

Package ‘antitrust’

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Type Package

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Suggests ggplot2, shiny, rhandsontable

Description

A collection of tools for antitrust practitioners, including the ability to calibrate different consumer demand systems and simulate the effects of mergers under different competitive regimes.

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logitNests.R logitNestsALM.R logitCap.R ces.R cesNests.R aids.R
pcaids.R pcaidsNests.R cmcr.R upp.R hhi.R sim.R auction2ndcap.R
auction2ndlogit.R Cournot.R Stackelberg.R auction2ndlogitALM.R
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antitrust-package *Tools for Antitrust Practitioners*

Description

A collection of tools for antitrust practitioners, including the ability to calibrate different consumer demand systems and simulate the effects of mergers under different competitive regimes.

Details

The DESCRIPTION file:

Package: antitrust
 Type: Package
 Title: Tools for Antitrust Practitioners
 Version: 0.99.10
 Date: 2018-06-09
 Author: Charles Taragin and Michael Sandfort
 Maintainer: Charles Taragin <charles.taragin@usdoj.gov>
 Imports: methods, MASS, evd, BB, numDeriv
 Suggests: ggplot2, shiny, rhandsontable
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 Collate: Antitrust.R Bertrand.R logit.R linear.R loglin.R logitALM.R logitNests.R logitNestsALM.R logitCap.R ces.R

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Auction2ndLogit-class	Class "Auction2ndLogit"
Auction2ndLogitALM-class	Class "Auction2ndLogitALM"
Bertrand	Bertrand Calibration and Merger Simulation With Logit, CES and AIDS Demand
Bertrand-class	Class "Bertrand"
CES-class	Class "CES"
CESALM-class	Class "CESALM"
CESNests-class	Class "CESNests"
CV-methods	Methods For Calculating Compensating Variation (CV)
Cournot	Multi-product Cournot/Stackelberg Calibration and Merger Simulation With Linear or Log-Linear Demand
Cournot-class	Class "Cournot"
HHI	Herfindahl-Hirschman Index
HypoMonTest	Methods For Implementing The Hypothetical Monopolist Test
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LogLin-class	Class "LogLin"
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LogitNests-class	Class "LogitNests"
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PCAIDSNests-class	Class "PCAIDSNests"
Stackelberg-class	Class "Stackelberg"

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antitrust_shiny	A Shiny Interface to the Antitrust Package
auction2nd.cap	(Capacity Constrained) 2nd Price Auction Model
auction2nd.logit	2nd Score Procurement Auction Model
calcProducerSurplusGrimTrigger,Bertrand-method	Methods For Evaluating Collusion
ces	(Nested) Constant Elasticity of Substitution Demand Calibration and Merger Simulation
cmcr-methods	Methods For Calculating Compensating Marginal Cost Reductions and Upwards Pricing Pressure Index (Bertrand)
cmcr.bertrand	Compensating Marginal Cost Reductions and Upwards Pricing Pressure (Bertrand)
cmcr.cournot	Compensating Marginal Cost Reductions and Upwards Pricing Pressure (Cournot)
diversion-methods	Methods For Calculating Diversion
elast-methods	Methods For Calculating Own and Cross-Price Elasticities
linear	Linear and Log-Linear Demand Calibration and Merger Simulation
logit	(Nested) Logit Demand Calibration and Merger Simulation
other-methods	Other Useful 'Bertrand' Methods
sim	Merger Simulation With User-Supplied Demand Parameters

To get Started:

1. Collect data on product prices, shares, margins and diversions (optional).
2. Specify how firms interact strategically (e.g. Bertrand, Cournot, Auction)
3. If you have data on many/all products in the market consider calibrating a demand system and simulating a merger with either a [bertrand.alm](#), [cournot](#), or [auction2nd.logit](#).
4. If you only have data on the merging parties' products, consider using [cmcr.bertrand](#) or [cmcr.cournot](#) to uncover the marginal cost reductions needed to offset a post-merger increase.

Disclaimer

The views expressed herein are entirely those of the authors and should not be purported to reflect those of the U.S. Department of Justice. The antitrust package has been released into the public domain without warranty of any kind, expressed or implied. Address: Economic Analysis Group, Antitrust Division, U.S. Department of Justice, 450 5th St. NW, Washington DC 20530. E-mail: charles.taragin@usdoj.gov and michael.sandfort@usdoj.gov.

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aids *(Nested) AIDS Calibration and Merger Simulation*

Description

Calibrates consumer demand using (nested) AIDS and then simulates the price effect of a merger between two firms under the assumption that all firms in the market are playing a differentiated products Bertrand game.

Usage

```
aids(shares,margins,prices,diversions,
      ownerPre,ownerPost,
      mktElast = NA_real_,
      insideSize = NA_real_,
      mcDelta=rep(0, length(shares)),
      subset=rep(TRUE, length(shares)),
      parmStart= rep(NA_real_,2),
      priceStart=runif(length(shares)),
      isMax=FALSE,
      control.slopes,
      control.equ,
      labels=paste("Prod",1:length(shares),sep=""),
      ...)
```

```
pcaids(shares,knownElast,mktElast=-1,
        prices,diversions,
        ownerPre,ownerPost,
        knownElastIndex=1,
        insideSize = NA_real_,
        mcDelta=rep(0, length(shares)),
        subset=rep(TRUE, length(shares)),
        priceStart=runif(length(shares)),
        isMax=FALSE,
        control.slopes,
        control.equ,
        labels=paste("Prod",1:length(shares),sep=""),
        ...)
```

```
pcaids.nests(shares,margins,knownElast,mktElast=-1,
              prices,ownerPre,ownerPost,
              nests=rep(1,length(shares)),
              knownElastIndex=1,
              insideSize = NA_real_,
              mcDelta=rep(0, length(shares)),
```

```

subset=rep(TRUE, length(shares)),
priceStart=runif(length(shares)),
isMax=FALSE,
nestsParmStart,
control.slopes,
control.equ,
labels=paste("Prod",1:length(shares),sep=""),
...)

```

Arguments

	Let k denote the number of products produced by all firms.
shares	A length k vector of product revenue shares. All shares must be between 0 and 1.
margins	A length k vector of product margins. All margins must be either be between 0 and 1, or NA.
prices	A length k vector product prices. Default is missing, in which case demand intercepts are not calibrated.
knownElast	A negative number equal to the pre-merger own-price elasticity for any of the k products.
mktElast	A negative number equal to the industry pre-merger price elasticity. Default is NA for aids and -1 for pcaids .
diversions	A $k \times k$ matrix of diversion ratios with diagonal elements equal to -1. Default is missing, in which case diversion according to revenue share is assumed.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product before the merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a $k \times k$ matrix of post-merger ownership shares.
knownElastIndex	An integer equal to the position of the 'knownElast' product in the 'shares' vector. Default is 1, which assumes that the own-price elasticity of the first product is known.
insideSize	Total expenditure (revenues) on products included in the simulation.
nests	A length k vector identifying which nest a product belongs to. Default is that all products belong to a single nest.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
parmStart	aids only. A vector of length 2 who elements equal to an initial guess for "known" element of the diagonal of the demand matrix and the market elasticity.

<code>priceStart</code>	A vector of length k whose elements equal to an initial guess of the proportional change in price caused by the merger. The default is to draw k random elements from a $[0,1]$ uniform distribution.
<code>isMax</code>	If TRUE, checks to see whether computed price equilibrium locally maximizes firm profits and returns a warning if not. Default is FALSE.
<code>nestsParmStart</code>	A vector of starting values used to solve for price coefficient and nest parameters. If missing then the random draws with the appropriate restrictions are employed.
<code>control.slopes</code>	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
<code>control.equ</code>	A list of <code>BBsolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
<code>labels</code>	A k -length vector of labels.
<code>...</code>	Additional options to feed to the <code>BBsolve</code> optimizer used to solve for equilibrium prices.

Details

Using product market revenue shares and all of the product product margins from at least two firms, `aids` is able to recover the slopes in a proportionally calibrated Almost Ideal Demand System (AIDS) without income effects. `aids` then uses these slopes to simulate the price effects of a merger between two firms under the assumption that all firms in the market are playing a differentiated Bertrand pricing game.

If prices are also supplied, `aids` is able to recover the intercepts from the AIDS demand system. Intercepts are helpful because they can be used to simulate pre- and post-merger price *levels* as well as price *changes*. What's more, the intercepts are necessary in order to calculate compensating variation.

`aids` assumes that diversion between the products in the market occurs according to revenue share. This assumption may be relaxed by setting 'diversions' equal to a $k \times k$ matrix of diversion ratios. The diagonal of this matrix must equal -1, the off-diagonal elements must be between 0 and 1, and the rows must sum to 1.

`pcaids` is almost identical to `aids`, but instead of assuming that at least two margins are known, `pcaids` assumes that the own-price elasticity of any single product, and the industry-wide own-price elasticity, are known. Demand intercepts cannot be recovered using `pcaids`.

`pcaids.nests` extends `pcaids` by allowing products to be grouped into nests. Although products within the same nest still have the independence of irrelevant alternatives (IIA) property, products in different nests do not. Note that the 'diversions' argument is absent from `pcaids.nests`.

`pcaids.nests` assumes that the share diversion between nests is symmetric (i.e. for 2 nests A and B, the diversion from A to B is the same as B to A). Therefore, if there are w nests, $2 \leq w \leq k$, then the model must estimate $w(w-1)/2$ distinct nesting parameters. To accomplish this, `pcaids.nests` uses margin information to produce estimates of the nesting parameters. It is important to note that the number of supplied margins must be at least as great as the number of nesting parameters in order for PCAIDS to work.

The nesting parameters are constrained to be between 0 and 1. Therefore, one way to test the validity of the nesting structure is to check whether the nesting parameters are between 0 and 1. The value

of the nesting parameters may be obtained from calling either the ‘summary’ or ‘getNestsParms’ functions.

Value

aids returns an instance of class `AIDS`, a child class of `Linear`. pcaids returns an instance of class `PCAIDS`, while pcaids.nests returns an instance of `PCAIDSNests`. Both are children of the `AIDS` class.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

Epstein, Roy and Rubinfeld, Daniel (2004). “Merger Simulation with Brand-Level Margin Data: Extending PCAIDS with Nests.” *The B.E. Journal of Economic Analysis & Policy*, **advances.4**(1), pp. 2.

Epstein, Roy and Rubinfeld, Daniel (2004). “Effects of Mergers Involving Differentiated Products.”

See Also

`linear` for a demand system based on quantities rather than revenue shares.

Examples

```
## Simulate a merger between two single-product firms A and B in a
## three-firm market (A, B, C). This example assumes that the merger is between
## the firms A and B and that A's own-price elasticity is
## known.
## Source: Epstein and Rubinfeld (2004), pg 9, Table 2.

prices <- c(2.9,3.4,2.2) ## optional for aids, unnecessary for pcaids
shares <- c(.2,.3,.5)

## The following are used by aids but not pcaids
## only two of the margins are required to calibrate the demand parameters
margins <- c(0.33, 0.36, 0.44)

## The following are used by pcaids, but not aids
knownElast<- -3
mktElast <- -1

## Define ownership using a vector of firm identities
ownerPre <- c("A","B","C")
ownerPost <- c("A","A","C")
```



```

## Alternatively, ownership could be defined using matrices
#ownerPre=diag(1,length(shares))
#ownerPost=ownerPre
#ownerPost[1,2] <- ownerPost[2,1] <- 1

## AIDS: the following assumes both prices and margins are known.
##      Prices are not needed to estimate price changes

result.aids <- aids(shares,margins,prices,ownerPre=ownerPre,ownerPost=ownerPost,labels=ownerPre)

print(result.aids)          # return predicted price change
summary(result.aids)       # summarize merger simulation

elast(result.aids,TRUE)    # returns premerger elasticities
elast(result.aids,FALSE)  # returns postmerger elasticities

diversion(result.aids,TRUE) # return premerger diversion ratios
diversion(result.aids,FALSE) # return postmerger diversion ratios

cmcr(result.aids)         #calculate compensating marginal cost reduction
upp(result.aids)          #calculate Upwards Pricing Pressure Index

## Implement the Hypothetical Monopolist Test
## for products A and B using a 5% SSNIP

HypoMonTest(result.aids,prodIndex=1:2)

CV(result.aids)           #calculate compensating variation as a percent of
                          #total expenditure
                          #CV can only be calculated if prices are supplied

## Get a detailed description of the 'AIDS' class slots
showClass("AIDS")

## Show all methods attached to the 'AIDS' Class
showMethods(classes="AIDS")

## Show which class have their own 'elast' method
showMethods("elast")

## Show the method definition for 'elast' and Class 'AIDS'
getMethod("elast","AIDS")

```

```

## PCAIDS: the following assumes that only one product's elasticity is
##      known as well as the market elasticity.

result.pcaids <- pcaids(shares,knownElast,mktElast,
                      ownerPre=ownerPre,ownerPost=ownerPost,
                      labels=ownerPre)

print(result.pcaids)          # return predicted price change
summary(result.pcaids)       # summarize merger simulation

elast(result.pcaids,TRUE)    # returns premerger elasticities
elast(result.pcaids,FALSE)  # returns postmerger elasticities

diversion(result.pcaids,TRUE) # return premerger diversion ratios
diversion(result.pcaids,FALSE) # return postmerger diversion ratios

cmcr(result.pcaids)          #calculate compensating marginal cost reduction

## Implement the Hypothetical Monopolist Test
## for products A and B using a 5% SSNIP

HypoMonTest(result.pcaids,prodIndex=1:2)

## Nested PCAIDS: in addition to the PCAIDS information requirements,
##      users must supply the nesting structure as well as margin information.

nests <- c('H','L','L') # product A assigned to nest H, products B and C assigned to nest L

result.pcaids.nests <- pcaids.nests(shares,knownElast,mktElast,margins=margins,
                                   nests=nests,ownerPre=ownerPre,
                                   ownerPost=ownerPost,labels=ownerPre)

```

AIDS-class

Class "AIDS"

Description

The "AIDS" class contains all the information needed to calibrate a AIDS demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function [aids](#).

Slots

Let k denote the number of products produced by all firms.

priceStart: A length- k vector of starting prices for the non-linear solver

insideSize: A positive number equal to total pre-merger revenues for all products included in the simulation.

mktElast: A negative number equal to the industry pre-merger price elasticity.

parmStart: A length 2 vector whose elements equal to an initial of a single diagonal element of the matrix of slope coefficients, as well as the market elasticity.

priceDelta: A length k vector containing the simulated price effects from the merger.

Extends

Class [Linear](#), directly. Class [Bertrand](#), by class “Linear”, distance 2.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

calcMargins signature(object, preMerger=TRUE) Calculates pre-merger or post-merger equilibrium margins.

calcPriceDelta signature(object, isMax=FALSE, ...) Computes the proportional change in each products’ price from the merger under the assumptions that consumer demand is AIDS and firms play a differentiated product Bertrand Nash pricing game. When isMax equals TRUE, a check is run to determine if the calculated equilibrium price vector locally maximizes profits. ‘...’ may be used to change the default values of [BBsolve](#), the non-linear equation solver.

calcPrices signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium prices under the assumptions that consumer demand is AIDS and firms play a differentiated product Bertrand Nash pricing game. return a vector of length- k vector of NAs if user did not supply prices.

calcPriceDeltaHypoMon signature(object, prodIndex, ...) Calculates the price changes that a Hypothetical Monopolist would impose on its products relative to pre-merger prices.

calcShares signature(object, preMerger = TRUE) Computes either pre-merger or post-merger equilibrium quantity shares under the assumptions that consumer demand is AIDS and firms play a differentiated product Bertrand Nash pricing game.

calcSlopes signature(object) Uncover AIDS demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

cmcr signature(object) Calculates compensated marginal cost reduction, the percentage decrease in the marginal costs of the merging parties’ products needed to offset a post-merger price increase.

