Package ‘bifurcatingr’

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Title Bifurcating Autoregressive Models

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Description Estimation of bifurcating autoregressive models of any order, p, BAR(p) as well as several types of bias correction for the least squares estimators of the autoregressive parameters as described in Zhou and Basawa (2005) <doi:10.1016/j.spl.2005.04.024> and Elbayoumi and Mostafa (2020) <doi:10.1002/sta4.342>. Currently, the bias correction methods supported include bootstrap (single, double and fast-double) bias correction and linear-bias-function-based bias correction. Functions for generating and plotting bifurcating autoregressive data from any BAR(p) model are also included. This new version includes calculating several type of bias-corrected and -uncorrected confidence intervals for the least squares estimators of the autoregressive parameters as described in Elbayoumi and Mostafa (2023) <doi:10.6339/23-JDS1092>.

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R topics documented:

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**bfa.boot.ci**

**Standard Normal Bootstrap Confidence Interval Function**

**Description**

This function calculates the standard normal bootstrap CI for the least squares estimator of the bifurcating autoregressive model.

**Usage**

```r
bfa.boot.ci(a1.ls, a1.ls.star, conf.level = 0.95)
```

**Arguments**

- `a1.ls` A numeric value of the least squares estimator of bifurcating autoregressive model
- `a1.ls.star` A numeric vector representing B replicates of the least squares estimator
- `conf.level` A numeric value representing the confidence level. Defaults to 0.95.

**Value**

A numeric vector representing the lower and upper limits of the confidence interval

**Examples**

```r
a1.ls <- 0.7
a1.ls.star <- c(rnorm(100,0.7,0.05))
bfa.boot.ci(a1.ls, a1.ls.star, conf.level= 0.95)
```
Description

This function performs linear-bias-function bias-correction (LBC), single bootstrap, double bootstrap, fast-double bootstrap, and double-bootstrap of the bias-correction least squares estimators of the autoregressive coefficients in a bifurcating autoregressive (BAR) model of any order $p$ as described in Elbayoumi & Mostafa (2020).

Usage

```
    bfa.boot.ls.bc(
        z,  # a numeric vector containing the tree data
        p,  # an integer determining the order of bifurcating autoregressive model to be fit to the data
        method = "boot1",  # method of bias correction. Currently, "boot1", "boot2", "boot2fast" and "LBC" are supported and they implement single bootstrap, double bootstrap, fast-double bootstrap, and linear-bias-function bias-correction, respectively.
        burn = 5,  # number of tree generations to discard before starting the bootstrap sample (replicate)
        B,  # number of bootstrap samples (replicates)
        boot.est = TRUE,  # a logical that determines whether the bootstrapped least squares estimates of the autoregressive coefficients should be returned. Defaults to TRUE.
        boot.data = FALSE  # a logical that determines whether the bootstrap samples should be returned. Defaults to FALSE.
    )
```

Arguments

- **z**: a numeric vector containing the tree data
- **p**: an integer determining the order of bifurcating autoregressive model to be fit to the data
- **method**: method of bias correction. Currently, "boot1", "boot2", "boot2fast" and "LBC" are supported and they implement single bootstrap, double bootstrap, fast-double bootstrap, and linear-bias-function bias-correction, respectively.
- **burn**: number of tree generations to discard before starting the bootstrap sample (replicate)
- **B**: number of bootstrap samples (replicates)
- **boot.est**: a logical that determines whether the bootstrapped least squares estimates of the autoregressive coefficients should be returned. Defaults to TRUE.
- **boot.data**: a logical that determines whether the bootstrap samples should be returned. Defaults to FALSE.

