Package ‘BiDAG’

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Title Bayesian Inference for Directed Acyclic Graphs
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Description Implementation of a collection of MCMC methods for Bayesian structure learning of directed acyclic graphs (DAGs), both from continuous and discrete data. For efficient inference on larger DAGs, the space of DAGs is pruned according to the data. To filter the search space, the algorithm employs a hybrid approach, combining constraint-based learning with search and score. A reduced search space is initially defined on the basis of a skeleton obtained by means of the PC-algorithm, and then iteratively improved with search and score. Search and score is then performed following two approaches: Order MCMC, or Partition MCMC. The BGe score is implemented for continuous data and the BDe score is implemented for binary data or categorical data. The algorithms may provide the maximum a posteriori (MAP) graph or a sample (a collection of DAGs) from the posterior distribution given the data. All algorithms are also applicable to structure learning of dynamic Bayesian networks.

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Encoding UTF-8
adjacency2dag

Description
This function derives a graph object corresponding to an adjacency matrix.

Usage
adjacency2dag(adj, nodes = NULL)

Arguments
adj	square adjacency matrix with elements in \{0, 1\}, representing a graph
nodes  (optional) labels of the nodes, c(1:n) are used by default

Value
object of class graphNEL (package ‘graph’); if element \text{adj}[i,j] equals 1, then there is a directed edge from node i to node j in the graph, and no edge otherwise
Examples

```r
adj<-matrix(rep(0,16),nrow=4)
adj[2,1]<-1
adj[1,4]<-1
adjacency2dag(adj)
```

Description

A synthetic dataset from Lauritzen and Spiegelhalter (1988) about lung diseases (tuberculosis, lung cancer or bronchitis) and visits to Asia.

Usage

Asia

Format

A data frame with 5000 rows and 8 binary variables:

- D (dyspnoea), binary 1/0 corresponding to "yes" and "no"
- T (tuberculosis), binary 1/0 corresponding to "yes" and "no"
- L (lung cancer), binary 1/0 corresponding to "yes" and "no"
- B (bronchitis), binary 1/0 corresponding to "yes" and "no"
- A (visit to Asia), binary 1/0 corresponding to "yes" and "no"
- S (smoking), binary 1/0 corresponding to "yes" and "no"
- X (chest X-ray), binary 1/0 corresponding to "yes" and "no"
- E (tuberculosis versus lung cancer/bronchitis), binary 1/0 corresponding to "yes" and "no"

Source

http://www.bnlearn.com/bnrepository/

References

Boston housing data

Description

A dataset containing information collected by the U.S Census Service concerning housing in the area of Boston, originally published by Harrison and Rubinfeld (1978).

Usage

Boston

Format

A data frame with 506 rows and 14 variables:

- CRIM - per capita crime rate by town
- ZN - proportion of residential land zoned for lots over 25,000 sq.ft.
- INDUS - proportion of non-retail business acres per town.
- CHAS - Charles River dummy variable (1 if tract bounds river; 0 otherwise)
- NOX - nitric oxides concentration (parts per 10 million)
- RM - average number of rooms per dwelling
- AGE - proportion of owner-occupied units built prior to 1940
- DIS - weighted distances to five Boston employment centres
- TAX - full-value property-tax rate per $10,000
- RAD - index of accessibility to radial highways
- PTRATIO - pupil-teacher ratio by town
- B - 1000(Bk - 0.63)^2 where Bk is the proportion of blacks by town
- LSTAT - percentage lower status of the population
- MEDV - Median value of owner-occupied homes in $1000's

Source

http://lib.stat.cmu.edu/datasets/boston

References

compareDAGs

Comparing two DAGs

Description
This function compares one (estimated) DAG to another DAG (true DAG), returning a vector of 3 values: structural Hamming distance, number of true positive edges and number of false positive edges.