CV signature(object) Calculate the amount of money a representative consumer would need to be paid to be just as well off as they were before the merger. Requires a length-k vector of pre-merger prices.

diversion signature(object, preMerger= TRUE) Computes a k x k matrix of diversion ratios.

elast signature(object , preMerger = TRUE) Computes a k x k matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("AIDS")           # get a detailed description of the class
showMethods(classes="AIDS") # show all methods defined for the class
```

Antitrust-class	<i>Class "Antitrust"</i>
-----------------	--------------------------

Description

The “Antitrust” class is a building block used to create other classes in this package. As such, it is most likely to be useful for developers who wish to code their own calibration/simulation routines.

Objects from the Class

Objects can be created by calls of the form `new("Antitrust", ...)`.

Slots

Let k denote the number of products produced by all firms.

pricePre: A length k vector of simulated pre-merger prices.

pricePost: A length k vector of simulated post-merger prices.

ownerPre: A $k \times k$ matrix of pre-merger ownership shares.

ownerPost: A $k \times k$ matrix of post-merger ownership shares.

labels: A length k vector of labels.

control.slopes: A list of [optim](#) control parameters passed to the calibration routine optimizer (typically the `calcSlopes` method).

control.equ: A list of [BBSolve](#) control parameters passed to the non-linear equation solver (typically the `calcPrices` method).

Methods

Many of the methods described below contain a ‘preMerger’ argument. The ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger values, while FALSE invokes the method using the post-merger ownership structure.

`calcPriceDelta` signature(object) Calculates the proportional change in product prices from a merger.

`ownerToMatrix` signature(object, preMerger = TRUE) Converts an ownership vector (or factor) to a k x k matrix of 1s and 0s.

`ownerToVec` signature(object, preMerger = TRUE) Converts a k x k ownership matrix to a length-k vector whose values identify an owner.

`show` signature(object) Displays the percentage change in prices due to the merger.

The “matrixOrList”, “matrixOrVector” and “characterOrList” Classes

The “matrixOrList”, “matrixOrVector” and “characterOrList” classes are virtual classes used for validity checking in the ‘ownerPre’ and ‘ownerPost’ slots of “Antitrust” and the ‘slopes’ slot in “Bertrand”.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Antitrust")           # get a detailed description of the class
showMethods(classes="Antitrust") # show all methods defined for the class
```

antitrust_shiny *A Shiny Interface to the Antitrust Package*

Description

A Shiny Interface to the Antitrust Package

Usage

```
antitrust_shiny()
```

Details

`antitrust_shiny` launches a shiny interface for the antitrust package. The shiny interface provides users with the ability to calibrate and simulate horizontal mergers using many of the supply and demand models included in the antitrust package.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
## launch shiny interface to antitrust package
## Not run:
antitrust_shiny()

## End(Not run)
```

auction2nd.cap

(Capacity Constrained) 2nd Price Auction Model

Description

Calibrates the parameters of bidder cost distributions and then simulates the price effect of a merger between two firms under the assumption that firms are competing in a (Capacity Constrained) 2nd price auction.

Usage

```
auction2nd.cap(capacities, margins, prices, reserve=NA, shareInside=NA,
  sellerCostCDF=c("punif", "pexp", "pweibull", "pgumbel", "pfrechet"),
  ownerPre, ownerPost,
  mcDelta=rep(0, length(capacities)),
  constrain.reserve=TRUE, parmsStart,
  control.slopes,
  labels=as.character(ownerPre), ...
  )
```

Arguments

	Let k denote the number of firms bidding in the auction.
capacities	A length k vector of firm capacities OR capacity shares.
margins	A length k vector of product margins. All margins must be either be between 0 and 1, or NA.
prices	A length k vector product prices. Prices may be NA.
reserve	A length 1 vector equal to the buyer's reserve price. Default is NA .
shareInside	A length 1 vector equal to the probability that the buyer does not select the outside option. Default is NA.

sellerCostCDF	A length l character vector indicating which probability distribution will be used to model bidder cost draws. Possible options are "punif", "pexp", "pweibull", "pgumbel", "pfrechet". Default is "punif".
ownerPre	A length k factor whose values indicate which firms are present in the market pre-merger.
ownerPost	A length k factor whose values indicate which firms are present in the market post-merger.
mcDelta	A vector of length k where each element equals the proportional change in a firm's capacity due to the merger. Default is 0, which assumes that the merger does not affect any products' capacity.
constrain.reserve	If TRUE, the buyer's post-merger optimal reserve price is assumed to equal the buyer's pre-merger optimal reserve price. If FALSE, the buyer re-calculates her optimal reserve price post-merger.
parmsStart	A vector of starting values for calibrated parameters. See below for more details
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
labels	A k-length vector of labels. Default is "Firm", where '#' is a number between 1 and the length of 'capacities'.
...	Additional options to feed to either <code>optim</code> or <code>constrOptim</code> .

Details

`auction2nd.cap` examines how a merger affects equilibrium bidding behavior when a single buyer is running a 2nd price procurement auction with bidders whose marginal cost of supplying a homogenous product is private information. This version of the model assumes that bidders are differentiated by their capacities in the sense that firms with greater capacity are more likely to have lower costs than firms with smaller capacities.

Using firm prices, shares, and margins, as well as information on the auction reserve price as well as the proportion of buyers who choose not to purchase from any bidder, `auction2nd.cap` calibrates the parameters of the common distribution from which bidder's costs are drawn (and, if not supplied, the implied reserve price) and then uses these calibrated parameters to calibrate the value to the buyer of selecting the outside option. Once these parameters have been calibrated, `auction2nd.cap` computes the buyer's optimal pre-merger reservation price, and if 'constrain.reserve' is FALSE, computes the buyer's optimal post-merger reservation price (setting 'constrain.reserve' to TRUE sets the buyer's post-merger optimal reserve equal to the buyer's pre-merger optimal reserve). The pre- and post-merger expected price, conditional on a particular bidder winning, are then calculated.

Currently, the common distribution from which costs may be drawn is restricted to be either: Uniform ("punif"), Exponential ("pexp"), Weibull ("pweibull"), Gumbel ("pgumbel"), or Frechet ("pfrechet"). Note that the Exponential is a single parameter distribution, the Uniform and Weibull are two parameter distributions, and the Gumbel and Frechet are 3 parameter distributions. Accordingly, sufficient price, margin, reserve, and outside share information must be supplied in order to calibrate the parameters of the specified distribution. `auction2nd.cap` returns an error if insufficient information is supplied.

Value

auction2nd.cap returns an instance of class [Auction2ndCap](#).

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>, with code contributed by Michael Sandfort and Nathan Miller

References

Keith Waehrer and Perry, Martin (2003). "The Effects of Mergers in Open Auction Markets", *Rand Journal of Economics*, **34**(2), pp. 287-304.

Examples

```
##Suppose there are 3 firms (A,B,C) participating in a procurement auction with
## an unknown reservation price and that firm A acquires firm B.

caps <- c(0.65,0.30,0.05)          # total capacity normalized to 1 in this example
inShare <- .67                    # probability that buyer does not select
                                  # any bidder
prices <- c(3.89, 3.79, 3.74)     # average price charged by each firm
margins <- c(.228, .209, 0.197)  # average margin earned by each firm
ownerPre <- ownerPost <-c("A","B","C")
ownerPost[ownerPost=="B"] <- "A"

##assume costs are uniformly distributed with unknown bounds
result.unif = auction2nd.cap(
  capacities=caps,
  margins=margins,prices=prices,reserve=NA,
  shareInside=inShare,
  sellerCostCDF="punif",
  ownerPre=ownerPre,ownerPost=ownerPost,
  labels=ownerPre
)

print(result.unif)
summary(result.unif)

## Get a detailed description of the 'Auction2ndCap' class slots
showClass("Auction2ndCap")

## Show all methods attached to the 'Auction2ndCap' Class
showMethods(classes="Auction2ndCap")
```

auction2nd.logit *2nd Score Procurement Auction Model*

Description

Calibrates consumer demand using Logit and then simulates the price effect of a merger between two firms under the assumption that all firms in the market are playing a differentiated products 2nd score auction game.

Usage

```
auction2nd.logit(prices,shares,margins,
                 ownerPre,ownerPost,
                 normIndex=ifelse(isTRUE(all.equal(sum(shares),
                 1, check.names=FALSE)), 1, NA),
                 mcDelta=rep(0,length(prices)),
                 subset=rep(TRUE,length(prices)),
                 mcDeltaOutside=0,
                 control.slopes,
                 labels=paste("Prod",1:length(prices),sep=""))
)
```

```
auction2nd.logit.alm(prices,shares,margins,
                    ownerPre,ownerPost,
                    mktElast = NA_real_,
                    insideSize = NA_real_,
                    mcDelta=rep(0,length(prices)),
                    subset=rep(TRUE,length(prices)),
                    mcDeltaOutside=0,
                    parmsStart,
                    control.slopes,
                    control.equ,
                    labels=paste("Prod",1:length(prices),sep=""))
)
```

Arguments

Let k denote the number of products produced by all firms playing the auction game.

prices A length k vector of product prices.

shares A length k vector of product (quantity) shares. Values must be between 0 and 1.

margins A length k vector of product margins (in levels, not percents), some of which may equal NA.

normIndex	An integer equalling the index (position) of the inside product whose mean valuation will be normalized to 1. Default is 1, unless ‘shares’ sum to less than 1, in which case the default is NA and an outside good is assumed to exist.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product pre-merger OR a k x k matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a k x k matrix of post-merger ownership shares.
mktElast	a negative value indicating market elasticity. Default is NA.
insideSize	An integer equal to total pre-merger units sold. If shares sum to one, this also equals the size of the market.
mcDelta	A vector of length k where each element equals the (level) change in a product’s marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products’ marginal cost.
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
mcDeltaOutside	A length 1 vector indicating the change in the marginal cost of the outside good. Default is 0.
parmsStart	A length 2 vector of starting values used to solve for price coefficient and the share of the outside good. The first element should always be the price coefficient and the second should be the outside good.
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
control.equ	A list of <code>BBsolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
labels	A k-length vector of labels. Default is "Prod#", where ‘#’ is a number between 1 and the length of ‘prices’.

Details

Using product prices, quantity shares and all of the product margins from at least one firm, `auction2nd.logit` is able to recover the price coefficient and product mean valuations in a Logit demand model. `auction2nd.logit` then uses these calibrated parameters to simulate a merger between two firms, under the assumption that firms are participating in a 2nd score procurement auction.

`auction2nd.logit.alm` is identical to `auction2nd.logit` except that it assumes that an outside product exists and uses additional margin information to estimate the share of the outside good.

Value

`auction2nd.logit` returns an instance of `Auction2ndLogit`, a child class of `Logit`.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

Miller, Nathan (2014). “Modeling the effects of mergers in procurement” *International Journal of Industrial Organization* , 37, pp. 201-208.

See Also

[logit](#)

Examples

```
## Calibration and simulation results from a merger between firms 2 and 3
## of a 4-firm market
## Source: Miller 2014 backup materials http://www.nathanhmler.org/research

share = c(0.29,0.40,0.28,0.03)

price = c(35.53, 154, 84.08, 53.16)
cost = c(NA, 101, NA, NA)

ownerPre <- ownerPost <- diag(length(share))

#Suppose products 2 and 3 merge
ownerPost[2,3] <- ownerPost[3,2] <- 1

margin = price - cost

result <- auction2nd.logit(price,share,margin,
ownerPre=ownerPre,ownerPost=ownerPost,normIndex=2)

print(result)
summary(result,revenue=FALSE)

##re-run without any price information except Firm 2

price <- rep(NA_real_, length(price))

result.noprice <- auction2nd.logit(price,share,margin,
ownerPre=ownerPre,ownerPost=ownerPost,normIndex=2)

print(result.noprice)
summary(result.noprice,revenue=FALSE)

## Get a detailed description of the 'Auction2ndLogit' class slots
showClass("Auction2ndLogit")

## Show all methods attached to the 'Auction2ndLogit' Class
showMethods(classes="Auction2ndLogit")
```

Auction2ndCap-class *Class "Auction2ndCap"*

Description

The "Auction2ndCap" class contains all the information needed to calibrate a 2nd price auction with capacity constraints

Objects from the Class

Objects can be created by using the constructor function [auction2nd.cap](#).

Slots

Let k denote the number of firms.

capacities: A length k vector of firm capacities.

margins: A length k vector of product margins, some of which may equal NA.

prices: A length k vector of product prices.

reserve: A length 1 vector equal to observed buyer's reserve price. May equal NA.

shareInside: A length 1 vector equal to the probability that a buyer does not select the outside option. May equal NA.

sellerCostCDF: A length 1 character vector equal to the name of the function that calculates the Cumulative Distribution (CDF) of SellerCosts.

sellerCostCDFLowerTail: A length 1 logical vector equal to TRUE if the probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.

sellerCostPDF: A function returning the Probability Density of Seller Costs.

sellerCostBounds: The bounds on the seller's CDF.

sellerCostParms: The parameters of the seller's CDF.

buyerValuation: Buyer's self-supply cost.

reservePre: Buyer's optimal pre-merger reservation price.

reservePost: Buyer's optimal post-merger reservation price.

mcDelta: A length k vector equal to the proportional change in a firm's capacity following the merger.

parmsStart: A vector of starting values.

Extends

Class [Antitrust](#), directly.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure. Likewise, for all methods containing the ‘exAnte’ argument, if ‘exAnte’ equals TRUE then the *ex ante* expected result for each firm is produced, while FALSE produces the expected result conditional on each firm winning the auction.

`calcBuyerExpectedCost` signature(object = Auction2ndCap, preMerger = TRUE) Computes the expected amount that the buyer will pay to the auction winner.

`calcBuyerValuation` signature(object = Auction2ndCap) Computes the value to the buyer of the outside option.

`calcExpectedLowestCost` signature(object = Auction2ndCap, preMerger = TRUE) Computes the expected lowest cost of the winning bid.

`calcExpectedPrice` signature(object = Auction2ndCap, preMerger = TRUE) Computes the expected price paid by the buyer.

`calcProducerSurplus` signature(object = Auction2ndCap, preMerger = TRUE, exAnte=TRUE) Computes the expected profits of each supplier

`calcMC` signature(object = Auction2ndCap, t, preMerger = TRUE, exAnte=TRUE) Computes the expected marginal cost of each supplier for a given capacity profile ‘t’. Default is ‘pre-Merger’ capacities.

`calcMargins` signature(object = Auction2ndCap, preMerger = TRUE, exAnte=TRUE) Compute each firm’s expected margin.

`calcOptimalReserve` signature(object = Auction2ndCap, preMerger = TRUE, lower, upper) Computes the bidder’s optimal reserve price.

`calcPrices` signature(object = Auction2ndCap, preMerger = TRUE, exAnte=TRUE) Computes the expected price that the buyer pays, conditional on the buyer purchasing from a particular firm.

`calcSellerCostParms` signature(object = Auction2ndCap) Calibrate the parameters of the Seller Cost CDF, as well as the reserve price, if not supplied.

`calcShares` signature(object = Auction2ndCap, preMerger = TRUE, exAnte=TRUE) Compute the probability that a firm wins.

`cdfG` signature(object = Auction2ndCap, c, preMerger=TRUE) Calculates the probability that a cost draw less than or equal to ‘c’ is realized for each firm. If ‘c’ is not supplied, the buyer reserve and total capacity is used.

`summary` signature(object = Auction2ndCap, exAnte=FALSE, parameters=FALSE, digits=2) Summarize the results of the calibration and simulation.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Auction2ndCap")           # get a detailed description of the class
showMethods(classes="Auction2ndCap") # show all methods defined for the class
```

Auction2ndLogit-class *Class "Auction2ndLogit"*

Description

The "Auction2ndLogit" class contains all the information needed to calibrate a Logit demand system and perform a merger simulation analysis under the assumption that firms are setting offers in a 2nd-score auction.

Objects from the Class

Objects can be created by using the constructor function `auction2nd.logit`.

Extends

Class `Logit`, directly. Class `Bertrand`, by class `Logit`, distance 2. Class `Antitrust`, by class `Bertrand`, distance 3.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcSlopes signature(object)` Uncover Logit ALM demand parameters. Assumes that firms are currently at equilibrium in a 2nd-score auction.

`calcMargins signature(object)` Compute model margins.

`calcMC signature(object)` Compute constant marginal costs implied by the model.

`calcShares signature(object)` Compute logit shares using cost estimates.

`calcSlopes signature(object)` Uncover Logit ALM demand parameters. Assumes that firms are currently at equilibrium in a 2nd-score auction.

`cmcr signature(object)` Compensating marginal cost reduction is not sensible in a 2nd-score auction. Method returns error.

`upp signature(object)` upward pricing pressure is not sensible in a 2nd-score auction. Method returns error.

`CV signature(object)` Compensating variation is simply the weighted average of the price changes.

