Package ‘haldensify’

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Title  Highly Adaptive Lasso Conditional Density Estimation
Version  0.2.3
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Description  An algorithm for flexible conditional density estimation based on application of pooled hazard regression to an artificial repeated measures dataset constructed by discretizing the support of the outcome variable. To facilitate non/semi-parametric estimation of the conditional density, the highly adaptive lasso, a nonparametric regression function shown to reliably estimate a large class of functions at a fast convergence rate, is utilized. The pooled hazards data augmentation formulation implemented was first described by Díaz and van der Laan (2011) <doi:10.2202/1557-4679.1356>. To complement the conditional density estimation utilities, tools for efficient nonparametric inverse probability weighted (IPW) estimation of the causal effects of stochastic shift interventions (modified treatment policies), directly utilizing the density estimation technique for construction of the generalized propensity score, are provided. These IPW estimators utilize undersmoothing (sieve estimation) of the conditional density estimators in order to achieve the non/semi-parametric efficiency bound.

Depends  R (>= 3.2.0)
Imports  stats, utils, dplyr, tibble, ggplot2, data.table, matrixStats, future.apply, assertthat, hal9001 (>= 0.4.1), origami (>= 1.0.3), rsample, rlang, scales, Rdpack
Suggests  testthat, knitr, rmarkdown, stringr, covr, future
License  MIT + file LICENSE
URL  https://github.com/nhejazi/haldensify
BugReports  https://github.com/nhejazi/haldensify/issues
Encoding  UTF-8
VignetteBuilder  knitr
RoxygenNote  7.1.2
RdMacros  Rdpack
NeedsCompilation  no
confint.ipw_haldensify

Confidence Intervals for IPW Estimates of the Causal Effects of Stochastic Shift Interventions

Description

Confidence Intervals for IPW Estimates of the Causal Effects of Stochastic Shift Interventions

Usage

```r
## S3 method for class 'ipw_haldensify'
confint(object, parm = seq_len(object$psi), level = 0.95, ...)
```

Arguments

- **object**: An object of class `ipw_haldensify`, produced by invoking the function `ipw_shift`, for which a confidence interval is to be computed.
- **parm**: A numeric vector indicating indices of `object$est` for which to return confidence intervals.
- **level**: A numeric indicating the nominal level of the confidence interval to be computed.
- **...**: Other arguments. Not currently used.
Details

Compute confidence intervals for estimates produced by \texttt{ipw_shift}.

Value

A named numeric vector containing the parameter estimate from a \texttt{ipw_haldensify} object, along-side lower/upper Wald-style confidence intervals at a specified coverage level.

Examples

```r
# simulate data
n_obs <- 50
W1 <- rbinom(n_obs, 1, 0.6)
W2 <- rbinom(n_obs, 1, 0.2)
A <- rnorm(n_obs, (2 * W1 - W2 - W1 * W2), 2)
Y <- rbinom(n_obs, 1, plogis(3 * A + W1 + W2 - W1 * W2))

# fit the IPW estimator
est_ipw_shift <- ipw_shift(
  W = cbind(W1, W2), A = A, Y = Y,
  delta = 0.5, n_bins = 3L, cv_folds = 2L,
  lambda_seq = exp(seq(-1, -13, length = 1000L)),
  # arguments passed to hal9001::fit_hal()
  max_degree = 1,
  # ...continue arguments for IPW
  undersmooth_type = "gcv"
)
confint(est_ipw_shift)
```

---

cv_haldensify

HAL Conditional Density Estimation in a Cross-validation Fold

Description

HAL Conditional Density Estimation in a Cross-validation Fold

Usage

```r
cv_haldensify(
  fold,
  long_data,
  wts = rep(1, nrow(long_data)),
  lambda_seq = exp(seq(-1, -13, length = 1000L)),
  smoothness_orders = 0L,
  ...
)
```
Arguments

fold Object specifying cross-validation folds as generated by a call to make_folds.
wts A numeric vector of observation-level weights, matching in its length the number of records present in the long format data. Default is to weight all observations equally.
lambda_seq A numeric sequence of values of the regularization parameter of Lasso regression; passed to fit_hal.
smoothness_orders A integer indicating the smoothness of the HAL basis functions; passed to fit_hal. The default is set to zero, for indicator basis functions.
... Additional (optional) arguments of fit_hal that may be used to control fitting of the HAL regression model. Possible choices include use_min, reduce_basis, return_lasso, and return_x_basis, but this list is not exhaustive. Consult the documentation of fit_hal for complete details.

