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all_max_rcpp

Sliding and disjoint block maxima

Description
Calculates the (sliding) maxima of all blocks of \( b \) contiguous values and all sets of the maxima of disjoint blocks of \( b \) contiguous values in the vector \( x \). This provides the first step of computations in \textit{spm}.

Usage
\begin{verbatim}
all_max_rcpp(x, b = 1, which_dj = c("all", "first", "last"), ...)
\end{verbatim}

Arguments
\begin{itemize}
\item \textbf{x} A numeric vector of raw observations.
\item \textbf{b} A numeric scalar. The block size.
\item \textbf{which_dj} A character scalar. Determines Which sets of disjoint maxima are calculated: "all", all sets; "first", only the set whose first block starts on the first observation in \( x \); "last", only the set whose last block end on the last observation in \( x \).
\item ... Further arguments to be passed to \textit{roll_max}.
\end{itemize}

Details
\textbf{Sliding maxima}. The function \textit{roll_max} in the \texttt{RcppRoll} package is used.

\textbf{Disjoint maxima}. If \( n = \text{length}(x) \) is an integer multiple of \( b \), or if \texttt{which_dj = "first"} or \texttt{which_dj = "last"} then only one set of \( n / b \) disjoint block maxima are returned. Otherwise, \( n - \text{floor}(n / b) \times b + 1 \) sets of \( \text{floor}(n / b) \) disjoint block maxima are returned. Set \( i \) are the disjoint maxima of \( x[i:(i + \text{floor}(n / b) - b - 1)] \). That is, all possible sets of contiguous disjoint maxima achieving the maxima length of \( \text{floor}(n / b) \) are calculated.

In both instances \texttt{na.rm = TRUE} is passed to \textit{max} so that blocks containing missing values produce a non-missing result.

Also returned are the values in \( x \) that contribute to each set of block maxima.

Value
A list containing
\begin{itemize}
\item \textbf{ys} a numeric vector containing one set of sliding block maxima.
\item \textbf{xv} a numeric vector containing the values that contribute to \textbf{ys}, that is, the whole input vector \( x \).
\item \textbf{yd} if \texttt{which_dj = "all"} a \texttt{floor}(n / b) by \( n - \text{floor}(n / b) \times b + 1 \) numeric matrix. Each column contains a set of disjoint maxima. Otherwise, a \texttt{floor}(n / b) by 1 numeric matrix containing one set of block maxima.
\end{itemize}
choose_b

if which_dj = "all" a floor(n / b) \* b by n - floor(n / b) \* b + 1 numeric matrix. Each column contains the values in x that contribute to the corresponding column in yd. Otherwise, a floor(n / b) by 1 numeric matrix containing one the one set of the values in x that contribute to yd.

See Also

spm for semiparametric estimation of the extremal index based on block maxima.

Examples

```r
x <- 1:11
all_max_rcpp(x, 3)
all_max_rcpp(x, 3, which_dj = "first")
all_max_rcpp(x, 3, which_dj = "last")
```

Description

Creates data for a plot to aid the choice of the block length b to supply to spm. The general idea is to select the smallest value of b above which estimates of the extremal index θ appear to be constant with respect to b, taking into account sampling variability. plot.choose_b creates the plot.

Usage

```r
choose_b(data, b, bias_adjust = c("BB3", "BB1", "N", "none"),
    constrain = TRUE, varN = TRUE, level = 0.95,
    interval_type = c("norm", "lik"), conf_scale = c("theta", "log"),
    type = c("vertical", "cholesky", "spectral", "none"))
```

Arguments

data A numeric vector of raw data. No missing values are allowed.
b A numeric scalar. The block size.
bias_adjust A character scalar. Is bias-adjustment of the raw estimate of θ performed using the bias-reduced estimator (bias_adjust = "BB3"), derived in Section 5 of Berghaus and Bucher (2018); or a simpler version (bias_adjust = "BB1"), in which the raw estimate is multiplied by (k - 1)/k, where k is the number of blocks; or the bias-adjustment of the empirical distribution function used to calculate the estimate, as detailed in Section 2 of Northrop (2015). When disjoint maxima are used bias_adjust = "BB1" and bias_adjust = "N" give identical estimates of the Berghaus and Bucher (2018) variant, as explained at the end of Section 5 of Berghaus and Bucher (2018). If bias_adjust = "none" then no bias-adjustment is performed.
choose_b

constrain A logical scalar. If `constrain = TRUE` then any estimates that are greater than 1 are set to 1, that is, they are constrained to lie in (0, 1]. This is carried out after any bias-adjustment. Otherwise, estimates that are greater than 1 may be obtained.

varN A logical scalar. If `varN = TRUE` then the estimation of the sampling variance of the Northrop (2015) estimator is tailored to that estimator. Otherwise, the sampling variance derived in Berghaus and Bucher (2018) is used. See Details for further information.

level A numeric scalar in (0, 1). The confidence level required.

interval_type A character scalar: "norm" for intervals of type (a), "lik" for intervals of type (b).

conf_scale A character scalar. If `interval_type = "norm"` then `conf_scale` determines the scale on which we use approximate large-sample normality of the estimators to estimate confidence intervals of type (a).

Any bias-adjustment requested in the original call to `spm`, using it's `bias_adjust` argument, is automatically applied here.

type A character scalar. The argument type to be passed to `conf_intervals` in the `chandwich` package in order to estimate the likelihood-based intervals. Using type = "none" is not advised because then the intervals are based on naive estimated standard errors. In particular, if (the default) sliding = TRUE was used in the call to `spm` then the unadjusted likelihood-based confidence intervals provide vast underestimates of uncertainty.

Details

For each block size in b the extremal index \( \theta \) is estimated using `spm`. The estimates of \( \theta \) approximate conf% confidence intervals for \( \theta \) are stored for plotting (by `plot.choose_b`) to produce a simple graphical diagnostic to inform the choice of block size. This plot is used to choose a block size above which the underlying value of \( \theta \) may be approximately constant. This is akin to a threshold stability plot: see Chapter 4 of Coles (2001), for example.

The nature of the calculation of the sampling variances of the estimates of \( \theta \) (see `spm` for details) means that `choose_b` may be a little slow to run if b contains many values, particularly if some of them are small.

For very small block sizes it may not be possible to estimate the confidence intervals. See Details in `spm`. For any such block sizes the intervals will be missing from the plot.

Value

An object of class c("choose_b", "exdex") containing

```
theta_sl, theta_dj
```

table numeric b by 3 matrices of estimates of \( \theta \) using sliding and disjoint blocks. Columns 1-3 relate to the estimators N2015, BB2018 and BB2018b.
choose_uk

lower_sl, lower_dj
   Similarly for the lower limits of the confidence intervals.
upper_sl, upper_dj
   Similarly for the upper limits of the confidence intervals.
b
   the input b
call
   the call to choose_b.

