Package ‘equaltestMI’

August 4, 2017

Type  Package
Title  Examine Measurement Invariance via Equivalence Testing and Projection Method
Version 0.1.0
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Description Functions for examining measurement invariance via equivalence testing along with adjusted RMSEA (root mean square error of approximation; Steiger & Lind, 1980) cutoff values. In particular, a projection-based method is implemented to test the equality of latent factor means across groups without assuming the equality of intercepts.
License GPL-3
Encoding UTF-8
LazyData true
Depends R (>= 3.1.0), lavaan, stats, utils
Suggests knitr, rmarkdown, MASS, semTools
BugReports https://github.com/gabriellajg/equaltestMI/issues
VignetteBuilder knitr
RoxygenNote 6.0.1
NeedsCompilation no
Repository CRAN
Date/Publication 2017-08-04 08:49:29 UTC

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eqMI.bootstrap

Description

Bootstrap procedure for projection-based latent means equality test

Usage

eqMI.bootstrap(..., B = 100, seed = 111)

Arguments

...  The same arguments as for any lavaan model. See lavaan::sem for more information.
B    The number of bootstrap samples. Default at 100.
seed The initial seed to generate bootstrap samples. Default at 111.
bootstrap If bootstrap resampling is used to obtain empirical p-value of the statistics.

Details

Perform bootstrap procedure when testing the equality of latent means using projection method. Note that raw data must be available for bootstrap resampling to be performed. With the projection method, the cross-group intercepts are not required to be the same for further tests. If bootstrap resampling is used, the test statistics are not referred to chi-squared distributions but to bootstrapped empirical distributions for significance testing. Percentage bootstrap critical values are calculated. This process might be time-consuming if the model is complex or the number of bootstrap samples (B) is large.

Value

bootstrap p-values of the tests of common and unique factors.

References

eqMI.covtest

Examples

data(HolzingerSwineford)
semmodeleqMI.covtest
L1 = V1 + V2 + V3
L2 = V4 + V5 + V6
L3 = V7 + V8
L4 = V9 + V10 + V11

## Not run:
run.bts <- eqMI.bootstrap(model = semmodel, data = HolzingerSwineford, 
group = "school", meanstructure = TRUE, B = 100, seed = 111)

## End(Not run)

eqMI.covtest Test the equality of two covariance matrices in population

Description

The first step of testing measurement invariance (MI) in multiple-group SEM analysis. The null hypothesis is tested using the method of Lagrange multipliers

Usage

eqMI.covtest(..., lamb0 = NULL)

Arguments

... The same arguments as for any lavaan model. See lavaan::sem for more information.
lamb0 initial coefficients of Lagrangian multiplier. If not pre-specified, 0.01 will be used.

Details

The eqMI.covtest function is the first step to test MI. Under null hypothesis testing (NHT), a non-significant statistic is generally an overall endorsement of MI. If the null hypothesis is rejected then one may proceed to test other aspects of MI.

Value

The likelihood ratio statistic, degrees of freedom, and p-value of the test.

References


eqMI.main

The main function to test measurement invariance

Description
Test measurement invariance with equivalence testing, projection methods, and adjusted RMSEA cutoffs for two groups.

Usage
eqMI.main(..., output = "both", equivalence.test = TRUE, adjRMSEA = TRUE,
    projection = FALSE, bootstrap = FALSE, quiet = FALSE, B = 100,
    seed = 111)

Arguments
...  The same arguments as for any lavaan model. See lavaan::sem for more information.

Users must explicitly specify the name of the input elements for this function to catch. For example, specify 'data = HolzingerSwineford' instead just 'HolzingerSwineford'.

output  If the function prints out results of covariance structure, mean structure, or both. The value of output must be mean, covariance, or both. When the tests involve mean structure (output = 'mean' or 'both'), both the strong and the strict tests of measurement invariance will be conducted.

equivalence.test  If equivalence.test=TRUE, equivalence testing is used for examining all statistics. RMSEA together with conventional or adjusted cutoff values will be used to gauge the goodness of fit.

adjRMSEA  If adjRMSEA=TRUE, adjusted RMSEA cutoff values are used for equivalence testing. See details in Yuan & Chan (2016).

projection  If projection=TRUE, projection method is used to test the equality of latent factor means. The advantage of the projection method over conventional multiple-group SEM approach is that the test of latent factor means can be conducted even when the equality of intercepts do not hold.