Details

Estimates the conditional density of A|W for a subset of the full set of observations based on the inputted structure of the cross-validation folds. This is a helper function intended to be used to select the optimal value of the penalization parameter for the highly adaptive lasso estimates of the conditional hazard (via cross_validate). The

Value

A list, containing density predictions, observations IDs, observation-level weights, and cross-validation indices for conditional density estimation on a single fold of the overall data.
fit_haldensity

n_bins = round(c(0.5, 1, 1.5, 2) * sqrt(length(A))),
cv_folds = 5L,
lambda_seq = exp(seq(-1, -13, length = 1000L)),
smoothness_orders = 0L,
...
)

Arguments

A The numeric vector of observed values.
W A data.frame, matrix, or similar giving the values of baseline covariates (potential confounders) for the observed units. These make up the conditioning set for the conditional density estimate.
wts A numeric vector of observation-level weights. The default is to weight all observations equally.
grid_type A character indicating the strategy to be used in creating bins along the observed support of A. For bins of equal range, use "equal_range"; consult the documentation of cut_interval for more information. To ensure each bin has the same number of observations, use "equal_mass"; consult the documentation of cut_number for details.
n_bins This numeric value indicates the number(s) of bins into which the support of A is to be divided. As with grid_type, multiple values may be specified, in which case cross-validation will be used to choose the optimal number of bins. The default sets the candidate choices of the number of bins based on heuristics tested in simulation.
cv_folds A numeric indicating the number of cross-validation folds to be used in fitting the sequence of HAL conditional density models.
lambda_seq A numeric sequence of values of the regularization parameter of Lasso regression; passed to fit_hal.
smoothness_orders A integer indicating the smoothness of the HAL basis functions; passed to fit_hal. The default is set to zero, for indicator basis functions.
...
Additional (optional) arguments of fit_hal that may be used to control fitting of the HAL regression model. Possible choices include use_min, reduce_basis, return_lasso, and return_x_basis, but this list is not exhaustive. Consult the documentation of fit_hal for complete details.

Details

Estimation of the conditional density of A|W via a cross-validated highly adaptive lasso, used to estimate the conditional hazard of failure in a given bin over the support of A.

Value

A list, containing density predictions for the sequence of fitted HAL models; the index and value of the L1 regularization parameter minimizing the density loss; and the sequence of empirical risks for the sequence of fitted HAL models.
Examples

```r
# simulate data: W ~ U[-4, 4] and A|W ~ N(mu = W, sd = 0.5)
n_train <- 50
w <- runif(n_train, -4, 4)
a <- rnorm(n_train, w, 0.5)
# fit cross-validated HAL-based density estimator of A|W
haldensify_cvfit <- fit_haldensify(
    A = a, W = w, n_bins = 10L, lambda_seq = exp(seq(-1, -10, length = 100)),
    # the following arguments are passed to hal9001::fit_hal()
    max_degree = 3, reduce_basis = 1 / sqrt(length(a))
)
```

format_long_hazards Generate Augmented (Long Format) Data for Pooled Hazards Regression

Description

Generate Augmented (Long Format) Data for Pooled Hazards Regression

Usage

```r
format_long_hazards(
    A,
    W,
    wts = rep(1, length(A)),
    grid_type = c("equal_range", "equal_mass"),
    n_bins = NULL,
    breaks = NULL
)
```

Arguments

- **A**: The numeric vector or similar of the observed values of an intervention for a group of observational units of interest.
- **W**: A data.frame, matrix, or similar giving the values of baseline covariates (potential confounders) for the observed units whose observed intervention values are provided in the previous argument.
- **wts**: A numeric vector of observation-level weights. The default is to weight all observations equally.
- **grid_type**: A character indicating the strategy (or strategies) to be used in creating bins along the observed support of the intervention A. For bins of equal range, use "equal_range"; consult documentation of cut_interval for more information. To ensure each bin has the same number of points, use "equal_mass"; consult documentation of cut_number for details.
- **n_bins**: Only used if grid_type is set to "equal_range" or "equal_mass". This numeric value indicates the number(s) of bins into which the support of A is to be divided.
breaks A numeric vector of break points to be used in dividing up the support of A. This is passed through the ... argument to cut.default by cut_interval or cut_number.

