Package ‘diseq’

May 12, 2021

Title    Estimation Methods for Markets in Equilibrium and Disequilibrium
Version  0.3.1
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Description Provides estimation methods for markets in equilibrium and
disequilibrium. Supports the estimation of an equilibrium and
four disequilibrium models with both correlated and independent shocks.
Also provides post-estimation analysis tools, such as aggregation,
marginal effect, and shortage calculations. The estimation methods are
based on full information maximum likelihood techniques given in
using the analytic derivative expressions calculated in
errors can be estimated by adjusting for heteroscedasticity or clustering.
The equilibrium estimation constitutes a case of a system of linear,
simultaneous equations. Instead, the disequilibrium models replace the
market-clearing condition with a non-linear,
short-side rule and allow for different specifications of price dynamics.

Language en-US

URL  https://github.com/pi-kappa-devel/diseq/
      https://diseq.pi-kappa.eu/

BugReports https://github.com/pi-kappa-devel/diseq/issues

Depends R (>= 3.5.0)

Imports bbmle (>= 1.0.20), dplyr (>= 0.7.6), grid, magrittr (>= 1.5),
      MASS (>= 7.3-50), methods, rlang (>= 0.2.1), systemfit (>=
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      RcppParallel

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Encoding UTF-8

LazyData true

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Suggests ggplot2 (>= 3.0.0), knitr (>= 1.20), numDeriv (>=
      2016.8.1.1), rmarkdown (>= 1.10), testthat (>= 2.0.0)
VignetteBuilder knitr

Collate 'data.R' 'diseq.R' 'equation_base.R' 'system_base.R'
  'diseq_basic.R' 'diseq_deterministic_adjustment.R'
  'diseq_directional.R' 'diseq_stochastic_adjustment.R'
  'equation_basic.R' 'equation_deterministic_adjustment.R'
  'equation_directional.R' 'equation_stochastic_adjustment.R'
  'equilibrium_model.R' 'system_basic.R' 'gradient_basic.R'
  'system_deterministic_adjustment.R'
  'gradient_deterministic_adjustment.R' 'system_directional.R'
  'gradient_directional.R' 'system_equilibrium.R'
  'gradient_stochastic_adjustment.R' 'hessian_basic.R'
  'hessian_directional.R' 'likelihood_basic.R'
  'likelihood_deterministic_adjustment.R'
  'likelihood_directional.R' 'likelihood_equilibrium.R'
  'likelihood_stochastic_adjustment.R' 'model_simulation.R'

LinkingTo Rcpp, RcppGSL

SystemRequirements C++11

NeedsCompilation yes

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The `diseq` package provides tools to estimate and analyze an equilibrium and four disequilibrium models. The equilibrium model can be estimated with either two-stage least squares or with full information maximum likelihood. The methods are asymptotically equivalent. The disequilibrium models are estimated using full information maximum likelihood. All maximum likelihood models can be estimated both with independent and correlated demand and supply shocks. The disequilibrium estimation is based on Maddala and Nelson (1974) doi: 10.2307/1914215. The package is using the expressions of the gradients of the likelihoods derived in Karapanagiotis (2020) doi: 10.2139/ssrn.3525622.

## Details

### Overview

This page gives an overview of the market model classes and the available documentation options of the package.

**Usage:** The easiest way to get accustomed with the functionality of the package is to check the accompanying vignettes and the README file. These can be found in the following links:

- `basic_usage` vignette("basic_usage",package = "diseq")
- `equilibrium_assessment` vignette("market_clearing_assessment",package = "diseq")

Additionally, one can use the documentation examples. Some of them illustrate the package functionality using the `houses` dataset.

**Market model classes:** The model hierarchy is described in the README file. See the documentation of the classes for initialization details.

**Equilibrium model classes:**

- `equilibrium_model` Equilibrium model that can be estimated using full information maximum likelihood or two-stage least squares.

**Disequilibrium model classes:**

- `diseq_basic` Disequilibrium model only with a basic short side rule.
- `diseq_directional` Disequilibrium model with directional sample separation.
equation_classes

diseq_deterministic_adjustment  Disequilibrium model with deterministic price dynamics.
diseq_stochastic_adjustment  Disequilibrium model with stochastic price dynamics.

---

**Description**

Equation classes

**Details**

Classes with data and functionality describing equations of model systems.

**Functions**

- `equation_base-class`: Equation base class
- `equation_basic-class`: Basic disequilibrium model equation class
- `equation_deterministic_adjustment-class`: Deterministic adjustment disequilibrium model equation class
- `equation_directional-class`: Directional disequilibrium model equation class
- `equation_stochastic_adjustment-class`: Stochastic adjustment disequilibrium model equation class

**Slots**

- `prefixed_specification`: The equation formula using prefixed variables.
- `formula`: The equation formula.
- `linear_model`: The estimated equation using linear regression.
- `name`: The name of the equation.
- `variable_prefix`: A prefix string for the variables of the equation.
- `independent_variables`: A vector with the right hand side variable names.
- `price_variable`: The price variable name.
- `control_variables`: Independent variables without the price variable.
- `independent_matrix`: A model data matrix with columns corresponding to the set of independent variables.
- `price_vector`: The vector of prices.
- `control_matrix`: A model data matrix with columns corresponding to the set of independent variables without prices.
- `alpha_beta`: A vector of right hand side coefficients.
- `alpha`: The price coefficient.
- `beta`: A vector of right hand side coefficient without the price coefficient.
var The variance of the equation’s shock.
sigma The standard deviation of the equation’s shock.

\[ h_x = \frac{x - \text{Ex}}{\sqrt{\text{Var}x}} \]

\[ z_{xy} = \frac{h_x - \rho_{xy}h_y}{\sqrt{1 - \rho_{xy}^2}} \]

psi

\[ \psi_x = \phi(h_x) \]

Psi

\[ \Psi_x = 1 - \Phi(z_{xy}) \]

mu_Q

\[ \mu_Q = \text{E}Q \]

var_Q

\[ V_Q = \text{Var}Q \]

sigma_Q

\[ \sigma_Q = \sqrt{\text{Var}Q} \]

den_Q

\[ \rho_Q = \frac{\text{Cov}(Q, P)}{\sqrt{\text{Var}Q \text{Var}P}} \]

rho_{1QP}

\[ \rho_{1,QP} = \frac{1}{\sqrt{1 - \rho_{QP}}} \]

rho_{2QP}

\[ \rho_{2,QP} = \rho_{QP}\rho_{1,QP} \]

sigma_{QP}

\[ \sigma_{QP} = \text{Cov}(Q, P) \]

h_Q As in slot h
z_{PQ} As in slot z
z_{QP} As in slot z

separation_subset A vector of indicators specifying the observations of the sample described by this equation according to the separation rule of the model.
Model estimation.