`calcPricesHypoMon signature(object)` Computes prices for a subset of firms under the control of a hypothetical monopolist playing a 2nd score auction.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Auction2ndLogit")           # get a detailed description of the class
showMethods(classes="Auction2ndLogit") # show all methods defined for the class
```

Auction2ndLogitALM-class

Class "Auction2ndLogitALM"

Description

The "Auction2ndLogitALM" class contains all the information needed to calibrate a Logit demand system with unobserved outside share and perform a merger simulation analysis under the assumption that firms are setting offers in a 2nd-score auction.

Objects from the Class

Objects can be created by using the constructor function `auction2nd.logit.alm`.

Extends

Class `Auction2ndLogit`, directly. Class `Logit`, distance 2. Class `Bertrand`, by class `Logit`, distance 3. Class `Antitrust`, by class `Bertrand`, distance 4.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcSlopes signature(object)` Uncover Logit ALM demand parameters. Assumes that firms are currently at equilibrium in a 2nd-score auction.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Auction2ndLogitALM")           # get a detailed description of the class
showMethods(classes="Auction2ndLogitALM") # show all methods defined for the class
```

Bertrand

Bertrand Calibration and Merger Simulation With Logit, CES and AIDS Demand

Description

Calibrates consumer demand using either a Logit, CES, or AIDS demand system and then simulates the prices effect of a merger between two firms under the assumption that all firms in the market are playing a Nash-Bertrand price setting game.

Usage

```

bertrand.alm(demand = c("logit", "ces", "aids"),
prices, quantities, margins,
ownerPre, ownerPost,
mktElast = NA_real_,
insideSize = ifelse(demand == "logit", sum(quantities, na.rm=TRUE),
                    sum(prices*quantities, na.rm=TRUE)),
diversions,
mcDelta=rep(0, length(prices)),
subset=rep(TRUE, length(prices)),
priceOutside=ifelse(demand=="logit", 0, 1),
priceStart = prices,
isMax=FALSE,
parmStart,
control.slopes,
control.equ,
labels=paste("Prod", 1:length(prices), sep=""),
...)

```

Arguments

	Let k denote the number of products produced by all firms.
demand	A character vector indicating which demand system to use. Currently allows logit (default), ces, or aids.
prices	A length k vector product prices. Default is missing, in which case demand intercepts are not calibrated.
quantities	A length k vector of product quantities.
margins	A length k vector of product margins. All margins must be either be between 0 and 1, or NA.
diversions	A $k \times k$ matrix of diversion ratios with diagonal elements equal to -1. Default is missing, in which case diversion according to revenue share is assumed.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product before the merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a $k \times k$ matrix of post-merger ownership shares.
mktElast	A negative number equal to the industry pre-merger price elasticity. Default is NA.
insideSize	Size of all units included in the market. For logit, this defaults to total quantity, while for aids and ces this defaults to total revenues.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.

subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
parmStart	aids only. A vector of length 2 who elements equal to an initial guess for "known" element of the diagonal of the demand matrix and the market elasticity.
priceOutside	A positive real number equal to the price of the outside good. Default either equals 1 for Logit demand or 0 for CES demand.
priceStart	A vector of length k who elements equal to an initial guess of the proportional change in price caused by the merger. For aids, the default is to draw k random elements from a [0,1] uniform distribution. For ces and logit, the default is prices.
isMax	If TRUE, checks to see whether computed price equilibrium locally maximizes firm profits and returns a warning if not. Default is FALSE.
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
control.equ	A list of <code>BBsolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
labels	A k-length vector of labels.
...	Additional options to feed to the <code>BBsolve</code> optimizer used to solve for equilibrium prices.

Details

The main purpose of this function is to provide a more convenient front-end for the `aids`, `logit.alm` and `ces` functions.

Using price, and quantity, information for all products in each market, as well as margin information for at least one products in each market, `bertrand.alm` is able to recover the slopes and intercepts of either a Logit, CES, or AIDS demand system. These parameters are then used to simulate the price effects of a merger between two firms under the assumption that the firms are playing a simultaneous price setting game.

'ownerPre' and 'ownerPost' values will typically be equal to either 0 (element [i,j] is not commonly owned) or 1 (element [i,j] is commonly owned), though these matrices may take on any value between 0 and 1 to account for partial ownership.

Value

`bertrand.alm` returns an instance of class `LogitALM`, `CESALM`, or `AIDS`, depending upon the value of the "demand" argument.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Bertrand-class	<i>Class “Bertrand”</i>
----------------	-------------------------

Description

The “Bertrand” class is a building block used to create other classes in this package. As such, it is most likely to be useful for developers who wish to code their own merger calibration/simulation routines.

Objects from the Class

Objects can be created by calls of the form `new("Bertrand", ...)`.

Slots

Let k denote the number of products produced by all firms.

shares: A length k vector containing observed output. Depending upon the model, output will be measured in units sold, quantity shares, or revenue shares.

mcDelta: A length k vector where each element equals the proportional change in a product’s marginal costs due to the merger.

slopes: A $k \times (k+1)$ matrix of linear demand intercepts and slope coefficients

subset A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded.

Extends

Class [Antitrust](#), directly.

Methods

Many of the methods described below contain a ‘preMerger’ and ‘revenue’ argument. The ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger values, while FALSE invokes the method using the post-merger ownership structure. The ‘revenue’ argument also takes on a value of TRUE or FALSE, where TRUE invokes the method using revenues, while FALSE invokes the method using quantities

calcMC signature(object, preMerger=TRUE) Calculates (constant) marginal cost for each product. For those classes that do not require prices, returns a length- k vector of NAs when prices are not supplied.

calcMargins signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium margins under the assumption that firms play a differentiated product Bertrand Nash pricing game.

cmcr signature(object) Calculates compensated marginal cost reduction, the percentage decrease in the marginal costs of the merging parties’ products needed to offset a post-merger price increase.

- HypoMonTest** signature(object,prodIndex,ssnip=.05,...) HypoMonTest implements the Hypothetical Monopolist Test for a given ‘ssnip’.
- calcPriceDeltaHypoMon** signature(object,prodIndex,...) Compute the proportional difference in product prices between the prices of products in ‘prodIndex’ (i.e. prices set by the Hypothetical Monopolist) and prices set in the pre-merger Bertrand equilibrium. ‘...’ may be used to pass arguments to the optimizer.
- diversionHypoMon** signature(object,prodIndex,...) Calculates the matrix of revenue diversions between all products included in the merger simulation, *irrespective of whether or not they are also included in ‘prodIndex’*.
- hhi** signature(object, preMerger= TRUE,revenue=FALSE) Compute either the pre-merger or post-merger Herfindahl-Hirschman Index (HHI) under the assumption that firms play a differentiated product Bertrand Nash pricing game.
- diversion** signature(object, preMerger = TRUE) Computes a k x k matrix of diversion ratios.
- summary** signature(object,revenue=TRUE,shares=TRUE,parameters=FALSE,digits=2) Summarizes the effect of the merger, including price and revenue changes. Setting ‘revenue’ equal to FALSE reports quantities rather than revenues. Setting ‘shares’ to FALSE reports quantities rather than than shares (when possible). Setting ‘parameters’ equal to TRUE reports all demand parameters. ‘digits’ controls the number of significant digits reported in output.
- plot** signature(x=object,scale=.1 Use **ggplot** to plot pre- and post-merger demand, marginal cost and equilibria. ‘scale’ controls the amount above marginal cost and below equilibrium price that is plotted.
- upp** signature(object) Calculate the Upwards Pricing Pressure (upp) index.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Bertrand")           # get a detailed description of the class
showMethods(classes="Bertrand") # show all methods defined for the class
```

ces

(Nested) Constant Elasticity of Substitution Demand Calibration and Merger Simulation

Description

Calibrates consumer demand using (Nested) Constant Elasticity of Substitution (CES) and then simulates the price effect of a merger between two firms under the assumption that all firms in the market are playing a differentiated products Bertrand pricing game.

Usage

```
ces(prices, shares, margins,
    ownerPre, ownerPost,
    normIndex=ifelse(sum(shares)<1, NA, 1),
    insideSize = NA_real_,
    mcDelta=rep(0, length(prices)),
    subset=rep(TRUE, length(prices)),
    priceOutside = 1,
    priceStart = prices,
    isMax=FALSE,
    control.slopes,
    control.equ,
    labels=paste("Prod", 1:length(prices), sep=""),
    ...
)
```

```
ces.alm(prices, shares, margins,
    ownerPre, ownerPost,
    mktElast = NA_real_,
    insideSize = NA_real_,
    mcDelta=rep(0, length(prices)),
    subset=rep(TRUE, length(prices)),
    priceOutside=1,
    priceStart = prices,
    isMax=FALSE,
    parmsStart,
    control.slopes,
    control.equ,
    labels=paste("Prod", 1:length(prices), sep=""),
    ...
)
```

```
ces.nests(prices, shares, margins,
    ownerPre, ownerPost,
    nests=rep(1, length(shares)),
    normIndex=ifelse(sum(shares)<1, NA, 1),
    insideSize = NA_real_,
    mcDelta=rep(0, length(prices)),
    subset=rep(TRUE, length(prices)),
    priceOutside = 1,
    priceStart = prices,
    isMax=FALSE,
    constraint = TRUE,
    parmsStart,
    control.slopes,
    control.equ,
    labels=paste("Prod", 1:length(prices), sep=""),
    ...
)
```

)

Arguments

	Let k denote the number of products produced by all firms playing the Bertrand pricing game.
prices	A length k vector of product prices.
shares	A length k vector of product revenue shares.
margins	A length k vector of product margins, some of which may equal NA.
nests	A length k vector identifying the nest that each product belongs to.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product pre-merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a $k \times k$ matrix of post-merger ownership shares.
mktElast	a negative value indicating market elasticity. Default is NA.
normIndex	An integer specifying the product index against which the mean values of all other products are normalized. Default is 1.
insideSize	total revenues included in the market.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
constraint	if TRUE, then the nesting parameters for all non-singleton nests are assumed equal. If FALSE, then each non-singleton nest is permitted to have its own value. Default is TRUE.
priceOutside	A length 1 vector indicating the price of the outside good. Default is 1.
priceStart	A length k vector of starting values used to solve for equilibrium price. Default is the 'prices' vector.
isMax	If TRUE, checks to see whether computed price equilibrium locally maximizes firm profits and returns a warning if not. Default is FALSE.
parmsStart	A vector of starting values used to solve for price coefficient and nest parameters. The first element should always be the price coefficient and the remaining elements should be nesting parameters. Theory requires the nesting parameters to be greater than the price coefficient. If missing then the random draws with the appropriate restrictions are employed.
labels	A k -length vector of labels. Default is "Prod#", where '#' is a number between 1 and the length of 'prices'.
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).

<code>control.equ</code>	A list of BBsolve control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
<code>...</code>	Additional options to feed to the BBsolve optimizer used to solve for equilibrium prices

Details

Using product prices, revenue shares and all of the product margins from at least one firm, `ces` is able to recover the price coefficient and product mean valuations in a Constant Elasticity of Substitution demand model. `ces` then uses these calibrated parameters to simulate the price effects of a merger between two firms under the assumption that that all firms in the market are playing a differentiated products Bertrand pricing game.

`ces.alm` is identical to `logit` except that it assumes that an outside product exists and uses additional margin information to estimate the share of the outside good.

`ces.nests` is identical to `ces` except that it includes the ‘nests’ argument which may be used to assign products to different nests. Nests are useful because they allow for richer substitution patterns between products. Products within the same nest are assumed to be closer substitutes than products in different nests. The degree of substitutability between products located in different nests is controlled by the value of the nesting parameter σ . The nesting parameters for singleton nests (nests containing only one product) are not identified and normalized to 1. The vector of sigmas is calibrated from the prices, revenue shares, and margins supplied by the user.

By default, all non-singleton nests are assumed to have a common value for σ . This constraint may be relaxed by setting ‘constraint’ to `FALSE`. In this case, at least one product margin must be supplied from a product within each nest.

In both `ces` and `ces.nests`, if revenue shares sum to 1, then one product’s mean value is not identified and must be normalized to 1. ‘normIndex’ may be used to specify the index (position) of the product whose mean value is to be normalized. If the sum of revenue shares is less than 1, both of these functions assume that there exists a $k+1$ st product in the market whose price and mean value are both normalized to 1.

Value

`ces` returns an instance of class [CES](#). `ces.alm` returns an instance of class [CESALM](#). `ces.nests` returns an instance of [CESNests](#), a child class of [CES](#).

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

Anderson, Simon, Palma, Andre, and Francois Thisse (1992). *Discrete Choice Theory of Product Differentiation*. The MIT Press, Cambridge, Mass.

Epstein, Roy and Rubinfeld, Daniel (2004). “Effects of Mergers Involving Differentiated Products.”

Sheu G (2011). “Price, Quality, and Variety: Measuring the Gains From Trade in Differentiated Products.” U.S Department of Justice.

See Also[logit](#)**Examples**

```

## Calibration and simulation results from a merger between Budweiser and
## Old Style. Assume that typical consumer spends 1% of income on beer,
## and that total beer expenditure in US is 1e9
## Source: Epstein/Rubinfeld 2004, pg 80

prodNames <- c("BUD", "OLD STYLE", "MILLER", "MILLER-LITE", "OTHER-LITE", "OTHER-REG")
ownerPre <-c("BUD", "OLD STYLE", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
ownerPost <-c("BUD", "BUD", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
nests <- c("R", "R", "R", "L", "L", "R")

price <- c(.0441, .0328, .0409, .0396, .0387, .0497)
shares <- c(.071, .137, .251, .179, .093, .269)
margins <- c(.3830, .5515, .5421, .5557, .4453, .3769)

names(price) <-
  names(shares) <-
  names(margins) <-
  prodNames

result.ces <-ces(price,shares,margins,ownerPre=ownerPre,ownerPost=ownerPost,
  labels=prodNames)

print(result.ces)          # return predicted price change
summary(result.ces)       # summarize merger simulation

elast(result.ces,TRUE)    # returns premerger elasticities
elast(result.ces,FALSE)  # returns postmerger elasticities

diversion(result.ces,TRUE) # return premerger diversion ratios
diversion(result.ces,FALSE) # return postmerger diversion ratios

cmcr(result.ces)          #calculate compensating marginal cost reduction
upp(result.ces)           #calculate Upwards Pricing Pressure Index

CV(result.ces)            #calculate compensating variation as a percent of
                          #representative consumer income

## Implement the Hypothetical Monopolist Test
## for BUD and OLD STYLE using a 5% SSNIP

HypoMonTest(result.ces,prodIndex=1:2)

## Get a detailed description of the 'CES' class slots
showClass("CES")

```

```

## Show all methods attached to the 'CES' Class
showMethods(classes="CES")

## Show which class have their own 'elast' method
showMethods("elast")

## Show the method definition for 'elast' and Class 'CES'
getMethod("elast", "CES")

```

CES-class

Class “CES”

Description

The “CES” class contains all the information needed to calibrate a CES demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function [ces](#).

Slots

Let k denote the number of products produced by all firms.

slopes: A list containing the coefficient on the numeraire (‘alpha’), the coefficient on price (‘gamma’), and the vector of mean valuations (‘meanval’)

priceOutside: The price of the outside good. Default is 1.

Extends

Class [Logit](#), directly. Class [Bertrand](#), by class [Logit](#), distance 2. Class [Antitrust](#), by class [Bertrand](#), distance 3.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcShares` signature(object, preMerger = TRUE, revenue=FALSE) Compute either pre-merger or post-merger equilibrium revenue shares under the assumptions that consumer demand is CES and firms play a differentiated product Bertrand Nash pricing game. 'revenue' takes on a value of TRUE or FALSE, where TRUE calculates revenue shares, while FALSE calculates quantity shares.

`calcSlopes` signature(object) Uncover CES demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

`CV` signature(object, revenueInside) Calculates compensating variation. If 'revenueInside' is missing, then CV returns compensating variation as a percent of the representative consumer's income. If 'revenueInside' equals the total expenditure on all products inside the market, then CV returns compensating variation in levels.

`elast` signature(object, preMerger = TRUE) Computes a $k \times k$ matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("CES")           # get a detailed description of the class
showMethods(classes="CES") # show all methods defined for the class
```

CESALM-class

Class "CESALM"

Description

The "CESALM" class contains all the information needed to calibrate a CES demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game with unknown market elasticity.

Objects from the Class

Objects can be created by using the constructor function `ces.alm`.

Slots

`parmsStart`: A length 2 vector whose first element equals an initial guess of the price coefficient and whose second element equals an initial guess of the outside share. The price coefficient's initial value must be negative and the outside share's initial value must be between 0 and 1 .