Details

Generates an augmented (long format, or repeated measures) dataset that includes multiple records for each observation, a single record for each discretized bin up to and including the bin in which a given observed value of A falls. Such bins are derived from selecting break points over the support of A. This repeated measures dataset is suitable for estimating the hazard of failing in a particular bin over A using a highly adaptive lasso (or other) classification model.

Value

A list containing the break points used in dividing the support of A into discrete bins, the length of each bin, and the reformatted data. The reformatted data is a data.table of repeated measures data, with an indicator for which bin an observation falls in, the bin ID, observation ID, values of W for each given observation, and observation-level weights.

Description

Cross-validated HAL Conditional Density Estimation

Usage

```r
haldensify(
  A,
  W,
  wts = rep(1, length(A)),
  grid_type = "equal_range",
  n_bins = round(c(0.5, 1, 1.5, 2) * sqrt(length(A))),
  cv_folds = 5L,
  lambda_seq = exp(seq(-1, -13, length = 1000L)),
  smoothness_orders = 0L,
  hal_basis_list = NULL,
  ...
)
```

Arguments

- `A` The numeric vector observed values.
- `W` A data.frame, matrix, or similar giving the values of baseline covariates (potential confounders) for the observed units. These make up the conditioning set for the density estimate. For estimation of a marginal density, specify a constant numeric vector or NULL.
wts  A numeric vector of observation-level weights. The default is to weight all observations equally.

grid_type  A character indicating the strategy to be used in creating bins along the observed support of A. For bins of equal range, use "equal_range"; consult the documentation of cut_interval for more information. To ensure each bin has the same number of observations, use "equal_mass"; consult the documentation of cut_number for details. The default is "equal_range" since this has been found to provide better performance in simulation experiments; however, both types may be specified (i.e., c("equal_range", "equal_mass")) together, in which case cross-validation will be used to select the optimal binning strategy.

n_bins  This numeric value indicates the number(s) of bins into which the support of A is to be divided. As with grid_type, multiple values may be specified, in which case cross-validation will be used to choose the optimal number of bins. The default sets the candidate choices of the number of bins based on heuristics tested in simulation.

cv_folds  A numeric indicating the number of cross-validation folds to be used in fitting the sequence of HAL conditional density models.

lambda_seq  A numeric sequence of values of the regularization parameter of Lasso regression; passed to fit_hal via its argument lambda.

smoothness_orders  A integer indicating the smoothness of the HAL basis functions; passed to fit_hal. The default is set to zero, for indicator basis functions.

hal_basis_list  A list consisting of a preconstructed set of HAL basis functions, as produced by fit_hal. The default of NULL results in creating such a set of basis functions. When specified, this is passed directly to the HAL model fitted upon the augmented (repeated measures) data structure, resulting in a much lowered computational cost. This is useful, for example, in fitting HAL conditional density estimates with external cross-validation or bootstrap samples.

...  Additional (optional) arguments of fit_hal that may be used to control fitting of the HAL regression model. Possible choices include use_min, reduce_basis, return_lasso, and return_x_basis, but this list is not exhaustive. Consult the documentation of fit_hal for complete details.

Details

Estimation of the conditional density A|W through using the highly adaptive lasso to estimate the conditional hazard of failure in a given bin over the support of A. Cross-validation is used to select the optimal value of the penalization parameters, based on minimization of the weighted log-likelihood loss for a density.

Value

Object of class haldensify, containing a fitted hal9001 object; a vector of break points used in binning A over its support W; sizes of the bins used in each fit; the tuning parameters selected by cross-validation; the full sequence (in lambda) of HAL models for the CV-selected number of bins and binning strategy; and the range of A.
**ipw_shift**

**Note**

Parallel evaluation of the cross-validation procedure to select tuning parameters for density estimation may be invoked via the framework exposed in the `future` ecosystem. Specifically, set `plan` for `future_mapply` to be used internally.