Description

All models are estimated using full information maximum likelihood. The \texttt{equilibrium\_model} can also be estimated using two-stage least squares. The maximum likelihood estimation is based on \texttt{mle2}. If no starting values are provided, the function uses linear regression estimates as initial values. The default optimization method is BFGS. For other alternatives see \texttt{mle2}. The implementation of the two-stage least square estimation of the \texttt{equilibrium\_model} is based on \texttt{systemfit}.

Usage

\begin{verbatim}
estimate(object, ...)

## S4 method for signature 'market_model'
estimate(
  object,
  gradient = "calculated",
  hessian = "calculated",
  standard_errors = "homoscedastic",
  ...
)

## S4 method for signature 'equilibrium_model'
estimate(object, method = "BFGS", ...)
\end{verbatim}

Arguments

\begin{itemize}
  \item \texttt{object} A model object.
  \item \texttt{...} Named parameter used in the model's estimation. These are passed further down to the estimation call. For the \texttt{equilibrium\_model} model, the parameters are passed to \texttt{systemfit}, if the method is set to 2SLS, or to \texttt{mle2} for any other method. For the rest of the models, the parameters are passed to \texttt{mle2}.
  \item \texttt{gradient} One of two potential options: 'numerical' and 'calculated'. By default, all the models are estimated using the analytic expressions of their likelihoods' gradients.
  \item \texttt{hessian} One of three potential options: 'skip', 'numerical', and 'calculated'. The default is to use the 'calculated' Hessian for the model that expressions are available and the 'numerical' Hessian in other cases. Calculated Hessian expressions are available for the basic and directional models.
  \item \texttt{standard_errors} One of three potential options: 'homoscedastic', 'heteroscedastic', or a vector with variables names for which standard error clusters are to be created. The default value is 'homoscedastic'. If the option 'heteroscedastic' is passed,
the variance-covariance matrix is calculated using heteroscedasticity adjusted (Huber-White) standard errors. If the vector is supplied, the variance-covariance matrix is calculated by grouping the score matrix based on the passed variables.

method
A string specifying the estimation method. When the passed value is among Nelder-Mead, BFGS, CG, L-BFGS-B, SANN, and Brent, the model is estimated using full information maximum likelihood based on mle2 functionality. When 2SLS is supplied, the model is estimated using two-stage least squares based on systemfit. In this case, the function returns a list containing the first and second stage estimates. The default value is BFGS.

Value
The object that holds the estimation result.

Functions
- estimate,market_model-method: Full information maximum likelihood estimation.

Examples

```r
# initialize the model using the houses dataset
model <- new("diseq_deterministic_adjustment", # model type
c("ID", "TREND"), "TREND", "HS", "RM", # keys, time, quantity, and price variables
"RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
"RM + TREND + W + L1RM + MA6DSF + MA3DHF + MONTH", # supply specification
fair_houses(), # data
correlated_shocks = FALSE # allow shocks to be correlated
)

# estimate the model object (BFGS is used by default)
est <- estimate(model)

# estimate the model by specifying the optimization details passed to the optimizer.
est <- estimate(model, control = list(maxit = 1e+5), method = "BFGS")

# summarize results
bbmle::summary(est)
```

---

**gradient**

**Gradient**

- **Description**
  Returns the gradient of the opposite of the log-likelihood evaluated at the passed parameters.
Usage

```r
gradient(object, parameters)
## S4 method for signature 'diseq_basic'
gradient(object, parameters)
## S4 method for signature 'diseq_deterministic_adjustment'
gradient(object, parameters)
## S4 method for signature 'diseq_directional'
gradient(object, parameters)
## S4 method for signature 'diseq_stochastic_adjustment'
gradient(object, parameters)
## S4 method for signature 'equilibrium_model'
gradient(object, parameters)
```

Arguments

- `object`: A model object.
- `parameters`: A vector of parameters at which the gradient is to be evaluated.

Value

The opposite of the model log likelihood's gradient.

Description

Returns the hessian of the opposite of the log-likelihood evaluated at the passed parameters.

Usage

```r
hessian(object, parameters)
## S4 method for signature 'diseq_basic'
hessian(object, parameters)
## S4 method for signature 'diseq_directional'
hessian(object, parameters)
```

Arguments

- `object`: A model object.
- `parameters`: A vector of parameters at which the hessian is to be evaluated.
Value
The opposite of the model log likelihood’s hessian.

<table>
<thead>
<tr>
<th>houses</th>
<th>Credit market data for US housing starts</th>
</tr>
</thead>
</table>

Description
Credit market data for US housing starts

Usage
data(houses)
fair_houses()

Format
A data frame with 138 rows and 7 columns

Details
The basic houses dataset (houses):
A dataset containing the monthly mortgage rates and other attributes of the US market for new, non-farm houses from July 1958 to December 1969. The variables are as follows:
- DATE The date of the record.
- HS Private non-farm housing starts in thousands of units (Not seasonally adjusted).
- RM FHA Mortgage rate series on new homes in units of 100 (beginning-of-month Data).
- DSLA Savings capital (deposits) of savings and loan associations in millions of dollars.
- DMSB Deposits of mutual savings banks in millions of dollars.
- DHLB Advances of the federal home loan bank to savings and loan associations in million of dollars.
- W Number of working days in month.

Generate the variables of the Fair & Jaffee (1972) dataset. (fair_houses):
Loads the houses dataset and creates the additional variables used by Fair & Jaffee (1972) doi: 10.2307/1913181. These are
- ID A dummy entity identifier that is always equal to one since the houses data have only a time series component.
- DSF Flow of deposits in savings and loan associations and mutual savings banks in million of dollars. Equal to

\[ DSLA_t + DMSB_t - (DSL A_{t-1} + DMSB_{t-1}). \]
• **DHF** Flow of advances of the federal home loan bank to savings and loan associations in million of dollars. Equal to \( DHLB_t - DHLB_{t-1} \).

• **MONTH** The month of the date of the observation.

• **L1RM** FHA Mortgage rate series on new homes in units of 100, lagged by one date.

• **L2RM** FHA Mortgage rate series on new homes in units of 100, lagged by two dates.

• **L1HS** Private non-farm housing starts in thousands of units (Not seasonally adjusted), lagged by one date.

• **CSHS** The cumulative sum of past housing starts. Used to proxy the stock of houses

• **MA6DSF** Moving average of order 6 of the flow of deposits in savings associations and loan associations and mutual savings banks.

• **MA3DHF** Moving average of order 3 of the flow of advances of the federal home loan bank to savings and loan associations.

• **TREND** A time trend variable.

Returns A modified version of the `houses` dataset.

