative to gam
set.seed(0)
dat <- gamSim(1,n=200,scale=2)
b <- gamm(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat)
plot(b$gam,pages=1)
summary(b$lme) # details of underlying lme fit
summary(b$gam) # gam style summary of fitted model
anova(b$gam)
gam.check(b$gam) # simple checking plots

b <- gamm(y~te(x0,x1)+s(x2)+s(x3),data=dat)
op <- par(mfrow=c(2,2))
plot(b$gam)
par(op)
rm(dat)

## Add a factor to the linear predictor, to be modelled as random
dat <- gamSim(6,n=200,scale=.2,dist="poisson")
b2<-gamm(y~s(x0)+s(x1)+s(x2),family=poisson,
         data=dat,random=list(fac=~1))
plot(b2$gam,pages=1)
fac <- dat$fac
```

```

rm(dat)
vis.gam(b2$gam)

## now an example with autocorrelated errors...
n <- 200;sig <- 2
x <- 0:(n-1)/(n-1)
f <- 0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10
e <- rnorm(n,0,sig)
for (i in 2:n) e[i] <- 0.6*e[i-1] + e[i]
y <- f + e
op <- par(mfrow=c(2,2))
## Fit model with AR1 residuals
b <- gamm(y~s(x,k=20),correlation=corAR1())
plot(b$gam);lines(x,f-mean(f),col=2)
## Raw residuals still show correlation, of course...
acf(residuals(b$gam),main="raw residual ACF")
## But standardized are now fine...
acf(residuals(b$lme,type="normalized"),main="standardized residual ACF")
## compare with model without AR component...
b <- gam(y~s(x,k=20))
plot(b);lines(x,f-mean(f),col=2)

## more complicated autocorrelation example - AR errors
## only within groups defined by `fac`
e <- rnorm(n,0,sig)
for (i in 2:n) e[i] <- 0.6*e[i-1]*(fac[i-1]==fac[i]) + e[i]
y <- f + e
b <- gamm(y~s(x,k=20),correlation=corAR1(form=~1|fac))
plot(b$gam);lines(x,f-mean(f),col=2)
par(op)

## more complex situation with nested random effects and within
## group correlation

set.seed(0)
n.g <- 10
n<-n.g*10*4
## simulate smooth part...
dat <- gamSim(1,n=n,scale=2)
f <- dat$f
## simulate nested random effects...
fa <- as.factor(rep(1:10,rep(4*n.g,10)))
ra <- rep(rnorm(10),rep(4*n.g,10))
fb <- as.factor(rep(rep(1:4,rep(n.g,4)),10))
rb <- rep(rnorm(4),rep(n.g,4))
for (i in 1:9) rb <- c(rb,rep(rnorm(4),rep(n.g,4)))
## simulate auto-correlated errors within groups
e<-array(0,0)
for (i in 1:40) {
  eg <- rnorm(n.g, 0, sig)
  for (j in 2:n.g) eg[j] <- eg[j-1]*0.6+ eg[j]
  e<-c(e,eg)
}

```

```

}
dat$y <- f + ra + rb + e
dat$fa <- fa; dat$fb <- fb
## fit model ...
b <- gamm(y~s(x0,bs="cr")+s(x1,bs="cr")+s(x2,bs="cr")+
  s(x3,bs="cr"),data=dat,random=list(fa=~1,fb=~1),
  correlation=corAR1())
plot(b$gam,pages=1)
summary(b$gam)
vis.gam(b$gam)

## Prediction from gam object, optionally adding
## in random effects.

## Extract random effects and make names more convenient...
refa <- ranef(b$lme,level=5)
rownames(refa) <- substr(rownames(refa),start=9,stop=20)
refb <- ranef(b$lme,level=6)
rownames(refb) <- substr(rownames(refb),start=9,stop=20)

## make a prediction, with random effects zero...
p0 <- predict(b$gam,data.frame(x0=.3,x1=.6,x2=.98,x3=.77))

## add in effect for fa = "2" and fb="2/4"...
p <- p0 + refa["2",1] + refb["2/4",1]

## and a "spatial" example...
library(nlme);set.seed(1);n <- 100
dat <- gamSim(2,n=n,scale=0) ## standard example
attach(dat)
old.par<-par(mfrow=c(2,2))
contour(truth$x,truth$z,truth$f) ## true function
f <- data$f ## true expected response
## Now simulate correlated errors...
cstr <- corGaus(.1,form = ~x+z)
cstr <- Initialize(cstr,data.frame(x=data$x,z=data$z))
V <- corMatrix(cstr) ## correlation matrix for data
Cv <- chol(V)
e <- t(Cv) %*% rnorm(n)*0.05 # correlated errors
## next add correlated simulated errors to expected values
data$y <- f + e ## ... to produce response
b<- gamm(y~s(x,z,k=50),correlation=corGaus(.1,form=~x+z),
  data=data)
plot(b$gam) # gamm fit accounting for correlation
# overfits when correlation ignored....
b1 <- gamm(y~s(x,z,k=50),data=data);plot(b1$gam)
b2 <- gamm(y~s(x,z,k=50),data=data);plot(b2)
par(old.par)

```

Description

A fitted GAM object returned by function `gam` and of class "gam" inheriting from classes "glm" and "lm". Method functions `anova`, `logLik`, `influence`, `plot`, `predict`, `print`, `residuals` and `summary` exist for this class.

All compulsory elements of "glm" and "lm" objects are present, but the fitting method for a GAM is different to a linear model or GLM, so that the elements relating to the QR decomposition of the model matrix are absent.

Value

A gam object has the following elements:

<code>aic</code>	AIC of the fitted model: bear in mind that the degrees of freedom used to calculate this are the effective degrees of freedom of the model, and the likelihood is evaluated at the maximum of the penalized likelihood in most cases, not at the MLE.
<code>assign</code>	Array whose elements indicate which model term (listed in <code>pterm</code> s) each parameter relates to: applies only to non-smooth terms.
<code>boundary</code>	did parameters end up at boundary of parameter space?
<code>call</code>	the matched call (allows update to be used with gam objects, for example).
<code>cmX</code>	column means of the model matrix (with elements corresponding to smooths set to zero) — useful for componentwise CI calculation.
<code>coefficients</code>	the coefficients of the fitted model. Parametric coefficients are first, followed by coefficients for each spline term in turn.
<code>control</code>	the gam control list used in the fit.
<code>converged</code>	indicates whether or not the iterative fitting method converged.
<code>data</code>	the original supplied data argument (for class "glm" compatibility). Only included if <code>gam</code> <code>control</code> argument element <code>keepData</code> is set to TRUE (default is FALSE).
<code>db.drho</code>	matrix of first derivatives of model coefficients w.r.t. log smoothing parameters.
<code>deviance</code>	model deviance (not penalized deviance).
<code>df.null</code>	null degrees of freedom.
<code>df.residual</code>	effective residual degrees of freedom of the model.
<code>edf</code>	estimated degrees of freedom for each model parameter. Penalization means that many of these are less than 1.
<code>edf1</code>	similar, but using alternative estimate of EDF. Useful for testing.
<code>edf2</code>	if estimation is by ML or REML then an edf that accounts for smoothing parameter uncertainty can be computed, this is it. <code>edf1</code> is a heuristic upper bound for <code>edf2</code> .
<code>family</code>	family object specifying distribution and link used.
<code>fitted.values</code>	fitted model predictions of expected value for each datum.
<code>formula</code>	the model formula.

<code>full.sp</code>	full array of smoothing parameters multiplying penalties (excluding any contribution from <code>min.sp</code> argument to <code>gam</code>). May be larger than <code>sp</code> if some terms share smoothing parameters, and/or some smoothing parameter values were supplied in the <code>sp</code> argument of <code>gam</code> .
<code>F</code>	Degrees of freedom matrix. This may be removed at some point, and should probably not be used.
<code>gcv.ubre</code>	The minimized smoothing parameter selection score: GCV, UBRE(AIC), GACV, negative log marginal likelihood or negative log restricted likelihood.
<code>hat</code>	array of elements from the leading diagonal of the ‘hat’ (or ‘influence’) matrix. Same length as response data vector.
<code>iter</code>	number of iterations of P-IRLS taken to get convergence.
<code>linear.predictors</code>	fitted model prediction of link function of expected value for each datum.
<code>method</code>	One of "GCV" or "UBRE", "REML", "P-REML", "ML", "P-ML", "PQL", "lme.ML" or "lme.REML", depending on the fitting criterion used.
<code>mgcv.conv</code>	A list of convergence diagnostics relating to the "magic" parts of smoothing parameter estimation - this will not be very meaningful for pure "outer" estimation of smoothing parameters. The items are: <code>full.rank</code> , The apparent rank of the problem given the model matrix and constraints; <code>rank</code> , The numerical rank of the problem; <code>fully.converged</code> , TRUE is multiple GCV/UBRE converged by meeting convergence criteria and FALSE if method stopped with a steepest descent step failure; <code>hess.pos.def</code> Was the hessian of the GCV/UBRE score positive definite at smoothing parameter estimation convergence?; <code>iter</code> How many iterations were required to find the smoothing parameters? <code>score.calls</code> , and how many times did the GCV/UBRE score have to be evaluated?; <code>rms.grad</code> , root mean square of the gradient of the GCV/UBRE score at convergence.
<code>min.edf</code>	Minimum possible degrees of freedom for whole model.
<code>model</code>	model frame containing all variables needed in original model fit.
<code>na.action</code>	The <code>na.action</code> used in fitting.
<code>nsdf</code>	number of parametric, non-smooth, model terms including the intercept.
<code>null.deviance</code>	deviance for single parameter model.
<code>offset</code>	model offset.
<code>optimizer</code>	optimizer argument to <code>gam</code> , or "magic" if it's a pure additive model.
<code>outer.info</code>	If ‘outer’ iteration has been used to fit the model (see <code>gam</code> argument <code>optimizer</code>) then this is present and contains whatever was returned by the optimization routine used (currently <code>nlm</code> or <code>optim</code>).
<code>paraPen</code>	If the <code>paraPen</code> argument to <code>gam</code> was used then this provides information on the parametric penalties. NULL otherwise.
<code>pred.formula</code>	one sided formula containing variables needed for prediction, used by <code>predict.gam</code>
<code>prior.weights</code>	prior weights on observations.
<code>pterms</code>	terms object for strictly parametric part of model.

R	Factor R from QR decomposition of weighted model matrix, unpivoted to be in same column order as model matrix (so need not be upper triangular).
rank	apparent rank of fitted model.
reml.scale	The scale (RE)ML scale parameter estimate, if (P-)(RE)ML used for smoothness estimation.
residuals	the working residuals for the fitted model.
rV	If present, $rV \% \% t(rV) * sig2$ gives the estimated Bayesian covariance matrix.
scale	when present, the scale (as sig2)
scale.estimated	TRUE if the scale parameter was estimated, FALSE otherwise.
sig2	estimated or supplied variance/scale parameter.
smooth	list of smooth objects, containing the basis information for each term in the model formula in the order in which they appear. These smooth objects are what gets returned by the <code>smooth.construct</code> objects.
sp	estimated smoothing parameters for the model. These are the underlying smoothing parameters, subject to optimization. For the full set of smoothing parameters multiplying the penalties see <code>full.sp</code> . Divide the scale parameter by the smoothing parameters to get, variance components, but note that this is not valid for smooths that have used rescaling to improve conditioning.
terms	terms object of model model frame.
var.summary	A named list of summary information on the predictor variables. If a parametric variable is a matrix, then the summary is a one row matrix, containing the observed data value closest to the column median, for each matrix column. If the variable is a factor the then summary is the modal factor level, returned as a factor, with levels corresponding to those of the data. For numerics and matrix arguments of smooths, the summary is the mean, nearest observed value to median and maximum, as a numeric vector. Used by <code>vis.gam</code> , in particular.
Ve	frequentist estimated covariance matrix for the parameter estimators. Particularly useful for testing whether terms are zero. Not so useful for CI's as smooths are usually biased.
Vp	estimated covariance matrix for the parameters. This is a Bayesian posterior covariance matrix that results from adopting a particular Bayesian model of the smoothing process. Particularly useful for creating credible/confidence intervals.
Vc	Under ML or REML smoothing parameter estimation it is possible to correct the covariance matrix <code>Vp</code> for smoothing parameter uncertainty. This is the corrected version.
weights	final weights used in IRLS iteration.
y	response data.

WARNINGS

This model object is different to that described in Chambers and Hastie (1993) in order to allow smoothing parameter estimation etc.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

A Key Reference on this implementation:

Wood, S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman & Hall/ CRC, Boca Raton, Florida

Key Reference on GAMs generally:

Hastie (1993) in Chambers and Hastie (1993) Statistical Models in S. Chapman and Hall.

Hastie and Tibshirani (1990) Generalized Additive Models. Chapman and Hall.

See Also

[gam](#)

gamSim

Simulate example data for GAMs

Description

Function used to simulate data sets to illustrate the use of [gam](#) and [gamm](#). Mostly used in help files to keep down the length of the example code sections.

Usage

```
gamSim(eg=1,n=400,dist="normal",scale=2,verbose=TRUE)
```

Arguments

eg	numeric value specifying the example required.
n	number of data to simulate.
dist	character string which may be used to specify the distribution of the response.
scale	Used to set noise level.
verbose	Should information about simulation type be printed?

Details

See the source code for exactly what is simulated in each case.

1. Gu and Wahba 4 univariate term example.
2. A smooth function of 2 variables.
3. Example with continuous by variable.
4. Example with factor by variable.
5. An additive example plus a factor variable.
6. Additive + random effect.
7. As 1 but with correlated covariates.

Value

Depends on eg, but usually a dataframe, which may also contain some information on the underlying truth. Sometimes a list with more items, including a data frame for model fitting. See source code or helpfile examples where the function is used for further information.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam](#), [gamm](#)

Examples

```
## see ?gam
```

gaulss

Gaussian location-scale model family

Description

The gaulss family implements Gaussian location scale additive models in which the mean and the logb of the standard deviation (see details) can depend on additive smooth predictors. Useable only with [gam](#), the linear predictors are specified via a list of formulae.

Usage

```
gaulss(link=list("identity", "logb"), b=0.01)
```

Arguments

link	two item list specifying the link for the mean and the standard deviation. See details.
b	The minimum standard deviation, for the "logb" link.

Details

Used with [gam](#) to fit Gaussian location - scale models. gam is called with a list containing 2 formulae, the first specifies the response on the left hand side and the structure of the linear predictor for the mean on the right hand side. The second is one sided, specifying the linear predictor for the standard deviation on the right hand side.

Link functions "identity", "inverse", "log" and "sqrt" are available for the mean. For the standard deviation only the "logb" link is implemented: $\eta = \log(\sigma - b)$ and $\sigma = b + \exp(\eta)$. This link is designed to avoid singularities in the likelihood caused by the standard deviation tending to zero.

The fitted values for this family will be a two column matrix. The first column is the mean, and the second column is the inverse of the standard deviation. Predictions using `predict.gam` will also produce 2 column matrices for type "link" and "response". The second column when type="response" is again on the reciprocal standard deviation scale (i.e. the square root precision scale).

The null deviance reported for this family is the sum of squares of the difference between the response and the mean response divided by the standard deviation of the response according to the model. The deviance is the sum of squares of residuals divided by model standard deviations.

Value

An object inheriting from class `general.family`.

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

Examples

```
library(mgcv);library(MASS)
b <- gam(list(accel~s(times,k=20,bs="ad"),~s(times)),
          data=mcycle,family=gaulss())
summary(b)
plot(b,pages=1,scale=0)
```

get.var

Get named variable or evaluate expression from list or data.frame

Description

This routine takes a text string and a data frame or list. It first sees if the string is the name of a variable in the data frame/ list. If it is then the value of this variable is returned. Otherwise the routine tries to evaluate the expression within the data.frame/list (but nowhere else) and if successful returns the result. If neither step works then NULL is returned. The routine is useful for processing gam formulae. If the variable is a matrix then it is coerced to a numeric vector, by default.

Usage

```
get.var(txt,data,vecMat=TRUE)
```

Arguments

txt	a text string which is either the name of a variable in data or when parsed is an expression that can be evaluated in data. It can also be neither in which case the function returns NULL.
data	A data frame or list.
vecMat	Should matrices be coerced to numeric vectors?

Value

The evaluated variable or NULL. May be coerced to a numeric vector if it's a matrix.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam](#)

Examples

```
require(mgcv)
y <- 1:4; dat<-data.frame(x=5:10)
get.var("x", dat)
get.var("y", dat)
get.var("x==6", dat)
dat <- list(X=matrix(1:6,3,2))
get.var("X", dat)
```

gevlss

Generalized Extreme Value location-scale model family

Description

The `gevlss` family implements Generalized Extreme Value location scale additive models in which the location, scale and shape parameters depend on additive smooth predictors. Usable only with [gam](#), the linear predictors are specified via a list of formulae.

Usage

```
gevlss(link=list("identity", "identity", "logit"))
```

Arguments

`link` three item list specifying the link for the location scale and shape parameters. See details.

Details

Used with `gam` to fit Generalized Extreme Value location scale and shape models. `gam` is called with a list containing 3 formulae: the first specifies the response on the left hand side and the structure of the linear predictor for the location parameter on the right hand side. The second is one sided, specifying the linear predictor for the log scale parameter on the right hand side. The third is one sided specifying the linear predictor for the shape parameter.

Link functions "identity" and "log" are available for the location (μ) parameter. There is no choice of link for the log scale parameter ($\rho = \log \sigma$). The shape parameter (ξ) defaults to a modified logit link restricting its range to $(-1, .5)$, the upper limit is required to ensure finite variance, while the lower limit ensures consistency of the MLE (Smith, 1985).

The fitted values for this family will be a three column matrix. The first column is the location parameter, the second column is the log scale parameter, the third column is the shape parameter.

This family does not produce a null deviance. Note that the distribution for $\xi = 0$ is approximated by setting ξ to a small number.

The derivative system code for this family is mostly auto-generated, and the family is still somewhat experimental.

Value

An object inheriting from class `general.family`.

References

Smith, R.L. (1985) Maximum likelihood estimation in a class of nonregular cases. *Biometrika* 72(1):67-90

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

Examples

```
library(mgcv)
Fi.gev <- function(z,mu,sigma,xi) {
  ## GEV inverse cdf.
  xi[abs(xi)<1e-8] <- 1e-8 ## approximate xi=0, by small xi
  x <- mu + ((-log(z))^-xi-1)*sigma/xi
}

## simulate test data..
f0 <- function(x) 2 * sin(pi * x)
f1 <- function(x) exp(2 * x)
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
  (10 * x)^3 * (1 - x)^10

set.seed(1)
n <- 500
x0 <- runif(n);x1 <- runif(n);x2 <- runif(n)
mu <- f2(x2)
rho <- f0(x0)
```

```

xi <- (f1(x1)-4)/9
y <- Fi.gev(runif(n),mu,exp(rho),xi)
dat <- data.frame(y,x0,x1,x2);pairs(dat)

## fit model...
b <- gam(list(y~s(x2),~s(x0),~s(x1)),family=gevlss,data=dat)

## plot and look at residuals...
plot(b,pages=1,scale=0)
summary(b)

par(mfrow=c(2,2))
mu <- fitted(b)[,1];rho <- fitted(b)[,2]
xi <- fitted(b)[,3]
## Get the predicted expected response...
fv <- mu + exp(rho)*(gamma(1-xi)-1)/xi
rsd <- residuals(b)
plot(fv,rsd);qqnorm(rsd)
plot(fv,residuals(b,"pearson"))
plot(fv,residuals(b,"response"))

```

identifiability

Identifiability constraints

Description

Smooth terms are generally only identifiable up to an additive constant. In consequence sum-to-zero identifiability constraints are imposed on most smooth terms. The exceptions are terms with by variables which cause the smooth to be identifiable without constraint (that doesn't include factor by variables), and random effect terms. Alternatively smooths can be set up to pass through zero at a user specified point.

Details

By default each smooth term is subject to the sum-to-zero constraint

$$\sum_i f(x_i) = 0.$$

The constraint is imposed by reparameterization. The sum-to-zero constraint causes the term to be orthogonal to the intercept: alternative constraints lead to wider confidence bands for the constrained smooth terms.

No constraint is used for random effect terms, since the penalty (random effect covariance matrix) anyway ensures identifiability in this case. Also if a by variable means that the smooth is anyway identifiable, then no extra constraint is imposed. Constraints are imposed for factor by variables, so that the main effect of the factor must usually be explicitly added to the model (the example below is an exception).

Occasionally it is desirable to substitute the constraint that a particular smooth curve should pass through zero at a particular point: the `pc` argument to `s`, `te`, `ti` and `t2` allows this: if specified then such constraints are always applied.

Author(s)

Simon N. Wood (s.wood@r-project.org)

Examples

```
## Example of three groups, each with a different smooth dependence on x
## but each starting at the same value...
require(mgcv)
set.seed(53)
n <- 100; x <- runif(3*n); z <- runif(3*n)
fac <- factor(rep(c("a", "b", "c"), each=100))
y <- c(sin(x[1:100]*4), exp(3*x[101:200])/10-.1, exp(-10*(x[201:300]-.5))/
      (1+exp(-10*(x[201:300]-.5)))-0.9933071) + z*(1-z)*5 + rnorm(100)*.4

## 'pc' used to constrain smooths to 0 at x=0...
b <- gam(y~s(x, by=fac, pc=0)+s(z))
plot(b, pages=1)
```

in.out

Which of a set of points lie within a polygon defined region

Description

Tests whether each of a set of points lie within a region defined by one or more (possibly nested) polygons. Points count as ‘inside’ if they are interior to an odd number of polygons.

Usage

```
in.out(bnd, x)
```

Arguments

bnd	A two column matrix, the rows of which define the vertices of polygons defining the boundary of a region. Different polygons should be separated by an NA row, and the polygons are assumed closed.
x	A two column matrix. Each row is a point to test for inclusion in the region defined by bnd.

Details

The algorithm works by counting boundary crossings (using compiled C code).

Value

A logical vector of length `nrow(x)`. TRUE if the corresponding row of `x` is inside the boundary and FALSE otherwise.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
library(mgcv)
data(columb.polys)
bnd <- columb.polys[[2]]
plot(bnd,type="n")
polygon(bnd)
x <- seq(7.9,8.7,length=20)
y <- seq(13.7,14.3,length=20)
gr <- as.matrix(expand.grid(x,y))
inside <- in.out(bnd,gr)
points(gr,col=as.numeric(inside)+1)
```

influence.gam

Extract the diagonal of the influence/hat matrix for a GAM

Description

Extracts the leading diagonal of the influence matrix (hat matrix) of a fitted gam object.

Usage

```
## S3 method for class 'gam'
influence(model,...)
```

Arguments

<code>model</code>	fitted model objects of class <code>gam</code> as produced by <code>gam()</code> .
<code>...</code>	un-used in this case

Details

Simply extracts hat array from fitted model. (More may follow!)

Value

An array (see above).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam](#)

initial.sp

Starting values for multiple smoothing parameter estimation

Description

Finds initial smoothing parameter guesses for multiple smoothing parameter estimation. The idea is to find values such that the estimated degrees of freedom per penalized parameter should be well away from 0 and 1 for each penalized parameter, thus ensuring that the values are in a region of parameter space where the smoothing parameter estimation criterion is varying substantially with smoothing parameter value.

Usage

```
initial.sp(X,S,off,expensive=FALSE,XX=FALSE)
```

Arguments

X	is the model matrix.
S	is a list of of penalty matrices. $S[[i]]$ is the i th penalty matrix, but note that it is not stored as a full matrix, but rather as the smallest square matrix including all the non-zero elements of the penalty matrix. Element 1,1 of $S[[i]]$ occupies element $off[i]$, $off[i]$ of the i th penalty matrix. Each $S[[i]]$ must be positive semi-definite.
off	is an array indicating the first parameter in the parameter vector that is penalized by the penalty involving $S[[i]]$.
expensive	if TRUE then the overall amount of smoothing is adjusted so that the average degrees of freedom per penalized parameter is exactly 0.5: this is numerically costly.
XX	if TRUE then X contains $X^T X$, rather than X .

Details

Basically uses a crude approximation to the estimated degrees of freedom per model coefficient, to try and find smoothing parameters which bound these e.d.f.'s away from 0 and 1.

Usually only called by [magic](#) and [gam](#).

Value

An array of initial smoothing parameter estimates.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[magic](#), [gam.outer](#), [gam](#),

inSide *Are points inside boundary?*

Description

Assesses whether points are inside a boundary. The boundary must enclose the domain, but may include islands.

Usage

```
inSide(bnd,x,y)
```

Arguments

bnd	This should have two equal length columns with names matching whatever is supplied in x and y. This may contain several sections of boundary separated by NA. Alternatively bnd may be a list, each element of which contains 2 columns named as above. See below for details.
x	x co-ordinates of points to be tested.
y	y co-ordinates of points to be tested.

Details

Segments of boundary are separated by NAs, or are in separate list elements. The boundary co-ordinates are taken to define nodes which are joined by straight line segments in order to create the boundary. Each segment is assumed to define a closed loop, and the last point in a segment will be assumed to be joined to the first. Loops must not intersect (no test is made for this).

The method used is to count how many times a line, in the y-direction from a point, crosses a boundary segment. An odd number of crossings defines an interior point. Hence in geographic applications it would be usual to have an outer boundary loop, possibly with some inner 'islands' completely enclosed in the outer loop.

The routine calls compiled C code and operates by an exhaustive search for each point in x, y.

Value

The function returns a logical array of the same dimension as x and y. TRUE indicates that the corresponding x, y point lies inside the boundary.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
require(mgcv)
m <- 300; n <- 150
xm <- seq(-1,4,length=m); yn<-seq(-1,1,length=n)
x <- rep(xm,n); y<-rep(yn,rep(m,n))
er <- matrix(fs.test(x,y),m,n)
bnd <- fs.boundary()
in.bnd <- inSide(bnd,x,y)
plot(x,y,col=as.numeric(in.bnd)+1,pch=".")
lines(bnd$x,bnd$y,col=3)
points(x,y,col=as.numeric(in.bnd)+1,pch=".")
## check boundary details ...
plot(x,y,col=as.numeric(in.bnd)+1,pch=".",ylim=c(-1,0),xlim=c(3,3.5))
lines(bnd$x,bnd$y,col=3)
points(x,y,col=as.numeric(in.bnd)+1,pch=".")
```

interpret.gam

Interpret a GAM formula

Description

This is an internal function of package `mgcv`. It is a service routine for `gam` which splits off the strictly parametric part of the model formula, returning it as a formula, and interprets the smooth parts of the model formula.

Not normally called directly.

Usage

```
interpret.gam(gf)
```

Arguments

`gf` A GAM formula as supplied to `gam` or `gamm`, or a list of such formulae, as supplied for some `gam` families.

Value

An object of class `split.gam.formula` with the following items:

<code>pf</code>	A model formula for the strictly parametric part of the model.
<code>pfok</code>	TRUE if there is a <code>pf</code> formula.
<code>smooth.spec</code>	A list of class <code>xx.smooth.spec</code> objects where <code>xx</code> depends on the basis specified for the term. (These can be passed to smooth constructor method functions to actually set up penalties and bases.)
<code>full.formula</code>	An expanded version of the model formula in which the options are fully expanded, and the options do not depend on variables which might not be available later.
<code>fake.formula</code>	A formula suitable for use in evaluating a model frame.
<code>response</code>	Name of the response variable.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam](#) [gamm](#)

jagam

Just Another Gibbs Additive Modeller: JAGS support for mgcv.

Description

Facilities to auto-generate model specification code and associated data to simulate with GAMs in JAGS (or BUGS). This is useful for inference about models with complex random effects structure best coded in JAGS. It is a very inefficient approach to making inferences about standard GAMs. The idea is that `jagam` generates template JAGS code, and associated data, for the smooth part of the model. This template is then directly edited to include other stochastic components. After simulation with the resulting model, facilities are provided for plotting and prediction with the model smooth components.

Usage

```
jagam(formula,family=gaussian,data=list(),file,weights=NULL,na.action,
offset=NULL,knots=NULL,sp=NULL,drop.unused.levels=TRUE,
control=gam.control(),centred=TRUE,sp.prior = "gamma",diagonalize=FALSE)
```

```
sim2jam(sam,pregam,edf.type=2,burnin=0)
```

Arguments

formula	A GAM formula (see formula.gam and also gam.models). This is exactly like the formula for a GLM except that smooth terms, <code>s</code> , <code>te</code> , <code>ti</code> and <code>t2</code> can be added to the right hand side to specify that the linear predictor depends on smooth functions of predictors (or linear functionals of these).
family	This is a family object specifying the distribution and link function to use. See glm and family for more details. Currently only gaussian, poisson, binomial and Gamma families are supported, but the user can easily modify the assumed distribution in the JAGS code.
data	A data frame or list containing the model response variable and covariates required by the formula. By default the variables are taken from <code>environment(formula)</code> : typically the environment from which <code>jagam</code> is called.
file	Name of the file to which JAGS model specification code should be written. See setwd for setting and querying the current working directory.
weights	prior weights on the data.
na.action	a function which indicates what should happen when the data contain 'NA's. The default is set by the 'na.action' setting of 'options', and is 'na.fail' if that is unset. The "factory-fresh" default is 'na.omit'.
offset	Can be used to supply a model offset for use in fitting. Note that this offset will always be completely ignored when predicting, unlike an offset included in formula: this conforms to the behaviour of <code>lm</code> and <code>glm</code> .
control	A list of fit control parameters to replace defaults returned by gam.control . Any control parameters not supplied stay at their default values. little effect on <code>jagam</code> .
knots	this is an optional list containing user specified knot values to be used for basis construction. For most bases the user simply supplies the knots to be used, which must match up with the <code>k</code> value supplied (note that the number of knots is not always just <code>k</code>). See tprs for what happens in the "tp"/"ts" case. Different terms can use different numbers of knots, unless they share a covariate.
sp	A vector of smoothing parameters can be provided here. Smoothing parameters must be supplied in the order that the smooth terms appear in the model formula (without forgetting null space penalties). Negative elements indicate that the parameter should be estimated, and hence a mixture of fixed and estimated parameters is possible. If smooths share smoothing parameters then <code>length(sp)</code> must correspond to the number of underlying smoothing parameters.
drop.unused.levels	by default unused levels are dropped from factors before fitting. For some smooths involving factor variables you might want to turn this off. Only do so if you know what you are doing.
centred	Should centring constraints be applied to the smooths, as is usual with GAMS? Only set this to FALSE if you know exactly what you are doing. If FALSE there is a (usually global) intercept for each smooth.
sp.prior	"gamma" or "log.uniform" prior for the smoothing parameters? Do check that the default parameters are appropriate for your model in the JAGS code.

diagonalize	Should smooths be re-parameterized to have i.i.d. Gaussian priors (where possible)? For Gaussian data this allows efficient conjugate samplers to be used, and it can also work well with GLMs if the JAGS "glm" module is loaded, but otherwise it is often better to update smoothers blockwise, and not do this.
sam	jags sample object, containing at least fields b (coefficients) and rho (log smoothing parameters). May also contain field mu containing monitored expected response.
pregam	standard mgcv GAM setup data, as returned in jagam return list.
edf.type	Since EDF is not uniquely defined and may be affected by the stochastic structure added to the JAGS model file, 3 options are offered. See details.
burnin	the amount of burn in to discard from the simulation chains. Limited to .9 of the chain length.

Details

Smooths are easily incorporated into JAGS models using multivariate normal priors on the smooth coefficients. The smoothing parameters and smoothing penalty matrices directly specify the prior multivariate normal precision matrix. Normally a smoothing penalty does not correspond to a full rank precision matrix, implying an improper prior inappropriate for Gibbs sampling. To rectify this problem the null space penalties suggested in Marra and Wood (2011) are added to the usual penalties.

In an additive modelling context it is usual to centre the smooths, to avoid the identifiability issues associated with having an intercept for each smooth term (in addition to a global intercept). Under Gibbs sampling with JAGS it is technically possible to omit this centring, since we anyway force propriety on the priors, and this propriety implies formal model identifiability. However, in most situations this formal identifiability is rather artificial and does not imply statistically meaningful identifiability. Rather it serves only to massively inflate confidence intervals, since the multiple intercept terms are not identifiable from the data, but only from the prior. By default then, jagam imposes standard GAM identifiability constraints on all smooths. The centred argument does allow you to turn this off, but it is not recommended. If you do set centred=FALSE then chain convergence and mixing checks should be particularly stringent.

The final technical issue for model setup is the setting of initial conditions for the coefficients and smoothing parameters. The approach taken is to take the default initial smoothing parameter values used elsewhere by mgcv, and to take a single PIRLS fitting step with these smoothing parameters in order to obtain starting values for the smooth coefficients. In the setting of fully conjugate updating the initial values of the coefficients are not critical, and good results are obtained without supplying them. But in the usual setting in which slice sampling is required for at least some of the updates then very poor results can sometimes be obtained without initial values, as the sampler simply fails to find the region of the posterior mode.

The sim2jam function takes the partial gam object (pregam) from jagam along with simulation output in standard rjags form and creates a reduced version of a gam object, suitable for plotting and prediction of the model's smooth components. sim2gam computes effective degrees of freedom for each smooth, but it should be noted that there are several possibilities for doing this in the context of a model with a complex random effects structure. The simplest approach (edf.type=0) is to compute the degrees of freedom that the smooth would have had if it had been part of an unweighted Gaussian additive model. One might choose to use this option if the model has been modified so that the response distribution and/or link are not those that were specified to jagam. The second

option is (`edf.type=1`) uses the edf that would have been computed by `gam` had it produced these estimates - in the context in which the JAGS model modifications have all been about modifying the random effects structure, this is equivalent to simply setting all the random effects to zero for the effective degrees of freedom calculation. The default option (`edf.type=2`) is to base the EDF on the sample covariance matrix, V_p , of the model coefficients. If the simulation output (`sim`) includes a `mu` field, then this will be used to form the weight matrix W in $XWX = t(X) \%*\% W \%*\% X$, where the EDF is computed from `rowSums(Vp*XWX)*scale`. If `mu` is not supplied then it is estimated from the the model matrix X and the mean of the simulated coefficients, but the resulting W may not be strictly compatible with the V_p matrix in this case. In the situation in which the fitted model is very different in structure from the regression model of the template produced by `jagam` then the default option may make no sense, and indeed it may be best to use option 0.

Value

For `jagam` a three item list containing

<code>pregam</code>	standard <code>mgcv</code> GAM setup data.
<code>jags.data</code>	list of arguments to be supplied to JAGS containing information referenced in model specification.
<code>jags.ini</code>	initialization data for smooth coefficients and smoothing parameters.

For `sim2jam` an object of class "jam": a partial version of an `mgcv gamObject`, suitable for plotting and predicting.

WARNINGS

Gibb's sampling is a very slow inferential method for standard GAMs. It is only likely to be worthwhile when complex random effects structures are required above what is possible with direct GAMM methods.

Check that the parameters of the priors on the parameters are fit for your purpose.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2016) Just Another Gibbs Additive Modeller: Interfacing JAGS and `mgcv`. *Journal of Statistical Software* 75(7):1-15 doi:10.18637/jss.v075.i07)

Marra, G. and S.N. Wood (2011) Practical variable selection for generalized additive models. *Computational Statistics & Data Analysis* 55(7): 2372-2387

Here is a key early reference to smoothing using BUGS (although the approach and smooths used are a bit different to `jagam`)

Crainiceanu, C. M. D Ruppert, & M.P. Wand (2005) Bayesian Analysis for Penalized Spline Regression Using WinBUGS *Journal of Statistical Software* 14.

See Also

[gam](#), [gamm](#), [bam](#)

Examples

```

## the following illustrates a typical workflow. To run the
## 'Not run' code you need rjags (and JAGS) to be installed.
require(mgcv)

set.seed(2) ## simulate some data...
n <- 400
dat <- gamSim(1,n=n,dist="normal",scale=2)
## regular gam fit for comparison...
b0 <- gam(y~s(x0)+s(x1) + s(x2)+s(x3),data=dat,method="REML")

## Set up JAGS code and data. In this one might want to diagonalize
## to use conjugate samplers. Usually call 'setwd' first, to set
## directory in which model file ("test.jags") will be written.
jd <- jagam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,file="test.jags",
            sp.prior="gamma",diagonalize=TRUE)

## In normal use the model in "test.jags" would now be edited to add
## the non-standard stochastic elements that require use of JAGS...

## Not run:
require(rjags)
load.module("glm") ## improved samplers for GLMs often worth loading
jm <- jags.model("test.jags",data=jd$jags.data,init=jd$jags.ini,n.chains=1)
list.samplers(jm)
sam <- jags.samples(jm,c("b","rho","scale"),n.iter=10000,thin=10)
jam <- sim2jam(sam,jd$pregam)
plot(jam,pages=1)
jam
pd <- data.frame(x0=c(.5,.6),x1=c(.4,.2),x2=c(.8,.4),x3=c(.1,.1))
fv <- predict(jam,newdata=pd)
## and some minimal checking...
require(coda)
effectiveSize(as.mcmc.list(sam$b))

## End(Not run)

## a gamma example...
set.seed(1); n <- 400
dat <- gamSim(1,n=n,dist="normal",scale=2)
scale <- .5; Ey <- exp(dat$f/2)
dat$y <- rgamma(n,shape=1/scale,scale=Ey*scale)
jd <- jagam(y~s(x0)+te(x1,x2)+s(x3),data=dat,family=Gamma(link=log),
            file="test.jags",sp.prior="log.uniform")

## In normal use the model in "test.jags" would now be edited to add
## the non-standard stochastic elements that require use of JAGS...

## Not run:
require(rjags)
## following sets random seed, but note that under JAGS 3.4 many
## models are still not fully repeatable (JAGS 4 should fix this)

```



```

jd$jags.ini$.RNG.name <- "base::Mersenne-Twister" ## setting RNG
jd$jags.ini$.RNG.seed <- 6 ## how to set RNG seed
jm <- jags.model("test.jags",data=jd$jags.data, inits=jd$jags.ini,n.chains=1)
list.samplers(jm)
sam <- jags.samples(jm,c("b","rho","scale","mu"),n.iter=10000,thin=10)
jam <- sim2jam(sam,jd$pregam)
plot(jam,pages=1)
jam
pd <- data.frame(x0=c(.5,.6),x1=c(.4,.2),x2=c(.8,.4),x3=c(.1,.1))
fv <- predict(jam,newdata=pd)

## End(Not run)

```

ldTweedie

*Log Tweedie density evaluation***Description**

A function to evaluate the log of the Tweedie density for variance powers between 1 and 2, inclusive. Also evaluates first and second derivatives of log density w.r.t. its scale parameter, ϕ , and p , or w.r.t. $\rho = \log(\phi)$ and θ where $p = (a+b \cdot \exp(\theta)) / (1 + \exp(\theta))$.

Usage

```
ldTweedie(y,mu=y,p=1.5,phi=1,rho=NA,theta=NA,a=1.001,b=1.999,all.derivs=FALSE)
```

Arguments

y	values at which to evaluate density.
mu	corresponding means (either of same length as y or a single value).
p	the variance of y is proportional to its mean to the power p. p must be between 1 and 2. 1 is Poisson like (exactly Poisson if $\phi=1$), 2 is gamma.
phi	The scale parameter. Variance of y is $\phi \cdot \mu^p$.
rho	optional log scale parameter. Over-rides phi if theta also supplied.
theta	parameter such that $p = (a+b \cdot \exp(\theta)) / (1 + \exp(\theta))$. Over-rides p if rho also supplied.
a	lower limit parameter (>1) used in definition of p from theta.
b	upper limit parameter (<2) used in definition of p from theta.
all.derivs	if TRUE then derivatives w.r.t. mu are also returned. Only available with rho and phi parameterization.

Details

A Tweedie random variable with $1 < p < 2$ is a sum of N gamma random variables where N has a Poisson distribution. The $p=1$ case is a generalization of a Poisson distribution and is a discrete distribution supported on integer multiples of the scale parameter. For $1 < p < 2$ the distribution is supported on the positive reals with a point mass at zero. $p=2$ is a gamma distribution. As p gets very close to 1 the continuous distribution begins to converge on the discretely supported limit at $p=1$.

ldTweedie is based on the series evaluation method of Dunn and Smyth (2005). Without the restriction on p the calculation of Tweedie densities is less straightforward. If you really need this case then the tweedie package is the place to start.

The rho, theta parameterization is useful for optimization of p and ϕ , in order to keep p bounded well away from 1 and 2, and ϕ positive. The derivatives near $p=1$ tend to infinity.

Note that if p and ϕ (or theta and rho) both contain only a single unique value, then the underlying code is able to use buffering to avoid repeated calls to expensive log gamma, di-gamma and tri-gamma functions (μ can still be a vector of different values). This is much faster than is possible when these parameters are vectors with different values.

Value

A matrix with 6 columns, or 10 if `all.derivs=TRUE`. The first is the log density of y (log probability if $p=1$). The second and third are the first and second derivatives of the log density w.r.t. ϕ . 4th and 5th columns are first and second derivative w.r.t. p , final column is second derivative w.r.t. ϕ and p .

If rho and theta were supplied then derivatives are w.r.t. these. In this case, and if `all.derivs=TRUE` then the 7th column is the derivative w.r.t. μ , the 8th is the 2nd derivative w.r.t. μ , the 9th is the mixed derivative w.r.t. theta and μ and the 10th is the mixed derivative w.r.t. rho and μ .

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Dunn, P.K. and G.K. Smith (2005) Series evaluation of Tweedie exponential dispersion model densities. *Statistics and Computing* 15:267-280

Tweedie, M. C. K. (1984). An index which distinguishes between some important exponential families. *Statistics: Applications and New Directions. Proceedings of the Indian Statistical Institute Golden Jubilee International Conference* (Eds. J. K. Ghosh and J. Roy), pp. 579-604. Calcutta: Indian Statistical Institute.

Examples

```
library(mgcv)
## convergence to Poisson illustrated
## notice how p>1.1 is OK
y <- seq(1e-10,10,length=1000)
p <- c(1.0001,1.001,1.01,1.1,1.2,1.5,1.8,2)
phi <- .5
```

```

fy <- exp(ldTweedie(y,mu=2,p=p[1],phi=phi)[,1])
plot(y,fy,type="l",ylim=c(0,3),main="Tweedie density as p changes")
for (i in 2:length(p)) {
  fy <- exp(ldTweedie(y,mu=2,p=p[i],phi=phi)[,1])
  lines(y,fy,col=i)
}

```

linear.functional.terms

Linear functionals of a smooth in GAMs

Description

`gam` allows the response variable to depend on linear functionals of smooth terms. Specifically dependencies of the form

$$g(\mu_i) = \dots + \sum_j L_{ij} f(x_{ij}) + \dots$$

are allowed, where the x_{ij} are covariate values and the L_{ij} are fixed weights. i.e. the response can depend on the weighted sum of the same smooth evaluated at different covariate values. This allows, for example, for the response to depend on the derivatives or integrals of a smooth (approximated by finite differencing or quadrature, respectively). It also allows dependence on predictor functions (sometimes called ‘signal regression’).

The mechanism by which this is achieved is to supply matrices of covariate values to the model smooth terms specified by `s` or `te` terms in the model formula. Each column of the covariate matrix gives rise to a corresponding column of predictions from the smooth. Let the resulting matrix of evaluated smooth values be F (F will have the same dimension as the covariate matrices). In the absence of a by variable then these columns are simply summed and added to the linear predictor. i.e. the contribution of the term to the linear predictor is $\text{rowSums}(F)$. If a by variable is present then it must be a matrix, L , say, of the same dimension as F (and the covariate matrices), and it contains the weights L_{ij} in the summation given above. So in this case the contribution to the linear predictor is $\text{rowSums}(L * F)$.

Note that if a **L1** (i.e. $\text{rowSums}(L)$) is a constant vector, or there is no by variable then the smooth will automatically be centred in order to ensure identifiability. Otherwise it will not be. Note also that for centred smooths it can be worth replacing the constant term in the model with $\text{rowSums}(L)$ in order to ensure that predictions are automatically on the right scale.

When predicting from the model it is not necessary to provide matrix covariate and by variable values. For example to simply examine the underlying smooth function one would use vectors of covariate values and vector by variables, with the by variable and equivalent of **L1**, above, set to vectors of ones.

Author(s)

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Examples

```

### matrix argument `linear operator' smoothing
library(mgcv)
set.seed(0)

#####
## simple summation example...#
#####

n<-400
sig<-2
x <- runif(n, 0, .9)
f2 <- function(x) 0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10
x1 <- x + .1

f <- f2(x) + f2(x1) ## response is sum of f at two adjacent x values
y <- f + rnorm(n)*sig

X <- matrix(c(x,x1),n,2) ## matrix covariate contains both x values
b <- gam(y~s(X))

plot(b) ## reconstruction of f
plot(f,fitted(b))

#####
## multivariate integral example. Function `test1' will be integrated#
## (by midpoint quadrature) over 100 equal area sub-squares covering #
## the unit square. Noise is added to the resulting simulated data. #
## `test1' is estimated from the resulting data using two alternative#
## smooths. #
#####

test1 <- function(x,z,sx=0.3,sz=0.4)
  { (pi*sx*sz)*(1.2*exp(-(x-0.2)^2/sx^2-(z-0.3)^2/sz^2)+
    0.8*exp(-(x-0.7)^2/sx^2-(z-0.8)^2/sz^2))
  }

## create quadrature (integration) grid, in useful order
ig <- 5 ## integration grid within square
mx <- mz <- (1:ig-.5)/ig
ix <- rep(mx,ig);iz <- rep(mz,rep(ig,ig))

og <- 10 ## observation grid
mx <- mz <- (1:og-1)/og
ox <- rep(mx,og);ox <- rep(ox,rep(ig^2,og^2))
oz <- rep(mz,rep(og,og));oz <- rep(oz,rep(ig^2,og^2))

x <- ox + ix/og;z <- oz + iz/og ## full grid, subsquare by subsquare

## create matrix covariates...
X <- matrix(x,og^2,ig^2,byrow=TRUE)
Z <- matrix(z,og^2,ig^2,byrow=TRUE)

```

```

## create simulated test data...
dA <- 1/(og*ig)^2 ## quadrature square area
F <- test1(X,Z) ## evaluate on grid
f <- rowSums(F)*dA ## integrate by midpoint quadrature
y <- f + rnorm(og^2)*5e-4 ## add noise
## ... so each y is a noisy observation of the integral of `test1'
## over a 0.1 by 0.1 sub-square from the unit square

## Now fit model to simulated data...

L <- X*0 + dA

## ... let F be the matrix of the smooth evaluated at the x,z values
## in matrices X and Z. rowSums(L*F) gives the model predicted
## integrals of `test1' corresponding to the observed `y'

L1 <- rowSums(L) ## smooths are centred --- need to add in L%*%1

## fit models to reconstruct `test1'....

b <- gam(y~s(X,Z,by=L)+L1-1) ## (L1 and const are confounded here)
b1 <- gam(y~te(X,Z,by=L)+L1-1) ## tensor product alternative

## plot results...

old.par<-par(mfrow=c(2,2))
x<-runif(n);z<-runif(n);
xs<-seq(0,1,length=30);zs<-seq(0,1,length=30)
pr<-data.frame(x=rep(xs,30),z=rep(zs,rep(30,30)))
truth<-matrix(test1(pr$x,pr$z),30,30)
contour(xs,zs,truth)
plot(b)
vis.gam(b,view=c("X","Z"),cond=list(L1=1,L=1),plot.type="contour")
vis.gam(b1,view=c("X","Z"),cond=list(L1=1,L=1),plot.type="contour")

#####
## A "signal" regression example...#
#####

rf <- function(x=seq(0,1,length=100)) {
## generates random functions...
  m <- ceiling(runif(1)*5) ## number of components
  f <- x*0;
  mu <- runif(m,min(x),max(x));sig <- (runif(m)+.5)*(max(x)-min(x))/10
  for (i in 1:m) f <- f+ dnorm(x,mu[i],sig[i])
  f
}

x <- seq(0,1,length=100) ## evaluation points

## example functional predictors...
par(mfrow=c(3,3));for (i in 1:9) plot(x,rf(x),type="l",xlab="x")

```

```

## simulate 200 functions and store in rows of L...
L <- matrix(NA,200,100)
for (i in 1:200) L[i,] <- rf() ## simulate the functional predictors

f2 <- function(x) { ## the coefficient function
  (0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10)/10
}

f <- f2(x) ## the true coefficient function

y <- L%*%f + rnorm(200)*20 ## simulated response data

## Now fit the model E(y) = L%*%f(x) where f is a smooth function.
## The summation convention is used to evaluate smooth at each value
## in matrix X to get matrix F, say. Then rowSum(L*F) gives E(y).

