Package ‘investr’

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Type Package
Title Inverse Estimation/Calibration Functions
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Description Functions to facilitate inverse estimation (e.g., calibration) in linear, generalized linear, nonlinear, and (linear) mixed-effects models. A generic function is also provided for plotting fitted regression models with or without confidence/prediction bands that may be of use to the general user. For a general overview of these methods, see Greenwell and Schubert Kabban (2014) <doi:10.32614/RJ-2014-009>.
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R topics documented:

arsenic ......................................................... 2
beetle ......................................................... 2
arsenic  Concentrations of arsenic in water samples

Description

The data give the actual and measured concentrations of arsenic present in water samples.

Format

A data frame with 32 rows and 2 columns.

Details

- actual True amount of arsenic present.
- measured Measured amount of arsenic present.

Source


dobson's beetle data

Description

The data give the number of flour beetles killed after five hour exposure to the insecticide carbon disulphide at eight different concentrations.

Format

A data frame with 8 rows and 3 columns.
Details

- ldose Log dose of carbon disulphide.
- y Number of beetles subjected to insecticide.
- n Number of beetles killed.

Source


---

Bladder volume data

Description

A series of 23 women patients attending a urodynamic clinic were recruited for a study. After successful voiding of the bladder, sterile water was introduced in additions of 10, 15, and then 25 ml increments up to a final cumulative total of 175 ml. At each volume a measure of height (H) in mm and depth (D) in mm of largest ultrasound bladder images were taken. The product $H \times D$ was taken as a measure of liquid volume.

Format

A data frame with 184 rows and 3 columns.

Details

- subject The subject ID.
- $H\times D$ The product $H \times D$ (mm$^2$).
- volume The true volume of sterile water in the bladder (ml).

Source

Calibrate for the simple linear regression model

Description

The function calibrate computes the maximum likelihood estimate and a confidence interval for the unknown predictor value that corresponds to an observed value of the response (or vector thereof) or specified value of the mean response. See the reference listed below for more details.

Usage

```r
calibrate(object, ...)  
## Default S3 method:  
calibrate(  
  object,  
  y0,  
  interval = c("inversion", "Wald", "none"),  
  level = 0.95,  
  mean.response = FALSE,  
  adjust = c("none", "Bonferroni", "Scheffe"),  
  k,  
  ...  
)

calibrate(formula, data = NULL, ..., subset, na.action = stats::na.fail)

calibrate(  
  object,  
  y0,  
  interval = c("inversion", "Wald", "none"),  
  level = 0.95,  
  mean.response = FALSE,  
  adjust = c("none", "Bonferroni", "Scheffe"),  
  k,  
  ...  
)
```

Arguments

- `object` A matrix, list, data frame, or object that inherits from class `lm`.
- `...` Additional optional arguments. At present, no optional arguments are used.
- `y0` The value of the observed response(s) or specified value of the mean response.
- `interval` The method to use for forming a confidence interval.
calibrate

level A numeric scalar between 0 and 1 giving the confidence level for the interval to be calculated.

mean.response Logical indicating whether confidence intervals should correspond to an observed response(s) (FALSE) or a specified value of the mean response (TRUE). Default is FALSE.

adjust A logical value indicating if an adjustment should be made to the critical value used in constructing the confidence interval. This useful when the calibration curve is to be used \( k > 0 \) times.

k The number of times the calibration curve is to be used for computing a confidence interval. Only needed when \( \text{adjust} = \text{TRUE} \).

formula A formula of the form \( y \sim x \).

data an optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which \( \text{lm} \) was called.

subset An optional vector specifying a subset of observations to be used in the fitting process.

na.action a function which indicates what should happen when the data contain NAs.

Value

An object of class "invest" containing the following components:

- \text{estimate} The estimate of \( x_0 \).
- \text{lower} The lower confidence limit for \( x_0 \).
- \text{upper} The upper confidence limit for \( x_0 \).
- \text{se} An estimate of the standard error (Wald interval only).
- \text{interval} The method used for calculating lower and upper (only used by \text{print} method).

Note

The \text{invest} function is more general, but is based on numerical techniques to find the solution. When the underlying model is that of the simple linear regression model with normal errors, closed-form expressions exist which are utilized by the \text{calibrate} function.