**Functions**

- `fair_houses`: Generate Fair & Jaffee (1972) dataset

**Source**

- **HS** Economic Reports of the President
- **RM** Fair (1971)
- **DLSA** Federal Reserve Bulletins
- **DMSB** Federal Reserve Bulletins
- **DHLB** Federal Reserve Bulletins
- **W** Manually calculated

**References**


**Examples**

data(houses)
head(houses)
head(fair_houses())
initialize_market_model

Model initialization

Description

Model initialization

Usage

```r
## S4 method for signature 'diseq_basic'
initialize(
  .Object,
  key_columns,
  quantity_column,
  price_column,
  demand_specification,
  supply_specification,
  data,
  correlated_shocks = TRUE,
  verbose = 0
)
```

```r
## S4 method for signature 'diseq_deterministic_adjustment'
initialize(
  .Object,
  key_columns,
  time_column,
  quantity_column,
  price_column,
  demand_specification,
  supply_specification,
  data,
  correlated_shocks = TRUE,
  verbose = 0
)
```

```r
## S4 method for signature 'diseq_directional'
initialize(
  .Object,
  key_columns,
  time_column,
  quantity_column,
  price_column,
  demand_specification,
  supply_specification,
  data,
)
correlated_shocks = TRUE,
verbose = 0
)

## S4 method for signature 'diseq_stochastic_adjustment'
initialize(
  .Object,
  key_columns,
  time_column,
  quantity_column,
  price_column,
  demand_specification,
  supply_specification,
  price_specification,
  data,
  correlated_shocks = TRUE,
  verbose = 0
)

## S4 method for signature 'equilibrium_model'
initialize(
  .Object,
  key_columns,
  quantity_column,
  price_column,
  demand_specification,
  supply_specification,
  data,
  correlated_shocks = TRUE,
  verbose = 0
)

### Arguments

- **.Object** The object to be constructed.
- **key_columns** Key columns of the data set.
- **quantity_column** The quantity variable of the data set.
- **price_column** The price variable of the data set.
- **demand_specification** A formula representation of the right hand side of the demand equation.
- **supply_specification** A formula representation of the right hand side of the supply equation.
- **data** The data set.
- **correlated_shocks** Should the model be estimated using correlated shocks?
- **verbose** Verbosity level.
### Details

The following two subsections describe the common initialization steps of all market model classes.

**Variable construction:** The constructor prepares the model’s variables using the passed specifications. The specification strings are expected to follow the syntax of `formula`. The construction of the model’s data uses the variables that are extracted by these specification. The demand variables are extracted by a formula that uses the `quantity_column` on the left hand side and the `demand_specification` on the right hand side of the formula. The supply variables are constructed by the `quantity_column` and the `supply_specification`. In the case of the `diseq_stochastic_adjustment` model, the price dynamics’ variables are extracted using the `price_specification`. The `price_specification` for the `diseq_stochastic_adjustment` should contain only terms other than that of excess demand. The excess demand term of the price equation is automatically added by the constructor.

**Data preparation:**

1. If the passed data set contains rows with NA values, they are dropped. If the verbosity level allows warnings, a warning is emitted reporting how many rows were dropped.
2. After dropping the rows, factor levels may be invalidated. If needed, the constructor readjusts the factor variables by removing the unobserved levels. Factor indicators and interaction terms are automatically created.
3. The primary key column is constructed by pasting the values of the `key_columns`.
4. In the cases of the `diseq_directional`, `diseq_deterministic_adjustment`, and the `diseq_stochastic_adjustment` models, a column with lagged prices is constructed. Since lagged prices are unavailable for the observations of the first time point, these observations are dropped. If the verbosity level allows the emission of information messages, the constructor prints the number of dropped observations.
5. In the cases of the `diseq_directional` and the `diseq_stochastic_adjustment` models, a column with price differences is created.

### Value

The initialized model.

### Functions

- `initialize,diseq_basic-method`: Basic disequilibrium model base constructor
- `initialize,diseq_deterministic_adjustment-method`: Disequilibrium model with deterministic price adjustment constructor
- `initialize,diseq_directional-method`: Directional disequilibrium model base constructor
- `initialize,diseq_stochastic_adjustment-method`: Disequilibrium model with stochastic price adjustment constructor
- `initialize,equilibrium_model-method`: Equilibrium model constructor
initialize_market_model

Examples

simulated_data <- simulate_data(
  "diseq_basic", 500, 3, # model type, observed entities, observed time points
  -0.9, 8.9, c(0.3, -0.2), c(-0.03, -0.01), # demand coefficients
  0.9, 4.2, c(0.03), c(-0.05, 0.02) # supply coefficients
)

# initialize the model
model <- new(
  "diseq_basic", # model type
  c("id", "date"), "Q", "P", # keys, quantity, and price variables
  "P + Xd1 + Xd2 + X1 + X2", "P + Xs1 + X1 + X2", # equation specifications
  simulated_data, # data
  correlated_shocks = FALSE # use independent shocks
)

show(model)

simulated_data <- simulate_data(
  "model type, observed entities and time points
  "diseq_deterministic_adjustment", 500, 3, # model type, observed entities, observed time points
  -0.9, 8.9, c(0.03, -0.02), c(-0.03, -0.01), # demand coefficients
  0.9, 4.2, c(0.03), c(0.05, 0.02), # supply coefficients
  1.4 # price adjustment coefficient
)

# initialize the model
model <- new(
  "diseq_deterministic_adjustment", # model type
  c("id", "date"), "date", "Q", "P", # keys, quantity, and price variables
  "P + Xd1 + Xd2 + X1 + X2", "P + Xs1 + X1 + X2", # equation specifications
  simulated_data, # data
  correlated_shocks = TRUE # allow shocks to be correlated
)

show(model)

simulated_data <- simulate_data(
  "model type, observed entities, observed time points
  "diseq_directional", 500, 3, # model type, observed entities, observed time points
  -0.2, 4.3, c(0.03, 0.02), c(0.03, 0.01), # demand coefficients
  0.0, 4.0, c(0.03), c(0.05, 0.02) # supply coefficients
)

# in the directional model prices cannot be included in both demand and supply
model <- new(
  "diseq_directional", # model type
  c("id", "date"), "date", "Q", "P", # keys, time point, quantity, and price variables
  "P + Xd1 + Xd2 + X1 + X2", "Xs1 + X1 + X2", # equation specifications
  simulated_data, # data
  correlated_shocks = TRUE # allow shocks to be correlated
)
marginal_effects

returns the estimated effect of a variable.
Usage

shortage_marginal(object, parameters, variable)
shortage_probability_marginal(object, parameters, variable, aggregate = "mean")

## S4 method for signature 'disequilibrium_model'
shortage_marginal(object, parameters, variable)

## S4 method for signature 'disequilibrium_model'
shortage_probability_marginal(object, parameters, variable, aggregate = "mean")

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>object</td>
<td>A disequilibrium model object.</td>
</tr>
<tr>
<td>parameters</td>
<td>A vector of parameters.</td>
</tr>
<tr>
<td>variable</td>
<td>Variable name for which the effect is calculated.</td>
</tr>
<tr>
<td>aggregate</td>
<td>Mode of aggregation. Valid options are &quot;mean&quot; (the default) and &quot;at_the_mean&quot;.</td>
</tr>
</tbody>
</table>

Value

The estimated effect of the passed variable.

Functions

- **shortage_marginal**: Marginal effect on market system

  Returns the estimated marginal effect of a variable on the market system. For a system variable \( x \) with demand coefficient \( \beta_{d,x} \) and supply coefficient \( \beta_{s,x} \), the marginal effect on the market system is given by

  \[
  M_x = \frac{\beta_{d,x} - \beta_{s,x}}{\sqrt{\sigma_{d,x}^2 + \sigma_{s,x}^2 - 2\rho_{ds}\sigma_{d,x}\sigma_{s,x}}}. 
  \]

- **shortage_probability_marginal**: Marginal effect on shortage probabilities

  Returns the estimated marginal effect of a variable on the probability of observing a shortage state. The mean marginal effect on the shortage probability is given by

  \[
  M_x \phi(D - S) 
  \]

  and the marginal effect at the mean by

  \[
  M_x \phi(E(D - S)), 
  \]

  where \( M_x \) is the marginal effect on the system, \( D \) is the demanded quantity, \( S \) the supplied quantity, and \( \phi \) is the standard normal density.
# Examples