References


See Also

plot.choose_b to produce the block length diagnostic plot.

Examples

# Newlyn seas surges
# Plot like the top left of Northrop (2015)
# Remove the last 14 values because 2880 has lots of factors
b_vals <- c(2,3,4,5,6,8,9,10,12,15,16,18,20,24,30,32,36,40,45,48,54,60)
res <- choose_b(newlyn[1:2880], b_vals)
# Some b are too small for the sampling variance of the sliding blocks
# estimator to be estimated
plot(res)
plot(res, estimator = "BB2018")
plot(res, maxima = "disjoint")

# S&P 500 index: similar to Berghaus and Bucher (2018), Fig 4 top left
b_vals <- c(10, seq(from = 25, to = 350, by = 25), 357)
res500 <- choose_b(sp500, b_vals)
plot(res500, ylim = c(0, 1))
plot(res500, estimator = "BB2018", ylim = c(0, 1))

choose_uk

Threshold u and runs parameter K diagnostic for the K-gaps estimator

Description

Creates data for a plot to aid the choice of the threshold and run parameter K for the K-gaps estimator (see kgaps). plot.choose_uk creates the plot.
choose_uk

Usage

choose_uk(data, u, k = 1)

Arguments

data A numeric vector of raw data. No missing values are allowed.

u, k Numeric vectors. u is a vector of extreme value thresholds applied to data. k is a vector of values of the run parameter $K$, as defined in Suveges and Davison (2010). See kgaps for more details.

Details

For each combination of threshold in u and $K$ in k the functions kgaps and kgaps_imt are called in order to estimate $\theta$ and to perform the information matrix test of Suveges and Davison (2010).

Value

An object (a list) of class c("choose_uk","exdex") containing

imt an object of class c("kgaps_imt","exdex") returned from kgaps_imt.

theta a length(u) by length(k) matrix. Element (i,j) of theta contains an object (a list) of class c("kgaps","exdex"), a result of a call kgaps(data,u[j],k[i]) to kgaps.

References


See Also

kgaps for maximum likelihood estimation of the extremal index $\theta$ using the $K$-gaps model.

kgaps_imt for the information matrix test under the $K$-gaps model

plot.choose_uk to produce the diagnostic plot.

Examples

### S&P 500 index

# Multiple thresholds and run parameters
u <- quantile(sp500, probs = seq(0.1, 0.9, by = 0.1))
imt_theta <- choose_uk(sp500, u = u, k = 1:5)
plot(imt_theta)
plot(imt_theta, uprob = TRUE)
plot(imt_theta, y = "theta")

# One run parameter K, many thresholds u
u <- quantile(sp500, probs = seq(0.1, 0.9, by = 0.1))
imt_theta <- choose_uk(sp500, u = u, k = 1)
plot(imt_theta)
plot(imt_theta, y = "theta")

# One threshold u, many run parameters K
u <- quantile(sp500, probs = 0.9)
imt_theta <- choose_uk(sp500, u = u, k = 1:5)
plot(imt_theta)
plot(imt_theta, y = "theta")

### Newlyn sea surges

u <- quantile(newlyn, probs = seq(0.1, 0.9, by = 0.1))
imt_theta <- choose_uk(newlyn, u = u, k = 1:5)
plot(imt_theta, uprob = TRUE)

---

**coef.iwls**

*Extract Model Coefficients from an "iwls" object*

**Description**

coef method for class c("iwls", "exdex").

**Usage**

```r
## S3 method for class 'iwls'
coef(object, ...)
```

**Arguments**

- `object` and object of class c("kaps", "exdex") returned from *iwls*.
- `...` Further arguments. None are used.

**Value**

A numeric scalar: the estimate of the extremal index \( \theta \).

---

**coef.kgaps**

*Extract Model Coefficients from a "kgaps" object*

**Description**

coef method for class c("kgaps", "exdex").

**Usage**

```r
## S3 method for class 'kgaps'
coef(object, ...)
```
coef.spm

Arguments

object and object of class c("kaps","exdex") returned from kgaps.

Further arguments. None are used.

Value

A numeric scalar: the estimate of the extremal index $\theta$.

Description

text

text

Usage

## S3 method for class 'spm'
coef(object, maxima = c("sliding","disjoint"),
estimator = "all", constrain = FALSE, ...)

Arguments

object and object of class c("spm","exdex") returned from spm.

maxima A character scalar specifying whether to return the estimate of the extremal index $\theta$ based on sliding maxima or on disjoint maxima.

estimator A character vector specifying which of the three variants of the semiparametric maxima estimator to use: "N2015", "BB2018" or "BB2018b". See spm for details. If estimator = "all" then all three estimates are returned.

constrain A logical scalar. If constrain = TRUE then any estimates that are greater than 1 are set to 1, that is, they are constrained to lie in (0, 1]. Otherwise, estimates that are greater than 1 may be obtained.

Further arguments. None are used.

Value

A numeric scalar (or a vector of length 2 if estimator = "both"): the required estimate(s) of the extremal index $\theta$.

References


confint.kgaps

Confidence intervals for the extremal index $\theta$

Description

confint method for objects of class c("kgaps", "exdex"). Computes confidence intervals for $\theta$ based on an object returned from kgaps. Two types of interval may be returned: (a) intervals based on approximate large-sample normality of the estimator of $\theta$, which are symmetric about the point estimate, and (b) likelihood-based intervals.

Usage

## S3 method for class 'kgaps'
confint(object, parm = "theta", level = 0.95,
interval_type = c("both", "norm", "lik"), conf_scale = c("theta",
"log"), constrain = TRUE, ...)

Arguments

- **object** An object of class c("kgaps", "exdex"), returned by kgaps.
- **parm** Specifies which parameter is to be given a confidence interval. Here there is only one option: the extremal index $\theta$.
- **level** The confidence level required. A numeric scalar in (0, 1).
- **interval_type** A character scalar: "norm" for intervals of type (a), "lik" for intervals of type (b).
- **conf_scale** A character scalar. If interval_type = "norm" then conf_scale determines the scale on which we use approximate large-sample normality of the estimator to estimate confidence intervals. If conf_scale = "theta" then confidence intervals are estimated for $\theta$ directly. If conf_scale = "log" then confidence intervals are first estimated for $\log \theta$ and then transformed back to the $\theta$-scale.
- **constrain** A logical scalar. If constrain = TRUE then any confidence limits that are greater than 1 are set to 1, that is, they are constrained to lie in (0, 1]. Otherwise, limits that are greater than 1 may be obtained. If constrain = TRUE then any lower confidence limits that are less than 0 are set to 0.
- **...** Further arguments. None are used currently.

