

Package ‘fmlogcondens’

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Type Package

Title Fast Multivariate Log-Concave Density Estimation

Version 1.0.2

Description A fast solver for the maximum likelihood estimator (MLE) of a multivariate log-concave probability function. Given a sample X, it estimates a non-parametric density function whose logarithm is a concave function. Many well-known parametric densities belong to that class, among them the normal density, the uniform density, the exponential distribution and many more. This package provides functions for the estimation of a log-concave density and a mixture of log-concave densities in multiple dimensions. While being similar to the package LogConcDEAD, fmlogcondens provides much fast run times for large samples (≥ 250 points). As a reference see Fabian Rathke, Christoph Schnörr (2015), <doi:10.1515/auom-2015-0053>.

License GPL (≥ 2)

URL <https://github.com/FabianRathke/fmlogcondens>

Depends R ($\geq 3.2.4$)

Imports geometry, MASS, mclust, mvtnorm

Encoding UTF-8

LazyData true

Suggests LogConcDEAD, knitr, rmarkdown

VignetteBuilder knitr

RoxygenNote 6.0.1

NeedsCompilation yes

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calcCvxHullFaces	<i>Calculates the convex hull of X</i>
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Description

calcCvxHullFaces returns the parameters of the convex hull of X: The indices of points in X that compose the faces of $\text{conv}(X)$ (one row per face) as well as the parameters of the hyperplanes that describe these faces.

Usage

```
calcCvxHullFaces(X)
```

Arguments

X	Set of data points (one sample per row)
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Value

A list consisting of parameters describing the convex hull of X:

cvh	A matrix of indices where each row constitutes one face
ACVH	A matrix where each row constitutes the normal vector of a face
bCVH	A vector where each entry constitutes the offset of the hyperplane for a face

compilationInfo	<i>Checks if AVX is active</i>
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Description

compilationInfo is a wrapper to a C function, which prints information about whether AVX extensions were activated during compilation. Active AVX speeds up computations significantly (by a factor of 4 to 8 roughly). More informations about how AVX can be enabled during installation can be found in documentation.

Usage

compilationInfo()

correctIntegral	<i>Normalizes Log-Concave Density</i>
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Description

correctIntegral normalizes a log-concave density parametrized by a set of hyperplane parameters. Works by calculating $y = \log(f(x))$ for each data point in X, normalizing y, and then recalculating a and b.

Usage

correctIntegral(X, mu, a, b, cvh)

Arguments

X	Set of data points (one sample per row)
mu	Mean vector of X that gets added back to X
a	Matrix where rows are hyperplane normals
b	Vector where entries are intercepts of hyperplanes
cvh	Matrix where each row is a set of indices of points in X describing one face of conv(X)

Value

Normalized hyperplane parameters (for the uncentered $X \leftarrow X + \mu$)

a, b	Hyperplane parameters of the normalized density.
y	Vector with values $y_i = \log(f(X_i))$ of the normalized density.
aSparse, bSparse	Input hyperplane parameters.

Examples

```
# draw samples from normal distribution
X <- matrix(rnorm(200),100,2)
# calculate parameters of convex hull of X
r <- calcCvxHullFaces(X)
# draw random parameters of 10 hyperplanes
a <- matrix(runif(10*2),10,2)
b <- runif(10)

# calculate parameters of convex hull of X
params <- correctIntegral(X,rep(0,2),a,b,r$cvh)
```

fmlcd

*Estimates a Log-Concave Density***Description**

fmlcd returns a MLE estimate of a log-concave density for X . After obtaining an initial parameter estimate the MLE objective with log-concavity and normalization constraint is optimized using a quasi-Newton approach for large scale optimization (BFGS-L). The logarithm of the optimal density $f(x)$ is a piecewise-linear function. Its parametrization in terms of a set of hyperplanes is returned.

Usage

```
fmlcd(X, w = rep(1/nrow(X), nrow(X)), init = "", verbose = 0,
      intEps = 0.001, objEps = 1e-07, offset = 0.1, maxIter = 10000)
```

Arguments

<code>X</code>	Matrix of data points (one sample per row)
<code>w</code>	Vector of sample weights (default: uniform weights)
<code>init</code>	String that sets the initialization approach. 'kernel' based on kernel density, 'smooth' based on smooth log-concave density, '' compares both and takes the optimal one. (default: '')
<code>verbose</code>	Int determining the verbosity of the code; 0 = no output to 3. (default: 0)
<code>intEps</code>	Stopping criteria for the numerical integration accuracy Optimization stops if both measurements are smaller than intEps and objEps Modification of this value is not recommended. (default: 1e-3)
<code>objEps</code>	Stopping criteria for the change in the objective function Optimization stops if both measurements are smaller than intEps and objEps Modification of this value is not recommended. (default: 1e-7)
<code>offset</code>	Smaller values correspond to slower hyperplane reduction. Offset should be a value smaller than 1. Modification of this value is not recommended. (default: 1e-1)
<code>maxIter</code>	Number of iterations in the main optimization (default: 1e4)

Value

Parametrization of $f(x)$ in terms of hyperplanes and function evaluations $y = \log(f(x))$

aOpt, bOpt Analytically normalized parameters of $f(x)$.
 logLike Log-likelihood of $f(x)$
 y Vector with values $y_i = \log(f(X_i))$ of the normalized density ($\logLike = \sum(y_i)$).
 aOptSparse, bOptSparse Sparse parametrization normalized on the integration grid.