Value

- **boot.bcest**: a matrix containing the bootstrapped bias-correction least squares estimates of the autoregressive coefficients
- **boot.data**: a matrix containing the bootstrap samples used
References


Examples

```r
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.boot.ls.bc(z, p=1, method="LBC", B=500)
hist(bfa.boot.ls.bc(z, p=1, method="LBC", B=500)$boot.bcest)
```

---

bfa.boot1.ls  
Single Bootstrap of Least Squares Estimators of BAR(p) Models

Description

This function performs single bootstrapping of the least squares estimators of the autoregressive coefficients in a bifurcating autoregressive (BAR) model of any order \( p \) as described in Elbayoumi and Mostafa (2020).

Usage

```r
bfa.boot1.ls(z, p, burn = 5, B, boot.est = TRUE, boot.data = FALSE)
```

Arguments

- **z**: a numeric vector containing the tree data
- **p**: an integer determining the order of bifurcating autoregressive model to be fit to the data
- **burn**: number of tree generations to discard before starting the bootstrap sample (replicate)
- **B**: number of bootstrap samples (replicates)
- **boot.est**: a logical that determines whether the bootstrapped least squares estimates of the autoregressive coefficients should be returned. Defaults to TRUE.
- **boot.data**: a logical that determines whether the bootstrap samples should be returned. Defaults to FALSE.

Value

- **boot.est**: a matrix containing the bootstrapped least squares estimates of the autoregressive coefficients
- **boot.data**: a matrix containing the bootstrap samples used

References

Examples

```r
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.boot1.ls(z, p=1, B=999)
```

**bfa.boot2.ls**  
*Double Bootstrap of Least Squares Estimators of BAR(p) Models*

**Description**

This function performs double bootstrapping of the least squares estimators of the autoregressive coefficients in a bifurcating autoregressive (BAR) model of any order \( p \) as described in Elbayoumi and Mostafa (2020).

**Usage**

```r
bfa.boot2.ls(z, p, burn = 5, B1, B2)
```

**Arguments**

- `z`: a numeric vector containing the tree data
- `p`: an integer determining the order of bifurcating autoregressive model to be fit to the data
- `burn`: number of tree generations to discard before starting the bootstrap sample (replicate)
- `B1`: number of bootstrap samples (replicates) used in first round of bootstrapping
- `B2`: number of bootstrap samples (replicates) used in second round of bootstrapping

**Value**

- `boot.est`: a matrix containing the first-stage bootstrapped least squares estimates of the autoregressive coefficients
- `boot2`: a matrix containing the second-stage bootstrapped least squares estimates of the autoregressive coefficients

**References**


**Examples**

```r
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.boot2.ls(z, p=1, B1=99, B2=9)
```
**bfa.boot2fast.ls**  
*Fast Double Bootstrap of Least Squares Estimators of BAR(p) Models*

**Description**

This function performs fast double bootstrapping of the least squares estimators of the autoregressive coefficients in a bifurcating autoregressive (BAR) model of any order \( p \) as described in Elbayoumi and Mostafa (2020).

**Usage**

```
bfa.boot2fast.ls(z, p, burn = 5, B)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>z</code></td>
<td>a numeric vector containing the tree data</td>
</tr>
<tr>
<td><code>p</code></td>
<td>an integer determining the order of bifurcating autoregressive model to be fit to the data</td>
</tr>
<tr>
<td><code>burn</code></td>
<td>number of tree generations to discard before starting the bootstrap sample (replicate)</td>
</tr>
<tr>
<td><code>B</code></td>
<td>number of bootstrap samples (replicates) used in first round of bootstrapping</td>
</tr>
</tbody>
</table>

**Value**

- `boot.est`: a matrix containing the first-stage bootstrapped least squares estimates of the autoregressive coefficients
- `boot2`: a matrix containing the second-stage bootstrapped least squares estimates of the autoregressive coefficients

**References**


**Examples**

```
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.boot2fast.ls(z, p=1, B=499)
```
bfa.lbc.ls  

*Linear Function Bias-Corrected Estimators for BAR(p); p=1,2,...,6*

**Description**

This function performs bias correction on the least squares estimators of the autoregressive coefficients in a BAR(p) model based on the assumption that the bias of the least squares estimator is approximately linear as a function of the parameter as described in Elbayoumi and Mostafa (2020).

**Usage**

