

Package ‘LAWBL’

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Type Package

Title Latent (Variable) Analysis with Bayesian Learning

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Description An analytical framework for latent variables with different Bayesian learning methods, including the partially confirmatory factor analysis (Chen, Guo, Zhang, & Pan, 2020) <DOI: 10.1037/met0000293>, its generalized version, and the partially confirmatory item response model (Chen, 2020) <DOI: 10.1007/s11336-020-09724-3>.

License GPL-3

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LazyData true

Depends R (>= 3.6.0)

Imports stats, MASS, coda

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URL <https://github.com/Jinsong-Chen/LAWBL>,
<https://jinsong-chen.github.io/LAWBL/>

BugReports <https://github.com/Jinsong-Chen/LAWBL/issues>

Suggests knitr, rmarkdown, testthat

VignetteBuilder knitr

NeedsCompilation no

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| | |
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| LAWBL-package | <i>LAWBL: Latent (Variable) Analysis with Bayesian Learning</i> |
|---------------|---|

Description

The long-term goal of this package is to provide an analytical framework for modeling latent variables with different Bayesian learning methods.

Details

Currently, this package includes the Partially Confirmatory Factor Analysis (PCFA) model for continuous data (Chen, Guo, Zhang, & Pan, 2020), the generalized PCFA (GPCFA) model covering continuous, categorical, and mixed-type data, and the partially confirmatory item response model (PCIRM) for continuous and dichotomous data with intercept terms (Chen, 2020). The three models represent a partially confirmatory approach covering a wide range of the exploratory-confirmatory continuum under the context of factor analysis and item response theory. For PCFA, GPCFA, and PCIRM, there are two major model variants with different constraints for identification. One assumes local independence (LI) with a more exploratory tendency, which can be also called the E-step. The other allows local dependence (LD) with a more confirmatory tendency, which can be also called the C-step. Parameters are obtained by sampling from the posterior distributions with the Markov chain Monte Carlo (MCMC) techniques. Different Bayesian Lasso methods are used to regularize the loading pattern and local dependence.

Note

This package is under development. You are very welcome to send me any comments or suggestions for improvements, and to share with me any problems you may encounter with the use of this package.

Author(s)

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References

- Chen, J., Guo, Z., Zhang, L., & Pan, J. (2020). A partially confirmatory approach to scale development with the Bayesian Lasso. *Psychological Methods*. Advance online publication. DOI:10.1037/met0000293
- Chen, J. (2020). A partially confirmatory approach to the multidimensional item response theory with the Bayesian Lasso. *Psychometrika*. 85(3), 738-774. DOI:10.1007/s11336-020-09724-3.

pcfa

(Generalized) Partially Confirmatory Factor Analysis

Description

PCFA is a partially confirmatory approach covering a wide range of the exploratory-confirmatory continuum in factor analytic models (Chen, Guo, Zhang, & Pan, 2020). The PCFA is only for continuous data, while the generalized PCFA (GPCFA) covers both continuous and categorical data. There are two major model variants with different constraints for identification. One assumes local independence (LI) with a more exploratory tendency, which can be also called the E-step. The other allows local dependence (LD) with a more confirmatory tendency, which can be also called the C-step. Parameters are obtained by sampling from the posterior distributions with the Markov chain Monte Carlo (MCMC) techniques. Different Bayesian Lasso methods are used to regularize the loading pattern and LD. The estimation results can be summarized with [summary.lawbl](#) and the factorial eigenvalue can be plotted with [plot_eigen](#).