Examples
data(HolzingerSwineford)
semmodel<-'
L1 <- V1 + V2 + V3
L2 <- V4 + V5 + V6
L3 <- V7 + V8
L4 <- V9 + V10 + V11
'
cov.test <- eqMI.covtest(model = semmodel,
                          data = HolzingerSwineford,
                          group="school")
bootstrap
If bootstrap=TRUE, bootstrap is used to obtain empirical p-values for testing the equality of cross-group latent factor means.

quiet
If quiet=FALSE (default), a summary is printed out containing an overview of the different models that are fitted, together with some model comparison tests and fit measures. The results of equivalence testing will also be printed if equivalence testing is used. If quiet=TRUE, no summary is printed but results will be stored in the object.

B
The number of bootstrap samples used in bootstrap approach.

seed
The initial seed to generate bootstrap samples. Default at 111.

Details
An all-in-one function with several added options to conduct a sequence of tests needed to evaluate MI. The chi-square statistics, except the one for testing the equality of covariance structure, are obtained based on lavaan::sem function. The test statistic of the covariance structure equality is obtained via the method of Lagrangian multiplier. Equivalence testing is enabled by setting equivalence.test=TRUE and this function will calculate T-size, RMSEA, and adjusted RMSEA cutoff values, and provide the goodness-of-fit.

Value
A list is returned with:

convention.sem Result of conventional multiple-group SEM using Lavaan. Returned object of eqMI.semtest.
projection.res Results of projection methods on tests of latent means. Returned object of eqMI.projection and eqMI.bootstrap.
eqMI.stat Test statistics, degrees of freedom, p-values, ncp, T-sizes, RMSEAs, their cutoff values, and the goodness-of-fit under equivalence testing. A formatted version of eqMI.stat is printed if quiet=FALSE.

References


Examples
```R
# Not run:
data(HolzingerSwineford)
semmodel<-
L1 =~ V1 + V2 + V3
L2 =~ V4 + V5 + V6
L3 =~ V7 + V8
L4 =~ V9 + V10 + V11
```


eqMI.ncp

Obtain noncentrality parameter of a chisquare distribution

Description

Calculate the noncentrality parameter as well as the model misspecification \( \epsilon_t \) given its lower-tail critical value.

Usage

eqMI.ncp(T, df, N, m, alpha = 0.05)

Arguments

- **T**: A chi-square statistic
- **df**: Degrees of freedom
- **N**: Total sample size of all groups
- **m**: Number of groups
- **alpha**: Significance level. Default at 0.05.
Details

This function is to compute the noncentrality parameter ncp, the model misspecification epsilon_t, and its corresponding RMSEA_t. With equivalence testing, the model misspecification is also the minimum tolerable size that a researcher needs to tolerate if one wishes to proceed with further restricted tests. The formula from Venables (1975) is used for obtaining the noncentrality parameter of a non-central chi-square distribution given its lower-tail critical value.

Value

The noncentrality parameter ncp, the minimum tolerable size epsilon_t, and RMSEA_t under equivalence testing.

References


Examples

alpha <- .05
n_1 <- 200
n_2 <- 200
N <- n_1 + n_2
m <- 2
# A made-up likelihood-ratio statistic
T_ml <- 8.824
df <- 6
eqMI.ncp(T = T_ml, df = df, N = N, m = m, alpha = alpha)

description

Perform projection method for testing the equality of latent means without requiring the equality of cross-group intercepts to hold.

Usage

eqMI.projection(...)

projection

Projection-based method for testing latent means equality
Arguments

The same arguments as for any lavaan model. See lavaan::sem for more information. All models fitted by Lavaan are estimated by fixing the variances of latent factors to 1.

Users must explicitly specify the name of the input elements for this function to catch. For example, specify `data = HolzingerSwineford` instead just `HolzingerSwineford`.

Details

Perform projection method for testing the equality of two latent means without requiring the cross-group intercepts to be the same. A validity index is provided as the proportion of the differences in manifest variables intercepts explained by latent mean differences as a gauge of the quality of measurements.

Value

A list is returned with:

- `fit.metric`: test of metric invariance (factor loadings). This is a prerequisite for testing equality of latent means.
- `mvdif.test`: t tests of the cross-group sample means for each variable.
- `chi.stat`: Three chi-square tests for intercepts, common factors, and unique factors. `chi.stat` will be needed for equivalence testing.
- `common.test`: t tests of common factors for each variable.
- `specific.test`: t tests of unique factors for each variable.
- `latent.test`: t tests of latent means
- `V.index`: validity index
- `Pmat`: projection matrix of intercepts into the space of common factors
- `Qmat`: projection matrix of intercepts into the space of unique factors

References


Examples

```r
data(HolzingerSwineford)
semmodel<-'
L1 <- V1 + V2 + V3
L2 <- V4 + V5 + V6
L3 <- V7 + V8
L4 <- V9 + V10 + V11
'
run.pj <- eqMI.projection(model = semmodel, data = HolzingerSwineford,
group = "school", meanstructure = TRUE)
```
**Description**

Generate adjusted cutoff values of RMSEA for equivalence testing corresponding to conventional cutoff values .01, .05, .08, and .10.