```r
bfa.lbc.ls(z, p)
```

**Arguments**

- `z`: a numeric vector containing the tree data
- `p`: an integer determining the order of bifurcating autoregressive model to be fit to the data

**Value**

- `coef.lbc`: linear-bias-function-based bias-corrected least squares estimates of the autoregressive coefficients

**References**


**Examples**

```r
z <- bfa.tree.gen(127, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.lbc.ls(z, p=1)
```

```
z <- bfa.tree.gen(127, 2, 1, 1, 0.5, 0.5, 0, 10, c(0.5, 0.3))
bfa.lbc.ls(z, p=2)
```

---

bfa.ls  

*Least Squares Estimation of Bifurcating Autoregressive Models*

**Description**

This function performs Least Squares estimation of bifurcating autoregressive (BFA) models of any order as described in Zhou and Basawa (2005).
Usage

bfa.ls(
    z, p,
    x.data = FALSE, y.data = FALSE, resids = FALSE,
    error.cor = TRUE, error.var = FALSE,
    conf = FALSE, conf.level = 0.95,
    B = 49, p.value = FALSE
)

Arguments

z a numeric vector containing the tree data
p an integer determining the order of bifurcating autoregressive model to be fit to the data
x.data a logical that determines whether the x data used in fitting the model should be returned. Defaults to FALSE.
y.data a logical that determines whether the y data used in fitting the model should be returned. Defaults to FALSE.
resids a logical that determines whether the model residuals should be returned. Defaults to FALSE.
error.cor a logical that determines whether the estimated correlation between pairs of model errors ($e_{2t}, e_{2t+1}$) should be returned. Defaults to TRUE.
error.var a logical that determines whether the estimated variance of the model errors should be returned. Defaults to FALSE.
cov.matrix a logical that determines whether the estimated variance-covariance matrix of the least squares estimates should be returned. Defaults to FALSE.
conf a logical that determines whether confidence intervals for model coefficients should be returned. Defaults to FALSE. If TRUE, asymptotic normal confidence intervals for the intercept and the slopes are calculated using cov.matrix. In addition, normal bootstrap confidence interval, and percentile confidence interval for the slope are calculated.
conf.level confidence level to be used in computing the normal confidence intervals for model coefficients when conf=TRUE. Defaults to 0.95.
B number of bootstrap samples (replicates)
p.value a logical that determines whether p-values for model coefficients should be returned. Defaults to FALSE. If TRUE, p-values are computed from normal distribution using estimated coefficients and cov.matrix.
bfa.ls.bc

Value

- **coeff** - a matrix containing the least squares estimates of the autoregressive coefficients
- **error.cor** - the least squares estimate of the correlation between pairs of model errors \( (e_{2t}, e_{2t+1}) \). Only returned if `error.cor=TRUE`
- **x** - a matrix containing the x data used in fitting the model. Only returned if `x.data=TRUE`
- **y** - a vector containing the y data used in fitting the model. Only returned if `y.data=TRUE`
- **resids** - the model residuals. Only returned if `resids=TRUE`
- **error.var** - the estimated variance of the model errors. Only returned if `error.var=TRUE`
- **cov.matrix** - the estimated variance-covariance matrix of the least squares coefficients. Only returned if `cov.matrix=TRUE`
- **conf** - a matrix of normal confidence intervals for model coefficients. Only returned if `conf=TRUE`
- **p.value** - a matrix of two-sided p-values for testing the significance of model coefficients. Computed from normal distribution and using the estimated covariance matrix `cov.matrix`. Only returned if `p.value=TRUE`

References


Examples

