

# Package ‘effsize’

March 21, 2017

**Type** Package

**Title** Efficient Effect Size Computation

**Version** 0.7.1

**Date** 2017-03-20

**Description** A collection of functions to compute the standardized effect sizes for experiments (Cohen d, Hedges g, Cliff delta, Vargha-Delaney A). The computation algorithms have been optimized to allow efficient computation even with very large data sets.

**URL** <http://github.com/mtorchiano/effsize/>

**BugReports** <https://github.com/mtorchiano/effsize/issues>

**License** GPL-2

**NeedsCompilation** no

**Repository** CRAN

**Suggests** testthat

**Author** Marco Torchiano [aut, cre]

**Maintainer** Marco Torchiano <marco.torchiano@polito.it>

**Date/Publication** 2017-03-21 06:50:33 UTC

## R topics documented:

effsize-package . . . . .	2
cliff.delta . . . . .	3
cohen.d . . . . .	5
print.effsize . . . . .	7
VD.A . . . . .	8

<b>Index</b>	<b>10</b>
--------------	-----------

## Description

This packages contains functions to compute effect sizes both based on means difference (Cohen's  $d$  and Hedges  $g$ ), dominance matrices (Cliff's Delta) and stochastic superiority (Vargha-Delaney  $A$ ).

The computation (especially for Cliff's Delta) is carried on with highly efficient algorithms.

## Details

The main functions are:

`cliff.delta`.

`cohen.d`.

`VD.A`.

## Change history

- 0.3.1** Fixed a bug in `cohen.d` when `PAIRED=TRUE`, now the `PAIRED` parameter has no effect, it is left just for compatibility. In a future code clean-up it may be removed
- 0.4** Implemented a new algorithm with improved memory and time complexity. In particular new time complexity is  $T = O(n1 * \log(n2))$  vs. the previous  $T = O(n1 * n2)$ , and new memory complexity  $M = O(n1 + n2)$  vs. the previous  $M = O(n1 * n2)$ . In practice now the computation becomes feasible in a "reasonable" time.
  - 0.4.1** Code clean-up and optimization using vectorized binary partitioning.
- 0.5** Added Vargha and Delaney  $A$  and fixed minor bugs with `Cohen.d`.
  - 0.5.1** Modified the Vargha and Delaney  $A$  computation to minimize accuracy errors.
  - 0.5.2** Fixed bug in `cliff.delta`.
  - 0.5.3** Fixed bug in `cohen.d.formula`.
  - 0.5.4** Fixed minor issue detected by check.
  - 0.5.5** Changed the `effsize` field magnitude to a factor value.
- 0.6.0** Implemented paired computation and CI computation with non-central t-distributions for `cohen.d`.
- 0.6.1** Added ability to specify factor vector and data vector for 'cliff.delta' function (thanks to Joses W. Ho).
- 0.6.2** `na.rm` in `cohen.d` removes all incomplete pairs when paired.
- 0.6.3** fixed bug in `cohen.d` when `na.rm=TRUE`, minor changes in the documentation (thanks to P.Thomas)
- 0.6.4** Fixed a bug related to paired `cohen.d` with NAs. Minor documentation changes
- 0.7.0** Refactored tests using `testthat` package. Fixed a bug in `cliff.delta` returning inconsistent results when the dominance matrix is returned. Fixed issue concerning CI. Fixed bug in `cohen.d` when using `noncentral` parameter for negative effect sizes.
- 0.7.1** Fixed minor bugs in Cliff delta and Cohen.d

**Author(s)**

Marco Torchiano <http://softeng.polito.it/torchiano/>

---

cliff.delta

*Cliff's Delta effect size for ordinal variables*

---

**Description**

Computes the Cliff's Delta effect size for ordinal variables with the related confidence interval using efficient algorithms.

**Usage**

```
cliff.delta(d, ... )

## S3 method for class 'formula'
cliff.delta(formula, data=list() ,conf.level=.95,
            use.unbiased=TRUE, use.normal=FALSE,
            return.dm=FALSE, ...)

## Default S3 method:
cliff.delta(d, f, conf.level=.95,
            use.unbiased=TRUE, use.normal=FALSE,
            return.dm=FALSE, ...)
```

**Arguments**

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values (see Details)
conf.level	confidence level of the confidence interval
use.unbiased	a logical indicating whether to compute the delta's variance using the "unbiased" estimate formula or the "consistent" estimate
use.normal	logical indicating whether to use the normal or Student-t distribution for the confidence interval estimation
return.dm	logical indicating whether to return the dominance matrix. <b>Warning:</b> the explicit computation of the dominance uses a sub-optimal algorithm both in terms of memory and time
formula	a formula of the form $y \sim f$ , where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding group
data	an optional matrix or data frame containing the variables in the formula formula. By default the variables are taken from <code>environment(formula)</code> .
...	further arguments to be passed to or from methods.

**Details**

Uses the original formula reported in (Cliff 1996).