```r
# initialize the model using the houses dataset
model <- new(
  "diseq_deterministic_adjustment", # model type
  c("ID", "TREND"), "TREND", "HS", "RM", # keys, time, quantity, and price variables
  "RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
  "RM + TREND + W + L1RM + MA6DSF + MA3DHF + MONTH", # supply specification
  fair_houses(), # data
correlated_shocks = FALSE # allow shocks to be correlated
)

# estimate the model object (BFGS is used by default)
est <- estimate(model, control = list(maxit = 1e+5))

# get the mean marginal effect of variable "RM" on the shortage probabilities
shortage_probability_marginal(model, est@coef, "RM")

# get the marginal effect at the mean of variable "RM" on the shortage probabilities
shortage_probability_marginal(model, est@coef, "CSHS", aggregate = "at_the_mean")

# get the marginal effect of variable "RM" on the system
shortage_marginal(model, est@coef, "RM")
```

---

### Description

Market side aggregation.

### Usage

```r
aggregate_demand(object, parameters)

aggregate_supply(object, parameters)
```

### Arguments

- `object`: A model object.
- `parameters`: A vector of model's parameters.
Details

Calculates the sample’s aggregate demand or supply at the passed set of parameters. If the model is static, as is for example the case of `equilibrium_model`, then all observations are aggregated. If the used data have a time dimension and aggregation per date is required, it can be manually performed using the `demanded_quantities` and `supplied_quantities` functions. If the model has a dynamic component, such as the `diseq_deterministic_adjustment`, then demanded and supplied quantities are automatically aggregated for each time point.

Value

The sum of the estimated demanded or supplied quantities evaluated at the given parameters.

Functions

- aggregate_demand: Demand aggregation.
- aggregate_supply: Supply aggregation.

See Also

demanded_quantities, supplied_quantities

Examples

```r
# initialize the basic model using the houses dataset
model <- new(
  "diseq_basic", # model type
c("ID", "TREND"), "HS", "RM", # keys, quantity, and price variables
  "RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
  "RM + TREND + W + L1RM + MA6DF + MA3DHF + MONTH", # supply specification
  fair_houses(), # data
correlated_shocks = FALSE # allow shocks to be correlated
)

# estimate the model object (BFGS is used by default)
est <- estimate(model)

# get estimated aggregate demand
aggregate_demand(model, est@coef)

# simulate the deterministic adjustment model
model <- simulate_model(
  "diseq_deterministic_adjustment", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.6, beta_d0 = 9.8, beta_d = c(0.3, -0.2), eta_d = c(0.6, -0.1),
    # supply coefficients
    alpha_s = 0.2, beta_s0 = 4.1, beta_s = c(0.9), eta_s = c(-0.5, 0.2),
    # price equation coefficients
    gamma = 0.9
  )
)```
market_descriptives

), seed = 1356
)

# estimate the model object
est <- estimate(model)

# get estimated aggregate demand
aggregate_demand(model, est@coef)

# get estimated aggregate demand
aggregate_supply(model, est@coef)

market_descriptives  Market side descriptive statistics

Description
Market side descriptive statistics

Usage

demand_descriptives(object)

supply_descriptives(object)

## S4 method for signature 'market_model'
demand_descriptives(object)

## S4 method for signature 'market_model'
supply_descriptives(object)

Arguments

object  A model object.

Details
Calculates and returns basic descriptive statistics for the model’s demand or supply side data. Factor variables are excluded from the calculations. The function calculates and returns:

• nobs Number of observations.
• nmval Number of missing values.
• min Minimum observation.
• max Maximum observation.
• range Observations’ range.
• sum Sum of observations.
• median Median observation.
• mean Mean observation.
• mean_se Mean squared error.
• mean_ce Confidence interval bound.
• var Variance.
• sd Standard deviation.
• coef_var Coefficient of variation.

Value

A data tibble containing descriptive statistics.

Functions

• demand_descriptives: Demand descriptive statistics.
• supply_descriptives: Supply descriptive statistics.

Examples

# initialize the basic model using the houses dataset
model <- new(
  "diseq_basic", # model type
c("ID", "TREND"), "HS", "RM", # keys, quantity, and price variables
  "RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
  "RM + TREND + W + L1RM + MA6DSF + MA3DHF + MONTH", # supply specification
  fair_houses(), # data
  correlated_shocks = FALSE # allow shocks to be correlated
)

# get descriptive statistics of demand side variables
demand_descriptives(model)

# get descriptive statistics of supply side variables
supply_descriptives(model)

market_models

Market model classes

Description

diseq_basic: The basic disequilibrium model consists of three equations. Two of them are the demand and supply equations. In addition, the model replaces the market clearing condition with the short side rule. The model is estimated using full information maximum likelihood.

\[
D_{nt} = X'_{d,nt}\beta_d + u_{d,nt},
\]

\[
S_{nt} = X'_{s,nt}\beta_s + u_{s,nt},
\]

\[
Q_{nt} = \min\{D_{nt}, S_{nt}\}.
\]
The disequilibrium model with deterministic price adjustment consists of four equations. The two market equations, the short side rule and price evolution equation. The first two equations are stochastic. The price equation is deterministic. The sample is separated based on the sign of the price changes as in the diseq_directional model. The model is estimated using full information maximum likelihood.

\[ D_{nt} = X'_{d,nt} \beta_d + P_{nt} \alpha_d + u_{d,nt}, \]
\[ S_{nt} = X'_{s,nt} \beta_s + P_{nt} \alpha_s + u_{s,nt}, \]
\[ Q_{nt} = \min\{D_{nt}, S_{nt}\}, \]
\[ \Delta P_{nt} = \frac{1}{\gamma} (D_{nt} - S_{nt}). \]

diseq_directional: The directional disequilibrium model consists of three equations and a separation rule. The market is described by a linear demand, a linear supply equation and the short side rule. The separation rule splits the sample into regimes of excess supply and excess demand. If a price change is positive at the time point of the observation, then the observation is classified as being in an excess demand regime. Otherwise, it is assumed that it represents an excess supply state. The model is estimated using full information maximum likelihood.