## create matrix of eval points for each function. Note that
## `smoothCon' is smart and will recognize the duplication...
X <- matrix(x,200,100,byrow=TRUE)

b <- gam(y~s(X,by=L,k=20))
par(mfrow=c(1,1))
plot(b,shade=TRUE);lines(x,f,col=2)

```

logLik.gam

Log likelihood for a fitted GAM, for AIC

Description

Function to extract the log-likelihood for a fitted gam model (note that the models are usually fitted by penalized likelihood maximization). Used by [AIC](#).

Usage

```

## S3 method for class 'gam'
logLik(object,...)

```

Arguments

object	fitted model objects of class gam as produced by gam().
...	un-used in this case

Details

Modification of logLik.glm which corrects the degrees of freedom for use with gam objects.

The function is provided so that [AIC](#) functions correctly with gam objects, and uses the appropriate degrees of freedom (accounting for penalization). Note, when using AIC for penalized models, that

the degrees of freedom are the effective degrees of freedom and not the number of parameters, and the model maximizes the penalized likelihood, not the actual likelihood. (See e.g. Hastie and Tibshirani, 1990, section 6.8.3 and also Wood 2008),

By default this routine uses a definition of the effective degrees of freedom that includes smoothing parameter uncertainty, if this is available (i.e. if smoothing parameter selection is by some variety of marginal likelihood).

Value

Standard logLik object: see [logLik](#).

Author(s)

Simon N. Wood <simon.wood@r-project.org> based directly on `logLik.glm`

References

Hastie and Tibshirani, 1990, Generalized Additive Models.

Wood, S.N. (2008) Fast stable direct fitting and smoothness selection for generalized additive models. *J.R.Statist. Soc. B* 70(3):495-518

See Also

[AIC](#)

<code>ls.size</code>	<i>Size of list elements</i>
----------------------	------------------------------

Description

Produces a named array giving the size, in bytes, of the elements of a list.

Usage

```
ls.size(x)
```

Arguments

`x` A list.

Value

A numeric vector giving the size in bytes of each element of the list `x`. The elements of the array have the same names as the elements of the list. If `x` is not a list then its size in bytes is returned, un-named.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
library(mgcv)
b <- list(M=matrix(runif(100),10,10),quote=
"The world is ruled by idiots because only an idiot would want to rule the world.",
fam=binomial())
ls.size(b)
```

magic

Stable Multiple Smoothing Parameter Estimation by GCV or UBRE

Description

Function to efficiently estimate smoothing parameters in generalized ridge regression problems with multiple (quadratic) penalties, by GCV or UBRE. The function uses Newton's method in multi-dimensions, backed up by steepest descent to iteratively adjust the smoothing parameters for each penalty (one penalty may have a smoothing parameter fixed at 1).

For maximal numerical stability the method is based on orthogonal decomposition methods, and attempts to deal with numerical rank deficiency gracefully using a truncated singular value decomposition approach.

Usage

```
magic(y,X,sp,S,off,L=NULL,lsp0=NULL,rank=NULL,H=NULL,C=NULL,
w=NULL,gamma=1,scale=1,gcv=TRUE,ridge.parameter=NULL,
control=list(tol=1e-6,step.half=25,rank.tol=
.Machine$double.eps^0.5),extra.rss=0,n.score=length(y),nthreads=1)
```

Arguments

y	is the response data vector.
X	is the model matrix (more columns than rows are allowed).
sp	is the array of smoothing parameters. The vector $L\%*\% \log(sp) + lsp0$ contains the logs of the smoothing parameters that actually multiply the penalty matrices stored in S (L is taken as the identity if NULL). Any sp values that are negative are autoinitialized, otherwise they are taken as supplying starting values. A supplied starting value will be reset to a default starting value if the gradient of the GCV/UBRE score is too small at the supplied value.

S	is a list of of penalty matrices. $S[[i]]$ is the i th penalty matrix, but note that it is not stored as a full matrix, but rather as the smallest square matrix including all the non-zero elements of the penalty matrix. Element 1,1 of $S[[i]]$ occupies element $off[i]$, $off[i]$ of the i th penalty matrix. Each $S[[i]]$ must be positive semi-definite. Set to <code>list()</code> if there are no smoothing parameters to be estimated.
off	is an array indicating the first parameter in the parameter vector that is penalized by the penalty involving $S[[i]]$.
L	is a matrix mapping $\log(sp)$ to the log smoothing parameters that actually multiply the penalties defined by the elems of S. Taken as the identity, if NULL. See above under sp.
lsp0	If L is not NULL this is a vector of constants in the linear transformation from $\log(sp)$ to the actual log smoothing parameters. So the logs of the smoothing parameters multiplying the $S[[i]]$ are given by $L\%*\log(sp) + lsp0$. Taken as 0 if NULL.
rank	is an array specifying the ranks of the penalties. This is useful, but not essential, for forming square roots of the penalty matrices.
H	is the optional offset penalty - i.e. a penalty with a smoothing parameter fixed at 1. This is useful for allowing regularization of the estimation process, fixed smoothing penalties etc.
C	is the optional matrix specifying any linear equality constraints on the fitting problem. If \mathbf{b} is the parameter vector then the parameters are forced to satisfy $\mathbf{Cb} = \mathbf{0}$.
w	the regression weights. If this is a matrix then it is taken as being the square root of the inverse of the covariance matrix of y , specifically $\mathbf{V}_y^{-1} = \mathbf{w}'\mathbf{w}$. If w is an array then it is taken as the diagonal of this matrix, or simply the weight for each element of y . See below for an example using this.
gamma	is an inflation factor for the model degrees of freedom in the GCV or UBRE score.
scale	is the scale parameter for use with UBRE.
gcv	should be set to TRUE if GCV is to be used, FALSE for UBRE.
ridge.parameter	It is sometimes useful to apply a ridge penalty to the fitting problem, penalizing the parameters in the constrained space directly. Setting this parameter to a value greater than zero will cause such a penalty to be used, with the magnitude given by the parameter value.
control	is a list of iteration control constants with the following elements: tol The tolerance to use in judging convergence. step.half If a trial step fails then the method tries halving it up to a maximum of <code>step.half</code> times. rank.tol is a constant used to test for numerical rank deficiency of the problem. Basically any singular value less than <code>rank_tol</code> multiplied by the largest singular value of the problem is set to zero.

extra.rss	is a constant to be added to the residual sum of squares (squared norm) term in the calculation of the GCV, UBRE and scale parameter estimate. In conjunction with n.score, this is useful for certain methods for dealing with very large data sets.
n.score	number to use as the number of data in GCV/UBRE score calculation: usually the actual number of data, but there are methods for dealing with very large datasets that change this.
nthreads	magic can make use of multiple threads if this is set to >1.

Details

The method is a computationally efficient means of applying GCV or UBRE (often approximately AIC) to the problem of smoothing parameter selection in generalized ridge regression problems of the form:

$$\text{minimise } \|\mathbf{W}(\mathbf{X}\mathbf{b} - \mathbf{y})\|^2 + \mathbf{b}'\mathbf{H}\mathbf{b} + \sum_{i=1}^m \theta_i \mathbf{b}'\mathbf{S}_i \mathbf{b}$$

possibly subject to constraints $\mathbf{C}\mathbf{b} = \mathbf{0}$. \mathbf{X} is a design matrix, \mathbf{b} a parameter vector, \mathbf{y} a data vector, \mathbf{W} a weight matrix, \mathbf{S}_i a positive semi-definite matrix of coefficients defining the i th penalty with associated smoothing parameter θ_i , \mathbf{H} is the positive semi-definite offset penalty matrix and \mathbf{C} a matrix of coefficients defining any linear equality constraints on the problem. \mathbf{X} need not be of full column rank.

The θ_i are chosen to minimize either the GCV score:

$$V_g = \frac{n\|\mathbf{W}(\mathbf{y} - \mathbf{A}\mathbf{y})\|^2}{[\text{tr}(\mathbf{I} - \gamma\mathbf{A})]^2}$$

or the UBRE score:

$$V_u = \|\mathbf{W}(\mathbf{y} - \mathbf{A}\mathbf{y})\|^2/n - 2\phi\text{tr}(\mathbf{I} - \gamma\mathbf{A})/n + \phi$$

where γ is gamma the inflation factor for degrees of freedom (usually set to 1) and ϕ is scale, the scale parameter. \mathbf{A} is the hat matrix (influence matrix) for the fitting problem (i.e the matrix mapping data to fitted values). Dependence of the scores on the smoothing parameters is through \mathbf{A} .

The method operates by Newton or steepest descent updates of the logs of the θ_i . A key aspect of the method is stable and economical calculation of the first and second derivatives of the scores w.r.t. the log smoothing parameters. Because the GCV/UBRE scores are flat w.r.t. very large or very small θ_i , it's important to get good starting parameters, and to be careful not to step into a flat region of the smoothing parameter space. For this reason the algorithm rescales any Newton step that would result in a $\log(\theta_i)$ change of more than 5. Newton steps are only used if the Hessian of the GCV/UBRE is positive definite, otherwise steepest descent is used. Similarly steepest descent is used if the Newton step has to be contracted too far (indicating that the quadratic model underlying Newton is poor). All initial steepest descent steps are scaled so that their largest component is 1. However a step is calculated, it is never expanded if it is successful (to avoid flat portions of the objective), but steps are successively halved if they do not decrease the GCV/UBRE score, until they do, or the direction is deemed to have failed. (Given the smoothing parameters the optimal \mathbf{b} parameters are easily found.)

The method is coded in C with matrix factorizations performed using LINPACK and LAPACK routines.

Value

The function returns a list with the following items:

<code>b</code>	The best fit parameters given the estimated smoothing parameters.
<code>scale</code>	the estimated (GCV) or supplied (UBRE) scale parameter.
<code>score</code>	the minimized GCV or UBRE score.
<code>sp</code>	an array of the estimated smoothing parameters.
<code>sp.full</code>	an array of the smoothing parameters that actually multiply the elements of S (same as <code>sp</code> if L was <code>NULL</code>). This is $\exp(L \times \log(sp))$.
<code>rV</code>	a factored form of the parameter covariance matrix. The (Bayesian) covariance matrix of the parameters b is given by $rV \%*\% t(rV) * scale$.
<code>gcv.info</code>	is a list of information about the performance of the method with the following elements: <ul style="list-style-type: none"> full.rank The apparent rank of the problem: number of parameters less number of equality constraints. rank The estimated actual rank of the problem (at the final iteration of the method). fully.converged is TRUE if the method converged by satisfying the convergence criteria, and FALSE if it covered by failing to decrease the score along the search direction. hess.pos.def is TRUE if the hessian of the UBRE or GCV score was positive definite at convergence. iter is the number of Newton/Steepest descent iterations taken. score.calls is the number of times that the GCV/UBRE score had to be evaluated. rms.grad is the root mean square of the gradient of the UBRE/GCV score w.r.t. the smoothing parameters. R The factor R from the QR decomposition of the weighted model matrix. This is un-pivoted so that column order corresponds to X. So it may not be upper triangular.

Note that some further useful quantities can be obtained using `magic.post.proc`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2004) Stable and efficient multiple smoothing parameter estimation for generalized additive models. *J. Amer. Statist. Ass.* 99:673-686

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[magic.post.proc.gam](#)

Examples

```

## Use `magic` for a standard additive model fit ...
library(mgcv)
set.seed(1);n <- 200;sig <- 1
dat <- gamSim(1,n=n,scale=sig)
k <- 30
## set up additive model
G <- gam(y~s(x0,k=k)+s(x1,k=k)+s(x2,k=k)+s(x3,k=k),fit=FALSE,data=dat)
## fit using magic (and gam default tolerance)
mgfit <- magic(G$y,G$X,G$sp,G$S,G$off,rank=G$rank,
              control=list(tol=1e-7,step.half=15))
## and fit using gam as consistency check
b <- gam(G=G)
mgfit$sp;b$sp # compare smoothing parameter estimates
edf <- magic.post.proc(G$X,mgfit,G$w)$edf # get e.d.f. per param
range(edf-b$edf) # compare

## p>n example... fit model to first 100 data only, so more
## params than data...

mgfit <- magic(G$y[1:100],G$X[1:100,],G$sp,G$S,G$off,rank=G$rank)
edf <- magic.post.proc(G$X[1:100,],mgfit,G$w[1:100])$edf

## constrain first two smooths to have identical smoothing parameters
L <- diag(3);L <- rbind(L[,1],L)
mgfit <- magic(G$y,G$X,rep(-1,3),G$S,G$off,L=L,rank=G$rank,C=G$C)

## Now a correlated data example ...
library(nlme)
## simulate truth
set.seed(1);n<-400;sig<-2
x <- 0:(n-1)/(n-1)
f <- 0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10
## produce scaled covariance matrix for AR1 errors...
V <- corMatrix(Initialize(corAR1(.6),data.frame(x=x)))
Cv <- chol(V) # t(Cv)%*%Cv=V
## Simulate AR1 errors ...
e <- t(Cv)%*%rnorm(n,0,sig) # so cov(e) = V * sig^2
## Observe truth + AR1 errors
y <- f + e
## GAM ignoring correlation
par(mfrow=c(1,2))
b <- gam(y~s(x,k=20))
plot(b);lines(x,f-mean(f),col=2);title("Ignoring correlation")
## Fit smooth, taking account of *known* correlation...
w <- solve(t(Cv)) # V^{-1} = w'w
## Use `gam` to set up model for fitting...
G <- gam(y~s(x,k=20),fit=FALSE)
## fit using magic, with weight *matrix*
mgfit <- magic(G$y,G$X,G$sp,G$S,G$off,rank=G$rank,C=G$C,w=w)
## Modify previous gam object using new fit, for plotting...
mg.stuff <- magic.post.proc(G$X,mgfit,w)

```

```
b$edf <- mg.stuff$edf;b$Vp <- mg.stuff$Vb
b$coefficients <- mgfit$b
plot(b);lines(x,f-mean(f),col=2);title("Known correlation")
```

magic.post.proc

Auxilliary information from magic fit

Description

Obtains Bayesian parameter covariance matrix, frequentist parameter estimator covariance matrix, estimated degrees of freedom for each parameter and leading diagonal of influence/hat matrix, for a penalized regression estimated by `magic`.

Usage

```
magic.post.proc(X,object,w=NULL)
```

Arguments

<code>X</code>	is the model matrix.
<code>object</code>	is the list returned by <code>magic</code> after fitting the model with model matrix <code>X</code> .
<code>w</code>	is the weight vector used in fitting, or the weight matrix used in fitting (i.e. supplied to <code>magic</code> , if one was.). If <code>w</code> is a vector then its elements are typically proportional to reciprocal variances (but could even be negative). If <code>w</code> is a matrix then <code>t(w)%*%w</code> should typically give the inverse of the covariance matrix of the response data supplied to <code>magic</code> .

Details

`object` contains rV (\mathbf{V} , say), and $scale$ (ϕ , say) which can be used to obtain the require quantities as follows. The Bayesian covariance matrix of the parameters is $\mathbf{V}\mathbf{V}'\phi$. The vector of estimated degrees of freedom for each parameter is the leading diagonal of $\mathbf{V}\mathbf{V}'\mathbf{X}'\mathbf{W}'\mathbf{W}\mathbf{X}$ where \mathbf{W} is either the weight matrix `w` or the matrix `diag(w)`. The hat/influence matrix is given by $\mathbf{W}\mathbf{X}\mathbf{V}\mathbf{V}'\mathbf{X}'\mathbf{W}'$.

The frequentist parameter estimator covariance matrix is $\mathbf{V}\mathbf{V}'\mathbf{X}'\mathbf{W}'\mathbf{W}\mathbf{X}\mathbf{V}\mathbf{V}'\phi$: it is sometimes useful for testing terms for equality to zero.

Value

A list with three items:

<code>Vb</code>	the Bayesian covariance matrix of the model parameters.
<code>Ve</code>	the frequentist covariance matrix for the parameter estimators.
<code>hat</code>	the leading diagonal of the hat (influence) matrix.
<code>edf</code>	the array giving the estimated degrees of freedom associated with each parameter.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[magic](#)

mgcv.FAQ

Frequently Asked Questions for package mgcv

Description

This page provides answers to some of the questions that get asked most often about mgcv

FAQ list

1. **How can I compare gamm models?** In the identity link normal errors case, then AIC and hypothesis testing based methods are fine. Otherwise it is best to work out a strategy based on the [summary.gam](#). Alternatively, simple random effects can be fitted with [gam](#), which makes comparison straightforward. Package [gamm4](#) is an alternative, which allows AIC type model selection for generalized models.
2. **How do I get the equation of an estimated smooth?** This slightly misses the point of semi-parametric modelling: the idea is that we estimate the form of the function from data without assuming that it has a particular simple functional form. Of course for practical computation the functions do have underlying mathematical representations, but they are not very helpful, when written down. If you do need the functional forms then see chapter 4 of Wood (2006). However for most purposes it is better to use [predict.gam](#) to evaluate the function for whatever argument values you need. If derivatives are required then the simplest approach is to use finite differencing (which also allows SEs etc to be calculated).
3. **Some of my smooths are estimated to be straight lines and their confidence intervals vanish at some point in the middle. What is wrong?** Nothing. Smooths are subject to sum-to-zero identifiability constraints. If a smooth is estimated to be a straight line then it consequently has one degree of freedom, and there is no choice about where it passes through zero — so the CI must vanish at that point.
4. **How do I test whether a smooth is significantly different from a straight line.** See [tprs](#) and the example therein.
5. **An example from an mgcv helpfile gives an error - is this a bug?** It might be, but first please check that the version of mgcv you have loaded into R corresponds to the version from which the helpfile came. Many such problems are caused by trying to run code only supported in a later mgcv version in an earlier version. Another possibility is that you have an object loaded whose name clashes with an mgcv function (for example you are trying to use the `mgcv.multinom` function, but have another object called `multinom` loaded.)

6. **Some code from Wood (2006) causes an error: why?** The book was written using mgcv version 1.3. To allow for REML estimation of smoothing parameters in versions 1.5, some changes had to be made to the syntax. In particular the function `gam.method` no longer exists. The smoothness selection method (GCV, REML etc) is now controlled by the `method` argument to `gam` while the optimizer is selected using the `optimizer` argument. See `gam` and <http://www.maths.bris.ac.uk/~sw15190/igam/index.html> for details.
7. **Why is a model object saved under a previous mgcv version not usable with the current mgcv version?** I'm sorry about this issue, I know it's really annoying. Here's my defence. Each mgcv version is run through an extensive test suite before release, to ensure that it gives the same results as before, unless there are good statistical reasons why not (e.g. improvements to p-value approximation, fixing of an error). However it is sometimes necessary to modify the internal structure of model objects in a way that makes an old style object unusable with a newer version. For example, bug fixes or new R features sometimes require changes in the way that things are computed which in turn require modification of the object structure. Similarly improvements, such as the ability to compute smoothing parameters by RE/ML require object level changes. The only fix to this problem is to access the old object using the original mgcv version (available on CRAN), or to recompute the fit using the current mgcv version.
8. **When using `gamm` or `gamm4`, the reported AIC is different for the `gam` object and the `lme` or `lmer` object. Why is this?** There are several reasons for this. The most important is that the models being used are actually different in the two representations. When treating the GAM as a mixed model, you are implicitly assuming that if you gathered a replicate dataset, the smooths in your model would look completely different to the smooths from the original model, except for having the same degree of smoothness. Technically you would expect the smooths to be drawn afresh from their distribution under the random effects model. When viewing the `gam` from the usual penalized regression perspective, you would expect smooths to look broadly similar under replication of the data. i.e. you are really using Bayesian model for the smooths, rather than a random effects model (it's just that the frequentist random effects and Bayesian computations happen to coincide for computing the estimates). As a result of the different assumptions about the data generating process, AIC model comparisons can give rather different answers depending on the model adopted. Which you use should depend on which model you really think is appropriate. In addition the computations of the AICs are different. The mixed model AIC uses the marginal likelihood and the corresponding number of model parameters. The `gam` model uses the penalized likelihood and the effective degrees of freedom.
9. **What does 'mgcv' stand for?** 'Mixed GAM Computation Vehicle', is my current best effort (let me know if you can do better). Originally it stood for 'Multiple GCV', which has long since ceased to be usefully descriptive, (and I can't really change 'mgcv' now without causing disruption). On a bad inbox day 'Mad GAM Computing Vulture'.
10. **My new method is failing to beat mgcv, what can I do?** If speed is the problem, then make sure that you use the slowest basis possible ("tp") with a large sample size, and experiment with different optimizers to find one that is slow for your problem. For prediction error/MSE, then leaving the smoothing basis dimensions at their arbitrary defaults, when these are inappropriate for the problem setting, is a good way of reducing performance. Similarly, using p-splines in place of derivative penalty based splines will often shave a little more from the performance here. Unlike REML/ML, prediction error based smoothness selection criteria such as Mallows Cp and GCV often produce a small proportion of severe overfits, so careful choice of smoothness selection method can help further. In particular GCV etc. usually result in worse confidence interval and p-value performance than ML or REML. If all this fails, try

using a really odd simulation setup for which mgcv is clearly not suited: for example poor performance is almost guaranteed for small noisy datasets with large numbers of predictors.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

mgcv . package

Mixed GAM Computation Vehicle with GCV/AIC/REML smoothness estimation and GAMMs by REML/PQL

Description

mgcv provides functions for generalized additive modelling ([gam](#) and [bam](#)) and generalized additive mixed modelling ([gamm](#), and [random.effects](#)). The term GAM is taken to include any model dependent on unknown smooth functions of predictors and estimated by quadratically penalized (possibly quasi-) likelihood maximization. Available distributions are covered in [family.mgcv](#) and available smooths in [smooth.terms](#).

Particular features of the package are facilities for automatic smoothness selection (Wood, 2004, 2011), and the provision of a variety of smooths of more than one variable. User defined smooths can be added. A Bayesian approach to confidence/credible interval calculation is provided. Linear functionals of smooths, penalization of parametric model terms and linkage of smoothing parameters are all supported. Lower level routines for generalized ridge regression and penalized linearly constrained least squares are also available.

Details

mgcv provides generalized additive modelling functions [gam](#), [predict.gam](#) and [plot.gam](#), which are very similar in use to the S functions of the same name designed by Trevor Hastie (with some extensions). However the underlying representation and estimation of the models is based on a penalized regression spline approach, with automatic smoothness selection. A number of other functions such as [summary.gam](#) and [anova.gam](#) are also provided, for extracting information from a fitted [gamObject](#).

Use of [gam](#) is much like use of [glm](#), except that within a gam model formula, isotropic smooths of any number of predictors can be specified using [s](#) terms, while scale invariant smooths of any number of predictors can be specified using [te](#), [ti](#) or [t2](#) terms. [smooth.terms](#) provides an overview of the built in smooth classes, and [random.effects](#) should be referred to for an overview of random effects terms (see also [mrf](#) for Markov random fields). Estimation is by penalized likelihood or quasi-likelihood maximization, with smoothness selection by GCV, GACV, gAIC/UBRE or (RE)ML. See [gam](#), [gam.models](#), [linear.functional.terms](#) and [gam.selection](#) for some discussion of model specification and selection. For detailed control of fitting see [gam.convergence](#), [gam](#) arguments method and optimizer and [gam.control](#). For checking and visualization see [gam.check](#),

[choose.k](#), [vis.gam](#) and [plot.gam](#). While a number of types of smoother are built into the package, it is also extendable with user defined smooths, see [smooth.construct](#), for example.

A Bayesian approach to smooth modelling is used to derive standard errors on predictions, and hence credible intervals (see Marra and Wood, 2012). The Bayesian covariance matrix for the model coefficients is returned in `Vp` of the `gamObject`. See [predict.gam](#) for examples of how this can be used to obtain credible regions for any quantity derived from the fitted model, either directly, or by direct simulation from the posterior distribution of the model coefficients. Approximate p-values can also be obtained for testing individual smooth terms for equality to the zero function, using similar ideas (see Wood, 2013a,b). Frequentist approximations can be used for hypothesis testing based model comparison. See [anova.gam](#) and [summary.gam](#) for more on hypothesis testing.

For large datasets (that is large `n`) see [bam](#) which is a version of [gam](#) with a much reduced memory footprint.

The package also provides a generalized additive mixed modelling function, [gamm](#), based on a PQL approach and `lme` from the `nlme` library (for an `lme4` based version, see package `gamm4`). [gamm](#) is particularly useful for modelling correlated data (i.e. where a simple independence model for the residual variation is inappropriate). In addition, low level routine [magic](#) can fit models to data with a known correlation structure.

Some underlying GAM fitting methods are available as low level fitting functions: see [magic](#). But there is little functionality that can not be more conveniently accessed via [gam](#). Penalized weighted least squares with linear equality and inequality constraints is provided by [pcls](#).

For a complete list of functions type `library(help=mgcv)`. See also [mgcv.FAQ](#).

Author(s)

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Part funded by EPSRC: EP/K005251/1

References

These provide details for the underlying `mgcv` methods, and fuller references to the large literature on which the methods are based.

Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36

Wood, S.N. (2004) Stable and efficient multiple smoothing parameter estimation for generalized additive models. *J. Amer. Statist. Ass.* 99:673-686.

Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. *Scandinavian Journal of Statistics*, 39(1), 53-74.

Wood, S.N. (2013a) A simple test for random effects in regression models. *Biometrika* 100:1005-1010

Wood, S.N. (2013b) On p-values for smooth components of an extended generalized additive model. *Biometrika* 100:221-228

Wood, S.N. (2006) *Generalized Additive Models: an introduction with R*, CRC

Development of mgcv version 1.8 was part funded by EPSRC grants EP/K005251/1 and EP/I000917/1.

Examples

```
## see examples for gam and gamm
```

mgcv.parallel	<i>Parallel computation in mgcv.</i>
---------------	--------------------------------------

Description

mgcv can make some use of multiple cores or a cluster.

`bam` can use an openMP based parallelization approach alongside discretisation of covariates to achieve substantial speed ups. This is selected using the `discrete=TRUE` option to `bam`, with the number of threads controlled via the `nthreads` argument. This is the approach that scales best. See example below.

Alternatively, function `bam` can use the facilities provided in the `parallel` package. See examples below. Note that most multi-core machines are memory bandwidth limited, so parallel speed up tends to be rather variable.

Function `gam` can use parallel threads on a (shared memory) multi-core machine via openMP (where this is supported). To do this, set the desired number of threads by setting `nthreads` to the number of cores to use, in the `control` argument of `gam`. Note that, for the most part, only the dominant $O(np^2)$ steps are parallelized (n is number of data, p number of parameters). For additive Gaussian models estimated by GCV, the speed up can be disappointing as these employ an $O(p^3)$ SVD step that can also have substantial cost in practice.

`magic` can also use multiple cores, but the same comments apply as for the GCV Gaussian additive model.

If `control$nthreads` is set to more than the number of cores detected, then only the number of detected cores is used. Note that using virtual cores usually gives very little speed up, and can even slow computations slightly. For example, many Intel processors reporting 4 cores actually have 2 physical cores, each with 2 virtual cores, so using 2 threads gives a marked increase in speed, while using 4 threads makes little extra difference.

Note that on Intel and similar processors the maximum performance is usually achieved by disabling Hyper-Threading in BIOS, and then setting the number of threads to the number of physical cores used. This prevents the operating system scheduler from sending 2 floating point intensive threads to the same physical core, where they have to share a floating point unit (and cache) and therefore slow each other down. The scheduler tends to do this under the manager - worker multi-threading approach used in mgcv, since the manager thread looks very busy up to the point at which the workers are set to work, and at the point of scheduling the scheduler has no way of knowing that the manager thread actually has nothing more to do until the workers are finished. If you are working on a many cored platform where you can not disable hyper-threading then it may be worth setting

the number of threads to one less than the number of physical cores, to reduce the frequency of such scheduling problems.

mgcv's work splitting always makes the simple assumption that all your cores are equal, and you are not sharing them with other floating point intensive threads.

In addition to hyper-threading several features may lead to apparently poor scaling. The first is that many CPUs have a Turbo mode, whereby a few cores can be run at higher frequency, provided the overall power used by the CPU does not exceed design limits, however it is not possible for all cores on the CPU to run at this frequency. So as you add threads eventually the CPU frequency has to be reduced below the Turbo frequency, with the result that you don't get the expected speed up from adding cores. Secondly, most modern CPUs have their frequency set dynamically according to load. You may need to set the system power management policy to favour high performance in order to maximize the chance that all threads run at the speed you were hoping for (you can turn off dynamic power control in BIOS, but then you turn off the possibility of Turbo also).

Because the computational burden in mgcv is all in the linear algebra, then parallel computation may provide reduced or no benefit with a tuned BLAS. This is particularly the case if you are using a multi threaded BLAS, but a BLAS that is tuned to make efficient use of a particular cache size may also experience loss of performance if threads have to share the cache.

Author(s)

Simon Wood <simon.wood@r-project.org>

References

<https://computing.llnl.gov/tutorials/openMP/>

Examples

```
## illustration of multi-threading with gam...

require(mgcv);set.seed(9)
dat <- gamSim(1,n=2000,dist="poisson",scale=.1)
k <- 12;bs <- "cr";ctrl <- list(nthreads=2)

system.time(b1<-gam(y~s(x0,bs=bs)+s(x1,bs=bs)+s(x2,bs=bs,k=k)
  ,family=poisson,data=dat,method="REML"))[3]

system.time(b2<-gam(y~s(x0,bs=bs)+s(x1,bs=bs)+s(x2,bs=bs,k=k),
  family=poisson,data=dat,method="REML",control=ctrl))[3]

## Poisson example on a cluster with 'bam'.
## Note that there is some overhead in initializing the
## computation on the cluster, associated with loading
## the Matrix package on each node. For this reason the
## sample sizes here are very small to keep CRAN happy, but at
## this low sample size you see little advantage of parallel computation.

k <- 13
dat <- gamSim(1,n=6000,dist="poisson",scale=.1)
require(parallel)
```

```

nc <- 2  ## cluster size, set for example portability
if (detectCores()>1) { ## no point otherwise
  cl <- makeCluster(nc)
  ## could also use makeForkCluster, but read warnings first!
} else cl <- NULL

system.time(b3 <- bam(y ~ s(x0,bs=bs,k=7)+s(x1,bs=bs,k=7)+s(x2,bs=bs,k=k)
  ,data=dat,family=poisson(),chunk.size=5000,cluster=cl))

fv <- predict(b3,cluster=cl) ## parallel prediction

if (!is.null(cl)) stopCluster(cl)
b3

## Alternative using the discrete option with bam...

system.time(b4 <- bam(y ~ s(x0,bs=bs,k=7)+s(x1,bs=bs,k=7)+s(x2,bs=bs,k=k)
  ,data=dat,family=poisson(),discrete=TRUE,nthreads=2))

```

missing.data

Missing data in GAMs

Description

If there are missing values in the response or covariates of a GAM then the default is simply to use only the ‘complete cases’. If there are many missing covariates, this can get rather wasteful. One possibility is then to use imputation. Another is to substitute a simple random effects model in which the by variable mechanism is used to set $s(x)$ to zero for any missing x , while a Gaussian random effect is then substituted for the ‘missing’ $s(x)$. See the example for details of how this works, and [gam.models](#) for the necessary background on by variables.

Author(s)

Simon Wood <simon.wood@r-project.org>

See Also

[gam.vcomp](#), [gam.models](#), [s](#), [smooth.construct.re.smooth.spec](#), [gam](#)

Examples

```

## The example takes a couple of minutes to run, so is marked
## don't run to save CRAN time.
## Not run:
require(mgcv)
par(mfrow=c(4,4),mar=c(4,4,1,1))
for (sim in c(1,7)) { ## cycle over uncorrelated and correlated covariates
  n <- 350;set.seed(2)

```

```

## simulate data but randomly drop 300 covariate measurements
## leaving only 50 complete cases...
dat <- gamSim(sim,n=n,scale=3) ## 1 or 7
drop <- sample(1:n,300) ## to
for (i in 2:5) dat[drop[1:75+(i-2)*75],i] <- NA

## process data.frame producing binary indicators of missingness,
## mx0, mx1 etc. For each missing value create a level of a factor
## idx0, idx1, etc. So idx0 has as many levels as x0 has missing
## values. Replace the NA's in each variable by the mean of the
## non missing for that variable...

dname <- names(dat)[2:5]
dat1 <- dat
for (i in 1:4) {
  by.name <- paste("m",dname[i],sep="")
  dat1[[by.name]] <- is.na(dat1[[dname[i]]])
  dat1[[dname[i]]][dat1[[by.name]]] <- mean(dat1[[dname[i]]],na.rm=TRUE)
  lev <- rep(1,n);lev[dat1[[by.name]]] <- 1:sum(dat1[[by.name]])
  id.name <- paste("id",dname[i],sep="")
  dat1[[id.name]] <- factor(lev)
  dat1[[by.name]] <- as.numeric(dat1[[by.name]])
}

## Fit a gam, in which any missing value contributes zero
## to the linear predictor from its smooth, but each
## missing has its own random effect, with the random effect
## variances being specific to the variable. e.g.
## for s(x0,by=ordered(!mx0)), declaring the `by' as an ordered
## factor ensures that the smooth is centred, but multiplied
## by zero when mx0 is one (indicating a missing x0). This means
## that any value (within range) can be put in place of the
## NA for x0. s(idx0,bs="re",by=mx0) produces a separate Gaussian
## random effect for each missing value of x0 (in place of s(x0),
## effectively). The `by' variable simply sets the random effect to
## zero when x0 is non-missing, so that we can set idx0 to any
## existing level for these cases.

b <- gam(y~s(x0,by=ordered(!mx0))+s(x1,by=ordered(!mx1))+
  s(x2,by=ordered(!mx2))+s(x3,by=ordered(!mx3))+
  s(idx0,bs="re",by=mx0)+s(idx1,bs="re",by=mx1)+
  s(idx2,bs="re",by=mx2)+s(idx3,bs="re",by=mx3)
  ,data=dat1,method="REML")

for (i in 1:4) plot(b,select=i) ## plot the smooth effects from b

## fit the model to the `complete case' data...
b2 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="REML")
plot(b2) ## plot the complete case results
}

## End(Not run)

```

model.matrix.gam *Extract model matrix from GAM fit*

Description

Obtains the model matrix from a fitted gam object.

Usage

```
## S3 method for class 'gam'  
model.matrix(object, ...)
```

Arguments

object fitted model object of class gam as produced by gam().
... other arguments, passed to [predict.gam](#).

Details

Calls [predict.gam](#) with no newdata argument and type="lpmatrix" in order to obtain the model matrix of object.

Value

A model matrix.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006b) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

See Also

[gam](#)

Examples

```
require(mgcv)  
n <- 15  
x <- runif(n)  
y <- sin(x*2*pi) + rnorm(n)*.2  
mod <- gam(y~s(x,bs="cc",k=6),knots=list(x=seq(0,1,length=6)))  
model.matrix(mod)
```

mono.con

*Monotonicity constraints for a cubic regression spline***Description**

Finds linear constraints sufficient for monotonicity (and optionally upper and/or lower boundedness) of a cubic regression spline. The basis representation assumed is that given by the gam, "cr" basis: that is the spline has a set of knots, which have fixed x values, but the y values of which constitute the parameters of the spline.

Usage

```
mono.con(x, up=TRUE, lower=NA, upper=NA)
```

Arguments

x	The array of knot locations.
up	If TRUE then the constraints imply increase, if FALSE then decrease.
lower	This specifies the lower bound on the spline unless it is NA in which case no lower bound is imposed.
upper	This specifies the upper bound on the spline unless it is NA in which case no upper bound is imposed.

Details

Consider the natural cubic spline passing through the points $\{x_i, p_i : i = 1 \dots n\}$. Then it is possible to find a relatively small set of linear constraints on \mathbf{p} sufficient to ensure monotonicity (and bounds if required): $\mathbf{A}\mathbf{p} \geq \mathbf{b}$. Details are given in Wood (1994).

Value

a list containing constraint matrix A and constraint vector b.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Gill, P.E., Murray, W. and Wright, M.H. (1981) *Practical Optimization*. Academic Press, London.

Wood, S.N. (1994) Monotonic smoothing splines fitted by cross validation. *SIAM Journal on Scientific Computing* **15**(5), 1126–1133.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[magic](#), [pcls](#)

Examples

```
## see ?pcls
```

mroot

Smallest square root of matrix

Description

Find a square root of a positive semi-definite matrix, having as few columns as possible. Uses either pivoted choleski decomposition or singular value decomposition to do this.

Usage

```
mroot(A,rank=NULL,method="chol")
```

Arguments

A	The positive semi-definite matrix, a square root of which is to be found.
rank	if the rank of the matrix A is known then it should be supplied. NULL or <1 imply that it should be estimated.
method	"chol" to use pivoted choleski decompositon, which is fast but tends to over-estimate rank. "svd" to use singular value decomposition, which is slow, but is the most accurate way to estimate rank.

Details

The function uses SVD, or a pivoted Choleski routine. It is primarily of use for turning penalized regression problems into ordinary regression problems.

Value

A matrix, **B** with as many columns as the rank of **A**, and such that $\mathbf{A} = \mathbf{B}\mathbf{B}'$.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Examples

```
require(mgcv)
set.seed(0)
a <- matrix(runif(24),6,4)
A <- a%*%t(a) ## A is +ve semi-definite, rank 4
B <- mroot(A) ## default pivoted choleski method
tol <- 100*.Machine$double.eps
chol.err <- max(abs(A-B%*%t(B)));chol.err
if (chol.err>tol) warning("mroot (chol) suspect")
B <- mroot(A,method="svd") ## svd method
```



```
svd.err <- max(abs(A-B%*%t(B)));svd.err
if (svd.err>tol) warning("mroot (svd) suspect")
```

multinom

GAM multinomial logistic regression

Description

Family for use with `gam`, implementing regression for categorical response data. Categories must be coded 0 to K, where K is a positive integer. `gam` should be called with a list of K formulae, one for each category except category zero (extra formulae for shared terms may also be supplied: see `formula.gam`). The first formula also specifies the response variable.

Usage

```
multinom(K=1)
```

Arguments

K There are K+1 categories and K linear predictors.

