

# Package ‘deldir’

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**Title** Delaunay Triangulation and Dirichlet (Voronoi) Tessellation

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**Depends** R (>= 0.99)

**Suggests** polyclip

**Imports** graphics, grDevices

**Description** Calculates the Delaunay triangulation and the Dirichlet or Voronoi tessellation (with respect to the entire plane) of a planar point set. Plots triangulations and tessellations in various ways. Clips tessellations to sub-windows. Calculates perimeters of tessellations. Summarises information about the tiles of the tessellation.

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deldir	<i>Delaunay triangulation and Dirichlet tessellation</i>
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## Description

This function computes the Delaunay triangulation (and hence the Dirichlet or Voronoi tessellation) of a planar point set according to the second (iterative) algorithm of Lee and Schacter — see REFERENCES. The triangulation is made to be with respect to the whole plane by suspending it from so-called ideal points  $(-\text{Inf}, -\text{Inf})$ ,  $(\text{Inf}, -\text{Inf})$ ,  $(\text{Inf}, \text{Inf})$ , and  $(-\text{Inf}, \text{Inf})$ . The triangulation is also enclosed in a finite rectangular window. A set of dummy points may be added, in various ways, to the set of data points being triangulated.

## Usage

```
deldir(x, y, dpl=NULL, rw=NULL, eps=1e-09, sort=TRUE, plotit=FALSE,
       digits=6, z=NULL, zdum=NULL, suppressMsge=FALSE, ...)
```

## Arguments

**x, y** These arguments specify the coordinates of the point set being triangulated or tessellated. These can be given by two separate arguments `x` and `y` which are vectors or by a single argument `x` which is either a data frame or a generic list, possibly one of class `ppp`. (See package `spatstat`.)

If `x` is a data frame then the `x` coordinates of the points to be triangulated or tessellated are taken to be the column of this data frame which is named “`x`” if there is one, else the first column of the data frame which is not named either “`y`” or “`z`”. The `y` coordinates are taken to be the column of this data frame which is named “`y`” if there is one. If there is no column named “`y`” but there are columns named “`x`” and “`z`” then the `y` coordinates are taken to be the first “other” column. If there no columns named either “`x`” or “`y`”, then the `x` coordinates are taken to be the first column not named “`z`” and the `y` coordinates are taken to be the *second* column not named “`z`”.

If there is a column named “`z`” and if the argument `z` (see below) is `NULL`, then this the column named “`z`” is taken to be the value of `z`.

If  $x$  is a list (but not a data frame) then it must have components named  $x$  and  $y$ , and possibly a component named  $z$ . The  $x$  and  $y$  components give the  $x$  and  $y$  coordinates respectively of the points to be triangulated or tessellated. If  $x$  is *not* of class `ppp`, if it has a component  $z$  and if argument  $z$  is `NULL`, then the  $z$  argument is set equal to this component  $z$ . If  $x$  is of class “`ppp`”, if the argument  $z$  is `NULL`, if  $x$  is “marked” (see package `spatstat`) and if the marks of  $x$  are a vector or a factor (as opposed to a data frame) then the  $z$  argument is set equal to these marks. In this case  $x$  should *not* have a component  $z$ , and at any rate such a component would be ignored.

<code>dpl</code>	<p>A list describing the structure of the dummy points to be added to the data being triangulated. The addition of these dummy points is effected by the auxiliary function <code>dumpts()</code>. The list may have components:</p> <ul style="list-style-type: none"> <li>• <code>ndx</code>: The <math>x</math>-dimension of a rectangular grid; if either <code>ndx</code> or <code>ndy</code> is null, no grid is constructed.</li> <li>• <code>ndy</code>: The <math>y</math>-dimension of the aforementioned rectangular grid.</li> <li>• <code>nrad</code>: The number of radii or “spokes”, emanating from each data point, along which dummy points are to be added.</li> <li>• <code>nper</code>: The number of dummy points per spoke.</li> <li>• <code>fctr</code>: A numeric “multiplicative factor” determining the length of each spoke; each spoke is of length equal to <code>fctr</code> times the mean nearest neighbour distance of the data. (This distance is calculated by the auxiliary function <code>mnnd()</code>.)</li> <li>• <code>x</code>: A vector of <math>x</math>-coordinates of “ad hoc” dummy points</li> <li>• <code>y</code>: A vector of the corresponding <math>y</math>-coordinates of “ad hoc” dummy points</li> </ul>
<code>rw</code>	<p>The coordinates of the corners of the rectangular window enclosing the triangulation, in the order (<code>xmin</code>, <code>xmax</code>, <code>ymin</code>, <code>ymax</code>). Any data points (including dummy points) outside this window are discarded. If this argument is omitted, it defaults to values given by the range of the data, plus and minus 10 percent.</p>
<code>eps</code>	<p>A value of epsilon used in testing whether a quantity is zero, mainly in the context of whether points are collinear. If anomalous errors arise, it is possible that these may averted by adjusting the value of <code>eps</code> upward or downward.</p>
<code>sort</code>	<p>Logical argument; if <code>TRUE</code> (the default) the data (including dummy points) are sorted into a sequence of “bins” prior to triangulation; this makes the algorithm slightly more efficient. Normally one would set <code>sort</code> equal to <code>FALSE</code> only if one wished to observe some of the fine detail of the way in which adding a point to a data set affected the triangulation, and therefore wished to make sure that the point in question was added last. Essentially this argument would get used only in a de-bugging process.</p>
<code>plotit</code>	<p>Logical argument; if <code>TRUE</code> a plot is produced. The nature of the plot may be controlled by using the <code>...</code> argument to pass appropriate arguments to <code>plot.deldir()</code>. Without “further instruction” a plot of the points being triangulated and of both the triangulation and the tessellation is produced;</p>
<code>digits</code>	<p>The number of decimal places to which all numeric values in the returned list should be rounded. Defaults to 6.</p>
<code>z</code>	<p>An optional vector of “auxiliary” values or “weights” associated with the respective points. (<b>NOTE:</b> These “weights” are values associated with the points</p>

and hence with the tiles of the tessellation produced. They **DO NOT** affect the tessellation, i.e. the tessellation produced is the same as it would be if there were no weights. The `deldir` package **DOES NOT** do weighted tessellation. (The so-called weights in fact need not be numeric.)

If `z` is left `NULL` then it is taken to be the third column of `x`, if `x` is a data frame or to be the `z` component of `x` if `x` is a generic list. If `z` is left `NULL` and if `x` is of class “`ppp`” and is “`marked`” (see package `spatstat`) and if in addition the marks are atomic (i.e. *not* a data frame) then `z` is taken to be the marks of `x`.