Extends

Class `Logit`, directly. Class `Bertrand`, by class `Logit`, distance 2. Class `Antitrust`, by class `Bertrand`, distance 3.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcSlopes signature(object)` Uncover CES ALM demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game with capacity constraints.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("CESALM")           # get a detailed description of the class
showMethods(classes="CESALM") # show all methods defined for the class
```

CESNests-class *Class “CESNests”*

Description

The “CESNests” class contains all the information needed to calibrate a nested CES demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function [ces.nests](#).

Slots

Let k denote the number of products produced by all firms.

nests: A length k vector identifying the nest that each product belongs to.

parmsStart: A length k vector whose elements equal an initial guess of the nesting parameter values.

constraint: A length 1 logical vector that equals TRUE if all nesting parameters are constrained to equal the same value and FALSE otherwise. Default is TRUE.

Extends

Class [CES](#), directly. Class [Logit](#), by class [CES](#), distance 2. Class [Bertrand](#), by class [Logit](#), distance 3. Class [Antitrust](#), by class [Bertrand](#), distance 4.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcShares` signature(object, preMerger = TRUE, revenue = FALSE) Compute either pre-merger or post-merger equilibrium revenue shares under the assumptions that consumer demand is nested CES and firms play a differentiated product Bertrand Nash pricing game. 'revenue' takes on a value of TRUE or FALSE, where TRUE calculates revenue shares, while FALSE calculates quantity shares.

`calcSlopes` signature(object) Uncover nested CES demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

`CV` signature(object, revenueInside) Calculates compensating variation. If 'revenueInside' is missing, then CV returns compensating variation as a percent of the representative consumer's income. If 'revenueInside' equals the total expenditure on all products inside the market, then CV returns compensating variation in levels.

`elast` signature(object, preMerger = TRUE) Computes a $k \times k$ matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("CESNests")           # get a detailed description of the class
showMethods(classes="CESNests") # show all methods defined for the class
```

cmcr-methods

*Methods For Calculating Compensating Marginal Cost Reductions
and Upwards Pricing Pressure Index (Bertrand)*

Description

Calculate the marginal cost reductions necessary to restore premerger prices in a merger, or the Upwards Pricing Pressure Index for the products of merging firms playing a differentiated products Bertrand pricing game.

Usage

```
## S4 method for signature 'ANY'
cmcr(object,market=FALSE)
## S4 method for signature 'ANY'
upp(object)
```

Arguments

object	An instance of one of the classes listed above.
market	If TRUE, calculates (post-merger) share-weighted average of metric. Default is FALSE.

Details

cmcr uses the results from the merger simulation and calibration methods associates with a particular class to compute the compensating marginal cost reduction (CMCR) for each of the merging parties' products.

Like cmcr, upp uses the results from the merger simulation and calibration to compute the upwards pricing pressure of the merger on each merging parties' products.

Value

cmcr returns a vector of length k equal to CMCR for the merging parties' products and 0 for all other products.

upp returns a vector of length k equal to the net UPP for the merging parties' products and 0 for all other products.

See Also

[cmcr.bertrand](#) is a function that calculates CMCR without the need to first calibrate a demand system and simulate a merger. Likewise, [upp.bertrand](#) calculates net UPP without the need to first calibrate a demand system and simulate a merger.

cmcr.bertrand	<i>Compensating Marginal Cost Reductions and Upwards Pricing Pressure (Bertrand)</i>
---------------	--

Description

Calculate the marginal cost reductions necessary to restore premerger prices (CMCR), or the net Upwards Pricing Pressure (UPP) in a merger involving firms playing a differentiated products Bertrand pricing game.

Usage

```
cmcr.bertrand(prices, margins, diversions, ownerPre,
              ownerPost=matrix(1,ncol=length(prices), nrow=length(prices)),
              labels=paste("Prod",1:length(prices),sep=""))
```

```
upp.bertrand(prices, margins, diversions, ownerPre,
             ownerPost=matrix(1,ncol=length(prices), nrow=length(prices)),
```

```
mcDelta=rep(0,length(prices)),
labels=paste("Prod",1:length(prices),sep="")
```

Arguments

	Let k denote the number of products produced by the merging parties.
prices	A length- k vector of product prices.
margins	A length- k vector of product margins.
diversions	A $k \times k$ matrix of diversion ratios with diagonal elements equal to -1.
ownerPre	EITHER a vector of length k whose values indicate which of the merging parties produced a product pre-merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	A $k \times k$ matrix of post-merger ownership shares. Default is a $k \times k$ matrix of 1s.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
labels	A length- k vector of product labels.

Details

All 'prices' elements must be positive, all 'margins' elements must be between 0 and 1, and all 'diversions' elements must be between 0 and 1 in absolute value. In addition, off-diagonal elements (i,j) of 'diversions' must equal an estimate of the diversion ratio from product i to product j (i.e. the estimated fraction of i 's sales that go to j due to a small increase in i 's price). Also, 'diversions' elements are positive if i and j are substitutes and negative if i and j are complements.

'ownerPre' will typically be a vector whose values equal 1 if a product is produced by firm 1 and 0 otherwise, though other values including firm name are acceptable. Optionally, 'ownerPre' may be set equal to a matrix of the merging firms pre-merger ownership shares. These ownership shares must be between 0 and 1.

'ownerPost' is an optional argument that should only be specified if one party to the acquisition is assuming partial control of the other party's assets. 'ownerPost' elements must be between 0 and 1.

Value

cmcr.bertrand returns a length- k vector whose values equal the percentage change in each products' marginal costs that the merged firms must achieve in order to offset a price increase.

upp.bertrand returns a length- k vector whose values equal the generalized pricing pressure (GePP) for each of the merging's parties' products, net any efficiency claims. GePP is a generalization of Upwards Pricing Pressure (UPP) that accomodates multi-product firms.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

- Farrell, Joseph and Shapiro, Carl (2010). "Antitrust Evaluation of Horizontal Mergers: An Economic Alternative to Market Definition." *The B.E. Journal of Theoretical Economics*, **10**(1), pp. 1-39.
- Jaffe, Sonia and Weyl Eric (2012). "The First-Order Approach to Merger Analysis." *SSRN eLibrary*
- Werden, Gregory (1996). "A Robust Test for Consumer Welfare Enhancing Mergers Among Sellers of Differentiated Products." *The Journal of Industrial Economics*, **44**(4), pp. 409-413.

See Also

[cmcr.cournot](#) for a homogeneous products Cournot version of CMCR, and [cmcr-methods](#) for calculating CMCR and UPP after calibrating demand system parameters and simulating a merger.

Examples

```
## Let k_1 = 1 and and k_2 = 2 ##

p1 = 50;      margin1 = .3
p2 = c(45,70); margin2 = c(.4,.6)
isOne=c(1,0,0)
diversions = matrix(c(-1,.5,.01,.6,-1,.1,.02,.2,-1),ncol=3)

cmcr.bertrand(c(p1,p2), c(margin1,margin2), diversions, isOne)
upp.bertrand(c(p1,p2), c(margin1,margin2), diversions, isOne)

## Calculate the necessary percentage cost reductions for various margins and
## diversion ratios in a two-product merger where both products have
## equal prices and diversions (see Werden 1996, pg. 412, Table 1)

margins = seq(.4,.7,.1)
diversions = seq(.05,.25,.05)
prices = rep(1,2) #assuming prices are equal, we can set product prices to 1
isOne = c(1,0)
result = matrix(ncol=length(margins),nrow=length(diversions),dimnames=list(diversions,margins))

for(m in 1:length(margins)){
  for(d in 1:length(diversions)){

    dMatrix = -diag(2)
    dMatrix[2,1] <- dMatrix[1,2] <- diversions[d]

    firmMargins = rep(margins[m],2)

    result[d,m] = cmcr.bertrand(prices, firmMargins, dMatrix, isOne)[1]

  }}

print(round(result,1))
```

cmcr.cournot	<i>Compensating Marginal Cost Reductions and Upwards Pricing Pressure (Cournot)</i>
--------------	---

Description

Calculate the average marginal cost reduction necessary to restore pre-merger prices, or the net Upwards Pricing Pressure in a two-product merger involving firms playing a homogeneous product Cournot pricing game.

Usage

```
cmcr.cournot(shares, mktElast)
```

```
upp.cournot(prices, margins, ownerPre,
            ownerPost=matrix(1, ncol=length(prices), nrow=length(prices)),
            mcDelta=rep(0, length(prices)),
            labels=paste("Prod", 1:length(prices), sep=""))
```

Arguments

shares	A length-2 vector containing merging party quantity shares.
mktElast	A length-1 containing the industry elasticity.
prices	A length-2 vector of product prices.
margins	A length-2 vector of product margins.
ownerPre	EITHER a vector of length 2 whose values indicate which of the merging parties produced a product pre-merger OR a 2 x 2 matrix of pre-merger ownership shares.
ownerPost	A 2 x 2 matrix of post-merger ownership shares. Default is a 2 x 2 matrix of 1s.
mcDelta	A vector of length 2 where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
labels	A length-2 vector of product labels.

Details

The 'shares' vector must have 2 elements, and all 'shares' elements must be between 0 and 1. The 'mktElast' vector must have 1 non-negative element.

Value

A vector with 1 element whose value equals the percentage change in the products' average marginal costs that the merged firms must achieve in order to offset a price increase.

Author(s)

Charles Taragin

References

Froeb, Luke and Werden, Gregory (1998). "A robust test for consumer welfare enhancing mergers among sellers of a homogeneous product." *Economics Letters*, **58**(3), pp. 367 - 369.

See Also

[cmcr.bertrand](#) for a differentiated products Bertrand version of this measure.

Examples

```

shares=c(.05,.65)
industryElast = 1.9

cmcr.cournot(shares,industryElast)

## Calculate the necessary percentage cost reductions for various shares and
## industry elasticities in a two-product merger where both firm
## products have identical share (see Froeb and
## Werden, 1998, pg. 369, Table 1)

deltaHHI = c(100, 500, 1000, 2500, 5000) #start with change in HHI
shares = sqrt(deltaHHI/(2*100^2)) #recover shares from change in HHI
industryElast = 1:3

result = matrix(nrow=length(deltaHHI),ncol=length(industryElast),
               dimnames=list(deltaHHI,industryElast))

for(s in 1:length(shares)){
  for(e in 1:length(industryElast)){

    result[s,e] = cmcr.cournot(rep(shares[s],2),industryElast[e])[1]

  }}

print(round(result,1))

```


Description

This page describes methods that may be used to explore how a merger affects firms' incentives to collude.

Usage

```
## S4 method for signature 'Bertrand'
calcProducerSurplusGrimTrigger(object,coalition,
                               discount,preMerger=TRUE,isCollusion=FALSE,...)
```

Arguments

	Let k denote the number of products in the market, and let c denote the number of firms in a coalition
object	An instance of one of the classes listed above.
coalition	A length c vector of integers indicating the index of the products participating in the coalition.
discount	A length k vector of values between 0 and 1 that represent the product-specific discount rate for all products produced by firms participating in the coalition. NAs are allowed
preMerger	TRUE returns pre-merger result, FALSE returns post-merger results. Default is TRUE.
isCollusion	TRUE recalculates demand and cost parameters under the assumption that the coalition specified in 'coalition' is operating pre-merger. FALSE (the default) uses demand and cost parameters calculated from the 'ownerPre' matrix.
...	Additional argument to pass to calcPrices

Details

calcProducerSurplusGrimTrigger calculates 'preMerger' product producer surplus (as well as other statistics – see below), under the assumption that firms are playing an N-player iterated Prisoner's Dilemma where in each period a coalition of firms decides whether to *cooperate* with one another by setting the joint surplus maximizing price on some 'coalition' of their products, or *defect* from the coalition by setting all of their products' prices to optimally undercut the prices of the coalition's products. Moreover, firms are assumed to play Grim Trigger strategies where each firm cooperates in the current period so long as *every* firm in the coalition cooperated last period and defects otherwise. product level 'discount' rates are then employed to determine whether a firm's discounted surplus from remaining in the coalition are greater than its surplus from optimally undercutting the coalition prices' for one period plus its discounted surplus when all firms set Nash-Bertrand prices in all subsequent periods.

Value

`calcProducerSurplusGrimTrigger` returns a data frame with rows equal to the number of products produced by any firm participating in the coalition and the following 5 columns

- Discount: The user-supplied discount rate
- Coord: Single period producer surplus from coordinating
- Defect: Single period producer surplus from defecting
- Punish: Single period producer surplus from punishing using Bertrand price
- IC: TRUE if the discounted producer surplus from coordinating across all firm products are greater than the surplus from defecting across all firm products for one period and receiving discounted Bertrand surplus for all subsequent periods under Grim Trigger.

Cournot

Multi-product Cournot/Stackelberg Calibration and Merger Simulation With Linear or Log-Linear Demand

Description

Calibrates consumer demand for multiple products using either a linear or log-linear demand system and then simulates the prices effect of a merger between two multi-plant firms under the assumption that all firms in the market are playing either a Cournot or Stackelberg quantity setting game.

Usage

```
cournot(prices, quantities,
        margins = matrix(NA_real_, nrow(quantities), ncol(quantities)),
        demand = rep("linear", length(prices)),
        cost = rep("linear", nrow(quantities)),
        mcfunPre = list(),
        mcfunPost = mcfunPre,
        vcfunPre = list(),
        vcfunPost = vcfunPre,
        capacitiesPre = rep(Inf, nrow(quantities)),
        capacitiesPost = capacitiesPre,
        productsPre = !is.na(quantities),
        productsPost = productsPre,
        ownerPre, ownerPost,
        mktElast = rep(NA_real_, length(prices)),
        mcDelta = rep(0, nrow(quantities)),
        quantityStart = as.vector(quantities),
        control.slopes,
        control.equ,
        labels,
```

```

)
...
stackelberg(prices,quantities,margins,
             demand = rep("linear",length(prices)),
             cost    = rep("linear",nrow(quantities)),
             isLeaderPre = matrix(FALSE,
                                   ncol = ncol(quantities),
                                   nrow= nrow(quantities)),
             isLeaderPost= isLeaderPre,
             mcfunPre=list(),
             mcfunPost=mcfunPre,
             vcfunPre=list(),
             vcfunPost=vcfunPre,
             dmcfunPre=list(),
             dmcfunPost=dmcfunPre,
             capacitiesPre = rep(Inf,nrow(quantities)),
             capacitiesPost = capacitiesPre,
             productsPre=!is.na(quantities),
             productsPost=productsPre,
             ownerPre,ownerPost,
             mcDelta =rep(0,nrow(quantities)),
             quantityStart=as.vector(quantities),
             control.slopes,
             control.equ,
             labels,
             ...
)

```

Arguments

	Let k denote the number of products and n denote the number of plants.
prices	A length k vector product prices.
quantities	An $n \times k$ matrix of product quantities. All quantities must either be positive, or if the product is not produced by a plant, NA.
margins	An $n \times k$ matrix of product margins. All margins must be either between 0 and 1, or NA.
demand	A length k character vector equal to "linear" if a product's demand curve is assumed to be linear or "log" if a product's demand curve is assumed to be log-linear.
cost	A length k character vector equal to "linear" if a plant's marginal cost curve is assumed to be linear or "constant" if a plant's marginal curve is assumed to be constant. Returns an error if a multi-plant firm with constant marginal costs does not have capacity constraints.
isLeaderPre	An $n \times k$ logical matrix equal to TRUE if a firm is a "leader" pre-merger for a particular product and FALSE otherwise. Default is FALSE, which is equivalent to cournot.

<code>isLeaderPost</code>	An $n \times k$ logical matrix equal to TRUE if a firm is a "leader" pre-merger for a particular product and FALSE otherwise. Default is FALSE, which is equivalent to cournot.
<code>mcfunPre</code>	a length n list of functions that calculate a plant's pre-merger marginal cost. If empty (the default), assumes quadratic costs.
<code>mcfunPost</code>	a length n list of functions that calculate a plant's post-merger marginal cost. If empty (the default), equals 'mcfunPre')
<code>vcfunPre</code>	a length n list of functions that calculate a plant's pre-merger variable cost. If empty (the default), assumes quadratic variable costs.
<code>vcfunPost</code>	a length n list of functions that calculate a plant's post-merger variable cost. If empty (the default), equals 'vcfunPre')
<code>dmcfunPre</code>	a length n list of functions that calculate the derivative of a plant's pre-merger marginal cost. If empty (the default), assumes quadratic variable costs.
<code>dmcfunPost</code>	a length n list of functions that calculate the derivative of a plant's post-merger marginal cost. If empty (the default), equals 'mcfunPre')
<code>capacitiesPre</code>	A length n numeric vector of pre-merger plant capacities. Default is Inf.
<code>capacitiesPost</code>	A length n numeric vector of post-merger plant capacities. Default 'capacitiesPre'.
<code>productsPre</code>	An $n \times k$ matrix that equals TRUE if pre-merger, a plant produces a product. Default is TRUE if 'quantities' is not NA.
<code>productsPost</code>	An $n \times k$ matrix that equals TRUE if post-merger, a plant produces a product. Default equals 'productsPre'.
<code>ownerPre</code>	EITHER a vector of length n whose values indicate which plants are commonly owned pre-merger OR an $n \times n$ matrix of pre-merger ownership shares.
<code>ownerPost</code>	EITHER a vector of length n whose values indicate which plants will be commonly owned after the merger OR an $n \times n$ matrix of post-merger ownership shares.
<code>mktElast</code>	A length k vector of product elasticities. Default is a length k vector of NAs
<code>mcDelta</code>	A length n vector where each element equals the proportional change in a firm's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
<code>quantityStart</code>	A length k vector of quantities used as the initial guess in the nonlinear equation solver. Default is 'quantities'.
<code>control.slopes</code>	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
<code>control.equ</code>	A list of <code>BBSolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcQuantities</code> method).
<code>labels</code>	A list with 2 elements. The first element is a vector of firm names, while the second element is a vector of products names. Default is 'O1:On', and 'P1:Pk'.
<code>...</code>	Additional options to feed to the solver. See below.