Usage

```
pcfa(  
  dat,  
  Q,  
  LD = TRUE,  
  cati = NULL,  
  PPMC = FALSE,  
  burn = 5000,  
  iter = 5000,  
  update = 1000,  
  missing = NA,  
  rseed = 12345,  
  digits = 4,  
  alas = FALSE,  
  verbose = FALSE  
)
```

Arguments

dat A $N \times J$ data matrix or *data.frame* consisting of the responses of N individuals to J items.

| | |
|---------|--|
| Q | A $J \times K$ design matrix for the loading pattern with K factors and J items. Elements are 1, -1, and 0 for specified, unspecified, and zero-fixed loadings, respectively. For models with LI or the E-step, one can specify a few (e.g., 2) loadings per factor. For models with LD or the C-step, the sufficient condition of one specified loading per item is suggested, although there can be a few items without any specified loading. See <code>Examples</code> . |
| LD | logical; TRUE for allowing LD (model with LD or C-step). |
| cati | The set of categorical (polytomous) items in sequence number (i.e., 1 to J); NULL for no and -1 for all items (default is NULL). |
| PPMC | logical; TRUE for conducting posterior predictive model checking. |
| burn | Number of burn-in iterations before posterior sampling. |
| iter | Number of formal iterations for posterior sampling (> 0). |
| update | Number of iterations to update the sampling information. |
| missing | Value for missing data (default is NA). |
| rseed | An integer for the random seed. |
| digits | Number of significant digits to print when printing numeric values. |
| alas | logical; for adaptive Lasso or not. The default is FALSE. |
| verbose | logical; to display the sampling information every update or not. <ul style="list-style-type: none"> • Feigen: Eigenvalue for each factor. • NLA_lg3: Number of Loading estimates $> .3$ for each factor. • Shrink: Ave. shrinkage parameter (for adaptive LASSO) for each factor. • Adj PSR: Adjusted PSR for each factor. • Ave. Thd: Ave. thresholds. • Acc Rate: Acceptance rate of threshold (MH algorithm). • LD$>.2 >.1$ LD$>.2 >.1$: # of LD terms larger than $.2$ and $.1$, and LD's shrinkage parameter. |

Value

pcfa returns an object of class `lawbl` without item intercepts. It contains a lot of information about the posteriors that can be summarized using `summary.lawbl`. The factorial eigenvalue can be plotted with `plot_eigen`.

References

Chen, J., Guo, Z., Zhang, L., & Pan, J. (2020). A partially confirmatory approach to scale development with the Bayesian Lasso. *Psychological Methods*. Advance online publication. DOI: 10.1037/met0000293.

Examples

```
#####
# Example 1: Estimation with continuous data & LD #
#####
```

```

dat <- sim18cfa1$dat
J <- ncol(dat)
K <- 3
Q<-matrix(-1,J,K);
Q[1:6,1]<-Q[7:12,2]<-Q[13:18,3]<-1

m0 <- pcfa(dat = dat, Q = Q, LD = TRUE, burn = 2000, iter = 2000)
summary(m0) # summarize basic information
summary(m0, what = 'qlambda') #summarize significant loadings in pattern/Q-matrix format
summary(m0, what = 'offpsx') #summarize significant LD terms

#####
# Example 1: Estimation with categorical data & LI #
#####
dat <- sim18ccfa40$dat
J <- ncol(dat)
K <- 3
Q<-matrix(-1,J,K);
Q[1:2,1]<-Q[7:8,2]<-Q[13:14,3]<-1

m1 <- pcfa(dat = dat, Q = Q, LD = FALSE, cati=-1, burn = 2000, iter = 2000)
summary(m1) # summarize basic information
summary(m1, what = 'qlambda') #summarize significant loadings in pattern/Q-matrix format
summary(m1, what = 'offpsx') #summarize significant LD terms
summary(m1, what='thd') #thresholds for categorical items

```

Description

pcirm is a partially confirmatory approach to item response models (Chen, 2020), which estimates the intercept for continuous and dichotomous data. Similar to PCFA and GPCFA, there are two major model variants with different constraints for identification. One assumes local independence (LI) with a more exploratory tendency, which can be also called the E-step. The other allows local dependence (LD) with a more confirmatory tendency, which can be also called the C-step. Parameters are obtained by sampling from the posterior distributions with the Markov chain Monte Carlo (MCMC) techniques. Different Bayesian Lasso methods are used to regularize the loading pattern and LD. The estimation results can be summarized with [summary.lawbl](#) and the factorial eigenvalue can be plotted with [plot_eigen](#).