References


Examples

# Arsenic example (simple linear regression with replication)
#
# Inverting a prediction interval for an individual response
arsenic.lm <- stats::lm(measured ~ actual, data = arsenic)
plotFit(arsenic.lm, interval = "prediction", shade = TRUE,
       col.pred = "lightblue")
(cal <- calibrate(arsenic.lm, y0 = 3, interval = "inversion"))
abline(h = 3)
segments(cal$estimate, 3, cal$estimate, par()$usr[3])
arrows(cal$lower, 3, cal$lower, par()$usr[3])
arrows(cal$upper, 3, cal$upper, par()$usr[3])

# Crystal weight example (simple linear regression)
#
# Inverting a confidence interval for the mean response
crystal.lm <- stats::lm(weight ~ time, data = crystal)
plotFit(crystal.lm, interval = "confidence", shade = TRUE,
        col.conf = "lightblue")
(cal <- calibrate(crystal.lm, y0 = 8, interval = "inversion",
                 mean.response = TRUE))
abline(h = 8)
segments(cal$estimate, 8, cal$estimate, par()$usr[3])
arrows(cal$lower, 8, cal$lower, par()$usr[3])
arrows(cal$upper, 8, cal$upper, par()$usr[3])

# Wald interval and approximate standard error based on the delta method
calibrate(crystal.lm, y0 = 8, interval = "Wald", mean.response = TRUE)

---

crystal

Crystal weight data

Description

The data give the growing time and final weight of crystals.

Format

A data frame with 14 rows and 2 columns.

Details

- time Time taken to grow (hours).
- weight Final weight of the crystal (grams).
**Source**


---

**Description**

Provides point and interval estimates for the unknown predictor value that corresponds to an observed value of the response (or vector thereof) or specified value of the mean response. See the references listed below for more details.

**Usage**

```r
invest(object, y0, ...)
```

```r
## S3 method for class 'lm'
invest(
  object,
  y0,
  interval = c("inversion", "Wald", "percentile", "none"),
  level = 0.95,
  mean.response = FALSE,
  x0.name,
  newdata,
  data,
  boot.type = c("parametric", "nonparametric"),
  nsim = 999,
  seed = NULL,
  progress = FALSE,
  lower,
  upper,
  extendInt = "no",
  tol = .Machine$double.eps^0.25,
  maxiter = 1000,
  adjust = c("none", "Bonferroni"),
  k,
  ...
)
```

```r
## S3 method for class 'glm'
invest(
  object,
  y0,
  interval = c("inversion", "Wald", "percentile", "none"),
  ...}
```
level = 0.95,
lower,
upper,
_x0_.name,
newdata,
data,
extendInt = "no",
tol = .Machine$double.eps^0.25,
maxiter = 1000,
...
)

## S3 method for class 'nls'
invest(
  object,
y0,
interval = c("inversion", "Wald", "percentile", "none"),
level = 0.95,
mean.response = FALSE,
data,
boot.type = c("parametric", "nonparametric"),
nsim = 1,
seed = NULL,
progress = FALSE,
lower,
upper,
extendInt = "no",
tol = .Machine$double.eps^0.25,
maxiter = 1000,
adjust = c("none", "Bonferroni"),
k,
...
)

## S3 method for class 'lme'
invest(
  object,
y0,
interval = c("inversion", "Wald", "percentile", "none"),
level = 0.95,
mean.response = FALSE,
data,
lower,
upper,
q1,
q2,
extendInt = "no",
tol = .Machine$double.eps^0.25,
maxiter = 1000,
...
)

Arguments

object An object that inherits from class `lm`, `glm`, `nls`, or `lme`.
y0 The value of the observed response(s) or specified value of the mean response. For `glm` objects, y0 should be on the scale of the response variable (e.g., a number between 0 and 1 for binomial families).
... Additional optional arguments. At present, no optional arguments are used.
interval The type of interval required.
level A numeric scalar between 0 and 1 giving the confidence level for the interval to be calculated.
mean.response Logical indicating whether confidence intervals should correspond to an individual response (FALSE) or a mean response (TRUE). For `glm` objects, this is always TRUE.
x0.name For multiple linear regression, a character string giving the name of the predictor variable of interest.
newdata For multiple linear regression, a `data.frame` giving the values of interest for all other predictor variables (i.e., those other than x0.name).
data An optional data frame. This is required if object$data is NULL.
boot.type Character string specifying the type of bootstrap to use when interval = "percentile". Options are "parametric" and "nonparametric".
nsim Positive integer specifying the number of bootstrap simulations; the bootstrap B (or R).
seed Optional argument to `set.seed`.
progress Logical indicating whether to display a text-based progress bar during the bootstrap simulation.
lower The lower endpoint of the interval to be searched.
upper The upper endpoint of the interval to be searched.
extendInt Character string specifying if the interval c(lower,upper) should be extended or directly produce an error when the inverse of the prediction function does not have differing signs at the endpoints. The default, "no", keeps the search interval and hence produces an error. Can be abbreviated. See the documentation for the base R function `uniroot` for details.
tol The desired accuracy passed on to `uniroot`. Recommend a minimum of 1e-10.
maxiter The maximum number of iterations passed on to `uniroot`.
adjust A logical value indicating if an adjustment should be made to the critical value used in calculating the confidence interval. This is useful for when the calibration curve is to be used multiple, say k, times.
k The number times the calibration curve is to be used for computing a confidence interval. Only needed when adjust = "Bonferroni".
Optional lower cutoff to be used in forming confidence intervals. Only used when object inherits from class `lme`. Defaults to `stats::qnorm((1+level)/2)`.

