Package ‘RegSDC’

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Type Package
Title Information Preserving Regression-Based Tools for Statistical Disclosure Control
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Imports SSBtools, MASS, methods
Description Implementation of the methods described in the paper with the above title: Langsrud, Ø. (2019) <doi:10.1007/s11222-018-9848-9>. Open view-only version at <https://rdcu.be/bfeWQ>. The package can be used to generate synthetic or hybrid continuous microdata, and the relationship to the original data can be controlled in several ways. A function for replacing suppressed tabular cell frequencies with decimal numbers is included.
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R topics documented:

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**Description**

The limit calculated by `FindAlpha` is used when alpha = 1 cannot be chosen (warning produced). In output, alpha is attribute.

**Usage**

```r
CalculateCdirect(a, b, epsAlpha = 1e-07, AlphaHandler = warning, 
alpha = NULL)
```

```r
CalculateC(a, b, ..., viaQR = NULL, returnAlpha = FALSE)
```

**Arguments**

- `a` matrix E in paper
- `b` matrix Eg in paper
- `epsAlpha` Precision constant for alpha calculation
- `AlphaHandler` Function (warning or stop) to be used when alpha<1
- `alpha` Possible with alpha as input instead of computing
- `...` Arguments to `CalculateCdirect`
- `viaQR` When TRUE QR is involved. This may be needed to handle colinear data. When NULL viaQR is set to TRUE if ordinary computations fail.
- `returnAlpha` When TRUE alpha (1 or value below 1) is returned instead of C. Attribute viaQR is included.

**Details**

When `epsAlpha=NULL` calculations are performed directly (alpha=1) and alpha is not attribute.

**Value**

Calculated C with attributes alpha and viaQR (when `CalculateC`)
FindAlpha

Author(s)
Øyvind Langsrud

Examples

x <- 1:10
y <- matrix(rnorm(30) + 1:30, 10, 3)
a <- residuals(lm(y ~ x))
b <- residuals(lm(2 * y + matrix(rnorm(30), 10, 3) - x))

a1 <- a
b1 <- b
a1[, 3] <- a[, 1] + a[, 2]
b1[, 3] <- b[, 1] + b[, 2]

alpha <- FindAlpha(a, b)
FindAlphaSimple(a, b)  # Same result as above
CalculateC(a, b)
CalculateCdirect(a, b)  # Same result as above without viaQR attribute
CalculateCdirect(a, b, alpha = alpha/(1 + 1e-07))  # Same result as above since epsAlpha = 1e-07
CalculateCdirect(a, b, alpha = alpha/2)  # OK
# CalculateCdirect(a,b, alpha = 2*alpha)  # Not OK

FindAlpha(a, b1)
# FindAlphaSimple(a,b1)  # Not working since b1 is collinear
CalculateC(a, b1, returnAlpha = TRUE)  # Almost same alpha as above (epsAlpha cause difference)

FindAlpha(b, a)
CalculateC(b, a, returnAlpha = TRUE)  # 1 returned (not same as above)
CalculateC(b, a)

FindAlpha(b1, a)  # alpha smaller than epsAlpha is set to 0 in CalculateC
CalculateC(b1, a)  # When alpha = 0 C is calculated by GenQR instead of chol

Description
Function to find the largest alpha that makes equation 10 in the paper solvable.

Usage
FindAlpha(a, b, tryViaQR = TRUE)

FindAlphaSimple(a, b)
**GenQR**

**Description**
Matrix X decomposed as Q and R (X=QR) where columns of Q are orthonormal. Ordinary QR or SVD may be used.

**Usage**
```r
GenQR(x, doSVD = FALSE, findR = TRUE, makeunique = findR, tol = 1e-07)
```

**Arguments**
- **x**: Matrix to be decomposed
- **doSVD**: When TRUE SVD instead of QR
- **findR**: When FALSE only Q returned
- **makeunique**: When TRUE force uniqueness by positive diagonal elements (QR) or by column sums (SVD)
- **tol**: As input to qr or, in the case of svd(), similar as input to MASS::ginv().

**Value**
alpha

**Note**
FindAlphaSimple performs the calculations by a simple/direct method. FindAlpha is made to handle problematic special cases.

