

Package ‘effsize’

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Type Package

Title Efficient Effect Size Computation

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Description A collection of functions to compute the standardized effect sizes for experiments (Cohen d, Hedges g, Cliff delta, Vargha-Delaney A). The computation algorithms have been optimized to allow efficient computation even with very large data sets.

URL <http://github.com/mtorchiano/effsize/>

BugReports <https://github.com/mtorchiano/effsize/issues>

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NeedsCompilation no

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Suggests testthat

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Description

This package contains functions to compute effect sizes both based on means difference (Cohen's d and Hedges g), dominance matrices (Cliff's Delta) and stochastic superiority (Vargha-Delaney A).

The computation (especially for Cliff's Delta) is carried on with highly efficient algorithms.

Details

The main functions are:

`cliff.delta`.

`cohen.d`.

`VD.A`.

Change history

- 0.3.1** Fixed a bug in `cohen.d` when `PAIRED=TRUE`, now the `PAIRED` parameter has no effect, it is left just for compatibility. In a future code clean-up it may be removed
- 0.4** Implemented a new algorithm with improved memory and time complexity. In particular new time complexity is $T = O(n1 * \log(n2))$ vs. the previous $T = O(n1 * n2)$, and new memory complexity $M = O(n1 + n2)$ vs. the previous $M = O(n1 * n2)$. In practice now the computation becomes feasible in a "reasonable" time.
- 0.4.1** Code clean-up and optimization using vectorized binary partitioning.
- 0.5** Added Vargha and Delaney A and fixed minor bugs with `cohen.d`.
- 0.5.1** Modified the Vargha and Delaney A computation to minimize accuracy errors.
- 0.5.2** Fixed bug in `cliff.delta`.
- 0.5.3** Fixed bug in `cohen.d` formula.
- 0.5.4** Fixed minor issue detected by check.
- 0.5.5** Changed the `effsize` field magnitude to a factor value.
- 0.6.0** Implemented paired computation and CI computation with non-central t-distributions for `cohen.d`.
- 0.6.1** Added ability to specify factor vector and data vector for 'cliff.delta' function (thanks to Jose W. Ho).
- 0.6.2** `na.rm` in `cohen.d` removes all incomplete pairs when paired.
- 0.6.3** fixed bug in `cohen.d` when `na.rm=TRUE`, minor changes in the documentation (thanks to P.Thomas)
- 0.6.4** Fixed a bug related to `pairedcohen.d` with NAs. Minor documentation changes
- 0.7.0** Refactored tests using `testthat` package. Fixed a bug in `cliff.delta` returning inconsistent results when the dominance matrix is returned. Fixed issue concerning CI. Fixed bug in `cohen.d` when using noncentral parameter for negative effect sizes.

- 0.7.1** Fixed minor bugs in cliff.delta and cohen.d
- 0.7.2** Fixed bugs in cohen.d, order of factors is now observed and CI are computed correctly
- 0.7.3** Fixed bugs in cohen.d, possible endless loop, cleaned code
- 0.7.4** Fixed bugs in cliff.delta when values are factors

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cliff.delta	<i>Cliff's Delta effect size for ordinal variables</i>
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Description

Computes the Cliff's Delta effect size for ordinal variables with the related confidence interval using efficient algorithms.

Usage

```
cliff.delta(d, ... )

## S3 method for class 'formula'
cliff.delta(formula, data=list() ,conf.level=.95,
            use.unbiased=TRUE, use.normal=FALSE,
            return.dm=FALSE, ...)

## Default S3 method:
cliff.delta(d, f, conf.level=.95,
            use.unbiased=TRUE, use.normal=FALSE,
            return.dm=FALSE, ...)
```

Arguments

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values (see Details)
conf.level	confidence level of the confidence interval
use.unbiased	a logical indicating whether to compute the delta's variance using the "unbiased" estimate formula or the "consistent" estimate
use.normal	logical indicating whether to use the normal or Student-t distribution for the confidence interval estimation
return.dm	logical indicating whether to return the dominance matrix. Warning: the explicit computation of the dominance uses a sub-optimal algorithm both in terms of memory and time

formula	a formula of the form $y \sim f$, where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding group
data	an optional matrix or data frame containing the variables in the formula formula. By default the variables are taken from <code>environment(formula)</code> .
...	further arguments to be passed to or from methods.

Details

Uses the original formula reported in (Cliff 1996).