Details

Two type of interval are calculated: (a) an interval based on the approximate large sample normality of the estimator of $\theta$ (if conf_scale = "theta") or of $\log \theta$ (if conf_scale = "log") and (b) a likelihood-based interval, based on the approximate large sample chi-squared, with 1 degree of freedom, distribution of the log-likelihood ratio statistic.
Value

A matrix with columns giving the lower and upper confidence limits. These are labelled as (1 - level)/2 and 1 - (1 - level)/2 in % (by default 2.5% and 97.5%). The row names indicate the type of interval: norm for intervals based on large sample normality and lik for likelihood-based intervals.

References


Examples

```r
u <- quantile(newlyn, probs = 0.90)
theta <- kgaps(newlyn, u)
confint(theta)
```

---

**Description**

`confint` method for objects of class `c("spm","exdex")`. Computes confidence intervals for θ based on an object returned from `spm`. Two types of interval may be returned: (a) intervals that are based on approximate large-sample normality of the estimators of θ (or of log θ if `conf_scale = "log"`), and which are symmetric about the respective point estimates, and (b) likelihood-based intervals based on an adjustment of a naive (pseudo-) loglikelihood, using the `adjust_loglik` function in the `chandwich` package.

**Usage**

```r
## S3 method for class 'spm'
confint(object, parm = "theta", level = 0.95,
        maxima = c("sliding", "disjoint"), interval_type = c("norm", "lik",
        "both"), conf_scale = c("theta", "log"), constrain = TRUE,
        bias_adjust = TRUE, type = c("vertical", "cholesky", "spectral",
        "none"), ...)
```

**Arguments**

- `object` An object of class `c("spm","exdex")`, returned by `spm`.
- `parm` Specifies which parameter is to be given a confidence interval. Here there is only one option: the extremal index θ.
- `level` A numeric scalar in (0, 1). The confidence level required.
- `maxima` A character scalar specifying whether to estimate confidence intervals based on sliding maxima or disjoint maxima.
interval_type  A character scalar: "norm" for intervals of type (a), "lik" for intervals of type (b).

conf_scale  A character scalar. If interval_type = "norm" then conf_scale determines the scale on which we use approximate large-sample normality of the estimators to estimate confidence intervals of type (a).

If conf_scale = "theta" then confidence intervals are estimated for \( \theta \) directly.
If conf_scale = "log" then confidence intervals are first estimated for \( \log \theta \) and then transformed back to the \( \theta \)-scale.

Any bias-adjustment requested in the original call to spm, using it's bias_adjust argument, is automatically applied here.

constrain  A logical scalar. If constrain = TRUE then any confidence limits that are greater than 1 are set to 1, that is, they are constrained to lie in \((0, 1]\). Otherwise, limits that are greater than 1 may be obtained. If constrain = TRUE then any lower confidence limits that are less than 0 are set to 0.

bias_adjust  A logical scalar. If bias_adjust = TRUE then, if appropriate, bias-adjustment is also applied to the loglikelihood before it is adjusted using adjust_loglik.
This is performed only if, in the call to spm, bias_adjust = "BB3" or "BB1" was specified, that is, we have object$bias_adjust = "BB3" or "BB1". In these cases the relevant component of object$bias_sl or object$bias_dj is used to scale \( \theta \) so that the location of the maximum of the loglikelihood lies at the bias-adjusted estimate of \( \theta \).

If bias_adjust = FALSE or object$bias_adjust = "none" or "N" then no bias-adjustment of the intervals is performed. In the latter case this is because the bias-adjustment is applied in the creation of the data in object$N2015_data and object$BB2018_data, on which the naive likelihood is based.

type  A character scalar. The argument type to be passed to conf_intervals in the chandwich package in order to estimate the likelihood-based intervals. Using type = "none" is not advised because then the intervals are based on naive estimated standard errors. In particular, if (the default) sliding = TRUE was used in the call to spm then the unadjusted likelihood-based confidence intervals provide vast underestimates of uncertainty.

Further arguments. None are used currently.

Details

The likelihood-based intervals are estimated using the adjust_loglik function in the chandwich package, followed by a call to conf_intervals. This adjusts the naive (pseudo-)loglikelihood so that the curvature of the adjust loglikelihood agrees with the estimated standard errors of the estimators. The option type = "none" should not be used in practice because the resulting confidence intervals will be wrong. In particular, in the intervals based on sliding maxima will provide vast underestimates of uncertainty.

If object$se contains NAs, because the block size \( b \) was too small or too large in the call to spm then confidence intervals cannot be estimated. A matrix of NAs will be returned. See the Details section of the spm documentation for more information.
A list of class c("confint_spm", "exdex") containing the following components.

cis
A matrix with columns giving the lower and upper confidence limits. These are labelled as (1 - level)/2 and 1 - (1 - level)/2 in % (by default 2.5% and 97.5%). The row names are a concatenation of the variant of the estimator (N2015 for Northrop (2015), BB2018 for Berghaus and Bucher (2018), BB2018b for the modified (by subtracting 1 / b) Berghaus and Bucher (2018) and the type of interval (norm for symmetric and lik for likelihood-based).

ciN
The object returned from `conf_intervals` that contains information about the adjusted loglikelihood for the Northrop (2015) variant of the estimator.

ciBB
The object returned from `conf_intervals` that contains information about the adjusted loglikelihood for the Berghaus and Bucher (2018) variant of the estimator.

ciBBb
The object returned from `conf_intervals` that contains information about the adjusted loglikelihood for the modified Berghaus and Bucher (2018) variant of the estimator.

call
The call to `spm`.

object
The input object.

maxima
The input maxima.

theta
The relevant estimates of $\theta$ returned from `adjust_loglik`. These are equal to `object$theta_sl` if `maxima = "sliding"`, `object$theta_dj` if `maxima = "disjoint"`, which provides a check that the results are correct.

References


See Also

`plot.confint_spm`: plot method for class c("confint_spm", "exdex").

Examples

```r
# Newlyn sea surges
theta <- spm(newlyn, 20)
confint(theta)
cis <- confint(theta, interval_type = "lik")
cis
plot(cis)

# S&P 500 index
theta <- spm(sp500, 100)
confint(theta)
```
```r
cis <- confint(theta, interval_type = "lik")
cis
plot(cis)
```

---

**exdex**  
**exdex: Estimation of the Extremal Index**

---

**Description**

The extremal index $\theta$ is a measure of the degree of local dependence in the extremes of a stationary process. The *exdex* package performs frequentist inference about $\theta$ using the methodologies proposed in Northrop (2015), Berghaus and Bucher (2018), Suveges (2007) and Suveges and Davison (2010).

**Details**

Functions to implement three estimators of the extremal index are provided, namely

- **spm**: semiparametric maxima estimator, using block maxima: (Northrop, 2015; Berghaus and Bucher, 2018)
- **kgaps**: $K$-gaps estimator, using threshold interexceedance times (Suveges and Davison, 2010)
- **iwls**: iterated weighted least squares estimator, using threshold interexceedance times: (Suveges, 2007)

See vignette("exdex-vignette",package = "exdex") for an overview of the package.