\[ D_{nt} = X'_{d,nt} \beta_d + u_{d,nt}, \]
\[ S_{nt} = X'_{s,nt} \beta_s + u_{s,nt}, \]
\[ Q_{nt} = \min\{D_{nt}, S_{nt}\}, \]
\[ \Delta P_{nt} \geq 0 \Rightarrow D_{nt} \geq S_{nt}. \]

diseq_stochastic_adjustment: The disequilibrium model with stochastic price adjustment is described by a system of four equations. Three of of them form a stochastic linear system of market equations coupled with a stochastic price evolution equation. The fourth equation is the short side rule. In contrast to the deterministic counterpart, the model does not impose any separation rule on the sample. It is estimated using full information maximum likelihood.

\[ D_{nt} = X'_{d,nt} \beta_d + P_{nt} \alpha_d + u_{d,nt}, \]
\[ S_{nt} = X'_{s,nt} \beta_s + P_{nt} \alpha_s + u_{s,nt}, \]
\[ Q_{nt} = \min\{D_{nt}, S_{nt}\}, \]
\[ \Delta P_{nt} = \frac{1}{\gamma} (D_{nt} - S_{nt}) + X'_{p,nt} \beta_p + u_{p,nt}. \]

equilibrium_model: The equilibrium model consists of thee equations. The demand, the supply and the market clearing equations. The model can be estimated using both full information maximum likelihood and two-stage least squares.

\[ D_{nt} = X'_{d,nt} \beta_d + P_{nt} \alpha_d + u_{d,nt}, \]
\[ S_{nt} = X'_{s,nt} \beta_s + P_{nt} \alpha_s + u_{s,nt}, \]
\[ Q_{nt} = D_{nt} = S_{nt}. \]

A necessary identification condition is that there is at least one control that is exclusively part of the demand and one control that is exclusively part of the supply equation. In the first stage of the two-stage least square estimation, prices are regressed on remaining controls from both the demand and supply equations. In the second stage, the demand and supply equation is estimated using the fitted prices instead of the observed.
Functions

- `market_model-class`: Base class for market models
- `disequilibrium_model-class`: Base class for disequilibrium models
- `diseq_basic-class`: Basic disequilibrium model with unknown sample separation.
- `diseq_deterministic_adjustment-class`: Disequilibrium model with deterministic price dynamics.
- `diseq_directional-class`: Directional disequilibrium model with sample separation.
- `diseq_stochastic_adjustment-class`: Disequilibrium model with stochastic price dynamics.
- `equilibrium_model-class`: Equilibrium model

Slots

- `logger` Logger object.
- `key_columns` Vector of column names that uniquely identify data records. For panel data this vector should contain an entity and a time point identifier.
- `time_column` Column name for the time point data.
- `explanatory_columns` Vector of explanatory column names for all model's equations.
- `data_columns` Vector of model's data column names. This is the union of the quantity, price and explanatory columns.
- `columns` Vector of primary key and data column names for all model's equations.
- `model_tibble` Model data tibble.
- `model_type_string` Model type string description.
- `system` Model's system of equations.

See Also

- `initialize_market_model`

---

**market_quantities**  
*Estimated market quantities.*

**Description**

Estimated market quantities.
Usage

demanded_quantities(object, parameters)

## S4 method for signature 'market_model'
demanded_quantities(object, parameters)

supplied_quantities(object, parameters)

## S4 method for signature 'market_model'
supplied_quantities(object, parameters)

Arguments

- object: A model object.
- parameters: A vector of model's parameters.

Details

Calculates and returns the estimated demanded or supplied quantities for each observation at the passed vector of parameters.

Value

A vector with the demanded quantities evaluated at the given parameter vector.

Functions

- demanded_quantities: Estimated demanded quantities.
- supplied_quantities: Estimated supplied quantities.

Examples

```r
# initialize the model using the houses dataset
model <- new(
  "diseq_basic", # model type
c("ID", "TREND"), "HS", "RM", # keys, quantity, and price variables
  "RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
  "RM + TREND + W + L1RM + MA6DSF + MA3DHF + MONTH", # supply specification
  fair_houses(), # data
  correlated_shocks = FALSE # allow shocks to be correlated
)

# estimate the model object (BFGS is used by default)
est <- estimate(model)

# get estimated demanded and supplied quantities
head(cbind(demanded_quantities(model, est@coef),
          supplied_quantities(model, est@coef)))
```
Market data and model simulation functionality based on the data generating process induced by the market model specifications.

**simulate_data:** Returns a data tibble with simulated data from a generating process that matches the passed model string. By default, the simulated observations of the controls are drawn from a normal distribution.

**simulate_model:** Simulates a data tibble based on the generating process of the passed model and uses it to initialize a model object. Data are simulated using the `simulate_data` function.

### Usage

```r
simulate_data(
  model_type_string,
  noobs = NA_integer_,
  tobs = NA_integer_,
  alpha_d = NA_real_,
  beta_d0 = NA_real_,
  beta_d = NA_real_,
  eta_d = NA_real_,
  alpha_s = NA_real_,
  beta_s0 = NA_real_,
  beta_s = NA_real_,
  eta_s = NA_real_,
  gamma = NA_real_,
  beta_p0 = NA_real_,
  beta_p = NA_real_,
  sigma_d = 1,
  sigma_s = 1,
  sigma_p = 1,
  rho_ds = 0,
  rho_dp = 0,
  rho_sp = 0,
  seed = NA_integer_,
  price_generator = function(n) stats::rnorm(n = n, mean = 2.5, sd = 0.5),
  control_generator = function(n) stats::rnorm(n = n, mean = 2.5, sd = 0.5),
  verbose = 0
)
```

## S4 method for signature 'ANY'

```r
simulate_data(
  model_type_string,
```

Arguments

- **model_type_string**
  - Model type. It should be among `equilibrium_model`, `diseq_basic`, `diseq_directional`, `diseq_deterministic_adjustment`, and `diseq_stochastic_adjustment`.

- **nobs**
  - Number of simulated entities.
tobs       Number of simulated dates.
alpha_d    Price coefficient of demand.
beta_d0    Constant coefficient of demand.
beta_d     Coefficients of exclusive demand controls.
eta_d      Demand coefficients of common controls.
alpha_s    Price coefficient of supply.
beta_s0    Constant coefficient of supply.
beta_s     Coefficients of exclusive supply controls.
eta_s      Supply coefficients of common controls.
gamma      Price equation’s stability factor.
beta_p0    Price equation’s constant coefficient.
beta_p     Price equation’s control coefficients.
sigma_d    Demand shock’s standard deviation.
sigma_s    Supply shock’s standard deviation.
sigma_p    Price equation shock’s standard deviation.
rho_ds     Demand and supply shocks’ correlation coefficient.
rho_dp     Demand and price shocks’ correlation coefficient.
rho_sp     Supply and price shocks’ correlation coefficient.
seed       Pseudo random number generator seed.

price_generator
Pseudo random number generator callback for prices. The default generator is $N(2.5, 0.25)$.

control_generator
Pseudo random number generator callback for non-price controls. The default generator is $N(2.5, 0.25)$.

verbose    Verbosity level.
simulation_parameters
List of parameters used in model simulation. See the simulate_data function for details.