Usage
compareDAGs(eDAG, trueDAG)

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>eDAG</td>
<td>an object of class <code>graphNEL</code> (package ‘graph’), representing the DAG which should be compared to a ground truth DAG</td>
</tr>
<tr>
<td>trueDAG</td>
<td>an object of class <code>graphNEL</code> (package ‘graph’), representing the ground truth DAG</td>
</tr>
</tbody>
</table>

Value
a vector of 3: SHD, number of true positive edges and number of false positive edges

Examples
```r
myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
myScore<-scoreparameters(20,"bge",myData)
## Not run:
eDAG<-orderMCMC(20,myScore)
compareDAGs(adjacency2dag(eDAG$max$DAG),myDAG)
## End(Not run)
```

dag.threshold

Estimating a graph corresponding to a posterior probability threshold

Description
This function constructs a directed graph (not necessarily acyclic) including all edges with a posterior probability above a certain threshold. The posterior probability is evaluated as the Monte Carlo estimate from a sample of DAGs obtained via an MCMC scheme.

Usage
dag.threshold(n, MCMCchain, pbarrier, pdag = FALSE, burnin = 0.2)
Arguments

- **n**: number of nodes in the Bayesian network
- **MCMCchain**: list of adjacency matrices with dimensions equal to n and elements in \{0, 1\}, representing a sample of DAGs from an MCMC scheme
- **pbarrier**: threshold such that only edges with a higher posterior probability will be retained in the directed graph summarising the sample of DAGs
- **pdag**: logical, if TRUE (FALSE by default) all DAGs in the MCMCchain are first converted to equivalence class (CPDAG) before the averaging
- **burnin**: (optional) number between 0 and 1, indicates the percentage of the samples which will be the discarded as ‘burn-in’ of the MCMC chain; the rest of the samples will be used to calculate the posterior probabilities; 0.2 by default

Value

A square matrix with dimensions equal to the number of variables representing the adjacency matrix of the directed graph summarising the sample of DAGs

Examples

```r
Bostonscore <- scoreparameters(14, "bge", Boston)
orderfit <- orderMCMC(14, Bostonscore, MAP=FALSE, iterations=25000, chainout=TRUE)
MCMCchain <- orderfit$chain$incidence
hdag <- dag.threshold(MCMCchain, pbarrier=0.9)
```

---

**dag2adjacencymatrix**

*Deriving an adjacency matrix of a graph*

Description

This function derives the adjacency matrix corresponding to a graph object

Usage

```r
dag2adjacencymatrix(g)
```

Arguments

- **g**: graph, object of class `graphNEL` (package ‘graph’)

Value

A square matrix whose dimensions are the number of nodes in the graph g, where element \([i, j]\) equals 1 if there is a directed edge from node i to node j in the graph g, and 0 otherwise
dag2skeletonadjacency  Deriving an adjacency matrix of the skeleton of a graph

Description

This function derives the skeleton matrix corresponding to a graph object.

Usage

dag2skeletonadjacency(g)

Arguments

g              graph, object of class graphNEL (package ‘graph’)

Value

a symmetric square matrix whose dimensions are the number of nodes in the graph g, where element 
[i, j] equals 1 if there is a directed edge from node i to node j, or from node j to node i, in the 
graph g, and 0 otherwise

Examples

myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
dag2skeletonadjacency(myDAG)

DAGscore  Calculating the BGe/BDe score of a single DAG

Description

This function calculates the score of a DAG defined by its adjacency matrix. Acceptable data 
matrices are homogeneous with all variables of the same type: continuous, binary or categorical. 
The BGe score is evaluated in the case of continuous data and the BDe score is evaluated for binary 
and categorical variables.

Usage

DAGscore(n, scoreparam, incidence)
edges.posterior

**Arguments**

- **n**: number of nodes in the Bayesian network
- **scoreparam**: an object of class `scoreparameters`, containing the data and scoring parameters; see constructor function `scoreparameters`
- **incidence**: a square matrix of dimensions equal to the number of nodes, representing the adjacency matrix of a DAG; the matrix entries are in \{0, 1\} such that `incidence[i,j]` equals 1 if there is a directed edge from node `i` to node `j` in the DAG and `incidence[i,j]` equals 0 otherwise

**Value**

the log of the BGe or BDe score of the DAG

**References**


**Examples**

```r
myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
adjacency<-dag2adjacencymatrix(myDAG)
myScore<-scoreparameters(20,"bge",myData)
DAGscore(20,myScore, adjacency)
```

edges.posterior **Estimating posterior probabilities of single edges**

**Description**

This function estimates the posterior probabilities of edges by averaging over a sample of DAGs obtained via an MCMC scheme.