```r
z <- bfa.tree.gen(127, 1, 1, 1, -0.9, -0.9, 0, 10, c(0.7))
bfa.ls(z, p=1)
bfa.ls(z, p=1, conf=TRUE, cov.matrix = TRUE, conf.level = 0.9, p.value=TRUE)
```

bfa.ls.bc

*Bias-Corrected Least Squares Estimators for Bifurcating Autoregressive Models*

Description

This function performs bias correction on the least squares estimators of the autoregressive coefficients in a BAR(p) model using single, double and fast-double bootstrapping, and the linear-bias-function approach as described in Elbayoumi and Mostafa (2021).

Usage

```r
bfa.ls.bc(
  z,
  p,
  method = "boot1",
  burn = 5,
  B1 = 999,
)```
B2 = 499,
boot.est = TRUE,
boot.data = FALSE
)

Arguments

z     a numeric vector containing the tree data
p     an integer determining the order of bifurcating autoregressive model to be fit to
      the data
method method of bias correction. Currently, "boot1", "boot2", "boot2fast" and "LBC"
      are supported and they implement single bootstrap, double bootstrap, fast-double
      bootstrap, and linear-bias-function bias-correction, respectively.
burn  number of tree generations to discard before starting the bootstrap sample (repli-
      cate)
B1    number of bootstrap samples (replicates) used in first round of bootstrapping
B2    number of bootstrap samples (replicates) used in second round of bootstrapping
boot.est a logical that determines whether the bootstrapped least squares estimates of the
          autoregressive coefficients should be returned. Defaults to TRUE.
boot.data a logical that determines whether the bootstrap samples should be returned. De-
           faults to FALSE.

Value

coef.ls.bc bias-corrected least squares estimates of the autoregressive coefficients

References


Examples

z <- bfa.tree.gen(63, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.ls.bc(z, p=2, method="boot1")
z <- bfa.tree.gen(63, 2, 1, 1, 0.5, 0.5, 0, 10, c(0.5, 0.3))
bfa.ls.bc(z, p=2, method="LBC")

bfa.ls.bc.ci

Bias-Corrected Confidence intervals of Least Squares Estimators for
Bifurcating Autoregressive Models

Description

This function performs bias correction confidence intervals on the least squares estimators of the
autoregressive coefficients in a BAR(p) model using single, fast-double, and the Bias-corrected and
accelerated bootstrapping as described in Elbayoumi and Mostafa (2023).
Usage

bfa.ls.bc.ci(
  z,
  p,
  method = "BCa",
  conf.int = "standard.normal.bc",
  conf.level = 0.95,
  B = 5,
  burn = 5
)

Arguments

z          a numeric vector containing the tree data
p          an integer determining the order of bifurcating autoregressive model to be fit to
           the data
method     method of bias correction. Currently, "boot1", "boot2fast", and "BCa" are sup-
           ported and they implement single bootstrap, fast-double bootstrap, and bias-
           corrected and accelerated bootstrap, respectively. Defaults to "BCa".
conf.int   type of the confidence interval. Currently, "standard.normal.bc", "percentile",
           and "percentile.bc" are supported and they implement corrected standard normal
           bootstrap CI, uncorrected percentile bootstrap CI, and corrected percentile boot-
           strap CI, respectively. If "boot1" method is selected, the "standard.normal.bc",
           "percentile", "percentile.bc" confidence intervals can be obtained. If "boot2fast"
           method is selected, the "standard.normal.bc" and "percentile.bc" confidence intervals
           can be obtained. No effect for conf.int, the "BCa" method is selected. Defaults to
           standard.normal.bc".
conf.level confidence level to be used in computing confidence intervals for model coeffi-
           cients. Defaults to 0.95.
B          number of bootstrap samples (replicates).
burn       number of tree generations to discard before starting the bootstrap sample (repli-
           cate). Defaults to 5.