... Additional parameters to be passed to the model’s constructor.

Value

simulate_data: The simulated data.
simulate_model: The simulated model.

Functions

• simulate_data: Simulate model data.
• simulate_model: Simulate model.
Maximize the log-likelihood.

**Description**

Maximizes the log-likelihood using the GSL implementation of the BFGS algorithm. This function is primarily intended for advanced usage. The `estimate` functionality is a fast, analysis-oriented alternative. If the GSL is not available, the function returns a trivial result list with status set equal to -1. If the C++17 execution policies are available, the implementation of the optimization is parallelized.

**Usage**

```
maximize_log_likelihood(
    object,  # A model object.
    start,   # Initializing vector.
    step,    # Optimization step.
    objective_tolerance,  # Objective optimization tolerance.
    gradient_tolerance  # Gradient optimization tolerance.
)
```

```
## S4 method for signature 'equilibrium_model'
maximize_log_likelihood(
    object,  # A model object.
    start,   # Initializing vector.
    step,    # Optimization step.
    objective_tolerance,  # Objective optimization tolerance.
    gradient_tolerance  # Gradient optimization tolerance.
)
```

**Arguments**

- **object**: A model object.
- **start**: Initializing vector.
- **step**: Optimization step.
- **objective_tolerance**: Objective optimization tolerance.
- **gradient_tolerance**: Gradient optimization tolerance.

**Value**

A list with the optimization output.
minus_log_likelihood

See Also

estimate

Examples

```r
model <- simulate_model(
  "equilibrium_model", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.9, beta_d0 = 14.9, beta_d = c(0.3, -0.2), eta_d = c(-0.03, -0.01),
    # supply coefficients
    alpha_s = 0.9, beta_s0 = 3.2, beta_s = c(0.03), eta_s = c(0.05, 0.02)
  ),
  seed = 99
)
# maximize the model's log-likelihood
mll <- maximize_log_likelihood(
  model,
  start = NULL, step = 1e-5,
  objective_tolerance = 1e-4, gradient_tolerance = 1e-3
)
mll
```

Description

Returns the opposite of the log-likelihood. The likelihood functions are based on Maddala and Nelson (1974) doi: 10.2307/1914215. The likelihood expressions that the function uses are derived in Karapanagiotis (2020) doi: 10.2139/ssrn.3525622. The function calculates the model's log likelihood by evaluating the log likelihood of each observation in the sample and summing the evaluation results.

Usage

```r
minus_log_likelihood(object, parameters)
```

## S4 method for signature 'diseq_basic'
minus_log_likelihood(object, parameters)

## S4 method for signature 'diseq_deterministic_adjustment'
minus_log_likelihood(object, parameters)
## S4 method for signature 'diseq_directional'
minus_log_likelihood(object, parameters)

## S4 method for signature 'diseq_stochastic_adjustment'
minus_log_likelihood(object, parameters)

## S4 method for signature 'equilibrium_model'
minus_log_likelihood(object, parameters)

**Arguments**

- **object**  
  A model object.

- **parameters**  
  A vector of parameters at which the function is to be evaluated.

**Value**

The opposite of the sum of the likelihoods evaluated for each observation.

---

### model_logger-class

**Logger class**

**Description**

Logger class

**Slots**

- **verbosity**  
  Controls the intensity of output messages. Errors are always printed. Other than this, a value of
  1 prints warnings,
  2 prints basic information,
  3 prints verbose information and,
  4 prints debug information.

**Description**

A unique identifying string for the model.

**Usage**

model_name(object)

## S4 method for signature 'market_model'
model_name(object)
Arguments

object A model object.

Value

A string representation of the model.

number_of_observations

Number of observations.

Description

Returns the number of observations that are used by an initialized model. The number of used observations may differ from the numbers of observations of the data set that was passed to the model’s initialization.

Usage

number_of_observations(object)

## S4 method for signature 'market_model'
number_of_observations(object)

Arguments

object A model object.

Value

The number of used observations.

plot,market_model,ANY-method

Plots the model.

Description

Displays a graphical illustration of the passed model object.

Usage

## S4 method for signature 'market_model,ANY'
plot(x)
scores

Arguments

x    A model object.

Examples

model <- simulate_model(
  "diseq_basic", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.9, beta_d0 = 8.9, beta_d = c(0.3, -0.2), eta_d = c(-0.03, -0.01),
    # supply coefficients
    alpha_s = 0.9, beta_s0 = 4.2, beta_s = c(0.03), eta_s = c(0.05, 0.02)
  ),
  seed = 44
)

# show model's illustration plot
plot(model)

scores

Likelihood scores.

Description

It calculates the gradient of the likelihood at the given parameter point for each observation in the sample. It, therefore, returns an n x k matrix, where n denotes the number of observations in the sample and k the number of estimated parameters. There order of the parameters is the same as the one that is used in the summary of the results.

Usage

scores(object, parameters)

## S4 method for signature 'diseq_basic'
scores(object, parameters)

## S4 method for signature 'diseq_deterministic_adjustment'
scores(object, parameters)

## S4 method for signature 'diseq_directional'
scores(object, parameters)

## S4 method for signature 'diseq_stochastic_adjustment'
scores(object, parameters)
## S4 method for signature 'equilibrium_model'
scores(object, parameters)

### Arguments

- **object**: A model object.
- **parameters**: A vector with model parameters.

### Value

The score matrix.

### Examples

```r
model <- simulate_model(
  "diseq_basic", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.9, beta_d0 = 8.9, beta_d = c(0.6), eta_d = c(-0.2),
    # supply coefficients
    alpha_s = 0.9, beta_s0 = 4.2, beta_s = c(0.03, 1.2), eta_s = c(0.1)
  ),
  seed = 7523
)

# estimate the model object (BFGS is used by default)
est <- estimate(model)

# Calculate the score matrix
head(scores(model, est@coef))
```

---

### shortage_analysis

**Analysis of shortages**

**Description**

Analysis of shortages

**Usage**

- `shortages(object, parameters)`
- `normalized_shortages(object, parameters)`
- `relative_shortages(object, parameters)`
shortage_probabilities(object, parameters)
shortage_indicators(object, parameters)
shortage_standard_deviation(object, parameters)

## S4 method for signature 'disequilibrium_model'
shortages(object, parameters)

## S4 method for signature 'disequilibrium_model'
normalized_shortages(object, parameters)

## S4 method for signature 'disequilibrium_model'
relative_shortages(object, parameters)

## S4 method for signature 'disequilibrium_model'
shortage_probabilities(object, parameters)

## S4 method for signature 'disequilibrium_model'
shortage_indicators(object, parameters)

## S4 method for signature 'disequilibrium_model'
shortage_standard_deviation(object, parameters)

## S4 method for signature 'diseq_stochastic_adjustment'
shortage_standard_deviation(object, parameters)

### Arguments

- **object**: A disequilibrium model object.
- **parameters**: A vector of parameters at which the shortages are evaluated.