<code>zdum</code>	Values of <code>z</code> to be associated with any dummy points that are created. See <b>Warnings</b> .
<code>suppressMsgs</code>	Logical scalar indicating whether a message (alerting the user to changes from previous versions of <code>deldir</code> ) should be suppressed.
<code>...</code>	Auxiliary arguments <code>add</code> , <code>wlines</code> , <code>wpoints</code> , <code>number</code> , <code>nex</code> , <code>col</code> , <code>lty</code> , <code>pch</code> , <code>xlim</code> , and <code>ylim</code> (and possibly other plotting parameters) may be passed to <code>plot.deldir()</code> through <code>...</code> if <code>plotit=TRUE</code> .

## Details

This package is a (straightforward) adaptation of the `Splus` library section “`delaunay`” to `R`. That library section is an implementation of the Lee-Schachter algorithm, which was originally written as a stand-alone Fortran program in 1987/88 by Rolf Turner, while with the Division of Mathematics and Statistics, CSIRO, Sydney, Australia. It was re-written as an `Splus` function (using dynamically loaded Fortran code), by Rolf Turner while visiting the University of Western Australia, May, 1995.

Further revisions were made December 1996. The author gratefully acknowledges the contributions, assistance, and guidance of Mark Berman, of D.M.S., CSIRO, in collaboration with whom this project was originally undertaken. The author also acknowledges much useful advice from Adrian Baddeley, formerly of D.M.S., CSIRO (now Professor of Statistics at Curtin University). Daryl Tingley of the Department of Mathematics and Statistics, University of New Brunswick provided some helpful insight. Special thanks are extended to Alan Johnson, of the Alaska Fisheries Science Centre, who supplied two data sets which were extremely valuable in tracking down some errors in the code.

Don MacQueen, of Lawrence Livermore National Lab, wrote an `Splus` driver function for the old stand-alone version of this software. That driver, which was available on Statlib, is now deprecated in favour of the current package “`delaunay`” package. Don also collaborated in the preparation of that package.

See the `ChangeLog` for information about further revisions and bug-fixes.

## Value

A list (of class `deldir`), invisible if `plotit=TRUE`, with components:

<code>delsgs</code>	A data frame with 6 columns. The first 4 entries of each row are the coordinates of the points joined by an edge of a Delaunay triangle, in the order $(x_1, y_1, x_2, y_2)$ . The last two entries are the indices of the two points which are joined.
<code>dirsgs</code>	A data frame with 10 columns. The first 4 entries of each row are the coordinates of the endpoints of one the edges of a Dirichlet tile, in the order $(x_1, y_1, x_2, y_2)$ .

The fifth and sixth entries, in the columns named `ind1` and `ind2`, are the indices of the two points, in the set being triangulated, which are separated by that edge. The seventh and eighth entries, in the columns named `bp1` and `bp2` are logical values. The entry in column `bp1` indicates whether the first endpoint of the corresponding edge of a Dirichlet tile is a boundary point (a point on the boundary of the rectangular window). Likewise for the entry in column `bp2` and the second endpoint of the edge.

The ninth and tenth entries, in columns named `thirdv1` and `thirdv2` are the indices of the third vertex of the Delaunay triangle whose circumcentre constitutes the corresponding vertex of the edge under consideration. (The other two vertices are indexed by the entries of columns `ind1` and `ind2`.)

The entries of columns `thirdv1` and `thirdv2` may (also) take the values `-1`, `-2`, `-3`, and `-4`. This will be the case if the circumcentre in question lies outside of the rectangular window `rw`. In these circumstances the corresponding endpoint of the tile edge is the intersection of the line joining the two circumcentres with the boundary of `rw`, and the numeric value of the entry of column “`vi3`” indicates which side. The numbering follows the convention for numbering the sides of a plot region in R: 1 for the bottom side, 2 for the left side, 3 for the top side and 4 for the right side.

Note that the entry in column `thirdv1` will be negative if and only if the corresponding entry in column `bp1` is `TRUE`. Similarly for columns `thirdv2` and `bp2`.

summary

a data frame with 9, 10 or 11 columns and `n.data + n.dum` rows (see below). The rows correspond to the points in the set being triangulated. Note that the row names are the indices of the points in the original sequence of points being triangulated/tessellated. Usually these will be the sequence 1, 2, ..., `npd` (“`n` plus dummy”). However if there were *duplicated* points then the row name corresponding to a point is the *first* of the indices of the set of duplicated points in which the given point appears. The columns are:

- `x` (the  $x$ -coordinate of the point)
- `y` (the  $y$ -coordinate of the point)
- `pt.type` (a character vector with entries “`data`” and “`dummy`”; present only if `n.dum > 0`)
- `z` (the auxiliary values or “weights”; present only if these were specified)
- `n.tri` (the number of Delaunay triangles emanating from the point)
- `del.area` ( $1/3$  of the total area of all the Delaunay triangles emanating from the point)
- `del.wts` (the corresponding entry of the `del.area` column divided by the sum of this column)
- `n.tside` (the number of sides — within the rectangular window — of the Dirichlet tile surrounding the point)
- `nbpt` (the number of points in which the Dirichlet tile intersects the boundary of the rectangular window)
- `dir.area` (the area of the Dirichlet tile surrounding the point)
- `dir.wts` (the corresponding entry of the `dir.area` column divided by the sum of this column).

Note that the factor of 1/3 associated with the `del.area` column arises because each triangle occurs three times — once for each corner.

<code>n.data</code>	the number of real (as opposed to dummy) points in the set which was triangulated, with any duplicate points eliminated. The first <code>n.data</code> rows of <code>summary</code> correspond to real points.
<code>n.dum</code>	the number of dummy points which were added to the set being triangulated, with any duplicate points (including any which duplicate real points) eliminated. The last <code>n.dum</code> rows of <code>summary</code> correspond to dummy points.
<code>del.area</code>	the area of the convex hull of the set of points being triangulated, as formed by summing the <code>del.area</code> column of <code>summary</code> .
<code>dir.area</code>	the area of the rectangular window enclosing the points being triangulated, as formed by summing the <code>dir.area</code> column of <code>summary</code> .
<code>rw</code>	the specification of the corners of the rectangular window enclosing the data, in the order (xmin, xmax, ymin, ymax).
<code>ind.orig</code>	A vector of the indices of the points (x,y) in the set of coordinates initially supplied (as data points or as dummy points) to <code>deldir()</code> before duplicate points (if any) were removed. These indices are used by <code>triang.list()</code> .

**Remark:**

If `ndx >= 2` and `ndy >= 2`, then the rectangular window IS the convex hull, and so the values of `del.area` and `dir.area` (if the latter is not NULL) are identical.