**Author(s)**
Øyvind Langsrud

**See Also**
See examples in the documentation of `CalculateC`.
Details

To handle dependency a usual decomposition of $X$ is $PX=QR$ where $P$ is a permutation matrix. This function returns $RP^T$ as $R$. When SVD, $Q=U$ and $R=SV^T$.

Value

List with $Q$ and $R$ or just $Q$

Author(s)

Øyvind Langsrud

Examples

```
GenQR(matrix(rnorm(15),5,3))
GenQR(matrix(rnorm(15),5,3)[,c(1,2,1,3)])
GenQR(matrix(rnorm(15),5,3)[,c(1,2,1,3)],TRUE)
```

RegSDCadd

Regression-based SDC Tools - Synthetic addition with residual correlation control

Description

Implementation of equation 6 (arbitrary residual data) and equation 7 (residual correlations) in the paper. The alpha limit is calculated (equation 9). The limit is used when $\alpha=1$ cannot be chosen (warning produced). In output, $\alpha$ is attribute.

Usage

```
RegSDCadd(y, resCorr = NULL, x = NULL, yStart = NULL,
          ensureIntercept = TRUE)
```

Arguments

<table>
<thead>
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<th>Argument</th>
<th>Description</th>
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<tbody>
<tr>
<td>y</td>
<td>Matrix of confidential variables</td>
</tr>
<tr>
<td>resCorr</td>
<td>Required residual correlations (possibly recycled)</td>
</tr>
<tr>
<td>x</td>
<td>Matrix of non-confidential variables</td>
</tr>
<tr>
<td>yStart</td>
<td>Arbitrary data whose residuals will be used. Will be calculated from resCorr when NULL.</td>
</tr>
<tr>
<td>ensureIntercept</td>
<td>Whether to ensure/include a constant term. Non-NULL x is subjected to $\text{EnsureIntercept}$</td>
</tr>
</tbody>
</table>

Details

Use $\text{epsAlpha}=$NULL to avoid calculation of $\alpha$. Use of $\alpha(<1)$ will produce a warning. Input matrices are subjected to $\text{EnsureMatrix}$. 
Value

Generated version of y with alpha as attribute

Author(s)

Øyvind Langsrud

Examples

```r
x <- matrix(1:10, 10, 1)
y <- matrix(rnorm(30) + 1:30, 10, 3)
yOut <- RegSDCadd(y, c(0.1, 0.2, 0.3), x)

# Correlations between residuals as required
diag(cor(residuals(lm(y ~ x)), residuals(lm(yOut ~ x))))

# Identical covariance matrices
cov(y) - cov(yOut)
cov(residuals(lm(y ~ x))) - cov(residuals(lm(yOut ~ x)))

# Identical regression results
summary(lm(y[, 1] ~ x))
summary(lm(yOut[, 1] ~ x))

# alpha as attribute
attr(yOut, "alpha")

# With yStart as input and alpha limit in use (warning produced)
yOut <- RegSDCadd(y, NULL, 2 * y + matrix(rnorm(30), 10, 3))
attr(yOut, "alpha")

# Same correlation for all variables
RegSDCadd(y, 0.2, x)
# But in this case RegSDCcomp is equivalent and faster
RegSDCComp(y, 0.2, x)

# Make nearly collinear data
y[, 3] <- y[, 1] + y[, 2] + 0.001 * y[, 3]
# Not possible to achieve correlations. Small alpha with warning.
RegSDCadd(y, c(0.1, 0.2, 0.3), x)
# Exact collinear data
y[, 3] <- y[, 1] + y[, 2]
# Zero alpha with warning
RegSDCadd(y, c(0.1, 0.2, 0.3), x)
```
RegSDCcomp

Description

Implementation of equation 8 in the paper.

Usage

RegSDCcomp(y, compCorr = NA, x = NULL, doSVD = FALSE, 
makeunique = TRUE, ensureIntercept = TRUE)

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>Matrix of confidential variables</td>
</tr>
<tr>
<td>compCorr</td>
<td>Required component score correlations (possibly recycled)</td>
</tr>
<tr>
<td>x</td>
<td>Matrix of non-confidential variables</td>
</tr>
<tr>
<td>doSVD</td>
<td>SVD when TRUE and QR when FALSE</td>
</tr>
<tr>
<td>makeunique</td>
<td>Parameter to be used in GenQR</td>
</tr>
<tr>
<td>ensureIntercept</td>
<td>Whether to ensure/include a constant term. Non-NULL x is subjected to EnsureIntercept</td>
</tr>
</tbody>
</table>

Details

NA component score correlation means independent random. Input matrices are subjected to EnsureMatrix.