If the dominance matrix is required i.e. `return.dm=TRUE`) the full matrix is computed thus using the naive algorithm. Otherwise, if `treatment` and `control` are factors then the optimized linear complexity algorithm is used, otherwise the RLE algorithm (with complexity  $n \log n$ ) is used.

**Value**

A list of class `effsize` containing the following components:

<code>estimate</code>	the Cliff's delta estimate
<code>conf.int</code>	the confidence interval of the delta
<code>var</code>	the estimated variance of the delta
<code>conf.level</code>	the confidence level used to compute the confidence interval
<code>dm</code>	the dominance matrix used for computation, only if <code>return.dm</code> is TRUE
<code>magnitude</code>	a qualitative assessment of the magnitude of effect size
<code>method</code>	the method used for computing the effect size, always "Cliff's Delta"
<code>variance.estimation</code>	the method used to compute the delta variance estimation, either "unbiased" or "consistent"
<code>CI.distribution</code>	the distribution used to compute the confidence interval, either "Normal" or "Student-t"

The magnitude is assessed using the thresholds provided in (Romano 2006), i.e.  $|\text{dl}| < 0.147$  "negligible",  $|\text{dl}| < 0.33$  "small",  $|\text{dl}| < 0.474$  "medium", otherwise "large"

**Author(s)**

Marco Torchiano <http://softeng.polito.it/torchiano/>

**References**

Norman Cliff (1996). Ordinal methods for behavioral data analysis. Routledge.

J. Romano, J. D. Kromrey, J. Coraggio, J. Skowronek, Appropriate statistics for ordinal level data: Should we really be using t-test and cohen's d for evaluating group differences on the NSSE and other surveys?, in: Annual meeting of the Florida Association of Institutional Research, 2006.

K.Y. Hogarty and J.D.Kromrey (1999). Using SAS to Calculate Tests of Cliff's Delta. Proceedings of the Twenty-Fourth Annual SAS User Group International Conference, Miami Beach, Florida, p 238. Available at: <http://www2.sas.com/proceedings/sugi24/Posters/p238-24.pdf>

**See Also**

[cohen.d](#), [print.effsize](#)

**Examples**

```
## Example data from Hogarty and Kromrey (1999)
treatment <- c(10,10,20,20,20,30,30,30,40,50)
control <- c(10,20,30,40,40,50)
res = cliff.delta(treatment,control,return.dm=TRUE)
print(res)
print(res$dm)
```

cohen.d

*Cohen's d and Hedges g effect size***Description**

Computes the Cohen's d and Hedges' g effect size statistics.

**Usage**

```
cohen.d(d, ...)
```

```
## S3 method for class 'formula'
cohen.d(formula,data=list(),...)
```

```
## Default S3 method:
cohen.d(d,f,pooled=TRUE,paired=FALSE,
        na.rm=FALSE, hedges.correction=FALSE,
        conf.level=0.95,noncentral=FALSE, ...)
```

**Arguments**

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values
pooled	a logical indicating whether compute pooled standard deviation or the whole sample standard deviation
paired	a logical indicating whether to consider the values as paired
na.rm	logical indicating whether NAs should be removed before computation; if paired==TRUE then all incomplete pairs are removed.
hedges.correction	logical indicating whether apply the Hedges correction
conf.level	confidence level of the confidence interval
formula	a formula of the form $y \sim f$ , where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding groups

data	an optional matrix or data frame containing the variables in the formula formula. By default the variables are taken from environment(formula).
noncentral	logical indicating whether to use non-central t distributions for computing the confidence interval.
...	further arguments to be passed to or from methods.

### Details

When `f` in the default version is a factor or a character, it must have two values and it identifies the two groups to be compared. Otherwise (e.g. `f` is numeric), it is considered as a sample to be compare to `d`.

In the formula version, if `f` is expected to be a factor, if that is not the case it is coerced to a factor and a warning is issued.

The function computes the value of Cohen's  $d$  statistics (Cohen 1988). If required (`hedges.correction==TRUE`) the Hedges  $g$  statistics is computed instead (Hedges and Holkin, 1985).

When `paired` is set, the effect size is computed using the approach suggested in (Gibbons et al. 1993).

The computation of the CI requires the use of non-central Student-t distributions that are used when `noncentral==TRUE`; otherwise a central distribution is used.

Also a quantification of the effect size magnitude is performed using the thresholds define in Cohen (1992). The magnitude is assessed using the thresholds provided in (Cohen 1992), i.e. `ldl<0.2` "negligible", `ldl<0.5` "small", `ldl<0.8` "medium", otherwise "large"

The variance of the  $d$  is computed using the conversion formula reported at page 238 of Cooper et al. (2009):

$$S_d^2 = \left( \frac{n_1 + n_2}{n_1 n_2} + \frac{d^2}{2df} \right) \left( \frac{n_1 + n_2}{df} \right)$$

### Value

A list of class `effsize` containing the following components:

estimate	the statistics estimate
conf.int	the confidence interval of the statistic
var	the estimated variance of the statistic
conf.level	the confidence level used to compute the confidence interval
magnitude	a qualitative assessment of the magnitude of effect size
method	the method used for computing the effect size, either "Cohen's $d$ " or "Hedges' $g$ "