**Side Effects**

If `plotit=TRUE` a plot of the triangulation and/or tessellation is produced or added to an existing plot.

**Warnings**

1. The process for determining if points are duplicated changed between versions 0.1-9 and 0.1-10. Previously there was an argument `frac` for this function, which defaulted to 0.0001. Points were deemed to be duplicates if the difference in x-coordinates was less than `frac` times the width of `rw` and y-coordinates was less than `frac` times the height of `rw`. This process has been changed to one which uses `duplicated()` on the data frame whose columns are x and y. As a result it may happen that points which were previously eliminated as duplicates will no longer be eliminated. (And possibly vice-versa.)
2. The components `delsgs` and `summary` of the value returned by `deldir()` are now *data frames* rather than matrices. The component `summary` was changed to allow the “auxiliary” values `z` to be of arbitrary mode (i.e. not necessarily numeric). The component `delsgs` was then changed for consistency. Note that the other “matrix-like” component `dirsgs` has been a data frame since time immemorial.

A message alerting the user to the foregoing two items is printed out the first time that `deldir()` is called with `suppressMsgs=FALSE` in a given session. In succeeding calls to `deldir()` in the same session, no message is printed. (I.e. the “alerting” message is printed *at most once* in any given session.)

The “alerting” message is *not* produced via the `warning()` function, so `suppressWarnings()` will *not* suppress its appearance. To effect such suppression (necessary only on the first call to `deldir()` in a given session) one must set the `suppressMsg` argument of `deldir` equal to `TRUE`.

3. If any dummy points are created, and if a vector `z`, of “auxiliary” values or “weights” associated with the points being triangulated, is supplied, then it is up to the user to supply the corresponding auxiliary values or weights associated with the dummy points. These values should be supplied as `zdum`. If `zdum` is not supplied then the auxiliary values or weights associated with the dummy points are all taken to be missing values (i.e. `NA`).

### Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

### References

Lee, D. T., and Schacter, B. J. Two algorithms for constructing a Delaunay triangulation, *Int. J. Computer and Information Sciences*, Vol. 9, No. 3, 1980, pp. 219 – 242.

Ahuja, N. and Schacter, B. J. (1983). *Pattern Models*. New York: Wiley.

### See Also

[plot.deldir\(\)](#), [tile.list\(\)](#), [triang.list\(\)](#)

### Examples

```
x <- c(2.3,3.0,7.0,1.0,3.0,8.0)
y <- c(2.3,3.0,2.0,5.0,8.0,9.0)
# An "alerting note" is printed.; let deldir() choose the
# rectangular window.
dxy1 <- deldir(x,y)

# User chooses the rectangular window.
dxy2 <- deldir(x,y,rw=c(0,10,0,10))

# Put dummy points at the corners of the rectangular
# window, i.e. at (0,0), (10,0), (10,10), and (0,10)
dxy3 <- deldir(x,y,dpl=list(ndx=2,ndy=2),rw=c(0,10,0,10))

# Plot the triangulation created (but not the tessellation).
## Not run:
dxy2 <- deldir(x,y,rw=c(0,10,0,10),plot=TRUE,wl='tr')

## End(Not run)

# Auxiliary values associated with points; 4 dummy points to be
# added so 4 dummy "z-values" provided.
z <- c(1.63,0.79,2.84,1.56,0.22,1.07)
zdum <- rep(42,4)
dxy4 <- deldir(x,y,dpl=list(ndx=2,ndy=2),rw=c(0,10,0,10),z=z,zdum=zdum)
```

---

`divchain`*Dividing chain; generic.*

---

**Description**

Generic function for creating the “dividing chain” of a Dirichlet tessellation. The tessellation must have been created from a set of points having associated categorical “weights”. The dividing chain consists of those edges of Dirichlet tiles which separate points having different values of the given weights.

**Usage**

```
divchain(x, ...)
```

**Arguments**

`x` Either an object specifying coordinates or an object of class “deldir”.  
`...` Arguments to be passed to the appropriate method for this generic function.

**Details**

If `x` is a (numeric) vector it will be taken to be the “x” coordinates of the points being tessellated. In this case the `...` arguments must contain a vector `y` specifying the “y” coordinates. The `...` arguments must also contain a *factor* `z` specifying the relevant “weights” argument. The argument `x` may also be a data frame or list from which the coordinates and the weights will be extracted. See [divchain.default\(\)](#) for details.

If `x` is an object of class class “deldir” then it must have been created with an appropriate (factor) “weights” argument, otherwise an error is given.

**Value**

An object of class “divchain”. See [divchain.deldir\(\)](#) for details.

**Note**

This function was created in response to a question asked on [stackoverflow.com](#) by a user named “Dan”.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

[divchain.default\(\)](#) [divchain.deldir\(\)](#) [deldir\(\)](#) [plot.divchain\(\)](#)



## Examples

```
set.seed(42)
x <- runif(50)
y <- runif(50)
z <- factor(kmeans(cbind(x,y),centers=4)$cluster)
dc1 <- divchain(x,y,z,rw=c(0,1,0,1))
dxy <- deldir(x,y,z=z,rw=c(0,1,0,1))
dc2 <- divchain(dxy)
```

---

divchain.default      *Dividing chain; default method.*

---

## Description

Create the “dividing chain” of the Dirichlet tessellation of a given set of points having distinguishing (categorical) “weights”. This dividing chain consists of those edges of Dirichlet tiles which separate points having different values of the given weights.

## Usage

```
## Default S3 method:
divchain(x, y, z, ...)
```

## Arguments

<code>x,y</code>	These provide the coordinates of the set of points being tessellated. Argument <code>x</code> may be a data frame or a list, in particular one of class <code>ppp</code> . (See the <code>spatstat</code> package.) For a full description see the discussion of these arguments in the help for <code>deldir()</code> .
<code>z</code>	A <i>factor</i> specifying “auxiliary” values or “weights” If this argument is left <code>NULL</code> then it is extracted, if possible, from the components of <code>x</code> . See <code>deldir()</code> for further details.
<code>...</code>	Other arguments to be passed to <code>deldir</code> .

## Value

An object of class `divchain`. See `divchain.deldir()` for details.

## Note

This function was created in response to a question asked on `stackoverflow.com` by a user named “Dan”.

## Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

[divchain.deldir\(\)](#) [deldir\(\)](#) [plot.divchain\(\)](#)

**Examples**

```
set.seed(42)
x <- runif(50)
y <- runif(50)
z <- factor(kmeans(cbind(x,y),centers=4)$cluster)
dcxy <- divchain(x,y,z,rw=c(0,1,0,1))
```

---

divchain.deldir      *Dividing chain; “deldir” method.*

---

**Description**

Create the “dividing chain” of a Dirichlet tessellation. The tessellation must have been created from a set of points having associated categorical “weights”. The dividing chain consists of those edges of Dirichlet tiles which separate points having different values of the given weights.