**Usage**

```r
eqmi.RMSEA(N, m, df)
```

**Arguments**

- **N**: Total sample size of all groups
- **m**: Number of groups
- **df**: Degree of freedom

**Details**

The adjusted cutoff values of RMSEA for equivalence testing can be obtained with `N`, `m`, `df` and transformed variables. Formulas are estimated using simulation studies and the coefficients are given in Table 11 of the reference.

**Value**

The adjusted cutoff values corresponding to conventional cutoff values .01, .05, .08, and .10.

**References**


**Examples**

```r
alpha <- .05;
N <- 200;
m <- 1;
T_ml <- 28.446; # the statistic T_ml for group 1;
df <- 24;
eqmi.RMSEA(N = N, m = m, df = df);
```
eqMI.semtest Measurement invariance tests using Lavaan

Description

Conventional multiple-group SEM to test measurement invariance. A sequence of chi-square and
chi-square difference tests will be conducted.

Usage

eqMI.semtest(..., output = "both", quiet = FALSE)

Arguments

... The same arguments as for any lavaan model. See lavaan::cfa for more information.

Users must explicitly specify the name of the input elements for this function to catch. For example, specify 'data = HolzingerSwineford' instead just 'HolzingerSwineford'.

output If the function prints out results of covariance structure, mean structure, or both.
The value of output must be mean, covariance, or both. When the tests involve mean structure (output = 'mean' or 'both'), both the strong and the strict tests of measurement invariance will be conducted.

quiet If FALSE (default), a summary is printed out containing an overview of the different models that are fitted, together with some model comparison tests. If TRUE, no summary is printed but results will be stored in the object.

Details

This is a wrapper function of the function measurementInvariance in package semTools with the following default options: std.lv = FALSE, fit.measures = "default", and method = "satorra.bentler.2001". See semTools::measurementInvariance for more information.

Value

A list is returned with:

LavaanOut A sublist in convention.sem. Contains Lavaan style output and results for each chi-square and chi-square difference.

Mean.part A sublist in convention.sem. Contains test statistics and fit measures on invariance tests of mean structure.

Cov.part A sublist in convention.sem. Contains test statistics and fit measures on invariance tests of covariance structure.
References


See Also

sem, measurementInvariance

Examples

data(HolzingerSwineford)
semmodel<-
L1 <- V1 + V2 + V3
L2 <- V4 + V5 + V6
L3 <- V7 + V8
L4 <- V9 + V10 + V11

## Not run:
run.sem <- eqM.semtest(model = semmodel, data = HolzingerSwineford,
    group = "school", meanstructure = TRUE)

## End(Not run)

HolzingerSwineford

Holzinger and Swineford (1939) cognitive tests data in 301 children from two schools

Description

This classic data set contains reported data on cognitive tests from two elementary schools.

Usage

data(HolzingerSwineford)

Format

A data frame with 301 observations on 11 numeric variables and a group indicator (12 variables in total).
Details

11 variables used in Deng and Yuan (2016) are included in this version of data, they are: visual perception, cubes, paper form board, paragraph comprehension, word classification, word meaning, counting dots, straight-curved capitals, deduction, problem reasoning, and series completion.

This data set with more variables are available in other R packages such as lavaan, MBESS, and OpenMX.

References


See Also
HolzingerSwineford1939, HS.data, HS.ability.data

Examples

data(HolzingerSwineford)

printInvarianceResult

Internal function to format the results of measurement invariance tests

Description

Internal function to format the results of measurement invariance tests

Usage

printInvarianceResult(FIT, fit.measures, method, quiet = FALSE)

Arguments

FIT parameter needed by printInvarianceResult().
fit.measures parameter needed by printInvarianceResult().
method parameter needed by printInvarianceResult(). Default at "satorra.bentler.2001".
quiet If quiet=FALSE (default), a summary is printed out containing an overview of the different models that are fitted, together with some model comparison tests and fit measures. The results of equivalence testing will also be printed if equivalence testing is used. If quiet=TRUE, no summary is printed but results will be stored in the object.
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