**Examples**

```r
# simulate data: W ~ U[-4, 4] and A|W ~ N(mu = W, sd = 0.5)
set.seed(429153)
n_train <- 50
w <- runif(n_train, -4, 4)
a <- rnorm(n_train, w, 0.5)
# learn relationship A|W using HAL-based density estimation procedure
haldensify_fit <- haldensify(
  A = a, W = w, n_bins = 10L, lambda_seq = exp(seq(-1, -10, length = 100)),
  # the following arguments are passed to hal9001::fit_hal()
  max_degree = 3, reduce_basis = 1 / sqrt(length(a))
)
```

---

**ipw_shift**

*IPW Estimates of the Causal Effects of Stochastic Shift Interventions*

**Description**

IPW Estimates of the Causal Effects of Stochastic Shift Interventions

**Usage**

```r
ipw_shift(
  W,
  A,
  Y,
  delta,
  n_bins = make_bins(A, "hist"),
  cv_folds = 10L,
  lambda_seq,
  ...,
  bin_type = c("equal_range", "equal_mass"),
  trim_density = FALSE,
  undersmooth_type = c("dcar", "plateau", "gcv", "all"),
  bootstrap = FALSE,
  n_boot = 1000L
)
```
Arguments

- **W**: A matrix, data.frame, or similar containing a set of baseline covariates.
- **A**: A numeric vector corresponding to a exposure variable. The parameter of interest is defined as a location shift of this quantity.
- **Y**: A numeric vector of the observed outcomes.
- **delta**: A numeric value indicating the shift in the exposure to be used in defining the target parameter. This is defined with respect to the scale of the exposure (A).
- **n_bins**: A numeric, scalar or vector, indicating the number of bins into which the support of A is to be partitioned for constructing conditional density estimates.
- **cv_folds**: A numeric giving the number of folds to be used for cross-validation. Note that this form of sample splitting is used for the selection of tuning parameters by empirical risk minimization, not for the estimation of nuisance parameters (i.e., to relax regularity conditions).
- **lambda_seq**: A numeric sequence of the regularization parameter (L1 norm of HAL coefficients) to be used in fitting HAL models.
- **...**: Additional arguments for model fitting to be passed directly to `haldensify`.
- **bin_type**: A character indicating the strategy to be used in creating bins along the observed support of A. For bins of equal range, use "equal_range"; to ensure each bin has the same number of observations, use instead "equal_mass". For more information, see documentation of `grid_type` in `haldensify`.
- **trim_density**: A logical indicating whether estimates of the conditional density should be trimmed. Refer to the `trim` argument of the `predict` method of `haldensify` for details. The default is FALSE since propensity score truncation can lead to estimation bias.
- **undersmooth_type**: A character indicating the selection strategy to be used in identifying an efficient IPW estimator. The choices include "gcv" for global cross-validation, "dcar" for solving the IPW representation of the EIF through, and "plateau" for an approach that balances changes in the parameter estimate and its mean squared error, based on Lepski’s method. The option “all” produces results based on all three selection strategies, sharing redundant computation between each.
- **bootstrap**: A logical indicating whether the estimator variance should be approximated using the nonparametric bootstrap. The default is FALSE, in which case the empirical variances of the IPW estimating function and the EIF are used for for estimator selection and for variance estimation, respectively. When set to TRUE, the bootstrap variance is used for both of these purposes instead. Note that the bootstrap is very computationally intensive and scales relatively poorly.
- **n_boot**: A numeric giving the number of bootstrap re-samples to be used in computing the mean squared error as part of the plateau selector criterion. Ignored when `undersmooth_type` is not "plateau".