**Usage**

```
## S3 method for class 'deldir'
divchain(x, ...)
```

**Arguments**

**x**                    An object of class “deldir”. This object must have been created in such a way that the points of the set being tessellated have associate categorical “weights”. That is, [deldir\(\)](#) must have been called with a *factor* valued z argument or the x argument to [deldir\(\)](#) must have had an appropriate component which could be taken to be z.

**...**                Not used.

**Value**

An object of class “divchain” consisting of a data frame with columns named “x0”, “y0”, “x1”, “y1”, “v01”, “v02”, “v03”, “v11”, “v12” and “v13”.

The columns named “x0” and “y0” consist of the coordinates of one endpoint of an edge of a Dirichlet tile and the columns named “x1” and “y1” consist of the coordinates of the other endpoint.

The columns named “vij”,  $i = 0, 1, j = 1, 2, 3$ , consist of the indices of the vertices of the Delaunay triangles whose circumcentres constitute the respective endpoints of the corresponding edge of a Dirichlet tile. The entries of column “vi3” may (also) take the values  $-1, -2, -3$ , and  $-4$ . This will be the case if the circumcentre in question lay outside of the rectangular window `rw` (see [deldir\(\)](#)) enclosing the points being tessellated. In these circumstances the corresponding endpoint of the tile edge is the intersection of the line joining the two circumcentres with the boundary of `rw`, and

the numeric value of the entry of column “vi3” indicates which side. The numbering follows the convention for numbering the sides of a plot region in R: 1 for the bottom side, 2 for the left side, 3 for the top side and 4 for the right side.

Note that the triple of vertices uniquely identify the endpoint of the tile edge.

The object has an attribute `rw` which is equal to the specification of the rectangular window within which the class “`deldir`” object `x` was constructed. (See [`deldir\(\)`](#).)

### Note

This function was created in response to a question asked on [stackoverflow.com](#) by a user named “Dan”.

### Author(s)

Rolf Turner <[r.turner@auckland.ac.nz](mailto:r.turner@auckland.ac.nz)>

### See Also

[`divchain.default\(\)`](#) [`deldir\(\)`](#) [`plot.divchain\(\)`](#)

### Examples

```
set.seed(42)
x <- runif(50)
y <- runif(50)
z <- factor(kmeans(cbind(x,y),centers=4)$cluster)
dxy <- deldir(x,y,z=z,rw=c(0,1,0,1))
dc <- divchain(dxy)
```

---

duplicatedxy

*Determine duplicated points.*

---

### Description

Find which points among a given set are duplicates of others.

### Usage

```
duplicatedxy(x, y)
```

### Arguments

`x` Either a vector of `x` coordinates of a set of (two dimensional) points, or a list (or data frame) with columns `x` and `y` giving the coordinates of a set of such points.

`y` A vector of `y` coordinates of a set of (two dimensional) points. Ignored if `x` is a list or data frame.

**Details**

Often it is of interest to associate each Dirichlet tile in a tessellation of a planar point set with the point determining the tile. This becomes problematic if there are *duplicate* points in the set being tessellated/triangulated. Duplicated points are automatically eliminated “internally” by `deldir()`. The association between tiles and the indices of the original set of points is now preserved by the component `ind.orig` of the object returned by `deldir()`. However confusion could still arise.

If it is of interest to associate Dirichlet tiles with the points determining them, then it is better to proceed by eliminating duplicate points to start with. This function (`duplicatedxy()`) provides a convenient way of doing so.

**Value**

A logical vector of length equal to the (original) number of points being considered, with entries TRUE if the corresponding point is a duplicate of a point with a smaller index, and FALSE otherwise.

**Warning**

Which indices will be considered to be indices of duplicated points (i.e. get TRUE values) will of course depend on the order in which the points are presented.

**Note**

The real work is done by the base **R** function `duplicated()`.

**Author(s)**

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**See Also**

`duplicated()`, `deldir()`

**Examples**

```
set.seed(42)
xy <- data.frame(x=runif(20),y=runif(20))
# Lots of duplicated points.
xy <- rbind(xy,xy[sample(1:20,20,TRUE),])
# Scramble.
ii <- sample(1:40,40)
x <- xy$x[ii]
y <- xy$y[ii]
# Unduplicate!
iii <- !duplicatedxy(x,y)
xu <- x[iii]
yu <- y[iii]
# The i-th tile is determined by (xu[i],yu[i]):
dxy <- deldir(xu,yu)
```

plot.deldir

*Plot objects produced by deldir***Description**

This is a method for plot.

**Usage**

```
## S3 method for class 'deldir'
plot(x, add=FALSE, wlines=c('both', 'triang', 'tess'),
      wpoints=c('both', 'real', 'dummy', 'none'),
      number=FALSE, cex=1, nex=1, col=NULL, lty=NULL,
      pch=NULL, xlim=NULL, ylim=NULL, axes=FALSE,
      xlab=if(axes) 'x' else '', ylab=if(axes) 'y' else '',
      showrect=FALSE, ...)
```

**Arguments**

x	An object of class "deldir" as constructed by the function deldir.
add	logical argument; should the plot be added to an existing plot?
wlines	"which lines?". I.e. should the Delaunay triangulation be plotted (wlines='triang'), should the Dirichlet tessellation be plotted (wlines='tess'), or should both be plotted (wlines='both', the default) ?
wpoints	"Which points to plot?". I.e. should the real points be plotted (wpoints='real'), should the dummy points be plotted (wpoints='dummy'), should both be plotted (wpoints='both', the default) or should no points be plotted (wpoints='none')?
number	Logical argument, defaulting to FALSE; if TRUE then the points plotted will be labelled with their index numbers (corresponding to the row numbers of the matrix "summary" in the output of deldir).
cex	The value of the character expansion argument cex to be used with the plotting symbols for plotting the points.
nex	The value of the character expansion argument nex to be used by the text function when numbering the points with their indices. Used only if number=TRUE.
col	The colour numbers for plotting the triangulation, the tessellation, the data points, the dummy points, and the point numbers, in that order; defaults to c(1,1,1,1,1). If fewer than five numbers are given, they are recycled. (If more than five numbers are given, the redundant ones are ignored.)
lty	The line type numbers for plotting the triangulation and the tessellation, in that order; defaults to 1:2. If only one value is given it is repeated. (If more than two numbers are given, the redundant ones are ignored.)
pch	The plotting symbols for plotting the data points and the dummy points, in that order; may be either integer or character; defaults to 1:2. If only one value is given it is repeated. (If more than two values are given, the redundant ones are ignored.)