**Usage**

```r
edges.posterior(MCMCchain, pdag = FALSE, burnin = 0.2, endstep = 1)
```
Arguments

MCMCchain list of square matrices with elements in \( \{0, 1\} \) and representing adjacency matrices of a sample of DAGs obtained via an MCMC scheme

pdag logical, if TRUE (FALSE by default) all DAGs in the MCMCchain are first converted to equivalence class (CPDAG) before the averaging

burnin (optional) number between 0 and 1, indicates the percentage of the samples which will be discarded as ‘burn-in’ of the MCMC chain; the rest of the samples will be used to calculate the posterior probabilities; 0.2 by default

dendstep (optional) number between 0 and 1; 1 by default

Value

a square matrix with dimensions equal to the number of variables; each entry \([i,j]\) is an estimate of the posterior probability of the edge from node \(i\) to node \(j\)

Examples

Bostonscore<-scoreparameters(14, "bge", Boston)
## Not run:
samplefit<-orderMCMC(14, Bostonscore, iterations=25000, chainout=TRUE)
MCMCchain<-samplefit$chain$incidence
edgesposterior<-edges.posterior(MCMCchain, burnin=0.2)
edgesposterior<-edges.posterior(MCMCchain, pdag=TRUE, burnin=0.2)
## End(Not run)

iterations.check Performance assessment of iterative MCMC scheme against a known Bayesian network

Description

This function calculates the number of true and false positives, the true positive rate, the structural Hamming distance and score for each iteration in the search procedure implemented in the iterativeMCMCsearch function

Usage

iterations.check(MCMCmult, truedag, sample = FALSE, cpdag = TRUE, pbarrier = 0.5)

Arguments

MCMCmult an object which of class MCMCmult, contained in the output of the function iterativeMCMCsearch, when its chainout argument is set to TRUE; contains adjacency matrices sampled at each iteration of search space expansion; accessible by MCMCout$chain, where MCMCout is the output of function iterativeMCMCsearch
iterativeMCMCsearch

Structure learning with an iterative order MCMC algorithm on an expanded search space

truedag  ground truth DAG which generated the data used in the search procedure; represented by an object of class graphNEL
sample  logical (FALSE by default), indicates if MCMCmult contains sample or maximum score DAGs
cpdag  logical, if TRUE (FALSE by default) all DAGs in the MCMCmult are first converted to their respective equivalence class (CPDAG) before the averaging if parameter sample set to TRUE
pbarrier  threshold such that only edges with a higher posterior probability will be retained in the directed graph summarising the sample of DAGs at each iteration from MCMCmult if parameter sample set to TRUE

Value

A matrix with the number of rows equal to the number of elements in MCMCmult, and 5 columns reporting for the maximally scoring DAG uncovered at each iteration (or for a summary over the sample of DAGs if sample parameter set to TRUE) the number of true positive edges (‘TP’), the number of false positive edges (‘FP’), the true positive rate (‘TPR’), the structural Hamming distance (‘SHD’) and the score of the DAG (‘SC’). Note that the maximum estimated DAG as well as the true DAG are first converted to the corresponding equivalence class (CPDAG) when calculating the SHD.

Examples

```r
myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
myScore<-scoreparameters(20, "bge", myData)
## Not run:
MAPestimate<-iterativeMCMCsearch(20, myScore, chainout=TRUE, scoreout=TRUE)
iterations.check(MAPestimate, myDAG)
## End(Not run)
```

Description

This function implements an iterative search for the maximum a posteriori (MAP) DAG, by means of order MCMC. At each iteration, the current search space is expanded by allowing each node to have up to one additional parent not already included in the search space. By default the initial search space is obtained through the PC-algorithm (using the functions skeleton and pc from the ‘pcalg’ package [Kalisch et al, 2012]). At each iteration order MCMC is employed to search for the MAP DAG. The edges in the MAP DAG are added to the initial search space to provide the search space for the next iteration. The algorithm iterates until no further score improvements can be achieved by expanding the search space. The final search space may be used for the sampling versions of orderMCMC and partitionMCMC.
Usage

iterativeMCMCsearch(n, scoreparam, plus1it = NULL, moveprobs = NULL, MAP = TRUE, posterior = 0.5, iterations = NULL, stepsave = NULL, softlimit = 9, hardlimit = 12, alpha = NULL, gamma = 1, startspace = NULL, blacklist = NULL, verbose = TRUE, chainout = FALSE, scoreout = FALSE, cpdag = FALSE, mergetype = "skeleton", addspace = NULL, scoretable = NULL, startorder = c(1:n))