### Details

The following methods offer functionality for analyzing estimated shortages in the disequilibrium models.

- **shortages**: Returns the predicted shortages at a given point.
- **normalized_shortages**: Returns the shortages normalized by the variance of the difference of the shocks at a given point.
- **relative_shortages**: Returns the shortages normalized by the supplied quantity at a given point.
- **shortage_probabilities**: Returns the shortage probabilities, i.e. the probabilities of an observation coming from an excess demand regime, at the given point.
- **shortage_indicators**: Returns a vector of indicators (Boolean values) for each observation. An element of the vector is TRUE for observations at which the estimated shortages are non-negative, i.e. the market at in an excess demand state. The remaining elements are FALSE. The evaluation of the shortages is performed using the passed parameter vector.
**shortage_standard_deviation:** Returns the variance of excess demand.

**Value**

A vector with the (modified) shortages.

**Functions**

- **shortages:** Shortages.
- **normalized_shortages:** Normalized shortages.
- **relative_shortages:** Relative shortages.
- **shortage_probabilities:** Shortage probabilities.
- **shortage_indicators:** Shortage indicators.
- **shortage_standard_deviation:** Shortage variance.

**Examples**

```r
# initialize the model using the houses dataset
model <- new(
  "diseq_deterministic_adjustment", # model type
c("ID", "TREND"), "TREND", "HS", "RM", # keys, time, quantity, and price variables
  "RM + TREND + W + CSHS + L1RM + L2RM + MONTH", # demand specification
  "RM + TREND + W + L1RM + MA6DSF + MA3DHF + MONTH", # supply specification
  fair_houses(), # data
correlated_shocks = FALSE # allow shocks to be correlated
)

# estimate the model object (BFGS is used by default)
est <- estimate(model, control = list(maxit = 1e+5))

# get estimated normalized shortages
head(normalized_shortages(model, est@coef))

# get estimated relative shortages
head(relative_shortages(model, est@coef))

# get the estimated shortage probabilities
head(shortage_probabilities(model, est@coef))

# get the estimated shortage indicators
head(shortage_indicators(model, est@coef))

# get the estimated shortages
head(shortages(model, est@coef))

# get the estimated shortage variance
shortage_standard_deviation(model, est@coef)
```
show

Prints a short description of the model.

Description

Sends basic information about the model to standard output.

Usage

show(object)

## S4 method for signature 'market_model'
show(object)

Arguments

object A model object.

Examples

```r
model <- simulate_model(
  "diseq_stochastic_adjustment", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.1, beta_d0 = 9.8, beta_d = c(0.3, -0.2), eta_d = c(0.6, -0.1),
    # supply coefficients
    alpha_s = 0.1, beta_s0 = 5.1, beta_s = c(0.9), eta_s = c(-0.5, 0.2),
    # price equation coefficients
    gamma = 1.2, beta_p0 = 3.1, beta_p = c(0.8)
  ),
  seed = 31
)

# print short model information
show(model)
```

summary,market_model-method

Summarizes the model.

Description

Prints basic information about the passed model object. In addition to the output of the `show` method, `summary` prints - the number of observations, - the number of observations in each equation for models with sample separation, and - various categories of variables.
Usage

```r
## S4 method for signature 'market_model'
summary(object)
```

Arguments

- `object`: A model object.

Examples

```r
model <- simulate_model(
  "diseq_stochastic_adjustment", list(
    # observed entities, observed time points
    nobs = 500, tobs = 3,
    # demand coefficients
    alpha_d = -0.1, beta_d0 = 9.8, beta_d = c(0.3, -0.2), eta_d = c(0.6, -0.1),
    # supply coefficients
    alpha_s = 0.1, beta_s0 = 5.1, beta_s = c(0.9), eta_s = c(-0.5, 0.2),
    # price equation coefficients
    gamma = 1.2, beta_p0 = 3.1, beta_p = c(0.8)
  ),
  seed = 556
)

# print model summary
summary(model)
```

system_classes

System classes

Description

System classes

Details

Classes with data and functionality describing systems of models.

Functions

- `system_base-class`: System base class
- `system_basic-class`: Basic model's system class
- `system_deterministic_adjustment-class`: Deterministic adjustment model's system class
- `system_directional-class`: Directional system class
- `system_equilibrium-class`: Equilibrium model's system class
- `system_stochastic_adjustment-class`: Stochastic adjustment model's system class
Slots

demand Demand equation.
supply Supply equation.
correlated_shocks Boolean indicating whether the shock of the equations of the system are correlated.
sample_separation Boolean indicating whether the sample of the system is separated.
quantity_variable The name of the quantity variable of the system.
price_variable The name of the price variable of the system.
quantity_vector A vector with the system’s observed quantities.
price_vector A vector with the system’s observed prices.
rho Correlation coefficient of demand and supply shocks.

\[ \rho_1 = \frac{1}{\sqrt{1 - \rho}} \]

\[ \rho_2 = \rho \rho_1 \]

lh Likelihood values for each observation.
gamma Excess demand coefficient.
delta

\[ \delta = \gamma + \alpha_d - \alpha_s \]

mu_P

\[ \mu_P = E_P \]

var_P

\[ V_P = \text{Var} P \]

sigma_P

\[ \sigma_P = \sqrt{V_P} \]

h_P

\[ h_P = \frac{P - \mu_P}{\sigma_P} \]

lagged_price_vector A vector with the system’s observed prices lagged by one date.
mu_Q

\[ \mu_Q = E Q \]

var_Q

\[ V_Q = \text{Var} Q \]
Let's analyze the provided mathematical expressions step by step:

1. **System Classes**
   - **Sigma_Q**
     \[ \sigma_Q = \sqrt{V_Q} \]
   - **H_Q**
     \[ h_Q = \frac{Q - \mu_Q}{\sigma_Q} \]
   - **Rho_QP**
     \[ \rho_{QP} = \frac{\text{Cov}(Q, P)}{\sqrt{\text{Var}Q \text{Var}P}} \]
   - **Rho_1QP**
     \[ \rho_{1,QP} = \frac{1}{\sqrt{1 - \rho_{QP}^2}} \]
   - **Rho_2QP**
     \[ \rho_{2,QP} = \rho_{QP} \rho_{1,QP} \]
   - **Z_QP**
     \[ z_{QP} = \frac{h_Q - \rho_{QP} h_P}{\sqrt{1 - \rho_{QP}^2}} \]
   - **Z_PQ**
     \[ z_{PQ} = \frac{h_P - \rho_{PQ} h_Q}{\sqrt{1 - \rho_{PQ}^2}} \]