Value

Generated version of y

Author(s)

Øyvind Langsrud

Examples

```r
x <- matrix(1:10, 10, 1)
y <- matrix(rnorm(30) + 1:30, 10, 3)

# Same as IPSO (RegSDCipso)
RegSDCcomp(y, NA, x)

# Using QR and SVD
yQR <- RegSDCcomp(y, c(0.1, 0.2, NA), x)
ySVD <- RegSDCcomp(y, c(0.1, 0.2, NA), x, doSVD = TRUE)

# Calculation of residuals
r <- residuals(lm(y ~ x))
rQR <- residuals(lm(yQR ~ x))
rSVD <- residuals(lm(ySVD ~ x))

# Correlations for two first components as required
```
RegSDCdata

Function that returns a dataset

Description

Function that returns a dataset

Usage

RegSDCdata(dataset)

Arguments

dataset Name of data set within the RegSDC package

Details

sec7data: Data in section 7 of the paper as a data frame
sec7y: Y in section 7 of the paper as a matrix
sec7x: X in section 7 of the paper as a matrix
sec7z: Z in section 7 of the paper as a matrix
sec7xAll: Xall in section 7 of the paper as a matrix
sec7zAll: Zall in section 7 of the paper as a matrix
sec7zAllSupp: As Zall with suppressed values set to NA

Value

data frame

Author(s)

Øyvind Langsrud
RegSDChybrid

Examples

RegSDCdata("sec7data")
RegSDCdata("sec7y")
RegSDCdata("sec7x")
RegSDCdata("sec7z")
RegSDCdata("sec7xAll")
RegSDCdata("sec7zAll")
RegSDCdata("sec7zAllSupp")

RegSDChybrid

Regression-based SDC Tools - Generalized microaggregation

Description

Implementation of the methodology in section 6 in the paper

Usage

RegSDChybrid(y, clusters = NULL, xLocal = NULL, xGlobal = NULL, clusterPieces = NULL, xClusterPieces = NULL, groupedClusters = NULL, xGroupedClusters = NULL, alternative = NULL, alpha = NULL, ySim = NULL, returnParts = FALSE, epsAlpha = 1e-07, makeunique = TRUE, tolerance = sqrt(.Machine$double.eps))

Arguments

  y                Matrix of confidential variables
  clusters         Vector of cluster coding
  xLocal           Matrix of x-variables to be crossed with clusters
  xGlobal          Matrix of x-variables NOT to be crossed with clusters
  clusterPieces    Vector of coding of cluster pieces
  xClusterPieces   Matrix of x-variables to be crossed with cluster pieces
  groupedClusters  Vector of coding of grouped clusters
  xGroupedClusters Matrix of x-variables to be crossed with grouped clusters
  alternative      One of "" (default), "a", "b" or "c"
  alpha            Possible to specify parameter used internally by alternative "c"
  ySim             Possible to specify the internally simulated data manually
  returnParts      Alternative output six matrices: y1 and y2 (fitted), e3s and e4s (new residuals), e3 and e4 (original residuals)
  epsAlpha         Precision constant for alpha calculation
  makeunique       Parameter to be used in GenQR
  tolerance        Parameter to Cdiff used within the algorithm
Details

Input matrices are subjected to EnsureMatrix. Necessary constant terms (intercept) are automatically included. That is, a column of ones is not needed in the input matrices.