Details

Using price, and quantity, information for all products in each market, as well as margin information for at least one products in each market, `cournot` is able to recover the slopes and intercepts of either a Linear or Log-linear demand system. These parameters are then used to simulate the price effects of a merger between two firms under the assumption that the firms are playing a homogeneous products simultaneous quantity setting game.

`stackelberg`, is similar to `cournot`, except that for a given product, firms are either "leaders" or "followers". leaders gain a first mover advantage over followers, which allows the leaders to anticipate how changes to their output will effect the follower's output decisions. Firms can be the leader for some products but the follower in others.

'`mcfunPre`' and '`mcfunPost`' are length `n` lists whose elements are 'R' functions that return a firm's marginal cost. The first argument of each function should be total firm quantities. By default, each firm is assumed to have quadratic costs with a firm-specific parameter calibrated from a firm's margin. '`vcfunPre`' and '`vcfunPost`' are similarly defined. '`sQuotedmcfunPre`' and '`dmcfunPost`' are the changes in marginal cost and are only required for `stackelberg`.

'`ownerPre`' and '`ownerPost`' values will typically be equal to either 0 (element `[i,j]` is not commonly owned) or 1 (element `[i,j]` is commonly owned), though these matrices may take on any value between 0 and 1 to account for partial ownership.

Under linear demand and linear marginal costs, an analytic solution to the Cournot quantity game exists. However, this solution can at times produce negative equilibrium quantities. To accommodate this issue, `cournot` uses `BBsolve` to find equilibrium quantities subject to a non-negativity constraint. . . . may be used to change the default options for `BBsolve`.

Value

`cournot` returns an instance of class `Cournot`. `stackelberg` returns an instance of class `Stackelberg`.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
## Simulate a Cournot merger between two single-plant firms
## producing a single product in a
## 5-firm market with linear demand and quadratic costs
```

```
n <- 5 #number of firms in market pre-merger
cap <- rnorm(n,mean = .5, sd = .1)
int <- 10
slope <- -.25
```

```
B.pre.c = matrix(slope,nrow=n,ncol=n)
diag(B.pre.c) = 2* diag(B.pre.c) - 1/cap
quantity.pre.c = rowSums(solve(B.pre.c) * -int)
price.pre.c = int + slope * sum(quantity.pre.c)
```

```

mc.pre.c = quantity.pre.c/cap
vc.pre.c = quantity.pre.c^2/(2*cap)
margin.pre.c = 1 - mc.pre.c/price.pre.c
ps.pre.c = price.pre.c*quantity.pre.c - vc.pre.c

mktQuant.pre.c = sum(quantity.pre.c)

## suppose firm 1 acquires firm 2
## This model has a closed form solution
B.post.c = B.pre.c
B.post.c[1,2] = 2*B.post.c[1,2]
B.post.c[2,1] = 2*B.post.c[2,1]

quantity.post.c = rowSums(solve(B.post.c) * -int)
price.post.c = int + slope * sum(quantity.post.c)
mc.post.c = quantity.post.c/cap
vc.post.c = quantity.post.c^2/(2*cap)
margin.post.c = 1 - mc.post.c/price.post.c
ps.post.c = price.post.c*quantity.post.c - vc.post.c

mktQuant.post.c = sum(quantity.post.c, na.rm=TRUE)

#check if merger is profitable for merging parties
isprofitable.c = ps.post.c - ps.pre.c
isprofitable.c= sum(isprofitable.c[1:2]) > 0

#prep inputs for Cournot
owner.pre <- diag(n)
owner.post <- owner.pre
owner.post[1,2] <- owner.post[2,1] <- 1

result.c <- cournot(prices = price.pre.c,quantities = as.matrix(quantity.pre.c),
                    margins=as.matrix(margin.pre.c),
                    ownerPre=owner.pre,ownerPost=owner.post)

print(result.c)          # return predicted price change
summary(result.c)       # summarize merger simulation

## check if 'cournot' yields the same result as closed-form solution
#print(all.equal(sum(result.c@quantityPre) , mktQuant.pre.c))
#print(all.equal(sum(result.c@quantityPost) , mktQuant.post.c))

## Simulate a Stackelberg merger between two single-plant firms
## producing a single product in a
## 5-firm market with linear demand and quadratic costs.
## Allow both merging parties to be followers pre-merger,
## but assume that they become leaders post-merger.

```

```
## Finally, assume that pre-merger, there is a single leader who ## remains a leader post-merger
## Note: This example uses setup from the above Cournot example
```

```
isLeader.pre = matrix(rep(FALSE,n), ncol=1)
isLeader.pre[n,] = TRUE
isLeader.post = isLeader.pre
isLeader.post[1:2,] = TRUE

passthru.pre = matrix(-slope^2/(2*slope - 1/cap))
passthru.post = passthru.pre
passthru.pre[isLeader.pre] = 0
passthru.post[isLeader.post] = 0

B.pre.s = matrix(slope,nrow=n,ncol=n)
diag(B.pre.s) = 2* diag(B.pre.s) - 1/cap
diag(B.pre.s)[n] = diag(B.pre.s)[n] + sum(passthru.pre)

quantity.pre.s = rowSums(solve(B.pre.s) * ( -int))
price.pre.s = int + slope * sum(quantity.pre.s)
mc.pre.s = quantity.pre.s/cap
vc.pre.s = quantity.pre.s^2/(2*cap)
margin.pre.s = 1 - mc.pre.s/price.pre.s
ps.pre.s = price.pre.s*quantity.pre.s - vc.pre.s

mktQuant.pre.s = sum(quantity.pre.s)

## suppose firm 1 acquires firm 2
## This model has a closed form solution
B.post.s = matrix(slope,nrow=n,ncol=n)
diag(B.post.s) = 2* diag(B.post.s) - 1/cap
B.post.s[1,2] = 2*B.post.s[1,2]
B.post.s[1,1:2] = B.post.s[1,1:2] + sum(passthru.post)
B.post.s[2,1] = 2*B.post.s[2,1]
B.post.s[2,1:2] = B.post.s[2,1:2] + sum(passthru.post)
diag(B.post.s)[n] = diag(B.post.s)[n] + sum(passthru.post)

quantity.post.s = rowSums(solve(B.post.s) * as.vector( -int ) )
price.post.s = int + slope * sum(quantity.post.s)
mc.post.s = quantity.post.s/cap
vc.post.s = quantity.post.s^2/(2*cap)
margin.post.s = 1 - mc.post.s/price.post.s
ps.post.s = price.post.s*quantity.post.s - vc.post.s

mktQuant.post.s = sum(quantity.post.s, na.rm=TRUE)

#check if merger is profitable for merging parties
isprofitable.s = ps.post.s - ps.pre.s
isprofitable.s = sum(isprofitable.s[1:2]) > 0

#prep inputs for Stackelberg
owner.pre <- diag(n)
owner.post <- owner.pre
```

```

owner.post[1,2] <- owner.post[2,1] <- 1

result.s <- stackelberg(prices = price.pre.s, quantities = as.matrix(quantity.pre.s),
                       margins=as.matrix(margin.pre.s), ownerPre=owner.pre,
                       ownerPost=owner.post,
                       isLeaderPre = isLeader.pre, isLeaderPost = isLeader.post)

print(result.s)          # return predicted price change
summary(result.s)       # summarize merger simulation

## check if 'stackelberg' yields the same result as closed-form solution
#print(all.equal(sum(result.s@quantityPre) , mktQuant.pre.s))
#print(all.equal(sum(result.s@quantityPost) , mktQuant.post.s))

```

Cournot-class

Class “*Cournot*”

Description

The “Cournot” class is a building block used to create other classes in this package. As such, it is most likely to be useful for developers who wish to code their own merger calibration/simulation routines.

Objects from the Class

Objects can be created by calls of the form `new("Cournot", ...)`.

Slots

Let k denote the number of products and n denote the number of plants.

intercepts: A length k vector containing the calibrated demand intercept.

mcfunPre: A length n list whose elements equal a function that calculates a plant’s pre-merger marginal cost.

mcfunPost: A length n list whose elements equal a function that calculates a plant’s post-merger marginal cost.

vcfunPre: A length n list whose elements equal a function that calculates a plant’s pre-merger variable cost.

vcfunPost: A length n list whose elements equal a function that calculates a plant’s post-merger variable cost.

prices: A length k vector of product prices.

quantities: An $n \times k$ matrix of plant quantities produced for each product.
margins: An $n \times k$ matrix of plant product margins.
quantityPre: An $n \times k$ matrix of predicted pre-merger quantities.
quantityPost: An $n \times k$ matrix of predicted post-merger quantities.
quantityStart: A length $n \times k$ vector of starting quantities for the non-linear solver.
productsPre: An $n \times k$ logical matrix whose elements are TRUE if a plant produces a product pre-merger and FALSE otherwise.
productsPost: An $n \times k$ logical matrix whose elements are TRUE if a plant produces a product post-merger and FALSE otherwise.
capacitiesPre: A length- n logical vector whose elements equal to pre-merger plant capacities. Infinite values are allowed.
capacitiesPost: A length- n logical vector whose elements equal to post-merger plant capacities. Infinite values are allowed.
demand: A length k character vector specifying whether product demand is linear ("linear") or log-linear ("log").
cost: A length k character vector equal to "linear" if a plant's marginal cost curve is assumed to be linear or "constant" if a plant's marginal curve is assumed to be constant. Returns an error if a multi-plant firm with constant marginal costs does not have capacity constraints.
mktElast: A length k vector of market elasticities.

Extends

Class [Bertrand](#), directly. Class [Antitrust](#), by class [Bertrand](#), distance 2.

Methods

Many of the methods described below contain a 'preMerger' and 'revenue' argument. The 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger values, while FALSE invokes the method using the post-merger ownership structure. The 'revenue' argument also takes on a value of TRUE or FALSE, where TRUE invokes the method using revenues, while FALSE invokes the method using quantities

calcMC signature(object,preMerger=TRUE) Calculates marginal cost for each product.

calcVC signature(object,preMerger=TRUE) Calculates variable cost for each product.

calcMargins signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium margins under the assumption that firms play a multi-product Cournot Nash pricing game.

cmcr signature(object) Calculates compensated marginal cost reduction, the percentage decrease in the marginal costs of the merging parties' products needed to offset a post-merger price increase.

HypoMonTest signature(object,prodIndex,ssnip=.05,...) HypoMonTest implements the Hypothetical Monopolist Test for a given 'ssnip'.

calcPriceDeltaHypoMon signature(object,prodIndex,...) Compute the proportional difference in product prices between the prices of products in 'prodIndex' (i.e. prices set by the Hypothetical Monopolist) and prices set in the pre-merger Cournot equilibrium. '...' may be used to pass arguments to the optimizer.

`hhi` signature(object, preMerger= TRUE, revenue=FALSE) Compute either the pre-merger or post-merger Herfindahl-Hirschman Index (HHI) under the assumption that firms play a multi-product Cournot Nash pricing game.

`diversion` signature(object, preMerger = TRUE) Computes a $k \times k$ matrix of diversion ratios.

`summary` signature(object, revenue=TRUE, shares=TRUE, parameters=FALSE, digits=2) Summarizes the effect of the merger, including price and revenue changes. Setting ‘revenue’ equal to FALSE reports quantities rather than revenues. Setting ‘shares’ to FALSE reports quantities rather than than shares (when possible). Setting ‘parameters’ equal to TRUE reports all demand parameters. ‘digits’ controls the number of significant digits reported in output.

`cmcr` signature(object) Calculates Compensating Marginal Cost Reduction (CMCR).

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Cournot")           # get a detailed description of the class
showMethods(classes="Cournot") # show all methods defined for the class
```

CV-methods

Methods For Calculating Compensating Variation (CV)

Description

Calculate the amount of money a consumer would need to be paid to be just as well off as they were before the merger.

Methods

signature(object = c(Logit, LogitNests, CES, CESNests)) All the information needed to compute CV is already available within the Logit, Nested Logit CES and Nested CES classes. In CES and Nested CES, CV cannot be calculated if the outside share cannot be inferred.

signature(object = AIDS) If the ‘insideSize’ slot to the “AIDS” class equals NA, CV is calculated as a percentage of total expenditure (revenues) on products included in the simulation. Otherwise CV is calculated in terms of dollars. Pre-merger prices for all products in the market must be supplied in order for CV to be calculated.

signature(object = c(Linear, LogLin)) Although no additional information is needed to calculate CV for either the “Linear” or “LogLin” classes, The CV method will fail if the appropriate restrictions on the demand parameters have not been imposed.

 defineMarketTools-methods

Methods For Implementing The Hypothetical Monopolist Test

Description

An Implementation of the Hypothetical Monopolist Test described in the 2010 Horizontal Merger Guidelines.

Usage

```
## S4 method for signature 'Bertrand'
HypoMonTest(object,prodIndex,ssnip=.05,...)
## S4 method for signature 'ANY'
calcPricesHypoMon(object,prodIndex)
## S4 method for signature 'ANY'
calcPriceDeltaHypoMon(object,prodIndex)
## S4 method for signature 'Bertrand'
diversionHypoMon(object,prodIndex,...)
## S4 method for signature 'AIDS'
diversionHypoMon(object)
```

Arguments

	Let k denote the number of products produced by all firms playing the Bertrand pricing game.
object	An instance of one of the classes listed above.
prodIndex	A vector of product indices that are to be placed under the control of the Hypothetical Monopolist.
ssnip	A number between 0 and 1 that equals the threshold for a “Small but Significant and Non-transitory Increase in Price” (SSNIP). Default is .05, or 5%.
...	Pass options to the optimizer used to solve for equilibrium prices.

Details

HypoMonTest is an implementation of the Hypothetical Monopolist Test on the products indexed by ‘prodIndex’ for a ‘ssnip’. The Hypothetical Monopolist Test determines whether a profit-maximizing Hypothetical Monopolist who controls the products indexed by ‘prodIndex’ would increase the price of at least one of the merging parties’ products in ‘prodIndex’ by a small, significant, and non-transitory amount (i.e. impose a SSNIP).

calcPriceDeltaHypoMon calculates the price changes relative to (predicted) pre-merger prices that a Hypothetical Monopolist would impose on the products indexed by ‘prodIndex’, holding the prices of products not controlled by the Hypothetical Monopolist fixed at pre-merger levels. With the exception of ‘AIDS’, the calcPriceDeltaHypoMon for all the classes listed above calls calcPricesHypoMon to compute price levels. calcPriceDeltaHypoMon is in turn called by HypoMonTest.

diversionHypoMon calculates the matrix of revenue diversions between all products included in the merger simulation, *irrespective* of whether or not they are also included in 'prodIndex'. This matrix is useful for diagnosing whether or not a product not included in 'prodIndex' may have a higher revenue diversion either to or from a product included in 'prodIndex'. Note that the 'AIDS' diversionHypoMon method does not contain the 'prodIndex' argument, as AIDS revenue diversions are only a function of demand parameters.

Value

HypoMonTest returns TRUE if a profit-maximizing Hypothetical Monopolist who controls the products indexed by 'prodIndex' would increase the price of at least one of the merging parties' products in 'prodIndex' by a 'ssnip', and FALSE otherwise. HypoMonTest returns an error if 'prodIndex' does not contain at least one of the merging parties products.

calcPriceDeltaHypoMon returns a vector of proportional price changes for all products placed under the control of the Hypothetical Monopolist (i.e. all products indexed by 'prodIndex'). calcPricesHypoMon is identical, but for price levels.

diversionHypoMon returns a $k \times k$ matrix of diversions, where element i,j is the diversion from product i to product j .

References

U.S. Department of Justice and Federal Trade Commission, *Horizontal Merger Guidelines*. Washington DC: U.S. Department of Justice, 2010. <http://www.justice.gov/atr/public/guidelines/hmg-2010.html> (accessed July 29, 2011).

diversion-methods

Methods For Calculating Diversion

Description

Calculate the diversion matrix between any two products in the market.