Usage

```

pcirm(
  dat,
  Q,
  LD = TRUE,

```

```

cati = NULL,
PPMC = FALSE,
burn = 5000,
iter = 5000,
update = 1000,
missing = NA,
rseed = 12345,
digits = 4,
alas = FALSE,
verbose = FALSE
)

```

Arguments

| | |
|---------|---|
| dat | A $N \times J$ data <i>matrix</i> or <i>data.frame</i> consisting of the responses of N individuals to J items. Only continuous and dichotomous data are supported. |
| Q | A $J \times K$ design matrix for the loading pattern with K factors and J items. Elements are 1, -1, and 0 for specified, unspecified, and zero-fixed loadings, respectively. For models with LI or the E-step, one can specify a few (e.g., 2) loadings per factor. For models with LD or the C-step, the sufficient condition of one specified loading per item is suggested, although there can be a few items without any specified loading. See Examples. |
| LD | logical; TRUE for allowing LD (model with LD or C-step). |
| cati | The set of dichotomous items in sequence number (i.e., 1 to J); NULL for no and -1 for all items (default is NULL). |
| PPMC | logical; TRUE for conducting posterior predictive model checking. |
| burn | Number of burn-in iterations before posterior sampling. |
| iter | Number of formal iterations for posterior sampling (> 0). |
| update | Number of iterations to update the sampling information. |
| missing | Value for missing data (default is NA). |
| rseed | An integer for the random seed. |
| digits | Number of significant digits to print when printing numeric values. |
| alas | logical; for adaptive Lasso or not. The default is FALSE. |
| verbose | logical; to display the sampling information every update or not. <ul style="list-style-type: none"> • Feigen: Eigenvalue for each factor. • NLA_lg3: Number of Loading estimates $> .3$ for each factor. • Shrink: Ave. shrinkage parameter (for adaptive LASSO) for each factor. • Adj PSR: Adjusted PSR for each factor. • Ave. Int.: Ave. item intercept. • LD$>.2 >.1$ LD$>.2 >.1$: # of LD terms larger than .2 and .1, and LD's shrinkage parameter. |

Value

pcirm returns an object of class `lawbl` with item intercepts. It contains a lot of information about the posteriors that can be summarized using `summary.lawbl`. The factorial eigenvalue can be plotted with `plot_eigen`.

References

Chen, J. (2020). A partially confirmatory approach to the multidimensional item response theory with the Bayesian Lasso. *Psychometrika*. 85(3), 738-774. DOI:10.1007/s11336-020-09724-3.

Examples

```
#####
# Example 1: Estimation with LD #
#####

dat <- sim24ccfa21$dat
J <- ncol(dat)
K <- 3
Q<-matrix(-1,J,K);
Q[1:8,1]<-Q[9:16,2]<-Q[17:24,3]<-1

m0 <- pcirm(dat = dat, Q = Q, LD = TRUE, cati = -1, burn = 2000,iter = 2000)
summary(m0) # summarize basic information
summary(m0, what = 'qlambda') #summarize significant loadings in pattern/Q-matrix format
summary(m0, what = 'offpsx') #summarize significant LD terms

#####
# Example 2: Estimation with LD #
#####

Q<-cbind(Q,-1);
Q[15:16,4]<-1

m1 <- pcirm(dat = dat, Q = Q, LD = FALSE, cati = -1, burn = 2000,iter = 2000)
summary(m1) # summarize basic information
summary(m1, what = 'qlambda') #summarize significant loadings in pattern/Q-matrix format
summary(m1, what = 'offpsx') #summarize significant LD terms
```

plot_eigen

Factorial eigenvalue plot

Description

Provide plots based on the factorial eigenvalues of a pcfa objects.

Usage

```
plot_eigen(obj, what = "trace")
```

Arguments

obj A lawbl object

what A list of options for what to plot.