Value

Bias.corrected.coef a matrix containing the bias-correction least squares estimates of the autoregres-
                     sive coefficients
BCa.ci          a matrix containing the lower and upper limits of corrected BCa confidence
                intervals, if method="BCa"
standard.normal.bc.ci
                a matrix containing the lower and upper limits of corrected confidence intervals,
                if method="boot1" and conf.int="standard.normal.bc" or conf.int="All"
percentile.ci   a matrix containing the lower and upper limits of uncorrected percentile confi-
                dence intervals, if method="boot1" and conf.int="percentile" or conf.int="All"
percentile.bc.ci

a matrix containing the lower and upper limits of corrected percentile confidence intervals, if method="boot1" and conf.int="percentile.bc" or conf.int="All"

standard.normal.bc.ci

a matrix containing the lower and upper limits of corrected confidence intervals, if method="boot2fast" and conf.int="standard.normal.bc" or conf.int="All"

percentile.bc.ci

a matrix containing the lower and upper limits of corrected percentile confidence intervals, if method="boot2fast" and conf.int="percentile.bc" or conf.int="All"

References


Examples

# Generating Non-contaminated normal BAR(1) tree and calculating the bias corrected
# standard normal CI for the autoregressive coefficients of the BAR(1) model
# Note that in this example (B=2) for speeding up the calculations.
# B must be set to 499 or more for calculation accuracy.
z <- bfa.tree.gen(15, 1, 1, 1, -0.9, -0.9, 0, 10, c(-0.5))
bfa.ls.bc.ci(z, p=1, method="boot1", B=2)

bfa.perc.bc.ci Bias Correction Percentile Confidence Interval Function

Description

This function calculates the Bias-Corrected percentile CI for the least squares estimator of the bifurcating autoregressive model.

Usage

bfa.perc.bc.ci(z, a1.ls, a1.ls.star, conf.level = 0.95)

Arguments

z a numeric vector containing the tree data.
a1.ls A numeric value of the least squares estimator of bifurcating autoregressive model
a1.ls.star A numeric vector representing B replicates of the least squares estimator
conf.level A numeric value representing the confidence level. Defaults to 0.95.
Value

A numeric vector representing the lower and upper limits of the bias corrected percentile confidence interval for the autoregressive coefficients of BAR model.

Examples

```r
# Generating Non-contaminated normal BAR(1) tree and calculating the bias
# corrected percentile CI for the autoregressive coefficients of the BAR(1) model
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
a1.ls <- bfa.ls(z,1)$coef[2]
a1.ls.star <- (rnorm(100,0.7,0.05))
bfa.perc.bc.ci(z, a1.ls, a1.ls.star, conf.level=0.95)
```

---

bfa.perc.ci  Percentile Bootstrap Confidence Interval Function

Description

This function calculates the percentile bootstrap CI for the least squares estimator of the bifurcating autoregressive model.

Usage

```r
bfa.perc.ci(a1.ls.star, conf.level = 0.95)
```

Arguments

- `a1.ls.star`: A numeric vector representing B replicates of the least squares estimator.
- `conf.level`: A numeric value representing the confidence level. Defaults to 0.95.

Value

A numeric vector representing the lower and upper limits of the confidence interval.

Examples

```r
a1.ls.star <- c(rnorm(100,0.7,0.05))
bfa.perc.ci(a1.ls.star, conf.level= 0.95)
```
bfa.scatterplot  Scatterplots for Bifurcating Autoregressive Data

Description
Draw scatterplots between observations at time $t$ and the lagged observations from the given bifurcating autoregressive tree data.

Usage
bfa.scatterplot(z, p, ...)

Arguments
- **z**: a numeric vector containing the tree data
- **p**: an integer determining the order of the bifurcating autoregressive model that is believed to best fit the data
- **...**: other graphical parameters that can be passed to `plot()` or `pairs()` (see `par` and `pairs`)

Value
A single scatterplot when $p=1$ or a matrix of scatterplots when $p>1$.