Details

The model has K linear predictors, η_j , each dependent on smooth functions of predictor variables, in the usual way. If response variable, y, contains the class labels 0,...,K then the likelihood for $y>0$ is $\exp(\eta_y)/\{1 + \sum_j \exp(\eta_j)\}$. If $y=0$ the likelihood is $1/\{1 + \sum_j \exp(\eta_j)\}$. In the two class case this is just a binary logistic regression model. The implementation uses the approach to GAMLSS models described in Wood, Pya and Saefken (2016).

The residuals returned for this model are simply the square root of -2 times the deviance for each observation, with a positive sign if the observed y is the most probable class for this observation, and a negative sign otherwise.

Use `predict` with `type="response"` to get the predicted probabilities in each category.

Note that the model is not completely invariant to category relabelling, even if all linear predictors have the same form. Realistically this model is unlikely to be suitable for problems with large numbers of categories. Missing categories are not supported.

Value

An object of class `general.family`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

See Also

[ocat](#)

Examples

```
library(mgcv)
set.seed(6)
## simulate some data from a three class model
n <- 1000
f1 <- function(x) sin(3*pi*x)*exp(-x)
f2 <- function(x) x^3
f3 <- function(x) .5*exp(-x^2)-.2
f4 <- function(x) 1
x1 <- runif(n);x2 <- runif(n)
eta1 <- 2*(f1(x1) + f2(x2))-0.5
eta2 <- 2*(f3(x1) + f4(x2))-1
p <- exp(cbind(0,eta1,eta2))
p <- p/rowSums(p) ## prob. of each category
cp <- t(apply(p,1,cumsum)) ## cumulative prob.
## simulate multinomial response with these probabilities
## see also ?rmultinom
y <- apply(cp,1,function(x) min(which(x>runif(1))))-1
## plot simulated data...
plot(x1,x2,col=y+3)

## now fit the model...
b <- gam(list(y~s(x1)+s(x2),~s(x1)+s(x2)),family=multinom(K=2))
plot(b,pages=1)
gam.check(b)

## now a simple classification plot...
expand.grid(x1=seq(0,1,length=40),x2=seq(0,1,length=40)) -> gr
pp <- predict(b,newdata=gr,type="response")
pc <- apply(pp,1,function(x) which(max(x)==x)[1])-1
plot(gr,col=pc+3,pch=19)
```

Description

Family for use with `gam` implementing smooth multivariate Gaussian regression. The means for each dimension are given by a separate linear predictor, which may contain smooth components. Extra linear predictors may also be specified giving terms which are shared between components (see `formula.gam`). The Choleski factor of the response precision matrix is estimated as part of fitting.

Usage

```
mvn(d=2)
```

Arguments

`d` The dimension of the response (>1).

Details

The response is `d` dimensional multivariate normal, where the covariance matrix is estimated, and the means for each dimension have separate linear predictors. Model specification is via a list of `gam` like formulae - one for each dimension. See example.

Currently the family ignores any prior weights, and is implemented using first derivative information sufficient for BFGS estimation of smoothing parameters. "response" residuals give raw residuals, while "deviance" residuals are standardized to be approximately independent standard normal if all is well.

Value

An object of class `general.family`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

See Also

[gaussian](#)

Examples

```
library(mgcv)
## simulate some data...
V <- matrix(c(2,1,1,2),2,2)
f0 <- function(x) 2 * sin(pi * x)
f1 <- function(x) exp(2 * x)
```

```

f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
  (10 * x)^3 * (1 - x)^10
n <- 300
x0 <- runif(n); x1 <- runif(n);
x2 <- runif(n); x3 <- runif(n)
y <- matrix(0, n, 2)
for (i in 1:n) {
  mu <- c(f0(x0[i])+f1(x1[i]), f2(x2[i]))
  y[i,] <- rmvn(1, mu, V)
}
dat <- data.frame(y0=y[,1], y1=y[,2], x0=x0, x1=x1, x2=x2, x3=x3)

## fit model...

b <- gam(list(y0~s(x0)+s(x1), y1~s(x2)+s(x3)), family=mvn(d=2), data=dat)
b
summary(b)
plot(b, pages=1)
solve(crossprod(b$family$data$R)) ## estimated cov matrix

```

negbin

GAM negative binomial families

Description

The `gam` modelling function is designed to be able to use the `negbin` family (a modification of MASS library `negative.binomial` family by Venables and Ripley), or the `nb` function designed for integrated estimation of parameter θ . θ is the parameter such that $\text{var}(y) = \mu + \mu^2/\theta$, where $\mu = E(y)$.

Two approaches to estimating θ are available (with `gam` only):

- With `negbin` then if ‘performance iteration’ is used for smoothing parameter estimation (see `gam`), then smoothing parameters are chosen by GCV and θ is chosen in order to ensure that the Pearson estimate of the scale parameter is as close as possible to 1, the value that the scale parameter should have.
- If ‘outer iteration’ is used for smoothing parameter selection with the `nb` family then θ is estimated alongside the smoothing parameters by ML or REML.

To use the first option, set the `optimizer` argument of `gam` to “perf” (it can sometimes fail to converge).

Usage

```

negbin(theta = stop("'theta' must be specified"), link = "log")
nb(theta = NULL, link = "log")

```

Arguments

theta	Either i) a single value known value of theta or ii) two values of theta specifying the endpoints of an interval over which to search for theta (this is an option only for negbin). For nb then a positive supplied theta is treated as a fixed known parameter, otherwise it is estimated (the absolute value of a negative theta is taken as a starting value).
link	The link function: one of "log", "identity" or "sqrt"

Details

nb allows estimation of the theta parameter alongside the model smoothing parameters, but is only useable with `gam` (not `bam` or `gamm`).

For negbin, if a single value of theta is supplied then it is always taken as the known fixed value and this is useable with `bam` and `gamm`. If theta is two numbers (`theta[2]>theta[1]`) then they are taken as specifying the range of values over which to search for the optimal theta. This option should only be used with performance iteration estimation (see `gam` argument `optimizer`), in which case the method of estimation is to choose $\hat{\theta}$ so that the GCV (Pearson) estimate of the scale parameter is one (since the scale parameter is one for the negative binomial). In this case θ estimation is nested within the IRLS loop used for GAM fitting. After each call to fit an iteratively weighted additive model to the IRLS pseudodata, the θ estimate is updated. This is done by conditioning on all components of the current GCV/Pearson estimator of the scale parameter except θ and then searching for the $\hat{\theta}$ which equates this conditional estimator to one. The search is a simple bisection search after an initial crude line search to bracket one. The search will terminate at the upper boundary of the search region is a Poisson fit would have yielded an estimated scale parameter <1 .

Value

For negbin an object inheriting from class `family`, with additional elements

<code>dvar</code>	the function giving the first derivative of the variance function w.r.t. μ .
<code>d2var</code>	the function giving the second derivative of the variance function w.r.t. μ .
<code>getTheta</code>	A function for retrieving the value(s) of theta. This also useful for retrieving the estimate of theta after fitting (see example).

For nb an object inheriting from class `extended.family`.

WARNINGS

`gamm` and `bam` do not support theta estimation

The negative binomial functions from the MASS library are no longer supported.

Author(s)

Simon N. Wood <simon.wood@r-project.org> modified from Venables and Ripley's `negative.binomial` family.

References

Wood, S.N., N. Pya and B. Saeften (2016), Smoothing parameter and model selection for general smooth models. Journal of the American Statistical Association. <http://arxiv.org/abs/1511.03864>

Venables, B. and B.R. Ripley (2002) Modern Applied Statistics in S, Springer.

Examples

```
library(mgcv)
set.seed(3)
n<-400
dat <- gamSim(1,n=n)
g <- exp(dat$f/5)

## negative binomial data...
dat$y <- rnbinom(g,size=3,mu=g)
## known theta fit ...
b0 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=negbin(3),data=dat)
plot(b0,pages=1)
print(b0)

## same with theta estimation...
b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=nb(),data=dat)
plot(b,pages=1)
print(b)
b$family$getTheta(TRUE) ## extract final theta estimate

## unknown theta via performance iteration...
b1 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=negbin(c(1,10)),
          optimizer="perf",data=dat)
plot(b1,pages=1)
print(b1)

## another example...
set.seed(1)
f <- dat$f
f <- f - min(f)+5;g <- f^2/10
dat$y <- rnbinom(g,size=3,mu=g)
b2 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=nb(link="sqrt"),
          data=dat,method="REML")
plot(b2,pages=1)
print(b2)
rm(dat)
```

Description

`gamm` works by transforming a GAMM into something that can be estimated by `lme`, but this involves creating new variables, the names of which should not clash with the names of other variables on which the model depends. This simple service routine checks a suggested name against a list of those in use, and if necessary modifies it so that there is no clash.

Usage

```
new.name(proposed,old.names)
```

Arguments

proposed	a suggested name
old.names	An array of names that must not be duplicated

Value

A name that is not in `old.names`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gamm](#)

Examples

```
require(mgcv)
old <- c("a","tuba","is","tubby")
new.name("tubby",old)
```

Description

It is common practice in statistical optimization to use log-parameterizations when a parameter ought to be positive. i.e. if an optimization parameter a should be non-negative then we use $a=\exp(b)$ and optimize with respect to the unconstrained parameter b . This often works well, but it does imply a rather limited working range for b : using 8 byte doubles, for example, if b 's magnitude gets much above 700 then a overflows or underflows. This can cause problems for numerical optimization methods.

notExp is a monotonic function for mapping the real line into the positive real line with much less extreme underflow and overflow behaviour than exp. It is a piece-wise function, but is continuous to second derivative: see the source code for the exact definition, and the example below to see what it looks like.

notLog is the inverse function of notExp.

The major use of these functions was originally to provide more robust pdMat classes for lme for use by `gamm`. Currently the `notExp2` and `notLog2` functions are used in their place, as a result of changes to the nlme optimization routines.

Usage

```
notExp(x)
```

```
notLog(x)
```

Arguments

`x` Argument array of real numbers (notExp) or positive real numbers (notLog).

Value

An array of function values evaluated at the supplied argument values.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

`pdTens`, `pdIdnot`, `gamm`

Examples

```
## Illustrate the notExp function:
## less steep than exp, but still monotonic.
require(mgcv)
x <- -100:100/10
op <- par(mfrow=c(2,2))
```



```

plot(x,notExp(x),type="l")
lines(x,exp(x),col=2)
plot(x,log(notExp(x)),type="l")
lines(x,log(exp(x)),col=2) # redundancy intended
x <- x/4
plot(x,notExp(x),type="l")
lines(x,exp(x),col=2)
plot(x,log(notExp(x)),type="l")
lines(x,log(exp(x)),col=2) # redundancy intended
par(op)
range(notLog(notExp(x))-x) # show that inverse works!

```

notExp2

Alternative to log parameterization for variance components

Description

notLog2 and notExp2 are alternatives to log and exp or [notLog](#) and [notExp](#) for re-parameterization of variance parameters. They are used by the [pdTens](#) and [pdIdnot](#) classes which in turn implement smooths for [gamm](#).

The functions are typically used to ensure that smoothing parameters are positive, but the notExp2 is not monotonic: rather it cycles between ‘effective zero’ and ‘effective infinity’ as its argument changes. The notLog2 is the inverse function of the notExp2 only over an interval centered on zero.

Parameterizations using these functions ensure that estimated smoothing parameters remain positive, but also help to ensure that the likelihood is never indefinite: once a working parameter pushes a smoothing parameter below ‘effective zero’ or above ‘effective infinity’ the cyclic nature of the notExp2 causes the likelihood to decrease, where otherwise it might simply have flattened.

This parameterization is really just a numerical trick, in order to get lme to fit gamm models, without failing due to indefiniteness. Note in particular that asymptotic results on the likelihood/REML criterion are not invalidated by the trick, unless parameter estimates end up close to the effective zero or effective infinity: but if this is the case then the asymptotics would also have been invalid for a conventional monotonic parameterization.

This reparameterization was made necessary by some modifications to the underlying optimization method in lme introduced in nlme 3.1-62. It is possible that future releases will return to the [notExp](#) parameterization.

Note that you can reset ‘effective zero’ and ‘effective infinity’: see below.

Usage

```
notExp2(x,d=.Options$mgcv.vc.logrange,b=1/d)
```

```
notLog2(x,d=.Options$mgcv.vc.logrange,b=1/d)
```

Arguments

x	Argument array of real numbers (notExp) or positive real numbers (notLog).
d	the range of notExp2 runs from $\exp(-d)$ to $\exp(d)$. To change the range used by <code>gamm</code> reset <code>mgcv.vc.logrange</code> using options .
b	determines the period of the cycle of notExp2.

Value

An array of function values evaluated at the supplied argument values.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[pdTens](#), [pdIdnot](#), [gamm](#)

Examples

```
## Illustrate the notExp2 function:
require(mgcv)
x <- seq(-50,50,length=1000)
op <- par(mfrow=c(2,2))
plot(x,notExp2(x),type="l")
lines(x,exp(x),col=2)
plot(x,log(notExp2(x)),type="l")
lines(x,log(exp(x)),col=2) # redundancy intended
x <- x/4
plot(x,notExp2(x),type="l")
lines(x,exp(x),col=2)
plot(x,log(notExp2(x)),type="l")
lines(x,log(exp(x)),col=2) # redundancy intended
par(op)
```

null.space.dimension *The basis of the space of un-penalized functions for a TPRS*

Description

The thin plate spline penalties give zero penalty to some functions. The space of these functions is spanned by a set of polynomial terms. `null.space.dimension` finds the dimension of this space, M , given the number of covariates that the smoother is a function of, d , and the order of the smoothing penalty, m . If m does not satisfy $2m > d$ then the smallest possible dimension for the null space is found given d and the requirement that the smooth should be visually smooth.

Usage

```
null.space.dimension(d,m)
```

Arguments

d is a positive integer - the number of variables of which the t.p.s. is a function.

m a non-negative integer giving the order of the penalty functional, or signalling that the default order should be used.

Details

Thin plate splines are only visually smooth if the order of the wiggleness penalty, m , satisfies $2m > d + 1$. If $2m < d + 1$ then this routine finds the smallest m giving visual smoothness for the given d , otherwise the supplied m is used. The null space dimension is given by:

$$M = (m + d - 1)! / (d!(m - 1)!)$$

which is the value returned.

Value

An integer (array), the null space dimension M .

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2003) Thin plate regression splines. J.R.Statist.Soc.B 65(1):95-114
<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[tprs](#)

Examples

```
require(mgcv)
null.space.dimension(2,0)
```

ocat *GAM ordered categorical family*

Description

Family for use with `gam`, implementing regression for ordered categorical data. A linear predictor provides the expected value of a latent variable following a logistic distribution. The probability of this latent variable lying between certain cut-points provides the probability of the ordered categorical variable being of the corresponding category. The cut-points are estimated along side the model smoothing parameters (using the same criterion). The observed categories are coded 1, 2, 3, ... up to the number of categories.

Usage

```
ocat(theta=NULL,link="identity",R=NULL)
```

Arguments

<code>theta</code>	cut point parameter vector (dimension $R-2$). If supplied and all positive, then taken to be the cut point increments (first cut point is fixed at -1). If any are negative then absolute values are taken as starting values for cutpoint increments.
<code>link</code>	The link function: only "identity" allowed at present (possibly for ever).
<code>R</code>	the number of categories.

Details

Such cumulative threshold models are only identifiable up to an intercept, or one of the cut points. Rather than remove the intercept, `ocat` simply sets the first cut point to -1. Use `predict.gam` with `type="response"` to get the predicted probabilities in each category.

Value

An object of class `extended.family`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

Examples

```

library(mgcv)
## Simulate some ordered categorical data...
set.seed(3);n<-400
dat <- gamSim(1,n=n)
dat$f <- dat$f - mean(dat$f)

alpha <- c(-Inf,-1,0,5,Inf)
R <- length(alpha)-1
y <- dat$f
u <- runif(n)
u <- dat$f + log(u/(1-u))
for (i in 1:R) {
  y[u > alpha[i]&u <= alpha[i+1]] <- i
}
dat$y <- y

## plot the data...
par(mfrow=c(2,2))
with(dat,plot(x0,y));with(dat,plot(x1,y))
with(dat,plot(x2,y));with(dat,plot(x3,y))

## fit ocat model to data...
b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=ocat(R=R),data=dat)
b
plot(b,pages=1)
gam.check(b)
summary(b)
b$family$getTheta(TRUE) ## the estimated cut points

## predict probabilities of being in each category
predict(b,dat[1:2,],type="response",se=TRUE)

```

Description

The ‘one standard error rule’ (see e.g. Hastie, Tibshirani and Friedman, 2009) is a way of producing smoother models than those directly estimated by automatic smoothing parameter selection methods. In the single smoothing parameter case, we select the largest smoothing parameter within one standard error of the optimum of the smoothing parameter selection criterion. This approach can be generalized to multiple smoothing parameters estimated by REML or ML.

Details

Under REML or ML smoothing parameter selection an asymptotic distributional approximation is available for the log smoothing parameters. Let ρ denote the log smoothing parameters that we want to increase to obtain a smoother model. The large sample distribution of the estimator of ρ is

$N(\rho, V)$ where V is the matrix returned by `sp.vcov`. Drop any elements of ρ that are already at ‘effective infinity’, along with the corresponding rows and columns of V . The standard errors of the log smoothing parameters can be obtained from the leading diagonal of V . Let the vector of these be d . Now suppose that we want to increase the estimated log smoothing parameters by an amount αd . We choose α so that $\alpha d^T V^{-1} d = \sqrt{2p}$, where p is the dimension of d and $2p$ the variance of a chi-squared r.v. with p degrees of freedom.

The idea is that we increase the log smoothing parameters in proportion to their standard deviation, until the RE/ML is increased by 1 standard deviation according to its asymptotic distribution.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Hastie, T, R. Tibshirani and J. Friedman (2009) *The Elements of Statistical Learning* 2nd ed. Springer.

See Also

[gam](#)

Examples

```
require(mgcv)
set.seed(2) ## simulate some data...
dat <- gamSim(1,n=400,dist="normal",scale=2)
b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="REML")
b
## only the first 3 smoothing parameters are candidates for
## increasing here...
V <- sp.vcov(b)[1:3,1:3] ## the approx cov matrix of sps
d <- diag(V)^.5          ## sp se.
## compute the log smoothing parameter step...
d <- sqrt(2*length(d))/d
sp <- b$sp ## extract original sp estimates
sp[1:3] <- sp[1:3]*exp(d) ## apply the step
## refit with the increased smoothing parameters...
b1 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="REML",sp=sp)
b;b1 ## compare fits
```

Description

Solves least squares problems with quadratic penalties subject to linear equality and inequality constraints using quadratic programming.

Usage

pcls(M)

Arguments

- M** is the single list argument to pcls. It should have the following elements:
- y** The response data vector.
 - w** A vector of weights for the data (often proportional to the reciprocal of the variance).
 - X** The design matrix for the problem, note that ncol(M\$X) must give the number of model parameters, while nrow(M\$X) should give the number of data.
 - C** Matrix containing any linear equality constraints on the problem (e.g. $\mathbf{C}\mathbf{p} = \mathbf{c}$). If you have no equality constraints initialize this to a zero by zero matrix. Note that there is no need to supply the vector \mathbf{c} , it is defined implicitly by the initial parameter estimates \mathbf{p} .
 - S** A list of penalty matrices. $S[[i]]$ is the smallest contiguous matrix including all the non-zero elements of the i th penalty matrix. The first parameter it penalizes is given by $\text{off}[i]+1$ (starting counting at 1).
 - off** Offset values locating the elements of M\$S in the correct location within each penalty coefficient matrix. (Zero offset implies starting in first location)
 - sp** An array of smoothing parameter estimates.
 - p** An array of feasible initial parameter estimates - these must satisfy the constraints, but should avoid satisfying the inequality constraints as equality constraints.
 - Ain** Matrix for the inequality constraints $\mathbf{A}_{in}\mathbf{p} > \mathbf{b}_{in}$.
 - bin** vector in the inequality constraints.

Details

This solves the problem:

$$\text{minimise } \|\mathbf{W}^{1/2}(\mathbf{X}\mathbf{p} - \mathbf{y})\|^2 + \sum_{i=1}^m \lambda_i \mathbf{p}'\mathbf{S}_i\mathbf{p}$$

subject to constraints $\mathbf{C}\mathbf{p} = \mathbf{c}$ and $\mathbf{A}_{in}\mathbf{p} > \mathbf{b}_{in}$, w.r.t. \mathbf{p} given the smoothing parameters λ_i . \mathbf{X} is a design matrix, \mathbf{p} a parameter vector, \mathbf{y} a data vector, \mathbf{W} a diagonal weight matrix, \mathbf{S}_i a positive semi-definite matrix of coefficients defining the i th penalty and \mathbf{C} a matrix of coefficients defining the linear equality constraints on the problem. The smoothing parameters are the λ_i . Note that \mathbf{X} must be of full column rank, at least when projected into the null space of any equality constraints. \mathbf{A}_{in} is a matrix of coefficients defining the inequality constraints, while \mathbf{b}_{in} is a vector involved in defining the inequality constraints.

Quadratic programming is used to perform the solution. The method used is designed for maximum stability with least squares problems: i.e. $\mathbf{X}'\mathbf{X}$ is not formed explicitly. See Gill et al. 1981.

Value

The function returns an array containing the estimated parameter vector.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Gill, P.E., Murray, W. and Wright, M.H. (1981) Practical Optimization. Academic Press, London.
 Wood, S.N. (1994) Monotonic smoothing splines fitted by cross validation SIAM Journal on Scientific Computing 15(5):1126-1133
<http://www.maths.bris.ac.uk/~sw15190/>

See Also

magic.mono.con

Examples

```
require(mgcv)
# first an un-penalized example - fit E(y)=a+bx subject to a>0
set.seed(0)
n <- 100
x <- runif(n); y <- x - 0.2 + rnorm(n)*0.1
M <- list(X=matrix(0,n,2),p=c(0.1,0.5),off=array(0,0),S=list(),
Ain=matrix(0,1,2),bin=0,C=matrix(0,0,0),sp=array(0,0),y=y,w=y*0+1)
M$X[,1] <- 1; M$X[,2] <- x; M$Ain[1,] <- c(1,0)
pcls(M) -> M$p
plot(x,y); abline(M$p,col=2); abline(coef(lm(y~x)),col=3)

# Penalized example: monotonic penalized regression spline ....

# Generate data from a monotonic truth.
x <- runif(100)*4-1;x <- sort(x);
f <- exp(4*x)/(1+exp(4*x)); y <- f+rnorm(100)*0.1; plot(x,y)
dat <- data.frame(x=x,y=y)
# Show regular spline fit (and save fitted object)
f.ug <- gam(y~s(x,k=10,bs="cr")); lines(x,fitted(f.ug))
# Create Design matrix, constraints etc. for monotonic spline...
sm <- smoothCon(s(x,k=10,bs="cr"),dat,knots=NULL)[[1]]
F <- mono.con(sm$xp); # get constraints
G <- list(X=sm$X,C=matrix(0,0,0),sp=f.ug$sp,p=sm$xp,y=y,w=y*0+1)
G$Ain <- F$A;G$bin <- F$b;G$S <- sm$S;G$off <- 0

p <- pcls(G); # fit spline (using s.p. from unconstrained fit)

fv<-Predict.matrix(sm,data.frame(x=x))%*%p
lines(x,fv,col=2)

# now a tprs example of the same thing...

f.ug <- gam(y~s(x,k=10)); lines(x,fitted(f.ug))
# Create Design matrix, constraints etc. for monotonic spline...
sm <- smoothCon(s(x,k=10,bs="tp"),dat,knots=NULL)[[1]]
```



```

xc <- 0:39/39 # points on [0,1]
nc <- length(xc) # number of constraints
xc <- xc*4-1 # points at which to impose constraints
A0 <- Predict.matrix(sm,data.frame(x=xc))
# ... A0%%p evaluates spline at xc points
A1 <- Predict.matrix(sm,data.frame(x=xc+1e-6))
A <- (A1-A0)/1e-6
## ... approx. constraint matrix (A%%p is -ve
## spline gradient at points xc)
G <- list(X=sm$X,C=matrix(0,0,0),sp=f.ug$sp,y=y,w=y*0+1,S=sm$S,off=0)
G$Ain <- A; # constraint matrix
G$bin <- rep(0,nc); # constraint vector
G$p <- rep(0,10); G$p[10] <- 0.1
# ... monotonic start params, got by setting coefs of polynomial part
p <- pcls(G); # fit spline (using s.p. from unconstrained fit)

fv2 <- Predict.matrix(sm,data.frame(x=x))%%p
lines(x,fv2,col=3)

#####
## monotonic additive model example...
#####

## First simulate data...

set.seed(10)
f1 <- function(x) 5*exp(4*x)/(1+exp(4*x));
f2 <- function(x) {
  ind <- x > .5
  f <- x*0
  f[ind] <- (x[ind] - .5)^2*10
  f
}
f3 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 +
  10 * (10 * x)^3 * (1 - x)^10
n <- 200
x <- runif(n); z <- runif(n); v <- runif(n)
mu <- f1(x) + f2(z) + f3(v)
y <- mu + rnorm(n)

## Preliminary unconstrained gam fit...
G <- gam(y~s(x)+s(z)+s(v,k=20),fit=FALSE)
b <- gam(G=G)

## generate constraints, by finite differencing
## using predict.gam ....
eps <- 1e-7
pd0 <- data.frame(x=seq(0,1,length=100),z=rep(.5,100),
  v=rep(.5,100))
pd1 <- data.frame(x=seq(0,1,length=100)+eps,z=rep(.5,100),
  v=rep(.5,100))
X0 <- predict(b,newdata=pd0,type="lpmatrix")
X1 <- predict(b,newdata=pd1,type="lpmatrix")

```

```

Xx <- (X1 - X0)/eps ## Xx %% coef(b) must be positive
pd0 <- data.frame(z=seq(0,1,length=100),x=rep(.5,100),
                 v=rep(.5,100))
pd1 <- data.frame(z=seq(0,1,length=100)+eps,x=rep(.5,100),
                 v=rep(.5,100))
X0 <- predict(b,newdata=pd0,type="lpmatrix")
X1 <- predict(b,newdata=pd1,type="lpmatrix")
Xz <- (X1-X0)/eps
G$Ain <- rbind(Xx,Xz) ## inequality constraint matrix
G$bin <- rep(0,nrow(G$Ain))
G$C = matrix(0,0,ncol(G$X))
G$sp <- b$sp
G$p <- coef(b)
G$off <- G$off-1 ## to match what pcls is expecting
## force initial parameters to meet constraint
G$p[11:18] <- G$p[2:9]<- 0
p <- pcls(G) ## constrained fit
par(mfrow=c(2,3))
plot(b) ## original fit
b$coefficients <- p
plot(b) ## constrained fit
## note that standard errors in preceding plot are obtained from
## unconstrained fit

```

pdIdnot

Overflow proof pdMat class for multiples of the identity matrix

Description

This set of functions is a modification of the pdMat class pdIdent from library nlme. The modification is to replace the log parameterization used in pdMat with a `notLog2` parameterization, since the latter avoids indefiniteness in the likelihood and associated convergence problems: the parameters also relate to variances rather than standard deviations, for consistency with the `pdTens` class. The functions are particularly useful for working with Generalized Additive Mixed Models where variance parameters/smoothing parameters can be very large or very small, so that overflow or underflow can be a problem.

These functions would not normally be called directly, although unlike the `pdTens` class it is easy to do so.

Usage

```

pdIdnot(value = numeric(0), form = NULL,
        nam = NULL, data = sys.frame(sys.parent()))

```

Arguments

value	Initialization values for parameters. Not normally used.
form	A one sided formula specifying the random effects structure.

nam a names argument, not normally used with this class.
 data data frame in which to evaluate formula.

Details

The following functions are provided: `Dim.pdIndot`, `coef.pdIndot`, `corMatrix.pdIndot`, `logDet.pdIndot`, `pdConstruct.pdIndot`, `pdFactor.pdIndot`, `pdMatrix.pdIndot`, `solve.pdIndot`, `summary.pdIndot`. (e.g. `mgcv::coef.pdIndot` to access.)

Note that while the `pdFactor` and `pdMatrix` functions return the inverse of the scaled random effect covariance matrix or its factor, the `pdConstruct` function is initialised with estimates of the scaled covariance matrix itself.

Value

A class `pdIndot` object, or related quantities. See the `nlme` documentation for further details.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Pinheiro J.C. and Bates, D.M. (2000) Mixed effects Models in S and S-PLUS. Springer

The `nlme` source code.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[te](#), [pdTens](#), [notLog2](#), [gamm](#)

Examples

```
# see gamm
```

pdTens

Functions implementing a pdMat class for tensor product smooths

Description

This set of functions implements an `nlme` library `pdMat` class to allow tensor product smooths to be estimated by `lme` as called by `gamm`. Tensor product smooths have a penalty matrix made up of a weighted sum of penalty matrices, where the weights are the smoothing parameters. In the mixed model formulation the penalty matrix is the inverse of the covariance matrix for the random effects of a term, and the smoothing parameters (times a half) are variance parameters to be estimated. It's not possible to transform the problem to make the required random effects covariance matrix look like one of the standard `pdMat` classes: hence the need for the `pdTens` class. A `notLog2` parameterization ensures that the parameters are positive.

These functions (pdTens, pdConstruct.pdTens, pdFactor.pdTens, pdMatrix.pdTens, coef.pdTens and summary.pdTens) would not normally be called directly.

Usage

```
pdTens(value = numeric(0), form = NULL,
       nam = NULL, data = sys.frame(sys.parent()))
```

Arguments

value	Initialization values for parameters. Not normally used.
form	A one sided formula specifying the random effects structure. The formula should have an attribute S which is a list of the penalty matrices the weighted sum of which gives the inverse of the covariance matrix for these random effects.
nam	a names argument, not normally used with this class.
data	data frame in which to evaluate formula.

Details

If using this class directly note that it is worthwhile scaling the S matrices to be of ‘moderate size’, for example by dividing each matrix by its largest singular value: this avoids problems with lme defaults ([smooth.construct.tensor.smooth.spec](#) does this automatically).

This appears to be the minimum set of functions required to implement a new pdMat class.

Note that while the pdFactor and pdMatrix functions return the inverse of the scaled random effect covariance matrix or its factor, the pdConstruct function is sometimes initialised with estimates of the scaled covariance matrix, and sometimes intialized with its inverse.

Value

A class pdTens object, or its coefficients or the matrix it represents or the factor of that matrix. pdFactor returns the factor as a vector (packed column-wise) (pdMatrix always returns a matrix).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Pinheiro J.C. and Bates, D.M. (2000) Mixed effects Models in S and S-PLUS. Springer
 The nlme source code.
<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[te gamm](#)

Examples

```
# see gamm
```

pen.edf	<i>Extract the effective degrees of freedom associated with each penalty in a gam fit</i>
---------	---

Description

Finds the coefficients penalized by each penalty and adds up their effective degrees of freedom. Very useful for [t2](#) terms, but hard to interpret for terms where the penalties penalize overlapping sets of parameters (e.g. [te](#) terms).

Usage

```
pen.edf(x)
```

Arguments

x an object inheriting from gam

Details

Useful for models containing [t2](#) terms, since it splits the EDF for the term up into parts due to different components of the smooth. This is useful for figuring out which interaction terms are actually needed in a model.

Value

A vector of EDFs, named with labels identifying which penalty each EDF relates to.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[t2](#)

Examples

```
require(mgcv)
set.seed(20)
dat <- gamSim(1,n=400,scale=2) ## simulate data
## following `t2' smooth basically separates smooth
## of x0,x1 into main effects + interaction...

b <- gam(y~t2(x0,x1,bs="tp",m=1,k=7)+s(x2)+s(x3),
         data=dat,method="ML")
pen.edf(b)
```

```

## label "rr" indicates interaction edf (range space times range space)
## label "nr" (null space for x0 times range space for x1) is main
##      effect for x1.
## label "rn" is main effect for x0
## clearly interaction is negligible

## second example with higher order marginals.

b <- gam(y~t2(x0,x1,bs="tp",m=2,k=7,full=TRUE)
        +s(x2)+s(x3),data=dat,method="ML")
pen.edf(b)

## In this case the EDF is negligible for all terms in the t2 smooth
## apart from the `main effects' (r2 and 2r). To understand the labels
## consider the following 2 examples....
## "r1" relates to the interaction of the range space of the first
##      marginal smooth and the first basis function of the null
##      space of the second marginal smooth
## "2r" relates to the interaction of the second basis function of
##      the null space of the first marginal smooth with the range
##      space of the second marginal smooth.

```

place.knots

Automatically place a set of knots evenly through covariate values

Description

Given a univariate array of covariate values, places a set of knots for a regression spline evenly through the covariate values.

Usage

```
place.knots(x,nk)
```

Arguments

x array of covariate values (need not be sorted).
nk integer indicating the required number of knots.

Details

Places knots evenly throughout a set of covariates. For example, if you had 11 covariate values and wanted 6 knots then a knot would be placed at the first (sorted) covariate value and every second (sorted) value thereafter. With less convenient numbers of data and knots the knots are placed within intervals between data in order to achieve even coverage, where even means having approximately the same number of data between each pair of knots.

Value

An array of knot locations.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[smooth.construct.cc.smooth.spec](#)

Examples

```
require(mgcv)
x<-runif(30)
place.knots(x,7)
rm(x)
```

plot.gam

Default GAM plotting

Description

Takes a fitted gam object produced by `gam()` and plots the component smooth functions that make it up, on the scale of the linear predictor. Optionally produces term plots for parametric model components as well.

Usage

```
## S3 method for class 'gam'
plot(x, residuals=FALSE, rug=TRUE, se=TRUE, pages=0, select=NULL, scale=-1,
      n=100, n2=40, pers=FALSE, theta=30, phi=30, jit=FALSE, xlab=NULL,
      ylab=NULL, main=NULL, ylim=NULL, xlim=NULL, too.far=0.1,
      all.terms=FALSE, shade=FALSE, shade.col="gray80", shift=0,
      trans=I, seWithMean=FALSE, unconditional=FALSE, by.resids=FALSE,
      scheme=0, ...)
```

Arguments

`x` a fitted gam object as produced by `gam()`.

`residuals` If TRUE then partial residuals are added to plots of 1-D smooths. If FALSE then no residuals are added. If this is an array of the correct length then it is used as the array of residuals to be used for producing partial residuals. If TRUE then the residuals are the working residuals from the IRLS iteration weighted by the IRLS weights. Partial residuals for a smooth term are the residuals that would be obtained by dropping the term concerned from the model, while leaving all other estimates fixed (i.e. the estimates for the term plus the residuals).

rug	when TRUE (default) then the covariate to which the plot applies is displayed as a rug plot at the foot of each plot of a 1-d smooth, and the locations of the covariates are plotted as points on the contour plot representing a 2-d smooth. Setting to FALSE will speed up plotting for large datasets.
se	when TRUE (default) upper and lower lines are added to the 1-d plots at 2 standard errors above and below the estimate of the smooth being plotted while for 2-d plots, surfaces at +1 and -1 standard errors are contoured and overlayed on the contour plot for the estimate. If a positive number is supplied then this number is multiplied by the standard errors when calculating standard error curves or surfaces. See also shade, below.
pages	(default 0) the number of pages over which to spread the output. For example, if pages=1 then all terms will be plotted on one page with the layout performed automatically. Set to 0 to have the routine leave all graphics settings as they are.
select	Allows the plot for a single model term to be selected for printing. e.g. if you just want the plot for the second smooth term set select=2.
scale	set to -1 (default) to have the same y-axis scale for each plot, and to 0 for a different y axis for each plot. Ignored if ylim supplied.
n	number of points used for each 1-d plot - for a nice smooth plot this needs to be several times the estimated degrees of freedom for the smooth. Default value 100.
n2	Square root of number of points used to grid estimates of 2-d functions for contouring.
pers	Set to TRUE if you want perspective plots for 2-d terms.
theta	One of the perspective plot angles.
phi	The other perspective plot angle.
jit	Set to TRUE if you want rug plots for 1-d terms to be jittered.
xlab	If supplied then this will be used as the x label for all plots.
ylab	If supplied then this will be used as the y label for all plots.
main	Used as title (or z axis label) for plots if supplied.
ylim	If supplied then this pair of numbers are used as the y limits for each plot.
xlim	If supplied then this pair of numbers are used as the x limits for each plot.
too.far	If greater than 0 then this is used to determine when a location is too far from data to be plotted when plotting 2-D smooths. This is useful since smooths tend to go wild away from data. The data are scaled into the unit square before deciding what to exclude, and too.far is a distance within the unit square. Setting to zero can make plotting faster for large datasets, but care then needed with interpretation of plots.
all.terms	if set to TRUE then the partial effects of parametric model components are also plotted, via a call to <code>termplot</code> . Only terms of order 1 can be plotted in this way.
shade	Set to TRUE to produce shaded regions as confidence bands for smooths (not available for parametric terms, which are plotted using <code>termplot</code>).
shade.col	define the color used for shading confidence bands.

shift	constant to add to each smooth (on the scale of the linear predictor) before plotting. Can be useful for some diagnostics, or with trans.
trans	function to apply to each smooth (after any shift), before plotting. shift and trans are occasionally useful as a means for getting plots on the response scale, when the model consists only of a single smooth.
seWithMean	if TRUE the component smooths are shown with confidence intervals that include the uncertainty about the overall mean. If FALSE then the uncertainty relates purely to the centred smooth itself. Marra and Wood (2012) suggests that TRUE results in better coverage performance, and this is also suggested by simulation.
unconditional	if TRUE then the smoothing parameter uncertainty corrected covariance matrix is used to compute uncertainty bands, if available. Otherwise the bands treat the smoothing parameters as fixed.
by.resids	Should partial residuals be plotted for terms with by variables? Usually the answer is no, they would be meaningless.
scheme	Integer or integer vector selecting a plotting scheme for each plot. See details.
...	other graphics parameters to pass on to plotting commands. See details for smooth plot specific options.

Details

Produces default plot showing the smooth components of a fitted GAM, and optionally parametric terms as well, when these can be handled by [termplot](#).

For smooth terms `plot.gam` actually calls plot method functions depending on the class of the smooth. Currently [random.effects](#), Markov random fields ([mrf](#)), [Spherical.Spline](#) and [factor.smooth.interaction](#) terms have special methods (documented in their help files), the rest use the defaults described below.

For plots of 1-d smooths, the x axis of each plot is labelled with the covariate name, while the y axis is labelled `s(cov, edf)` where `cov` is the covariate name, and `edf` the estimated (or user defined for regression splines) degrees of freedom of the smooth. `scheme == 0` produces a smooth curve with dashed curves indicating 2 standard error bounds. `scheme == 1` illustrates the error bounds using a shaded region.

For `scheme==0`, contour plots are produced for 2-d smooths with the x-axes labelled with the first covariate name and the y axis with the second covariate name. The main title of the plot is something like `s(var1, var2, edf)`, indicating the variables of which the term is a function, and the estimated degrees of freedom for the term. When `se=TRUE`, estimator variability is shown by overlaying contour plots at plus and minus 1 s.e. relative to the main estimate. If `se` is a positive number then contour plots are at plus or minus `se` multiplied by the s.e. Contour levels are chosen to try and ensure reasonable separation of the contours of the different plots, but this is not always easy to achieve. Note that these plots can not be modified to the same extent as the other plot.

For 2-d smooths `scheme==1` produces a perspective plot, while `scheme==2` produces a heatmap, with overlaid contours.

Smooths of more than 2 variables are not plotted, but see [vis.gam](#).

Fine control of plots for parametric terms can be obtained by calling [termplot](#) directly, taking care to use its `terms` argument.

Note that, if `seWithMean=TRUE`, the confidence bands include the uncertainty about the overall mean. In other words although each smooth is shown centred, the confidence bands are obtained as if every other term in the model was constrained to have average 0, (average taken over the covariate values), except for the smooth concerned. This seems to correspond more closely to how most users interpret componentwise intervals in practice, and also results in intervals with close to nominal (frequentist) coverage probabilities by an extension of Nychka's (1988) results presented in Marra and Wood (2012).

Several smooth plots methods using `image` will accept a `colors` argument, which can be anything documented in `heat.colors` (in which case something like `colors=rainbow(50)` is appropriate), or the `grey` function (in which case something like `colors=grey(0:50/50)` is needed). Another option is `contour.col` which will set the contour colour for some plots. These options are useful for producing grey scale pictures instead of colour.

Sometimes you may want a small change to a default plot, and the arguments to `plot.gam` just won't let you do it. In this case, the quickest option is sometimes to clone the `smooth.construct` and `Predict.matrix` methods for the smooth concerned, modifying only the returned smoother class (e.g. to `foo.smooth`). Then copy the plot method function for the original class (e.g. `mgcv:::plot.mgcv.smooth`), modify the source code to plot exactly as you want and rename the plot method function (e.g. `plot.foo.smooth`). You can then use the cloned smooth in models (e.g. `s(x,bs="foo")`), and it will automatically plot using the modified plotting function.

Value

The functions main purpose is its side effect of generating plots. It also silently returns a list of the data used to produce the plots, which can be used to generate customized plots.

WARNING

Note that the behaviour of this function is not identical to `plot.gam()` in S-PLUS.

Plotting can be slow for models fitted to large datasets. Set `rug=FALSE` to improve matters. If it's still too slow set `too.far=0`, but then take care not to overinterpret smooths away from supporting data.

Plots of 2-D smooths with standard error contours shown can not easily be customized.

The function can not deal with smooths of more than 2 variables!

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Henric Nilsson <henric.nilsson@statisticon.se> donated the code for the shade option.

The design is inspired by the S function of the same name described in Chambers and Hastie (1993) (but is not a clone).

References

Chambers and Hastie (1993) *Statistical Models in S*. Chapman & Hall.

Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. *Scandinavian Journal of Statistics*.

Nychka (1988) Bayesian Confidence Intervals for Smoothing Splines. *Journal of the American Statistical Association* 83:1134-1143.

Wood S.N. (2006) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.

See Also

[gam](#), [predict.gam](#), [vis.gam](#)

Examples

```
library(mgcv)
set.seed(0)
## fake some data...
f1 <- function(x) {exp(2 * x)}
f2 <- function(x) {
  0.2*x^11*(10*(1-x))^6+10*(10*x)^3*(1-x)^10
}
f3 <- function(x) {x*0}

n<-200
sig2<-4
x0 <- rep(1:4,50)
x1 <- runif(n, 0, 1)
x2 <- runif(n, 0, 1)
x3 <- runif(n, 0, 1)
e <- rnorm(n, 0, sqrt(sig2))
y <- 2*x0 + f1(x1) + f2(x2) + f3(x3) + e
x0 <- factor(x0)

## fit and plot...
b<-gam(y~x0+s(x1)+s(x2)+s(x3))
plot(b,pages=1,residuals=TRUE,all.terms=TRUE,shade=TRUE,shade.col=2)
plot(b,pages=1,seWithMean=TRUE) ## better coverage intervals

## just parametric term alone...
termpplot(b,terms="x0",se=TRUE)

## more use of color...
op <- par(mfrow=c(2,2),bg="blue")
x <- 0:1000/1000
for (i in 1:3) {
  plot(b,select=i,rug=FALSE,col="green",
       col.axis="white",col.lab="white",all.terms=TRUE)
  for (j in 1:2) axis(j,col="white",labels=FALSE)
  box(col="white")
  eval(parse(text=paste("fx <- f",i,"(x)",sep="")))
  fx <- fx-mean(fx)
  lines(x,fx,col=2) ## overlay `truth' in red
}
par(op)
```

```
## example with 2-d plots, and use of schemes...
b1 <- gam(y~x0+s(x1,x2)+s(x3))
op <- par(mfrow=c(2,2))
plot(b1,all.terms=TRUE)
par(op)
op <- par(mfrow=c(2,2))
plot(b1,all.terms=TRUE,scheme=1)
par(op)
op <- par(mfrow=c(2,2))
plot(b1,all.terms=TRUE,scheme=c(2,1))
par(op)
```

polys.plot

Plot geographic regions defined as polygons

Description

Produces plots of geographic regions defined by polygons, optionally filling the polygons with a color or grey shade dependent on a covariate.