- trace: The trace of each factor's eigenvalue.
- density: The trace of each factor's eigenvalue.
- APSR: The pseudo Gelman-Rubin diagnostics of each factor's eigenvalue.

Examples

```
dat <- sim18cfa0$dat
J <- ncol(dat)
K <- 3
Q<-matrix(-1,J,K);
Q[1:2,1]<-Q[7:8,2]<-Q[13:14,3]<-1

m0 <- pcfa(dat = dat, Q = Q, LD = FALSE, burn = 1000, iter = 1000)
plot_eigen(m0) # trace
plot_eigen(m0, what='density')
plot_eigen(m0, what='APSR')
```

sim18ccfa40

Simulated CCFA data with LI and missingness

Description

Categorical CFA data simulated based on 18 items, 3 factors, and 4 categories with local independence and 10

Usage

```
sim18ccfa40
```

Format

A list with components:

dat A dataset with simulated responses of 1000 individuals to 18 items

qlam Loading pattern and values used to simulated the data

`sim18ccfa41`*Simulated CCFA data with LD and missingness*

Description

Categorical CFA data simulated based on 18 items, 3 factors, and 4 categories with local dependence and 10

Usage`sim18ccfa41`**Format**

A list with components:

`dat` A dataset with simulated responses of 1000 individuals to 18 items

`qlam` Loading pattern and values used to simulated the data

`LD` Local dependence between items (LD effect = .3)

`sim18cfa0`*Simulated CFA data with LI*

Description

CFA data simulated based on 18 items, 3 factors and local independence; factorial correlation $\Phi = .3$.

Usage`sim18cfa0`**Format**

A list with components:

`dat` A dataset with simulated responses of 1000 individuals to 18 items

`qlam` Loading pattern and values used to simulated the data

sim18cfa1

Simulated CFA data with LD

Description

CFA data simulated based on 18 items, 3 factors and local dependence; factorial correlation $\Phi = .3$.

Usage

sim18cfa1

Format

A list with components:

dat A dataset with simulated responses of 1000 individuals to 18 items

qlam Loading pattern and values used to simulated the data

LD Local dependence between items (LD effect = .3)

sim18mcfa41

Simulated MCFA data with LD and Missingness

Description

CFA data mixed with continuous and categorical responses simulated based on 3 factors, 12 4-category items, 6 continuous items, local dependence, and 10 factorial correlation $\Phi = .3$.

Usage

sim18mcfa41

Format

A list with components:

dat A dataset with simulated responses of 500 individuals to 18 items

qlam Loading pattern and values used to simulated the data

LD Local dependence between items (LD effect = .3)

| | |
|-------------|---|
| sim24ccfa21 | <i>Simulated CCFA data (dichotomous) with LD and a minor factor/trait</i> |
|-------------|---|

Description

Categorical CFA data simulated based on 24 items, 4 factors, 2 categories and local dependence; factorial correlation $\Phi = .3$. The last factor/trait is minor (measured by cross-loadings only).

Usage

```
sim24ccfa21
```

Format

A list with components:

dat A dataset with simulated responses of 1000 individuals to 24 items

qlam Loading pattern and values used to simulated the data

LD Local dependence between items (LD effect = .3)

| | |
|---------|--|
| sim_lvm | <i>Simulating data with Latent Variable Modeling</i> |
|---------|--|

Description

sim_lvm can simulate data based on factor analysis or item response models with different response formats (continuous or categorical), loading patterns and residual covariance (local dependence) structures.