2. **Price Equation**
   - **Zeta**
     \[ \zeta = \sqrt{1 - \rho_{DS}^2 - \rho_{DP}^2 - \rho_{SP}^2 + 2 \rho_{DP} \rho_{DS} \rho_{SP}} \]
   - **Zeta_DD**
     \[ \zeta_{DD} = 1 - \rho_{SP}^2 \]
   - **Zeta_DS**
     \[ \zeta_{DS} = \rho_{DS} - \rho_{DP} \rho_{SP} \]
   - **Zeta_DP**
     \[ \zeta_{DP} = \rho_{DP} - \rho_{DS} \rho_{SP} \]
   - **Zeta_SS**
     \[ \zeta_{SS} = 1 - \rho_{DP}^2 \]
\[ \zeta_{SP} = \rho_{SP} - \rho_{DS}\rho_{DP} \]

\[ \zeta_{PP} = 1 - \rho_{DS}^2 \]

\[ \mu_D = ED \]

\[ V_D = \text{Var}D \]

\[ \sigma_D = \sqrt{V_D} \]

\[ \mu_S = ES \]

\[ V_S = \text{Var}S \]

\[ \sigma_S = \sqrt{V_S} \]

\[ \sigma_{DP} = \text{Cov}(D, P) \]

\[ \sigma_{DS} = \text{Cov}(D, S) \]

\[ \sigma_{SP} = \text{Cov}(S, P) \]

\[ \rho_{DS} = \frac{\text{Cov}(D, S)}{\sqrt{\text{Var}D\text{Var}S}} \]

\[ \rho_{DP} = \frac{\text{Cov}(D, P)}{\sqrt{\text{Var}D\text{Var}P}} \]

\[ \rho_{SP} = \frac{\text{Cov}(S, P)}{\sqrt{\text{Var}S\text{Var}P}} \]
\[ h_D = \frac{D - \mu_D}{\sigma_D} \]

\[ h_S = \frac{S - \mu_S}{\sigma_S} \]

\[ z_{DP} = \frac{h_D - \rho_{DP} h_P}{\sqrt{1 - \rho_{DP}^2}} \]

\[ z_{PD} = \frac{h_P - \rho_{PD} h_D}{\sqrt{1 - \rho_{PD}^2}} \]

\[ z_{SP} = \frac{h_S - \rho_{SP} h_P}{\sqrt{1 - \rho_{SP}^2}} \]

\[ z_{PS} = \frac{h_P - \rho_{PS} h_S}{\sqrt{1 - \rho_{PS}^2}} \]

\[ \omega_D = \frac{h_D \zeta_{DD} - h_S \zeta_{DS} - h_P \zeta_{DP}}{\zeta_{DD}} \]

\[ \omega_S = \frac{h_S \zeta_{SS} - h_S \zeta_{SS} - h_P \zeta_{SP}}{\zeta_{SS}} \]

\[ w_D = -\frac{h_D^2}{2\zeta_{SS}} - 2h_D h_P \rho_{DP} + h_P^2 \]

\[ w_S = -\frac{h_S^2}{2\zeta_{DD}} - 2h_S h_P \rho_{SP} + h_P^2 \]

\[ \psi_D = \phi \left( \frac{\omega_D}{\zeta} \right) \]
\[ \psi_S = \phi \left( \frac{\omega_S}{\zeta} \right) \]

\[ \Psi_D = 1 - \Phi \left( \frac{\omega_D}{\zeta} \right) \]

\[ \Psi_S = 1 - \Phi \left( \frac{\omega_S}{\zeta} \right) \]

\[ g_D = \frac{\psi_D}{\Psi_D} \]

\[ g_S = \frac{\psi_S}{\Psi_S} \]

\text{rho_ds} \quad \text{Shadows rho in the \texttt{diseq_stochastic_adjustment} model}

\text{rho_dp} \quad \text{Correlation of demand and price equations’ shocks.}

\text{rho_sp} \quad \text{Correlation of supply and price equations’ shocks.}

\text{L_D} \quad \text{Likelihood conditional on excess supply.}

\text{L_S} \quad \text{Likelihood conditional on excess demand.}

---

<table>
<thead>
<tr>
<th>variable_names</th>
<th>Variable name access</th>
</tr>
</thead>
</table>

### Description

Methods that provide access to the prefixed variable names that the package uses.

- **prefixed_const_variable**: The constant coefficient name is constructed by concatenating the equation prefix with \texttt{CONST}.
- **prefixed_independent_variables**: The names of the independent variables are constructed by concatenating the equation prefix with the column names of the data \texttt{tibble}.
- **prefixed_price_variable**: The price variable name is constructed by concatenating the equation prefix with the name of the price column.
- **prefixed_control_variables**: The controls of the equation are the independent variables without the price variable. Their names are constructed by concatenating the equation prefix with the name of the price column.
prefixed_control_variables: The variance variable is constructed by concatenating the equation prefix with \texttt{VARIANCE}.

prefixed_quantity_variable: The quantity variable name is constructed by concatenating the equation prefix with the name of the quantity column.

lagged_price_variable: The lagged price variable name is constructed by concatenating \texttt{LAGGED} with the price variable name.

price_differences_variable: The price difference variable name is constructed by concatenating the price variable name with \texttt{DIFF}.

Usage

\begin{verbatim}
  prefixed_const_variable(object)
  prefixed_independent_variables(object)
  prefixed_price_variable(object)
  prefixed_control_variables(object)
  prefixed_variance_variable(object)
  prefixed_quantity_variable(object)

  ## S4 method for signature 'equation_base'
  prefixed_const_variable(object)

  ## S4 method for signature 'equation_base'
  prefixed_independent_variables(object)

  ## S4 method for signature 'equation_base'
  prefixed_price_variable(object)

  ## S4 method for signature 'equation_base'
  prefixed_control_variables(object)

  ## S4 method for signature 'equation_base'
  prefixed_variance_variable(object)

  ## S4 method for signature 'equation_base'
  prefixed_quantity_variable(object)

  lagged_price_variable(object)

  price_differences_variable(object)

  ## S4 method for signature 'system_base'
  lagged_price_variable(object)
\end{verbatim}
## S4 method for signature 'system_base'

`price_differences_variable(object)`

**Arguments**

- `object`: An equation object.

**Value**

The prefixed variable name(s).

**Functions**

- `prefixed_const_variable`: Constant coefficient variable name.
- `prefixed_independent_variables`: Independent variable names.
- `prefixed_price_variable`: Price coefficient variable name.
- `prefixed_control_variables`: Control variable names.
- `prefixed_variance_variable`: Variance variable name.
- `prefixed_quantity_variable`: Quantity variable name.
- `lagged_price_variable`: Lagged price variable name.
- `price_differences_variable`: Price differences variable name.
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