Usage

```
## S4 method for signature 'ANY'
diversion(object,preMerger=TRUE,revenue=FALSE)
```

Arguments

object	An instance of one of the classes listed above.
preMerger	If TRUE, calculates pre-merger price elasticities. If FALSE, calculates post-merger price elasticities. Default is TRUE.
revenue	If TRUE, calculates revenue diversion. If FALSE, calculates quantity diversion. Default is TRUE for 'Bertrand' and FALSE for 'AIDS'.

Value

returns a k x k matrix of diversion ratios, where the i,jth element is the diversion from i to j.

Methods

diversion signature(object=Bertrand,preMerger=TRUE, revenue=FALSE) When ‘revenue’ is FALSE (the default), this method uses the results from the merger calibration and simulation to compute the *quantity* diversion matrix between any two products in the market. Element i,j of this matrix is the quantity diversion from product i to product j, or the proportion of product i’s sales that leave (go to) i for (from) j due to a increase (decrease) in i’s price. Mathematically, quantity diversion is $\frac{-\epsilon_{ji}share_i}{\epsilon_{ii}share_i}$, where ϵ_{ij} is the cross-price elasticity from i to j.

When ‘revenue’ is TRUE, this method computes the revenue diversion matrix between any two products in the market. Element i,j of this matrix is the revenue diversion from product i to product j, or the proportion of product i’s revenues that leave (go to) i for (from) j due to a increase (decrease) in i’s price. Mathematically, revenue diversion is $-\frac{\epsilon_{ji}(\epsilon_{jj}-1)r_j}{\epsilon_{jj}(\epsilon_{ii}-1)r_i}$ where r_i is the revenue share of product i.

When ‘preMerger’ is TRUE, diversions are calculated at pre-merger equilibrium prices, and when ‘preMerger’ is FALSE, they are calculated at post-merger equilibrium prices.

diversion signature(object=AIDS,preMerger=TRUE, revenue=TRUE) When ‘revenue’ is TRUE (the default), this method computes the *revenue* diversion matrix between any two products in the market. For AIDS, the revenue diversion from i to j is $\frac{\beta_{ji}}{\beta_{ij}}$, where β_{ij} is the percentage change in product i’s revenue due to a change in j’s price.

When ‘revenue’ is FALSE, this callNextMethod is invoked. Will yield a matrix of NAs if the user did not supply prices.

When ‘preMerger’ is TRUE, diversions are calculated at pre-merger equilibrium prices, and when ‘preMerger’ is FALSE, they are calculated at post-merger equilibrium prices.

Description

Calculate the own and cross-price elasticity between any two products in the market.

Usage

```
## S4 method for signature 'ANY'
elast(object,preMerger=TRUE,market=FALSE)
```

Arguments

- object An instance of one of the classes listed above.
- preMerger If TRUE, calculates pre-merger price elasticities. If FALSE, calculates post-merger price elasticities. Default is TRUE.
- market If TRUE, calculates the market (aggregate) elasticity. If FALSE, calculates matrix of own- and cross-price elasticities. Default is FALSE.

Details

When 'market' is FALSE, this method computes the matrix of own and cross-price elasticities. Element i,j of this matrix is the percentage change in the demand for good i from a small change in the price of good j . When 'market' is TRUE, this method computes the market (aggregate) elasticities using share-weighted prices.

When 'preMerger' is TRUE, elasticities are calculated at pre-merger equilibrium prices and shares, and when 'preMerger' is FALSE, they are calculated at post-merger equilibrium prices and shares.

Value

returns a $k \times k$ matrix of own- and cross-price elasticities, where k is the number of products in the market

HHI	<i>Herfindahl-Hirschman Index</i>
-----	-----------------------------------

Description

Calculate the Herfindahl-Hirschman Index with arbitrary ownership and control.

Usage

```
HHI(shares,
    owner=diag(length(shares)),
    control)
```

Arguments

	Let k denote the number of products produced by the merging parties.
	A length- k vector of product quantity shares.
shares	EITHER a vector of length k whose values indicate which of the merging parties produced a product OR a $k \times k$ matrix of ownership shares. Default is a diagonal matrix, which assumes that each product is owned by a separate firm.
control	EITHER a vector of length k whose values indicate which of the merging parties have the ability to make pricing or output decisions OR a $k \times k$ matrix of control shares. Default is a $k \times k$ matrix equal to 1 if 'owner' > 0 and 0 otherwise.

Details

All 'shares' must be between 0 and 1. When 'owner' is a matrix, the i,j th element of 'owner' should equal the percentage of product j 's profits earned by the owner of product i . When 'owner' is a vector, HHI generates a $k \times k$ matrix of whose i,j th element equals 1 if products i and j are commonly owned and 0 otherwise. 'control' works in a fashion similar to 'owner'.

Value

HHI returns a number between 0 and 10,000

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

Salop, Steven and O'Brien, Daniel (2000) "Competitive Effects of Partial Ownership: Financial Interest and Corporate Control" 67 Antitrust L.J. 559, pp. 559-614.

See Also

[other-methods](#) for computing HHI following merger simulation.

Examples

```
## Consider a market with 5 products labeled 1-5. 1,2 are produced
## by Firm A, 2,3 are produced by Firm B, 3 is produced by Firm C.
## The pre-merger product market shares are

shares = c(.15,.2,.25,.35,.05)
owner  = c("A","A","B","B","C")
nprod  = length(shares)

HHI(shares,owner)

## Suppose that Firm A acquires a 75% ownership stake in product 3, and
## Firm B get a 10% ownership stake in product 1. Assume that neither
## firm cedes control of the product to the other.

owner <- diag(nprod)

owner[1,2] <- owner[2,1] <- owner[3,4] <- owner[4,3] <- 1
control <- owner
owner[1,1] <- owner[2,1] <- .9
owner[3,1] <- owner[4,1] <- .1
owner[1,3] <- owner[2,3] <- .75
owner[3,3] <- owner[4,3] <- .25

HHI(shares,owner,control)

## Suppose now that in addition to the ownership stakes described
## earlier, B receives 30% of the control of product 1
control[1,1] <- control[2,1] <- .7
control[3,1] <- control[4,1] <- .3

HHI(shares,owner,control)
```

linear

*Linear and Log-Linear Demand Calibration and Merger Simulation***Description**

Calibrates consumer demand using either a linear or log-linear demand system and then simulates the prices effect of a merger between two firms under the assumption that all firms in the market are playing a differentiated products Bertrand game.

Usage

```
linear(prices,quantities,margins,
       diversions,
       symmetry=TRUE,
       ownerPre,ownerPost,
       mcDelta=rep(0,length(prices)),
       subset=rep(TRUE, length(prices)),
       priceStart=prices,
       control.slopes,
       labels=paste("Prod",1:length(prices),sep=""),
       ...
       )
```

```
loglinear(prices,quantities,margins,
          diversions,
          ownerPre,ownerPost,
          mcDelta=rep(0,length(prices)),
          subset=rep(TRUE, length(prices)),
          priceStart=prices,
          control.equ,
          labels=paste("Prod",1:length(prices),sep=""),
          ...
          )
```

Arguments

	Let k denote the number of products produced by all firms.
prices	A length k vector product prices.
quantities	A length k vector of product quantities.
margins	A length k vector of product margins. All margins must be either be between 0 and 1, or NA.
diversions	A $k \times k$ matrix of diversion ratios with diagonal elements equal to -1. Default is missing, in which case diversion according to quantity share is assumed.

symmetry	If TRUE, requires the matrix of demand slope coefficients to be symmetric and homogeneous of degree 0 in prices, both of which suffice to make demand consistent with utility maximization theory. Default is TRUE.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product pre-merger OR a k x k matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a k x k matrix of post-merger ownership shares.
mcDelta	A length k vector where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
priceStart	A length k vector of prices used as the initial guess in the nonlinear equation solver. Default is 'prices'.
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
control.equ	A list of <code>BBsolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
labels	A k-length vector of labels. Default is "Prod#", where '#' is a number between 1 and the length of 'prices'.
...	Additional options to feed to the solver. See below.

Details

Using price, quantity, and diversion information for all products in a market, as well as margin information for (at least) all the products of any firm, `linear` is able to recover the slopes and intercepts in a Linear demand system and then uses these demand parameters to simulate the price effects of a merger between two firms under the assumption that the firms are playing a differentiated Bertrand pricing game.

`loglinear` uses the same information as `linear` to uncover the slopes and intercepts in a Log-Linear demand system, and then uses these demand parameters to simulate the price effects of a merger of two firms under the assumption that the firms are playing a differentiated Bertrand pricing game.

'diversion' must be a square matrix whose off-diagonal elements [i,j] estimate the diversion ratio from product i to product j (i.e. the estimated fraction of i's sales that go to j due to a small increase in i's price). Off-diagonal elements are restricted to be non-negative (products are assumed to be substitutes), diagonal elements must equal -1, and rows must sum to 0 (negative if you wish to include an outside good) . If 'diversion' is missing, then diversion according to quantity share is assumed.

'ownerPre' and 'ownerPost' values will typically be equal to either 0 (element [i,j] is not commonly owned) or 1 (element [i,j] is commonly owned), though these matrices may take on any value between 0 and 1 to account for partial ownership.

Under linear demand, an analytic solution to the Bertrand pricing game exists. However, this solution can at times produce negative equilibrium quantities. To accommodate this issue, `linear` uses

`constrOptim` to find equilibrium prices with non-negative quantities. ... may be used to change the default options for `constrOptim`.

`loglinear` uses the non-linear equation solver `BBsolve` to find equilibrium prices. ... may be used to change the default options for `BBsolve`.

Value

`linear` returns an instance of class `Linear`. `loglinear` returns an instance of `LogLin`, a child class of `Linear`.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

von Haefen, Roger (2002). "A Complete Characterization Of The Linear, Log-Linear, And Semi-Log Incomplete Demand System Models." *Journal of Agricultural and Resource Economics*, **27**(02). <http://ideas.repec.org/a/ags/jlaare/31118.html>.

See Also

`aids` for a demand system based on revenue shares rather than quantities.

Examples

```
## Simulate a merger between two single-product firms in a
## three-firm market with linear demand with diversions
## that are proportional to shares.
## This example assumes that the merger is between
## the first two firms

n <- 3 #number of firms in market
price <- c(2.9,3.4,2.2)
quantity <- c(650,998,1801)
margin <- c(.435,.417,.370)

#simulate merger between firms 1 and 2
owner.pre <- diag(n)
owner.post <- owner.pre
owner.post[1,2] <- owner.post[2,1] <- 1

result.linear <- linear(price,quantity,margin,ownerPre=owner.pre,ownerPost=owner.post)

print(result.linear)          # return predicted price change
```

```

summary(result.linear)      # summarize merger simulation

elast(result.linear,TRUE)   # returns premerger elasticities
elast(result.linear,FALSE) # returns postmerger elasticities

diversion(result.linear,TRUE) # returns premerger diversion ratios
diversion(result.linear,FALSE) # returns postmerger diversion ratios

cmcr(result.linear)        # returns the compensating marginal cost reduction

CV(result.linear)          # returns representative agent compensating variation

## Implement the Hypothetical Monopolist Test
## for products 1 and 2 using a 5% SSNIP

#HypoMonTest(result.linear,prodIndex=1:2)

## Get a detailed description of the 'Linear' class slots
showClass("Linear")

## Show all methods attached to the 'Linear' Class
showMethods(classes="Linear")

## Show which class have their own 'elast' method
showMethods("elast")

## Show the method definition for 'elast' and Class 'Linear'
getMethod("elast","Linear")

```

Linear-class

Class "*Linear*"

Description

The “Linear” class contains all the information needed to calibrate a Linear demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated Bertrand products pricing game.

Objects from the Class

Objects can be created by using the constructor function [linear](#).

Slots

Let k denote the number of products produced by all firms.

intercepts: A length k vector of demand intercepts.

prices: A length k vector product prices.

quantities: A length k vector of product quantities.

margins: A length k vector of product margins. All margins must be between 0 and 1.

diversion: A $k \times k$ matrix of diversion ratios with diagonal elements equal to 1.

priceStart: A length k vector of prices used as the initial guess in the nonlinear equation solver.

symmetry: If TRUE, requires the matrix of demand slope coefficients to be consistent with utility maximization theory.

Extends

Class [Bertrand](#), directly. Class [Antitrust](#), by class [Bertrand](#), distance 2.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcPrices` signature(object, preMerger = TRUE, ...) Compute either pre-merger or post-merger equilibrium prices under the assumptions that consumer demand is Logit and firms play a differentiated product Bertrand Nash pricing game. ‘...’ may be used to change the default values of `constrOptim`, the non-linear equation solver used to enforce non-negative equilibrium quantities.

`calcPriceDeltaHypoMon` signature(object, prodIndex, ...) Calculates the price changes that a Hypothetical Monopolist would impose on its products relative to pre-merger prices.

`calcQuantities` signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium quantities under the assumptions that consumer demand is Linear and firms play a differentiated product Bertrand Nash pricing game.

`calcShares` signature(object, preMerger = TRUE, revenue = FALSE) Compute either pre-merger or post-merger equilibrium quantity shares under the assumptions that consumer demand is Linear and firms play a differentiated product Bertrand Nash pricing game.

`calcSlopes` signature(object) Uncover slopes and intercept from a Linear demand system. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

`CV` signature(object = "Linear") Calculate the amount of money a representative consumer would need to be paid to be just as well off as they were before the merger.

`elast` signature(object, preMerger = TRUE) Computes a $k \times k$ matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Linear")           # get a detailed description of the class
showMethods(classes="Linear") # show all methods defined for the class
```

```
logit                        (Nested) Logit Demand Calibration and Merger Simulation
```

Description

Calibrates consumer demand using (Nested) Logit and then simulates the price effect of a merger between two firms under the assumption that all firms in the market are playing a differentiated products Bertrand pricing game.

Usage

```
logit(prices, shares, margins,
      ownerPre, ownerPost,
      normIndex=ifelse(isTRUE(all.equal(sum(shares), 1,
                                         check.names=FALSE)), 1, NA),
      mcDelta=rep(0, length(prices)),
      subset=rep(TRUE, length(prices)),
      insideSize = NA_real_,
      priceOutside = 0,
      priceStart = prices,
      isMax=FALSE,
      control.slopes,
      control.equ,
      labels=paste("Prod", 1:length(prices), sep=""),
      ...
)
logit.alm(prices, shares, margins,
         ownerPre, ownerPost,
         mktElast = NA_real_,
         insideSize = NA_real_,
         mcDelta=rep(0, length(prices)),
         subset=rep(TRUE, length(prices)),
         priceOutside = 0,
         priceStart = prices,
         isMax=FALSE,
         parmsStart,
         control.slopes,
         control.equ,
         labels=paste("Prod", 1:length(prices), sep=""),
         ...
)
logit.nests(prices, shares, margins,
```

```

ownerPre,ownerPost,
nests=rep(1,length(shares)),
normIndex=ifelse(sum(shares) < 1,NA,1),
mcDelta=rep(0,length(prices)),
subset=rep(TRUE, length(prices)),
priceOutside = 0,
priceStart = prices,
isMax=FALSE,
constraint = TRUE,
parmsStart,
control.slopes,
control.equ,
labels=paste("Prod",1:length(prices),sep=""),
...
)

```

```

logit.nests.alm(prices,shares,margins,
ownerPre,ownerPost,
nests=rep(1,length(shares)),
mcDelta=rep(0,length(prices)),
subset=rep(TRUE, length(prices)),
priceOutside = 0,
priceStart = prices,
isMax=FALSE,
constraint = TRUE,
parmsStart,
control.slopes,
control.equ,
labels=paste("Prod",1:length(prices),sep=""),
...
)

```

```

logit.cap(prices,shares,margins,
ownerPre,ownerPost,
capacitiesPre=rep(Inf,length(prices)),
capacitiesPost=capacitiesPre,
insideSize,
normIndex=ifelse(sum(shares)<1,NA,1),
mcDelta=rep(0,length(prices)),
subset=rep(TRUE, length(prices)),
priceOutside = 0,
priceStart = prices,
isMax=FALSE,
control.slopes,
control.equ,
labels=paste("Prod",1:length(prices),sep=""),
...
)

```