Arguments

n number of nodes in the Bayesian network
scoreparam an object of class scoreparameters, containing the data and scoring parameters; see constructor function scoreparameters
plus1it (optional) integer, a number of iterations of search space expansion; by default the algorithm iterates until no score improvement can be achieved by further expanding the search space
moveprobs (optional) a numerical vector of 4 values in \{0,1\} corresponding to the probabilities of the following MCMC moves in the order space:
  • exchanging 2 random nodes in the order
  • exchanging 2 adjacent nodes in the order
  • placing a single node elsewhere in the order
  • staying still
MAP logical, if TRUE (default) the search targets the MAP DAG (a DAG with maximum score), if FALSE at each MCMC step a DAG is sampled from the order proportionally to its score; when expanding a search space when MAP=TRUE all edges from the maximum scoring DAG are added to the new space, when MAP=FALSE only edges with posterior probability higher than defined by parameter posterior are added to the search space
posterior logical, when MAP set to FALSE defines posterior probability threshold for adding the edges to the search space
iterations (optional) integer, the number of MCMC steps, the default value is \(3.5n^2 \log n\)
stepsave (optional) integer, thinning interval for the MCMC chain, indicating the number of steps between two output iterations, the default is \(\text{iterations}/1000\)
softlimit (optional) integer, limit on the size of parent sets beyond which adding undirected edges is restricted; below this limit edges are added to expand the parent sets based on the undirected skeleton of the MAP DAG (or from its CPDAG, depending on the parameter mergecp), above the limit only the directed edges are added from the MAP DAG; the limit is 9 by default
hardlimit (optional) integer, limit on the size of parent sets beyond which the search space is not further expanded to prevent long runtimes; the limit is 12 by default
alpha (optional) numerical significance value in \(\{0,1\}\) for the conditional independence tests in the PC-stage (by default 0.4 for \(n < 50\), \(20/n\) for \(n > 50\))
gamma (optional) tuning parameter which transforms the score by raising it to this power, 1 by default
iterativeMCMCsearch

startspace (optional) a square matrix, of dimensions equal to the number of nodes, which defines the search space for the order MCMC in the form of an adjacency matrix; if NULL, the skeleton obtained from the PC-algorithm will be used; if startspace[i,j] equals to 1 (0) it means that the edge from node i to node j is included (excluded) from the search space; to include an edge in both directions, both startspace[i,j] and startspace[j,i] should be 1

blacklist (optional) a square matrix, of dimensions equal to the number of nodes, which defines edges to exclude from the search space; if blacklist[i,j] equals to 1 it means that the edge from node i to node j is excluded from the search space

verbose logical, if TRUE (default) prints messages on the progress of execution

chainout logical, if TRUE (default) the saved MCMC steps are returned, FALSE by default

scoreout logical, if TRUE the search space from the last plus1 iterations and the corresponding score tables are returned, FALSE by default

cpdag logical, if set to TRUE the equivalence class (CPDAG) found by the PC algorithm is used as a search space, when FALSE (default) the undirected skeleton used as a search space

mergetype defines which edges are added to the search space at each expansion iteration; if set to
  • "dag", then edges from maximum scoring DAG are added;
  • "cpdag", then the maximum scoring DAG is first converted to the CPDAG, from which all edges are added to the search space;
  • "skeleton", then the maximum scoring DAG is first converted to the skeleton, from which all edges are added to the search space

addspace (optional) a square matrix, of dimensions equal to the number of nodes, which defines the edges, which are added at to the search space only at the first iteration of iterative search and do not necessarily stay afterwards; defined in the form of an adjacency matrix; if addspace[i,j] equals to 1 (0) it means that the edge from node i to node j is included (excluded) from the search space; to include an edge in both directions, both addspace[i,j] and addspace[j,i] should be 1

scoretable (optional) list of score tables which has to match startspace and addspace

startorder (optional) integer vector of length n, which will be used as the starting order in the MCMC algorithm, the default order is c(1:n)

Value

Depends on the logical parameters chainout and scoreout. If both are FALSE (default), an object of class MCMCmax, containing a list of 4 elements:
  • DAG - the adjacency matrix of the DAG with maximal score
  • order - an order it belongs to
  • score - the score of the reported DAG
  • it - the iteration at which maximum was reached