Examples

```
# draw samples from normal distribution
X <- matrix(rnorm(200),100,2)
# calculate parameters of convex hull of X
r <- calcCvxHullFaces(X)
# draw random parameters of 10 hyperplanes
a <- matrix(runif(10*2),10,2)
b <- runif(10)

# calculate parameters of convex hull of X
params <- correctIntegral(X,rep(0,2),a,b,r$cvh)
```

fmlcdEM

*Estimates a Log-Concave Mixture Density***Description**

fmlcdEM Utilizes the EM approach to obtain a mixture of log-concave densities. Utilizes Gaussian hierarchical clustering to initialize the posterior probabilities of class affiliation (as proposed by the package LogConcDEAD by Cule et al.).

Usage

```
fmlcdEM(X, K = 2, posterior, verbose = 0, maxIter = 50)
```

Arguments

X Matrix of data points (one sample per row)
 K Number of latent variables (default: 2)
 posterior Matrix with posterior probabilities for class affiliation; Initialized if not provided using a Gaussian hierarchical clustering.
 verbose Int determining the verbosity of the code; 0 = no output to 3. (default: 0)
 maxIter Maximal number of EM iterations. (default: 50)

Value

Parametrization of the mixture density

params	List of length K, where each entry contains the hyperplane for one density
densEst	Matrix where each row contains the marginal distribution $p(x)$
tau	Marginal distribution over the latent variable $p(z)$

paramFitGammaOne	<i>Parameter Initialization Based on a Smooth Log-Concave Density</i>
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Description

paramFitGammaOne fits in a first step a log-concave density to data points X with weights w using a smoothness parameter of $\gamma=1$. In a second step, it calculates the upper convex hull of the set X and $\log(y)$, where y_i is the smooth log-concave density evaluated at X_i . It returns the hyperplane parameters of the faces of this upper convex hull.

Usage

```
paramFitGammaOne(X, w, ACVH, bCVH, cvh)
```

Arguments

X	Set of data points (one sample per row)
w	Vector with weights for X ($\sum(w)=1$)
ACVH	Matrix where each row constitutes the normal vector of a face of $\text{conv}(X)$
bCVH	Vector where each entry constitutes the intercept for a face of $\text{conv}(X)$
cvh	Matrix where each row is a set of indices of points in X describing one face of $\text{conv}(X)$

Value

A list containing the description of the upper convex hull of $(X, \log(y))$ in term of hyperplane parameters:

a	A matrix where each row constitutes a hyperplane normal
b	A vector where each entry constitutes the intercept of a hyperplane

Note the difference

Examples

```
# draw samples from normal distribution
X <- matrix(rnorm(200), 100, 2)
# calculate parameters of convex hull of X
r <- calcCvxHullFaces(X)
# find initial hyperplane parameters based on a smooth log-concave density
params <- paramFitGammaOne(X, rep(1 / nrow(X), nrow(X)), r$ACVH, r$bCVH, r$cvh)
```

paramFitKernelDensity *Parameter Initialization Based on a Kernel Density*

Description

paramFitKernelDensity first fits a kernel density to a sample X with weight vector w . It then calculates the parameters of the piecewise linear function defined to be the upper convex hull of $(X, \log(y))$.

Usage

```
paramFitKernelDensity(X, w, cvh, h = apply(X, 2, sd) * n^(-1/(d + 4)))
```

Arguments

X	Set of data points (one sample per row)
w	Vector with weights for X ($\text{sum}(w) == 1$)
cvh	Matrix where each row is a set of indices of points in X describing one face of $\text{conv}(X)$
h	Scalar parameter that governs the Gaussian kernel

Value

A list containing the description of the upper convex hull of $(X, \log(y))$ in term of hyperplane parameters:

a	A matrix where each row constitutes the normal vector of a face
b	A vector where each entry constitutes the offset of a face

Examples

```
# draw samples from normal distribution
X <- matrix(rnorm(200), 100, 2)
# calculate parameters of convex hull of X
r <- calcCvxHullFaces(X)
# find initial hyperplane parameters based on a kernel density estimator with Gaussian kernel
params <- paramFitKernelDensity(X, rep(1 / nrow(X), nrow(X)), r$cvh)
```

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