Usage

```
sim_lvm(  
  N = 1000,  
  K = 3,  
  ipf = 8,  
  cpf = 2,  
  lam = 0.7,  
  lac = 0.3,  
  phi = 0.5,  
  ph1 = -1,  
  ecr = 0,  
  ome_out = FALSE,  
  cati = NULL,  
  noc = c(4),  
  misp = 0,
```

```

rseed = 333,
necw = K,
necb = K,
add_ind = c(),
add_la = 0.5,
add_phi = 0,
zero_it = 0,
digits = 4
)

```

Arguments

| | |
|---------|---|
| N | Sample size. |
| K | Number of factors. |
| ipf | Items per factor. |
| cpf | Cross-loadings per factor. |
| lam | Number of formal iterations for posterior sampling. |
| lac | Number of iterations to update the sampling information. |
| phi | Homogeneous correlations between any two factors. |
| ph1 | Correlation between factor 1 and 2 (if it's different from phi). |
| ecr | Residual correlation (local dependence). |
| ome_out | Output factor score or not. |
| cati | The set of categorical (polytomous) items in sequence number (i.e., 1 to J); NULL for no and -1 for all (default is NULL). |
| noc | Number of categories for categorical items |
| misp | Proportion of missingness. |
| rseed | An integer for the random seed. |
| necw | Number of within-factor local dependence. |
| necb | Number of between-factor local dependence. |
| add_ind | (Additional) minor factor with cross-loadings. |
| add_la | Value of cross-loadings on (Additional) minor factor. |
| add_phi | Correlations between (Additional) minor factor and other factors. |
| zero_it | Surplus items with zero loading. |
| digits | Number of significant digits to print when printing numeric values. |

Value

An object of class `list` containing the data, loading, and factorial correlation matrix.

Examples

```
# for continuous data with cross-loadings and local dependence effect .3
out <- sim_lvm(N=1000,K=3,ipf=6,lam = .7, lac=.3,ecr=.3)
summary(out$dat)
out$MLA
out$ofd_ind

# for categorical data with cross-loadings .4 and 10% missingness
out <- sim_lvm(N=1000,K=3,ipf=6,lam = .7, lac=.4,cati=-1,noc=4,misp=.1)
summary(out$dat)
out$MLA
out$ofd_ind
```

summary.lawbl

*Summary method for pcfa objectects***Description**

Provide basic information for an PCFA object, and summarize various posteriors.

Usage

```
## S3 method for class 'lawbl'
summary(
  object,
  what = "basic",
  med = FALSE,
  SL = 0.05,
  detail = FALSE,
  digits = 4,
  ...
)
```

Arguments

| | |
|--------|---|
| object | A lawbl object |
| what | A list of options for what to summarize. <ul style="list-style-type: none"> • basic: Basic information about the model and posteriors. • lambda: Loading estimates. • qlambda: Loading estimates in pattern/Q-matrix format. • eigen: Factorial eigen value. • dpsx: Diagonal elements in the residual covariance matrix PSX. • offpsx: Off-diagonal elements in PSX; local dependence terms. • phi: Factorial correlations. |

| | |
|--------|--|
| | <ul style="list-style-type: none"> • thd: Threshold estimates. • int: Intercept estimates (for <code>pcirm</code> only). • shrink: (Ave) shrinkage for each factor's loadings and LD (if LD in <code>pcfa = T</code>). • all: All above information. |
| med | logical; if the posterior median (TRUE) or mean (FALSE) is used as the estimate. |
| SL | Significance level for interval estimate. The default is .05. |
| detail | logical; if only significant (FALSE) or all (TRUE) estimates are presented. |
| digits | Number of significant digits to print when printing numeric values. |
| ... | additional arguments |

Value

A list or matrix containing the summarized information based on the option `what`.

Examples

```
dat <- sim18cfa0$dat
J <- ncol(dat)
K <- 3
Q<-matrix(-1,J,K);
Q[1:2,1]<-Q[7:8,2]<-Q[13:14,3]<-1

m0 <- pcfa(dat = dat, Q = Q, LD = FALSE,burn = 1000, iter = 1000)
summary(m0) # summarize basic information
summary(m0, what = 'lambda') #summarize significant loadings
summary(m0, what = 'qlambda') #summarize significant loadings in pattern/Q-matrix format
summary(m0, what = 'offpsx') #summarize significant LD terms
```

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