Usage

```
polys.plot(pc,z=NULL,scheme="heat",lab="",...)
```

Arguments

pc	A named list of matrices. Each matrix has two columns. The matrix rows each define the vertex of a boundary polygon. If a boundary is defined by several polygons, then each of these must be separated by an NA row in the matrix. See mrf for an example.
z	A vector of values associated with each area (item) of pc. If the vector elements have names then these are used to match elements of z to areas defined in pc. Otherwise pc and z are assumed to be in the same order. If z is NULL then polygons are not filled.
scheme	One of "heat" or "grey", indicating how to fill the polygons in accordance with the value of z.
lab	label for plot.
...	other arguments to pass to plot (currently only if z is NULL).

Details

Any polygon within another polygon counts as a hole in the area. Further nesting is dealt with by treating any point that is interior to an odd number of polygons as being within the area, and all other points as being exterior. The routine is provided to facilitate plotting with models containing [mrf](#) smooths.

Value

Simply produces a plot.

Author(s)

Simon Wood <simon.wood@r-project.org>

See Also

[mrf](#) and [columb.polys](#).

Examples

```
## see also ?mrf for use of z
require(mgcv)
data(columb.polys)
polys.plot(columb.polys)
```

predict.bam

Prediction from fitted Big Additive Model model

Description

Essentially a wrapper for [predict.gam](#) for prediction from a model fitted by [bam](#). Can compute on a parallel cluster.

Takes a fitted bam object produced by [bam](#) and produces predictions given a new set of values for the model covariates or the original values used for the model fit. Predictions can be accompanied by standard errors, based on the posterior distribution of the model coefficients. The routine can optionally return the matrix by which the model coefficients must be pre-multiplied in order to yield the values of the linear predictor at the supplied covariate values: this is useful for obtaining credible regions for quantities derived from the model (e.g. derivatives of smooths), and for lookup table prediction outside R (see example code below).

Usage

```
## S3 method for class 'bam'
predict(object,newdata,type="link",se.fit=FALSE,terms=NULL,
        exclude=NULL,block.size=50000,newdata.guaranteed=FALSE,
        na.action=na.pass,cluster=NULL,discrete=TRUE,n.threads=1,...)
```

Arguments

object	a fitted bam object as produced by bam .
newdata	A data frame or list containing the values of the model covariates at which predictions are required. If this is not provided then predictions corresponding to the original data are returned. If newdata is provided then it should contain all the variables needed for prediction: a warning is generated if not.

type	When this has the value "link" (default) the linear predictor (possibly with associated standard errors) is returned. When type="terms" each component of the linear predictor is returned separately (possibly with standard errors): this includes parametric model components, followed by each smooth component, but excludes any offset and any intercept. type="iterms" is the same, except that any standard errors returned for smooth components will include the uncertainty about the intercept/overall mean. When type="response" predictions on the scale of the response are returned (possibly with approximate standard errors). When type="lpmatrix" then a matrix is returned which yields the values of the linear predictor (minus any offset) when postmultiplied by the parameter vector (in this case se.fit is ignored). The latter option is most useful for getting variance estimates for quantities derived from the model: for example integrated quantities, or derivatives of smooths. A linear predictor matrix can also be used to implement approximate prediction outside R (see example code, below).
se.fit	when this is TRUE (not default) standard error estimates are returned for each prediction.
terms	if type=="terms" or type="iterms" then only results for the terms (smooth or parametric) named in this array will be returned. Otherwise any smooth terms not named in this array will be set to zero. If NULL then all terms are included.
exclude	if type=="terms" or type="iterms" then terms (smooth or parametric) named in this array will not be returned. Otherwise any smooth terms named in this array will be set to zero. If NULL then no terms are excluded.
block.size	maximum number of predictions to process per call to underlying code: larger is quicker, but more memory intensive.
newdata.guaranteed	Set to TRUE to turn off all checking of newdata except for sanity of factor levels: this can speed things up for large prediction tasks, but newdata must be complete, with no NA values for predictors required in the model.
na.action	what to do about NA values in newdata. With the default na.pass, any row of newdata containing NA values for required predictors, gives rise to NA predictions (even if the term concerned has no NA predictors). na.exclude or na.omit result in the dropping of newdata rows, if they contain any NA values for required predictors. If newdata is missing then NA handling is determined from object\$na.action.
cluster	predict.bam can compute in parallel using parLapply from the parallel package, if it is supplied with a cluster on which to do this (a cluster here can be some cores of a single machine). See details and example code for bam .
discrete	if TRUE then discrete prediction methods used with model fitted by discrete methods. FALSE for regular prediction.
n.threads	if se.fit=TRUE and discrete prediction is used then parallel computation can be used to speed up se calculation. This specifies number of hthreads to use.
...	other arguments.

Details

The standard errors produced by `predict.gam` are based on the Bayesian posterior covariance matrix of the parameters ψ in the fitted `bam` object.

To facilitate plotting with `termplot`, if object possesses an attribute `"para.only"` and `type=="terms"` then only parametric terms of order 1 are returned (i.e. those that `termplot` can handle).

Note that, in common with other prediction functions, any offset supplied to `gam` as an argument is always ignored when predicting, unlike offsets specified in the `gam` model formula.

See the examples in `predict.gam` for how to use the `lpmatrix` for obtaining credible regions for quantities derived from the model.

Value

If `type=="lpmatrix"` then a matrix is returned which will give a vector of linear predictor values (minus any offset) at the supplied covariate values, when applied to the model coefficient vector. Otherwise, if `se.fit` is TRUE then a 2 item list is returned with items (both arrays) `fit` and `se.fit` containing predictions and associated standard error estimates, otherwise an array of predictions is returned. The dimensions of the returned arrays depends on whether `type` is `"terms"` or not: if it is then the array is 2 dimensional with each term in the linear predictor separate, otherwise the array is 1 dimensional and contains the linear predictor/predicted values (or corresponding s.e.s). The linear predictor returned termwise will not include the offset or the intercept.

`newdata` can be a data frame, list or `model.frame`: if it's a model frame then all variables must be supplied.

WARNING

Predictions are likely to be incorrect if data dependent transformations of the covariates are used within calls to `smooths`. See examples in `predict.gam`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

The design is inspired by the `S` function of the same name described in Chambers and Hastie (1993) (but is not a clone).

References

Chambers and Hastie (1993) *Statistical Models in S*. Chapman & Hall.

Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. *Scandinavian Journal of Statistics*.

Wood S.N. (2006b) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.

See Also

[bam](#), [predict.gam](#)

Examples

```
## for parallel computing see examples for ?bam

## for general useage follow examples in ?predict.gam
```

predict.gam

Prediction from fitted GAM model

Description

Takes a fitted gam object produced by `gam()` and produces predictions given a new set of values for the model covariates or the original values used for the model fit. Predictions can be accompanied by standard errors, based on the posterior distribution of the model coefficients. The routine can optionally return the matrix by which the model coefficients must be pre-multiplied in order to yield the values of the linear predictor at the supplied covariate values: this is useful for obtaining credible regions for quantities derived from the model (e.g. derivatives of smooths), and for lookup table prediction outside R (see example code below).

Usage

```
## S3 method for class 'gam'
predict(object,newdata,type="link",se.fit=FALSE,terms=NULL,
        exclude=NULL,block.size=NULL,newdata.guaranteed=FALSE,
        na.action=na.pass,unconditional=FALSE,...)
```

Arguments

object	a fitted gam object as produced by <code>gam()</code> .
newdata	A data frame or list containing the values of the model covariates at which predictions are required. If this is not provided then predictions corresponding to the original data are returned. If <code>newdata</code> is provided then it should contain all the variables needed for prediction: a warning is generated if not.
type	When this has the value "link" (default) the linear predictor (possibly with associated standard errors) is returned. When <code>type="terms"</code> each component of the linear predictor is returned seperately (possibly with standard errors): this includes parametric model components, followed by each smooth component, but excludes any offset and any intercept. <code>type="iterms"</code> is the same, except that any standard errors returned for smooth components will include the uncertainty about the intercept/overall mean. When <code>type="response"</code> predictions on the scale of the response are returned (possibly with approximate standard errors). When <code>type="lpmatrix"</code> then a matrix is returned which yields the values of the linear predictor (minus any offset) when postmultiplied by the parameter vector (in this case <code>se.fit</code> is ignored). The latter option is most useful for getting variance estimates for quantities derived from the model: for example integrated quantities, or derivatives of smooths. A linear predictor matrix can also be used to implement approximate prediction outside R (see example code, below).

<code>se.fit</code>	when this is TRUE (not default) standard error estimates are returned for each prediction.
<code>terms</code>	if <code>type=="terms"</code> or <code>type=="iterms"</code> then only results for the terms (smooth or parametric) named in this array will be returned. Otherwise any smooth terms not named in this array will be set to zero. If NULL then all terms are included.
<code>exclude</code>	if <code>type=="terms"</code> or <code>type=="iterms"</code> then terms (smooth or parametric) named in this array will not be returned. Otherwise any smooth terms named in this array will be set to zero. If NULL then no terms are excluded. Note that this is the term names as it appears in the model summary, see example.
<code>block.size</code>	maximum number of predictions to process per call to underlying code: larger is quicker, but more memory intensive. Set to < 1 to use total number of predictions as this. If NULL then block size is 1000 if new data supplied, and the number of rows in the model frame otherwise.
<code>newdata.guaranteed</code>	Set to TRUE to turn off all checking of newdata except for sanity of factor levels: this can speed things up for large prediction tasks, but newdata must be complete, with no NA values for predictors required in the model.
<code>na.action</code>	what to do about NA values in newdata. With the default <code>na.pass</code> , any row of newdata containing NA values for required predictors, gives rise to NA predictions (even if the term concerned has no NA predictors). <code>na.exclude</code> or <code>na.omit</code> result in the dropping of newdata rows, if they contain any NA values for required predictors. If newdata is missing then NA handling is determined from <code>object\$na.action</code> .
<code>unconditional</code>	if TRUE then the smoothing parameter uncertainty corrected covariance matrix is used, when available, otherwise the covariance matrix conditional on the estimated smoothing parameters is used.
<code>...</code>	other arguments.

Details

The standard errors produced by `predict.gam` are based on the Bayesian posterior covariance matrix of the parameters ψ in the fitted `gam` object.

To facilitate plotting with `termplot`, if object possesses an attribute `"para.only"` and `type=="terms"` then only parametric terms of order 1 are returned (i.e. those that `termplot` can handle).

Note that, in common with other prediction functions, any offset supplied to `gam` as an argument is always ignored when predicting, unlike offsets specified in the `gam` model formula.

See the examples for how to use the `lpmatrix` for obtaining credible regions for quantities derived from the model.

Value

If `type=="lpmatrix"` then a matrix is returned which will give a vector of linear predictor values (minus any offset) at the supplied covariate values, when applied to the model coefficient vector. Otherwise, if `se.fit` is TRUE then a 2 item list is returned with items (both arrays) `fit` and `se.fit` containing predictions and associated standard error estimates, otherwise an array of predictions is returned. The dimensions of the returned arrays depends on whether `type` is `"terms"` or not: if it is

then the array is 2 dimensional with each term in the linear predictor separate, otherwise the array is 1 dimensional and contains the linear predictor/predicted values (or corresponding s.e.s). The linear predictor returned termwise will not include the offset or the intercept.

newdata can be a data frame, list or model.frame: if it's a model frame then all variables must be supplied.

WARNING

Predictions are likely to be incorrect if data dependent transformations of the covariates are used within calls to smooths. See examples.

Note that the behaviour of this function is not identical to `predict.gam()` in Splus.

`type="terms"` does not exactly match what `predict.lm` does for parametric model components.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

The design is inspired by the S function of the same name described in Chambers and Hastie (1993) (but is not a clone).

References

Chambers and Hastie (1993) Statistical Models in S. Chapman & Hall.

Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. Scandinavian Journal of Statistics, 39(1), 53-74.

Wood S.N. (2006b) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

See Also

[gam](#), [gamm](#), [plot.gam](#)

Examples

```
library(mgcv)
n<-200
sig <- 2
dat <- gamSim(1,n=n,scale=sig)

b<-gam(y~s(x0)+s(I(x1^2))+s(x2)+offset(x3),data=dat)

newd <- data.frame(x0=(0:30)/30,x1=(0:30)/30,x2=(0:30)/30,x3=(0:30)/30)
pred <- predict.gam(b,newd)
pred0 <- predict(b,newd,exclude="s(x0)") ## prediction excluding a term

#####
## difference between "terms" and "iterms"
#####
nd2 <- data.frame(x0=c(.25,.5),x1=c(.25,.5),x2=c(.25,.5),x3=c(.25,.5))
predict(b,nd2,type="terms",se=TRUE)
```

```

predict(b,nd2,type="iterms",se=TRUE)

#####
## now get variance of sum of predictions using lpmatrix
#####

Xp <- predict(b,newd,type="lpmatrix")

## Xp %*% coef(b) yields vector of predictions

a <- rep(1,31)
Xs <- t(a) %*% Xp ## Xs %*% coef(b) gives sum of predictions
var.sum <- Xs %*% b$Vp %*% t(Xs)

#####
## Now get the variance of non-linear function of predictions
## by simulation from posterior distribution of the params
#####

rmvn <- function(n,mu,sig) { ## MVN random deviates
  L <- mroot(sig);m <- ncol(L);
  t(mu + L%*%matrix(rnorm(m*n),m,n))
}

br <- rmvn(1000,coef(b),b$Vp) ## 1000 replicate param. vectors
res <- rep(0,1000)
for (i in 1:1000)
{ pr <- Xp %*% br[i,] ## replicate predictions
  res[i] <- sum(log(abs(pr))) ## example non-linear function
}
mean(res);var(res)

## loop is replace-able by following ....

res <- colSums(log(abs(Xp %*% t(br))))

#####
# illustration of unsafe scale dependent transforms in smooths...
#####

b0 <- gam(y~s(x0)+s(x1)+s(x2)+x3,data=dat) ## safe
b1 <- gam(y~s(x0)+s(I(x1/2))+s(x2)+scale(x3),data=dat) ## safe
b2 <- gam(y~s(x0)+s(scale(x1))+s(x2)+scale(x3),data=dat) ## unsafe
pd <- dat; pd$x1 <- pd$x1/2; pd$x3 <- pd$x3/2
par(mfrow=c(1,2))
plot(predict(b0,pd),predict(b1,pd),main="b0 and b1 predictions match")
abline(0,1,col=2)
plot(predict(b0,pd),predict(b2,pd),main="b2 unsafe, doesn't match")
abline(0,1,col=2)

#####

```

```

## The following shows how to use an "lpmatrix" as a lookup
## table for approximate prediction. The idea is to create
## approximate prediction matrix rows by appropriate linear
## interpolation of an existing prediction matrix. The additivity
## of a GAM makes this possible.
## There is no reason to ever do this in R, but the following
## code provides a useful template for predicting from a fitted
## gam *outside* R: all that is needed is the coefficient vector
## and the prediction matrix. Use larger `Xp`/ smaller `dx` and/or
## higher order interpolation for higher accuracy.
#####

xn <- c(.341,.122,.476,.981) ## want prediction at these values
x0 <- 1      ## intercept column
dx <- 1/30   ## covariate spacing in `newd`
for (j in 0:2) { ## loop through smooth terms
  cols <- 1+j*9 +1:9      ## relevant cols of Xp
  i <- floor(xn[j+1]*30) ## find relevant rows of Xp
  w1 <- (xn[j+1]-i*dx)/dx ## interpolation weights
  ## find approx. predict matrix row portion, by interpolation
  x0 <- c(x0,Xp[i+2,cols]*w1 + Xp[i+1,cols]*(1-w1))
}
dim(x0)<-c(1,28)
fv <- x0%*%coef(b) + xn[4];fv ## evaluate and add offset
se <- sqrt(x0%*%b$Vp%*%t(x0));se ## get standard error
## compare to normal prediction
predict(b,newdata=data.frame(x0=xn[1],x1=xn[2],
                             x2=xn[3],x3=xn[4]),se=TRUE)

#####
## Differentiating the smooths in a model (with CIs for derivatives)
#####

## simulate data and fit model...
dat <- gamSim(1,n=300,scale=sig)
b<-gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat)
plot(b,pages=1)

## now evaluate derivatives of smooths with associated standard
## errors, by finite differencing...
x.mesh <- seq(0,1,length=200) ## where to evaluate derivatives
newd <- data.frame(x0 = x.mesh,x1 = x.mesh, x2=x.mesh,x3=x.mesh)
X0 <- predict(b,newd,type="lpmatrix")

eps <- 1e-7 ## finite difference interval
x.mesh <- x.mesh + eps ## shift the evaluation mesh
newd <- data.frame(x0 = x.mesh,x1 = x.mesh, x2=x.mesh,x3=x.mesh)
X1 <- predict(b,newd,type="lpmatrix")

Xp <- (X1-X0)/eps ## maps coefficients to (fd approx.) derivatives
colnames(Xp)      ## can check which cols relate to which smooth

par(mfrow=c(2,2))

```

```

for (i in 1:4) { ## plot derivatives and corresponding CIs
  Xi <- Xp*0
  Xi[, (i-1)*9+1:9+1] <- Xp[, (i-1)*9+1:9+1] ## Xi%%coef(b) = smooth deriv i
  df <- Xi%%coef(b) ## ith smooth derivative
  df.sd <- rowSums(Xi%%b$Vp*Xi)^.5 ## cheap diag(Xi%%b$Vp%%t(Xi))^ .5
  plot(x.mesh, df, type="l", ylim=range(c(df+2*df.sd, df-2*df.sd)))
  lines(x.mesh, df+2*df.sd, lty=2); lines(x.mesh, df-2*df.sd, lty=2)
}

```

 Predict.matrix

Prediction methods for smooth terms in a GAM

Description

Takes smooth objects produced by `smooth.construct` methods and obtains the matrix mapping the parameters associated with such a smooth to the predicted values of the smooth at a set of new covariate values.

In practice this method is often called via the wrapper function [PredictMat](#).

Usage

```

Predict.matrix(object, data)
Predict.matrix2(object, data)

```

Arguments

object	is a smooth object produced by a <code>smooth.construct</code> method function. The object contains all the information required to specify the basis for a term of its class, and this information is used by the appropriate <code>Predict.matrix</code> function to produce a prediction matrix for new covariate values. Further details are given in smooth.construct .
data	A data frame containing the values of the (named) covariates at which the smooth term is to be evaluated. Exact requirements are as for smooth.construct and <code>smooth.construct2</code> .

Details

Smooth terms in a GAM formula are turned into smooth specification objects of class `xx.smooth.spec` during processing of the formula. Each of these objects is converted to a smooth object using an appropriate `smooth.construct` function. The `Predict.matrix` functions are used to obtain the matrix that will map the parameters associated with a smooth term to the predicted values for the term at new covariate values.

Note that new smooth classes can be added by writing a new `smooth.construct` method function and a corresponding `Predict.matrix` method function: see the example code provided for [smooth.construct](#) for details.

Value

A matrix which will map the parameters associated with the smooth to the vector of values of the smooth evaluated at the covariate values given in object. If the smooth class is one which generates offsets the corresponding offset is returned as attribute "offset" of the matrix.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

See Also

[gam](#), [gamm](#), [smooth.construct](#), [PredictMat](#)

Examples

```
# See smooth.construct examples
```

```
Predict.matrix.cr.smooth
```

Predict matrix method functions

Description

The various built in smooth classes for use with [gam](#) have associate [Predict.matrix](#) method functions to enable prediction from the fitted model.

Usage

```
## S3 method for class 'cr.smooth'
Predict.matrix(object, data)
## S3 method for class 'cs.smooth'
Predict.matrix(object, data)
## S3 method for class 'cyclic.smooth'
Predict.matrix(object, data)
## S3 method for class 'pspline.smooth'
Predict.matrix(object, data)
## S3 method for class 'tensor.smooth'
Predict.matrix(object, data)
## S3 method for class 'tprs.smooth'
Predict.matrix(object, data)
## S3 method for class 'ts.smooth'
Predict.matrix(object, data)
## S3 method for class 't2.smooth'
Predict.matrix(object, data)
```

Arguments

object	a smooth object, usually generated by a <code>smooth.construct</code> method having processed a smooth specification object generated by an <code>s</code> or <code>te</code> term in a <code>gam</code> formula.
data	A data frame containing the values of the (named) covariates at which the smooth term is to be evaluated. Exact requirements are as for <code>smooth.construct</code> and <code>smooth.construct2</code> .

Details

The Predict matrix function is not normally called directly, but is rather used internally by `predict.gam` etc. to predict from a fitted `gam` model. See `Predict.matrix` for more details, or the specific `smooth.construct` pages for details on a particular smooth class.

Value

A matrix mapping the coefficients for the smooth term to its values at the supplied data values.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

Examples

```
## see smooth.construct
```

Predict.matrix.soap.film

Prediction matrix for soap film smooth

Description

Creates a prediction matrix for a soap film smooth object, mapping the coefficients of the smooth to the linear predictor component for the smooth. This is the `Predict.matrix` method function required by `gam`.

Usage

```
## S3 method for class 'soap.film'
Predict.matrix(object,data)
## S3 method for class 'sw'
Predict.matrix(object,data)
## S3 method for class 'sf'
Predict.matrix(object,data)
```

Arguments

object	A class "soap.film", "sf" or "sw" object.
data	A list list or data frame containing the arguments of the smooth at which predictions are required.

Details

The smooth object will be largely what is returned from [smooth.construct.so.smooth.spec](#), although elements X and S are not needed, and need not be present, of course.

Value

A matrix. This may have an "offset" attribute corresponding to the contribution from any known boundary conditions on the smooth.

Author(s)

Simon N. Wood <s.wood@bath.ac.uk>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[smooth.construct.so.smooth.spec](#)

Examples

```
## This is a lower level example. The basis and
## penalties are obtained explicitly
## and `magic` is used as the fitting routine...

require(mgcv)
set.seed(66)

## create a boundary...
fsb <- list(fs.boundary())

## create some internal knots...
knots <- data.frame(x=rep(seq(-.5,3,by=.5),4),
```



```

y=rep(c(-.6,-.3,.3,.6),rep(8,4))

## Simulate some fitting data, inside boundary...
n<-1000
x <- runif(n)*5-1;y<-runif(n)*2-1
z <- fs.test(x,y,b=1)
ind <- inSide(fsb,x,y) ## remove outsiders
z <- z[ind];x <- x[ind]; y <- y[ind]
n <- length(z)
z <- z + rnorm(n)*.3 ## add noise

## plot boundary with knot and data locations
plot(fsb[[1]]$x,fsb[[1]]$y,type="l");points(knots$x,knots$y,pch=20,col=2)
points(x,y,pch=".",col=3);

## set up the basis and penalties...
sob <- smooth.construct2(s(x,y,bs="so",k=40,xt=list(bnd=fsb,nmax=100)),
                        data=data.frame(x=x,y=y),knots=knots)
## ... model matrix is element 'X' of sob, penalties matrices
## are in list element 'S'.

## fit using 'magic'
um <- magic(z,sob$X,sp=c(-1,-1),sob$S,off=c(1,1))
beta <- um$b

## produce plots...
par(mfrow=c(2,2),mar=c(4,4,1,1))
m<-100;n<-50
xm <- seq(-1,3.5,length=m);yn<-seq(-1,1,length=n)
xx <- rep(xm,n);yy<-rep(yn,rep(m,n))

## plot truth...
tru <- matrix(fs.test(xx,yy),m,n) ## truth
image(xm,yn,tru,col=heat.colors(100),xlab="x",ylab="y")
lines(fsb[[1]]$x,fsb[[1]]$y,lwd=3)
contour(xm,yn,tru,levels=seq(-5,5,by=.25),add=TRUE)

## Plot soap, by first predicting on a fine grid...

## First get prediction matrix...
X <- Predict.matrix2(sob,data=list(x=xx,y=yy))

## Now the predictions...
fv <- X%*%beta

## Plot the estimated function...
image(xm,yn,matrix(fv,m,n),col=heat.colors(100),xlab="x",ylab="y")
lines(fsb[[1]]$x,fsb[[1]]$y,lwd=3)
points(x,y,pch=".")
contour(xm,yn,matrix(fv,m,n),levels=seq(-5,5,by=.25),add=TRUE)

## Plot TPRS...
b <- gam(z~s(x,y,k=100))

```

```
fv.gam <- predict(b,newdata=data.frame(x=xx,y=yy))
names(sob$sd$bnd[[1]]) <- c("xx","yy","d")
ind <- inSide(sob$sd$bnd,xx,yy)
fv.gam[!ind]<-NA
image(xm,yn,matrix(fv.gam,m,n),col=heat.colors(100),xlab="x",ylab="y")
lines(fsb[[1]]$x,fsb[[1]]$y,lwd=3)
points(x,y,pch=".")
contour(xm,yn,matrix(fv.gam,m,n),levels=seq(-5,5,by=.25),add=TRUE)
```

print.gam

Print a Generalized Additive Model object.

Description

The default print method for a gam object.

Usage

```
## S3 method for class 'gam'
print(x, ...)
```

Arguments

x, ... fitted model objects of class gam as produced by gam().

Details

Prints out the family, model formula, effective degrees of freedom for each smooth term, and optimized value of the smoothness selection criterion used. See [gamObject](#) (or `names(x)`) for a listing of what the object contains. [summary.gam](#) provides more detail.

Note that the optimized smoothing parameter selection criterion reported is one of GCV, UBRE(AIC), GACV, negative log marginal likelihood (ML), or negative log restricted likelihood (REML).

If rank deficiency of the model was detected then the apparent rank is reported, along with the length of the coefficient vector (rank in absence of rank deficiency). Rank deficiency occurs when not all coefficients are identifiable given the data. Although the fitting routines (except `gamm`) deal gracefully with rank deficiency, interpretation of rank deficient models may be difficult.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) Generalized Additive Models: An Introduction with R. CRC/ Chapman and Hall, Boca Raton, Florida.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also[gam](#), [summary.gam](#)

qq.gam	<i>QQ plots for gam model residuals</i>
--------	---

Description

Takes a fitted gam object produced by `gam()` and produces QQ plots of its residuals (conditional on the fitted model coefficients and scale parameter). If the model distributional assumptions are met then usually these plots should be close to a straight line (although discrete data can yield marked random departures from this line).

Usage

```
qq.gam(object, rep=0, level=.9, s.rep=10,
        type=c("deviance", "pearson", "response"),
        pch=".", rl.col=2, rep.col="gray80", ...)
```

Arguments

<code>object</code>	a fitted gam object as produced by <code>gam()</code> (or a <code>glm</code> object).
<code>rep</code>	How many replicate datasets to generate to simulate quantiles of the residual distribution. 0 results in an efficient simulation free method for direct calculation, if this is possible for the object family.
<code>level</code>	If simulation is used for the quantiles, then reference intervals can be provided for the QQ-plot, this specifies the level. 0 or less for no intervals, 1 or more to simply plot the QQ plot for each replicate generated.
<code>s.rep</code>	how many times to randomize uniform quantiles to data under direct computation.
<code>type</code>	what sort of residuals should be plotted? See residuals.gam .
<code>pch</code>	plot character to use. 19 is good.
<code>rl.col</code>	color for the reference line on the plot.
<code>rep.col</code>	color for reference bands or replicate reference plots.
<code>...</code>	extra graphics parameters to pass to plotting functions.

Details

QQ-plots of the the model residuals can be produced in one of two ways. The cheapest method generates reference quantiles by associating a quantile of the uniform distribution with each datum, and feeding these uniform quantiles into the quantile function associated with each datum. The resulting quantiles are then used in place of each datum to generate approximate quantiles of residuals. The residual quantiles are averaged over `s.rep` randomizations of the uniform quantiles to data.

The second method is to use direct simulation. For each replicate, data are simulated from the fitted model, and the corresponding residuals computed. This is repeated `rep` times. Quantiles are readily obtained from the empirical distribution of residuals so obtained. From this method reference bands are also computable.

Even if `rep` is set to zero, the routine will attempt to simulate quantiles if no quantile function is available for the family. If no random deviate generating function family is available (e.g. for the quasi families), then a normal QQ-plot is produced. The routine conditions on the fitted model coefficients and the scale parameter estimate.

The plots are very similar to those proposed in Ben and Yohai (2004), but are substantially cheaper to produce (the interpretation of residuals for binary data in Ben and Yohai is not recommended).

Note that plots for raw residuals from fits to binary data contain almost no useful information about model fit. Whether the residual is negative or positive is decided by whether the response is zero or one. The magnitude of the residual, given its sign, is determined entirely by the fitted values. In consequence only the most gross violations of the model are detectable from QQ-plots of residuals for binary data. To really check distributional assumptions from residuals for binary data you have to be able to group the data somehow. Binomial models other than binary are ok.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

N.H. Augustin, E-A Sauleaub, S.N. Wood (2012) On quantile quantile plots for generalized linear models *Computational Statistics & Data Analysis*. 56(8), 2404-2409.

M.G. Ben and V.J. Yohai (2004) *JCGS* 13(1), 36-47.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[choose.k](#), [gam](#)

Examples

```
library(mgcv)
## simulate binomial data...
set.seed(0)
n.samp <- 400
dat <- gamSim(1,n=n.samp,dist="binary",scale=.33)
p <- binomial()$linkinv(dat$f) ## binomial p
n <- sample(c(1,3),n.samp,replace=TRUE) ## binomial n
dat$y <- rbinom(n,n,p)
dat$n <- n

lr.fit <- gam(y/n~s(x0)+s(x1)+s(x2)+s(x3)
             ,family=binomial,data=dat,weights=n,method="REML")

par(mfrow=c(2,2))
```

```

## normal QQ-plot of deviance residuals
qqnorm(residuals(lr.fit),pch=19,cex=.3)
## Quick QQ-plot of deviance residuals
qq.gam(lr.fit,pch=19,cex=.3)
## Simulation based QQ-plot with reference bands
qq.gam(lr.fit,rep=100,level=.9)
## Simulation based QQ-plot, Pearson resid, all
## simulated reference plots shown...
qq.gam(lr.fit,rep=100,level=1,type="pearson",pch=19,cex=.2)

## Now fit the wrong model and check...

pif <- gam(y~s(x0)+s(x1)+s(x2)+s(x3)
           ,family=poisson,data=dat,method="REML")
par(mfrow=c(2,2))
qqnorm(residuals(pif),pch=19,cex=.3)
qq.gam(pif,pch=19,cex=.3)
qq.gam(pif,rep=100,level=.9)
qq.gam(pif,rep=100,level=1,type="pearson",pch=19,cex=.2)

## Example of binary data model violation so gross that you see a problem
## on the QQ plot...

y <- c(rep(1,10),rep(0,20),rep(1,40),rep(0,10),rep(1,40),rep(0,40))
x <- 1:160
b <- glm(y~x,family=binomial)
par(mfrow=c(2,2))
## Note that the next two are not necessarily similar under gross
## model violation...
qq.gam(b)
qq.gam(b,rep=50,level=1)
## and a much better plot for detecting the problem
plot(x,residuals(b),pch=19,cex=.3)
plot(x,y);lines(x,fitted(b))

## alternative model
b <- gam(y~s(x,k=5),family=binomial,method="ML")
qq.gam(b)
qq.gam(b,rep=50,level=1)
plot(x,residuals(b),pch=19,cex=.3)
plot(b,residuals=TRUE,pch=19,cex=.3)

```

Description

The smooth components of GAMs can be viewed as random effects for estimation purposes. This means that more conventional random effects terms can be incorporated into GAMs in two ways.

The first method converts all the smooths into fixed and random components suitable for estimation by standard mixed modelling software. Once the GAM is in this form then conventional random effects are easily added, and the whole model is estimated as a general mixed model. `gamm` and `gamm4` from the `gamm4` package operate in this way.

The second method represents the conventional random effects in a GAM in the same way that the smooths are represented — as penalized regression terms. This method can be used with `gam` by making use of `s(...,bs="re")` terms in a model: see `smooth.construct.re.smooth.spec`, for full details. The basic idea is that, e.g., `s(x,z,g,bs="re")` generates an i.i.d. Gaussian random effect with model matrix given by `model.matrix(~x:z:g-1)` — in principle such terms can take any number of arguments. This simple approach is sufficient for implementing a wide range of commonly used random effect structures. For example if `g` is a factor then `s(g,bs="re")` produces a random coefficient for each level of `g`, with the random coefficients all modelled as i.i.d. normal. If `g` is a factor and `x` is numeric, then `s(x,g,bs="re")` produces an i.i.d. normal random slope relating the response to `x` for each level of `g`. If `h` is another factor then `s(h,g,bs="re")` produces the usual i.i.d. normal `g - h` interaction. Note that a rather useful approximate test for zero random effect is also implemented for such terms based on Wood (2013). If the precision matrix is known to within a multiplicative constant, then this can be supplied via the `xt` argument of `s`. See `smooth.construct.re.smooth.spec` for details and example.

Alternatively, but less straightforwardly, the `paraPen` argument to `gam` can be used: see `gam.models`. If smoothing parameter estimation is by ML or REML (e.g. `gam(...,method="REML")`) then this approach is a completely conventional likelihood based treatment of random effects.

`gam` can be slow for fitting models with large numbers of random effects, because it does not exploit the sparsity that is often a feature of parametric random effects. It can not be used for models with more coefficients than data. However `gam` is often faster and more reliable than `gamm` or `gamm4`, when the number of random effects is modest.

To facilitate the use of random effects with `gam`, `gam.vcomp` is a utility routine for converting smoothing parameters to variance components. It also provides confidence intervals, if smoothness estimation is by ML or REML.

Note that treating random effects as smooths does not remove the usual problems associated with testing variance components for equality to zero: see `summary.gam` and `anova.gam`.

Author(s)

Simon Wood <simon.wood@r-project.org>

References

- Wood, S.N. (2013) A simple test for random effects in regression models. *Biometrika* 100:1005-1010
- Wood, S.N. (2011) Fast stable restricted maximum likelihood and marginal likelihood estimation of semiparametric generalized linear models. *Journal of the Royal Statistical Society (B)* 73(1):3-36
- Wood, S.N. (2008) Fast stable direct fitting and smoothness selection for generalized additive models. *Journal of the Royal Statistical Society (B)* 70(3):495-518
- Wood, S.N. (2006) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

See Also

[gam.vcomp](#), [gam.models](#), [smooth.terms](#), [smooth.construct.re.smooth.spec](#), [gamm](#)

Examples

```
## see also examples for gam.models, gam.vcomp, gamm
## and smooth.construct.re.smooth.spec

## simple comparison of lme and gam
require(mgcv)
require(nlme)
b0 <- lme(travel~1,data=Rail,~1|Rail,method="REML")

b <- gam(travel~s(Rail,bs="re"),data=Rail,method="REML")

intervals(b0)
gam.vcomp(b)
anova(b)

## simulate example...
dat <- gamSim(1,n=400,scale=2) ## simulate 4 term additive truth

fac <- as.factor(sample(1:20,400,replace=TRUE))
dat$X <- model.matrix(~fac-1)
b <- rnorm(20)*.5
dat$y <- dat$y + dat$X%*%b

rm1 <- gam(y ~ s(fac,bs="re")+s(x0)+s(x1)+s(x2)+s(x3),data=dat,method="ML")
gam.vcomp(rm1)

fv0 <- predict(rm1,exclude="s(fac)") ## predictions setting r.e. to 0
fv1 <- predict(rm1) ## predictions setting r.e. to predicted values
```

residuals.gam

Generalized Additive Model residuals

Description

Returns residuals for a fitted gam model object. Pearson, deviance, working and response residuals are available.

Usage

```
## S3 method for class 'gam'
residuals(object, type = "deviance",...)
```

Arguments

object	a gam fitted model object.
type	the type of residuals wanted. Usually one of "deviance", "pearson", "scaled.pearson", "working", or "response".
...	other arguments.

Details

Response residuals are the raw residuals (data minus fitted values). Scaled Pearson residuals are raw residuals divided by the standard deviation of the data according to the model mean variance relationship and estimated scale parameter. Pearson residuals are the same, but multiplied by the square root of the scale parameter (so they are independent of the scale parameter): $((y-\mu)/\sqrt{V(\mu)})$, where y is data μ is model fitted value and V is model mean-variance relationship.). Both are provided since not all texts agree on the definition of Pearson residuals. Deviance residuals simply return the deviance residuals defined by the model family. Working residuals are the residuals returned from model fitting at convergence.

Families can supply their own residual function, which is used in place of the standard function if present, (e.g. [cox.ph](#)).

Value

A vector of residuals.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam](#)

rig	<i>Generate inverse Gaussian random deviates</i>
-----	--

Description

Generates inverse Gaussian random deviates.

Usage

```
rig(n, mean, scale)
```

Arguments

n	the number of deviates required. If this has length > 1 then the length is taken as the number of deviates required.
mean	vector of mean values.
scale	vector of scale parameter values (lambda, see below)

Details

If x is the returned vector, then $E(x) = \text{mean}$ while $\text{var}(x) = \text{scale} * \text{mean}^3$. For density and distribution functions see the `statmod` package. The algorithm used is Algorithm 5.7 of Gentle (2003), based on Michael et al. (1976). Note that `scale` here is the scale parameter in the GLM sense, which is the reciprocal of the usual ‘lambda’ parameter.

Value

A vector of inverse Gaussian random deviates.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Gentle, J.E. (2003) *Random Number Generation and Monte Carlo Methods* (2nd ed.) Springer.

Michael, J.R., W.R. Schucany & R.W. Hass (1976) Generating random variates using transformations with multiple roots. *The American Statistician* 30, 88-90.

<http://www.maths.bris.ac.uk/~sw15190/>

Examples

```
require(mgcv)
set.seed(7)
## An inverse.gaussian GAM example, by modify `gamSim' output...
dat <- gamSim(1,n=400,dist="normal",scale=1)
dat$f <- dat$f/4 ## true linear predictor
Ey <- exp(dat$f);scale <- .5 ## mean and GLM scale parameter
## simulate inverse Gaussian response...
dat$y <- rig(Ey,mean=Ey,scale=.2)
big <- gam(y~ s(x0)+ s(x1)+s(x2)+s(x3),family=inverse.gaussian(link=log),
          data=dat,method="REML")
plot(big,pages=1)
gam.check(big)
summary(big)
```

 rmvn

Generate multivariate normal deviates

Description

Generates multivariate normal random deviates.

Usage

```
rmvn(n, mu, V)
```

Arguments

n	number of simulated vectors required.
mu	the mean of the vectors: either a single vector of length $p = \text{ncol}(V)$ or an n by p matrix.
V	A positive semi definite covariance matrix.

Details

Uses a ‘square root’ of V to transform standard normal deviates to multivariate normal with the correct covariance matrix.

Value

An n row matrix, with each row being a draw from a multivariate normal density with covariance matrix V and mean vector μ . Alternatively each row may have a different mean vector if μ is a vector.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[ldTweedie](#), [Tweedie](#)

Examples

```
library(mgcv)
V <- matrix(c(2,1,1,2),2,2)
mu <- c(1,3)
n <- 1000
z <- rmvn(n,mu,V)
crossprod(sweep(z,2,colMeans(z)))/n ## observed covariance matrix
colMeans(z) ## observed mu
```

Rrank

Find rank of upper triangular matrix

Description

Finds rank of upper triangular matrix R , by estimating condition number of upper rank by rank block, and reducing rank until this is acceptably low. Assumes R has been computed by a method that uses pivoting, usually pivoted QR or Choleski.

Usage

```
Rrank(R, tol=.Machine$double.eps^.9)
```

Arguments

R An upper triangular matrix, obtained by pivoted QR or pivoted Choleski.
tol the tolerance to use for judging rank.

Details

The method is based on Cline et al. (1979) as described in Golub and van Loan (1996).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Cline, A.K., C.B. Moler, G.W. Stewart and J.H. Wilkinson (1979) An estimate for the condition number of a matrix. SIAM J. Num. Anal. 16, 368-375

Golub, G.H, and C.F. van Loan (1996) Matrix Computations 3rd ed. Johns Hopkins University Press, Baltimore.

Examples

```
set.seed(0)
n <- 10;p <- 5
X <- matrix(runif(n*(p-1)),n,p)
qrx <- qr(X,LAPACK=TRUE)
Rrank(qr.R(qrx))
```

rTweedie

Generate Tweedie random deviates

Description

Generates Tweedie random deviates, for powers between 1 and 2.

Usage

```
rTweedie(mu,p=1.5,phi=1)
```

Arguments

mu vector of expected values for the deviates to be generated. One deviate generated for each element of mu.
p the variance of a deviate is proportional to its mean, mu to the power p. p must be between 1 and 2. 1 is Poisson like (exactly Poisson if phi=1), 2 is gamma.
phi The scale parameter. Variance of the deviates is given by is $\phi * \mu^p$.

Details

A Tweedie random variable with $1 < p < 2$ is a sum of N gamma random variables where N has a Poisson distribution, with mean $\mu^{(2-p)/((2-p)*\phi)}$. The Gamma random variables that are summed have shape parameter $(2-p)/(p-1)$ and scale parameter $\phi*(p-1)*\mu^{(p-1)}$ (note that this scale parameter is different from the scale parameter for a GLM with Gamma errors).

This is a restricted, but faster, version of `rtweedie` from the `tweedie` package.

Value

A vector of random deviates from a Tweedie distribution, expected value vector μ , variance vector $\phi*\mu^p$.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Peter K Dunn (2009). `tweedie`: Tweedie exponential family models. R package version 2.0.2. <https://cran.r-project.org/package=tweedie>

See Also

[ldTweedie](#), [Tweedie](#)

Examples

```
library(mgcv)
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
  (10 * x)^3 * (1 - x)^10
n <- 300
x <- runif(n)
mu <- exp(f2(x)/3+1.1); x <- x*10 - 4
y <- rTweedie(mu, p=1.5, phi=1.3)
b <- gam(y~s(x, k=20), family=Tweedie(p=1.5))
b
plot(b)
```

Description

Function used in definition of smooth terms within `gam` model formulae. The function does not evaluate a (spline) smooth - it exists purely to help set up a model using spline based smooths.