**References**


**See Also**

- **spm** for estimation of the extremal index $\theta$ using a semiparametric maxima method.
- **kgaps** for maximum likelihood estimation of the extremal index $\theta$ using the $K$-gaps model.
- **iwls**: iterated weighted least squares estimator.
- **newlyn** and **sp500** for example datasets.
Iterated weighted least squares estimation of the extremal index

Description

Estimates the extremal index $\theta$ using the iterated weighted least squares method of Suveges (2007). At the moment no estimates of uncertainty are provided.

Usage

iwls(data, u, maxit = 100)

Arguments

data: A numeric vector of raw data. No missing values are allowed.
u: A numeric scalar. Extreme value threshold applied to data.
maxit: A numeric scalar. The maximum number of iterations.

Details

The iterated weighted least squares algorithm on page 46 of Suveges (2007) is used to estimate the value of the extremal index. This approach uses the time gaps between successive exceedances in the data data of the threshold $u$. The $i$th gap is defined as $T_i - 1$, where $T_i$ is the difference in the occurrence time of exceedance $i$ and exceedance $i + 1$. Therefore, threshold exceedances at adjacent time points produce a gap of zero.

The model underlying this approach is an exponential-point mas mixture for scaled gaps, that is, gaps multiplied by the proportion of values in data that exceed $u$. Under this model scaled gaps are zero (‘within-cluster’ interexceedance times) with probability $1 - \theta$ and otherwise (‘between-cluster’ interexceedance times) follow an exponential distribution with mean $1/\theta$. The estimation method is based on fitting the ‘broken stick’ model of Ferro (2003) to an exponential quantile-quantile plot of all of the scaled gaps. Specifically, the broken stick is a horizontal line and a line with gradient $1/\theta$ which intersect at $(\log(\theta), 0)$. The algorithm on page 46 of Suveges (2007) uses a weighted least squares minimization applied to the exponential part of this model to seek a compromise between the role of $\theta$ as the proportion of interexceedance times that are between-cluster and the reciprocal of the mean of an exponential distribution for these interexceedance times. The weights (see Ferro (2003)) are based on the variances of order statistics of a standard exponential sample: larger order statistics have larger sampling variabilities and therefore receive smaller weight than smaller order statistics.

Note that in step (1) of the algorithm on page 46 of Suveges there is a typo: $N_c + 1$ should be $N$, where $N$ is the number of threshold exceedances. Also, the gaps are scaled as detailed above, not by their mean.

Value

An object (a list) of class "iwls", "exdex" containing

theta: The estimate of $\theta$. 

conv        A convergence indicator: 0 indicates successful convergence; 1 indicates that maxit has been reached.
niter       The number of iterations performed.
n_gaps      The number of time gaps between successive exceedances.
call        The call to iwls.

References


See Also

- `kgaps` for maximum likelihood estimation of the extremal index \( \theta \) using the \( K \)-gaps model.
- `spm` for estimation of the extremal index \( \theta \) using a semiparametric maxima method.

Examples

```r
### S&P 500 index
u <- quantile(sp500, probs = 0.60)
theta <- iwls(sp500, u)
theta

### Newlyn sea surges
u <- quantile(newlyn, probs = 0.90)
theta <- iwls(newlyn, u)
theta
```

kgaps

Maximum likelihood estimation for the \( K \)-gaps model

Description

Calculates maximum likelihood estimates of the extremal index \( \theta \) based on the \( K \)-gaps model for threshold inter-exceedances times of Suveges and Davison (2010).

Usage

```r
kgaps(data, u, k = 1, inc_cens = FALSE)
```
### Arguments

- **data**: A numeric vector of raw data. No missing values are allowed.
- **u**: A numeric scalar. Extreme value threshold applied to data.
- **k**: A numeric scalar. Run parameter \( K \), as defined in Suveges and Davison (2010). Threshold inter-exceedances times that are not larger than \( k \) units are assigned to the same cluster, resulting in a \( K \)-gap equal to zero. Specifically, the \( K \)-gap \( S \) corresponding to an inter-exceedance time of \( T \) is given by \( S = \max(T - K, 0) \).
- **inc_cens**: A logical scalar indicating whether or not to include contributions from censored inter-exceedance times relating to the first and last observation. See Attalides (2015) for details.

### Details

The maximum likelihood estimate of the extremal index \( \theta \) under the \( K \)-gaps model of Suveges and Davison (2010) is calculated. If \( \text{inc}_\text{cens} = \text{TRUE} \) then information from censored inter-exceedance times is included in the likelihood to be maximized, following Attalides (2015). The form of the log-likelihood is given in the **Details** section of `kgaps_stat`.

It is possible that the estimate of \( \theta \) is equal to 1, and also possible that it is equal to 0. `kgaps_stat` explains the respective properties of the data that cause these events to occur.

### Value

An object (a list) of class c("kgaps", "exdex") containing

- **theta**: The maximum likelihood estimate (MLE) of \( \theta \).
- **se**: The estimated standard error of the MLE.
- **ss**: The list of summary statistics returned from `kgaps_stat`.
- **k, u, inc_cens**: The input values of \( k \), \( u \) and \( \text{inc}_\text{cens} \).
- **call**: The call to `kgaps`.

### References


### See Also

- `confint.kgaps` to estimate confidence intervals for \( \theta \).
- `kgaps_imt` for the information matrix test, which may be used to inform the choice of the pair \((u,k)\).
- `choose_uk` for a diagnostic plot based on `kgaps_imt`.
- `kgaps_stat` for the calculation of sufficient statistics for the \( K \)-gaps model.
- `kgaps_post` in the revdbayes package for Bayesian inference about \( \theta \) using the \( K \)-gaps model.
spm for estimation of the extremal index \( \theta \) using a semiparametric maxima method.

iwls: iterated weighted least squares estimator.

Examples

```r
### S&P 500 index
u <- quantile(sp500, probs = 0.60)
theta <- kgaps(sp500, u)
theta
summary(theta)

### Newlyn sea surges
u <- quantile(newlyn, probs = 0.60)
theta <- kgaps(newlyn, u, k = 2)
theta
summary(theta)
```

kgaps_imt

Information matrix test under the \( K \)-gaps model

Description

Performs the information matrix test (IMT) of Suveges and Davison (2010) to diagnose misspecification of the \( K \)-gaps model

Usage

```r
kgaps_imt(data, u, k = 1)
```

Arguments

data A numeric vector of raw data. No missing values are allowed.

u, k Numeric vectors. \( u \) is a vector of extreme value thresholds applied to data. \( k \) is a vector of values of the run parameter \( K \), as defined in Suveges and Davison (2010). See kgaps for more details.