If the dominance matrix is required i.e. `return.dm=TRUE`) the full matrix is computed thus using the naive algorithm. Otherwise, if `treatment` and `control` are factors then the optimized linear complexity algorithm is used, otherwise the RLE algorithm (with complexity $n \log n$) is used.

Value

A list of class `effsize` containing the following components:

<code>estimate</code>	the Cliff's delta estimate
<code>conf.int</code>	the confidence interval of the delta
<code>var</code>	the estimated variance of the delta
<code>conf.level</code>	the confidence level used to compute the confidence interval
<code>dm</code>	the dominance matrix used for computation, only if <code>return.dm</code> is <code>TRUE</code>
<code>magnitude</code>	a qualitative assessment of the magnitude of effect size
<code>method</code>	the method used for computing the effect size, always "Cliff's Delta"
<code>variance.estimation</code>	the method used to compute the delta variance estimation, either "unbiased" or "consistent"
<code>CI.distribution</code>	the distribution used to compute the confidence interval, either "Normal" or "Student-t"

The magnitude is assessed using the thresholds provided in (Romano 2006), i.e. `ldl<0.147` "negligible", `ldl<0.33` "small", `ldl<0.474` "medium", otherwise "large"

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References

- Norman Cliff (1996). Ordinal methods for behavioral data analysis. Routledge.
- J. Romano, J. D. Kromrey, J. Coraggio, J. Skowronek, Appropriate statistics for ordinal level data: Should we really be using t-test and cohen's d for evaluating group differences on the NSSE and other surveys?, in: Annual meeting of the Florida Association of Institutional Research, 2006.
- K.Y. Hogarty and J.D.Kromrey (1999). Using SAS to Calculate Tests of Cliff's Delta. Proceedings of the Twenty-Fourth Annual SAS User Group International Conference, Miami Beach, Florida, p 238. Available at: <http://www2.sas.com/proceedings/sugi24/Posters/p238-24.pdf>

See Also

[cohen.d](#), [print.effsize](#)

Examples

```
## Example data from Hogarty and Kromrey (1999)
treatment <- c(10,10,20,20,20,30,30,30,40,50)
control <- c(10,20,30,40,40,50)
res = cliff.delta(treatment,control,return.dm=TRUE)
print(res)
print(res$dm)
```

cohen.d

Cohen's d and Hedges' g effect size

Description

Computes the Cohen's d and Hedges' g effect size statistics.

Usage

```
cohen.d(d, ...)
```

```
## S3 method for class 'formula'
cohen.d(formula,data=list(),...)
```

```
## Default S3 method:
cohen.d(d,f,pooled=TRUE,paired=FALSE,
        na.rm=FALSE, hedges.correction=FALSE,
        conf.level=0.95,noncentral=FALSE, ...)
```

Arguments

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values
pooled	a logical indicating whether compute pooled standard deviation or the whole sample standard deviation. If pooled=FALSE (default) pooled sd is used, if pooled=TRUE the standard deviation of the the control group (the second argument or the one corresponding the the second level of the factor) is used instead.
paired	a logical indicating whether to consider the values as paired
na.rm	logical indicating whether NAs should be removed before computation; if paired==TRUE then all incomplete pairs are removed.

hedges.correction	logical indicating whether apply the Hedges correction
conf.level	confidence level of the confidence interval
formula	a formula of the form $y \sim f$, where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding groups
data	an optional matrix or data frame containing the variables in the formula <code>formula</code> . By default the variables are taken from <code>environment(formula)</code> .
noncentral	logical indicating whether to use non-central t distributions for computing the confidence interval.
...	further arguments to be passed to or from methods.

Details

When `f` in the default version is a factor or a character, it must have two values and it identifies the two groups to be compared. Otherwise (e.g. `f` is numeric), it is considered as a sample to be compare to `d`.

In the formula version, if `f` is expected to be a factor, if that is not the case it is coerced to a factor and a warning is issued.

The function computes the value of Cohen's d statistics (Cohen 1988). If required (`hedges.correction==TRUE`) the Hedges g statistics is computed instead (Hedges and Holkin, 1985).

When `paired` is set, the effect size is computed using the approach suggested in (Gibbons et al. 1993).

The computation of the CI requires the use of non-central Student-t distributions that are used when `noncentral==TRUE`; otherwise a central distribution is used.