Usage

```
s(..., k=-1, fx=FALSE, bs="tp", m=NA, by=NA, xt=NULL, id=NULL, sp=NULL, pc=NULL)
```

Arguments

- `...` a list of variables that are the covariates that this smooth is a function of. Transformations whose form depends on the values of the data are best avoided here: e.g. `s(log(x))` is fine, but `s(I(x/sd(x)))` is not (see [predict.gam](#)).
- `k` the dimension of the basis used to represent the smooth term. The default depends on the number of variables that the smooth is a function of. `k` should not be less than the dimension of the null space of the penalty for the term (see [null.space.dimension](#)), but will be reset if it is. See [choose.k](#) for further information.
- `fx` indicates whether the term is a fixed d.f. regression spline (TRUE) or a penalized regression spline (FALSE).
- `bs` a two letter character string indicating the (penalized) smoothing basis to use. (eg "tp" for thin plate regression spline, "cr" for cubic regression spline). see [smooth.terms](#) for an overview of what is available.
- `m` The order of the penalty for this term (e.g. 2 for normal cubic spline penalty with 2nd derivatives when using default t.p.r.s basis). NA signals autoinitialization. Only some smooth classes use this. The "ps" class can use a 2 item array giving the basis and penalty order separately.
- `by` a numeric or factor variable of the same dimension as each covariate. In the numeric vector case the elements multiply the smooth, evaluated at the corresponding covariate values (a 'varying coefficient model' results). For the numeric by variable case the resulting smooth is not usually subject to a centering constraint (so the `by` variable should not be added as an additional main effect). In the factor by variable case a replicate of the smooth is produced for each factor level (these smooths will be centered, so the factor usually needs to be added as a main effect as well). See [gam.models](#) for further details. A by variable may also be a matrix if covariates are matrices: in this case implements linear functional of a smooth (see [gam.models](#) and [linear.functional.terms](#) for details).
- `xt` Any extra information required to set up a particular basis. Used e.g. to set large data set handling behaviour for "tp" basis.
- `id` A label or integer identifying this term in order to link its smoothing parameters to others of the same type. If two or more terms have the same `id` then they will have the same smoothing parameters, and, by default, the same bases (first occurrence defines basis type, but data from all terms used in basis construction). An `id` with a factor by variable causes the smooths at each factor level to have the same smoothing parameter.
- `sp` any supplied smoothing parameters for this term. Must be an array of the same length as the number of penalties for this smooth. Positive or zero elements are taken as fixed smoothing parameters. Negative elements signal autoinitialization. Over-rides values supplied in `sp` argument to [gam](#). Ignored by [gamm](#).

pc If not NULL, signals a point constraint: the smooth should pass through zero at the point given here (as a vector or list with names corresponding to the smooth names). Never ignored if supplied. See [identifiability](#).

Details

The function does not evaluate the variable arguments. To use this function to specify use of your own smooths, note the relationships between the inputs and the output object and see the example in [smooth.construct](#).

Value

A class `xx.smooth.spec` object, where `xx` is a basis identifying code given by the `bs` argument of `s`. These `smooth.spec` objects define smooths and are turned into bases and penalties by `smooth.construct` method functions.

The returned object contains the following items:

term	An array of text strings giving the names of the covariates that the term is a function of.
bs.dim	The dimension of the basis used to represent the smooth.
fixed	TRUE if the term is to be treated as a pure regression spline (with fixed degrees of freedom); FALSE if it is to be treated as a penalized regression spline
dim	The dimension of the smoother - i.e. the number of covariates that it is a function of.
p.order	The order of the t.p.r.s. penalty, or 0 for auto-selection of the penalty order.
by	is the name of any by variable as text ("NA" for none).
label	A suitable text label for this smooth term.
xt	The object passed in as argument <code>xt</code> .
id	An identifying label or number for the smooth, linking it to other smooths. Defaults to NULL for no linkage.
sp	array of smoothing parameters for the term (negative for auto-estimation). Defaults to NULL.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2003) Thin plate regression splines. *J.R.Statist.Soc.B* 65(1):95-114
 Wood S.N. (2006) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.
<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[te](#), [gam](#), [gamm](#)

Examples

```

# example utilising `by' variables
library(mgcv)
set.seed(0)
n<-200;sig2<-4
x1 <- runif(n, 0, 1);x2 <- runif(n, 0, 1);x3 <- runif(n, 0, 1)
fac<-c(rep(1,n/2),rep(2,n/2)) # create factor
fac.1<-rep(0,n)+(fac==1);fac.2<-1-fac.1 # and dummy variables
fac<-as.factor(fac)
f1 <- exp(2 * x1) - 3.75887
f2 <- 0.2 * x1^11 * (10 * (1 - x1))^6 + 10 * (10 * x1)^3 * (1 - x1)^10
f<-f1*fac.1+f2*fac.2+x2
e <- rnorm(n, 0, sqrt(abs(sig2)))
y <- f + e
# NOTE: smooths will be centered, so need to include fac in model...
b<-gam(y~fac+s(x1,by=fac)+x2)
plot(b,pages=1)

```

scat

*GAM scaled t family for heavy tailed data***Description**

Family for use with [gam](#), implementing regression for the heavy tailed response variables, y , using a scaled t model. The idea is that $(y - \mu)/\sigma \sim t_\nu$ where μ is determined by a linear predictor, while σ and ν are parameters to be estimated alongside the smoothing parameters.

Usage

```
scat(theta = NULL, link = "identity")
```

Arguments

theta the parameters to be estimated $\nu = 2 + \exp(\theta_1)$ and $\sigma = \exp(\theta_2)$. If supplied and positive, then taken to be fixed values of ν and σ . If any negative, then absolute values taken as starting values.

link The link function: one of "identity", "log" or "inverse".

Details

Useful in place of Gaussian, when data are heavy tailed.

Value

An object of class `extended.family`.

Author(s)

Natalya Pya (nyp20@bath.ac.uk)

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. Journal of the American Statistical Association. <http://arxiv.org/abs/1511.03864>

Examples

```
library(mgcv)
## Simulate some t data...
set.seed(3);n<-400
dat <- gamSim(1,n=n)
dat$y <- dat$f + rt(n,df=3)*2

b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=scat(link="identity"),data=dat)

b
plot(b,pages=1)
```

sdiag

Extract or modify diagonals of a matrix

Description

Extracts or modifies sub- or super- diagonals of a matrix.

Usage

```
sdiag(A,k=0)
sdiag(A,k=0) <- value
```

Arguments

A	a matrix
k	sub- (negative) or super- (positive) diagonal of a matrix. 0 is the leading diagonal.
value	single value, or vector of the same length as the diagonal.

Value

A vector containing the requested diagonal, or a matrix with the requested diagonal replaced by value.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Examples

```
require(mgcv)
A <- matrix(1:35,7,5)
A
sdiag(A,1) ## first super diagonal
sdiag(A,-1) ## first sub diagonal

sdiag(A) <- 1 ## leading diagonal set to 1
sdiag(A,3) <- c(-1,-2) ## set 3rd super diagonal
```

single.index

*Single index models with mgcv***Description**

Single index models contain smooth terms with arguments that are linear combinations of other covariates. e.g. $s(X\alpha)$ where α has to be estimated. For identifiability, assume $\|\alpha\| = 1$ with positive first element. One simple way to fit such models is to use `gam` to profile out the smooth model coefficients and smoothing parameters, leaving only the α to be estimated by a general purpose optimizer.

Example code is provided below, which can be easily adapted to include multiple single index terms, parametric terms and further smooths. Note the initialization strategy. First estimate α without penalization to get starting values and then do the full fit. Otherwise it is easy to get trapped in a local optimum in which the smooth is linear. An alternative is to initialize using fixed penalization (via the `sp` argument to `gam`).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Examples

```
require(mgcv)

si <- function(theta,y,x,z,opt=TRUE,k=10,fx=FALSE) {
  ## Fit single index model using gam call, given theta (defines alpha).
  ## Return ML if opt==TRUE and fitted gam with theta added otherwise.
  ## Suitable for calling from 'optim' to find optimal theta/alpha.
  alpha <- c(1,theta) ## constrained alpha defined using free theta
  kk <- sqrt(sum(alpha^2))
  alpha <- alpha/kk ## so now ||alpha||=1
  a <- x%%alpha ## argument of smooth
  b <- gam(y~s(a,fx=fx,k=k)+s(z),family=poisson,method="ML") ## fit model
  if (opt) return(b$gcv.ubre) else {
    b$alpha <- alpha ## add alpha
    J <- outer(alpha,-theta/kk^2) ## compute Jacobian
    for (j in 1:length(theta)) J[j+1,j] <- J[j+1,j] + 1/kk
  }
}
```

```

    b$J <- J ## dalpha_i/dtheta_j
    return(b)
  }
} ## si

## simulate some data from a single index model...

set.seed(1)
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
  (10 * x)^3 * (1 - x)^10
n <- 200; m <- 3
x <- matrix(runif(n*m), n, m) ## the covariates for the single index part
z <- runif(n) ## another covariate
alpha <- c(1, -1, .5); alpha <- alpha/sqrt(sum(alpha^2))
eta <- as.numeric(f2((x%*%alpha+.41)/1.4)+1+z^2*2)/4
mu <- exp(eta)
y <- rpois(n, mu) ## Poi response

## now fit to the simulated data...

th0 <- c(-.8, .4) ## close to truth for speed
## get initial theta, using no penalization...
f0 <- nlm(si, th0, y=y, x=x, z=z, fx=TRUE, k=5)
## now get theta/alpha with smoothing parameter selection...
f1 <- nlm(si, f0$estimate, y=y, x=x, z=z, hessian=TRUE, k=10)
theta.est <- f1$estimate

## Alternative using 'optim' ('Not run' simply to keep
## CRAN check time down)...
## Not run:
th0 <- rep(0, m-1)
## get initial theta, using no penalization...
f0 <- optim(th0, si, y=y, x=x, z=z, fx=TRUE, k=5)
## now get theta/alpha with smoothing parameter selection...
f1 <- optim(f0$par, si, y=y, x=x, z=z, hessian=TRUE, k=10)
theta.est <- f1$par

## End(Not run)
## extract and examine fitted model...

b <- si(theta.est, y, x, z, opt=FALSE) ## extract best fit model
plot(b, pages=1)
b
b$alpha
## get sd for alpha...
Vt <- b$J%*%solve(f1$hessian, t(b$J))
diag(Vt)^.5

```

Description

Uses Lanczos iteration to find the truncated eigen-decomposition of a symmetric matrix.

Usage

```
slanczos(A,k=10,k1=-1,tol=.Machine$double.eps^.5,nt=1)
```

Arguments

A	A symmetric matrix.
k	Must be non-negative. If k1 is negative, then the k largest magnitude eigenvalues are found, together with the corresponding eigenvectors. If k1 is non-negative then the k highest eigenvalues are found together with their eigenvectors and the k1 lowest eigenvalues with eigenvectors are also returned.
k1	If k1 is non-negative then the k1 lowest eigenvalues are returned together with their corresponding eigenvectors (in addition to the k highest eigenvalues + vectors). negative k1 signals that the k largest magnitude eigenvalues should be returned, with eigenvectors.
tol	tolerance to use for convergence testing of eigenvalues. Error in eigenvalues will be less than the magnitude of the dominant eigenvalue multiplied by tol (or the machine precision!).
nt	number of threads to use for leading order iterative multiplication of A by vector. May show no speed improvement on two processor machine.

Details

If k1 is non-negative, returns the highest k and lowest k1 eigenvalues, with their corresponding eigenvectors. If k1 is negative, returns the largest magnitude k eigenvalues, with corresponding eigenvectors.

The routine implements Lanczos iteration with full re-orthogonalization as described in Demmel (1997). Lanczos iteration iteratively constructs a tridiagonal matrix, the eigenvalues of which converge to the eigenvalues of A, as the iteration proceeds (most extreme first). Eigenvectors can also be computed. For small k and k1 the approach is faster than computing the full symmetric eigendecomposition. The tridiagonal eigenproblems are handled using LAPACK.

The implementation is not optimal: in particular the inner tridiagonal problems could be handled more efficiently, and there would be some savings to be made by not always returning eigenvectors.

Value

A list with elements values (array of eigenvalues); vectors (matrix with eigenvectors in its columns); iter (number of iterations required).

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Demmel, J. (1997) Applied Numerical Linear Algebra. SIAM

See Also

[cyclic.p.spline](#)

Examples

```
require(mgcv)
## create some x's and knots...
set.seed(1);
n <- 700; A <- matrix(runif(n*n),n,n); A <- A+t(A)

## compare timings of slanczos and eigen
system.time(er <- slanczos(A,10))
system.time(um <- eigen(A,symmetric=TRUE))

## confirm values are the same...
ind <- c(1:6,(n-3):n)
range(er$values-um$values[ind]); range(abs(er$vectors)-abs(um$vectors[,ind]))
```

smooth.construct

Constructor functions for smooth terms in a GAM

Description

Smooth terms in a GAM formula are turned into smooth specification objects of class `xx.smooth.spec` during processing of the formula. Each of these objects is converted to a smooth object using an appropriate `smooth.construct` function. New smooth classes can be added by writing a new `smooth.construct` method function and a corresponding `Predict.matrix` method function (see example code below).

In practice, `smooth.construct` is usually called via `smooth.construct2` and the wrapper function `smoothCon`, in order to handle by variables and centering constraints (see the `smoothCon` documentation if you need to handle these things directly, for a user defined smooth class).

Usage

```
smooth.construct(object,data,knots)
smooth.construct2(object,data,knots)
```

Arguments

`object` is a smooth specification object, generated by an `s` or `te` term in a GAM formula. Objects generated by `s` terms have class `xx.smooth.spec` where `xx` is given by the `bs` argument of `s` (this convention allows the user to add their own smoothers). If `object` is not class `tensor.smooth.spec` it will have the following elements:

- term** The names of the covariates for this smooth, in an array.
- bs.dim** Argument *k* of the *s* term generating the object. This is the dimension of the basis used to represent the term (or, arguably, 1 greater than the basis dimension for *cc* terms). *bs.dim*<0 indicates that the constructor should set this to the default value.
- fixed** TRUE if the term is to be unpenalized, otherwise FALSE.
- dim** the number covariates of which this smooth is a function.
- p.order** the order of the smoothness penalty or NA for autoselection of this. This is argument *m* of the *s* term that generated object.
- by** the name of any by variable to multiply this term as supplied as an argument to *s*. "NA" if there is no such term.
- label** A suitable label for use with this term.
- xt** An object containing information that may be needed for basis setup (used, e.g. by "tp" smooths to pass optional information on big dataset handling).
- id** Any identity associated with this term — used for linking bases and smoothing parameters. NULL by default, indicating no linkage.
- sp** Smoothing parameters for the term. Any negative are estimated, otherwise they are fixed at the supplied value. Unless NULL (default), over-rides *sp* argument to [gam](#).

If object is of class `tensor.smooth.spec` then it was generated by a *te* term in the GAM formula, and specifies a smooth of several variables with a basis generated as a tensor product of lower dimensional bases. In this case the object will be different and will have the following elements:

- margin** is a list of smooth specification objects of the type listed above, defining the bases which have their tensor product formed in order to construct this term.
- term** is the array of names of the covariates that are arguments of the smooth.
- by** is the name of any by variable, or "NA".
- fx** is an array, the elements of which indicate whether (TRUE) any of the margins in the tensor product should be unpenalized.
- label** A suitable label for use with this term.
- dim** is the number of covariates of which this smooth is a function.
- mp** TRUE if multiple penalties are to be used.
- np** TRUE if 1-D marginal smooths are to be re-parameterized in terms of function values.
- id** Any identity associated with this term — used for linking bases and smoothing parameters. NULL by default, indicating no linkage.
- sp** Smoothing parameters for the term. Any negative are estimated, otherwise they are fixed at the supplied value. Unless NULL (default), over-rides *sp* argument to [gam](#).

data

For `smooth.construct` a data frame or list containing the evaluation of the elements of `object$term`, with names given by `object$term`. The last entry will be the *by* variable, if `object$by` is not "NA". For `smooth.construct2` data need only be an object within which `object$term` can be evaluated, the variables can be in any order, and there can be irrelevant variables present as well.

`knots` an optional data frame or list containing the knots relating to `object$term`. If it is `NULL` then the knot locations are generated automatically. The structure of knots should be as for `data`, depending on whether `smooth.construct` or `smooth.construct2` is used.

Details

There are built in methods for objects with the following classes: `tp.smooth.spec` (thin plate regression splines: see [tprs](#)); `ts.smooth.spec` (thin plate regression splines with shrinkage-to-zero); `cr.smooth.spec` (cubic regression splines: see [cubic.regression.spline](#)); `cs.smooth.spec` (cubic regression splines with shrinkage-to-zero); `cc.smooth.spec` (cyclic cubic regression splines); `ps.smooth.spec` (Eilers and Marx (1986) style P-splines: see [p.spline](#)); `cp.smooth.spec` (cyclic P-splines); `ad.smooth.spec` (adaptive smooths of 1 or 2 variables: see [adaptive.smooth](#)); `re.smooth.spec` (simple random effect terms); `mrf.smooth.spec` (Markov random field smoothers for smoothing over discrete districts); `tensor.smooth.spec` (tensor product smooths).

There is an implicit assumption that the basis only depends on the knots and/or the set of unique covariate combinations; i.e. that the basis is the same whether generated from the full set of covariates, or just the unique combinations of covariates.

Plotting of smooths is handled by plot methods for smooth objects. A default `mgcv.smooth` method is used if there is no more specific method available. Plot methods can be added for specific smooth classes, see source code for `mgcv:::plot.sos.smooth`, `mgcv:::plot.random.effect`, `mgcv:::plot.mgcv.smooth` for example code.

Value

The input argument `object`, assigned a new class to indicate what type of smooth it is and with at least the following items added:

`X` The model matrix from this term. This may have an "offset" attribute: a vector of length `nrow(X)` containing any contribution of the smooth to the model offset term. `by` variables do not need to be dealt with here, but if they are then an item `by.done` must be added to the object.

`S` A list of positive semi-definite penalty matrices that apply to this term. The list will be empty if the term is to be left un-penalized.

`rank` An array giving the ranks of the penalties.

`null.space.dim` The dimension of the penalty null space (before centering).

The following items may be added:

`C` The matrix defining any identifiability constraints on the term, for use when fitting. If this is `NULL` then `smoothCon` will add an identifiability constraint that each term should sum to zero over the covariate values. Set to a zero row matrix if no constraints are required. If a supplied `C` has an attribute "always.apply" then it is never ignored, even if any `by` variables of a smooth imply that no constraint is actually needed. Code for creating `C` should check whether the specification object already contains a zero row matrix, and leave this unchanged if it is (since this signifies no constraint should be produced).

<code>Cp</code>	An optional matrix supplying alternative identifiability constraints for use when predicting. By default the fitting constraints are used. This option is useful when some sort of simple sparse constraint is required for fitting, but the usual sum-to-zero constraint is required for prediction so that, e.g. the CIs for model components are as narrow as possible.
<code>no.rescale</code>	if this is non-NULL then the penalty coefficient matrix of the smooth will not be rescaled for enhanced numerical stability (rescaling is the default, because <code>gamm</code> requires it). Turning off rescaling is useful if the values of the smoothing parameters should be interpretable in a model, for example because they are inverse variance components.
<code>df</code>	the degrees of freedom associated with this term (when unpenalized and unconstrained). If this is null then <code>smoothCon</code> will set it to the basis dimension. <code>smoothCon</code> will reduce this by the number of constraints.
<code>te.ok</code>	0 if this term should not be used as a tensor product marginal, 1 if it can be used and plotted, and 2 if it can be used but not plotted. Set to 1 if NULL.
<code>plot.me</code>	Set to FALSE if this smooth should not be plotted by <code>plot.gam</code> . Set to TRUE if NULL.
<code>side.constrain</code>	Set to FALSE to ensure that the smooth is never subject to side constraints as a result of nesting.
<code>L</code>	smooths may depend on fewer ‘underlying’ smoothing parameters than there are elements of <code>S</code> . In this case <code>L</code> is the matrix mapping the vector of underlying log smoothing parameters to the vector of logs of the smoothing parameters actually multiplying the <code>S[[i]]</code> . <code>L=NULL</code> signifies that there is one smoothing parameter per <code>S[[i]]</code> .

Usually the returned object will also include extra information required to define the basis, and used by `Predict.matrix` methods to make predictions using the basis. See the `Details` section for links to the information included for the built in smooth classes.

`tensor.smooth` returned objects will additionally have each element of the `margin` list updated in the same way. `tensor.smooths` also have a list, `XP`, containing re-parameterization matrices for any 1-D marginal terms re-parameterized in terms of function values. This list will have NULL entries for marginal smooths that are not re-parameterized, and is only long enough to reach the last re-parameterized marginal in the list.

WARNING

User defined smooth objects should avoid having attributes names `"qrc"` or `"nCons"` as these are used internally to provide constraint free parameterizations.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2003) Thin plate regression splines. *J.R.Statist.Soc.B* 65(1):95-114

Wood, S.N. (2006) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

The code given in the example is based on the smooths advocated in:

Ruppert, D., M.P. Wand and R.J. Carroll (2003) *Semiparametric Regression*. Cambridge University Press.

However if you want p-splines, rather than splines with derivative based penalties, then the built in "ps" class is probably a marginally better bet. It's based on

Eilers, P.H.C. and B.D. Marx (1996) *Flexible Smoothing with B-splines and Penalties*. *Statistical Science*, 11(2):89-121

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[s.get.var](#), [gamm](#), [gam](#), [Predict.matrix](#), [smoothCon](#), [PredictMat](#)

Examples

```
## Adding a penalized truncated power basis class and methods
## as favoured by Ruppert, Wand and Carroll (2003)
## Semiparametric regression CUP. (No advantage to actually
## using this, since mgcv can happily handle non-identity
## penalties.)

smooth.construct.tr.smooth.spec<-function(object,data,knots)
## a truncated power spline constructor method function
## object$p.order = null space dimension
{ m <- object$p.order[1]
  if (is.na(m)) m <- 2 ## default
  if (m<1) stop("silly m supplied")
  if (object$bs.dim<0) object$bs.dim <- 10 ## default
  nk<-object$bs.dim-m-1 ## number of knots
  if (nk<=0) stop("k too small for m")
  x <- data[[object$term]] ## the data
  x.shift <- mean(x) # shift used to enhance stability
  k <- knots[[object$term]] ## will be NULL if none supplied
  if (is.null(k)) # space knots through data
  { n<-length(x)
    k<-quantile(x[2:(n-1)],seq(0,1,length=nk+2))[2:(nk+1)]
  }
  if (length(k)!=nk) # right number of knots?
  stop(paste("there should be ",nk," supplied knots"))
  x <- x - x.shift # basis stabilizing shift
  k <- k - x.shift # knots treated the same!
  X<-matrix(0,length(x),object$bs.dim)
  for (i in 1:(m+1)) X[,i] <- x^(i-1)
  for (i in 1:nk) X[,i+m+1]<-(x-k[i])^m*as.numeric(x>k[i])
  object$X<-X # the finished model matrix
  if (!object$fixed) # create the penalty matrix
  { object$S[[1]]<-diag(c(rep(0,m+1),rep(1,nk)))
  }
}
```



```

object$rank<-nk # penalty rank
object$null.space.dim <- m+1 # dim. of unpenalized space
## store "tr" specific stuff ...
object$knots<-k;object$m<-m;object$x.shift <- x.shift

object$df<-ncol(object$X) # maximum DoF (if unconstrained)

class(object)<-"tr.smooth" # Give object a class
object
}

Predict.matrix.tr.smooth<-function(object,data)
## prediction method function for the `tr` smooth class
{ x <- data[[object$term]]
  x <- x - object$x.shift # stabilizing shift
  m <- object$m; # spline order (3=cubic)
  k<-object$knots # knot locations
  nk<-length(k) # number of knots
  X<-matrix(0,length(x),object$bs.dim)
  for (i in 1:(m+1)) X[,i] <- x^(i-1)
  for (i in 1:nk) X[,i+m+1] <- (x-k[i])^m*as.numeric(x>k[i])
  X # return the prediction matrix
}

# an example, using the new class...
require(mgcv)
set.seed(100)
dat <- gamSim(1,n=400,scale=2)
b<-gam(y~s(x0,bs="tr",m=2)+s(x1,bs="ps",m=c(1,3))+
      s(x2,bs="tr",m=3)+s(x3,bs="tr",m=2),data=dat)
plot(b,pages=1)
b<-gamm(y~s(x0,bs="tr",m=2)+s(x1,bs="ps",m=c(1,3))+
      s(x2,bs="tr",m=3)+s(x3,bs="tr",m=2),data=dat)
plot(b$gam,pages=1)
# another example using tensor products of the new class
dat <- gamSim(2,n=400,scale=.1)$data
b <- gam(y~te(x,z,bs=c("tr","tr"),m=c(2,2)),data=dat)
vis.gam(b)

```

```
smooth.construct.ad.smooth.spec
```

Adaptive smooths in GAMs

Description

`gam` can use adaptive smooths of one or two variables, specified via terms like `s(...,bs="ad",...)`. (`gamm` can not use such terms — check out package `AdaptFit` if this is a problem.) The basis for such a term is a (tensor product of) p-spline(s) or cubic regression spline(s). Discrete P-spline type penalties are applied directly to the coefficients of the basis, but the penalties themselves have a basis representation, allowing the strength of the penalty to vary with the covariates. The coefficients of the penalty basis are the smoothing parameters.

When invoking an adaptive smoother the k argument specifies the dimension of the smoothing basis (default 40 in 1D, 15 in 2D), while the m argument specifies the dimension of the penalty basis (default 5 in 1D, 3 in 2D). For an adaptive smooth of two variables k is taken as the dimension of both marginal bases: different marginal basis dimensions can be specified by making k a two element vector. Similarly, in the two dimensional case m is the dimension of both marginal bases for the penalties, unless it is a two element vector, which specifies different basis dimensions for each marginal (If the penalty basis is based on a thin plate spline then m specifies its dimension directly).

By default, P-splines are used for the smoothing and penalty bases, but this can be modified by supplying a list as argument `xt` with a character vector `xt$bs` specifying the smoothing basis type. Only "ps", "cp", "cc" and "cr" may be used for the smoothing basis. The penalty basis is always a B-spline, or a cyclic B-spline for cyclic bases.

The total number of smoothing parameters to be estimated for the term will be the dimension of the penalty basis. Bear in mind that adaptive smoothing places quite severe demands on the data. For example, setting $m=10$ for a univariate smooth of 200 data is rather like estimating 10 smoothing parameters, each from a data series of length 20. The problem is particularly serious for smooths of 2 variables, where the number of smoothing parameters required to get reasonable flexibility in the penalty can grow rather fast, but it often requires a very large smoothing basis dimension to make good use of this flexibility. In short, adaptive smooths should be used sparingly and with care.

In practice it is often as effective to simply transform the smoothing covariate as it is to use an adaptive smooth.

Usage

```
## S3 method for class 'ad.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(..., bs="ad", ...)</code>
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as data. Can be NULL

Details

The constructor is not normally called directly, but is rather used internally by `gam`. To use for basis setup it is recommended to use `smooth.construct2`.

This class can not be used as a marginal basis in a tensor product smooth, nor by `gamm`.

Value

An object of class "pspline.smooth" in the 1D case or "tensor.smooth" in the 2D case.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

Examples

```

## Comparison using an example taken from AdaptFit
## library(AdaptFit)
require(mgcv)
set.seed(0)
x <- 1:1000/1000
mu <- exp(-400*(x-.6)^2)+5*exp(-500*(x-.75)^2)/3+2*exp(-500*(x-.9)^2)
y <- mu+0.5*rnorm(1000)

##fit with default knots
## y.fit <- asp(y~f(x))

par(mfrow=c(2,2))
## plot(y.fit,main=round(cor(fitted(y.fit),mu),digits=4))
## lines(x,mu,col=2)

b <- gam(y~s(x,bs="ad",k=40,m=5)) ## adaptive
plot(b,shade=TRUE,main=round(cor(fitted(b),mu),digits=4))
lines(x,mu-mean(mu),col=2)

b <- gam(y~s(x,k=40)) ## non-adaptive
plot(b,shade=TRUE,main=round(cor(fitted(b),mu),digits=4))
lines(x,mu-mean(mu),col=2)

b <- gam(y~s(x,bs="ad",k=40,m=5,xt=list(bs="cr")))
plot(b,shade=TRUE,main=round(cor(fitted(b),mu),digits=4))
lines(x,mu-mean(mu),col=2)

## A 2D example (marked, 'Not run' purely to reduce
## checking load on CRAN).
## Not run:
par(mfrow=c(2,2),mar=c(1,1,1,1))
x <- seq(-.5, 1.5, length= 60)
z <- x
f3 <- function(x,z,k=15) { r<-sqrt(x^2+z^2);f<-exp(-r^2*k);f}
f <- outer(x, z, f3)
op <- par(bg = "white")

## Plot truth...
persp(x,z,f,theta=30,phi=30,col="lightblue",ticktype="detailed")

n <- 2000
x <- runif(n)*2-.5
z <- runif(n)*2-.5
f <- f3(x,z)
y <- f + rnorm(n)*.1

## Try tprs for comparison...
b0 <- gam(y~s(x,z,k=150))
vis.gam(b0,theta=30,phi=30,ticktype="detailed")

## Tensor product with non-adaptive version of adaptive penalty

```

```

b1 <- gam(y~s(x,z,bs="ad",k=15,m=1),gamma=1.4)
vis.gam(b1,theta=30,phi=30,ticktype="detailed")

## Now adaptive...
b <- gam(y~s(x,z,bs="ad",k=15,m=3),gamma=1.4)
vis.gam(b,theta=30,phi=30,ticktype="detailed")
cor(fitted(b0),f);cor(fitted(b),f)

## End(Not run)

```

```
smooth.construct.bs.smooth.spec
```

Penalized B-splines in GAMs

Description

`gam` can use smoothing splines based on univariate B-spline bases with derivative based penalties, specified via terms like `s(x,bs="bs",m=c(3,2))`. `m[1]` controls the spline order, with `m[1]=3` being a cubic spline, `m[1]=2` being quadratic, and so on. The integrated square of the `m[2]`th derivative is used as the penalty. So `m=c(3,2)` is a conventional cubic spline. If `m` is supplied as a single number, then it is taken to be `m[1]` and `m[2]=m[1]-1`, which is only a conventional smoothing spline in the `m=3`, cubic spline case. Notice that the definition of the spline order in terms of `m[1]` is intuitive, but differs to that used with the `tprs` and `p.spline` bases. See details for options for controlling the interval over which the penalty is evaluated (which can matter if it is necessary to extrapolate).

Usage

```

## S3 method for class 'bs.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'Bspline.smooth'
Predict.matrix(object, data)

```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(x,bs="bs",...)</code>
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be <code>NULL</code> . See details for further information.

Details

The basis and penalty are sparse (although sparse matrices are not used to represent them). $m[2] > m[1]$ will generate an error, since in that case the penalty would be based on an undefined derivative of the basis, which makes no sense.

The default basis dimension, k , is the larger of 10 and m . $m[1]$ is the lower limit on basis dimension. If knots are supplied, then the number of supplied knots should be $k + m[1] + 1$, and the range of the middle $k - m[1] + 1$ knots should include all the covariate values. Alternatively, 2 knots can be supplied, denoting the lower and upper limits between which the spline can be evaluated (making this range too wide mean that there is no information about some basis coefficients, because the corresponding basis functions have a span that includes no data). Unlike P-splines, splines with derivative based penalties can have uneven knot spacing, without a problem.

Another option is to supply 4 knots. Then the outer 2 define the interval over which the penalty is to be evaluated, while the inner 2 define an interval within which all but the outermost 2 knots should lie. Normally the outer 2 knots would be the interval over which predictions might be required, while the inner 2 knots define the interval within which the data lie. This option allows the penalty to apply over a wider interval than the data, while still placing most of the basis functions where the data are. This is useful in situations in which it is necessary to extrapolate slightly with a smooth. Only applying the penalty over the interval containing the data amounts to a model in which the function could be less smooth outside the interval than within it, and leads to very wide extrapolation confidence intervals. However the alternative of evaluating the penalty over the whole real line amounts to asserting certainty that the function has some derivative zeroed away from the data, which is equally unreasonable. It is preferable to build a model in which the same smoothness assumptions apply over both data and extrapolation intervals, but not over the whole real line. See example code for practical illustration.

Linear extrapolation is used for prediction that requires extrapolation (i.e. prediction outside the range of the interior $k - m[1] + 1$ knots — the interval over which the penalty is evaluated). Such extrapolation is not allowed in basis construction, but is when predicting.

It is possible to set a `deriv` flag in a smooth specification or smooth object, so that a model or prediction matrix produces the requested derivative of the spline, rather than evaluating it.

Value

An object of class "Bspline.smooth". See `smooth.construct`, for the elements that this object will contain.

WARNING

`m` directly controls the spline order here, which is intuitively sensible, but different to other bases.

Author(s)

Simon N. Wood <simon.wood@r-project.org>. Extrapolation ideas joint with David Miller.

References

Wood, S.N. (2016) P-splines with derivative based penalties and tensor product smoothing of unevenly distributed data. Statistics and Computing. <http://arxiv.org/abs/1605.02446>

See Also[p.spline](#)**Examples**

```

require(mgcv)
set.seed(5)
dat <- gamSim(1,n=400,dist="normal",scale=2)
bs <- "bs"
b <- gam(y~s(x0,bs=bs,m=c(4,2))+s(x1,bs=bs)+s(x2,k=15,bs=bs,m=c(4,3))+
        s(x3,bs=bs,m=c(1,0)),data=dat,method="REML")
plot(b,pages=1)

## Extrapolation example, illustrating the importance of considering
## the penalty carefully if extrapolating...
f3 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 * (10 * x)^3 *
        (1 - x)^10 ## test function
n <- 100;x <- runif(n)
y <- f3(x) + rnorm(n)*2
## first a model with first order penalty over whole real line (red)
b0 <- gam(y~s(x,m=1,k=20),method="ML")
## now a model with first order penalty evaluated over (-.5,1.5) (black)
op <- options(warn=-1)
b <- gam(y~s(x,bs="bs",m=c(3,1),k=20),knots=list(x=c(-.5,0,1,1.5)),
        method="ML")
options(op)
## and the equivalent with same penalty over data range only (blue)
b1 <- gam(y~s(x,bs="bs",m=c(3,1),k=20),method="ML")
pd <- data.frame(x=seq(-.7,1.7,length=200))
fv <- predict(b,pd,se=TRUE)
ul <- fv$fit + fv$se.fit*2; ll <- fv$fit - fv$se.fit*2
plot(x,y,xlim=c(-.7,1.7),ylim=range(c(y,ll,ul)),main=
     "1st order penalties: red tps; blue bs over (0,1); black bs over (-.5,1.5)")
## penalty defined on (-.5,1.5) gives plausible predictions and intervals
## over this range...
lines(pd$x,fv$fit);lines(pd$x,ul,lty=2);lines(pd$x,ll,lty=2)
fv <- predict(b0,pd,se=TRUE)
ul <- fv$fit + fv$se.fit*2; ll <- fv$fit - fv$se.fit*2
## penalty defined on whole real line gives constant width intervals away
## from data, as slope there must be zero, to avoid infinite penalty:
lines(pd$x,fv$fit,col=2)
lines(pd$x,ul,lty=2,col=2);lines(pd$x,ll,lty=2,col=2)
fv <- predict(b1,pd,se=TRUE)
ul <- fv$fit + fv$se.fit*2; ll <- fv$fit - fv$se.fit*2
## penalty defined only over the data interval (0,1) gives wild and wide
## extrapolation since penalty has been `turned off' outside data range:
lines(pd$x,fv$fit,col=4)
lines(pd$x,ul,lty=2,col=4);lines(pd$x,ll,lty=2,col=4)

## construct smooth of x. Model matrix sm$X and penalty
## matrix sm$S[[1]] will have many zero entries...
x <- seq(0,1,length=100)

```

```

sm <- smoothCon(s(x,bs="bs"),data.frame(x))[[1]]

## another example checking penalty numerically...
m <- c(4,2); k <- 15; b <- runif(k)
sm <- smoothCon(s(x,bs="bs",m=m,k=k),data.frame(x),
                scale.penalty=FALSE)[[1]]
sm$deriv <- m[2]
h0 <- 1e-3; xk <- sm$knots[(m[1]+1):(k+1)]
Xp <- PredictMat(sm,data.frame(x=seq(xk[1]+h0/2,max(xk)-h0/2,h0)))
sum((Xp%*%b)^2*h0) ## numerical approximation to penalty
b%*%sm$S[[1]]%*%b ## `exact` version

## ...repeated with uneven knot spacing...
m <- c(4,2); k <- 15; b <- runif(k)
## produce the required 20 unevenly spaced knots...
knots <- data.frame(x=c(-.4,-.3,-.2,-.1,-.001,.05,.15,
                      .21,.3,.32,.4,.6,.65,.75,.9,1.001,1.1,1.2,1.3,1.4))
sm <- smoothCon(s(x,bs="bs",m=m,k=k),data.frame(x),
                knots=knots,scale.penalty=FALSE)[[1]]
sm$deriv <- m[2]
h0 <- 1e-3; xk <- sm$knots[(m[1]+1):(k+1)]
Xp <- PredictMat(sm,data.frame(x=seq(xk[1]+h0/2,max(xk)-h0/2,h0)))
sum((Xp%*%b)^2*h0) ## numerical approximation to penalty
b%*%sm$S[[1]]%*%b ## `exact` version

```

```
smooth.construct.cr.smooth.spec
```

Penalized Cubic regression splines in GAMs

Description

`gam` can use univariate penalized cubic regression spline smooths, specified via terms like `s(x, bs="cr")`. `s(x, bs="cs")` specifies a penalized cubic regression spline which has had its penalty modified to shrink towards zero at high enough smoothing parameters (as the smoothing parameter goes to infinity a normal cubic spline tends to a straight line.) `s(x, bs="cc")` specifies a cyclic penalized cubic regression spline smooth.

'Cardinal' spline bases are used: Wood (2006) sections 4.1.2 and 4.1.3 gives full details. These bases have very low setup costs. For a given basis dimension, `k`, they typically perform a little less well than thin plate regression splines, but a little better than `p`-splines. See [te](#) to use these bases in tensor product smooths of several variables.

Default `k` is 10.

Usage

```

## S3 method for class 'cr.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'cs.smooth.spec'

```

```
smooth.construct(object, data, knots)
## S3 method for class 'cc.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

object	a smooth specification object, usually generated by a term <code>s(..., bs="cr", ...)</code> , <code>s(..., bs="cs", ...)</code> or <code>s(..., bs="cc", ...)</code>
data	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
knots	a list containing any knots supplied for basis setup — in same order and with same names as data. Can be NULL. See details.

Details

The constructor is not normally called directly, but is rather used internally by `gam`. To use for basis setup it is recommended to use `smooth.construct2`.

If they are not supplied then the knots of the spline are placed evenly throughout the covariate values to which the term refers: For example, if fitting 101 data with an 11 knot spline of x then there would be a knot at every 10th (ordered) x value. The parameterization used represents the spline in terms of its values at the knots. The values at neighbouring knots are connected by sections of cubic polynomial constrained to be continuous up to and including second derivative at the knots. The resulting curve is a natural cubic spline through the values at the knots (given two extra conditions specifying that the second derivative of the curve should be zero at the two end knots).

The shrinkage version of the smooth, eigen-decomposes the wiggleness penalty matrix, and sets its 2 zero eigenvalues to small multiples of the smallest strictly positive eigenvalue. The penalty is then set to the matrix with eigenvectors corresponding to those of the original penalty, but eigenvalues set to the perturbed versions. This penalty matrix has full rank and shrinks the curve to zero at high enough smoothing parameters.

Note that the cyclic smoother will wrap at the smallest and largest covariate values, unless knots are supplied. If only two knots are supplied then they are taken as the end points of the smoother (provided all the data lie between them), and the remaining knots are generated automatically.

The cyclic smooth is not subject to the condition that second derivatives go to zero at the first and last knots.

Value

An object of class `"cr.smooth"` `"cs.smooth"` or `"cyclic.smooth"`. In addition to the usual elements of a smooth class documented under `smooth.construct`, this object will contain:

xp	giving the knot locations used to generate the basis.
BD	class <code>"cyclic.smooth"</code> objects include matrix BD which transforms function values at the knots to second derivatives at the knots.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

Examples

```
## cyclic spline example...
require(mgcv)
set.seed(6)
x <- sort(runif(200)*10)
z <- runif(200)
f <- sin(x*2*pi/10)+.5
y <- rpois(exp(f),exp(f))

## finished simulating data, now fit model...
b <- gam(y ~ s(x,bs="cc",k=12) + s(z),family=poisson,
         knots=list(x=seq(0,10,length=12)))

## or more simply
b <- gam(y ~ s(x,bs="cc",k=12) + s(z),family=poisson,
         knots=list(x=c(0,10)))

## plot results...
par(mfrow=c(2,2))
plot(x,y);plot(b,select=1,shade=TRUE);lines(x,f-mean(f),col=2)
plot(b,select=2,shade=TRUE);plot(fitted(b),residuals(b))
```

smooth.construct.ds.smooth.spec

Low rank Duchon 1977 splines

Description

Thin plate spline smoothers are a special case of the isotropic splines discussed in Duchon (1977). A subset of this more general class can be invoked by terms like $s(x, z, bs="ds", m=c(1, .5))$ in a [gam](#) model formula. In the notation of Duchon (1977) m is given by $m[1]$ (default value 2), while s is given by $m[2]$ (default value 0).

Duchon's (1977) construction generalizes the usual thin plate spline penalty as follows. The usual TPS penalty is given by the integral of the squared Euclidian norm of a vector of mixed partial m th order derivatives of the function w.r.t. its arguments. Duchon re-expresses this penalty in the Fourier domain, and then weights the squared norm in the integral by the Euclidean norm of the fourier frequencies, raised to the power $2s$. s is a user selected constant taking integer values divided by 2. If d is the number of arguments of the smooth, then it is required that $-d/2 < s < d/2$. To obtain continuous functions we further require that $m + s > d/2$. If $s=0$ then the usual thin plate spline is recovered.

The construction is amenable to exactly the low rank approximation method given in Wood (2003) to thin plate splines, with similar optimality properties, so this approach to low rank smoothing is

used here. For large datasets the same subsampling approach as is used in the `tp` case is employed here to reduce computational costs.

These smoothers allow the use of lower orders of derivative in the penalty than conventional thin plate splines, while still yielding continuous functions. For example, we can set $m = 1$ and $s = d/2 - .5$ in order to use first derivative penalization for any d (which has the advantage that the dimension of the null space of unpenalized functions is only $d+1$).

Usage

```
## S3 method for class 'ds.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'duchon.spline'
Predict.matrix(object, data)
```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(..., bs="ds", ...)</code> .
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be NULL

Details

The default basis dimension for this class is $k=M+k_{.def}$ where M is the null space dimension (dimension of unpenalized function space) and $k_{.def}$ is 10 for dimension 1, 30 for dimension 2 and 100 for higher dimensions. This is essentially arbitrary, and should be checked, but as with all penalized regression smoothers, results are statistically insensitive to the exact choice, provided it is not so small that it forces oversmoothing (the smoother's degrees of freedom are controlled primarily by its smoothing parameter).

The constructor is not normally called directly, but is rather used internally by `gam`. To use for basis setup it is recommended to use `smooth.construct2`.

For these classes the specification object will contain information on how to handle large datasets in their `xt` field. The default is to randomly subsample 2000 'knots' from which to produce a reduced rank eigen approximation to the full basis, if the number of unique predictor variable combinations in excess of 2000. The default can be modified via the `xt` argument to `s`. This is supplied as a list with elements `max.knots` and `seed` containing a number to use in place of 2000, and the random number seed to use (either can be missing). Note that the random sampling will not effect the state of R's RNG.

For these bases `knots` has two uses. Firstly, as mentioned already, for large datasets the calculation of the `tp` basis can be time-consuming. The user can retain most of the advantages of the approach by supplying a reduced set of covariate values from which to obtain the basis - typically the number of covariate values used will be substantially smaller than the number of data, and substantially larger than the basis dimension, k . This approach is the one taken automatically if the number of unique covariate values (combinations) exceeds `max.knots`. The second possibility is to avoid the eigen-decomposition used to find the spline basis altogether and simply use the basis implied by the

chosen knots: this will happen if the number of knots supplied matches the basis dimension, k . For a given basis dimension the second option is faster, but gives poorer results (and the user must be quite careful in choosing knot locations).