Details

The IMT is performed over a grid of all combinations of threshold and \( K \) in the vectors \( u \) and \( k \). If the estimate of \( \theta \) is 0 then the IMT statistic, and its associated \( p \)-value will be NA.

For details of the IMT see Suveges and Davison (2010). There are some typing errors on pages 18-19 that have been corrected in producing the code: the penultimate term inside \( \{ \ldots \} \) in the middle equation on page 18 should be \( (c_j(K))^2 \), as should the penultimate term in the first equation on page 19; the \( \{ \ldots \} \) bracket should be squared in the 4th equation on page 19; the factor \( n \) should be \( N - 1 \) in the final equation on page 19.
kgaps_stat

Value
An object (a list) of class c("kgaps_imt","exdex") containing

imt A length(u) by length(k) numeric matrix. Column i contains, for \( K = k[i] \), the values of the information matrix test statistic for the set of thresholds in \( u \). The column names are the values in codek. The row names are the approximate empirical percentage quantile levels of the thresholds in \( u \).
p A length(u) by length(k) numeric matrix containing the corresponding \( p \)-values for the test.
theta A length(u) by length(k) numeric matrix containing the corresponding estimates of \( \theta \).
u,k The input \( u \) and \( k \).

References

See Also
kgaps for maximum likelihood estimation of the extremal index \( \theta \) using the \( K \)-gaps model.

Examples
```r
  u <- quantile(newlyn, probs = seq(0.1, 0.9, by = 0.1))
  imt <- kgaps_imt(newlyn, u, k = 1:5)
```

kgaps_stat Sufficient statistics for the \( K \)-gaps model

Description
Calculates sufficient statistics for the \( K \)-gaps model for the extremal index \( \theta \).

Usage
```r
  kgaps_stat(data, u, k = 1, inc_cens = FALSE)
```

Arguments

- **data** A numeric vector of raw data. No missing values are allowed.
- **u** A numeric scalar. Extreme value threshold applied to data.
- **k** A numeric scalar. Run parameter \( K \), as defined in Suveges and Davison (2010). Threshold inter-exceedances times that are not larger than \( k \) units are assigned to the same cluster, resulting in a \( K \)-gap equal to zero. Specifically, the \( K \)-gap \( S \) corresponding to an inter-exceedance time of \( T \) is given by \( S = \max(T - K, 0) \).
inc_cens A logical scalar indicating whether or not to include contributions from censored inter-exceedance times relating to the first and last observation. See Attalides (2015) for details.

Details

The sample $K$-gaps are $S_0, S_1, ..., S_{N-1}, S_N$, where $S_1, ..., S_{N-1}$ are uncensored and $S_0$ and $S_N$ are censored. Under the assumption that the $K$-gaps are independent, the log-likelihood of the $K$-gaps model is given by

$$l(\theta; S_0, \ldots, S_N) = N_0 \log(1 - \theta) + 2N_1 \log \theta - \theta q(S_0 + \cdots + S_N),$$

where $q$ is the threshold exceedance probability, $N_0$ is the number of sample $K$-gaps that are equal to zero and (apart from an adjustment for the contributions of $S_0$ and $S_N$) $N_1$ is the number of positive sample $K$-gaps. Specifically, $N_1$ is equal to the number of $S_1, ..., S_{N-1}$ that are positive plus $(I_0 + I_N)/2$, where $I_0 = 1$ if $S_0$ is greater than zero and similarly for $I_N$. The differing treatment of uncensored and censored $K$-gaps reflects differing contributions to the likelihood. For full details see Suveges and Davison (2010) and Attalides (2015).

If $N_1 = 0$ then we are in the degenerate case where there is one cluster (all $K$-gaps are zero) and the likelihood is maximized at $\theta = 0$.

If $N_0 = 0$ then all exceedances occur singly (all $K$-gaps are positive) and the likelihood is maximized at $\theta = 1$.

Value

A list containing the sufficient statistics, with components

- $N_0$ the number of zero $K$-gaps
- $N_1$ contribution from non-zero $K$-gaps (see Details)
- sum_qs the sum of the (scaled) $K$-gaps, i.e. $q(S_0 + \cdots + S_N)$, where $q$ is estimated by the proportion of threshold exceedances.
- n_kgaps the number of $K$-gaps, including 2 censored $K$-gaps if inc_cens = TRUE.

References


See Also

kgaps for maximum likelihood estimation of the extremal index $\theta$ using the $K$-gaps model.

Examples

```r
u <- quantile(newlyn, probs = 0.90)
k gaps_stat(newlyn, u)
```
Description

The vector `newlyn` contains 2894 maximum sea-surges measured at Newlyn, Cornwall, UK over the period 1971-1976. The observations are the maximum hourly sea-surge heights over contiguous 15-hour time periods.

Usage

`newlyn`

Format

A vector of length 2894.

Source


References


---

**nobs.iwls**

*Extract the Number of Observations from an "iwls" object*

Description

`nobs` method for class `c("iwls","exdex")`.

Usage

```r
## S3 method for class 'iwls'
nobs(object, ...)
```

Arguments

- `object` and object of class `c("iwls","exdex")` returned from `iwls`.
- `...` Further arguments. None are used.
nobs.kgaps

Extract the Number of Observations from a "kgaps" object

Description
nobs method for class c("kgaps","exdex").

Usage
## S3 method for class 'kgaps'
nobs(object, ...)

Arguments

object and object of class c("kgaps","exdex") returned from kgaps.

... Further arguments. None are used.

Value
A numeric scalar: the number of inter-exceedance times used in the fit. If \( x\text{'inc_cens' = TRUE} \) then this includes 2 censored observations.

nobs.spm

Extract the Number of Observations from an "spm" object

Description
nobs method for class c("spm","exdex").

Usage
## S3 method for class 'spm'
nobs(object, maxima = c("sliding","disjoint"), ...)

Arguments

object and object of class c("spm","exdex") returned from spm.

maxima A character scalar specifying whether to return the number of observed sliding maxima or disjoint maxima.

... Further arguments. None are used.

Value
A numeric scalar: the number of observations used in the fit.
plot.choose_b

Plot block length diagnostic for the semiparametric maxima estimator

Description

plot method for objects inheriting from class "choose_b", returned from choose_b

Usage

## S3 method for class 'choose_b'
plot(x, y, ..., estimator = c("N2015", "BB2018"),
     maxima = c("sliding", "disjoint"))

Arguments

x an object of class c("choose_b", "exdex"), a result of a call to choose_b.
y Not used.
... Additional arguments passed on to matplot and/or axis.
maxima Should the estimator be based on sliding or disjoint maxima?

Details

Produces a simple diagnostic plot to aid the choice of block length \( b \) based on the object returned from choose_b. Estimates of \( b \) and approximate conf\% confidence intervals are plotted against the value of \( b \) used to produce each estimate. The type of confidence interval is determined by the arguments interval_type, conf_scale and type provided in the call to choose_b.