Optional upper cutoff to be used in forming confidence intervals. Only used when object inherits from class `lme`. Defaults to `stats::qnorm((1-level)/2)`.

Value

Returns an object of class "invest" or, if `interval = "percentile"`, of class `c("invest","bootCal")`. The generic function `{plot}` can be used to plot the output of the bootstrap simulation when `interval = "percentile"`.

An object of class "invest" containing the following components:

- **estimate** The estimate of x0.
- **lwr** The lower confidence limit for x0.
- **upr** The upper confidence limit for x0.
- **se** An estimate of the standard error (Wald and percentile intervals only).
- **bias** The bootstrap estimate of bias (percentile interval only).
- **bootreps** Vector of bootstrap replicates (percentile interval only).
- **nsim** The number of bootstrap replicates (percentile interval only).
- **interval** The method used for calculating lower and upper (only used by `{print}` method).

References


Examples

```r
# Dobson's beetle data (generalized linear model)
#
# Complementary log-log model
mod <- glm(cbind(y, n-y) ~ ldose, data = beetle,
           family = binomial(link = "cloglog"))
```
plotFit(mod, pch = 19, cex = 1.2, lwd = 2,
       xlab = "Log dose of carbon disulphide",
       interval = "confidence", shade = TRUE,
       col.conf = "lightskyblue")

# Approximate 95% confidence intervals and standard error for LD50
invest(mod, y0 = 0.5)
invest(mod, y0 = 0.5, interval = "Wald")

# Nasturtium example (nonlinear least-squares with replication)
#
# Log-logistic model
mod <- nls(weight ~ theta1/(1 + exp(theta2 + theta3 * log(conc)));
           start = list(theta1 = 1000, theta2 = -1, theta3 = 1),
           data = nasturtium)
plotFit(mod, lwd.fit = 2)

# Compute approximate 95% calibration intervals
invest(mod, y0 = c(309, 296, 419), interval = "inversion")
invest(mod, y0 = c(309, 296, 419), interval = "Wald")

# Bootstrap calibration intervals. In general, nsim should be as large as
# reasonably possible (say, nsim = 9999).
boo <- invest(mod, y0 = c(309, 296, 419), interval = "percentile",
              nsim = 300, seed = 101)
boo # print bootstrap summary
plot(boo) # plot results

# Bladder volume example (random coefficient model)
#
# Load required packages
library(nlme)

# Plot data
plot(HD^(3/2) ~ volume, data = bladder, pch = 19,
     col = adjustcolor("black", alpha.f = 0.5))

# Fit a random intercept and slope model
bladder <- na.omit(bladder)
ris <- lme(HD^(3/2) ~ volume, data = bladder, random = ~volume|subject)
invest(ris, y0 = 500)
invest(ris, y0 = 500, interval = "Wald")
Description
Inverse estimation, also referred to as the calibration problem, is a classical and well-known problem in regression. In simple terms, it involves the use of an observed value of the response (or specified value of the mean response) to make inference on the corresponding unknown value of the explanatory variable.

Details
A detailed introduction to investr has been published in The R Journal: "investr: An R Package for Inverse Estimation." You can track development at https://github.com/bgreenwell/investr. To report bugs or issues, contact the main author directly or submit them to https://github.com/bgreenwell/investr/issues.

As of right now, investr supports (univariate) inverse estimation with objects of class:

- lm — linear models (multiple predictor variables allowed)
- glm — generalized linear models (multiple predictor variables allowed)
- nls — nonlinear least-squares models
- lme — linear mixed-effects models (fit using the nlme package)

Bioassay on Nasturtium

Description
The data give the actual concentrations of an agrochemical present in soil samples versus the weight of the plant after three weeks of growth.

Format
A data frame with 42 rows and 2 columns.