Value

An object of class "duchon.spline". In addition to the usual elements of a smooth class documented under [smooth.construct](#), this object will contain:

shift	A record of the shift applied to each covariate in order to center it around zero and avoid any co-linearity problems that might otherwise occur in the penalty null space basis of the term.
Xu	A matrix of the unique covariate combinations for this smooth (the basis is constructed by first stripping out duplicate locations).
UZ	The matrix mapping the smoother parameters back to the parameters of a full Duchon spline.
null.space.dimension	The dimension of the space of functions that have zero wiggleness according to the wiggleness penalty for this term.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Duchon, J. (1977) Splines minimizing rotation-invariant semi-norms in Sobolev spaces. in W. Shemp and K. Zeller (eds) Construction theory of functions of several variables, 85-100, Springer, Berlin.

Wood, S.N. (2003) Thin plate regression splines. J.R.Statist.Soc.B 65(1):95-114

See Also

[Spherical.Spline](#)

Examples

```
require(mgcv)
eg <- gamSim(2,n=200,scale=.05)
attach(eg)
op <- par(mfrow=c(2,2),mar=c(4,4,1,1))
b0 <- gam(y~s(x,z,bs="ds",m=c(2,0),k=50),data=data) ## tps
b <- gam(y~s(x,z,bs="ds",m=c(1,.5),k=50),data=data) ## first deriv penalty
b1 <- gam(y~s(x,z,bs="ds",m=c(2,.5),k=50),data=data) ## modified 2nd deriv

persp(truth$x,truth$z,truth$f,theta=30) ## truth
vis.gam(b0,theta=30)
vis.gam(b,theta=30)
vis.gam(b1,theta=30)
```

```
detach(eg)
```

```
smooth.construct.fs.smooth.spec
```

Factor smooth interactions in GAMs

Description

Simple factor smooth interactions, which are efficient when used with [gamm](#). This smooth class allows a separate smooth for each level of a factor, with the same smoothing parameter for all smooths. It is an alternative to using factor by variables.

See the discussion of by variables in [gam.models](#) for more general alternatives for factor smooth interactions (including interactions of tensor product smooths with factors).

Usage

```
## S3 method for class 'fs.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'fs.interaction'
Predict.matrix(object, data)
```

Arguments

object	For the <code>smooth.construct</code> method a smooth specification object, usually generated by a term <code>s(x, ..., bs="fs",)</code> . For the <code>predict.Matrix</code> method an object of class <code>"fs.interaction"</code> produced by the <code>smooth.construct</code> method.
data	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> .
knots	a list containing any knots supplied for smooth basis setup.

Details

This class produces a smooth for each level of a single factor variable. Within a [gam](#) formula this is done with something like `s(x, fac, bs="fs")`, which is almost equivalent to `s(x, by=fac, id=1)` (with the `gam` argument `select=TRUE`). The terms are fully penalized, with separate penalties on each null space component: for this reason they are not centred (no sum-to-zero constraint).

The class is particularly useful for use with [gamm](#), where estimation efficiently exploits the nesting of the smooth within the factor. Note however that: i) `gamm` only allows one conditioning factor for smooths, so `s(x)+s(z, fac, bs="fs")+s(v, fac, bs="fs")` is OK, but `s(x)+s(z, fac1, bs="fs")+s(v, fac2, bs="fs")` is not; ii) all additional random effects and correlation structures will be treated as nested within the factor of the smooth factor interaction.

Note that `gamm4` from the `gamm4` package suffers from none of the restrictions that apply to `gamm`, and `"fs"` terms can be used without side-effects.

Any singly penalized basis can be used to smooth at each factor level. The default is `"tp"`, but alternatives can be supplied in the `xt` argument of `s` (e.g. `s(x, fac, bs="fs", xt="cr")` or

$s(x, \text{fac}, \text{bs}="fs", \text{xt}=\text{list}(\text{bs}="cr"))$. The k argument to $s(\dots, \text{bs}="fs")$ refers to the basis dimension to use for each level of the factor variable.

Note one computational bottleneck: currently `gam` (or `gamm4`) will produce the full posterior covariance matrix for the smooths, including the smooths at each level of the factor. This matrix can get large and computationally costly if there are more than a few hundred levels of the factor. Even at one or two hundred levels, care should be taken to keep down k .

The plot method for this class has two schemes. `scheme==0` is in colour, while `scheme==1` is black and white.

Value

An object of class `"fs.interaction"` or a matrix mapping the coefficients of the factor smooth interaction to the smooths themselves.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

See Also

[gam.models](#), [gamm](#)

Examples

```
library(mgcv)
set.seed(0)
## simulate data...
f0 <- function(x) 2 * sin(pi * x)
f1 <- function(x,a=2,b=-1) exp(a * x)+b
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
      (10 * x)^3 * (1 - x)^10
n <- 500;nf <- 25
fac <- sample(1:nf,n,replace=TRUE)
x0 <- runif(n);x1 <- runif(n);x2 <- runif(n)
a <- rnorm(nf)*.2 + 2;b <- rnorm(nf)*.5
f <- f0(x0) + f1(x1,a[fac],b[fac]) + f2(x2)
fac <- factor(fac)
y <- f + rnorm(n)*2
## so response depends on global smooths of x0 and
## x2, and a smooth of x1 for each level of fac.

## fit model (note p-values not available when fit
## using gamm)...
bm <- gamm(y~s(x0)+ s(x1,fac,bs="fs",k=5)+s(x2,k=20))
plot(bm$gam,pages=1)
summary(bm$gam)

## Could also use...
## b <- gam(y~s(x0)+ s(x1,fac,bs="fs",k=5)+s(x2,k=20),method="ML")
## ... but its slower (increasingly so with increasing nf)
## b <- gam(y~s(x0)+ t2(x1,fac,bs=c("tp","re"),k=5,full=TRUE)+
```

```
##      s(x2,k=20),method="ML"))
## ... is exactly equivalent.
```

```
smooth.construct.gp.smooth.spec
```

Low rank Gaussian process smooths

Description

Gaussian process/kriging models based on simple covariance functions can be written in a very similar form to thin plate and Duchon spline models (e.g. Handcock, Meier, Nychka, 1994), and low rank versions produced by the eigen approximation method of Wood (2003). Kammann and Wand (2003) suggest a particularly simple form of the Matern covariance function with only a single smoothing parameter to estimate, and this class implements this and other similar models.

Usually invoked by an `s(..., bs="gp")` term in a gam formula. Argument `m` selects the covariance function, sets the range parameter and any power parameter. If `m` is not supplied then it defaults to NA and the covariance function suggested by Kammann and Wand (2003) along with their suggested range parameter is used. Otherwise `m[1]` between 1 and 5 selects the correlation function from respectively, spherical, power exponential, and Matern with $\kappa = 1.5, 2.5$ or 3.5 . `m[2]` if present specifies the range parameter, with non-positive or absent indicating that the Kammann and Wand estimate should be used. `m[3]` can be used to specify the power for the power exponential which otherwise defaults to 1.

Usage

```
## S3 method for class 'gp.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'gp.smooth'
Predict.matrix(object, data)
```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(..., bs="ms", ...)</code> .
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be NULL

Details

Let $\rho > 0$ be the range parameter, $0 < \kappa \leq 2$ and d denote the distance between two points. Then the correlation functions indexed by `m[1]` are:

1. $1 - 1.5d/\rho + 0.5(d/\rho)^3$ if $d \leq \rho$ and 0 otherwise.
2. $\exp(-(d/\rho)^\kappa)$.

3. $\exp(-d/\rho)(1 + d/\rho)$.
4. $\exp(-d/\rho)(1 + d/\rho + (d/\rho)^2/3)$.
5. $\exp(-d/\rho)(1 + d/\rho + 2(d/\rho)^2/5 + (d/\rho)^3/15)$.

See Fahrmeir et al. (2013) section 8.1.6, for example.

The default basis dimension for this class is $k=M+k.def$ where M is the null space dimension (dimension of unpenalized function space) and $k.def$ is 10 for dimension 1, 30 for dimension 2 and 100 for higher dimensions. This is essentially arbitrary, and should be checked, but as with all penalized regression smoothers, results are statistically insensitive to the exact choice, provided it is not so small that it forces oversmoothing (the smoother's degrees of freedom are controlled primarily by its smoothing parameter).

The constructor is not normally called directly, but is rather used internally by `gam`. To use for basis setup it is recommended to use `smooth.construct2`.

For these classes the specification object will contain information on how to handle large datasets in their `xt` field. The default is to randomly subsample 2000 'knots' from which to produce a reduced rank eigen approximation to the full basis, if the number of unique predictor variable combinations in excess of 2000. The default can be modified via the `xt` argument to `s`. This is supplied as a list with elements `max.knots` and `seed` containing a number to use in place of 2000, and the random number seed to use (either can be missing). Note that the random sampling will not effect the state of R's RNG.

For these bases `knots` has two uses. Firstly, as mentioned already, for large datasets the calculation of the `tp` basis can be time-consuming. The user can retain most of the advantages of the approach by supplying a reduced set of covariate values from which to obtain the basis - typically the number of covariate values used will be substantially smaller than the number of data, and substantially larger than the basis dimension, k . This approach is the one taken automatically if the number of unique covariate values (combinations) exceeds `max.knots`. The second possibility is to avoid the eigen-decomposition used to find the spline basis altogether and simply use the basis implied by the chosen knots: this will happen if the number of knots supplied matches the basis dimension, k . For a given basis dimension the second option is faster, but gives poorer results (and the user must be quite careful in choosing knot locations).

Value

An object of class "gp.smooth". In addition to the usual elements of a smooth class documented under `smooth.construct`, this object will contain:

<code>shift</code>	A record of the shift applied to each covariate in order to center it around zero and avoid any co-linearity problems that might otherwise occur in the penalty null space basis of the term.
<code>Xu</code>	A matrix of the unique covariate combinations for this smooth (the basis is constructed by first stripping out duplicate locations).
<code>UZ</code>	The matrix mapping the smoother parameters back to the parameters of a full GP smooth.
<code>null.space.dimension</code>	The dimension of the space of functions that have zero wiggleness according to the wiggleness penalty for this term.
<code>gp.defn</code>	the type, range parameter and power parameter defining the correlation function.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

- Fahrmeir, L., T. Kneib, S. Lang and B. Marx (2013) Regression, Springer.
- Handcock, M. S., K. Meier and D. Nychka (1994) Journal of the American Statistical Association, 89: 401-403
- Kammann, E. E. and M.P. Wand (2003) Geoaddivitive Models. Applied Statistics 52(1):1-18.
- Wood, S.N. (2003) Thin plate regression splines. J.R.Statist.Soc.B 65(1):95-114

See Also

[tprs](#)

Examples

```
require(mgcv)
eg <- gamSim(2,n=200,scale=.05)
attach(eg)
op <- par(mfrow=c(2,2),mar=c(4,4,1,1))
b0 <- gam(y~s(x,z,k=50),data=data) ## tps
b <- gam(y~s(x,z,bs="gp",k=50),data=data) ## Matern spline default range
b1 <- gam(y~s(x,z,bs="gp",k=50,m=c(1,.5)),data=data) ## spherical

persp(truth$x,truth$z,truth$f,theta=30) ## truth
vis.gam(b0,theta=30)
vis.gam(b,theta=30)
vis.gam(b1,theta=30)

detach(eg)
```

smooth.construct.mrf.smooth.spec

Markov Random Field Smooths

Description

For data observed over discrete spatial units, a simple Markov random field smoother is sometimes appropriate. These functions provide such a smoother class for mgcv. See details for how to deal with regions with missing data.

Usage

```
## S3 method for class 'mrf.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'mrf.smooth'
Predict.matrix(object, data)
```


Arguments

object	For the smooth.construct method a smooth specification object, usually generated by a term <code>s(x, ..., bs="mrf", xt=list(polys=foo))</code> . <code>x</code> is a factor variable giving labels for geographic districts, and the <code>xt</code> argument is obligatory: see details. For the Predict.Matrix method an object of class "mrf.smooth" produced by the smooth.construct method.
data	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
knots	If there are more geographic areas than data were observed for, then this argument is used to provide the labels for all the areas (observed and unobserved).

Details

A Markov random field smooth over a set of discrete areas is defined using a set of area labels, and a neighbourhood structure for the areas. The covariate of the smooth is the vector of area labels corresponding to each observation. This covariate should be a factor, or capable of being coerced to a factor.

The neighbourhood structure is supplied in the `xt` argument to `s`. This must contain at least one of the elements `polys`, `nb` or `penalty`.

polys contains the polygons defining the geographic areas. It is a list with as many elements as there are geographic areas. `names(polys)` must correspond to the levels of the argument of the smooth, in any order (i.e. it gives the area labels). `polys[[i]]` is a 2 column matrix the rows of which specify the vertices of the polygon(s) defining the boundary of the *i*th area. A boundary may be made up of several closed loops: these must be separated by NA rows. A polygon within another is treated as a hole. The first polygon in any `polys[[i]]` should not be a hole. An example of the structure is provided by `columb.polys` (which contains an artificial hole in its second element, for illustration). Any list elements with duplicate names are combined into a single NA separated matrix.

Plotting of the smooth is not possible without a `polys` object.

If `polys` is the only element of `xt` provided, then the neighbourhood structure is computed from it automatically. To count as neighbours, polygons must exactly share one of more vertices.

nb is a named list defining the neighbourhood structure. `names(nb)` must correspond to the levels of the covariate of the smooth (i.e. the area labels), but can be in any order. `nb[[i]]` is a vector indexing the neighbours of the *i*th area. All indices are relative to `nb` itself, but can be translated using `names(nb)`.

If no `penalty` is provided then it is computed automatically from this list. The *i*th row of the penalty matrix will be zero everywhere, except in the *i*th column, which will contain the number of neighbours of the *i*th geographic area, and the columns corresponding to those geographic neighbours, which will each contain -1.

penalty if this is supplied, then it is used as the penalty matrix. It should be positive semi-definite. Its row and column names should correspond to the levels of the covariate.

If no basis dimension is supplied then the constructor produces a full rank MRF, with a coefficient for each geographic area. Otherwise a low rank approximation is obtained based on truncation of the parameterization given in Wood (2006) Section 4.10.4.

Note that smooths of this class have a built in plot method, and that the utility function `in.out` can be useful for working with discrete area data. The plot method has two schemes, `scheme==0` is colour, `scheme==1` is grey scale.

The situation in which there are areas with no data requires special handling. You should set `drop.unused.levels=FALSE` in the model fitting function, `gam`, `bam` or `gamm`, having first ensured that any fixed effect factors do not contain unobserved levels. Also make sure that the basis dimension is set to ensure that the total number of coefficients is less than the number of observations.

Value

An object of class "mrf.smooth" or a matrix mapping the coefficients of the MRF smooth to the predictions for the areas listed in data.

Author(s)

Simon N. Wood <simon.wood@r-project.org> and Thomas Kneib (Fabian Scheipl prototyped the low rank MRF idea)

References

Wood S.N. (2006) Generalized additive models: an introduction with R. CRC.

See Also

`in.out`, `polys.plot`

Examples

```
library(mgcv)
## Load Columbus Ohio crime data (see ?columbus for details and credits)
data(columb)      ## data frame
data(columb.polys) ## district shapes list
xt <- list(polys=columb.polys) ## neighbourhood structure info for MRF
par(mfrow=c(2,2))
## First a full rank MRF...
b <- gam(crime ~ s(district,bs="mrf",xt=xt),data=columb,method="REML")
plot(b,scheme=1)
## Compare to reduced rank version...
b <- gam(crime ~ s(district,bs="mrf",k=20,xt=xt),data=columb,method="REML")
plot(b,scheme=1)
## An important covariate added...
b <- gam(crime ~ s(district,bs="mrf",k=20,xt=xt)+s(income),
         data=columb,method="REML")
plot(b,scheme=c(0,1))

## plot fitted values by district
par(mfrow=c(1,1))
fv <- fitted(b)
names(fv) <- as.character(columb$district)
polys.plot(columb.polys,fv)
```

smooth.construct.ps.smooth.spec
P-splines in GAMs

Description

`gam` can use univariate P-splines as proposed by Eilers and Marx (1996), specified via terms like `s(x,bs="ps")`. These terms use B-spline bases penalized by discrete penalties applied directly to the basis coefficients. Cyclic P-splines are specified by model terms like `s(x,bs="cp",...)`. These bases can be used in tensor product smooths (see [te](#)).

The advantage of P-splines is the flexible way that penalty and basis order can be mixed. This often provides a useful way of ‘taming’ an otherwise poorly behaved smooth. However, in regular use, splines with derivative based penalties (e.g. `"tp"` or `"cr"` bases) tend to result in slightly better MSE performance, presumably because the good approximation theoretic properties of splines are rather closely connected to the use of derivative penalties.

Usage

```
## S3 method for class 'ps.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'cp.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(x,bs="ps",...)</code> or <code>s(x,bs="cp",...)</code>
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be NULL. See details for further information.

Details

A smooth term of the form `s(x,bs="ps",m=c(2,3))` specifies a 2nd order P-spline basis (cubic spline), with a third order difference penalty (0th order is a ridge penalty) on the coefficients. If `m` is a single number then it is taken as the basis order and penalty order. The default is the ‘cubic spline like’ `m=c(2,2)`.

The default basis dimension, `k`, is the larger of 10 and `m[1]+1` for a `"ps"` terms and the larger of 10 and `m[1]` for a `"cp"` term. `m[1]+1` and `m[1]` are the lower limits on basis dimension for the two types.

If `knots` are supplied, then the number of knots should be one more than the basis dimension (i.e. `k+1`) for a `"cp"` smooth. For the `"ps"` basis the number of supplied knots should be `k + m[1] + 2`, and the range of the middle `k-m[1]` knots should include all the covariate values. See example.

Alternatively, for both types of smooth, 2 knots can be supplied, denoting the lower and upper limits between which the spline can be evaluated (Don't make this range too wide, however, or you can end up with no information about some basis coefficients, because the corresponding basis functions have a span that includes no data!). Note that P-splines don't make much sense with uneven knot spacing.

Linear extrapolation is used for prediction that requires extrapolation (i.e. prediction outside the range of the interior $k-m[1]$ knots). Such extrapolation is not allowed in basis construction, but is when predicting.

For the "ps" basis it is possible to set flags in the smooth specification object, requesting setup according to the SCOP-spline monotonic smoother construction of Pya and Wood (2015). As yet this is not supported by any modelling functions in `mgcv` (see package `scam`). Similarly it is possible to set a `deriv` flag in a smooth specification or smooth object, so that a model or prediction matrix produces the requested derivative of the spline, rather than evaluating it. See examples below.

Value

An object of class "pspline.smooth" or "cp.smooth". See [smooth.construct](#), for the elements that this object will contain.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

- Eilers, P.H.C. and B.D. Marx (1996) Flexible Smoothing with B-splines and Penalties. *Statistical Science*, 11(2):89-121
- Pya, N., and Wood, S.N. (2015). Shape constrained additive models. *Statistics and Computing*, 25(3), 543-559.

See Also

[cSplineDes](#), [adaptive.smooth](#)

Examples

```
## see ?gam
## cyclic example ...
require(mgcv)
set.seed(6)
x <- sort(runif(200)*10)
z <- runif(200)
f <- sin(x*2*pi/10)+.5
y <- rpois(exp(f),exp(f))

## finished simulating data, now fit model...
b <- gam(y ~ s(x,bs="cp") + s(z,bs="ps"),family=poisson)

## example with supplied knot ranges for x and z (can do just one)
b <- gam(y ~ s(x,bs="cp") + s(z,bs="ps"),family=poisson,
```

```

      knots=list(x=c(0,10),z=c(0,1)))

## example with supplied knots...
bk <- gam(y ~ s(x,bs="cp",k=12) + s(z,bs="ps",k=13),family=poisson,
          knots=list(x=seq(0,10,length=13),z=(-3):13/10))

## plot results...
par(mfrow=c(2,2))
plot(b,select=1,shade=TRUE);lines(x,f-mean(f),col=2)
plot(b,select=2,shade=TRUE);lines(z,0*z,col=2)
plot(bk,select=1,shade=TRUE);lines(x,f-mean(f),col=2)
plot(bk,select=2,shade=TRUE);lines(z,0*z,col=2)

## Example using monotonic constraints via the SCOP-spline
## construction, and of computing derivatives...
x <- seq(0,1,length=100); dat <- data.frame(x)
sspec <- s(x,bs="ps")
sspec$mono <- 1
sm <- smoothCon(sspec,dat)[[1]]
sm$deriv <- 1
Xd <- PredictMat(sm,dat)
## generate random coefficients in the unconstrained
## parameterization...
b <- runif(10)*3-2.5
## exponentiate those parameters indicated by sm$g.index
## to obtain coefficients meeting the constraints...
b[sm$g.index] <- exp(b[sm$g.index])
## plot monotonic spline and its derivative
par(mfrow=c(2,2))
plot(x,sm$X%*%b,type="l",ylab="f(x)")
plot(x,Xd%*%b,type="l",ylab="f'(x)")
## repeat for decrease...
sspec$mono <- -1
sm1 <- smoothCon(sspec,dat)[[1]]
sm1$deriv <- 1
Xd1 <- PredictMat(sm1,dat)
plot(x,sm1$X%*%b,type="l",ylab="f(x)")
plot(x,Xd1%*%b,type="l",ylab="f'(x)")

## Now with sum to zero constraints as well...
sspec$mono <- 1
sm <- smoothCon(sspec,dat,absorb.cons=TRUE)[[1]]
sm$deriv <- 1
Xd <- PredictMat(sm,dat)
b <- b[-1] ## dropping first param
plot(x,sm$X%*%b,type="l",ylab="f(x)")
plot(x,Xd%*%b,type="l",ylab="f'(x)")

sspec$mono <- -1
sm1 <- smoothCon(sspec,dat,absorb.cons=TRUE)[[1]]
sm1$deriv <- 1
Xd1 <- PredictMat(sm1,dat)
plot(x,sm1$X%*%b,type="l",ylab="f(x)")

```

```
plot(x, Xd1%*%b, type="l", ylab="f'(x)")
```

```
smooth.construct.re.smooth.spec
```

Simple random effects in GAMs

Description

`gam` can deal with simple independent random effects, by exploiting the link between smooths and random effects to treat random effects as smooths. `s(x, bs="re")` implements this. Such terms can have any number of predictors, which can be any mixture of numeric or factor variables. The terms produce a parametric interaction of the predictors, and penalize the corresponding coefficients with a multiple of the identity matrix, corresponding to an assumption of i.i.d. normality. See details.

Usage

```
## S3 method for class 're.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'random.effect'
Predict.matrix(object, data)
```

Arguments

<code>object</code>	For the <code>smooth.construct</code> method a smooth specification object, usually generated by a term <code>s(x, ..., bs="re", ...)</code> . For the <code>Predict.matrix</code> method an object of class "random.effect" produced by the <code>smooth.construct</code> method.
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	generically a list containing any knots supplied for basis setup — unused at present.

Details

Exactly how the random effects are implemented is best seen by example. Consider the model term `s(x, z, bs="re")`. This will result in the model matrix component corresponding to $\sim x:z-1$ being added to the model matrix for the whole model. The coefficients associated with the model matrix component are assumed i.i.d. normal, with unknown variance (to be estimated). This assumption is equivalent to an identity penalty matrix (i.e. a ridge penalty) on the coefficients. Because such a penalty is full rank, random effects terms do not require centering constraints.

If the nature of the random effect specification is not clear, consider a couple more examples: `s(x, bs="re")` results in `model.matrix(~x-1)` being appended to the overall model matrix, while `s(x, v, w, bs="re")` would result in `model.matrix(~x:v:w-1)` being appended to the model matrix. In both cases the corresponding model coefficients are assumed i.i.d. normal, and are hence subject to ridge penalties.

If the random effect precision matrix is of the form $\sum_j \lambda_j S_j$ for known matrices S_j and unknown parameters λ_j , then a list containing the S_j can be supplied in the `xt` argument of `s`. In this case an array `rank` should also be supplied in `xt` giving the ranks of the S_j matrices. See simple example below.

Note that `smooth ids` are not supported for random effect terms. Unlike most smooth terms, side conditions are never applied to random effect terms in the event of nesting (since they are identifiable without side conditions).

Random effects implemented in this way do not exploit the sparse structure of many random effects, and may therefore be relatively inefficient for models with large numbers of random effects, when `gamm4` or `gamm` may be better alternatives. Note also that `gam` will not support models with more coefficients than data.

The situation in which factor variable random effects intentionally have unobserved levels requires special handling. You should set `drop.unused.levels=FALSE` in the model fitting function, `gam`, `bam` or `gamm`, having first ensured that any fixed effect factors do not contain unobserved levels.

Value

An object of class "random.effect" or a matrix mapping the coefficients of the random effect to the random effects themselves.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2008) Fast stable direct fitting and smoothness selection for generalized additive models. *Journal of the Royal Statistical Society (B)* 70(3):495-518

See Also

[gam.vcomp](#), [gamm](#)

Examples

```
## see ?gam.vcomp

require(mgcv)
## simulate simple random effect example
set.seed(4)
nb <- 50; n <- 400
b <- rnorm(nb)*2 ## random effect
r <- sample(1:nb,n,replace=TRUE) ## r.e. levels
y <- 2 + b[r] + rnorm(n)
r <- factor(r)
## fit model....
b <- gam(y ~ s(r,bs="re"),method="REML")
gam.vcomp(b)

## example with supplied precision matrices...
```

```

b <- c(rnorm(nb/2)*2,rnorm(nb/2)*.5) ## random effect now with 2 variances
r <- sample(1:nb,n,replace=TRUE) ## r.e. levels
y <- 2 + b[r] + rnorm(n)
r <- factor(r)
## known precision matrix components...
S <- list(diag(rep(c(1,0),each=nb/2)),diag(rep(c(0,1),each=nb/2)))
b <- gam(y ~ s(r,bs="re",xt=list(S=S,rank=c(nb/2,nb/2))),method="REML")
gam.vcomp(b)
summary(b)

```

smooth.construct.so.smooth.spec

Soap film smoother constructor

Description

Sets up basis functions and wiggleness penalties for soap film smoothers (Wood, Bravington and Hedley, 2008). Soap film smoothers are based on the idea of constructing a 2-D smooth as a film of soap connecting a smoothly varying closed boundary. Unless smoothing very heavily, the film is distorted towards the data. The smooths are designed not to smooth across boundary features (peninsulas, for example).

The so version sets up the full smooth. The sf version sets up just the boundary interpolating soap film, while the sw version sets up the wiggly component of a soap film (zero on the boundary). The latter two are useful for forming tensor products with soap films, and can be used with `gamm` and `gamm4`. To use these to simply set up a basis, then call via the wrapper `smooth.construct2` or `smoothCon`.

Usage

```

## S3 method for class 'so.smooth.spec'
smooth.construct(object,data,knots)
## S3 method for class 'sf.smooth.spec'
smooth.construct(object,data,knots)
## S3 method for class 'sw.smooth.spec'
smooth.construct(object,data,knots)

```

Arguments

object	A smooth specification object as produced by a <code>s(...,bs="so",xt=list(bnd=bnd,...))</code> term in a gam formula. Note that the <code>xt</code> argument to <code>s</code> <i>must</i> be supplied, and should be a list, containing at least a boundary specification list (see details). <code>xt</code> may also contain various options controlling the boundary smooth (see details), and PDE solution grid. The dimension of the bases for boundary loops is specified via the <code>k</code> argument of <code>s</code> , either as a single number to be used for each boundary loop, or as a vector of different basis dimensions for the various boundary loops.
data	A list or data frame containing the arguments of the smooth.

`knots` list or data frame with two named columns specifying the knot locations within the boundary. The column names should match the names of the arguments of the `smooth`. The number of knots defines the **interior** basis dimension (i.e. it is **not** supplied via argument `k` of `s`).

Details

For soap film smooths the following **must** be supplied:

- `k` the basis dimension for each boundary loop smooth.
- `xt` the boundary specification for the smooth.
- `knots` the locations of the interior knots for the smooth.

When used in a GAM then `k` and `xt` are supplied via `s` while `knots` are supplied in the `knots` argument of `gam`.

The `bnd` element of the `xt` list is a list of lists (or data frames), specifying the loops that define the boundary. Each boundary loop list must contain 2 columns giving the co-ordinates of points defining a boundary loop (when joined sequentially by line segments). Loops should not intersect (not checked). A point is deemed to be in the region of interest if it is interior to an odd number of boundary loops. Each boundary loop list may also contain a column `f` giving known boundary conditions on a loop.

The `bndSpec` element of `xt`, if non-NULL, should contain

- `bs` the type of cyclic smoothing basis to use: one of "cc" and "cp". If not "cc" then a cyclic p-spline is used, and argument `m` must be supplied.
- `knot.space` set to "even" to get even knot spacing with the "cc" basis.
- `m` 1 or 2 element array specifying order of "cp" basis and penalty.

Currently the code will not deal with more than one level of nesting of loops, or with separate loops without an outer enclosing loop: if there are known boundary conditions (identifiability constraints get awkward).

Note that the function `locator` provides a simple means for defining boundaries graphically, using something like `bnd <- as.data.frame(locator(type="l"))`, after producing a plot of the domain of interest (right click to stop). If the real boundary is very complicated, it is probably better to use a simpler smooth boundary enclosing the true boundary, which represents the major boundary features that you don't want to smooth across, but doesn't follow every tiny detail.

Model set up, and prediction, involves evaluating basis functions which are defined as the solution to PDEs. The PDEs are solved numerically on a grid using sparse matrix methods, with bilinear interpolation used to obtain values at any location within the smoothing domain. The dimension of the PDE solution grid can be controlled via element `nmax` (default 200) of the list supplied as argument `xt` of `s` in a `gam` formula: it gives the number of cells to use on the longest grid side.

A little theory: the soap film smooth $f(x, y)$ is defined as the solution of

$$f_{xx} + f_{yy} = g$$

subject to the condition that $f = s$, on the boundary curve, where s is a smooth function (usually a cyclic penalized regression spline). The function g is defined as the solution of

$$g_{xx} + g_{yy} = 0$$

where $g = 0$ on the boundary curve and $g(x_k, y_k) = c_k$ at the 'knots' of the surface; the c_k are model coefficients.

In the simplest case, estimation of the coefficients of f (boundary coefficients plus c_k 's) is by minimization of

$$\|z - f\|^2 + \lambda_s J_s(s) + \lambda_f J_f(f)$$

where J_s is usually some cubic spline type wiggleness penalty on the boundary smooth and J_f is the integral of $(f_x x + f_y y)^2$ over the interior of the boundary. Both penalties can be expressed as quadratic forms in the model coefficients. The λ 's are smoothing parameters, selectable by GCV, REML, AIC, etc. z represents noisy observations of f .

Value

A list with all the elements of object plus

sd	A list defining the PDE solution grid and domain boundary, and including the sparse LU factorization of the PDE coefficient matrix.
X	The model matrix: this will have an "offset" attribute, if there are any known boundary conditions.
S	List of smoothing penalty matrices (in smallest non-zero submatrix form).
irng	A vector of scaling factors that have been applied to the model matrix, to ensure nice conditioning.

In addition there are all the elements usually added by `smooth.construct` methods.

WARNINGS

Soap film smooths are quite specialized, and require more setup than most smoothers (e.g. you have to supply the boundary and the interior knots, plus the boundary smooth basis dimension(s)). It is worth looking at the reference.

Author(s)

Simon N. Wood <simon.wood@project.org>

References

Wood, S.N., M.V. Bravington and S.L. Hedley (2008) "Soap film smoothing", *J.R.Statist.Soc.B* 70(5), 931-955.

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[Predict.matrix.soap.film](#)

Examples

```

require(mgcv)

#####
## simple test function...
#####

fsb <- list(fs.boundary())
nmax <- 100
## create some internal knots...
knots <- data.frame(v=rep(seq(-.5,3,by=.5),4),
                    w=rep(c(-.6,-.3,.3,.6),rep(8,4)))
## Simulate some fitting data, inside boundary...
set.seed(0)
n<-600
v <- runif(n)*5-1;w<-runif(n)*2-1
y <- fs.test(v,w,b=1)
names(fsb[[1]]) <- c("v","w")
ind <- inSide(fsb,x=v,y=w) ## remove outsiders
y <- y + rnorm(n)*.3 ## add noise
y <- y[ind];v <- v[ind]; w <- w[ind]
n <- length(y)

par(mfrow=c(3,2))
## plot boundary with knot and data locations
plot(fsb[[1]]$v,fsb[[1]]$w,type="l");points(knots,pch=20,col=2)
points(v,w,pch=".");

## Now fit the soap film smoother. 'k' is dimension of boundary smooth.
## boundary supplied in 'xt', and knots in 'knots'...

nmax <- 100 ## reduced from default for speed.
b <- gam(y~s(v,w,k=30,bs="so",xt=list(bnd=fsb,nmax=nmax)),knots=knots)

plot(b) ## default plot
plot(b,scheme=1)
plot(b,scheme=2)
plot(b,scheme=3)

vis.gam(b,plot.type="contour")

#####
# Fit same model in two parts...
#####

par(mfrow=c(2,2))
vis.gam(b,plot.type="contour")

b1 <- gam(y~s(v,w,k=30,bs="sf",xt=list(bnd=fsb,nmax=nmax))+
          s(v,w,k=30,bs="sw",xt=list(bnd=fsb,nmax=nmax)),knots=knots)
vis.gam(b,plot.type="contour")

```

```

plot(b1)

#####
## Now an example with known boundary condition...
#####

## Evaluate known boundary condition at boundary nodes...
fsb[[1]]$f <- fs.test(fsb[[1]]$v,fsb[[1]]$w,b=1,exclude=FALSE)

## Now fit the smooth...
bk <- gam(y~s(v,w,bs="so",xt=list(bnd=fsb,nmax=nmax)),knots=knots)
plot(bk) ## default plot

#####
## tensor product example (marked
## 'Not run' to reduce CRAN checking load)
#####
## Not run:
n <- 10000
v <- runif(n)*5-1;w<-runif(n)*2-1
t <- runif(n)
y <- fs.test(v,w,b=1)
y <- y + 4.2
y <- y^(.5+t)
fsb <- list(fs.boundary())
names(fsb[[1]]) <- c("v","w")
ind <- inSide(fsb,x=v,y=w) ## remove outsiders
y <- y[ind];v <- v[ind]; w <- w[ind]; t <- t[ind]
n <- length(y)
y <- y + rnorm(n)*.05 ## add noise
knots <- data.frame(v=rep(seq(-.5,3,by=.5),4),
                    w=rep(c(-.6,-.3,.3,.6),rep(8,4)))

## notice NULL element in 'xt' list - to indicate no xt object for "cr" basis...
bk <- gam(y~ te(v,w,t,bs=c("sf","cr"),k=c(25,4),d=c(2,1),
                xt=list(list(bnd=fsb,nmax=nmax),NULL))+
          te(v,w,t,bs=c("sw","cr"),k=c(25,4),d=c(2,1),
                xt=list(list(bnd=fsb,nmax=nmax),NULL)),knots=knots)

par(mfrow=c(3,2))
m<-100;n<-50
xm <- seq(-1,3.5,length=m);yn<-seq(-1,1,length=n)
xx <- rep(xm,n);yy<-rep(yn,rep(m,n))
tru <- matrix(fs.test(xx,yy),m,n)+4.2 ## truth

image(xm,yn,tru^.5,col=heat.colors(100),xlab="v",ylab="w",
      main="truth")
lines(fsb[[1]]$v,fsb[[1]]$w,lwd=3)
contour(xm,yn,tru^.5,add=TRUE)

vis.gam(bk,view=c("v","w"),cond=list(t=0),plot.type="contour")

image(xm,yn,tru,col=heat.colors(100),xlab="v",ylab="w",

```

```

      main="truth")
lines(fsb[[1]]$v,fsb[[1]]$w,lwd=3)
contour(xm,yn,tru,add=TRUE)

vis.gam(bk,view=c("v","w"),cond=list(t=.5),plot.type="contour")

image(xm,yn,tru^1.5,col=heat.colors(100),xlab="v",ylab="w",
      main="truth")
lines(fsb[[1]]$v,fsb[[1]]$w,lwd=3)
contour(xm,yn,tru^1.5,add=TRUE)

vis.gam(bk,view=c("v","w"),cond=list(t=1),plot.type="contour")

## End(Not run)

#####
# nested boundary example...
#####

bnd <- list(list(x=0,y=0),list(x=0,y=0))
seq(0,2*pi,length=100) -> theta
bnd[[1]]$x <- sin(theta);bnd[[1]]$y <- cos(theta)
bnd[[2]]$x <- .3 + .3*sin(theta);
bnd[[2]]$y <- .3 + .3*cos(theta)
plot(bnd[[1]]$x,bnd[[1]]$y,type="l")
lines(bnd[[2]]$x,bnd[[2]]$y)

## setup knots
k <- 8
xm <- seq(-1,1,length=k);ym <- seq(-1,1,length=k)
x=rep(xm,k);y=rep(ym,rep(k,k))
ind <- inSide(bnd,x,y)
knots <- data.frame(x=x[ind],y=y[ind])
points(knots$x,knots$y)

## a test function

f1 <- function(x,y) {
  exp(-(x-.3)^2-(y-.3)^2)
}

## plot the test function within the domain
par(mfrow=c(2,3))
m<-100;n<-100
xm <- seq(-1,1,length=m);yn<-seq(-1,1,length=n)
x <- rep(xm,n);y<-rep(yn,rep(m,n))
ff <- f1(x,y)
ind <- inSide(bnd,x,y)
ff[!ind] <- NA
image(xm,yn,matrix(ff,m,n),xlab="x",ylab="y")
contour(xm,yn,matrix(ff,m,n),add=TRUE)
lines(bnd[[1]]$x,bnd[[1]]$y,lwd=2);lines(bnd[[2]]$x,bnd[[2]]$y,lwd=2)

```

```

## Simulate data by noisy sampling from test function...

set.seed(1)
x <- runif(300)*2-1;y <- runif(300)*2-1
ind <- inSide(bnd,x,y)
x <- x[ind];y <- y[ind]
n <- length(x)
z <- f1(x,y) + rnorm(n)*.1

## Fit a soap film smooth to the noisy data
nmax <- 60
b <- gam(z~s(x,y,k=c(30,15),bs="so",xt=list(bnd=bnd,nmax=nmax)),
         knots=knots,method="REML")
plot(b) ## default plot
vis.gam(b,plot.type="contour") ## prettier version

## trying out separated fits...
ba <- gam(z~s(x,y,k=c(30,15),bs="sf",xt=list(bnd=bnd,nmax=nmax))+
         s(x,y,k=c(30,15),bs="sw",xt=list(bnd=bnd,nmax=nmax)),
         knots=knots,method="REML")
plot(ba)
vis.gam(ba,plot.type="contour")

```

smooth.construct.sos.smooth.spec

Splines on the sphere

Description

`gam` can use isotropic smooths on the sphere, via terms like `s(la,lo,bs="sos",m=2,k=100)`. There must be exactly 2 arguments to such a smooth. The first is taken to be latitude (in degrees) and the second longitude (in degrees). `m` (default 0) is an integer in the range -1 to 4 determining the order of the penalty used. For $m > 0$, $(m+2)/2$ is the penalty order, with $m=2$ equivalent to the usual second derivative penalty. $m=0$ signals to use the 2nd order spline on the sphere, computed by Wendelberger's (1981) method. $m = -1$ results in a [Duchon.spline](#) being used (with $m=2$ and $s=1/2$), following an unpublished suggestion of Jean Duchon.

`k` (default 50) is the basis dimension.

Usage

```

## S3 method for class 'sos.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'sos.smooth'
Predict.matrix(object, data)

```

Arguments

`object` a smooth specification object, usually generated by a term `s(...,bs="sos",...)`.

data	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
knots	a list containing any knots supplied for basis setup — in same order and with same names as data. Can be NULL

Details

For $m > 0$, the smooths implemented here are based on the pseudosplines on the sphere of Wahba (1981) (there is a correction of table 1 in 1982, but the correction has a misprint in the definition of A — the A given in the 1981 paper is correct). For $m = 0$ (default) then a second order spline on the sphere is used which is the analogue of a second order thin plate spline in 2D: the computation is based on Chapter 4 of Wendelberger, 1981. Optimal low rank approximations are obtained using exactly the approach given in Wood (2003). For $m = -1$ a smooth of the general type discussed in Duchon (1977) is used: the sphere is embedded in a 3D Euclidean space, but smoothing employs a penalty based on second derivatives (so that locally as the smoothing parameter tends to zero we recover a "normal" thin plate spline on the tangent space). This is an unpublished suggestion of Jean Duchon.

Note that the null space of the penalty is always the space of constant functions on the sphere, whatever the order of penalty.

This class has a plot method, with 3 schemes. `scheme==0` plots one hemisphere of the sphere, projected onto a circle. The plotting sphere has the north pole at the top, and the 0 meridian running down the middle of the plot, and towards the viewer. The smoothing sphere is rotated within the plotting sphere, by specifying the location of its pole in the co-ordinates of the viewing sphere. `theta`, `phi` give the longitude and latitude of the smoothing sphere pole within the plotting sphere (in plotting sphere co-ordinates). (You can visualize the smoothing sphere as a globe, free to rotate within the fixed transparent plotting sphere.) The value of the smooth is shown by a heat map overlaid with a contour plot. `lat`, `lon` gridlines are also plotted.

`scheme==1` is as `scheme==0`, but in black and white, without the image plot. `scheme>1` calls the default plotting method with scheme decremented by 2.

Value

An object of class "sos.smooth". In addition to the usual elements of a smooth class documented under [smooth.construct](#), this object will contain:

Xu	A matrix of the unique covariate combinations for this smooth (the basis is constructed by first stripping out duplicate locations).
UZ	The matrix mapping the parameters of the reduced rank spline back to the parameters of a full spline.

Author(s)

Simon Wood <simon.wood@r-project.org>, with help from Grace Wahba ($m=0$ case) and Jean Duchon ($m = -1$ case).

References

- Wahba, G. (1981) Spline interpolation and smoothing on the sphere. *SIAM J. Sci. Stat. Comput.* 2(1):5-16
- Wahba, G. (1982) Erratum. *SIAM J. Sci. Stat. Comput.* 3(3):385-386.
- Wendelberger, J. (1981) PhD Thesis, University of Wisconsin.
- Wood, S.N. (2003) Thin plate regression splines. *J.R.Statist.Soc.B* 65(1):95-114

See Also

[Duchon.spline](#)

Examples

```
require(mgcv)
set.seed(0)
n <- 400

f <- function(la,lo) { ## a test function...
  sin(lo)*cos(la-.3)
}

## generate with uniform density on sphere...
lo <- runif(n)*2*pi-pi ## longitude
la <- runif(3*n)*pi-pi/2
ind <- runif(3*n)<=cos(la)
la <- la[ind];
la <- la[1:n]

ff <- f(la,lo)
y <- ff + rnorm(n)*.2 ## test data

## generate data for plotting truth...
lam <- seq(-pi/2,pi/2,length=30)
lom <- seq(-pi,pi,length=60)
gr <- expand.grid(la=lam,lo=lom)
fz <- f(gr$la,gr$lo)
zm <- matrix(fz,30,60)

require(mgcv)
dat <- data.frame(la = la *180/pi,lo = lo *180/pi,y=y)

## fit spline on sphere model...
bp <- gam(y~s(la,lo,bs="sos",k=60),data=dat)

## pure knot based alternative...
ind <- sample(1:n,100)
bk <- gam(y~s(la,lo,bs="sos",k=60),
  knots=list(la=dat$la[ind],lo=dat$lo[ind]),data=dat)

b <- bp
```



```

cor(fitted(b), ff)

## plot results and truth...

pd <- data.frame(la=gr$la*180/pi, lo=gr$lo*180/pi)
fv <- matrix(predict(b, pd), 30, 60)

par(mfrow=c(2,2), mar=c(4,4,1,1))
contour(lom, lam, t(zm))
contour(lom, lam, t(fv))
plot(bp, rug=FALSE)
plot(bp, scheme=1, theta=-30, phi=20, pch=19, cex=.5)

```

```
smooth.construct.t2.smooth.spec
```

Tensor product smoothing constructor

Description

A special `smooth.construct` method function for creating tensor product smooths from any combination of single penalty marginal smooths, using the construction of Wood, Scheipl and Faraway (2013).

Usage

```
## S3 method for class 't2.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

<code>object</code>	a smooth specification object of class <code>t2.smooth.spec</code> , usually generated by a term like <code>t2(x, z)</code> in a <code>gam</code> model formula
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be <code>NULL</code> . See details for further information.