If chainout is TRUE an object of class MCMCtrace is additionally returned, contains 4 lists (each of the 4 lists has length iterations/stepsave, i.e. the number of saved MCMC steps):
orderMCMC

Structure learning with the order MCMC algorithm

Description

This function implements the order MCMC algorithm for the structure learning of Bayesian networks. This function can be used for MAP discovery and for sampling from the posterior distribution of DAGs given the data. Due to the superexponential size of the search space as the number of nodes increases, the MCMC search is performed on a reduced search space. By default the search space is limited to the skeleton found through the PC algorithm by means of conditional independence tests (using the functions skeleton and pc from the ‘pcalg’ package [Kalisch et al, 2012]).
It is also possible to define an arbitrary search space by inputting an adjacency matrix, for example estimated by partial correlations or other network algorithms. Also implemented is the possibility to expand the default or input search space, by allowing each node in the network to have one additional parent. This offers improvements in the learning and sampling of Bayesian networks.

**Usage**

```r
orderMCMC(n, scoreparam, MAP = TRUE, plus1 = TRUE, startspace = NULL,
blacklist = NULL, startorder = c(1:n), scoretable = NULL,
moveprobs = NULL, iterations = NULL, stepsave = NULL,
alpha = NULL, cpdag = FALSE, gamma = 1, chainout = FALSE,
scoreout = FALSE, verbose = FALSE)
```

**Arguments**

- `n` number of nodes in the Bayesian network
- `scoreparam` an object of class `scoreparameters`, containing the data and score parameters, see constructor function `scoreparameters`
- `MAP` logical, if TRUE (default) the search targets the MAP DAG (a DAG with maximum score), if FALSE at each MCMC step a DAG is sampled from the order proportionally to its score
- `plus1` logical, if TRUE (default) the search is performed on the extended search space
- `startspace` (optional) a square matrix, of dimensions equal to the number of nodes, which defines the search space for the order MCMC in the form of an adjacency matrix. If NULL, the skeleton obtained from the PC-algorithm will be used. If `startspace[i,j]` equals to 1 (0) it means that the edge from node i to node j is included (excluded) from the search space. To include an edge in both directions, both `startspace[i,j]` and `startspace[j,i]` should be 1.
- `blacklist` (optional) a square matrix, of dimensions equal to the number of nodes, which defines edges to exclude from the search space. If `blacklist[i,j]` equals to 1 it means that the edge from node i to node j is excluded from the search space.
- `startorder` (optional) integer vector of length n, which will be used as the starting order in the MCMC algorithm, the default order is `c(1:n)`
- `scoretable` (optional) list of score tables calculated for example by the last iteration of the iterativeMCMCSearch function, to avoid their recomputation The score tables must match the permissible parents in the search space defined by the `startspace` parameter.
- `moveprobs` (optional) a numerical vector of 3 values in \{0,1\} corresponding to the probabilities of the following MCMC moves in the order space
  - exchanging 2 random nodes in the order
  - exchanging 2 adjacent nodes in the order
  - placing a single node elsewhere in the order
  - staying still
- `iterations` (optional) integer, the number of MCMC steps, the default value is $5n^2 \log n$
- `stepsave` (optional) integer, thinning interval for the MCMC chain, indicating the number of steps between two output iterations, the default is `iterations/1000`
alpha (optional) numerical significance value in $\{0, 1\}$ for the conditional independence tests at the PC algorithm stage (by default $0.4$ for $n < 50$, $20/n$ for $n > 50$)

cpdag (optional) logical, if TRUE the CPDAG returned by the PC algorithm will be used as the search space, if FALSE (default) the full undirected skeleton will be used as the search space

gamma (optional) tuning parameter which transforms the score by raising it to this power, $1$ by default

chainout logical, if TRUE the saved MCMC steps are returned, FALSE by default

scoreout logical, if TRUE the search space and score tables are returned, FALSE by default

verbose logical, if TRUE messages about the algorithm’s progress will be printed, FALSE by default

Value

Depends on the logical parameters chainout and scoreout. If both are FALSE (default), an object of class MCMCmax, containing a list of 3 elements:

- DAG - the adjacency matrix of the DAG with maximal score
- order - an order it belongs to
- score - the score of the reported DAG