Value

Nothing is returned.

Examples

See the examples in choose_b.

References


See Also

choose_b.
plot.choose.uk

Plot Threshold $u$ and runs parameter $K$ diagnostic for the $K$-gaps estimator

Description

plot method for objects inheriting from class "choose.uk", returned from choose.uk

Usage

## S3 method for class 'choose.uk'
plot(x, y = c("imts", "theta"), level = 0.95,
     interval_type = c("norm", "lik"), conf_scale = c("theta", "log"),
     alpha = 0.05, constrain = TRUE, for_abline = list(lty = 2, lwd = 1,
     col = 1), digits = 3, uprob = FALSE, leg_pos = if (y == "imts")
     "topright" else "topleft", ...)

Arguments

x an object of class c("choose.uk", "exdex"), a result of a call to choose.uk.

y A character scalar indicating what should be plotted on the vertical axes of the
plot: information matrix test statistics (IMTS) if y = "imts" and estimates of
$\theta$ if y = "theta". If y = "theta", and either x$u$ or x$k have length one,
then 100level% confidence intervals are added to the plot.

level A numeric scalar in (0, 1). The confidence level used in calculating confidence
intervals for $\theta$. Only relevant if y = "theta" and either x$u$ or x$k have length
one.

interval_type A character scalar. The type of confidence interval to be plotted, if y = "theta".
See confint.kgaps.

conf_scale A character scalar. If interval_type = "norm" then conf_scale determines
the scale on which we use approximate large-sample normality of the estimator
to estimate confidence intervals. See confint.kgaps.

alpha A numeric vector with entries in (0, 1). The size of the test to be performed.

constrain A logical scalar. The argument constrain to confint.kgaps.

for_abline Only relevant when y = "imts" and at one of u or k is scalar. A list of graphical
parameters to be passed to abline to indicate the critical value of the informa-
tion matrix test (IMT) implied by alpha.

digits An integer. Used for formatting the value of the threshold with signif before
adding its value to a plot.

uprob A logical scalar. Should we plot x$u$ on the horizontal axis (uprob = FALSE) or
the approximate sample quantile to which x$u$ corresponds (uprob = FALSE)?

leg_pos A "character scalar. The position of any legend added to a plot. Only relevant
when both the arguments u and k in the call to choose.uk have length greater
than one.

... Additional arguments passed to matplot.
Details

The type of plot produced depends mainly on \( y \).

If \( y = "imts" \) then the values of IMTS are plotted against the thresholds in \( x_u \) (or their corresponding approximate sample quantile levels if \( uprob = \text{TRUE} \)) for each value of \( K \) in \( x_k \). Horizontal lines are added to indicate the critical values of the IMT for the significance levels in \( \alpha \). We would not reject at the 100\( \alpha \)% level combinations of threshold and \( K \) corresponding to values of the IMTS that fall below the line.

If \( y = "theta" \) then estimates of \( \theta \) are plotted on the vertical axis. If both \( x_u \) and \( x_k \) have length greater than one then only these estimates are plotted. If either \( x_u \) or \( x_k \) have length one then approximate 100\( \alpha \)% confidence intervals are added to the plot and the variable, \( x_u \) or \( x_k \) that has length greater than one is plotted on the horizontal axis.

Value

Nothing is returned.

Examples

See the examples in \texttt{choose.uk}.

See Also

\texttt{choose.uk}.

---

\texttt{plot.confint_spm} \hspace{1cm} \textit{Plot diagnostics for a confint_spm object}

---

Description

\texttt{plot} method for an objects of class c("confint_spm","exdex").

Usage

\footnotesize

```r
## S3 method for class 'confint_spm'
plot(x, y = NULL, estimator = "all", ndec = 2, 
    ...) # Not used.
```

Arguments

\begin{itemize}
\item \texttt{x} \hspace{1cm} an object of class c("confint_spm","exdex"). a result of a call to \texttt{confint.spm}.
\item \texttt{y} \hspace{1cm} Not used.
\item \texttt{estimator} \hspace{1cm} A character vector specifying which of the three variants of the semiparametric maxima estimator to include in the plot: "N2015", "BB2018" or "BB2018b". See \texttt{spm} for details. If \texttt{estimator = "all"} then all three are included.
\item \texttt{ndec} \hspace{1cm} An integer scalar. The legend (if included on the plot) contains the confidence limits rounded to \texttt{ndec} decimal places.
\end{itemize}

Further arguments to be passed to \texttt{plot.confint}. 

---
print.confint_spm

Value
Nothing is returned.

Examples
See the examples in confint.spm.

See Also
  confint.spm: confint method for class c("spm","exdex").

print.confint_spm

Print method for a confint_spm object

Description
print method for class c("confint_spm","exdex").

Usage
## S3 method for class 'confint_spm'
print(x, ...)

Arguments
  x               an object of class c("confint_spm","exdex"), a result of a call to confint.spm.
  ...             Additional optional arguments to be passed to print.default

Details
Prints the matrix of confidence intervals for θ.

Value
The argument x, invisibly, as for all print methods.

See Also
  spm for estimation of the extremal index θ using a semiparametric maxima method.
  confint.spm: confint method for class "spm".
print.iwls

Print method for an "iwls" object

Description
print method for class c("iwls", "exdex").

Usage
## S3 method for class 'iwls'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

Arguments
- x: an object of class c("iwls", "exdex"), a result of a call to iwls.
- digits: The argument digits to print.default.
- ...: Additional arguments. None are used in this function.

Details
Prints the original call to iwls and the estimate of the extremal index \( \theta \).

Value
The argument x, invisibly, as for all print methods.

See Also
- iwls for maximum likelihood estimation of the extremal index \( \theta \) using the \( K \)-gaps model.

print.kgaps

Print method for a "kgaps" object

Description
print method for class c("kgaps", "exdex").

Usage
## S3 method for class 'kgaps'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
Arguments

- **x**: an object of class c("kgaps", "exdex"), a result of a call to `kgaps`.
- **digits**: The argument `digits` to `print.default`.
- **...**: Additional arguments. None are used in this function.

Details

Prints the original call to `kgaps` and the estimate of the extremal index $\theta$.

Value

The argument `x`, invisibly, as for all `print` methods.

See Also

- `kgaps`: for maximum likelihood estimation of the extremal index $\theta$ using the K-gaps model.
- `confint.kgaps`: confint method for class "kgaps".