Details

Tensor product smooths are smooths of several variables which allow the degree of smoothing to be different with respect to different variables. They are useful as smooth interaction terms, as they are invariant to linear rescaling of the covariates, which means, for example, that they are insensitive to the measurement units of the different covariates. They are also useful whenever isotropic smoothing is inappropriate. See [t2](#), [te](#), [smooth.construct](#) and [smooth.terms](#). The construction employed here produces tensor smooths for which the smoothing penalties are non-overlapping portions of the identity matrix. This makes their estimation by mixed modelling software rather easy.

Value

An object of class "t2.smooth".

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., F. Scheipl and J.J. Faraway (2013) Straightforward intermediate rank tensor product smoothing in mixed models. *Statistics and Computing* 23: 341-360.

See Also

[t2](#)

Examples

```
## see ?t2
```

```
smooth.construct.tensor.smooth.spec
```

Tensor product smoothing constructor

Description

A special smooth.construct method function for creating tensor product smooths from any combination of single penalty marginal smooths.

Usage

```
## S3 method for class 'tensor.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

object	a smooth specification object of class tensor.smooth.spec, usually generated by a term like te(x, z) in a gam model formula
data	a list containing just the data (including any by variable) required by this term, with names corresponding to object\$term (and object\$by). The by variable is the last element.
knots	a list containing any knots supplied for basis setup — in same order and with same names as data. Can be NULL. See details for further information.

Details

Tensor product smooths are smooths of several variables which allow the degree of smoothing to be different with respect to different variables. They are useful as smooth interaction terms, as they are invariant to linear rescaling of the covariates, which means, for example, that they are insensitive to the measurement units of the different covariates. They are also useful whenever isotropic smoothing is inappropriate. See [te](#), [smooth.construct](#) and [smooth.terms](#).

Value

An object of class "tensor.smooth". See [smooth.construct](#), for the elements that this object will contain.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

See Also

[cSplineDes](#)

Examples

```
## see ?gam
```

smooth.construct.tp.smooth.spec

Penalized thin plate regression splines in GAMs

Description

[gam](#) can use isotropic smooths of any number of variables, specified via terms like `s(x, z, bs="tp", m=3)` (or just `s(x, z)` as this is the default basis). These terms are based on thin plate regression splines. `m` specifies the order of the derivatives in the thin plate spline penalty. If `m` is a vector of length 2 and the second element is zero, then the penalty null space of the smooth is not included in the smooth: this is useful if you need to test whether a smooth could be replaced by a linear term, for example.

Thin plate regression splines are constructed by starting with the basis and penalty for a full thin plate spline and then truncating this basis in an optimal manner, to obtain a low rank smoother. Details are given in Wood (2003). One key advantage of the approach is that it avoids the knot placement problems of conventional regression spline modelling, but it also has the advantage that smooths of lower rank are nested within smooths of higher rank, so that it is legitimate to use conventional hypothesis testing methods to compare models based on pure regression splines. Note

that the basis truncation does not change the meaning of the thin plate spline penalty (it penalizes exactly what it would have penalized for a full thin plate spline).

The t.p.r.s. basis and penalties can become expensive to calculate for large datasets. For this reason the default behaviour is to randomly subsample `max.knots` unique data locations if there are more than `max.knots` such, and to use the sub-sample for basis construction. The sampling is always done with the same random seed to ensure repeatability (does not reset R RNG). `max.knots` is 2000, by default. Both `seed` and `max.knots` can be modified using the `xt` argument to `s`. Alternatively the user can supply knots from which to construct a basis.

The "ts" smooths are t.p.r.s. with the penalty modified so that the term is shrunk to zero for high enough smoothing parameter, rather than being shrunk towards a function in the penalty null space (see details).

Usage

```
## S3 method for class 'tp.smooth.spec'
smooth.construct(object, data, knots)
## S3 method for class 'ts.smooth.spec'
smooth.construct(object, data, knots)
```

Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>s(...,bs="tp",...)</code> or <code>s(...,bs="ts",...)</code>
<code>data</code>	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code>). The by variable is the last element.
<code>knots</code>	a list containing any knots supplied for basis setup — in same order and with same names as <code>data</code> . Can be NULL

Details

The default basis dimension for this class is $k=M+k.def$ where M is the null space dimension (dimension of unpenalized function space) and $k.def$ is 8 for dimension 1, 27 for dimension 2 and 100 for higher dimensions. This is essentially arbitrary, and should be checked, but as with all penalized regression smoothers, results are statistically insensitive to the exact choice, provided it is not so small that it forces oversmoothing (the smoother's degrees of freedom are controlled primarily by its smoothing parameter).

The default is to set m (the order of derivative in the thin plate spline penalty) to the smallest value satisfying $2m > d+1$ where d is the number of covariates of the term: this yields 'visually smooth' functions. In any case $2m>d$ must be satisfied.

The constructor is not normally called directly, but is rather used internally by `gam`. To use for basis setup it is recommended to use `smooth.construct2`.

For these classes the specification object will contain information on how to handle large datasets in their `xt` field. The default is to randomly subsample 2000 'knots' from which to produce a tprs basis, if the number of unique predictor variable combinations in excess of 2000. The default can be modified via the `xt` argument to `s`. This is supplied as a list with elements `max.knots` and `seed`

containing a number to use in place of 2000, and the random number seed to use (either can be missing).

For these bases knots has two uses. Firstly, as mentioned already, for large datasets the calculation of the tp basis can be time-consuming. The user can retain most of the advantages of the t.p.r.s. approach by supplying a reduced set of covariate values from which to obtain the basis - typically the number of covariate values used will be substantially smaller than the number of data, and substantially larger than the basis dimension, k . This approach is the one taken automatically if the number of unique covariate values (combinations) exceeds `max.knots`. The second possibility is to avoid the eigen-decomposition used to find the t.p.r.s. basis altogether and simply use the basis implied by the chosen knots: this will happen if the number of knots supplied matches the basis dimension, k . For a given basis dimension the second option is faster, but gives poorer results (and the user must be quite careful in choosing knot locations).

The shrinkage version of the smooth, eigen-decomposes the wiggleness penalty matrix, and sets its zero eigenvalues to small multiples of the smallest strictly positive eigenvalue. The penalty is then set to the matrix with eigenvectors corresponding to those of the original penalty, but eigenvalues set to the perturbed versions. This penalty matrix has full rank and shrinks the curve to zero at high enough smoothing parameters.

Value

An object of class "tprs.smooth" or "ts.smooth". In addition to the usual elements of a smooth class documented under [smooth.construct](#), this object will contain:

<code>shift</code>	A record of the shift applied to each covariate in order to center it around zero and avoid any co-linearity problems that might otehrwise occur in the penalty null space basis of the term.
<code>Xu</code>	A matrix of the unique covariate combinations for this smooth (the basis is constructed by first stripping out duplicate locations).
<code>UZ</code>	The matrix mapping the t.p.r.s. parameters back to the parameters of a full thin plate spline.
<code>null.space.dimension</code>	The dimension of the space of functions that have zero wiggleness according to the wiggleness penalty for this term.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2003) Thin plate regression splines. J.R.Statist.Soc.B 65(1):95-114

Examples

```
require(mgcv); n <- 100; set.seed(2)
x <- runif(n); y <- x + x^2*.2 + rnorm(n) *.1
## is smooth significantly different from straight line?
summary(gam(y~s(x,m=c(2,0))+x,method="REML")) ## not quite
## is smooth significatly different from zero?
```

```
summary(gam(y~s(x),method="REML")) ## yes!

## example of knot based tprs...
k <- 10; m <- 2
y <- y[order(x)]; x <- x[order(x)]
b <- gam(y~s(x,k=k,m=m),method="REML",
        knots=list(x=seq(0,1,length=k)))
X <- model.matrix(b)
par(mfrow=c(1,2))
plot(x,X[,1],ylim=range(X),type="l")
for (i in 2:ncol(X)) lines(x,X[,i],col=i)

## compare with eigen based (default)
b1 <- gam(y~s(x,k=k,m=m),method="REML")
X1 <- model.matrix(b1)
plot(x,X1[,1],ylim=range(X1),type="l")
for (i in 2:ncol(X1)) lines(x,X1[,i],col=i)
## see ?gam
```

smooth.terms

Smooth terms in GAM

Description

Smooth terms are specified in a `gam` formula using `s`, `te`, `ti` and `t2` terms. Various smooth classes are available, for different modelling tasks, and users can add smooth classes (see [user.defined.smooth](#)). What defines a smooth class is the basis used to represent the smooth function and quadratic penalty (or multiple penalties) used to penalize the basis coefficients in order to control the degree of smoothness. Smooth classes are invoked directly by `s` terms, or as building blocks for tensor product smoothing via `te`, `ti` or `t2` terms (only smooth classes with single penalties can be used in tensor products). The smooths built into the `mgcv` package are all based one way or another on low rank versions of splines. For the full rank versions see Wahba (1990).

Note that smooths can be used rather flexibly in `gam` models. In particular the linear predictor of the GAM can depend on (a discrete approximation to) any linear functional of a smooth term, using by variables and the ‘summation convention’ explained in [linear.functional.terms](#).

The single penalty built in smooth classes are summarized as follows

Thin plate regression splines `bs="tp"`. These are low rank isotropic smoothers of any number of covariates. By isotropic is meant that rotation of the covariate co-ordinate system will not change the result of smoothing. By low rank is meant that they have far fewer coefficients than there are data to smooth. They are reduced rank versions of the thin plate splines and use the thin plate spline penalty. They are the default smooth for `s` terms because there is a defined sense in which they are the optimal smoother of any given basis dimension/rank (Wood, 2003). Thin plate regression splines do not have ‘knots’ (at least not in any conventional sense): a truncated eigen-decomposition is used to achieve the rank reduction. See [tprs](#) for further details.

`bs="ts"` is as `"tp"` but with a modification to the smoothing penalty, so that the null space is also penalized slightly and the whole term can therefore be shrunk to zero.

- Duchon splines** `bs="ds"`. These generalize thin plate splines. In particular, for any given number of covariates they allow lower orders of derivative in the penalty than thin plate splines (and hence a smaller null space). See [Duchon.spline](#) for further details.
- Cubic regression splines** `bs="cr"`. These have a cubic spline basis defined by a modest sized set of knots spread evenly through the covariate values. They are penalized by the conventional integrated square second derivative cubic spline penalty. For details see [cubic.regression.spline](#) and e.g. Wood (2006a).
`bs="cs"` specifies a shrinkage version of `"cr"`.
`bs="cc"` specifies a cyclic cubic regression splines (see [cyclic.cubic.spline](#)). i.e. a penalized cubic regression splines whose ends match, up to second derivative.
- Splines on the sphere** `bs="sos"`. These are two dimensional splines on a sphere. Arguments are latitude and longitude, and they are the analogue of thin plate splines for the sphere. Useful for data sampled over a large portion of the globe, when isotropy is appropriate. See [Spherical.Spline](#) for details.
- P-splines** `bs="ps"`. These are P-splines as proposed by Eilers and Marx (1996). They combine a B-spline basis, with a discrete penalty on the basis coefficients, and any sane combination of penalty and basis order is allowed. Although this penalty has no exact interpretation in terms of function shape, in the way that the derivative penalties do, P-splines perform almost as well as conventional splines in many standard applications, and can perform better in particular cases where it is advantageous to mix different orders of basis and penalty.
`bs="cp"` gives a cyclic version of a P-spline (see [cyclic.p.spline](#)).
- Random effects** `bs="re"`. These are parametric terms penalized by a ridge penalty (i.e. the identity matrix). When such a smooth has multiple arguments then it represents the parametric interaction of these arguments, with the coefficients penalized by a ridge penalty. The ridge penalty is equivalent to an assumption that the coefficients are i.i.d. normal random effects. See [smooth.construct.re.smooth.spec](#).
- Markov Random Fields** `bs="mrf"`. These are popular when space is split up into discrete contiguous geographic units (districts of a town, for example). In this case a simple smoothing penalty is constructed based on the neighbourhood structure of the geographic units. See [mrf](#) for details and an example.
- Gaussian process smooths** `bs="gp"`. Gaussian process models with a variety of simple correlation functions can be represented as smooths. See [gp.smooth](#) for details.
- Soap film smooths** `bs="so"` (actually not single penalized, but `bs="sw"` and `bs="sf"` allows splitting into single penalty components for use in tensor product smoothing). These are finite area smoothers designed to smooth within complicated geographical boundaries, where the boundary matters (e.g. you do not want to smooth across boundary features). See [soap](#) for details.

Broadly speaking the default penalized thin plate regression splines tend to give the best MSE performance, but they are slower to set up than the other bases. The knot based penalized cubic regression splines (with derivative based penalties) usually come next in MSE performance, with the P-splines doing just a little worse. However the P-splines are useful in non-standard situations.

All the preceding classes (and any user defined smooths with single penalties) may be used as marginal bases for tensor product smooths specified via [te](#), [ti](#) or [t2](#) terms. Tensor product smooths are smooth functions of several variables where the basis is built up from tensor products of bases for smooths of fewer (usually one) variable(s) (marginal bases). The multiple penalties for these

smooths are produced automatically from the penalties of the marginal smooths. Wood (2006b) and Wood, Scheipl and Faraway (2012), give the general recipe for these constructions.

- te** te smooths have one penalty per marginal basis, each of which is interpretable in a similar way to the marginal penalty from which it is derived. See Wood (2006b).
- ti** ti smooths exclude the basis functions associated with the ‘main effects’ of the marginal smooths, plus interactions other than the highest order specified. These provide a stable and interpretable way of specifying models with main effects and interactions. For example if we are interested in linear predictor $f_1(x) + f_2(z) + f_3(x, z)$, we might use model formula $y \sim s(x) + s(z) + ti(x, z)$ or $y \sim ti(x) + ti(z) + te(x, z)$. A similar construction involving te terms instead will be much less statistically stable.
- t2** t2 uses an alternative tensor product construction that results in more penalties each having a simple non-overlapping structure allowing use with the gamm4 package. It is a natural generalization of the SS-ANOVA construction, but the penalties are a little harder to interpret. See Wood, Scheipl and Faraway (2012/13).

Tensor product smooths often perform better than isotropic smooths when the covariates of a smooth are not naturally on the same scale, so that their relative scaling is arbitrary. For example, if smoothing with respect to time and distance, an isotropic smoother will give very different results if the units are cm and minutes compared to if the units are metres and seconds: a tensor product smooth will give the same answer in both cases (see **te** for an example of this). Note that te terms are knot based, and the thin plate splines seem to offer no advantage over cubic or P-splines as marginal bases.

Some further specialist smoothers that are not suitable for use in tensor products are also available.

Adaptive smoothers bs="ad" Univariate and bivariate adaptive smooths are available (see [adaptive.smooth](#)).

These are appropriate when the degree of smoothing should itself vary with the covariates to be smoothed, and the data contain sufficient information to be able to estimate the appropriate variation. Because this flexibility is achieved by splitting the penalty into several ‘basis penalties’ these terms are not suitable as components of tensor product smooths, and are not supported by gamm.

Factor smooth interactions bs="fs" Smooth factor interactions are often produced using by variables (see [gam.models](#)), but a special smoother class (see [factor.smooth.interaction](#)) is available for the case in which a smooth is required at each of a large number of factor levels (for example a smooth for each patient in a study), and each smooth should have the same smoothing parameter. The "fs" smoothers are set up to be efficient when used with [gamm](#), and have penalties on each null space component (i.e. they are fully ‘random effects’).

Author(s)

Simon Wood <simon.wood@r-project.org>

References

- Eilers, P.H.C. and B.D. Marx (1996) Flexible Smoothing with B-splines and Penalties. *Statistical Science*, 11(2):89-121
- Wahba (1990) *Spline Models of Observational Data*. SIAM
- Wood, S.N. (2003) Thin plate regression splines. *J.R.Statist.Soc.B* 65(1):95-114

Wood, S.N. (2006a) *Generalized Additive Models: an introduction with R*, CRC

Wood, S.N. (2006b) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

Wood S.N., F. Scheipl and J.J. Faraway (2013) Straightforward intermediate rank tensor product smoothing in mixed models. *Statistical Computing*. 23(3), 341-360. [online 2012]

See Also

[s](#), [te](#), [t2](#) [tprs](#), [Duchon.spline](#), [cubic.regression.spline](#), [p.spline](#), [mrf](#), [soap](#), [Spherical.Spline](#), [adaptive.smooth](#), [user.defined.smooth](#), [smooth.construct.re.smooth.spec](#), [smooth.construct.gp.smooth.spec](#),

Examples

```
## see examples for gam and gamm
```

smooth2random	<i>Convert a smooth to a form suitable for estimating as random effect</i>
---------------	--

Description

A generic function for converting mgcv smooth objects to forms suitable for estimation as random effects by e.g. lme. Exported mostly for use by other package developers.

Usage

```
smooth2random(object, vnames, type=1)
```

Arguments

object	an mgcv smooth object.
vnames	a vector of names to avoid as dummy variable names in the random effects form.
type	1 for lme, otherwise lmer.

Details

There is a duality between smooths and random effects which means that smooths can be estimated using mixed modelling software. This function converts standard mgcv smooth objects to forms suitable for estimation by lme, for example. A service routine for [gamm](#) exported for use by package developers.

Value

A list.

`rand` a list of random effects, including grouping factors, and a fixed effects matrix. Grouping factors, model matrix and model matrix name attached as attributes, to each element.

`trans.D` A vector, `trans.D`, that transforms coefs, in order [`rand1`, `rand2`,... `fix`] back to original parameterization. If null, then taken as vector of ones. `b.original = trans.U %*% (trans.D*b`

`trans.U` A matrix, `trans.U`, that transforms coefs, in order [`rand1`, `rand2`,... `fix`] back to original parameterization. If null, then not needed. If null then taken as identity.

`Xf` A matrix for the fixed effects, if any.

`fixed` TRUE/FALSE, indicating if term was unpenalized or not. If unpenalized then other stuff may not be returned (it's not a random effect).

`rind` an index vector such that if `br` is the vector of random coefficients for the term, `br[rind]` is the coefs in order for this term.

`pen.ind` index of which penalty penalizes each coefficient: 0 for unpenalized.

Author(s)

Simon N. Wood <simon.wood@r-project.org>.

References

Wood S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall/CRC Press.

See Also

[gamm](#)

Examples

```
library(mgcv)
x <- runif(30)
sm <- smoothCon(s(x), data.frame(x=x))[[1]]
smooth2random(sm, "")
```

smoothCon

*Prediction/Construction wrapper functions for GAM smooth terms***Description**

Wrapper functions for construction of and prediction from smooth terms in a GAM. The purpose of the wrappers is to allow user-transparent re-parameterization of smooth terms, in order to allow identifiability constraints to be absorbed into the parameterization of each term, if required. The routine also handles ‘by’ variables and construction of identifiability constraints automatically, although this behaviour can be over-ridden.

Usage

```
smoothCon(object, data, knots=NULL, absorb.cons=FALSE,
          scale.penalty=TRUE, n=nrow(data), dataX=NULL,
          null.space.penalty=FALSE, sparse.cons=0,
          diagonal.penalty=FALSE, apply.by=TRUE, modCon=0)
PredictMat(object, data, n=nrow(data))
```

Arguments

object	is a smooth specification object or a smooth object.
data	A data frame, model frame or list containing the values of the (named) covariates at which the smooth term is to be evaluated. If it’s a list then n must be supplied.
knots	An optional data frame supplying any knot locations to be supplied for basis construction.
absorb.cons	Set to TRUE in order to have identifiability constraints absorbed into the basis.
scale.penalty	should the penalty coefficient matrix be scaled to have approximately the same ‘size’ as the inner product of the terms model matrix with itself? This can improve the performance of gamm fitting.
n	number of values for each covariate, or if a covariate is a matrix, the number of rows in that matrix: must be supplied explicitly if data is a list.
dataX	Sometimes the basis should be set up using data in data, but the model matrix should be constructed with another set of data provided in dataX — n is assumed to be the same for both. Facilitates smooth id’s.
null.space.penalty	Should an extra penalty be added to the smooth which will penalize the components of the smooth in the penalty null space: provides a way of penalizing terms out of the model altogether.
apply.by	set to FALSE to have basis setup exactly as in default case, but to return add an additional matrix X0 to the return object, containing the model matrix without the by variable, if a by variable is present. Useful for bam discrete method setup.

<code>sparse.cons</code>	If 0 then default sum to zero constraints are used. If -1 then sweep and drop sum to zero constraints are used (default with <code>bam</code>). If 1 then one coefficient is set to zero as constraint for sparse smooths. If 2 then sparse coefficient sum to zero constraints are used for sparse smooths. None of these options has an effect if the smooth supplies its own constraint.
<code>diagonal.penalty</code>	If TRUE then the smooth is reparameterized to turn the penalty into an identity matrix, with the final diagonal elements zeroed (corresponding to the penalty nullspace). May result in a matrix <code>diagRP</code> in the returned object for use by <code>PredictMat</code> .
<code>modCon</code>	force modification of any smooth supplied constraints. 0 - do nothing. 1 - delete supplied constraints, replacing with automatically generated ones. 2 - set fit and predict constraint to predict constraint. 3 - set fit and predict constraint to fit constraint.

Details

These wrapper functions exist to allow smooths specified using `smooth.construct` and `Predict.matrix` method functions to be re-parameterized so that identifiability constraints are no longer required in fitting. This is done in a user transparent manner, but is typically of no importance in use of GAMs. The routine's also handle by variables and will create default identifiability constraints.

If a user defined smooth constructor handles by variables itself, then its returned smooth object should contain an object by `.done`. If this does not exist then `smoothCon` will use the default code. Similarly if a user defined `Predict.matrix` method handles by variables internally then the returned matrix should have a `"by.done"` attribute.

Default centering constraints, that terms should sum to zero over the covariates, are produced unless the smooth constructor includes a matrix C of constraints. To have no constraints (in which case you had better have a full rank penalty!) the matrix C should have no rows. There is an option to use centering constraint that generate no, or limited infill, if the smoother has a sparse model matrix.

`smoothCon` returns a list of smooths because factor by variables result in multiple copies of a smooth, each multiplied by the dummy variable associated with one factor level. `smoothCon` modifies the smooth object labels in the presence of by variables, to ensure that they are unique, it also stores the level of a by variable factor associated with a smooth, for later use by `PredictMat`.

The parameterization used by `gam` can be controlled via `gam.control`.

Value

From `smoothCon` a list of smooth objects returned by the appropriate `smooth.construct` method function. If constraints are to be absorbed then the objects will have attributes `"qrc"` and `"nCons"`. `"nCons"` is the number of constraints. `"qrc"` is usually the qr decomposition of the constraint matrix (returned by `qr`), but if it is a single positive integer it is the index of the coefficient to set to zero, and if it is a negative number then this indicates that the parameters are to sum to zero.

For `predictMat` a matrix which will map the parameters associated with the smooth to the vector of values of the smooth evaluated at the covariate values given in object.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[gam.control](#), [smooth.construct](#), [Predict.matrix](#)

Examples

```
## example of using smoothCon and PredictMat to set up a basis
## to use for regression and make predictions using the result
library(MASS) ## load for mcycle data.
## set up a smoother...
sm <- smoothCon(s(times,k=10),data=mcycle,knots=NULL)[[1]]
## use it to fit a regression spline model...
beta <- coef(lm(mcycle$accel~sm$X-1))
with(mcycle,plot(times,accel)) ## plot data
times <- seq(0,60,length=200) ## creat prediction times
## Get matrix mapping beta to spline prediction at 'times'
Xp <- PredictMat(sm,data.frame(times=times))
lines(times,Xp*%beta) ## add smooth to plot

## Same again but using a penalized regression spline of
## rank 30....
sm <- smoothCon(s(times,k=30),data=mcycle,knots=NULL)[[1]]
E <- t(mroot(sm$S[[1]])) ## square root penalty
X <- rbind(sm$X,0.1*E) ## augmented model matrix
y <- c(mcycle$accel,rep(0,nrow(E))) ## augmented data
beta <- coef(lm(y~X-1)) ## fit penalized regression spline
Xp <- PredictMat(sm,data.frame(times=times)) ## prediction matrix
with(mcycle,plot(times,accel)) ## plot data
lines(times,Xp*%beta) ## overlay smooth
```

sp.vcov

Extract smoothing parameter estimator covariance matrix from (RE)ML GAM fit

Description

Extracts the estimated covariance matrix for the log smoothing parameter estimates from a (RE)ML estimated gam object, provided the fit was with a method that evaluated the required Hessian.

Usage

```
sp.vcov(x)
```

Arguments

x a fitted model object of class gam as produced by gam().

Details

Just extracts the inverse of the hessian matrix of the negative (restricted) log likelihood w.r.t the log smoothing parameters, if this has been obtained as part of fitting.

Value

A matrix corresponding to the estimated covariance matrix of the log smoothing parameter estimators, if this can be extracted, otherwise NULL. If the scale parameter has been (RE)ML estimated (i.e. if the method was "ML" or "REML" and the scale parameter was unknown) then the last row and column relate to the log scale parameter.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) On confidence intervals for generalized additive models based on penalized regression splines. Australian and New Zealand Journal of Statistics. 48(4): 445-464.

See Also

[gam](#), [gam.vcomp](#)

Examples

```
require(mgcv)
n <- 100
x <- runif(n); z <- runif(n)
y <- sin(x*2*pi) + rnorm(n)*.2
mod <- gam(y~s(x,bs="cc",k=10)+s(z),knots=list(x=seq(0,1,length=10)),
           method="REML")
sp.vcov(mod)
```

spasm.construct

Experimental sparse smoothers

Description

These are experimental sparse smoothing functions, and should be left well alone!

Usage

```
spasm.construct(object, data)
spasm.sp(object, sp, w=rep(1, object$nobs), get.trH=TRUE, block=0, centre=FALSE)
spasm.smooth(object, X, residual=FALSE, block=0)
```

Arguments

object	sparse smooth object
data	data frame
sp	smoothing parameter value
w	optional weights
get.trH	Should (estimated) trace of sparse smoother matrix be returned
block	index of block, 0 for all blocks
centre	should sparse smooth be centred?
X	what to smooth
residual	apply residual operation?

WARNING

It is not recommended to use these yet

Author(s)

Simon N. Wood <simon.wood@r-project.org>

step.gam

Alternatives to step.gam

Description

There is no `step.gam` in package `mgcv`. The `mgcv` default for model selection is to use either prediction error criteria such as GCV, GACV, Mallows' Cp/AIC/UBRE or the likelihood based methods of REML or ML. Since the smoothness estimation part of model selection is done in this way it is logically most consistent to perform the rest of model selection in the same way. i.e. to decide which terms to include or omit by looking at changes in GCV, AIC, REML etc.

To facilitate fully automatic model selection the package implements two smooth modification techniques which can be used to allow smooths to be shrunk to zero as part of smoothness selection.

Shrinkage smoothers are smoothers in which a small multiple of the identity matrix is added to the smoothing penalty, so that strong enough penalization will shrink all the coefficients of the smooth to zero. Such smoothers can effectively be penalized out of the model altogether, as part of smoothing parameter estimation. 2 classes of these shrinkage smoothers are implemented: "cs" and "ts", based on cubic regression spline and thin plate regression spline smoothers (see [s](#))

Null space penalization An alternative is to construct an extra penalty for each smooth which penalizes the space of functions of zero wiggleness according to its existing penalties. If all the smoothing parameters for such a term tend to infinity then the term is penalized to zero, and is effectively dropped from the model. The advantage of this approach is that it can be implemented automatically for any smooth. The `select` argument to `gam` causes this latter approach to be used. Unpenalized terms (e.g. `s(x, fx=TRUE)`) remain unpenalized.

REML and ML smoothness selection are equivalent under this approach, and simulation evidence suggests that they tend to perform a little better than prediction error criteria, for model selection.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Marra, G. and S.N. Wood (2011) Practical variable selection for generalized additive models Computational Statistics and Data Analysis 55,2372-2387

See Also

[gam.selection](#)

Examples

```
## an example of GCV based model selection as
## an alternative to stepwise selection, using
## shrinkage smoothers...
library(mgcv)
set.seed(0);n <- 400
dat <- gamSim(1,n=n,scale=2)
dat$x4 <- runif(n, 0, 1)
dat$x5 <- runif(n, 0, 1)
attach(dat)
## Note the increased gamma parameter below to favour
## slightly smoother models...
b<-gam(y~s(x0,bs="ts")+s(x1,bs="ts")+s(x2,bs="ts")+
  s(x3,bs="ts")+s(x4,bs="ts")+s(x5,bs="ts"),gamma=1.4)
summary(b)
plot(b,pages=1)

## Same again using REML/ML
b<-gam(y~s(x0,bs="ts")+s(x1,bs="ts")+s(x2,bs="ts")+
  s(x3,bs="ts")+s(x4,bs="ts")+s(x5,bs="ts"),method="REML")
summary(b)
plot(b,pages=1)

## And once more, but using the null space penalization
b<-gam(y~s(x0,bs="cr")+s(x1,bs="cr")+s(x2,bs="cr")+
  s(x3,bs="cr")+s(x4,bs="cr")+s(x5,bs="cr"),
  method="REML",select=TRUE)
summary(b)
plot(b,pages=1)

detach(dat);rm(dat)
```


summary.gam

*Summary for a GAM fit***Description**

Takes a fitted gam object produced by `gam()` and produces various useful summaries from it. (See [sink](#) to divert output to a file.)

Usage

```
## S3 method for class 'gam'
summary(object, dispersion=NULL, freq=FALSE, p.type = 0, ...)

## S3 method for class 'summary.gam'
print(x,digits = max(3, getOption("digits") - 3),
      signif.stars = getOption("show.signif.stars"),...)
```

Arguments

<code>object</code>	a fitted gam object as produced by <code>gam()</code> .
<code>x</code>	a <code>summary.gam</code> object produced by <code>summary.gam()</code> .
<code>dispersion</code>	A known dispersion parameter. NULL to use estimate or default (e.g. 1 for Poisson).
<code>freq</code>	By default p-values for parametric terms are calculated using the Bayesian estimated covariance matrix of the parameter estimators. If this is set to TRUE then the frequentist covariance matrix of the parameters is used instead.
<code>p.type</code>	determines how p-values are computed for smooth terms. 0 uses a test statistic with distribution determined by the un-rounded edf of the term. 1 uses upwardly biased rounding of the edf and -1 uses a version of the test statistic with a null distribution that has to be simulated. 5 is the approximation in Wood (2006). Other options are poor, generate a warning, and are only of research interest. See details.
<code>digits</code>	controls number of digits printed in output.
<code>signif.stars</code>	Should significance stars be printed alongside output.
<code>...</code>	other arguments.

Details

Model degrees of freedom are taken as the trace of the influence (or hat) matrix \mathbf{A} for the model fit. Residual degrees of freedom are taken as number of data minus model degrees of freedom. Let \mathbf{P}_i be the matrix giving the parameters of the i th smooth when applied to the data (or pseudodata in the generalized case) and let \mathbf{X} be the design matrix of the model. Then $tr(\mathbf{X}\mathbf{P}_i)$ is the edf for the i th term. Clearly this definition causes the edf's to add up properly! An alternative version of EDF is more appropriate for p-value computation, and is based on the trace of $2\mathbf{A} - \mathbf{A}\mathbf{A}$.

`print.summary.gam` tries to print various bits of summary information useful for term selection in a pretty way.

P-values for smooth terms are usually based on a test statistic motivated by an extension of Nychka's (1988) analysis of the frequentist properties of Bayesian confidence intervals for smooths (Marra and Wood, 2012). These have better frequentist performance (in terms of power and distribution under the null) than the alternative strictly frequentist approximation. When the Bayesian intervals have good across the function properties then the p-values have close to the correct null distribution and reasonable power (but there are no optimality results for the power). Full details are in Wood (2013b), although what is computed is actually a slight variant in which the components of the test statistic are weighted by the iterative fitting weights.

Note that for terms with no unpenalized terms (such as Gaussian random effects) the Nychka (1988) requirement for smoothing bias to be substantially less than variance breaks down (see e.g. appendix of Marra and Wood, 2012), and this results in incorrect null distribution for p-values computed using the above approach. In this case it is necessary to use an alternative approach designed for random effects variance components, and this is done. See Wood (2013a) for details: the test is based on a likelihood ratio statistic (with the reference distribution appropriate for the null hypothesis on the boundary of the parameter space).

All p-values are computed without considering uncertainty in the smoothing parameter estimates.

In simulations the p-values have best behaviour under ML smoothness selection, with REML coming second. In general the p-values behave well, but neglecting smoothing parameter uncertainty means that they may be somewhat too low when smoothing parameters are highly uncertain. High uncertainty happens in particular when smoothing parameters are poorly identified, which can occur with nested smooths or highly correlated covariates (high concavity).

If `p.type=5` then the frequentist approximation for p-values of smooth terms described in section 4.8.5 of Wood (2006) is used. The approximation is not as good as the default, and is no longer recommended.

By default the p-values for parametric model terms are also based on Wald tests using the Bayesian covariance matrix for the coefficients. This is appropriate when there are "re" terms present, and is otherwise rather similar to the results using the frequentist covariance matrix (`freq=TRUE`), since the parametric terms themselves are usually unpenalized. Default P-values for parameteric terms that are penalized using the `paraPen` argument will not be good. However if such terms represent conventional random effects with full rank penalties, then setting `freq=TRUE` is appropriate.

Value

`summary.gam` produces a list of summary information for a fitted `gam` object.

<code>p.coeff</code>	is an array of estimates of the strictly parametric model coefficients.
<code>p.t</code>	is an array of the <code>p.coeff</code> 's divided by their standard errors.
<code>p.pv</code>	is an array of p-values for the null hypothesis that the corresponding parameter is zero. Calculated with reference to the t distribution with the estimated residual degrees of freedom for the model fit if the dispersion parameter has been estimated, and the standard normal if not.
<code>m</code>	The number of smooth terms in the model.
<code>chi.sq</code>	An array of test statistics for assessing the significance of model smooth terms. See details.

<code>s.pv</code>	An array of approximate p-values for the null hypotheses that each smooth term is zero. Be warned, these are only approximate.
<code>se</code>	array of standard error estimates for all parameter estimates.
<code>r.sq</code>	The adjusted r-squared for the model. Defined as the proportion of variance explained, where original variance and residual variance are both estimated using unbiased estimators. This quantity can be negative if your model is worse than a one parameter constant model, and can be higher for the smaller of two nested models! The proportion null deviance explained is probably more appropriate for non-normal errors. Note that <code>r.sq</code> does not include any offset in the one parameter model.
<code>dev.expl</code>	The proportion of the null deviance explained by the model. The null deviance is computed taking account of any offset, so <code>dev.expl</code> can be substantially lower than <code>r.sq</code> when an offset is present.
<code>edf</code>	array of estimated degrees of freedom for the model terms.
<code>residual.df</code>	estimated residual degrees of freedom.
<code>n</code>	number of data.
<code>np</code>	number of model coefficients (regression coefficients, not smoothing parameters or other parameters of likelihood).
<code>rank</code>	apparent model rank.
<code>method</code>	The smoothing selection criterion used.
<code>sp.criterion</code>	The minimized value of the smoothness selection criterion. Note that for ML and REML methods, what is reported is the negative log marginal likelihood or negative log restricted likelihood.
<code>scale</code>	estimated (or given) scale parameter.
<code>family</code>	the family used.
<code>formula</code>	the original GAM formula.
<code>dispersion</code>	the scale parameter.
<code>pTerms.df</code>	the degrees of freedom associated with each parametric term (excluding the constant).
<code>pTerms.chi.sq</code>	a Wald statistic for testing the null hypothesis that the each parametric term is zero.
<code>pTerms.pv</code>	p-values associated with the tests that each term is zero. For penalized fits these are approximate. The reference distribution is an appropriate chi-squared when the scale parameter is known, and is based on an F when it is not.
<code>cov.unscaled</code>	The estimated covariance matrix of the parameters (or estimators if <code>freq=TRUE</code>), divided by scale parameter.
<code>cov.scaled</code>	The estimated covariance matrix of the parameters (estimators if <code>freq=TRUE</code>).
<code>p.table</code>	significance table for parameters
<code>s.table</code>	significance table for smooths
<code>p.Terms</code>	significance table for parametric model terms

WARNING

The p-values are approximate and neglect smoothing parameter uncertainty. They are likely to be somewhat too low when smoothing parameter estimates are highly uncertain: do read the details section. If the exact values matter, read Wood (2013a or b).

P-values for terms penalized via ‘paraPen’ are unlikely to be correct.

Author(s)

Simon N. Wood <simon.wood@r-project.org> with substantial improvements by Henric Nilsson.

References

Marra, G and S.N. Wood (2012) Coverage Properties of Confidence Intervals for Generalized Additive Model Components. *Scandinavian Journal of Statistics*, 39(1), 53-74.

Nychka (1988) Bayesian Confidence Intervals for Smoothing Splines. *Journal of the American Statistical Association* 83:1134-1143.

Wood, S.N. (2013a) A simple test for random effects in regression models. *Biometrika* 100:1005-1010

Wood, S.N. (2013b) On p-values for smooth components of an extended generalized additive model. *Biometrika* 100:221-228

Wood S.N. (2006) *Generalized Additive Models: An Introduction with R*. Chapman and Hall/CRC Press.

See Also

[gam](#), [predict.gam](#), [gam.check](#), [anova.gam](#), [gam.vcomp](#), [sp.vcov](#)

Examples

```
library(mgcv)
set.seed(0)

dat <- gamSim(1,n=200,scale=2) ## simulate data

b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),data=dat)
plot(b,pages=1)
summary(b)

## now check the p-values by using a pure regression spline....
b.d <- round(summary(b)$edf)+1 ## get edf per smooth
b.d <- pmax(b.d,3) # can't have basis dimension less than 3!
bc<-gam(y~s(x0,k=b.d[1],fx=TRUE)+s(x1,k=b.d[2],fx=TRUE)+
        s(x2,k=b.d[3],fx=TRUE)+s(x3,k=b.d[4],fx=TRUE),data=dat)
plot(bc,pages=1)
summary(bc)

## Example where some p-values are less reliable...
dat <- gamSim(6,n=200,scale=2)
b <- gam(y~s(x0,m=1)+s(x1)+s(x2)+s(x3)+s(fac,bs="re"),data=dat)
```

```

## Here s(x0,m=1) can be penalized to zero, so p-value approximation
## cruder than usual...
summary(b)

## p-value check - increase k to make this useful!
k<-20;n <- 200;p <- rep(NA,k)
for (i in 1:k)
{ b<-gam(y~te(x,z),data=data.frame(y=rnorm(n),x=runif(n),z=runif(n)),
  method="ML")
  p[i]<-summary(b)$s.p[1]
}
plot(((1:k)-0.5)/k,sort(p))
abline(0,1,col=2)
ks.test(p,"punif") ## how close to uniform are the p-values?