If chainout is TRUE an object of class MCMCtrace is additionally returned, contains 4 lists (each of the 4 lists has length iterations/stepsave, i.e. the number of saved MCMC steps):

- incidence - contains a list of adjacency matrices of DAGs sampled at each step of MCMC
- DAGscores - contains a list of scores of DAGs sampled at each step of MCMC
- orderscores - contains a list of scores of orders of DAGs sampled at each step of MCMC
- order - contains a list of permutations of the nodes of DAGs sampled at each step of MCMC

If scoreout is TRUE an object of class MCMCspace is additionally returned, contains a list of 2 elements:

- adjacency - the adjacency matrix representing the search space
- scoretable - the list of score tables corresponding to this search space

References


Examples

## Not run:
# find a MAP DAG with search space defined by PC and plus1 neighbourhood
Bostonscore <- scoreparameters(14, "bge", Boston)
orderMAPfit <- orderMCMC(14, Bostonscore)
orderMAPfit$max$score
# sample DAGs with order MCMC
ordersamplefit <- orderMCMC(14, Bostonscore, MAP = FALSE, chainout = TRUE)

## End(Not run)

partitionMCMC

DAG structure sampling with partition MCMC

Description

This function implements the partition MCMC algorithm for the structure learning of Bayesian networks. This procedure provides an unbiased sample from the posterior distribution of DAGs given the data. The search space can be defined either by a preliminary run of the iterativeMCMCsearch function or by a given adjacency matrix (which can be the full matrix with zero on the diagonal, to consider the entire space of DAGs, feasible only for a limited number of nodes).

Usage

partitionMCMC(n, scoreparam, startspace = NULL, blacklist = NULL,
              scoretable = NULL, startDAG = NULL, moveprobs = NULL,
              iterations = NULL, stepsave = NULL, gamma = 1, verbose = TRUE)

Arguments

n number of nodes in the Bayesian network
scoreparam an object of class scoreparameters, containing the data and scoring parameters; see constructor function scoreparameters.
startspace (optional) a square matrix, of dimensions equal to the number of nodes, which defines the search space for the order MCMC in the form of an adjacency matrix; if NULL, the skeleton obtained from the PC-algorithm will be used. If startspace[i,j] equals to 1 (0) it means that the edge from node i to node j is included (excluded) from the search space. To include an edge in both directions, both startspace[i,j] and startspace[j,i] should be 1.
blacklist (optional) a square matrix, of dimensions equal to the number of nodes, which defines edges to exclude from the search space; if blacklist[i,j]=1 it means that the edge from node i to node j is excluded from the search space
scoretable (optional) list of score tables calculated for example by the last iteration of the iterativeMCMCsearch function, to avoid their recomputation; the score tables must match the permissible parents in the search space defined by the startspace parameter
partitionMCMC

(startDAG (optional) an adjacency matrix of dimensions equal to the number of nodes, representing a DAG in the search space defined by startspace. If startspace is defined but startDAG is not, an empty DAG will be used by default

moveprobs (optional) a numerical vector of 5 values in $\{0, 1\}$ corresponding to the following MCMC move probabilities in the space of partitions:

- swap any two elements from different partition elements
- swap any two elements in adjacent partition elements
- split a partition element or join one
- move a single node into another partition element or into a new one
- stay still

iterations (optional) integer, the number of MCMC steps, the default value is $8n^2 \log n$

steprate (optional) integer, thinning interval for the MCMC chain, indicating the number of steps between two output iterations, the default is iterations/1000

gamma (optional) tuning parameter which transforms the score by raising it to this power, 1 by default

verbose logical, if set to TRUE (default) messages about progress will be printed

Value

an object of class `MCMCtrace`, which contains a list of 5 elements (each list contains iterations/steprate elements):

- incidence - contains a list of adjacency matrices of DAGs sampled at each step of MCMC
- DAGscores - contains a list of scores of DAGs sampled at each step of MCMC
- partitionscores - contains a list of scores of partitions of DAGs sampled at each step of MCMC
- order - contains a list of permutations of the nodes in partitions of DAGs sampled at each step of MCMC
- partition - contains a list of partitions of DAGs sampled at each step of MCMC

References


## Examples

```r
## Not run:
myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
myScore<-scoreparameters(20, "bge", myData)
partfit<-partitionMCMC(20,myScore)
sample.check(20,partfit$chain$incidence,myDAG)
## End(Not run)
```

**sample.check**

*Performance assessment of sampling algorithms against a known Bayesian network*

### Description

This function calculates the number of true and false positives and the structural Hamming distance between a ground truth DAG and a directed graph summarising a sample of DAGs obtained from an MCMC scheme, as the posterior probability threshold is varied.