Value

Generated version of y

Author(s)

Øyvind Langsrud

Examples

# Generate example data for introductory examples
y <- matrix(rnorm(30) + 1:30, 10, 3)
x <- matrix(1:10, 10, 1)  # x <- 1:10 is equivalent

# Same as RegSDCipso(y)
yOut <- RegSDChybrid(y)

# With a single cluster both are same as RegSDCipso(y, x)
yOut <- RegSDChybrid(y, xLocal = x)
yOut <- RegSDChybrid(y, xGlobal = x)

# Define two clusters
clust <- rep(1:2, each = 5)

# MHa and MHB in paper
yMHa <- RegSDCipso(y, clusters = clust, xLocal = x)
yMHB <- RegSDCipso(y, clusterPieces = clust, xLocal = x)

# An extended variant of MHB as mentioned in paper paragraph below definition of MHa/MHB
yMHBExt <- RegSDCipso(y, clusterPieces = clust, xClusterPieces = x)

# Identical means within clusters
aggregate(y, list(clust = clust), mean)
aggregate(yMHa, list(clust = clust), mean)
aggregate(yMHB, list(clust = clust), mean)
aggregate(yMHBExt, list(clust = clust), mean)

# Identical global regression results
summary(lm(y[,1] ~ x))
summary(lm(yMHa[,1] ~ x))
summary(lm(yMHB[,1] ~ x))
summary(lm(yMHBExt[,1] ~ x))

# MHA: Identical local regression results
summary(lm(y[,1] ~ x, subset = clust == 1))
summary(lm(yMHa[,1] ~ x, subset = clust == 1))
# MHB: Different results
summary(lm(yMHB[, 1] ~ x, subset = clust == 1))

# MHBExt: Same estimates and different std. errors
summary(lm(yMHBExt[, 1] ~ x, subset = clust == 1))

#############################################################
# Generate example data for more advanced examples
#############################################################
x <- matrix((1:90) * (1 + runif(90)), 30, 3)
x1 <- x[, 1]
x2 <- x[, 2]
x3 <- x[, 3]
y <- matrix(rnorm(90), 30, 3) + x
clust <- paste("c", rep(1:3, each = 10), sep = "")

######### Run main algorithm
z0 <- RegSDChybrid(y, clusters = clust, xLocal = x3, xGlobal = cbind(x1, x2))

# Corresponding models by lm
lmy <- lm(y ~ clust + x1 + x2 + x3:clust)
lm0 <- lm(z0 ~ clust + x1 + x2 + x3:clust)

# Preserved regression coef (x3 within clusters)
coef(lmy) - coef(lm0)

# Preservation of x3 coef locally can also be seen by local regression
coef(lm(y ~ x3, subset = clust == "c2")) - coef(lm(z0 ~ x3, subset = clust == "c2"))

# Covariance matrix preserved
cov(resid(lmy)) - cov(resid(lm0))

# But not preserved within clusters
cov(resid(lmy)[clust == "c2", ]) - cov(resid(lm0)[clust == "c2", ])

######### Modification (a)
z0 <- RegSDChybrid(y, clusters = clust, xLocal = x3, xGlobal = cbind(x1, x2), alternative = "a")
lma <- lm(z0 ~ clust + x1 + x2 + x3:clust)

# Now covariance matrices preserved within clusters
cov(resid(lmy)[clust == "c2", ]) - cov(resid(lma)[clust == "c2", ])

# If we estimate coef for x1 and x2 within clusters,
# they become identical and identical to global estimates
coef(lma)
coef(lm(z0 ~ clust + x1:clust + x2:clust + x3:clust))

######### Modification (c) with automatic calculation of alpha
# The result depends on the randomly generated data
# When the result is that alpha=1, modification (b) is equivalent
z0 <- RegSDChybrid(y, clusters = clust, xLocal = x3, xGlobal = cbind(x1, x2), alternative = "c")
lmc <- lm(z0 ~ clust + x1 + x2 + x3:clust)
# Preserved regression coef as above
coef(lmy) - coef(lmc)

# Again covariance matrices preserved within clusters
cov(resid(lmy)[clust == "c2", ]) - cov(resid(lmc)[clust == "c2", ])

# If we estimate coef for x1 and x2 within clusters, # results are different from modification (a) above
coeff(lmc)
coef(lm(zc - clust + x1:clust + x2:clust + x3:clust))

#############################################################
# Make groups of clusters (d) and cluster pieces (e)
#############################################################
clustGr <- paste("gr", ceiling(rep(1:3, each = 10)/2 + 0.1), sep = "")
clustP <- c("a", "a", rep("b", 28))

########## Modifications (c), (d) and (e)
zGrP <- RegSDChybrid(y, clusters = clust, clusterPieces = clustP, groupedClusters = clustGr,
xLocal = x3, xGroupedClusters = x2, xGlobal = x1, alternative = "c")