Examples
```r
z <- bfa.tree.gen(63, 1, 1, 2, 0.5, 0.5, 0.2, 10, c(0.7))
bfa.scatterplot(z, 1)
z <- bfa.tree.gen(63, 2, 1, 2, 0.5, 0.5, 0.2, 10, c(0.7, 0.2))
bfa.scatterplot(z, 2)
bfa.scatterplot(z, 2, lower.panel=NULL)
```

bfa.subtree  Subtree Extractor

Description
This function extracts subtree of size $(2^p - 1)$ from the end of a given bifurcating autoregressive tree (model) of order $p$.

Usage
bfa.subtree(n, p)
Arguments

- **n**: subtree size (integer)
- **p**: an integer determining the order of bifurcating autoregressive model

Value

A numeric vector representing a subtree of size \((2^p - 1)\) from the end of a given bifurcating autoregressive tree.

Examples

```r
bfa.subtree(31, 1)
bfa.subtree(31, 2)
```

### Description

This function generates bifurcating autoregressive (BFA) trees of any size based on a BFA model of any order.

### Usage

```r
bfa.tree.gen(n, p, s1, s2, r1, r2, g, intercept, ar.coef, dist = "cnorm", a)
```

Arguments

- **n**: tree size (integer)
- **p**: an integer determining the order of bifurcating autoregressive model
- **s1**: standard deviation of the errors distribution
- **s2**: standard deviation of the second component of the mixture normal distribution generating contaminated errors. \(s2\) should be greater than \(s1\). \(s2\) is only effective when \(g > 0\).
- **r1**: correlation between pairs of errors
- **r2**: is used in combination with \(r1\) to compute the correlation between pairs of errors in the second component of the mixture normal distribution generating the contaminated errors. \(r2\) is only effective when \(g > 0\).
- **g**: proportion of contamination when contaminated normal distribution is selected, or a positive value representing the degrees of freedom when skew t-student distribution is selected. Defaults to zero producing non-contaminated multivariate normal errors.
- **intercept**: the intercept in the BAR model generating the tree
- **ar.coef**: a vector of length \(p\) giving the autoregressive coefficients in the BAR model generating the tree

### Bifurcating Autoregressive Tree generator

- **bfa.tree.gen**

- **Arguments**
  - **n**: tree size (integer)
  - **p**: an integer determining the order of bifurcating autoregressive model
  - **s1**: standard deviation of the errors distribution
  - **s2**: standard deviation of the second component of the mixture normal distribution generating contaminated errors. \(s2\) should be greater than \(s1\). \(s2\) is only effective when \(g > 0\).
  - **r1**: correlation between pairs of errors
  - **r2**: is used in combination with \(r1\) to compute the correlation between pairs of errors in the second component of the mixture normal distribution generating the contaminated errors. \(r2\) is only effective when \(g > 0\).
  - **g**: proportion of contamination when contaminated normal distribution is selected, or a positive value representing the degrees of freedom when skew t-student distribution is selected. Defaults to zero producing non-contaminated multivariate normal errors.
  - **intercept**: the intercept in the BAR model generating the tree
  - **ar.coef**: a vector of length \(p\) giving the autoregressive coefficients in the BAR model generating the tree

- **Value**
  A numeric vector representing a subtree of size \((2^p - 1)\) from the end of a given bifurcating autoregressive tree.

- **Examples**
  ```r
  bfa.subtree(31, 1)
bfa.subtree(31, 2)
  ```
determine the distribution of the error. Three distributions are available; Contaminated normal distribution "cnorm", Skew normal distribution "snorm", and Skew t-student distribution "st".

a an integer which regulates the slant of the density when skew normal distribution or skew t-student distribution is selected. Defaults to zero producing non-skewed multivariate normal errors, and non-skewed multivariate t-student errors for the tree generation.

Value
A numeric vector representing a bifurcating autoregressive (BFA) tree with n observations.