## A Gamma example, by modify `gamSim' output...

dat <- gamSim(1,n=400,dist="normal",scale=1)
dat$f <- dat$f/4 ## true linear predictor
Ey <- exp(dat$f);scale <- .5 ## mean and GLM scale parameter
## Note that `shape' and `scale' in `rgamma' are almost
## opposite terminology to that used with GLM/GAM...
dat$y <- rgamma(Ey*0,shape=1/scale,scale=Ey*scale)
bg <- gam(y~ s(x0)+ s(x1)+s(x2)+s(x3),family=Gamma(link=log),
  data=dat,method="REML")
summary(bg)

```

Description

Alternative to `te` for defining tensor product smooths in a `gam` formula. Results in a construction in which the penalties are non-overlapping multiples of identity matrices (with some rows and columns zeroed). The construction, which is due to Fabian Scheipl (mgcv implementation, 2010), is analogous to Smoothing Spline ANOVA (Gu, 2002), but using low rank penalized regression spline marginals. The main advantage of this construction is that it is useable with `gamm4` from package `gamm4`.

Usage

```
t2(..., k=NA,bs="cr",m=NA,d=NA,by=NA,xt=NULL,
  id=NULL,sp=NULL,full=FALSE,ord=NULL,pc=NULL)
```

Arguments

... a list of variables that are the covariates that this smooth is a function of. Transformations whose form depends on the values of the data are best avoided here: e.g. `t2(log(x),z)` is fine, but `t2(I(x/sd(x)),z)` is not (see `predict.gam`).

k	the dimension(s) of the bases used to represent the smooth term. If not supplied then set to 5^d . If supplied as a single number then this basis dimension is used for each basis. If supplied as an array then the elements are the dimensions of the component (marginal) bases of the tensor product. See choose.k for further information.
bs	array (or single character string) specifying the type for each marginal basis. "cr" for cubic regression spline; "cs" for cubic regression spline with shrinkage; "cc" for periodic/cyclic cubic regression spline; "tp" for thin plate regression spline; "ts" for t.p.r.s. with extra shrinkage. See smooth.terms for details and full list. User defined bases can also be used here (see smooth.construct for an example). If only one basis code is given then this is used for all bases.
m	The order of the spline and its penalty (for smooth classes that use this) for each term. If a single number is given then it is used for all terms. A vector can be used to supply a different m for each margin. For marginals that take vector m (e.g. p.spline and Duchon.spline), then a list can be supplied, with a vector element for each margin. NA autoinitializes. m is ignored by some bases (e.g. "cr").
d	array of marginal basis dimensions. For example if you want a smooth for 3 covariates made up of a tensor product of a 2 dimensional t.p.r.s. basis and a 1-dimensional basis, then set $d=c(2,1)$. Incompatibilities between built in basis types and dimension will be resolved by resetting the basis type.
by	a numeric or factor variable of the same dimension as each covariate. In the numeric vector case the elements multiply the smooth evaluated at the corresponding covariate values (a 'varying coefficient model' results). In the factor case causes a replicate of the smooth to be produced for each factor level. See gam.models for further details. May also be a matrix if covariates are matrices: in this case implements linear functional of a smooth (see gam.models and linear.functional.terms for details).
xt	Either a single object, providing any extra information to be passed to each marginal basis constructor, or a list of such objects, one for each marginal basis.
id	A label or integer identifying this term in order to link its smoothing parameters to others of the same type. If two or more smooth terms have the same id then they will have the same smoothing parameters, and, by default, the same bases (first occurrence defines basis type, but data from all terms used in basis construction).
sp	any supplied smoothing parameters for this term. Must be an array of the same length as the number of penalties for this smooth. Positive or zero elements are taken as fixed smoothing parameters. Negative elements signal auto-initialization. Over-rides values supplied in sp argument to gam . Ignored by gamm .
full	If TRUE then there is a separate penalty for each combination of null space column and range space. This gives strict invariance. If FALSE each combination of null space and range space generates one penalty, but the columns of each null space basis are treated as one group. The latter is more parsimonious, but does mean that invariance is only achieved by an arbitrary rescaling of null space basis vectors.

ord	an array giving the orders of terms to retain. Here order means number of marginal range spaces used in the construction of the component. NULL to retain everything.
pc	If not NULL, signals a point constraint: the smooth should pass through zero at the point given here (as a vector or list with names corresponding to the smooth names). Never ignored if supplied. See identifiability .

Details

Smooths of several covariates can be constructed from tensor products of the bases used to represent smooths of one (or sometimes more) of the covariates. To do this ‘marginal’ bases are produced with associated model matrices and penalty matrices. These are reparameterized so that the penalty is zero everywhere, except for some elements on the leading diagonal, which all have the same non-zero value. This reparameterization results in an unpenalized and a penalized subset of parameters, for each marginal basis (see e.g. appendix of Wood, 2004, for details).

The re-parameterized marginal bases are then combined to produce a basis for a single function of all the covariates (dimension given by the product of the dimensions of the marginal bases). In this set up there are multiple penalty matrices — all zero, but for a mixture of a constant and zeros on the leading diagonal. No two penalties have a non-zero entry in the same place.

Essentially the basis for the tensor product can be thought of as being constructed from a set of products of the penalized (range) or unpenalized (null) space bases of the marginal smooths (see Gu, 2002, section 2.4). To construct one of the set, choose either the null space or the range space from each marginal, and from these bases construct a product basis. The result is subject to a ridge penalty (unless it happens to be a product entirely of marginal null spaces). The whole basis for the smooth is constructed from all the different product bases that can be constructed in this way. The separately penalized components of the smooth basis each have an interpretation in terms of the ANOVA - decomposition of the term. See [pen.edf](#) for some further information.

Note that there are two ways to construct the product. When `full=FALSE` then the null space bases are treated as a whole in each product, but when `full=TRUE` each null space column is treated as a separate null space. The latter results in more penalties, but is the strict analog of the SS-ANOVA approach.

Tensor product smooths are especially useful for representing functions of covariates measured in different units, although they are typically not quite as nicely behaved as t.p.r.s. smooths for well scaled covariates.

Note also that GAMs constructed from lower rank tensor product smooths are nested within GAMs constructed from higher rank tensor product smooths if the same marginal bases are used in both cases (the marginal smooths themselves are just special cases of tensor product smooths.)

Note that tensor product smooths should not be centred (have identifiability constraints imposed) if any marginals would not need centering. The constructor for tensor product smooths ensures that this happens.

The function does not evaluate the variable arguments.

Value

A class `t2.smooth.spec` object defining a tensor product smooth to be turned into a basis and penalties by the `smooth.construct.tensor.smooth.spec` function.

The returned object contains the following items:

margin	A list of smooth . spec objects of the type returned by <code>s</code> , defining the basis from which the tensor product smooth is constructed.
term	An array of text strings giving the names of the covariates that the term is a function of.
by	is the name of any by variable as text ("NA" for none).
fx	logical array with element for each penalty of the term (tensor product smooths have multiple penalties). TRUE if the penalty is to be ignored, FALSE, otherwise.
label	A suitable text label for this smooth term.
dim	The dimension of the smoother - i.e. the number of covariates that it is a function of.
mp	TRUE is multiple penalties are to be used (default).
np	TRUE to re-parameterize 1-D marginal smooths in terms of function values (default).
id	the <code>id</code> argument supplied to <code>te</code> .
sp	the <code>sp</code> argument supplied to <code>te</code> .

Author(s)

Simon N. Wood <simon.wood@r-project.org> and Fabian Scheipl

References

Wood S.N., F. Scheipl and J.J. Faraway (2013, online Feb 2012) Straightforward intermediate rank tensor product smoothing in mixed models. *Statistical Computing*. 23(3):341-360

Gu, C. (2002) *Smoothing Spline ANOVA*, Springer.

Alternative approaches to functional ANOVA decompositions, *not* implemented by `t2` terms, are discussed in:

Belitz and Lang (2008) Simultaneous selection of variables and smoothing parameters in structured additive regression models. *Computational Statistics & Data Analysis*, 53(1):61-81

Lee, D-J and M. Durban (2011) P-spline ANOVA type interaction models for spatio-temporal smoothing. *Statistical Modelling*, 11:49-69

Wood, S.N. (2006) Low-Rank Scale-Invariant Tensor Product Smooths for Generalized Additive Mixed Models. *Biometrics* 62(4): 1025-1036.

See Also

[te](#) [s](#), [gam](#), [gamm](#),

Examples

```
# following shows how tensor product deals nicely with
# badly scaled covariates (range of x 5% of range of z )
require(mgcv)
test1<-function(x,z,sx=0.3,sz=0.4)
```



```

{ x<-x*20
  (pi**sx*sz)*(1.2*exp(-(x-0.2)^2/sx^2-(z-0.3)^2/sz^2)+
  0.8*exp(-(x-0.7)^2/sx^2-(z-0.8)^2/sz^2))
}
n<-500
old.par<-par(mfrow=c(2,2))
x<-runif(n)/20;z<-runif(n);
xs<-seq(0,1,length=30)/20;zs<-seq(0,1,length=30)
pr<-data.frame(x=rep(xs,30),z=rep(zs,rep(30,30)))
truth<-matrix(test1(pr$x,pr$z),30,30)
f <- test1(x,z)
y <- f + rnorm(n)*0.2
b1<-gam(y~s(x,z))
persp(xs,zs,truth);title("truth")
vis.gam(b1);title("t.p.r.s")
b2<-gam(y~t2(x,z))
vis.gam(b2);title("tensor product")
b3<-gam(y~t2(x,z,bs=c("tp","tp")))
vis.gam(b3);title("tensor product")
par(old.par)

test2<-function(u,v,w,sv=0.3,sw=0.4)
{ ((pi**sv*sw)*(1.2*exp(-(v-0.2)^2/sv^2-(w-0.3)^2/sw^2)+
  0.8*exp(-(v-0.7)^2/sv^2-(w-0.8)^2/sw^2)))*(u-0.5)^2*20
}
n <- 500
v <- runif(n);w<-runif(n);u<-runif(n)
f <- test2(u,v,w)
y <- f + rnorm(n)*0.2

## tensor product of 2D Duchon spline and 1D cr spline
m <- list(c(1,.5),0)
b <- gam(y~t2(v,w,u,k=c(30,5),d=c(2,1),bs=c("ds","cr"),m=m))

## look at the edf per penalty. "rr" denotes interaction term
## (range space range space). "rn" is interaction of null space
## for u with range space for v,w...
pen.edf(b)

## plot results...
op <- par(mfrow=c(2,2))
vis.gam(b,cond=list(u=0),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=.33),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=.67),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=1),color="heat",zlim=c(-0.2,3.5))
par(op)

b <- gam(y~t2(v,w,u,k=c(25,5),d=c(2,1),bs=c("tp","cr"),full=TRUE),
  method="ML")
## more penalties now. numbers in labels like "r1" indicate which
## basis function of a null space is involved in the term.
pen.edf(b)

```

te	<i>Define tensor product smooths or tensor product interactions in GAM formulae</i>
----	---

Description

Functions used for the definition of tensor product smooths and interactions within gam model formulae. `te` produces a full tensor product smooth, while `ti` produces a tensor product interaction, appropriate when the main effects (and any lower interactions) are also present.

The functions do not evaluate the smooth - they exist purely to help set up a model using tensor product based smooths. Designed to construct tensor products from any marginal smooths with a basis-penalty representation (with the restriction that each marginal smooth must have only one penalty).

Usage

```
te(..., k=NA, bs="cr", m=NA, d=NA, by=NA, fx=FALSE,
     mp=TRUE, np=TRUE, xt=NULL, id=NULL, sp=NULL, pc=NULL)
ti(..., k=NA, bs="cr", m=NA, d=NA, by=NA, fx=FALSE,
     np=TRUE, xt=NULL, id=NULL, sp=NULL, mc=NULL, pc=NULL)
```

Arguments

...	a list of variables that are the covariates that this smooth is a function of. Transformations whose form depends on the values of the data are best avoided here: e.g. <code>te(log(x), z)</code> is fine, but <code>te(I(x/sd(x)), z)</code> is not (see predict.gam).
k	the dimension(s) of the bases used to represent the smooth term. If not supplied then set to 5^d . If supplied as a single number then this basis dimension is used for each basis. If supplied as an array then the elements are the dimensions of the component (marginal) bases of the tensor product. See choose.k for further information.
bs	array (or single character string) specifying the type for each marginal basis. "cr" for cubic regression spline; "cs" for cubic regression spline with shrinkage; "cc" for periodic/cyclic cubic regression spline; "tp" for thin plate regression spline; "ts" for t.p.r.s. with extra shrinkage. See smooth.terms for details and full list. User defined bases can also be used here (see smooth.construct for an example). If only one basis code is given then this is used for all bases.
m	The order of the spline and its penalty (for smooth classes that use this) for each term. If a single number is given then it is used for all terms. A vector can be used to supply a different <code>m</code> for each margin. For marginals that take vector <code>m</code> (e.g. p.spline and Duchon.spline), then a list can be supplied, with a vector element for each margin. NA autoinitializes. <code>m</code> is ignored by some bases (e.g. "cr").

d	array of marginal basis dimensions. For example if you want a smooth for 3 covariates made up of a tensor product of a 2 dimensional t.p.r.s. basis and a 1-dimensional basis, then set $d=c(2,1)$. Incompatibilities between built in basis types and dimension will be resolved by resetting the basis type.
by	a numeric or factor variable of the same dimension as each covariate. In the numeric vector case the elements multiply the smooth evaluated at the corresponding covariate values (a ‘varying coefficient model’ results). In the factor case causes a replicate of the smooth to be produced for each factor level. See gam.models for further details. May also be a matrix if covariates are matrices: in this case implements linear functional of a smooth (see gam.models and linear.functional.terms for details).
fx	indicates whether the term is a fixed d.f. regression spline (TRUE) or a penalized regression spline (FALSE).
mp	TRUE to use multiple penalties for the smooth. FALSE to use only a single penalty: single penalties are not recommended and are deprecated - they tend to allow only rather wiggly models.
np	TRUE to use the ‘normal parameterization’ for a tensor product smooth. This represents any 1-d marginal smooths via parameters that are function values at ‘knots’, spread evenly through the data. The parameterization makes the penalties easily interpretable, however it can reduce numerical stability in some cases.
xt	Either a single object, providing any extra information to be passed to each marginal basis constructor, or a list of such objects, one for each marginal basis.
id	A label or integer identifying this term in order to link its smoothing parameters to others of the same type. If two or more smooth terms have the same id then they will have the same smoothing parameters, and, by default, the same bases (first occurrence defines basis type, but data from all terms used in basis construction).
sp	any supplied smoothing parameters for this term. Must be an array of the same length as the number of penalties for this smooth. Positive or zero elements are taken as fixed smoothing parameters. Negative elements signal auto-initialization. Over-rides values supplied in sp argument to gam . Ignored by gamm .
mc	For ti smooths you can specify which marginals should have centering constraints applied, by supplying 0/1 or FALSE/TRUE values for each marginal in this vector. By default all marginals are constrained, which is what is appropriate for, e.g., functional ANOVA models. Note that ‘ti’ only applies constraints to the marginals, so if you turn off all marginal constraints the term will have no identifiability constraints. Only use this if you really understand how marginal constraints work.
pc	If not NULL, signals a point constraint: the smooth should pass through zero at the point given here (as a vector or list with names corresponding to the smooth names). Never ignored if supplied. See identifiability .

Details

Smooths of several covariates can be constructed from tensor products of the bases used to represent smooths of one (or sometimes more) of the covariates. To do this ‘marginal’ bases are produced

with associated model matrices and penalty matrices, and these are then combined in the manner described in `tensor.prod.model.matrix` and `tensor.prod.penalties`, to produce a single model matrix for the smooth, but multiple penalties (one for each marginal basis). The basis dimension of the whole smooth is the product of the basis dimensions of the marginal smooths.

An option for operating with a single penalty (The Kronecker product of the marginal penalties) is provided, but it is rarely of practical use, and is deprecated: the penalty is typically so rank deficient that even the smoothest resulting model will have rather high estimated degrees of freedom.

Tensor product smooths are especially useful for representing functions of covariates measured in different units, although they are typically not quite as nicely behaved as t.p.r.s. smooths for well scaled covariates.

It is sometimes useful to investigate smooth models with a main-effects + interactions structure, for example

$$f_1(x) + f_2(z) + f_3(x, z)$$

This functional ANOVA decomposition is supported by `ti` terms, which produce tensor product interactions from which the main effects have been excluded, under the assumption that they will be included separately. For example the `~ ti(x) + ti(z) + ti(x,z)` would produce the above main effects + interaction structure. This is much better than attempting the same thing with `so` `te` terms representing the interactions (although `mgcv` does not forbid it). Technically `ti` terms are very simple: they simply construct tensor product bases from marginal smooths to which identifiability constraints (usually sum-to-zero) have already been applied: correct nesting is then automatic (as with all interactions in a GLM framework).

The ‘normal parameterization’ (`np=TRUE`) re-parameterizes the marginal smooths of a tensor product smooth so that the parameters are function values at a set of points spread evenly through the range of values of the covariate of the smooth. This means that the penalty of the tensor product associated with any particular covariate direction can be interpreted as the penalty of the appropriate marginal smooth applied in that direction and averaged over the smooth. Currently this is only done for marginals of a single variable. This parameterization can reduce numerical stability when used with marginal smooths other than `"cc"`, `"cr"` and `"cs"`: if this causes problems, set `np=FALSE`.

Note that tensor product smooths should not be centred (have identifiability constraints imposed) if any marginals would not need centering. The constructor for tensor product smooths ensures that this happens.

The function does not evaluate the variable arguments.

Value

A class `tensor.smooth.spec` object defining a tensor product smooth to be turned into a basis and penalties by the `smooth.construct.tensor.smooth.spec` function.

The returned object contains the following items:

<code>margin</code>	A list of <code>smooth.spec</code> objects of the type returned by <code>s</code> , defining the basis from which the tensor product smooth is constructed.
<code>term</code>	An array of text strings giving the names of the covariates that the term is a function of.
<code>by</code>	is the name of any by variable as text (<code>"NA"</code> for none).
<code>fx</code>	logical array with element for each penalty of the term (tensor product smooths have multiple penalties). <code>TRUE</code> if the penalty is to be ignored, <code>FALSE</code> , otherwise.

label	A suitable text label for this smooth term.
dim	The dimension of the smoother - i.e. the number of covariates that it is a function of.
mp	TRUE is multiple penalties are to be used (default).
np	TRUE to re-parameterize 1-D marginal smooths in terms of function values (default).
id	the id argument supplied to te.
sp	the sp argument supplied to te.
inter	TRUE if the term was generated by ti, FALSE otherwise.
mc	the argument mc supplied to ti.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006a) Low rank scale invariant tensor product smooths for generalized additive mixed models. *Biometrics* 62(4):1025-1036

<http://www.maths.bris.ac.uk/~sw15190/>

See Also

[s,gam,gamm](#), [smooth.construct.tensor.smooth.spec](#)

Examples

```
# following shows how tensor product deals nicely with
# badly scaled covariates (range of x 5% of range of z )
require(mgcv)
test1 <- function(x,z,sx=0.3,sz=0.4) {
  x <- x*20
  (pi**x**sz)*(1.2*exp(-(x-0.2)^2/sx^2-(z-0.3)^2/sz^2)+
  0.8*exp(-(x-0.7)^2/sx^2-(z-0.8)^2/sz^2))
}
n <- 500
old.par <- par(mfrow=c(2,2))
x <- runif(n)/20;z <- runif(n);
xs <- seq(0,1,length=30)/20;zs <- seq(0,1,length=30)
pr <- data.frame(x=rep(xs,30),z=rep(zs,rep(30,30)))
truth <- matrix(test1(pr$x,pr$z),30,30)
f <- test1(x,z)
y <- f + rnorm(n)*0.2
b1 <- gam(y~s(x,z))
persp(xs,zs,truth);title("truth")
vis.gam(b1);title("t.p.r.s")
b2 <- gam(y~te(x,z))
vis.gam(b2);title("tensor product")
```

```

b3 <- gam(y~ ti(x) + ti(z) + ti(x,z))
vis.gam(b3);title("tensor anova")

## now illustrate partial ANOVA decomp...
vis.gam(b3);title("full anova")
b4 <- gam(y~ ti(x) + ti(x,z,mc=c(0,1))) ## note z constrained!
vis.gam(b4);title("partial anova")
plot(b4)

par(old.par)

## now with a multivariate marginal....

test2<-function(u,v,w,sv=0.3,sw=0.4)
{ ((pi**sv**sw)*(1.2*exp(-(v-0.2)^2/sv^2-(w-0.3)^2/sw^2)+
  0.8*exp(-(v-0.7)^2/sv^2-(w-0.8)^2/sw^2)))*(u-0.5)^2*20
}
n <- 500
v <- runif(n);w<-runif(n);u<-runif(n)
f <- test2(u,v,w)
y <- f + rnorm(n)*0.2
# tensor product of 2D Duchon spline and 1D cr spline
m <- list(c(1,.5),rep(0,0)) ## example of list form of m
b <- gam(y~te(v,w,u,k=c(30,5),d=c(2,1),bs=c("ds","cr"),m=m))
op <- par(mfrow=c(2,2))
vis.gam(b,cond=list(u=0),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=.33),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=.67),color="heat",zlim=c(-0.2,3.5))
vis.gam(b,cond=list(u=1),color="heat",zlim=c(-0.2,3.5))
par(op)

```

tensor.prod.model.matrix

Utility functions for constructing tensor product smooths

Description

Produce model matrices or penalty matrices for a tensor product smooth from the model matrices or penalty matrices for the marginal bases of the smooth.

Usage

```

tensor.prod.model.matrix(X)
tensor.prod.penalties(S)

```

Arguments

X	a list of model matrices for the marginal bases of a smooth
S	a list of penalties for the marginal bases of a smooth.

Details

If $X[[1]]$, $X[[2]]$... $X[[m]]$ are the model matrices of the marginal bases of a tensor product smooth then the i th row of the model matrix for the whole tensor product smooth is given by $X[[1]][i,] \% \% X[[2]][i,] \% \% \dots X[[m]][i,]$, where $\% \%$ is the Kronecker product. Of course the routine operates column-wise, not row-wise!

If $S[[1]]$, $S[[2]]$... $S[[m]]$ are the penalty matrices for the marginal bases, and $I[[1]]$, $I[[2]]$... $I[[m]]$ are corresponding identity matrices, each of the same dimension as its corresponding penalty, then the tensor product smooth has m associate penalties of the form:

$$S[[1]] \% \% I[[2]] \% \% \dots I[[m]],$$

$$I[[1]] \% \% S[[2]] \% \% \dots I[[m]]$$

...

$$I[[1]] \% \% I[[2]] \% \% \dots S[[m]].$$

Of course it's important that the model matrices and penalty matrices are presented in the same order when constructing tensor product smooths.

Value

Either a single model matrix for a tensor product smooth, or a list of penalty terms for a tensor product smooth.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) Low rank scale invariant tensor product smooths for Generalized Additive Mixed Models. *Biometrics* 62(4):1025-1036

See Also

[te](#), [smooth.construct.tensor.smooth.spec](#)

Examples

```
require(mgcv)
X <- list(matrix(1:4,2,2),matrix(5:10,2,3))
tensor.prod.model.matrix(X)

S<-list(matrix(c(2,1,1,2),2,2),matrix(c(2,1,0,1,2,1,0,1,2),3,3))
tensor.prod.penalties(S)
```

`trichol`*Choleski decomposition of a tri-diagonal matrix*

Description

Computes Choleski decomposition of a (symmetric positive definite) tri-diagonal matrix stored as a leading diagonal and sub/super diagonal.

Usage

```
trichol(ld, sd)
```

Arguments

<code>ld</code>	leading diagonal of matrix
<code>sd</code>	sub-super diagonal of matrix

Details

Calls `dpttrf` from LAPACK. The point of this is that it has $O(n)$ computational cost, rather than the $O(n^3)$ required by dense matrix methods.

Value

A list with elements `ld` and `sd`. `ld` is the leading diagonal and `sd` is the super diagonal of bidiagonal matrix \mathbf{B} where $\mathbf{B}^T \mathbf{B} = \mathbf{T}$ and \mathbf{T} is the original tridiagonal matrix.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Anderson, E., Bai, Z., Bischof, C., Blackford, S., Dongarra, J., Du Croz, J., Greenbaum, A., Hammarling, S., McKenney, A. and Sorensen, D., 1999. LAPACK Users' guide (Vol. 9). Siam.

See Also

[bandchol](#)

Examples

```
require(mgcv)
## simulate some diagonals...
set.seed(19); k <- 7
ld <- runif(k)+1
sd <- runif(k-1) -.5
```



```
## get diagonals of chol factor...
trichol(ld,sd)

## compare to dense matrix result...
A <- diag(ld);for (i in 1:(k-1)) A[i,i+1] <- A[i+1,i] <- sd[i]
R <- chol(A)
diag(R);diag(R[,-1])
```

trind.generator	<i>Generates index arrays for upper triangular storage</i>
-----------------	--

Description

Generates index arrays for upper triangular storage up to order four. Useful when working with higher order derivatives, which generate symmetric arrays. Mainly intended for internal use.

Usage

```
trind.generator(K = 2)
```

Arguments

K positive integer determining the size of the array.

Details

Suppose that $m=1$ and you fill an array using code like `for(i in 1:K) for(j in i:K) for(k in j:K) for(l in k:K) {a[,m] <- something; m <- m+1 }` and do this because actually the same "something" would be stored for any permutation of the indices i,j,k,l . Clearly in storage we have the restriction $l \geq k \geq j \geq i$, but for access we want no restriction on the indices. `i4[i,j,k,l]` produces the appropriate m for unrestricted indices. `i3` and `i2` do the same for 3d and 2d arrays.

Value

A list where the entries `i1` to `i4` are arrays in up to four dimensions, containing K indexes along each dimension.

Author(s)

Simon N. Wood <simon.wood@r-project.org>.

Examples

```

library(mgcv)
A <- trind.generator(3)

# All permutations of c(1, 2, 3) point to the same index (5)
A$1[1, 2, 3]
A$1[2, 1, 3]
A$1[2, 3, 1]
A$1[3, 1, 2]
A$1[1, 3, 2]

```

Tweedie

*GAM Tweedie families***Description**

Tweedie families, designed for use with [gam](#) from the [mgcv](#) library. Restricted to variance function powers between 1 and 2. A useful alternative to [quasi](#) when a full likelihood is desirable. Tweedie is for use with fixed p . `tw` is for use when p is to be estimated during fitting. For fixed p between 1 and 2 the Tweedie is an exponential family distribution with variance given by the mean to the power p .

`tw` is only useable with [gam](#), not `bam` or `gamm`. Tweedie works with all three.

Usage

```

Tweedie(p=1, link = power(0))
tw(theta = NULL, link = "log", a=1.01, b=1.99)

```

Arguments

<code>p</code>	the variance of an observation is proportional to its mean to the power p . p must be greater than 1 and less than or equal to 2. 1 would be Poisson, 2 is gamma.
<code>link</code>	The link function: one of "log", "identity", "inverse", "sqrt", or a power link (Tweedie only).
<code>theta</code>	Related to the Tweedie power parameter by $p = \exp(a + b \exp(\theta)) / (1 + \exp(\theta))$. If this is supplied as a positive value then it is taken as the fixed value for p . If it is a negative values then its absolute value is taken as the initial value for p .
<code>a</code>	lower limit on p for optimization.
<code>b</code>	upper limit on p for optimization.

Details

A Tweedie random variable with $1 < p < 2$ is a sum of N gamma random variables where N has a Poisson distribution. The $p=1$ case is a generalization of a Poisson distribution and is a discrete distribution supported on integer multiples of the scale parameter. For $1 < p < 2$ the distribution is supported on the positive reals with a point mass at zero. $p=2$ is a gamma distribution. As p gets

very close to 1 the continuous distribution begins to converge on the discretely supported limit at $p=1$, and is therefore highly multimodal. See `ldTweedie` for more on this behaviour.

Tweedie is based partly on the `poisson` family, and partly on `tweedie` from the `statmod` package. It includes extra components to work with all `mgcv` GAM fitting methods as well as an `aic` function.

The Tweedie density involves a normalizing constant with no closed form, so this is evaluated using the series evaluation method of Dunn and Smyth (2005), with extensions to also compute the derivatives w.r.t. p and the scale parameter. Without restricting p to $(1,2)$ the calculation of Tweedie densities is more difficult, and there does not currently seem to be an implementation which offers any benefit over `quasi`. If you need this case then the `tweedie` package is the place to start.

Value

For `Tweedie`, an object inheriting from class `family`, with additional elements

<code>dvar</code>	the function giving the first derivative of the variance function w.r.t. μ .
<code>d2var</code>	the function giving the second derivative of the variance function w.r.t. μ .
<code>ls</code>	A function returning a 3 element array: the saturated log likelihood followed by its first 2 derivatives w.r.t. the scale parameter.

For `tw`, an object of class `extended.family`.

Author(s)

Simon N. Wood <simon.wood@r-project.org>.

References

Dunn, P.K. and G.K. Smyth (2005) Series evaluation of Tweedie exponential dispersion model densities. *Statistics and Computing* 15:267-280

Tweedie, M. C. K. (1984). An index which distinguishes between some important exponential families. *Statistics: Applications and New Directions. Proceedings of the Indian Statistical Institute Golden Jubilee International Conference* (Eds. J. K. Ghosh and J. Roy), pp. 579-604. Calcutta: Indian Statistical Institute.

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

See Also

[ldTweedie](#), [rTweedie](#)

Examples

```
library(mgcv)
set.seed(3)
n<-400
## Simulate data...
dat <- gamSim(1,n=n,dist="poisson",scale=.2)
dat$y <- rTweedie(exp(dat$f),p=1.3,phi=.5) ## Tweedie response
```

```

## Fit a fixed p Tweedie, with wrong link ...
b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3), family=Tweedie(1.25,power(.1)),
        data=dat)
plot(b,pages=1)
print(b)

## Same by approximate REML...
b1 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3), family=Tweedie(1.25,power(.1)),
        data=dat,method="REML")
plot(b1,pages=1)
print(b1)

## estimate p as part of fitting

b2 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3), family=tw(),
        data=dat,method="REML")
plot(b2,pages=1)
print(b2)

rm(dat)

```

uniquecombs

find the unique rows in a matrix

Description

This routine returns a matrix or data frame containing all the unique rows of the matrix or data frame supplied as its argument. That is, all the duplicate rows are stripped out. Note that the ordering of the rows on exit need not be the same as on entry. It also returns an index attribute for relating the result back to the original matrix.

Usage

```
uniquecombs(x,ordered=FALSE)
```

Arguments

x	is an R matrix (numeric), or data frame.
ordered	set to TRUE to have the rows of the returned object in the same order regardless of input ordering.

Details

Models with more parameters than unique combinations of covariates are not identifiable. This routine provides a means of evaluating the number of unique combinations of covariates in a model.

When x has only one column then the routine uses `unique` and `match` to get the index. When there are multiple columns then it uses `paste0` to produce labels for each row, which should be unique

if the row is unique. Then `unique` and `match` can be used as in the single column case. Obviously the pasting is inefficient, but still quicker for large n than the C based code that used to be called by this routine, which had $O(n \log(n))$ cost. In principle a hash table based solution in C would be only $O(n)$ and much quicker in the multicolumn case.

`unique` and `duplicated`, can be used in place of this, if the full index is not needed. Relative performance is variable.

If x is not a matrix or data frame on entry then an attempt is made to coerce it to a data frame.

Value

A matrix or data frame consisting of the unique rows of x (in arbitrary order).

The matrix or data frame has an "index" attribute. `index[i]` gives the row of the returned matrix that contains row i of the original matrix.

WARNINGS

If a dataframe contains variables of a type other than numeric, logical, factor or character, which either have no `as.character` method, or whose `as.character` method is a many to one mapping, then the routine is likely to fail.

If the character representation of a dataframe variable (other than of class factor or character) contains `*` then in principle the method could fail (but with a warning).

Author(s)

Simon N. Wood <simon.wood@r-project.org> with thanks to Jonathan Rougier

See Also

`unique`, `duplicated`, `match`.

Examples

```
require(mgcv)

## matrix example...
X <- matrix(c(1,2,3,1,2,3,4,5,6,1,3,2,4,5,6,1,1,1),6,3,byrow=TRUE)
print(X)
Xu <- uniquecombs(X);Xu
ind <- attr(Xu,"index")
## find the value for row 3 of the original from Xu
Xu[ind[3],];X[3,]

## same with fixed output ordering
Xu <- uniquecombs(X,TRUE);Xu
ind <- attr(Xu,"index")
## find the value for row 3 of the original from Xu
Xu[ind[3],];X[3,]

## data frame example...
```

```
df <- data.frame(f=factor(c("er",3,"b","er",3,3,1,2,"b")),
  x=c(.5,1,1.4,.5,1,.6,4,3,1.7),
  bb = c(rep(TRUE,5),rep(FALSE,4)),
  fred = c("foo","a","b","foo","a","vf","er","r","g"),
  stringsAsFactors=FALSE)
uniquecombs(df)
```

vcov.gam

*Extract parameter (estimator) covariance matrix from GAM fit***Description**

Extracts the Bayesian posterior covariance matrix of the parameters or frequentist covariance matrix of the parameter estimators from a fitted gam object.

Usage

```
## S3 method for class 'gam'
vcov(object, freq = FALSE, dispersion = NULL, unconditional=FALSE, ...)
```

Arguments

object	fitted model object of class gam as produced by gam().
freq	TRUE to return the frequentist covariance matrix of the parameter estimators, FALSE to return the Bayesian posterior covariance matrix of the parameters.
dispersion	a value for the dispersion parameter: not normally used.
unconditional	if TRUE (and freq==FALSE) then the Bayesian smoothing parameter uncertainty corrected covariance matrix is returned, if available.
...	other arguments, currently ignored.

Details

Basically, just extracts object\$Ve or object\$Vp from a [gamObject](#).

Value

A matrix corresponding to the estimated frequentist covariance matrix of the model parameter estimators/coefficients, or the estimated posterior covariance matrix of the parameters, depending on the argument freq.

Author(s)

Henric Nilsson. Maintained by Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N. (2006) On confidence intervals for generalized additive models based on penalized regression splines. Australian and New Zealand Journal of Statistics. 48(4): 445-464.

See Also[gam](#)**Examples**

```
require(mgcv)
n <- 100
x <- runif(n)
y <- sin(x*2*pi) + rnorm(n)*.2
mod <- gam(y~s(x,bs="cc",k=10),knots=list(x=seq(0,1,length=10)))
diag(vcov(mod))
```

vis.gam

*Visualization of GAM objects***Description**

Produces perspective or contour plot views of gam model predictions, fixing all but the values in view to the values supplied in cond.

Usage

```
vis.gam(x,view=NULL,cond=list(),n.grid=30,too.far=0,col=NA,
        color="heat",contour.col=NULL,se=-1,type="link",
        plot.type="persp",zlim=NULL,nCol=50,...)
```

Arguments

x	a gam object, produced by gam()
view	an array containing the names of the two main effect terms to be displayed on the x and y dimensions of the plot. If omitted the first two suitable terms will be used. Note that variables coerced to factors in the model formula won't work as view variables, and vis.gam can not detect that this has happened when setting defaults.
cond	a named list of the values to use for the other predictor terms (not in view). Variables omitted from this list will have the closest observed value to the median for continuous variables, or the most commonly occurring level for factors. Parametric matrix variables have all the entries in each column set to the observed column entry closest to the column median.
n.grid	The number of grid nodes in each direction used for calculating the plotted surface.
too.far	plot grid nodes that are too far from the points defined by the variables given in view can be excluded from the plot. too.far determines what is too far. The grid is scaled into the unit square along with the view variables and then grid nodes more than too.far from the predictor variables are excluded.

<code>col</code>	The colours for the facets of the plot. If this is NA then if <code>se>0</code> the facets are transparent, otherwise the colour scheme specified in <code>color</code> is used. If <code>col</code> is not NA then it is used as the facet colour.
<code>color</code>	the colour scheme to use for plots when <code>se<=0</code> . One of "topo", "heat", "cm", "terrain", "gray" or "bw". Schemes "gray" and "bw" also modify the colors used when <code>se>0</code> .
<code>contour.col</code>	sets the colour of contours when using <code>plot.type="contour"</code> . Default scheme used if NULL.
<code>se</code>	if less than or equal to zero then only the predicted surface is plotted, but if greater than zero, then 3 surfaces are plotted, one at the predicted values minus <code>se</code> standard errors, one at the predicted values and one at the predicted values plus <code>se</code> standard errors.
<code>type</code>	"link" to plot on linear predictor scale and "response" to plot on the response scale.
<code>plot.type</code>	one of "contour" or "persp".
<code>zlim</code>	a two item array giving the lower and upper limits for the z-axis scale. NULL to choose automatically.
<code>nCol</code>	The number of colors to use in color schemes.
<code>...</code>	other options to pass on to <code>persp</code> , <code>image</code> or <code>contour</code> . In particular <code>ticktype="detailed"</code> will add proper axes labelling to the plots.

Details

The x and y limits are determined by the ranges of the terms named in `view`. If `se<=0` then a single (height colour coded, by default) surface is produced, otherwise three (by default see-through) meshes are produced at mean and +/- `se` standard errors. Parts of the x-y plane too far from data can be excluded by setting `too.far`

All options to the underlying graphics functions can be reset by passing them as extra arguments `...`: such supplied values will always over-ride the default values used by `vis.gam`.

Value

Simply produces a plot.

WARNINGS

The routine can not detect that a variable has been coerced to factor within a model formula, and will therefore fail if such a variable is used as a `view` variable. When setting default `view` variables it can not detect this situation either, which can cause failures if the coerced variables are the first, otherwise suitable, variables encountered.

Author(s)

Simon Wood <simon.wood@r-project.org>

Based on an original idea and design by Mike Lonergan.

See Also

[persp](#) and [gam](#).

Examples

```

library(mgcv)
set.seed(0)
n<-200;sig2<-4
x0 <- runif(n, 0, 1);x1 <- runif(n, 0, 1)
x2 <- runif(n, 0, 1)
y<-x0^2+x1*x2 +runif(n,-0.3,0.3)
g<-gam(y~s(x0,x1,x2))
old.par<-par(mfrow=c(2,2))
# display the prediction surface in x0, x1 ....
vis.gam(g,ticktype="detailed",color="heat",theta=-35)
vis.gam(g,se=2,theta=-35) # with twice standard error surfaces
vis.gam(g, view=c("x1","x2"),cond=list(x0=0.75)) # different view
vis.gam(g, view=c("x1","x2"),cond=list(x0=0.75),theta=210,phi=40,
        too.far=.07)
# ..... areas where there is no data are not plotted

# contour examples...
vis.gam(g, view=c("x1","x2"),plot.type="contour",color="heat")
vis.gam(g, view=c("x1","x2"),plot.type="contour",color="terrain")
vis.gam(g, view=c("x1","x2"),plot.type="contour",color="topo")
vis.gam(g, view=c("x1","x2"),plot.type="contour",color="cm")

par(old.par)

# Examples with factor and "by" variables

fac<-rep(1:4,20)
x<-runif(80)
y<-fac+2*x^2+rnorm(80)*0.1
fac<-factor(fac)
b<-gam(y~fac+s(x))

vis.gam(b,theta=-35,color="heat") # factor example

z<-rnorm(80)*0.4
y<-as.numeric(fac)+3*x^2*z+rnorm(80)*0.1
b<-gam(y~fac+s(x,by=z))

vis.gam(b,theta=-35,color="heat",cond=list(z=1)) # by variable example

vis.gam(b,view=c("z","x"),theta=-135) # plot against by variable

```

ziP

*GAM zero-inflated Poisson regression family***Description**

Family for use with `gam`, implementing regression for zero inflated Poisson data when the complementary log log of the zero probability is linearly dependent on the log of the Poisson parameter. Use with great care, noting that simply having many zero response observations is not an indication of zero inflation: the question is whether you have too many zeroes given the specified model.

This sort of model is really only appropriate when none of your covariates help to explain the zeroes in your data. If your covariates predict which observations are likely to have zero mean then adding a zero inflated model on top of this is likely to lead to identifiability problems. Identifiability problems may lead to fit failures, or absurd values for the linear predictor or predicted values.

Usage

```
ziP(theta = NULL, link = "identity", b=0)
```

Arguments

theta	the 2 parameters controlling the slope and intercept of the linear transform of the mean controlling the zero inflation rate. If supplied then treated as fixed parameters (θ_1 and θ_2), otherwise estimated.
link	The link function: only the "identity" is currently supported.
b	a non-negative constant, specifying the minimum dependence of the zero inflation rate on the linear predictor.

Details

The probability of a zero count is given by $1 - p$, whereas the probability of count $y > 0$ is given by the truncated Poisson probability function $p\mu^y / ((\exp(\mu) - 1)y!)$. The linear predictor gives $\log \mu$, while $\eta = \log(-\log(1 - p))$ and $\eta = \theta_1 + \{b + \exp(\theta_2)\} \log \mu$. The theta parameters are estimated alongside the smoothing parameters. Increasing the b parameter from zero can greatly reduce identifiability problems, particularly when there are very few non-zero data.

The fitted values for this model are the log of the Poisson parameter. Use the `predict` function with `type="response"` to get the predicted expected response. Note that the theta parameters reported in model summaries are θ_1 and $b + \exp(\theta_2)$.

These models should be subject to very careful checking, especially if fitting has not converged. It is quite easy to set up models with identifiability problems, particularly if the data are not really zero inflated, but simply have many zeroes because the mean is very low in some parts of the covariate space. See example for some obvious checks. Take convergence warnings seriously.

Value

An object of class `extended.family`.

WARNINGS

Zero inflated models are often over-used. Having lots of zeroes in the data does not in itself imply zero inflation. Having too many zeroes *given the model mean* may imply zero inflation.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. Journal of the American Statistical Association. <http://arxiv.org/abs/1511.03864>

See Also

[ziplss](#)

Examples

```
rzip <- function(gamma,theta= c(-2,.3)) {
  ## generate zero inflated Poisson random variables, where
  ## lambda = exp(gamma), eta = theta[1] + exp(theta[2])*gamma
  ## and 1-p = exp(-exp(eta)).
  y <- gamma; n <- length(y)
  lambda <- exp(gamma)
  eta <- theta[1] + exp(theta[2])*gamma
  p <- 1- exp(-exp(eta))
  ind <- p > runif(n)
  y[!ind] <- 0
  np <- sum(ind)
  ## generate from zero truncated Poisson, given presence...
  y[ind] <- qpois(runif(np,dpois(0,lambda[ind]),1),lambda[ind])
  y
}

library(mgcv)
## Simulate some ziP data...
set.seed(1);n<-400
dat <- gamSim(1,n=n)
dat$y <- rzip(dat$f/4-1)

b <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=ziP(),data=dat)

b$outer.info ## check convergence!!
b
plot(b,pages=1)
plot(b,pages=1,unconditional=TRUE) ## add s.p. uncertainty
gam.check(b)
## more checking...
```

```

## 1. If the zero inflation rate becomes decoupled from the linear predictor,
## it is possible for the linear predictor to be almost unbounded in regions
## containing many zeroes. So examine if the range of predicted values
## is sane for the zero cases?
range(predict(b,type="response")[b$y==0])

## 2. Further plots...
par(mfrow=c(2,2))
plot(predict(b,type="response"),residuals(b))
plot(predict(b,type="response"),b$y);abline(0,1,col=2)
plot(b$linear.predictors,b$y)
qq.gam(b,rep=20,level=1)

## 3. Refit fixing the theta parameters at their estimated values, to check we
## get essentially the same fit...
thb <- b$family$getTheta()
b0 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=ziP(theta=thb),data=dat)
b;b0

## Example fit forcing minimum linkage of prob present and
## linear predictor. Can fix some identifiability problems.
b2 <- gam(y~s(x0)+s(x1)+s(x2)+s(x3),family=ziP(b=.3),data=dat)

```

ziplss

Zero inflated Poisson location-scale model family

Description

The `ziplss` family implements a zero inflated Poisson model in which one linear predictor controls the probability of presence and the other controls the mean given presence. Useable only with `gam`, the linear predictors are specified via a list of formulae. Should be used with care: simply having a large number of zeroes is not an indication of zero inflation.

Requires integer count data.

Usage

```
ziplss(link=list("identity","identity"))
```

Arguments

`link` two item list specifying the link - currently only identity links are possible, as parameterization is directly in terms of log of Poisson response and logit of probability of presence.

Details

Used with `gam` to fit 2 stage zero inflated Poisson models. `gam` is called with a list containing 2 formulae, the first specifies the response on the left hand side and the structure of the linear predictor for the Poisson parameter on the right hand side. The second is one sided, specifying the linear predictor for the probability of presence on the right hand side.

The fitted values for this family will be a two column matrix. The first column is the log of the Poisson parameter, and the second column is the complimentary log log of probability of presence.. Predictions using `predict.gam` will also produce 2 column matrices for type "link" and "response".

The null deviance computed for this model assumes that a single probability of presence and a single Poisson parameter are estimated.

For data with large areas of covariate space over which the response is zero it may be advisable to use low order penalties to avoid problems. For 1D smooths uses e.g. `s(x,m=1)` and for isotropic smooths use `Duchon.splines` in place of thin plate terms with order 1 penalties, e.g `s(x,z,m=c(1,.5))` — such smooths penalize towards constants, thereby avoiding extreme estimates when the data are uninformative.

Value

An object inheriting from class `general.family`.

WARNINGS

Zero inflated models are often over-used. Having lots of zeroes in the data does not in itself imply zero inflation. Having too many zeroes *given the model mean* may imply zero inflation.

Author(s)

Simon N. Wood <simon.wood@r-project.org>

References

Wood, S.N., N. Pya and B. Saefken (2016), Smoothing parameter and model selection for general smooth models. *Journal of the American Statistical Association*. <http://arxiv.org/abs/1511.03864>

Examples

```
library(mgcv)
## simulate some data...
f0 <- function(x) 2 * sin(pi * x); f1 <- function(x) exp(2 * x)
f2 <- function(x) 0.2 * x^11 * (10 * (1 - x))^6 + 10 *
      (10 * x)^3 * (1 - x)^10
n <- 500;set.seed(5)
x0 <- runif(n); x1 <- runif(n)
x2 <- runif(n); x3 <- runif(n)

## Simulate probability of potential presence...
eta1 <- f0(x0) + f1(x1) - 3
```

```
p <- binomial()$linkinv(eta1)
y <- as.numeric(runif(n)<p) ## 1 for presence, 0 for absence

## Simulate y given potentially present (not exactly model fitted!)...
ind <- y>0
eta2 <- f2(x2[ind])/3
y[ind] <- rpois(exp(eta2),exp(eta2))

## Fit ZIP model...
b <- gam(list(y~s(x2)+s(x3),~s(x0)+s(x1)),family=ziplss())
b$outer.info ## check convergence

summary(b)
plot(b,pages=1)
```

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