xlim	The limits on the x-axis. Defaults to rw[1:2] where rw is the rectangular window specification returned by deldir().
ylim	The limits on the y-axis. Defaults to rw[3:4] where rw is the rectangular window specification returned by deldir().
axes	Logical scalar. Should axes be drawn on the plot?
xlab	Label for the x-axis. Defaults to x if axes is TRUE and to the empty string if axes is FALSE. Ignored if add=TRUE.
ylab	Label for the y-axis. Defaults to y if axes is TRUE and to the empty string if axes is FALSE. Ignored if add=TRUE.
showrect	Logical scalar; show the enclosing rectangle rw (see <a href="#">deldir()</a> ) be plotted?
...	Further plotting parameters to be passed to plot() segments() or points() or text(). Unlikely to be used.

### Details

The points in the set being triangulated are plotted with distinguishing symbols. By default the real points are plotted as circles (pch=1) and the dummy points are plotted as triangles (pch=2).

### Side Effects

A plot of the points being triangulated is produced or added to an existing plot. As well, the edges of the Delaunay triangles and/or of the Dirichlet tiles are plotted. By default the triangles are plotted with solid lines (lty=1) and the tiles with dotted lines (lty=2).

### Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

### See Also

[deldir\(\)](#)

### Examples

```
## Not run:
try <- deldir(x,y,list(ndx=2,ndy=2),c(0,10,0,10))
plot(try)
#
deldir(x,y,list(ndx=4,ndy=4),plot=TRUE,add=TRUE,wl='te',
       col=c(1,1,2,3,4),num=TRUE)
# Plots the tessellation, but does not save the results.
try <- deldir(x,y,list(ndx=2,ndy=2),c(0,10,0,10),plot=TRUE,wl='tr',
             wp='n')
# Plots the triangulation, but not the points, and saves the
# returned structure.

## End(Not run)
```

---

plot.divchain                    *Plot a dividing chain.*

---

## Description

Plot the dividing chain of a Dirichlet tessellation. The tessellation must have been created from a set of points having associated categorical “weights”. The dividing chain consists of those edges of Dirichlet tiles which separate points having different values of the given weights.

## Usage

```
## S3 method for class 'divchain'  
plot(x, add = FALSE, ...)
```

## Arguments

x	An object of class “divchain”. See <a href="#">divchain.deldir()</a> for details.
add	Logical scalar. If add=TRUE the plot of the dividing chain is added to an existing plot.
...	Graphical parameters such as main, xlab, col.main, col.lab. In particular if bty is supplied (as a value other than n) a “box” will be drawn around the plot that is formed when add=FALSE. Also a non-standard graphical parameter boxcol may be supplied which will be taken to be the colour with which the box is drawn. If a col argument is supplied, this determines the colour for plotting the segments constituting the dividing chain.

## Value

None.

## Note

This function was created in response to a question asked on [stackoverflow.com](#) by a user named “Dan”.

## Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

## See Also

[divchain\(\)](#) [divchain.default\(\)](#) [divchain.deldir\(\)](#) [deldir\(\)](#)

**Examples**

```

set.seed(42)
x <- runif(50)
y <- runif(50)
z <- factor(kmeans(cbind(x,y),centers=4)$cluster)
dc <- divchain(x,y,z,rw=c(0,1,0,1))
plot(dc,lwd=2,col="blue",bty="o")

```

---

plot.tile.list

*Plot Dirchlet (Voronoi) tiles*


---

**Description**

A method for plot. Plots (sequentially) the tiles associated with each point in the set being tessellated.

**Usage**

```

## S3 method for class 'tile.list'
plot(x, verbose = FALSE, close = FALSE, pch = 1,
      fillcol = getCol(x,warn=warn), col.pts=NULL,
      col.num=NULL,border=NULL, showpoints = !number,
      add = FALSE, asp = 1, clipp=NULL, xlab = "x",
      ylab = "y", main = "", warn=FALSE,
      number=FALSE,adj=NULL,...)

```

**Arguments**

x	A list of the tiles in a tessellation, as produced the function <code>tile.list()</code> .
verbose	Logical scalar; if TRUE the tiles are plotted one at a time (with a “Go?” prompt after each) so that the process can be watched.
close	Logical scalar; if TRUE the outer edges of of the tiles (i.e. the edges which are contained in the enclosing rectangle) are drawn. Otherwise tiles on the periphery of the tessellation are left “open”.
pch	The plotting character (or vector of plotting characters) with which to plot the points of the pattern which was tessellated. Ignored if <code>showpoints</code> is FALSE.
fillcol	Optional vector (possibly of length 1, i.e. a scalar) whose entries can be interpreted as colours by <code>col2rgb()</code> . The <i>i</i> -th entry indicates with which colour to fill the <i>i</i> -th tile. Note that an NA entry cause the tile to be left unfilled. This argument will be replicated to have length equal to the number of tiles.
col.pts	Optional vector like unto <code>fillcol</code> whose entries can be interpreted as colours by <code>col2rgb()</code> . The <i>i</i> -th entry indicates with which colour to plot the <i>i</i> -th point. This argument will be replicated to have length equal to the number of tiles. Ignored if <code>showpoints</code> is FALSE.



col.num	Optional vector like unto col.pts. Determines the colours in which the point numbers (see number below). This argument will be replicated to have length equal to the number of tiles. Ignored if number is FALSE.
border	A <i>scalar</i> indicating the colour with which to plot the tile boundaries. Defaults to black unless all of the fill colours specified by fillcol are black, in which case it defaults to white. If length(border) > 1 then an error is given.
showpoints	Logical scalar; if TRUE the points of the pattern which was tessellated are plotted.
add	Logical scalar; should the plot of the tiles be added to an existing plot?
asp	The aspect ratio of the plot; integer scalar or NA. Set this argument equal to NA to allow the data to determine the aspect ratio and hence to make the plot occupy the complete plotting region in both x and y directions. This is inadvisable; see the <b>Warnings</b> .
clipp	An object specifying a polygon to which the tessellation being plotted should be clipped. It should consist either of: <ul style="list-style-type: none"> <li>• a list containing two components x and y giving the coordinates of the vertices of a single polygon. The last vertex should not repeat the first vertex. Or:</li> <li>• a list of list(x,y) structures giving the coordinates of the vertices of several polygons.</li> </ul> <p>If this argument is provided then the plot of the tessellation is “clipped” to the polygon specified by clipp.</p>
xlab	Label for the x-axis (used only if add is FALSE).
ylab	Label for the y-axis (used only if add is FALSE).
main	A title for the plot (used only if add is FALSE).
warn	Logical scalar passed to the internal function getCol(). Should a warning be issued if the z components of the entries of x cannot all be interpreted as colours. See <b>Notes</b> .
number	Logical scalar; if TRUE the numbers of the points determining the tiles are plotted in the tiles. Note that if number is TRUE then showpoints defaults to FALSE
adj	The “adjustment” argument to text(). If number and showpoints are both TRUE it defaults to -1 (so that the numbers and point symbols are not superimposed). If number is TRUE and showpoints is FALSE it defaults to 0. If number is FALSE it is ignored.
...	Optional arguments; may be passed to points() and text().