Examples

# Non-contaminated normal BAR(1) tree:
bfa.tree.gen(127, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
# Non-contaminated normal BAR(2) tree:
bfa.tree.gen(127, 2, 1, 1, 0.5, 0.5, 0, 10, c(0.5, 0.3))
# Contaminated normal BAR(1) tree:
bfa.tree.gen(127, 1, 1, 2, 0.5, 0.5, 0.2, 10, c(0.7))
# BAR(1) tree with error generated from skewed-t distribution with skewness equals to -3:
bfa.tree.gen(127, 1, 1, 2, 0.5, 0.5, 0, 10, c(0.7), dist="snorm", -3)
# BAR(2) tree with error generated from skewed-t distribution with skewness equals to 3:
bfa.tree.gen(127, 2, 1, 2, 0.5, 0.5, 0, 10, c(0.7, 0.5), dist="snorm", 3)
# BAR(1) tree with error generated from skewed-t distribution with skewness equals
# to -3 and df equals to 10:
bfa.tree.gen(127, 1, 1, 2, 0.5, 0.5, 0.2, 10, c(0.7), dist="st", -3)
# BAR(2) tree with error generated from skewed-t distribution with skewness equals
# to 3 and df equals to 1:
bfa.tree.gen(127, 2, 1, 2, 0.5, 0.5, 0.2, 10, c(0.7, 0.5), dist="st", 3)

bfa.tree.plot

Plotting bifurcating autoregressive trees

Description
This function graphs bifurcating autoregressive (BFA) tree data.

Usage
bfa.tree.plot(
  z,
  digits,
  shape = "none",
  vertex.size = 10,
  text.size = 1,
  text.color = "black",
  vertex.color = "gold",
  dist = "none",
  a = 0,
  ...)
Arguments

z a numeric vector containing the tree data
digits an integer indicating the number of decimal places to be displayed in vertex labels
shape the shape of the vertex. Currently “circle”, “square”, “csquare”, “rectangle”, “crectangle”, “vrectangle”, and “none” are supported. Defaults to “none” which does not display the vertices at all.
vertex.size a numeric scalar or vector defining the size of the vertex or vertices. If a vector is supplied, vertex sizes may differ. Defaults to 10.
text.size the font size of vertex labels. Defaults to 1.
text.color the color of vertex labels. If it is a character vector, then it may either contain integer values, named colors or RGB specified colors with three or four bytes. Defaults to “black”.
vertex.color the fill color of the vertex. If you don’t want some or all vertices to have any color, supply NA. The default is “gold”. See also the options in text.color.
vertex.asp a parameter that controls the aspect ratio of the plot, The default value is 0.25.
arrow.size the size of the arrows. The default value is 0.5.
arrow.width the width of the arrows. The default value is 0.5.
arrow.color the color of the arrows. The default is “black”. See also the options in text.color.
plot.margin the amount of empty space around the plot, it is a numeric vector of length four. Usually values between 0 and 0.5 are meaningful, but negative values are also possible and in that case it will make the plot zoom in to a part of the graph. If it is shorter than four, recycling will occur. The default value is -0.3.

Details

For more details about the graph options see igraph.plotting.

Value

A binary tree displaying the BFA data.

Examples

z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
bfa.tree.plot(z)
bfa.tree.plot(z, shape= "circle")
bfa.tree.plot(z, shape= "circle", text.color="white", vertex.color = "darkgrey")
Bias-Corrected and Accelerated bootstrap Confidence Interval (BCa) Function.

Description

This function calculates the Bias-Corrected and Accelerated bootstrap (BCa) CI for the least squares estimator of the bifurcating autoregressive model.

Usage

```r
boot.bca.ci(z, p, B = 99, J = 2, conf.level = 0.95)
```

Arguments

- `z`: a numeric vector containing the tree data.
- `p`: an integer determining the order of bifurcating autoregressive model to be fit to the data.
- `B`: number of bootstrap samples (replicates). Defaults to 99.
- `J`: an integer determining the number of vectors of bootstrap replicates. Defaults to 2.
- `conf.level`: A numeric value representing the confidence level. Defaults to 0.95.