### Usage

```r
sample.check(n, MCMCchain, truedag, pbarrier = c(0.99, 0.95, 0.9, 0.8, 0.7, 0.6, 0.5, 0.4, 0.3, 0.2), pdag = TRUE, burnin = 0.2)
```

### Arguments

- `n`: number of nodes in the Bayesian network
- `MCMCchain`: list of adjacency matrices with dimensions equal to `n` and elements in `{0,1}`, representing a sample of DAGs from an MCMC scheme
- `truedag`: ground truth DAG which generated the data used in the search procedure; represented by an object of class `graphNEL`
- `pbarrier`: (optional) a vector of numeric values between 0 and 1, defining posterior probabilities according to which the edges of assessed structures are drawn, please note very low barriers can lead to very dense structures; by default `pbarrier = c(0.99, 0.95, 0.9, 0.8, 0.7, 0.6, 0.5, 0.4, 0.3, 0.2)`
- `pdag`: logical, if TRUE (default) all DAGs in the MCMCchain are first converted to equivalence class (CPDAG) before the averaging
- `burnin`: (optional) number between 0 and 1, indicates the percentage of the samples which will be the discarded as ‘burn-in’ of the MCMC chain; the rest of the samples will be used to calculate the posterior probabilities; 0.2 by default

### Value

A matrix with the number of rows equal to the number of posterior thresholds tested, and 4 columns reporting for each thresholded directed graphs the number of true positive edges (‘TP’), the number of false positive edges (‘FP’), the structural Hamming distance (‘SHD’) and the posterior threshold
scoreagainstDAG

Calculating the score of a sample against a DAG

Description
This function calculates the score of a given sample against a DAG represented by its incidence matrix.

Usage
scoreagainstDAG(n, scoreparam, incidence, datatoscore = NULL, marginalise = FALSE)

Arguments
- **n**: number of nodes in the Bayesian network
- **scoreparam**: an object of class scoreparameters; see constructor function scoreparameters
- **incidence**: a square matrix of dimensions equal to the number of variables with entries in \{0,1\}, representing the adjacency matrix of the DAG against which the score is calculated
- **datatoscore**: (optional) a matrix (vector) containing binary (for BDe score) or continuous (for the BGe score) observations (or just one observation) to be scored; the number of columns should be equal to the number of variables in the Bayesian network, the number of rows should be equal to the number of observations; by default all data from scoreparam parameter is used
- **marginalise**: (optional for continuous data), whether to use the posterior mean for scoring (default) or to marginalise over the posterior distribution (more computationally costly)

Value
the log of the BDe/BGe score of given observations against a DAG
References


Examples

```r
## Not run:
myDAG <- pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData <- pcalg::rmvDAG(200, myDAG)
adjacency <- dag2adjacencymatrix(myDAG)
param <- scoreparameters()
scoreagainstDAG(20, myData, adjacency)

## End(Not run)
```

scoreparameters

Initialising score object

Description

This function returns an object of class scoreparameters containing the data and parameters needed for calculation of the BDe/BGe score, or a user defined score.

Usage

```r
scoreparameters(n, scoretype = c("bge", "bde", "bdecat", "dbn", "usr"),
data, weightvector = NULL, bgnodes = NULL, bgepar = list(am = 1, aw
= NULL), bdepar = list(chi = 0.5, edgepf = 2), bdecatpar = list(chi =
0.5, edgepf = 2), dbnpar = list(dbnscoretype = c("bge", "bde",
"bdecat"), slices = 2), usrpar = list(pctesttype = c("bge", "bde",
"bdecat")), edgepmat = NULL, nodeslabels = NULL)
```