Details
- conc True concentration of agrochemical (g/ha).
- weight Weight of plant (mg) after 3 weeks’ growth.

Source

References
**plot.bootCal**  
*Plots method for bootstrap calibration*

**Description**

The `plot` method for "bootCal" objects. In particular, this method takes a "bootCal" object and produces plots for the bootstrap replicates of the inverse estimate.

**Usage**

```r
## S3 method for class 'bootCal'
plot(x, ...)  
```

**Arguments**

- `x`  
  An object that inherits from class "bootCal".
- `...`  
  Additional optional arguments. At present, no optional arguments are used.

**Value**

`x` is returned invisibly.

---

**plotFit**  
*Plotting fitted models*

**Description**

Generic function for plotting predictions from various types of fitted models. `plotFit` currently supports objects of class `lm`, `glm`, and `nls`. A default method also exists which may be used for plotting the fitted mean response from other model fits (e.g., `lqs` and `rlm` from the `MASS` package).

**Usage**

```r
plotFit(object, ...)  
```

**## Default S3 method:**

```r
plotFit(
   object,
   type = c("response", "link"),
   interval = c("none", "both", "confidence", "prediction"),
   level = 0.95,
   data,
   adjust = c("none", "Bonferroni", "Scheffe"),
   k,
   ...,
)
```

---
```r
shade = FALSE,
extend.range = FALSE,
hide = TRUE,
col.conf = if (shade) grDevices::grey(0.7) else "black",
col.pred = if (shade) grDevices::grey(0.9) else "black",
border.conf = col.conf,
border.pred = col.pred,
col.fit = "black",
lty.conf = if (shade) 1 else 2,
lty.pred = if (shade) 1 else 3,
lty.fit = 1,
lwd.conf = 1,
lwd.pred = 1,
lwd.fit = 1,
n = 500,
xlab,
ylab,
xlim,
ylim
)
```

**Arguments**

- **object**: A fitted model object. Typically, an object that inherits from class `lm`, `glm`, or `nls` (but others may work too).
- **...**: Additional optional arguments passed on to `plot`.
- **type**: The type of prediction required. The default is on the scale of the response variable; the alternative "link" is on the scale of the linear predictor. This option is only used when plotting `glm` objects.
- **interval**: A character string indicating if a prediction band, confidence band, both, or none should be plotted.
- **level**: The desired confidence level.
- **data**: An optional data frame containing the variables in the model.
- **adjust**: A character string indicating the type of adjustment (if any) to make to the confidence/prediction bands.
- **k**: An integer to be used in computing the critical value for the confidence/prediction bands. Only needed when adjust = "Bonferroni", or when adjust = "Scheffe" and interval = "prediction".
- **shade**: A logical value indicating if the band should be shaded.
- **extend.range**: A logical value indicating if the fitted regression line and bands (if any) should extend to the edges of the plot. Default is FALSE.
- **hide**: A logical value indicating if the fitted model should be plotted on top of the points (FALSE) or behind them (TRUE). Default is TRUE.
- **col.conf**: Shade color for confidence band.
- **col.pred**: Shade color for prediction band.
plotFit

border.conf  The color to use for the confidence band border.
border.pred  The color to use for the prediction band border.
col.fit       The color to use for the fitted line.
lty.conf      Line type to use for confidence band border.
lty.pred      Line type to use for prediction band border.
lty.fit       Line type to use for the fitted regression line.
lwd.conf      Line width to use for confidence band border.
lwd.pred      Line width to use for prediction band border.
lwd.fit       Line width to use for the fitted regression line.
n            The number of predictor values at which to evaluate the fitted model (larger gives a smoother plot).
xlab          A title for the x axis.
ylab          A title for the y axis.
xlim          The x limits (x1, x2) of the plot.
ylim          The y limits (y1, y2) of the plot.

Value

No return value (called for side effects).

Note

By default, the plotted intervals are unadjusted (i.e., pointwise) intervals. For simultaneous intervals, use adjust = "Bonferroni" or adjust = "Scheffe". For the Bonferroni adjustment, you must specify a value for k, the number of intervals for which the coverage is to hold simultaneously. For the Scheffe adjustment, specifying a value for k is only required when interval = "prediction"; if interval = "confidence", k is set equal to p, the number of regression parameters. For example, if object is a simple linear regression model, then calling plotFit with interval = "confidence" and adjust = "Scheffe" will plot the Working-Hotelling band.

Confidence/prediction bands for nonlinear regression (i.e., objects of class nls) are based on the linear approximation described in Bates & Watts (2007).