Examples

```r
# simulate data
```
n.obs <- 50
W1 <- rbinom(n.obs, 1, 0.6)
W2 <- rbinom(n.obs, 1, 0.2)
A <- rnorm(n.obs, (2 * W1 - W2 - W1 * W2), 2)
Y <- rbinom(n.obs, 1, plogis(3 * A + W1 + W2 - W1 * W2))

# fit the IPW estimator
est_ipw_shift <- ipw_shift(
  W = cbind(W1, W2), A = A, Y = Y,
  delta = 0.5, n_bins = 3L, cv_folds = 2L,
  lambda_seq = exp(seq(-1, -10, length = 100L)),
  # arguments passed to hal9001::fit_hal()
  max_degree = 1,
  # ...continue arguments for IPW
  undersmooth_type = "gcv"
)

map_hazard_to_density    Map Predicted Hazard to Predicted Density for a Single Observation

Description
Map Predicted Hazard to Predicted Density for a Single Observation

Usage
map_hazard_to_density(hazard_pred_single_obs)

Arguments
hazard_pred_single_obs
A numeric vector of predicted hazard of failure in a given bin (under a given partitioning of the support) for a single observational unit based on a long format data structure (from format_long_hazards). This is the probability that a given value falls in a corresponding bin, given that it has not yet failed (fallen in a preceding bin), as per Díaz I, van der Laan MJ (2011). “Super learner based conditional density estimation with application to marginal structural models.” International Journal of Biostatistics, 7(1), 1–20..

Details
For a single observation, map a predicted hazard of failure (as an occurrence in a particular bin, under a given partitioning of the support) to a density.

Value
A matrix composed of a single row and a number of columns specified by the grid of penalization parameters used in fitting of the highly adaptive lasso. This is the predicted conditional density for a given observation, re-mapped from the hazard scale.
plot.haldensify

Plot Method for HAL Conditional Density Estimates

Description

Plot Method for HAL Conditional Density Estimates

Usage

## S3 method for class 'haldensify'
plot(x, ..., type = c("risk", "density"))

Arguments

x Object of class haldensify, containing conditional density estimates, as produced by haldensify.

... Additional arguments to be passed plot, currently ignored.

type A character indicating the type of plot to be produced. Options include visualizing the empirical risks of the conditional density estimators across a grid of values of the regularization parameter and a plot of the estimated conditional density (based on the estimator selected by cross-validation). The latter has yet to be implemented.

Value

Object of class ggplot containing a plot of the desired type.

Examples

# simulate data: W ~ U[-4, 4] and A|W ~ N(mu = W, sd = 0.5)
n_train <- 50
w <- runif(n_train, -4, 4)
a <- rnorm(n_train, w, 0.5)
# learn relationship A|W using HAL-based density estimation procedure
haldensify_fit <- haldensify(
  A = a, W = w, n_bins = 3,
  lambda_seq = exp(seq(-1, -10, length = 50)),
  # the following arguments are passed to hal9001::fit_hal()
  max_degree = 3, reduce_basis = 0.1
)
plot(haldensify_fit)
**predict.haldensify**  
*Prediction Method for HAL Conditional Density Estimation*

---

**Description**

Prediction Method for HAL Conditional Density Estimation

**Usage**

```r
# S3 method for class 'haldensify'
predict(
  object,
  ..., 
  new_A,
  new_W,
  trim = TRUE,
  trim_min = NULL,
  lambda_select = c("cv", "undersmooth", "all")
)
```

**Arguments**

- `object`  
  An object of class `haldensify`, containing the results of fitting the highly adaptive lasso for conditional density estimation, as produced by a call to `haldensify`.

- `...`  
  Additional arguments passed to `predict` as necessary.

- `new_A`  
  The numeric vector or similar of the observed values for which a conditional density estimate is to be generated.

- `new_W`  
  A `data.frame`, `matrix`, or similar giving the values of baseline covariates (potential confounders) for the conditioning set of the observed values `A`.

- `trim`  
  A logical indicating whether estimates of the conditional density below the value indicated in `trim_min` should be truncated. The default value of `TRUE` enforces truncation of any values below the cutoff specified in `trim_min` and similarly truncates predictions for any of `new_A` falling outside of the training support.