```

logit.cap.alm(prices,shares,margins,
              ownerPre,ownerPost,
              capacitiesPre=rep(Inf,length(prices)),
              capacitiesPost=capacitiesPre,
              mktElast = NA_real_,
              insideSize,
              mcDelta=rep(0,length(prices)),
              subset=rep(TRUE,length(prices)),
              priceOutside = 0,
              priceStart = prices,
              isMax=FALSE,
              parmsStart,
              control.slopes,
              control.equ,
              labels=paste("Prod",1:length(prices),sep=""),
              ...
)

```

Arguments

	Let k denote the number of products produced by all firms playing the Bertrand pricing game.
prices	A length k vector of product prices.
shares	A length k vector of product (quantity) shares. Values must be between 0 and 1.
margins	A length k vector of product margins, some of which may equal NA.
nests	A length k vector identifying the nest that each product belongs to.
capacitiesPre	A length k vector of pre-merger product capacities. Capacities must be at least as great as shares * insideSize.
capacitiesPost	A length k vector of post-merger product capacities.
insideSize	An integer equal to total pre-merger units sold. If shares sum to one, this also equals the size of the market.
normIndex	An integer equalling the index (position) of the inside product whose mean valuation will be normalized to 1. Default is 1, unless 'shares' sum to less than 1, in which case the default is NA and an outside good is assumed to exist.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product pre-merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a $k \times k$ matrix of post-merger ownership shares.
mktElast	a negative value indicating market elasticity. Default is NA.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.

subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
constraint	if TRUE, then the nesting parameters for all non-singleton nests are assumed equal. If FALSE, then each non-singleton nest is permitted to have its own value. Default is TRUE.
priceOutside	A length 1 vector indicating the price of the outside good. Default is 0.
priceStart	A length k vector of starting values used to solve for equilibrium price. Default is the 'prices' vector.
isMax	If TRUE, checks to see whether computed price equilibrium locally maximizes firm profits and returns a warning if not. Default is FALSE.
parmsStart	For <code>logit.cap.alm</code> , a length-2 vector of starting values used to solve for the price coefficient and outside share (in that order). For <code>logit.nests</code> , the first element should always be the price coefficient and the remaining elements should be the nesting parameters. Theory requires the nesting parameters to be greater than the price coefficient. If missing then the random draws with the appropriate restrictions are employed.
control.slopes	A list of <code>optim</code> control parameters passed to the calibration routine optimizer (typically the <code>calcSlopes</code> method).
control.equ	A list of <code>BBsolve</code> control parameters passed to the non-linear equation solver (typically the <code>calcPrices</code> method).
labels	A k-length vector of labels. Default is "Prod#", where '#' is a number between 1 and the length of 'prices'.
...	Additional options to feed to the <code>BBsolve</code> optimizer used to solve for equilibrium prices.

Details

Using product prices, quantity shares and all of the product margins from at least one firm, `logit` is able to recover the price coefficient and product mean valuations in a Logit demand model. `logit` then uses these calibrated parameters to simulate a merger between two firms.

`logit.alm` is identical to `logit` except that it assumes that an outside product exists and uses additional margin information to estimate the share of the outside good. If market elasticity is known, it may be supplied using the 'mktElast' argument.

`logit.nests` is identical to `logit` except that it includes the 'nests' argument which may be used to assign products to different nests. Nests are useful because they allow for richer substitution patterns between products. Products within the same nest are assumed to be closer substitutes than products in different nests. The degree of substitutability between products located in different nests is controlled by the value of the nesting parameter sigma. The nesting parameters for singleton nests (nests containing only one product) are not identified and normalized to 1. The vector of sigmas is calibrated from the prices, revenue shares, and margins supplied by the user.

By default, all non-singleton nests are assumed to have a common value for sigma. This constraint may be relaxed by setting 'constraint' to FALSE. In this case, at least one product margin must be supplied from a product within each nest.

`logit.nests.alm` is identical to `logit.nests` except that it assumes that an outside product exists and uses additional margin information to estimate the share of the outside good.

`logit.cap` is identical to `logit` except that firms are playing the Bertrand pricing game under exogenously supplied capacity constraints. Unlike `logit`, `logit.cap` requires users to specify capacity constraints via ‘capacities’ and the number of potential customers in a market via ‘mktSize’. ‘mktSize’ is needed to transform ‘shares’ into quantities that must be directly compared to ‘capacities’.

In `logit`, `logit.nests` and `logit.cap`, if quantity shares sum to 1, then one product’s mean value is not identified and must be normalized to 0. ‘normIndex’ may be used to specify the index (position) of the product whose mean value is to be normalized. If the sum of revenue shares is less than 1, both of these functions assume that there exists a $k+1$ st product in the market whose price and mean value are both normalized to 0.

Value

`logit` returns an instance of class `Logit`. `logit.alm` returns an instance of `LogitALM`, a child class of `Logit`. `logit.nests` returns an instance of `LogitNests`, a child class of `Logit`. `logit.cap` returns an instance of `LogitCap`, a child class of `Logit`.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

References

Anderson, Simon, Palma, Andre, and Francois Thisse (1992). *Discrete Choice Theory of Product Differentiation*. The MIT Press, Cambridge, Mass.

Epstein, Roy and Rubinfeld, Daniel (2004). “Effects of Mergers Involving Differentiated Products.”

Werden, Gregory and Froeb, Luke (1994). “The Effects of Mergers in Differentiated Products Industries: Structural Merger Policy and the Logit Model”, *Journal of Law, Economics, & Organization*, **10**, pp. 407-426.

Froeb, Luke, Tschantz, Steven and Phillip Crooke (2003). “Bertrand Competition and Capacity Constraints: Mergers Among Parking Lots”, *Journal of Econometrics*, **113**, pp. 49-67.

Froeb, Luke and Werden, Greg (1996). “Computational Economics and Finance: Modeling and Analysis with Mathematica, Volume 2.” In Varian H (ed.), chapter Simulating Mergers among Noncooperative Oligopolists, pp. 177-95. Springer-Verlag, New York.

See Also

[ces](#)

Examples

```
## Calibration and simulation results from a merger between Budweiser and
## Old Style.
## Source: Epstein/Rubinfeld 2004, pg 80
```

```

prodNames <- c("BUD", "OLD STYLE", "MILLER", "MILLER-LITE", "OTHER-LITE", "OTHER-REG")
ownerPre <-c("BUD", "OLD STYLE", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
ownerPost <-c("BUD", "BUD", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
nests <- c("Reg", "Reg", "Reg", "Light", "Light", "Reg")

price <- c(.0441, .0328, .0409, .0396, .0387, .0497)
shares <- c(.066, .172, .253, .187, .099, .223)
margins <- c(.3830, .5515, .5421, .5557, .4453, .3769)

insideSize <- 1000

names(price) <-
  names(shares) <-
  names(margins) <-
  prodNames

result.logit <- logit(price, shares, margins,
  ownerPre=ownerPre, ownerPost=ownerPost,
  insideSize = insideSize,
  labels=prodNames)

print(result.logit)          # return predicted price change
summary(result.logit)       # summarize merger simulation

elast(result.logit, TRUE)   # returns premerger elasticities
elast(result.logit, FALSE) # returns postmerger elasticities

diversion(result.logit, TRUE) # return premerger diversion ratios
diversion(result.logit, FALSE) # return postmerger diversion ratios

cmcr(result.logit)          #calculate compensating marginal cost reduction
upp(result.logit)           #calculate Upwards Pricing Pressure Index

CV(result.logit)            #calculate representative agent compensating variation

## Implement the Hypothetical Monopolist Test
## for BUD and OLD STYLE using a 5% SSNIP

HypoMonTest(result.logit, prodIndex=1:2)

## Get a detailed description of the 'Logit' class slots
showClass("Logit")

## Show all methods attached to the 'Logit' Class
showMethods(classes="Logit")

```

```
## Show which classes have their own 'elast' method
showMethods("elast")

## Show the method definition for 'elast' and Class 'Logit'
getMethod("elast", "Logit")

#
# Logit With capacity Constraints
#

cap      <- c(66,200,300,200,99,300) # BUD and OTHER-LITE are capacity constrained
result.cap <- logit.cap(price,shares,margins,capacitiesPre=cap,
                       insideSize=insideSize,ownerPre=ownerPre,
                       ownerPost=ownerPost,labels=prodNames)

print(result.cap)
```

Logit-class

Class "Logit"

Description

The "Logit" class contains all the information needed to calibrate a Logit demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function `logit`.

Slots

Let k denote the number of products produced by all firms.

prices: A length k vector of product prices.

margins: A length k vector of product margins, some of which may equal NA.

normIndex: An integer specifying the product index against which the mean values of all other products are normalized.

shareInside: The share of customers that purchase any of the products included in the 'prices' vector.

priceOutside: The price of the outside good. Default is 0.

slopes: A list containing the coefficient on price ('alpha') and the vector of mean valuations ('meanval')

mktElast: A length 1 vector of market elasticities.

priceStart: A length-k vector of starting prices for the non-linear solver

insideSize: A positive number equal to total pre-merger quantities (revenues for CES) for all products included in the simulation.

mktSize: A positive number equal to total quantities (revenues for CES) pre-merger for all products in the simulations as well as the outside good.

Extends

Class [Bertrand](#), directly. Class [Antitrust](#), by class [Bertrand](#), distance 2.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

calcPrices signature(object = Logit, preMerger = TRUE, isMax=FALSE,...) Compute either pre-merger or post-merger equilibrium prices under the assumptions that consumer demand is Logit and firms play a differentiated product Bertrand Nash pricing game. When isMax equals TRUE, a check is run to determine if the calculated equilibrium price vector locally maximizes profits. ‘...’ may be used to change the default values of [BBsolve](#), the non-linear equation solver.

calcPriceDeltaHypoMon signature(object = Logit, prodIndex,...) Calculates the price changes that a Hypothetical Monopolist would impose on its products relative to pre-merger prices.

calcShares signature(object = Logit, preMerger = TRUE, revenue = FALSE) Compute either pre-merger or post-merger equilibrium shares under the assumptions that consumer demand is Logit and firms play a differentiated product Bertrand Nash pricing game. ‘revenue’ takes on a value of TRUE or FALSE, where TRUE calculates revenue shares, while FALSE calculates quantity shares.

calcSlopes signature(object = Logit) Uncover Logit demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

CV signature(object = Logit) Calculate the amount of money a representative consumer would need to be paid to be just as well off as they were before the merger.

elast signature(object = Logit, preMerger = TRUE) Computes a k x k matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Logit")           # get a detailed description of the class
showMethods(classes="Logit") # show all methods defined for the class
```

LogitALM-class	Class "LogitALM"
----------------	------------------

Description

The "LogitALM" class contains all the information needed to calibrate a Logit demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game with unknown market elasticity.

Objects from the Class

Objects can be created by using the constructor function `logit.alm`.

Slots

parmsStart: A length 2 vector whose first element equals an initial guess of the price coefficient and whose second element equals an initial guess of the outside share. The price coefficient's initial value must be negative and the outside share's initial value must be between 0 and 1 .

Extends

Class `Logit`, directly. Class `Bertrand`, by class `Logit`, distance 2. Class `Antitrust`, by class `Bertrand`, distance 3.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcSlopes signature(object)` Uncover Logit ALM demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game with capacity constraints.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("LogitALM")           # get a detailed description of the class
showMethods(classes="LogitALM") # show all methods defined for the class
```

 LogitCap-class

 Class “LogitCap” and “LogitCapALM”

Description

The “LogitCap” class contains all the information needed to calibrate a Logit demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game with capacity constraints. “LogitCapALM” extends “LogitCap” to allow for an unobserved outside share.

Objects from the Class

Objects can be created by using the constructor function `logit.cap` and `logit.cap.alm`.

Slots

Let k denote the number of products produced by all firms.

`capacitiesPre`: A length k vector whose elements equal pre-merger product capacities.

`capacitiesPost`: A length k vector whose elements equal post-merger product capacities.

Extends

Class `Logit`, directly. Class `Bertrand`, by class `Logit`, distance 2. Class `Antitrust`, by class `Bertrand`, distance 3.

Methods

For all of methods containing the ‘preMerger’ argument, ‘preMerger’ takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

`calcPrices` signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium shares under the assumptions that consumer demand is Logit and firms play a differentiated product Bertrand Nash pricing game with capacity constraints.

`calcQuantities` signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium quantities under the assumptions that consumer demand is Linear and firms play a differentiated product Bertrand Nash pricing game.

`calcMargins` signature(object, preMerger = TRUE) Computes equilibrium product margins assuming that firms are playing a Nash-Bertrand pricing game with capacity constraints. Note that margins for capacity constrained firms are not identified from the firm’s first-order conditions, and so must be supplied by the user.

`calcSlopes` signature(object) Uncover Logit demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game with capacity constraints.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("LogitCap")           # get a detailed description of the class
showMethods(classes="LogitCap") # show all methods defined for the class
```

LogitNests-class *Class "LogitNests"*

Description

The "LogitNests" class contains all the information needed to calibrate a nested Logit demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function [logit.nests](#).

Slots

Let k denote the number of products produced by all firms.

nests: A length k vector identifying the nest that each product belongs to.

parmsStart: A length k vector whose elements equal an initial guess of the nesting parameter values.

constraint: A length 1 logical vector that equals TRUE if all nesting parameters are constrained to equal the same value and FALSE otherwise. Default is TRUE.

Extends

Class [Logit](#), directly. Class [Bertrand](#), by class [Logit](#), distance 2.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

calcShares signature(object, preMerger = TRUE, revenue = FALSE) Compute either pre-merger or post-merger equilibrium shares under the assumptions that consumer demand is Logit and firms play a differentiated product Bertrand Nash pricing game. 'revenue' takes on a value of TRUE or FALSE, where TRUE calculates revenue shares, while FALSE calculates quantity shares.

calcSlopes signature(object) Uncover nested Logit demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

CV signature(object) Calculate the amount of money a representative consumer would need to be paid to be just as well off as they were before the merger.

elast signature(object, preMerger = TRUE) Computes a k x k matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("LogitNests")           # get a detailed description of the class
showMethods(classes="LogitNests") # show all methods defined for the class
```

LogitNestsALM-class *Class "LogitNestsALM"*

Description

The "LogitNestsALM" class contains all the information needed to calibrate a nested Logit demand system under the assumption that the share of the outside product is not known. Once the model parameters have been calibrated, methods exist that perform a merger simulation analysis under the assumption that firms are playing a differentiated products Bertrand pricing game.

Objects from the Class

Objects can be created by using the constructor function `logit.nests.alm`.

Extends

Class `LogitNests`, directly. Class `Logit`, by class `LogitNests`, distance 2. Class `Bertrand`, by class `Logit`, distance 3. Class `Antitrust`, by class `Bertrand`, distance 4.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

calcSlopes signature(object) Uncover nested Logit demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

elast signature(object, preMerger = TRUE) Computes a k x k matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("LogitNestsALM")           # get a detailed description of the class
showMethods(classes="LogitNestsALM") # show all methods defined for the class
```

LogLin-class

Class "LogLin"

Description

The "LogLin" class contains all the information needed to calibrate a Log-Linear demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated Bertrand products pricing game.

Objects from the Class

Objects can be created by using the constructor function [loglin](#).

Slots

symmetry: If TRUE, requires the matrix of demand slope coefficients to be consistent with utility maximization theory Default is FALSE

Extends

Class [Linear](#), directly. Class [Bertrand](#), by class [Linear](#), distance 2. Class [Antitrust](#), by class [Bertrand](#), distance 3.

Methods

For all of methods containing the 'preMerger' argument, 'preMerger' takes on a value of TRUE or FALSE, where TRUE invokes the method using the pre-merger ownership structure, while FALSE invokes the method using the post-merger ownership structure.

[calcPrices](#) signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium prices under the assumptions that consumer demand is Log-Linear and firms play a differentiated product Bertrand Nash pricing game.

[calcPriceDeltaHypoMon](#) signature(object, prodIndex, ...) Calculates the price changes that a Hypothetical Monopolist would impose on its products relative to pre-merger prices.

[calcQuantities](#) signature(object, preMerger = TRUE) Compute either pre-merger or post-merger equilibrium quantities under the assumptions that consumer demand is Log-Linear and firms play a differentiated product Bertrand Nash pricing game.