**Value**

NULL; side effect is a plot.

**Warnings**

- The behaviour of this function with respect to “clipping” has changed substantially since the previous release of deldir, i.e. 1.1-0. The argument clipwin has been re-named clipp (“p” for “polygon”). Clipping is now effected via the new package polyclip. The spatstat

package is no longer used. The argument `use.gpclip` has been eliminated, since `gpclip` (which used to be called upon by `spatstat` has been superceded by `polyclip` which has an unrestrictive license.

- As of release 0.1-1 of the `deldir` package, the argument `fillcol` to this function *replaces* the old argument `polycol`, but behaves somewhat differently.
- The argument `showrect` which was present in versions of this function prior to release 0.1-1 has been eliminated. It was redundant.
- As of release 0.1-1 the `col.pts` argument *might* behave somewhat differently from how it behaved in the past.
- The arguments `border`, `clipp`, and `warn` are new as of release 0.1-1.
- Users, unless they *really* understand what they are doing and why they are doing it, are *strongly advised* not to set the value of `asp` but rather to leave `asp` equal to its default value of 1. Any other value distorts the tessellation and destroys the perpendicular appearance of lines which are indeed perpendicular. (And conversely can cause lines which are not perpendicular to appear as if they are.)

### Notes

- If `clipp` is not `NULL` and `showpoints` is `TRUE` then it is possible that some of the points “shown” will not fall inside any of the plotted tiles. (This will happen if the parts of the tiles in which they fall have been “clipped” out.) If a tile is clipped out *completely* then the point which determines that tile is *not* plotted irrespective of the value of `showpoints`.
- If the `z` components of the entries of `x` cannot all be interpreted as colours (e.g. if there *aren't* any `z` components, which will be the case if no such values were supplied in the call to `deldir()`) then the internal function `getCol()` returns `NA`. This value of `fillcol` results (as is indicated by the argument list entry for `fillcol`) in (all of) the tiles being left unfilled.
- The new behaviour in respect of the colours with which to fill the plotted tiles, and the argument `clipp` were added at the request of Chris Triggs.
- The argument `asp` was added at the request of Zubin Dowlaty.

### Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

### See Also

[deldir\(\)](#), [tile.list\(\)](#), [triang.list\(\)](#), [plot.triang.list\(\)](#)

### Examples

```
set.seed(42)
x <- runif(20)
y <- runif(20)
z <- deldir(x,y,rw=c(0,1,0,1))
w <- tile.list(z)
plot(w)
ccc <- heat.colors(20) # Or topo.colors(20), or terrain.colors(20)
# or cm.colors(20), or rainbow(20).
```

```

plot(w,fillcol=ccc,close=TRUE)
if(require(polyclip)) {
  CP <- list(x=c(0.49,0.35,0.15,0.20,0.35,0.42,
               0.43,0.62,0.46,0.63,0.82,0.79),
            y=c(0.78,0.86,0.79,0.54,0.58,0.70,
               0.51,0.46,0.31,0.20,0.37,0.54))
  plot(w,clipp=CP,showpoints=FALSE,fillcol=topo.colors(20))
}
plot(w,number=TRUE,col.num="red")
plot(w,number=TRUE,col.num="red",cex=0.5)
plot(w,showpoints=TRUE,number=TRUE,col.pts="green",col.num="red")

```

---

plot.triang.list	<i>Plot Delaunay triangles</i>
------------------	--------------------------------

---

### Description

A method for plot. Plots the triangles of a Delaunay triangulation of a set of points in the plane.

### Usage

```

## S3 method for class 'triang.list'
plot(x, showrect = FALSE, add = FALSE,
      xlab = "x", ylab = "y", main = "", asp = 1, ...)

```

### Arguments

x	An object of class “triang.list” as produced by <code>triang.list()</code> .
showrect	Logical scalar; show the enclosing rectangle rw (see <code>deldir()</code> ) be plotted?
add	Logical scalar; should the plot of the triangles be added to an existing plot?
xlab	Label for the x-axis.
ylab	Label for the y-axis.
main	A title for the plot (used only if add is FALSE).
asp	The aspect ratio of the plot; integer scalar or NA. Set this argument equal to NA to allow the data to determine the aspect ratio and hence to make the plot occupy the complete plotting region in both x and y directions. This is inadvisable; see the <b>Warnings</b> .
...	Arguments passed to <code>polygon()</code> which does the actual plotting of the triangles.

### Value

None. This function has the side effect of producing (or adding to) a plot.

### Warnings

The user is *strongly advised* not to set the value of `asp` but rather to leave `asp` equal to its default value of 1. Any other value distorts the tessellation and destroys the perpendicular appearance of lines which are indeed perpendicular. (And conversely can cause lines which are not perpendicular to appear as if they are.)

The argument `asp` was added at the request of Zubin Dowlaty.

### Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

### See Also

[deldir\(\)](#), [plot.triang.list\(\)](#), [tile.list\(\)](#), [plot.tile.list\(\)](#)

### Examples

```
set.seed(42)
x <- runif(20)
y <- runif(20)
d <- deldir(x,y)
ttt <- triang.list(d)
plot(ttt,border="red",showrect=TRUE)
sss <- tile.list(d)
plot(sss)
plot(ttt,add=TRUE,border="blue")
```

---

print.tileInfo	<i>Print a summary of tile information.</i>
----------------	---

---

### Description

Print a reasonably readable summary of an object of class `tileInfo` as produced by the `tileInfo()` function.

### Usage

```
## S3 method for class 'tileInfo'
print(x, digits = 4, ...)
```

### Arguments

<code>x</code>	An object of class <code>tileInfo</code> as produced by the <code>tileInfo()</code> function.
<code>digits</code>	The (maximum) number of decimal digits to which the output is to be printed.
<code>...</code>	Not used. Present for compatibility with the generic <code>print()</code> function.