- `trim_min`  
  A numeric indicating the minimum allowed value of the resultant density predictions. Any predicted density values below this tolerance threshold are set to the indicated minimum. The default is to use a scaled inverse square root of the sample size of the prediction set, i.e., 5/sqrt(n)/log(n) (another notable choice is 1/sqrt(n)). If there are observations in the prediction set with values of `new_A` outside of the support of the training set (i.e., provided in the argument `A` to `haldensify`), their predictions are similarly truncated.

- `lambda_select`  
  A character indicating whether to return the predicted density for the value of the regularization parameter chosen by the global cross-validation selector or whether to return an undersmoothed sequence (which starts with the cross-validation selector’s choice but also includes all values in the sequence that are...
less restrictive). The default is "cv" for the global cross-validation selector. Setting the choice to "undersmooth" returns a matrix of predicted densities, with each column corresponding to a value of the regularization parameter less than or equal to the choice made by the global cross-validation selector. When "all" is set, predictions are returned for the full sequence of the regularization parameter on which the HAL model object was fitted.

Details

Method for computing and extracting predictions of the conditional density estimates based on the highly adaptive lasso estimator, returned as an S3 object of class haldensify from haldensify.

Value

A numeric vector of predicted conditional density values from a fitted haldensify object.

Examples

```r
# simulate data: W ~ U[-4, 4] and A|W ~ N(mu = W, sd = 0.5)
n_train <- 50
w <- runif(n_train, -4, 4)
a <- rnorm(n_train, w, 0.5)
# HAL-based density estimator of A|W
haldensify_fit <- haldensify(
  A = a, W = w, n_bins = 10L, lambda_seq = exp(seq(-1, -10, length = 100)),
  max_degree = 3, reduce_basis = 1 / sqrt(length(a))
)
# predictions to recover conditional density of A|W
new_a <- seq(-4, 4, by = 0.1)
new_w <- rep(0, length(new_a))
pred_dens <- predict(haldensify_fit, new_A = new_a, new_W = new_w)
```

Description

Print: Highly Adaptive Lasso Conditional Density Estimates

Usage

```
## S3 method for class 'haldensify'
print(x, ...)  
```

Arguments

- `x` An object of class haldensify.
- `...` Other options (not currently used).
Details

The print method for objects of class haldensify

Value

None. Called for the side effect of printing an informative summary of slots of objects of class haldensify.

Examples

```r
# simulate data: W ~ U[-4, 4] and A|W ~ N(mu = W, sd = 0.5)
set.seed(429153)
n_train <- 50
w <- runif(n_train, -4, 4)
a <- rnorm(n_train, w, 0.5)

# learn relationship A|W using HAL-based density estimation procedure
haldensify_fit <- haldensify(
  A = a, W = w, n_bins = c(3, 5),
  lambda_seq = exp(seq(-1, -15, length = 50L)),
  max_degree = 3, reduce_basis = 0.1
)
print(haldensify_fit)
```

print.ipw_haldensify

---

**Description**

Print: IPW Estimates of the Causal Effects of Stochastic Shift Interventions

**Usage**

```r
## S3 method for class 'ipw_haldensify'
print(x, ..., ci_level = 0.95)
```

**Arguments**

- `x` An object of class ipw_haldensify.
- `...` Other options (not currently used).
- `ci_level` A numeric indicating the level of the confidence interval to be computed.

**Details**

The print method for objects of class ipw_haldensify
print.ipw_haldensify

Value

None. Called for the side effect of printing an informative summary of slots of objects of class ipw_haldensify.

Examples

```r
# simulate data
n_obs <- 50
W1 <- rbinom(n_obs, 1, 0.6)
W2 <- rbinom(n_obs, 1, 0.2)
A <- rnorm(n_obs, (2 * W1 - W2 - W1 * W2), 2)
Y <- rbinom(n_obs, 1, plogis(3 * A + W1 + W2 - W1 * W2))

# fit the IPW estimator
est_ipw_shift <- ipw_shift(
  W = cbind(W1, W2), A = A, Y = Y,
  delta = 0.5, n_bins = 3L, cv_folds = 2L,
  lambda_seq = exp(seq(-1, -10, length = 100L)),
  # arguments passed to hal9001::fit_hal()
  max_degree = 1,
  # ...continue arguments for IPW
  undersmooth_type = "gcv"
)

print(est_ipw_shift)
```
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