Arguments

- **n**: number of nodes (variables) in the Bayesian network (excluding background nodes)
- **scoretype**: the score to be used to assess the DAG structure: "bge" for Gaussian data, "bde" for binary data, "bdecat" for categorical data, "dbn" for dynamic Bayesian networks, "usr" for a user defined score
- **data**: the data matrix with n columns (the number of variables) and a number of rows equal to the number of observations
- **weightvector**: (optional) a numerical vector of positive values representing the weight of each observation; should be NULL (default) for non-weighted data
- **bgnodes**: (optional) a numerical vector which contains numbers of columns in the data defining background nodes, background nodes are nodes which have no parents but can be parents of other nodes in the network
scoreparameters

bgepar a list which contains parameters for BGe score:
- am (optional) a positive numerical value, 1 by default
- aw (optional) a positive numerical value should be more than n+1, n+am+1 by default

bdepar a list which contains parameters for BDe score for binary data:
- chi (optional) a positive number of prior pseudo counts used by the BDe score, 0.5 by default
- edgepf (optional) a positive numerical value providing the edge penalization factor to be combined with the BDe score, 2 by default

bdecatpar a list which contains parameters for BDe score for categorical data:
- chi (optional) a positive number of prior pseudo counts used by the BDe score, 0.5 by default
- edgepf (optional) a positive numerical value providing the edge penalization factor to be combined with the BDe score, 2 by default

dbnpar which type of score to use for the slices
- dbnscoretype (optional) "bge" for continuous data, "bde" for binary data or "bdecat" for categorical
- slices the number of time slices

usrpar a list which contains parameters for the user defined score
- pctesttype (optional) "bde" to use the independence test for binary data, "bge" for continuous data

edgepmat (optional) a matrix of positive numerical values providing the per edge penalization factor to be added to the score, NULL by default

nodeslabels (optional) a vector of characters which denote the names of nodes in the Bayesian network

Value

an object of class scoreparameters, which includes all necessary information for calculating the BDe/BGe score

References


Examples

myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
myScore<-scoreparameters(20, "bge", myData)

Description

This function returns an object of class scoreparameters containing the data and parameters needed for calculation of the BDe/BGe score, or a user defined score.

Usage

scoreparameters.tested(n, scoretype = c("bge", "bde", "bdecat", "usr"),
data, weightvector = NULL, bgnodes = NULL, bgepar = list(am = 1, aw = NULL), bdepar = list(chi = 0.5, edgepf = 2), bdecatpar = list(chi = 0.5, edgepf = 2), usrpar = list(pctesttype = c("bge", "bde", "bdecat")), edgepmat = NULL, nodeslabels = NULL)

Arguments

n number of nodes (variables) in the Bayesian network (excluding background nodes)
scoretype the score to be used to assess the DAG structure: "bge" for Gaussian data, "bde" for binary data, "bdecat" for categorical data, "usr" for a user defined score
data the data matrix with n columns (the number of variables) and a number of rows equal to the number of observations
weightvector (optional) a numerical vector of positive values representing the weight of each observation; should be NULL (default) for non-weighted data
bgnodes (optional) a numerical vector which contains numbers of columns in the data defining background nodes, background nodes are nodes which have no parents but can be parents of other nodes in the network
bgepar a list which contains parameters for BGe score:
  • am (optional) a positive numerical value, 1 by default
  • aw (optional) a positive numerical value should be more than n+1, n+am+1 by default
bdepar a list which contains parameters for BDe score for binary data:
  • chi (optional) a positive number of prior pseudo counts used by the BDe score, 0.5 by default
  • edgepf (optional) a positive numerical value providing the edge penalization factor to be combined with the BDe score, 2 by default
scoreparameters tested

bdecatpar a list which contains parameters for BDe score for categorical data:
  - chi (optional) a positive number of prior pseudo counts used by the BDe score, 0.5 by default
  - edgepf (optional) a positive numerical value providing the edge penalization factor to be combined with the BDe score, 2 by default

usrpar a list which contains parameters for the user defined score
  - pctesttype (optional) "bde" to use the independence test for binary data, "bge" for continuous data

dgepmat (optional) a matrix of positive numerical values providing the per edge penalization factor to be added to the score, NULL by default

nodeslabels (optional) a vector of characters which denote the names of nodes in the Bayesian network

Value

an object of class scoreparameters, which includes all necessary information for calculating the BDe/BGe score

References


Examples

myDAG<-pcalg::randomDAG(20, prob=0.15, lB = 0.4, uB = 2)
myData<-pcalg::rmvDAG(200, myDAG)
myScore<-scoreparameters(20, "bge", myData)
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