### Author(s)

Marco Torchiano <http://softeng.polito.it/torchiano/>

## References

- Cohen, J. (1988). *Statistical power analysis for the behavioral sciences* (2nd ed.). New York: Academic Press.
- Hedges, L. V. & Olkin, I. (1985). *Statistical methods for meta-analysis*. Orlando, FL: Academic Press.
- Cohen, J. (1992). A power primer. *Psychological Bulletin*, 112, 155-159.
- The Handbook of Research Synthesis and Meta-Analysis (Cooper, Hedges, & Valentine, 2009)
- David C. Howell (2010). Confidence Intervals on Effect Size. Available at: <https://www.uvm.edu/~Edhowell/methods7/Supplements/Confidence%20Intervals%20on%20Effect%20Size.pdf>
- Cumming, G.; Finch, S. (2001). A primer on the understanding, use, and calculation of confidence intervals that are based on central and noncentral distributions. *Educational and Psychological Measurement*, 61, 633-649.
- Gibbons, R. D., Hedeker, D. R., & Davis, J. M. (1993). Estimation of effect size from a series of experiments involving paired comparisons. *Journal of Educational Statistics*, 18, 271-279.

## See Also

[cliff.delta](#), [VD.A](#), [print.essize](#)

## Examples

```
treatment = rnorm(100,mean=10)
control = rnorm(100,mean=12)
d = (c(treatment,control))
f = rep(c("Treatment","Control"),each=100)
## compute Cohen's d
## treatment and control
cohen.d(treatment,control)
## data and factor
cohen.d(d,f)
## formula interface
cohen.d(d ~ f)
## compute Hedges' g
cohen.d(d,f,hedges.correction=TRUE)
```

---

print.essize

*Prints effect size*

---

## Description

Prints the results of an effect size computation

## Usage

```
## S3 method for class 'essize'
print(x, ...)
```

**Arguments**

x                    the effect size result  
...                   further parameters are currently ignored

**Details**

Shows the estimate value and, when available, the confidence interval.

**Note**

This is still work in progress..

**Author(s)**

Marco Torchiano <http://softeng.polito.it/torchiano/>

**References**

See the main function [cliff.delta](#).

**See Also**

[cliff.delta](#) [cohen.d](#)

---

VD.A

*Vargha and Delaney A measure*

---

**Description**

Computes the Vargha and Delaney A effect size measure.

**Usage**

```
VD.A(d, ...)  
  
## S3 method for class 'formula'  
VD.A(formula,data=list(), ...)  
  
## Default S3 method:  
VD.A(d,f, ...)
```



**Arguments**

d	a numeric vector giving either the data values (if f is a factor) or the treatment group values (if f is a numeric vector)
f	either a factor with two levels or a numeric vector of values
formula	a formula of the form $y \sim f$ , where y is a numeric variable giving the data values and f a factor with two levels giving the corresponding group
data	an optional matrix or data frame containing the variables in the formula formula. By default the variables are taken from environment(formula).
...	further arguments to be passed to or from methods.

**Details**

The function computes the Vargha and Delaney A effect size measure (Vargha and Delaney, 2000).

**Value**

A list of class `effsize` containing the following components:

estimate	the A statistics estimate
magnitude	a qualitative assessment of the magnitude of effect size
method	the method used, i.e. "Vargha and Delaney A"

**Author(s)**

Marco Torchiano <http://softeng.polito.it/torchiano/>

**References**

A. Vargha and H. D. Delaney. "A critique and improvement of the CL common language effect size statistics of McGraw and Wong." *Journal of Educational and Behavioral Statistics*, 25(2):101-132, 2000

**See Also**

[cliff.delta](#), [cohen.d](#), [print.effsize](#)

**Examples**

```
treatment = rnorm(100,mean=10)
control = rnorm(100,mean=12)
d = (c(treatment,control))
f = rep(c("Treatment","Control"),each=100)
## compute Vargha and Delaney A
## treatment and control
VD.A(treatment,control)
## data and factor
VD.A(d,f)
## formula interface
VD.A(d ~ f)
```

# Index

- \*Topic **Cliff**
    - cliff.delta, 3
    - effsize-package, 2
  - \*Topic **Cohen**
    - cohen.d, 5
    - effsize-package, 2
  - \*Topic **Hedges**
    - cohen.d, 5
    - effsize-package, 2
  - \*Topic **Vargha and Delaney**
    - VD.A, 8
  - \*Topic **effect size**
    - cliff.delta, 3
    - cohen.d, 5
    - effsize-package, 2
    - VD.A, 8
  - \*Topic **package**
    - effsize-package, 2
- cliff.delta, 2, 3, 7–9
- cohen.d, 2, 4, 5, 8, 9
- effsize (effsize-package), 2
- effsize-package, 2
- print.effsize, 4, 7, 7, 9
- VD.A, 2, 7, 8