# Corresponding models by lm
lmGrP <- lm(zGrP - clust:clustP + x1 + x2:clustGr + x3:clust - 1)
lmY <- lm(y - clust:clustP + x1 + x2:clustGr + x3:clust - 1)

# Preserved regression coef
coef(lmY) - coef(lmGrP)

# Identical means within cluster pieces
aggregate(y, list(clust = clust, clustP = clustP), mean)
aggregate(zGrP, list(clust = clust, clustP = clustP), mean)

# Covariance matrix preserved
cov(resid(lmY)) - cov(resid(lmGrP))

# Covariance matrices preserved within clusters
cov(resid(lmY)[clust == "c2", ]) - cov(resid(lmGrP)[clust == "c2", ])

# Covariance matrices not preserved within cluster pieces
cov(resid(lmY)[clustP == "a", ]) - cov(resid(lmGrP)[clustP == "a", ])

---

**Description**

Implementation of equation 4 in the paper.
Usage

RegSDCipso(y, x = NULL, ensureIntercept = TRUE)

Arguments

y        Matrix of confidential variables
x        Matrix of non-confidential variables
ensureIntercept  Whether to ensure/include a constant term. Non-NULL x is subjected to EnsureIntercept

Details

Input matrices are subjected to EnsureMatrix.

Value

Generated version of y

Author(s)

Øyvind Langsrud

Examples

x <- matrix(1:5, 5, 1)
y <- matrix(rnorm(15) + 1:15, 5, 3)
ySynth <- RegSDCipso(y, x)

# Identical regression results
summary(lm(y[, 1] ~ x))
summary(lm(ySynth[, 1] ~ x))

# Identical covariance matrices
cov(y) - cov(ySynth)
cov(residuals(lm(y ~ x))) - cov(residuals(lm(ySynth ~ x)))
Arguments

- \( y \)  
  Matrix of confidential variables

- \( y_{\text{New}} \)  
  Matrix of \( y \)-data for new scores

- \( x \)  
  Matrix of non-confidential variables

- \( \text{doSVD} \)  
  SVD when TRUE and QR when FALSE

- \( \text{ensureIntercept} \)  
  Whether to ensure/include a constant term. Non-NULL \( x \) is subjected to \texttt{EnsureIntercept}

Details

\( \text{doSVD} \) has effect on decomposition of \( y \) and \( y_{\text{New}} \). Input matrices are subjected to \texttt{EnsureMatrix}.

Value

Generated version of \( y \)

Author(s)

Øyvind Langsrud

Examples

```r
x <- matrix(1:5, 5, 1)
y <- matrix(rnorm(15) + 1:15, 5, 3)

# Same as IPSO (RegSDCipso)
RegSDCnew(y, matrix(rnorm(15), 5, 3), x)

# Close to \( y \)
RegSDCnew(y, y + 0.001 * matrix(rnorm(15), 5, 3), x)
```

Description

Implementation based on equations 11, 12 and 17 in the paper.

Usage

```r
RegSDCromm(y, lambda = Inf, x = NULL, doSVD = FALSE, ensureIntercept = TRUE)
```
Arguments

- **y**: Matrix of confidential variables
- **lambda**: ROMM parameter
- **x**: Matrix of non-confidential variables
- **doSVD**: SVD when TRUE and QR when FALSE
- **ensureIntercept**: Whether to ensure/include a constant term. Non-NULL x is subjected to `EnsureIntercept`.

Details

doSVD has effect on decomposition of y. The exact behaviour of the method depends on the choice of the decomposition method because of the sequentially phenomenon mentioned in the paper. The similarity to the original data will tend to be highest for the first component. Input matrices are subjected to `EnsureMatrix`.