Also a quantification of the effect size magnitude is performed using the thresholds define in Cohen (1992). The magnitude is assessed using the thresholds provided in (Cohen 1992), i.e. `ldl<0.2` "negligible", `ldl<0.5` "small", `ldl<0.8` "medium", otherwise "large"

The variance of the d is computed using the conversion formula reported at page 238 of Cooper et al. (2009):

$$S_d^2 = \left(\frac{n_1 + n_2}{n_1 n_2} + \frac{d^2}{2df} \right) \left(\frac{n_1 + n_2}{df} \right)$$

Value

A list of class `effsize` containing the following components:

<code>estimate</code>	the statistic estimate
<code>conf.int</code>	the confidence interval of the statistic
<code>var</code>	the estimated variance of the statistic
<code>conf.level</code>	the confidence level used to compute the confidence interval
<code>magnitude</code>	a qualitative assessment of the magnitude of effect size
<code>method</code>	the method used for computing the effect size, either "Cohen's d " or "Hedges' g "

Author(s)

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References

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). New York: Academic Press.

Hedges, L. V. & Olkin, I. (1985). Statistical methods for meta-analysis. Orlando, FL: Academic Press.

Cohen, J. (1992). A power primer. Psychological Bulletin, 112, 155-159.

The Handbook of Research Synthesis and Meta-Analysis (Cooper, Hedges, & Valentine, 2009)

David C. Howell (2010). Confidence Intervals on Effect Size. Available at: <https://www.uvm.edu/~7Edhowell/methods7/Supplements/Confidence%20Intervals%20on%20Effect%20Size.pdf>

Cumming, G.; Finch, S. (2001). A primer on the understanding, use, and calculation of confidence intervals that are based on central and noncentral distributions. Educational and Psychological Measurement, 61, 633-649.

Gibbons, R. D., Hedeker, D. R., & Davis, J. M. (1993). Estimation of effect size from a series of experiments involving paired comparisons. Journal of Educational Statistics, 18, 271-279.

See Also

[cliff.delta](#), [VD.A](#), [print.effsize](#)

Examples

```
treatment = rnorm(100,mean=10)
control = rnorm(100,mean=12)
d = (c(treatment,control))
f = rep(c("Treatment","Control"),each=100)
## compute Cohen's d
## treatment and control
cohen.d(treatment,control)
## data and factor
cohen.d(d,f)
## formula interface
cohen.d(d ~ f)
## compute Hedges' g
cohen.d(d,f,hedges.correction=TRUE)
```

print.essize	<i>Prints effect size</i>
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Description

Prints the results of an effect size computation

Usage

```
## S3 method for class 'essize'  
print(x, ...)
```

Arguments

x	the effect size result
...	further parameters are currently ignored

Details

Shows the estimate value and, when available, the confidence interval.

Note

This is still work in progress..

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References

See the main function [cliff.delta](#).

See Also

[cliff.delta cohen.d](#)

Description

Computes the Vargha and Delaney A effect size measure.

Usage

```
VD.A(d, ...)  
  
## S3 method for class 'formula'  
VD.A(formula,data=list(), ...)  
  
## Default S3 method:  
VD.A(d,f, ...)
```

Arguments

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values
formula	a formula of the form $y \sim f$, where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding group
data	an optional matrix or data frame containing the variables in the formula formula. By default the variables are taken from <code>environment(formula)</code> .
...	further arguments to be passed to or from methods.

Details

The function computes the Vargha and Delaney A effect size measure (Vargha and Delaney, 2000).

Value

A list of class `effsize` containing the following components:

estimate	the A statistics estimate
magnitude	a qualitative assessment of the magnitude of effect size
method	the method used, i.e. "Vargha and Delaney A"

Author(s)

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References

A. Vargha and H. D. Delaney. "A critique and improvement of the CL common language effect size statistics of McGraw and Wong." *Journal of Educational and Behavioral Statistics*, 25(2):101-132, 2000

See Also

[cliff.delta](#), [cohen.d](#), [print.effsize](#)

Examples

```
treatment = rnorm(100,mean=10)
control = rnorm(100,mean=12)
d = (c(treatment,control))
f = rep(c("Treatment","Control"),each=100)
## compute Vargha and Delaney A
## treatment and control
VD.A(treatment,control)
## data and factor
VD.A(d,f)
## formula interface
VD.A(d ~ f)
```

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