## Details

The list produced by `tileInfo()` is a bit messy and hard to comprehend, especially if there is a large number of tiles. This print method produces a screen display which is somewhat more perspicuous.

There are three components to the display:

- A matrix, each row of which is the vector of edge lengths of the tile. The number of columns is the *maximum* of the lengths of the edge length vectors. Rows corresponding to shorter vectors are filled in with blanks. The row names of the matrix indicate the number of the point corresponding to the tile. Note that this number is the index of the point in the original sequence of points that is being tessellated.
- A table of the edge counts of the tiles.
- A simple print out of the areas of the tiles (rounded to a maximum of digits decimal digits).

This screen display is for “looking at” only. In order to do further calculations on the output of `tileInfo` it is necessary to delve into the bowels of `x` and extract the relevant bits.

In order to get a decent looking display you may (if there are tiles with a large number of edges) need to widen the window in which you are displaying the output and increase the value of the `width` option. E.g. use `options(width=120)`.

## Value

None.

## Author(s)

Rolf Turner <r.turner@auckland.ac.nz>

## See Also

[tileInfo\(\)](#)

## Examples

```
set.seed(179)
x <- runif(100)
y <- runif(100)
dxy <- deldir(x,y,rw=c(0,1,0,1))
ixy1 <- tileInfo(dxy)
print(ixy1)
ixy2 <- tileInfo(dxy,bndry=TRUE)
print(ixy2)
```

---

seaweed	<i>seaweed</i>
---------	----------------

---

### Description

A data frame whose columns are the coordinates of the centroids of the cells in a seaweed frond. The points are estimates-by-eye of where the centroids of the cells occur.

### Usage

```
data("seaweed")
```

### Format

A data frame with 266 observations on the following 2 variables.

x The  $x$ -coordinates of the cell centroids.

y The  $y$ -coordinates of the cell centroids.

### Source

These data were kindly supplied by Dr. John Bothwell of the Department of Biosciences, Durham University. The data were collected by Kevin Yun and Georgia Campbell, members of Dr. Bothwell's research group.

### Examples

```
# data(seaweed)
# It is unnecessary to use \code{data} since \code{seaweed} is
# a "first class object". It is "lazily loaded".

dsw <- deldir(seaweed)
isw <- tileInfo(dsw)
options(width=120)
# Expand the width of the terminal window.
isw
tsw <- tile.list(dsw)
plot(tsw,number=TRUE,col.num="red",cex=0.5,adj=0.5)
```

---

tile.centroids	<i>Compute centroids of Dirichlet (Voronoi) tiles</i>
----------------	---

---

**Description**

Given a list of Dirichlet tiles, as produced by `tile.list()`, produces a data frame consisting of the centroids of those tiles.

**Usage**

```
tile.centroids(xxx)
```

**Arguments**

xxx                    A list of the tiles (produced by `tile.list()`) in a Dirichlet tessellation of a set of planar points.

**Value**

A data frame with two columns named `x` and `y`. Each row of this data frame constitutes the centroid of one of the Dirichlet tiles.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**References**

URL <http://en.wikipedia.org/wiki/Centroid>

**See Also**

[tile.list\(\)](#)

**Examples**

```
set.seed(42)
x <- runif(20)
y <- runif(20)
d <- deldir(x,y)
l <- tile.list(d)
g <- tile.centroids(l)
## Not run:
plot(l,close=TRUE)
points(g,pch=20,col="red")

## End(Not run)
```

---

tile.list	<i>Create a list of tiles in a tessellation</i>
-----------	---

---

### Description

For each point in the set being tessellated produces a list entry describing the Dirichlet/Voronoi tile containing that point.

### Usage

```
tile.list(object)
```

### Arguments

object            An object of class `deldir` as produced by the function `deldir()`.

### Value

A list with one entry for each of the points in the set being tessellated. Each entry is in turn a list with components

ptNum	The index of the point in the original sequence of points that is being tessellated. Note that if a point is one of a set of <i>duplicated</i> points then ptNum is the <i>first</i> of the indices of the points in this set.
pt	The coordinates of the point whose tile is being described.
ptType	The “type” of the pt, either “data” or “dummy”. Present only if any dummy points were specified in the call to <code>deldir()</code> .
x	The x coordinates of the vertices of the tile, in anticlockwise order.
y	The y coordinates of the vertices of the tile, in anticlockwise order.
bp	Vector of logicals indicating whether the tile vertex is a “real” vertex, or a <i>boundary point</i> , i.e. a point where the tile edge intersects the boundary of the enclosing rectangle.
z	The “auxiliary value” or “weight” associated with the pt; present only if such values were supplied in the call to <code>deldir()</code> .
area	The area of the tile.

### Acknowledgement

The author expresses sincere thanks to Majid Yazdani who found and pointed out a serious bug in `tile.list` in a previous version (0.0-5) of the `deldir` package.



**Warning**

The set of vertices of each tile may be “incomplete”. Only vertices which lie within the enclosing rectangle, and “boundary points” are listed.

Note that the enclosing rectangle may be specified by the user in the call to `deldir()`.

In contrast to some earlier versions of `deldir`, the corners of the enclosing rectangle are now include as vertices of tiles. I.e. a tile which in fact extends beyond the rectangular window and contains a corner of that window will have that corner added to its list of vertices. Thus the corresponding polygon is the intersection of the tile with the enclosing rectangle.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

`deldir()`, `plot.tile.list()` `triang.list()` `plot.triang.list()`

**Examples**

```
x <- runif(20)
y <- runif(20)
z <- deldir(x,y)
w <- tile.list(z)

z <- deldir(x,y,rw=c(0,1,0,1))
w <- tile.list(z)

z <- deldir(x,y,rw=c(0,1,0,1),dpl=list(ndx=2,ndy=2))
w <- tile.list(z)
```

---

tileInfo

*Extract information from a tile list.*

---

**Description**

Produces a summary of information about the tiles in an object of class `deldir` as produced by the function `deldir()`.

**Usage**

```
tileInfo(object, bndry = FALSE)
```

**Arguments**

`object` An object of class `deldir` as produced by the function `deldir()`.

`bndry` Logical scalar. If TRUE then the “boundary” tiles (those tiles having edges forming part of the “rectangular window” enclosing the tessellation) are included in the summary. Otherwise they are not included.