[calcSlopes](#) signature(object) Uncover slopes and intercept from a Log-Linear demand system. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

[elast](#) signature(object, preMerger = TRUE) Computes a k x k matrix of own and cross-price elasticities.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("LogLin")           # get a detailed description of the class
showMethods(classes="LogLin") # show all methods defined for the class
```

other-methods

Other Useful 'Bertrand' Methods

Description

Methods defined for the 'Bertrand' class and its child classes.

Usage

```
## S4 method for signature 'ANY'
calcShares(object,preMerger=TRUE,revenue=FALSE)
## S4 method for signature 'ANY'
calcQuantities(object,preMerger=TRUE, market=FALSE)
## S4 method for signature 'ANY'
calcRevenues(object,preMerger=TRUE, market=FALSE)
## S4 method for signature 'ANY'
calcPrices(object,preMerger=TRUE,subset,...)
## S4 method for signature 'Antitrust'
calcPriceDelta(object,levels=FALSE,market=FALSE,...)
## S4 method for signature 'AIDS'
calcPriceDelta(object,isMax=FALSE,levels=FALSE,subset,market=FALSE,...)
## S4 method for signature 'Bertrand'
calcProducerSurplus(object,preMerger=TRUE)
## S4 method for signature 'ANY'
calcMargins(object,preMerger=TRUE)
## S4 method for signature 'Bertrand'
calcMC(object,preMerger=TRUE)
## S4 method for signature 'ANY'
calcSlopes(object,preMerger=TRUE)
## S4 method for signature 'Bertrand'
calcDiagnostics(object,labels=object@labels)
## S4 method for signature 'Bertrand'
getParms(object,digits=10)
## S4 method for signature 'Bertrand'
hhi(object,preMerger=TRUE,revenue=FALSE,insideonly=TRUE)
## S4 method for signature 'Antitrust'
ownerToMatrix(object,preMerger=TRUE)
## S4 method for signature 'Antitrust'
ownerToVec(object,preMerger=TRUE)
```

```
## S4 method for signature 'Bertrand'
plot(x,scale=.1)
## S4 method for signature 'Bertrand'
summary(object,revenue=TRUE,shares=TRUE,levels=FALSE,
parameters=FALSE,market=FALSE,insideOnly=TRUE,digits=2,...)
```

Arguments

	Let k denote the number of products
object	An instance of one of the classes listed above.
x	Used only in plot method. Should always be set equal to object
preMerger	If TRUE, returns pre-merger outcome. If FALSE, returns post-merger outcome. Default is TRUE.
isMax	If TRUE, uses numerical derivatives to determine if equilibrium price vector is a local maximum. Default is FALSE.
revenue	If TRUE, returns revenues. If FALSE, returns quantities. Default is TRUE
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
shares	If TRUE, returns shares. If FALSE, returns levels. Default is TRUE
parameters	If TRUE, reports demand and cost parameters. Default is FALSE
levels	If TRUE, report results in levels. If FALSE, report results in percents. Default is FALSE
insideOnly	If TRUE, normalizes sum of inside shares to 1. Default is FALSE
digits	The number of significant digits to round printed results.
scale	The proportion below marginal cost and above equilibrium price that should be plotted. Default is .1
insideonly	If TRUE, excludes the share of the outside good from the calculation. Default is TRUE.
market	If TRUE, reports market-level summary. Otherwise reports product/plant level summary. Default is FALSE
labels	A length- k vector product labels. Default is object@labels
...	Arguments to be passed to non-linear solver, OR for summary to CV.

Methods

calcShares signature(object= c(Linear,AIDS,Logit,LogitNests,CES,CESNests),preMerger=TRUE, revenue=FALSE)
 Computes equilibrium product shares assuming that firms are playing a Nash-Bertrand or Cournot game. 'revenue' takes on a value of TRUE or FALSE, where TRUE calculates revenue shares, while FALSE calculates quantity shares.

- calcQuantities** signature(object=c(AIDS,CES,Cournot,Linear,Logit,LogLin,Logit,LogitCap,Stackelberg),preMerger=TRUE) Computes equilibrium product quantities assuming that firms are playing a Nash-Bertrand, 2nd Score Auction, or Cournot game. Setting 'market' to TRUE returns total market quantity.
- calcRevenues** signature(object=c(Bertrand, AIDS, CES),preMerger=TRUE, market=FALSE) Computes equilibrium product revenues assuming that firms are playing a Nash-Bertrand, 2nd Score Auction, or Cournot game. Setting 'market' to TRUE returns total market revenue.
- calcPrices** signature(object=c(Linear,LogLin,AIDS,Logit,LogitNests,LogitCap,CES,CESNests),preMerger=TRUE) Computes equilibrium product price levels assuming that firms are playing a Nash-Bertrand or Cournot game. '...' may be used to feed additional options to the optimizer responsible for computing equilibrium prices. Typically, [BBSolve](#) is used, but see the appropriate document for further details.
- calcPriceDelta** signature(object=Antitrust, market=FALSE, ...) Computes equilibrium price changes due to a merger assuming that firms are playing a Nash-Bertrand or Cournot game. This is a wrapper method for computing the difference between pre- and post-merger equilibrium prices
- calcPriceDelta** signature(object=AIDS,isMax=FALSE,subset,market=FALSE,...) Computes equilibrium price changes due to a merger assuming that firms are playing a Nash-Bertrand or Cournot game and LA-AIDS. This method calls a non-linear equations solver to find a sequence of price changes that satisfy the Bertrand FOCs.
- calcProducerSurplus** signature(object=Bertrand,preMerger=TRUE) Computes equilibrium producer surplus.
- calcMargins** signature(object=c(Bertrand,LogitCap),preMerger=TRUE) Computes equilibrium product margins assuming that firms are playing a Nash-Bertrand or Cournot game. For "LogitCap", assumes firms are playing a Nash-Bertrand or Cournot game with capacity constraints.
- calcDiagnostics** signature(object=c(Bertrand,Cournot),labels) Computes the percentage difference between predicted and observed pre-merger prices, shares, margins and market elasticities (if supplied). 'labels' is used to specify row labels.
- calcVC** signature(object=Cournot,preMerger=TRUE) Computes either pre- or post-merger variable costs. Variable costs are assumed to be quadratic by default. Post-merger variable costs are equal to pre-merger variable costs multiplied by 1+'mcDelta', a length-k vector of marginal cost changes. 'mcDelta' will typically be between 0 and 1.
- calcMC** signature(object=Bertrand,preMerger=TRUE) Computes either pre- or post-merger marginal costs. Marginal costs are assumed to be constant. Post-merger marginal costs are equal to pre-merger marginal costs multiplied by 1+'mcDelta', a length-k vector of marginal cost changes. 'mcDelta' will typically be between 0 and 1.
- calcdMC** signature(object=Cournot,preMerger=TRUE) Computes the derivative of either pre- or post-merger marginal costs. the derivative of Marginal costs is assumed to be constant. Post-merger marginal costs are equal to pre-merger marginal costs multiplied by 1+'mcDelta', a length-k vector of marginal cost changes. 'mcDelta' will typically be between 0 and 1.
- calcSlopes** signature(object=c(Linear,LogLin,AIDS,PCAIDSNests,Logit,LogitNests,LogitCap,CES,CESNests),preMerger=TRUE) Computes demand parameters assuming that firms are playing a Nash-Bertrand or Cournot game.
- getParms** signature(object=Bertrand,digits=10) Returns a list of model-specific demand parameters. 'digits' specifies the number of significant digit to return (default 10).

- hhi** signature(object=Bertrand,preMerger=TRUE,revenue=FALSE, insideonly=TRUE)
Computes the Herfindahl-Hirschman Index (HHI) using simulated market shares and either pre- or post-merger ownership information. Outside shares are excluded from the calculation.
- ownerToMatrix** signature(object=Antitrust,preMerger=TRUE)
converts a length-k ownership vector into a k x k ownership matrix where element i,j equals 1 if products i and j are commonly owned, and 0 otherwise.
- ownerToVec** signature(object=Antitrust,preMerger=TRUE)
converts a k x k ownership matrix into a length-k ownership vector
- plot** signature(x,scale=.1) Use [ggplot](#) to plot pre- and post-merger demand, marginal cost and equilibria. 'scale' controls the amount above marginal cost and below equilibrium price that is plotted.
- show** signature(object=Antitrust) Displays the percentage change in prices due to the merger.
- summary** signature(object=c(Bertrand,AIDS),revenue=TRUE,shares=TRUE,parameters=FALSE,digits=2,...)
Summarizes the effect of the merger, including price and revenue changes. Setting 'revenue' equal to FALSE reports quantities rather than revenues. Setting 'shares' to FALSE reports quantities rather than than shares (when possible). Setting 'parameters' equal to TRUE reports all demand parameters. 'digits' controls the number of significant digits reported in output. '...' allows other arguments to be passed to a CV method.
- upp** signature(object) Calculate the Upwards Pricing Pressure (upp) index.

PCAIDS-class

Class "PCAIDS"

Description

The "PCAIDS" class contains all the information needed to calibrate a PCAIDS demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated Bertrand products pricing game.

Objects from the Class

Objects can be created by using the constructor [pcaids](#).

Slots

Let k denote the number of products produced by all firms.

knownElast: A negative number equal to the pre-merger own-price elasticity for any of the k products.

knownElastIndex: An integer equal to the position of the 'knownElast' product in the 'shares' vector.

Extends

Class [AIDS](#), directly. Class [Linear](#), by class [AIDS](#), distance 2. Class [Bertrand](#), by class [Linear](#), distance 3. Class [Antitrust](#), by class [Bertrand](#), distance 4.

Methods

`calcSlopes signature(object)` Uncover nested CES demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("PCAIDS")           # get a detailed description of the class
showMethods(classes="PCAIDS") # show all methods defined for the class
```

PCAIDSNests-class *Class "PCAIDSNests"*

Description

The "PCAIDSNests" class contains all the information needed to calibrate a nested PCAIDS demand system and perform a merger simulation analysis under the assumption that firms are playing a differentiated Bertrand products pricing game.

Objects from the Class

Objects can be created by using the constructor `pcaids.nests`.

Slots

Let k denote the number of products produced by all firms.

`nests`: A length k vector identifying which nest a product belongs to.

`nestsParms`: A length k vector containing nesting parameters.

Extends

Class `PCAIDS`, directly. Class `AIDS`, by class `PCAIDS`, distance 2. Class `Linear`, by class `AIDS`, distance 3. Class `Bertrand`, by class `Linear`, distance 4. Class `Antitrust`, by class `Bertrand`, distance 5.

Methods

`calcSlopes signature(object)` Uncover nested CES demand parameters. Assumes that firms are currently at equilibrium in a differentiated product Bertrand Nash pricing game.

`getNestsParms signature(object)` Returns a matrix containing the calibrated nesting parameters.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("PCAIDSNests")          # get a detailed description of the class
showMethods(classes="PCAIDSNests") # show all methods defined for the class
```

 sim

Merger Simulation With User-Supplied Demand Parameters

Description

Simulates the price effects of a merger between two firms with user-supplied demand parameters under the assumption that all firms in the market are playing a differentiated products Bertrand pricing game.

Usage

```
sim(prices,
    demand=c( "Linear", "AIDS", "LogLin",
              "Logit", "CES", "LogitNests",
              "CESNests", "LogitCap"),
    demand.param,
    ownerPre, ownerPost, nests, capacities,
    mcDelta=rep(0, length(prices)),
    subset=rep(TRUE, length(prices)),
    priceOutside,
    priceStart,
    labels=paste("Prod", 1:length(prices), sep=""), ...
)
```

Arguments

	Let k denote the number of products produced by all firms.
prices	A length k vector of product prices.
demand	A character string indicating the type of demand system to be used in the merger simulation. Supported demand systems are linear ('Linear'), log-linear ('LogLin'), logit ('Logit'), nested logit ('LogitNests'), ces ('CES'), nested CES ('CESNests') and capacity constrained Logit ('LogitCap').
demand.param	See Below.
ownerPre	EITHER a vector of length k whose values indicate which firm produced a product pre-merger OR a $k \times k$ matrix of pre-merger ownership shares.
ownerPost	EITHER a vector of length k whose values indicate which firm produced a product after the merger OR a $k \times k$ matrix of post-merger ownership shares.

nests	A length k vector identifying the nest that each product belongs to. Must be supplied when 'demand' equals 'CESNests' and 'LogitNests'.
capacities	A length k vector of product capacities. Must be supplied when 'demand' equals 'LogitCap'.
mcDelta	A vector of length k where each element equals the proportional change in a product's marginal costs due to the merger. Default is 0, which assumes that the merger does not affect any products' marginal cost.
subset	A vector of length k where each element equals TRUE if the product indexed by that element should be included in the post-merger simulation and FALSE if it should be excluded. Default is a length k vector of TRUE.
priceOutside	A length 1 vector indicating the price of the outside good. This option only applies to the 'Logit' class and its child classes. Default for 'Logit', 'LogitNests', and 'LogitCap' is 0, and for 'CES' and 'CesNests' is 1.
priceStart	A length k vector of starting values used to solve for equilibrium price. Default is the 'prices' vector for all values of demand except for 'AIDS', which is set equal to a vector of 0s.
labels	A k-length vector of labels. Default is "Prod#", where '#' is a number between 1 and the length of 'prices'.
...	Additional options to feed to the optimizer used to solve for equilibrium prices.

Details

Using user-supplied demand parameters, *sim* simulates the effects of a merger in a market where firms are playing a differentiated products pricing game.

If 'demand' equals 'Linear', 'LogLin', or 'AIDS', then 'demand.param' must be a list containing 'slopes', a $k \times k$ matrix of slope coefficients, and 'intercepts', a length-k vector of intercepts. Additionally, if 'demand' equals 'AIDS', 'demand.param' must contain 'mktElast', an estimate of aggregate market elasticity. For 'Linear' demand models, *sim* returns an error if any intercepts are negative, and for both 'Linear', 'LogLin', and 'AIDS' models, *sim* returns an error if not all diagonal elements of the slopes matrix are negative.

If 'demand' equals 'Logit' or 'LogitNests', then 'demand.param' must equal a list containing

- alpha The price coefficient.
- meanval A length-k vector of mean valuations 'meanval'. If none of the values of 'meanval' are zero, an outside good is assumed to exist.

If demand equals 'CES' or 'CESNests', then 'demand.param' must equal a list containing

- gamma The price coefficient,
- alpha The coefficient on the numeraire good. May instead be calibrated using 'shareInside',
- meanval A length-k vector of mean valuations 'meanval'. If none of the values of 'meanval' are zero, an outside good is assumed to exist,
- shareInside The budget share of all products in the market. Default is 1, meaning that all consumer wealth is spent on products in the market. May instead be specified using 'alpha'.

Value

sim returns an instance of the class specified by the ‘demand’ argument.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

See Also

The S4 class documentation for: [Linear](#), [AIDS](#), [LogLin](#), [Logit](#), [LogitNests](#), [CES](#), [CESNests](#)

Examples

```
## Calibration and simulation results from a merger between Budweiser and
## Old Style. Note that the in the following model there is no outside
## good; BUD's mean value has been normalized to zero.

## Source: Epstein/Rubinfeld 2004, pg 80

prodNames <- c("BUD", "OLD STYLE", "MILLER", "MILLER-LITE", "OTHER-LITE", "OTHER-REG")
ownerPre <-c("BUD", "OLD STYLE", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
ownerPost <-c("BUD", "BUD", "MILLER", "MILLER", "OTHER-LITE", "OTHER-REG")
nests <- c("Reg", "Reg", "Reg", "Light", "Light", "Reg")

price <- c(.0441, .0328, .0409, .0396, .0387, .0497)

demand.param=list(alpha=-48.0457,
                  meanval=c(0,0.4149233,1.1899885,0.8252482,0.1460183,1.4865730)
                  )

sim.logit <- sim(price,demand="Logit",demand.param,ownerPre=ownerPre,ownerPost=ownerPost)

print(sim.logit)           # return predicted price change
summary(sim.logit)        # summarize merger simulation

elast(sim.logit,TRUE)     # returns premerger elasticities
elast(sim.logit,FALSE)   # returns postmerger elasticities

diversion(sim.logit,TRUE) # return premerger diversion ratios
diversion(sim.logit,FALSE) # return postmerger diversion ratios

cmcr(sim.logit)           #calculate compensating marginal cost reduction
upp(sim.logit)           #calculate Upwards Pricing Pressure Index

CV(sim.logit)            #calculate representative agent compensating variation
```

Stackelberg-class *Class "Stackelberg"*

Description

The "Stackelberg" class is a building block used to create other classes in this package. As such, it is most likely to be useful for developers who wish to code their own merger calibration/simulation routines.

Objects from the Class

Objects can be created by calls of the form `new("Stackelberg", ...)`.

Slots

Let k denote the number of products and n denote the number of plants.

dmcfunPre: A length n list whose elements equal a function that calculates the derivative of a plant's pre-merger marginal cost with respect to that plant's output.

dmcfunPost: A length n list whose elements equal a function that calculates the derivative of a plant's post-merger marginal cost with respect to that plant's output.

isLeaderPre: An $n \times k$ logical matrix whose elements are TRUE if a plant produces a product pre-merger and FALSE otherwise.

isLeaderPost: An $n \times k$ logical matrix whose elements are TRUE if a plant produces a product post-merger and FALSE otherwise.

Extends

Class [Cournot](#), directly. Class [Bertrand](#), by class [Cournot](#), distance 2. Class [Antitrust](#), by class [Bertrand](#), distance 3.

Author(s)

Charles Taragin <charles.taragin@usdoj.gov>

Examples

```
showClass("Stackelberg")           # get a detailed description of the class
showMethods(classes="Stackelberg") # show all methods defined for the class
```

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