Description

`print method for an "spm" object`

Usage

```r
## S3 method for class 'spm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

- **x**: an object of class c("spm", "exdex"), a result of a call to `spm`.
- **digits**: The argument `digits` to `print.default`.
- **...**: Additional arguments. None are used in this function.

Details

Prints the original call to `spm` and the estimates of the extremal index $\theta$, based on all three variants of the semiparametric maxima estimator and both sliding and disjoint blocks.

Value

The argument `x`, invisibly, as for all `print` methods.
print.summary.kgaps

See Also

spm for estimation of the extremal index \( \theta \) using a semiparametric maxima method.

confint.spm: confint method for class "spm".

Description

print method for an object \( x \) of class “summary.kgaps”.

Usage

## S3 method for class 'summary.kgaps'
print(x, ...)

Arguments

\( x \) An object of class "summary.pm", a result of a call to summary.kgaps.

\( \ldots \) Additional arguments passed on to print.default.

Value

Prints the numeric matrix \( x \$\text{summary} \) returned from summary.kgaps.

Examples

See the examples in kgaps.

See Also

kgaps for estimation of the extremal index \( \theta \) using a semiparametric maxima method.

confint.kgaps for estimation of confidence intervals for \( \theta \).
print.summary.spm  Print method for objects of class "summary.spm"

Description

print method for an object x of class "summary.spm".

Usage

## S3 method for class 'summary.spm'
print(x, ...)

Arguments

x  An object of class "summary.spm", a result of a call to summary.spm.
...
Additional arguments passed on to print.default.

Value

Prints the numeric matrix x$summary returned from summary.spm.

Examples

See the examples in spm.

See Also

spm for estimation of the extremal index \( \theta \) using a semiparametric maxima method.

confint.spm for estimation of confidence intervals for \( \theta \).

---

sp500  Daily log returns of the Standard and Poor (S&P) 500 index

Description

Daily log returns of the S&P 500 index, that is, the log of the ratio of successive daily closing prices, from 3rd January 1990 to 9th October 2018.

Usage

sp500

Format

A vector of length 7250, created using zoo with an "index" attribute giving the date of the corresponding negated log return.

---

sp500

Daily log returns of the Standard and Poor (S&P) 500 index

Description

Daily log returns of the S&P 500 index, that is, the log of the ratio of successive daily closing prices, from 3rd January 1990 to 9th October 2018.

Usage

sp500

Format

A vector of length 7250, created using zoo with an "index" attribute giving the date of the corresponding negated log return.
Description

Estimates the extremal index $\theta$ using a semiparametric block maxima estimator of Northrop (2015) ("N2015") and a variant of this estimator studied by Berghaus and Bucher (2018) ("BB2018"), using both sliding (overlapping) block maxima and disjoint (non-overlapping) block maxima. A simple modification (subtraction of $1/b$, where $b$ is the block size) of the Berghaus and Bucher (2018) estimator ("BB2018b") is also calculated. Estimates of uncertainty are calculated using the asymptotic theory developed by Berghaus and Bucher (2018).

Usage

```r
spm(data, b, bias_adjust = c("BB3", "BB1", "N", "none"),
     constrain = TRUE, varN = TRUE, which_dj = c("last", "first"))
```

Arguments

data: A numeric vector of raw data. No missing values are allowed.
b: A numeric scalar. The block size.
bias_adjust: A character scalar. Is bias-adjustment of the raw estimate of $\theta$ performed using the bias-reduced estimator (bias_adjust = "BB3"), derived in Section 5 of Berghaus and Bucher (2018); or a simpler version (bias_adjust = "BB1"), in which the raw estimate is multiplied by $(k - 1)/k$, where $k$ is the number of blocks; or the bias-adjustment of the empirical distribution function used to calculate the estimate, as detailed in Section 2 of Northrop (2015). When disjoint maxima are used bias_adjust = "BB1" and bias_adjust = "N" give identical estimates of the Berghaus and Bucher (2018) variant, as explained at the end of Section 5 of Berghaus and Bucher (2018). If bias_adjust = "none" then no bias-adjustment is performed.

constrain: A logical scalar. If constrain = TRUE then any estimates that are greater than 1 are set to 1, that is, they are constrained to lie in (0, 1]. This is carried out after any bias-adjustment. Otherwise, estimates that are greater than 1 may be obtained.

varN: A logical scalar. If varN = TRUE then the estimation of the sampling variance of the Northrop (2015) estimator is tailored to that estimator. Otherwise, the sampling variance derived in Berghaus and Bucher (2018) is used. See Details for further information.

which_dj: A character scalar. Determines which set of disjoint maxima are used to calculate an estimate of $\theta$: "first", only the set whose first block starts on the first observation in x; "last", only the set whose last block ends on the last observation in x.
Details

The extremal index $\theta$ is estimated using the semiparametric maxima estimator of Northrop (2015) and variant of this studied by Berghaus and Bucher (2018). In each case a sample of 'data' is derived from the input data `data`, based on the empirical distribution function of these data evaluated at the maximum values of of blocks of $b$ contiguous values in `data`.

The estimators are based on an assumption that these 'data' are sampled approximately from an exponential distribution with mean $1/\theta$. For details see page 2309 of Berghaus and Bucher (2018), where the 'data' for the Northrop (2015) estimator are denoted $Y$ and those for the Berghaus and Bucher (2018) are denoted $Z$. For convenience, we will refer to these values as the $Y$-data and the $Z$-data.

The approximate nature of the model for the $Y$-data arises from the estimation of the distribution function $F$. A further approximation motivates the use of the $Z$-data. If $F$ is known then the variable $Z/b$ has a beta$(1, b\theta)$ distribution, so that that is, $Z$ has mean $1/(\theta + 1/b)$. Therefore, an exponential distribution with mean $1/(\theta + 1/b)$ may provide a better approximate model, which provides the motivation for subtracting $1/b$ from the Berghaus and Bucher (2018) estimator. Indeed, the resulting estimates are typically close to those of the Northrop (2015) estimator.

If `sliding = TRUE` then the function uses sliding block maxima, that is, the largest value observed in all $(\text{length}(\text{data}) - b + 1)$ blocks of $b$ observations. If `sliding = FALSE` then disjoint block maxima, that is, the largest values in $(\text{floor}(n / b))$ disjoint blocks of $b$ observations, are used.

Estimation of the sampling variances of the estimators is based on Proposition 4.1 on page 2319 of Berghaus and Bucher (2018). For the Northrop (2015) variant the user has the choice either to use the sampling variance based on the Berghaus and Bucher (2018) estimator, i.e. the $Z$-data ($\text{varN} = \text{FALSE}$) or an analogous version tailored to the Northrop (2015) estimator that uses the $Y$-data ($\text{varN} = \text{TRUE}$).

The estimates of the sampling variances of the sliding blocks estimators are inferred from those of the disjoint blocks estimators (see page 2319 of Berghaus and Bucher (2018)). The calculation of the latter uses a set of disjoint block maxima. If `length(data)` is not an integer multiple of $b$ then there will be more than one set of these, and all are equally valid. In this event we perform the calculation for all such sets and use the mean of the resulting estimates. This reduces the sampling variability of the estimates at the expense of slowing down the calculation somewhat, particularly if $b$ is small. This may become apparent when calling `spm` repeatedly in `choose_b`.

This estimator of the sampling variance of the sliding blocks estimator is not constrained to be positive: a negative estimate may result if the block size is small. In this event **no warning will be given until the returned object is printed** and, for the affected estimator ("N2015" or "BB2018/BB2018b"),

- the corresponding estimated standard errors using sliding blocks will be missing in `se_sl` in the returned object,
- if `bias_adjust == "BB3"` then bias-adjustment based on `bias_adjust == "BB1"` will instead be performed when using sliding blocks, because the former relies on the estimated variances of the estimators.

Similarly, bias adjustment under `adjust = "BB3"` and/or subtraction of $1/b$ in the "BB2018b" case may, rare cases, produce a negative estimate of $\theta$. In these instances an estimate of zero is returned, but the values returned in `bias_dj` and `bias_sl` are not changed.
**Value**

A list of class `c("spm","exdex")` containing the components listed below. The components that are vectors are labelled to indicate the estimator to which the constituent values relate: "N2015" for Northrop (2015), "BB2018" for Berghaus and Bucher (2018) and "BB2018b" for the modified version.

- **theta_sl, theta_dj**
  Vectors containing the estimates of $\theta$ resulting from sliding maxima and disjoint maxima respectively.

- **se_sl, se_dj**
  The estimated standard errors associated with the estimates in theta_sl and theta_dj. The values for "BB2018" and "BB2018b" are identical.

- **bias_sl, bias_dj**
  The respective values of the bias-adjustment applied to the raw estimates, that is, the values subtracted from the raw estimates. For estimator BB2018b this includes a contribution for the subtraction of $1/b$. If bias_adjust = "N" or "none" then bias_sl and bias_dj are `c(0,0,1/b)`.

- **raw_theta_sl, raw_theta_dj**
  Vectors containing the raw estimates of $\theta$, prior to any bias_adjustment.

- **uncon_theta_sl, uncon_theta_dj**
  The (bias_adjusted) estimates of $\theta$ before the constraint that they lie in $(0, 1]$ has been applied.

- **data_sl, data_dj**
  Matrices containing the Y-data and Z-data for the sliding an disjoint maxima respectively. The first columns are the Y-data, the second columns the Z-data.

- **sigma2dj, sigma2dj_for_sl**
  Estimates of the variance $\sigma^2_{dj}$ defined on pages 2314-2315 of Berghaus and Bucher (2018). The form of the estimates is given on page 2319. sigma2dj is used in estimating the standard error se_dj, sigma2dj_for_sl in estimating the standard error se_sl.

- **sigma2sl**
  Estimates of the variance $\sigma^2_{sl}$, defined on pages 2314-2315 of Berghaus and Bucher (2018). The form of the estimates is given on page 2319. sigma2dj_for_sl is used to estimate $\sigma^2_{dj}$ for this purpose.

- **b**
  The input value of b.

- **bias_adjust**
  The input value of bias_adjust.

- **call**
  The call to `spm`.

**References**


See Also

`confint.spm` to estimate confidence intervals for `theta`.

`kgaps` for maximum likelihood estimation of the extremal index \(\theta\) using the \(K\)-gaps model.

`iwls`: iterated weighted least squares estimator.

Examples