**Value**

A list with components:

<code>indivTiles</code>	This is itself a list with one entry for each tile in “object”. It is in fact a <i>named</i> list, the names being of form <code>tile.n</code> , where <code>n</code> is equal to the value of <code>ptNum</code> (see below) corresponding to the tile. The entries of <code>indivTiles</code> are themselves in turn lists with entries <code>edgeLengths</code> (a vector of the lengths of the edges of the tiles), <code>numEdges</code> (an integer equal to the number of edges of the tile), <code>area</code> (a positive number equal to the area of the tile) and <code>ptNum</code> (an integer equal to the number of the point determining the tile). Note that <code>ptNum</code> is the number of the point in the <i>original</i> sequence of points that were tessellated.
<code>allEdgeCounts</code>	An integer vector of the edge counts (given by <code>numEdge</code> for each tile) of the tiles.
<code>tabEdgeCounts</code>	A table of <code>numEdge</code> .
<code>allEdgeLengths</code>	A vector of all of the tile edge lengths; a catenation of the <code>edgeLengths</code> components of the entries of <code>indivTiles</code> . Note that there will be many duplicate lengths since each tile edge is, in general, an edge of <i>two</i> tiles.
<code>Areas</code>	A vector of the areas of the tiles.
<code>uniqueEdgeLengths</code>	A vector of the lengths of the tiles edges with the duplicates (which occur in <code>allEdgeLengths</code> ) being eliminated. Each tile edge is represented only once.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

`deldir()` `tile.list()` `print.tileInfo()`

**Examples**

```
set.seed(42)
x <- runif(20)
y <- runif(20)
dxy <- deldir(x,y,rw=c(0,1,0,1))
ixy1 <- tileInfo(dxy)
ixy2 <- tileInfo(dxy,bndry=TRUE)
```

---

tilePerim

*Calculate tile perimeters.*

---

**Description**

Calculates the perimeters of all of the Dirichlet (Voronoi) tiles in a tessellation of a set of planar points. Also calculates the sum and the mean of these perimeters.



---

`triang.list`*Create a list of Delaunay triangles*

---

**Description**

From an object of class “deldir” produces a list of the Delaunay triangles in the triangulation of a set of points in the plane.

**Usage**

```
triang.list(object)
```

**Arguments**

`object` An object of class “deldir” as produced by `deldir()`.

**Value**

A list each of whose components is a  $3 \times 3$ ,  $3 \times 4$  or  $3 \times 5$  data frame corresponding to one of the Delaunay triangles specified by “object”. The rows of each such data frame correspond to the vertices of the corresponding Delaunay triangle. The columns are:

- `ptNum` (the index of the point in the original sequence of points that is being triangulated. Note that if a point is one of a set of *duplicated* points then `ptNum` is the *first* of the indices of the points in this set.)
- `ptType` (the type of the vertex; “data” or “dummy”; present only if there were any dummy points specified)
- `x` (the  $x$ -coordinate of the vertex)
- `y` (the  $y$ -coordinate of the vertex)
- `z` (the “auxiliary value” or “weight”  $z$  associated with the vertex; present only if such values were supplied in the call to `deldir()`)

The returned value has an attribute “`rw`” consisting of the enclosing rectangle of the triangulation.

**Note**

The code of this function was taken more-or-less directly from code written by Adrian Baddeley for the “`delaunay()`” function in the “`spatstat`” package.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

`deldir()`, `plot.triang.list()`, `tile.list()`, `plot.tile.list()`

## Examples

```
set.seed(42)
x <- runif(20)
y <- runif(20)
z <- sample(1:100,20)
d <- deldir(x,y,z=z)
ttt <- triang.list(d)
```

---

triMat	<i>Produce matrix of triangle vertex indices.</i>
--------	---

---

## Description

Lists the indices of the vertices of each Delaunay triangle in the triangulation of a planar point set. The indices are listed (in increasing numeric order) as the rows of an  $n \times 3$  matrix where  $n$  is the number of Delaunay triangles in the triangulation.

## Usage

```
triMat(object)
```

## Arguments

**object** An object of class `deldir` (as produced by the function `deldir()`) specifying the Delaunay triangulation and Dirichlet (Voronoi) tessellation of a planar point set.

## Details

This function was suggested by Robin Hankin of the School of Mathematical and Computing Sciences at Auckland University of Technology.

## Value

An  $n \times 3$  matrix where  $n$  is the number of Delaunay triangles in the triangulation specified by `object`. The  $i^{th}$  row consists of the indices (in the original list of points being triangulated) of vertices of the  $i^{th}$  Delaunay triangle. The indices are listed in increasing numeric order in each row.

## Note

Earlier versions of this function (prior to release 0.1-14 of **deldir**) could sometimes give incorrect results. This happened if the union of three contiguous Delaunay triangles happened to constitute another triangle. This latter triangle would appear in the list of triangles produced by `triMat()` but is *not* itself a Delaunay triangle. The updated version of `triMat()` now checks for this possibility and gives (*I think!*) correct results.

Many thanks to Jay Call, who pointed out this bug to me.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

[deldir\(\)](#) [triang.list\(\)](#) [plot.triang.list\(\)](#)

**Examples**

```
# These are the data used by Jay Call to illustrate the bug
# that appeared in a previous incarnation of triMat.
xy <- data.frame(
  x = c(0.048,0.412,0.174,0.472,0.607,0.565,0.005,0.237,0.810,0.023),
  y = c(0.512,0.928,0.955,0.739,0.946,0.134,0.468,0.965,0.631,0.782)
)
dxy <- deldir(xy)
M <- triMat(dxy)
plot(dxy,wlines="triang",num=TRUE,axes=FALSE,col=c(1,1,1,1,2))
# The triangle with vertices {4,5,8} was listed in the output of
# the previous (buggy) version of triMat(). It is NOT a Delaunay
# triangle and hence should NOT be listed.
```

---

which.tile

*Determine the tile containing a given point.*

---

**Description**

Finds the Dirchlet/Voronoi tile of a tessellation produced by `deldir` that contains a given point.

**Usage**

```
which.tile(x, y, tl)
```

**Arguments**

<code>x</code>	The x coordinate of the point in question.
<code>y</code>	The y coordinate of the point in question.
<code>tl</code>	A tile list, as produced by the function <code>tile.list()</code> from a tessellation produced by <code>deldir()</code> .

**Details**

Just minimises the distance from the point in question to the points of the pattern determining the tiles.

**Value**

An integer equal to the index of the tile in which the given point lies.

**Author(s)**

Rolf Turner <r.turner@auckland.ac.nz>

**See Also**

[tile.list\(\)](#) [deldir\(\)](#).

**Examples**

```
set.seed(42)
x <- runif(20,0,100)
y <- runif(20,0,100)
dxy <- deldir(x,y)
txy <- tile.list(dxy)
i <- which.tile(30,50,txy) # The value of i here is 14.
plot(txy,showpoints=FALSE)
text(x,y,labels=1:length(txy),col="red")
points(30,50,pch=20,col="blue")
```

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