Value

Generated version of y

Author(s)

Øyvind Langsrud

Examples

```r
x <- matrix(1:5, 5, 1)
y <- matrix(rnorm(15) + 1:15, 5, 3)

# Same as IPSO (RegSDCipso)
RegSDCromm(y, Inf, x)

# Close to IPSO
RegSDCromm(y, 100, x)

# Close to y
RegSDCromm(y, 0.001, x)
```

Description

Assume that frequencies to be published, z, can be computed from inner frequencies, y, via \( z = t(x) \times y \), where x is a dummy matrix. Assuming correct suppression, this function will generate safe inner cell frequencies as decimal numbers.
Usage

SuppressDec(x, z = NULL, y = NULL, suppressed = NULL, digits = 9,
    nRep = 1, yDeduct = NULL, resScale = NULL, rmse = NULL)

Arguments

x Dummy matrix where the dimensions matches z and/or y input. Sparse matrix
    (Matrix package) is possible.

z Frequencies to be published. All, only the safe ones or with suppressed as NA.

y Inner cell frequencies.

suppressed Logical vector defining the suppressed elements of z.

digits Output close to whole numbers will be rounded using digits as input to RoundWhole.

nRep Integer, when >1, several y’s will be generated. Extra columns in output.

yDeduct Values to be subtracted from y and added back after the calculations. Can be
    used to perform the modulo method described in the paper (see examples).

resScale Residuals will be scaled by resScale.

rmse Desired root mean square error (residual standard error). Will be used when
    resScale is NULL or cannot be used.

Details

This function makes use of ReduceX and RegSDCipso.

Value

The inner cell frequencies as decimal numbers

Note

Capital letters, X, Y and Z, are used in the paper.

Author(s)

Øyvind Langsrud

Examples

# Same data as in the paper
z <- RegSDCdata("sec7z")
x <- RegSDCdata("sec7x")
y <- RegSDCdata("sec7y") # Now z is t(x) %*% y
zAll <- RegSDCdata("sec7zAll")
zAllSupp <- RegSDCdata("sec7zAllSupp")
xAll <- RegSDCdata("sec7xAll")

# When no suppression, output is identical to y
SuppressDec(xAll, zAll, y)
SuppressDec(xAll, zAll) # y can be seen in z
# Similar to Y* in paper (but other random values)
SuppressDec(x, z, y)

# Residual standard error forced to be 1
SuppressDec(x, z, y, rmse = 1)

# Seven ways of obtaining the same output
SuppressDec(x, z, rmse = 1)  # slower, y must be estimated
SuppressDec(x, y = y, rmse = 1)
SuppressDec(xAll, zAllSupp, y, rmse = 1)
SuppressDec(xAll, zAllSupp, rmse = 1)  # slower, y must be estimated
SuppressDec(xAll, zAll, y, is.na(zAllSupp), rmse = 1)
SuppressDec(xAll, zAll, suppressed = is.na(zAllSupp), rmse = 1)  # y seen in z
SuppressDec(xAll, y = y, suppressed = is.na(zAllSupp), rmse = 1)

# YhatMod4 and YhatMod10 in Table 2 in paper
SuppressDec(xAll, zAllSupp, y, yDeduct = 4 * (y%/%4), resScale = 0)
SuppressDec(xAll, zAllSupp, y, yDeduct = 10 * (y%/%10), rmse = 0)

# As data in Table 3 in paper (but other random values)
SuppressDec(xAll, zAllSupp, y, yDeduct = 10 * (y%/%10), resScale = 0.1)

# rmse instead of resScale and 5 draws
SuppressDec(xAll, zAllSupp, y, yDeduct = 10 * (y%/%10), rmse = 1, nRep = 5)

---

Z2Yhat

** Suppressed tabular data: Yhat from X and Z **

### Description
Implementation of equation 21 in the paper.

### Usage

```r
Z2Yhat(z, x, digits = 9)
```

### Arguments

- `z`  
  Z as a matrix

- `x`  
  X as a matrix

- `digits`  
  When non-NULL, output values close to whole numbers will be rounded using digits as input to `RoundWhole`.

### Details
Generalized inverse is computed by `ginv`. In practise, the computations can be speeded up using reduced versions of X and Z. See `ReduceX`. 
Value
Yhat as a matrix

Author(s)
Øyvind Langsrud

See Also
IpsoExtra

Examples

```r
# Same data as in the paper
z <- RegSDCdata("sec7z")
x <- RegSDCdata("sec7x")
Z2Yhat(z, x)

# With y known, yHat can be computed in other ways
y <- RegSDCdata("sec7y")  # Now z is t(x) %*% y
fitted(lm(y ~ x - 1))
IpsoExtra(y, x, FALSE, resScale = 0)
```
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