```r
### Newlyn sea surges
theta <- spm(newlyn, 20)
theta
summary(theta)

### S&P 500 index
theta <- spm(sp500, 100)
theta
summary(theta)
```

summary.kgaps

Summary method for a "kgaps" object

Description

summary method for class "kgaps"

Usage

```r
## S3 method for class 'kgaps'
summary(object, digits = max(3, getOption("digits") - 3L), ...)
```

Arguments

- `object` an object of class "kgaps", a result of a call to `kgaps`.
- `digits` An integer. Used for number formatting with `signif`.
- `...` Additional arguments. None are used in this function.

Value

Returns a list containing the list element `object$call` and a numeric matrix `summary` giving the Estimate of the extremal index \(\theta\) and the estimated standard error (Std. Error).

Examples

See the examples in `kgaps`.
summary.spm

See Also

kgaps for estimation of the extremal index $\theta$ using a semiparametric maxima method.
confint.kgaps for estimation of confidence intervals for $\theta$.

---

**summary.spm**

*Summary method for an "spm" object*

**Description**

summary method for class "spm"

**Usage**

```r
## S3 method for class 'spm'
summary(object, digits = max(3, getOption("digits") - 3L),
     ...)
```

**Arguments**

- **object**: an object of class "spm", a result of a call to `spm`.
- **digits**: An integer. Used for number formatting with `signif`.
- **...**: Additional arguments. None are used in this function.

**Value**

Returns a list containing the list element `object$call` and a numeric matrix `summary` giving, for all three variants of the semiparametric estimator and both sliding and disjoint blocks, the (bias-adjusted) Estimate of the extremal index $\theta$, the estimated standard error (Std. Error), and the bias adjustment (Bias adj.) applied to obtain the estimate, i.e. the value subtracted from the raw estimate. If any of the (bias-adjusted) estimates are greater than 1 then a column containing the unconstrained estimates (Uncon. estimate) is added.

**Examples**

See the examples in `spm`.

**See Also**

`spm` for estimation of the extremal index $\theta$ using a semiparametric maxima method.
`confint.spm` for estimation of confidence intervals for $\theta$. 
vcov.kgaps  

*Calculate Variance-Covariance Matrix for a "kgaps" object*

**Description**

vcov method for class c("kgaps", "exdex").

**Usage**

```r
## S3 method for class 'kgaps'
vcov(object, ...)
```

**Arguments**

- `object` and object of class c("kgaps", "exdex") returned from `kgaps`.
- `...` Further arguments. None are used.

**Value**

A 1 by 1 numeric matrix containing the estimated variance of the estimator.

vcov.spm  

*Calculate Variance-Covariance Matrix for an "spm" object*

**Description**

vcov method for class c("spm", "exdex").

**Usage**

```r
## S3 method for class 'spm'
vcov(object, maxima = c("sliding", "disjoint"),
estimator = "all", ...)
```

**Arguments**

- `object` and object of class c("spm", "exdex") returned from `spm`.
- `maxima` A character scalar specifying whether to return the estimated variance of the estimator of the extremal index \( \theta \) based on sliding maxima or on disjoint maxima.
- `estimator` A character vector specifying which of the three variants of the semiparametric maxima estimator to use: "N2015", "BB2018" or "BB2018b". See `spm` for details. If `estimator = "all"` then the estimated variances of all variants are returned.
- `...` Further arguments. None are used.
Value

A 1 by 1 numeric matrix if estimator = "N2015" or "BB2018" and a vector of length 2 if estimator = "both", containing the estimated variance(s) of the estimator(s).

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