Value

- `coef`: a matrix containing the least squares estimates of the autoregressive coefficients
- `limits`: A numeric vector representing the lower and upper limits of the BCa confidence interval for the autoregressive coefficients of BAR model

Examples

```r
# Generating Non-contaminated normal BAR(1) tree and calculating the BCa CI for
# the autoregressive coefficients of the BAR(1) model
z <- bfa.tree.gen(31, 1, 1, 1, 0.5, 0.5, 0, 10, c(0.7))
boot.bca.ci(z, p = 1, B = 99, J = 2, conf.level = 0.95)
# Generating Non-contaminated normal BAR(2) tree and calculating the BCa CI for
# the autoregressive coefficients of the BAR(2) model
z <- bfa.tree.gen(127, 2, 1, 1, 0.5, 0.5, 0, 10, c(0.5, 0.3))
boot.bca.ci(z, p = 2, B = 99, J = 2, conf.level = 0.95)
```
**ecoli**

Lifetimes (in minutes) of lineage E. coli cells.

**Description**

A real cell lineage dataset taken from Cowan and Staudte (1986). The values represent the lifetimes in minutes of lineage E. coli cells. It contains 31 observations making which can be described by a bifurcating autoregressive tree with 4 generations.

**Usage**

ecoli

**Format**

A data frame with 31 rows and 1 variable:

- **lifetime**  E. coli cells lifetime, in minutes

**Source**


---

**emt6**

Mean Lifetimes (in tenths of hours) of EMT6 (BALB/c mouse mammary tumor) cells.

**Description**

A real cell lineage dataset taken from Staudte et al. (1984). The values represent the mean lifetimes in tenths of hours obtained from averaging observations from 41 bifurcating trees. The averaging of observations and the tree are made by Elbayoumi and Mostafa (2023).

**Usage**

emt6

**Format**

A data frame with 63 rows and 1 variable:

- **mean.lifetime**  EMT6 cells lifetime, in tenths of hours

**Source**

Description

This function generates contaminated multivariate normal errors that are used in the generation of the Bifurcating autoregressive tree.

Usage

```r
rcontmnorm(
  n,
  d = 2,
  mu1 = rep(0, d),
  sigma1 = diag(d),
  mu2 = rep(0, d),
  sigma2 = diag(d),
  g
)
```

Arguments

- `n`: sample size
- `d`: dimension. Defaults to 2 for bivariate normal errors.
- `mu1`: mean vector for first multivariate normal distribution. Defaults to the zero vector.
- `sigma1`: variance-covariance matrix for first multivariate normal distribution. Defaults to the d by d identity matrix, where d is the dimension.
- `mu2`: mean vector for second multivariate normal distribution. Defaults to the zero vector.
- `sigma2`: variance-covariance matrix for second multivariate normal distribution. Defaults to the d by d identity matrix, where d is the dimension.
- `g`: proportion of contamination. Defaults to zero producing non-contaminated multivariate normal data.

Value

An n by d contaminated multivariate normal matrix.

Examples

```r
#Non-contaminated bivariate normal:
rcontmnorm(10, sigma2=2^2*matrix(c(1,0,0,1),nrow=2) , g=0)
#Contaminated bivariate normal with 20% contamination:
rcontmnorm(10, sigma2=2^2*matrix(c(1,0,0,1),nrow=2) , g=0.2)
```
Description

This function generates multivariate normal errors that are used in the generation of the Bifurcating autoregressive tree.

Usage

```r
rmnorm(n, d = 2, mu = rep(0, d), sigma = diag(d))
```

Arguments

- `n`: sample size
- `d`: dimension. Defaults to 2 for bivariate normal errors.
- `mu`: mean vector. Defaults to the zero vector.
- `sigma`: variance-covariance matrix. Defaults to the d by d identity matrix, where d is the dimension.

Value

An n by d multivariate normal matrix.

Examples

```r
rmnorm(10)
rmnorm(10, 3)
```
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