References


See Also

plotfit
Examples

# A nonlinear least squares example (see ?datasets::Puromycin and
# ?investr::predFit)
data(Puromycin, package = "datasets")
Puromycin2 <- Puromycin[Puromycin$state == "treated", ][, 1:2]
Puro.nls <- nls(rate ~ Vm * conc/(K + conc), data = Puromycin2,
start = c(Vm = 200, K = 0.05))
plotFit(Puro.nls, interval = "both", pch = 19, shade = TRUE,
col.conf = "skyblue4", col.pred = "lightskyblue2")

---

predFit predictions from a Fitted Model

Description

Generic prediction method for various types of fitted models. predFit can be used to obtain standard errors of fitted values and adjusted/unadjusted confidence/prediction intervals for objects of class "lm", "nls", and "glm".

Usage

predFit(object, ...)

## Default S3 method:
predFit(object, ...)

## S3 method for class 'lm'
predFit(
  object,
  newdata,
  se.fit = FALSE,
  interval = c("none", "confidence", "prediction"),
  level = 0.95,
  adjust = c("none", "Bonferroni", "Scheffe"),
  k,
  ...)

## S3 method for class 'glm'
predFit(
  object,
  newdata,
  type = c("link", "response"),
  se.fit = FALSE,
  interval = c("none", "confidence"),
  level = 0.95,
  ...
## S3 method for class 'nls'
predFit(
  object,
  newdata,
  se.fit = FALSE,
  interval = c("none", "confidence", "prediction"),
  level = 0.95,
  adjust = c("none", "Bonferroni", "Scheffe"),
  k,
  ...
)

## S3 method for class 'lme'
predFit(object, newdata, se.fit = FALSE, ...)

### Arguments

**object**  
An object that inherits from class "lm", "glm", "nls", or "lme".

**...**  
Additional optional arguments. At present, no optional arguments are used.

**newdata**  
An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.

**se.fit**  
A logical value indicating if standard errors are required. Default is FALSE.

**interval**  
Type of interval to be calculated. Can be one of "none" (default), "confidence", or "prediction". Default is "none".

**level**  
A numeric scalar between 0 and 1 giving the confidence level for the intervals (if any) to be calculated. Default is 0.95.

**adjust**  
A logical value indicating if an adjustment should be made to the critical value used in calculating the confidence interval. This is useful for when the calibration curve is to be used multiple, say k, times. Default is FALSE.

**k**  
The number times the calibration curve is to be used for computing a confidence/prediction interval. Only needed when adjust = "Bonferroni".

**type**  
Character string specifying the type of prediction. Current options are type = "link" (the default) and type = "response".

### Details

Confidence and prediction intervals for linear models (i.e., "lm" objects) are obtained according to the usual formulas. Nonlinear and generalized linear models (i.e., "nls" and "glm" objects), on the other hand, rely on Taylor-series approximations for the standard errors used in forming the intervals. Approximate standard errors for the fitted values in linear mixed-effects models (i.e., "lme" objects) can also be computed; however, these rely on the approximate variance-covariance matrix of the fixed-effects estimates and often underestimate the true standard error. More accurate standard errors can be obtained using the parametric bootstrap; see bootMer for details.

For linear and nonlinear models, it is possible to request adjusted confidence or prediction intervals using the Bonferroni method (adjust = "Bonferroni") or Scheffe’s method (adjust = "Scheffe").
"Scheffe"). For the Bonferroni adjustment, you must specify a value for k, the number of intervals for which the coverage is to hold simultaneously. For the Scheffe adjustment, specifying a value for k is only required when interval = "prediction"; if interval = "confidence", k is set equal to p, the number of regression parameters. For example, calling plotFit on "lm" objects with interval = "confidence" and adjust = "Scheffe" will plot the Working-Hotelling band.

Value

If se.fit = FALSE, then predFit() returns a vector of predictions or a matrix of predictions and bounds with column names fit, lwr, and upr if interval is not "none". (This function is more so meant for internal use.)

If se.fit = TRUE, then a list with the following components is returned:

- fit a vector or matrix as described above;
- se.fit a vector containing the standard errors of the predicted means;
- residual.scale the residual standard deviations;
- df the residual degrees of freedom.

Examples

# A linear regression example (see ?datasets::cars)
cars.lm <- lm(dist ~ speed + I(speed^2), data = cars)
predFit(cars.lm, interval = "confidence")

# A nonlinear least squares example (see ?datasets::Puromycin)
data(Puromycin, package = "datasets")
Puromycin2 <- Puromycin[Puromycin$state == "treated", ][, 1:2]
Puro.nls <- nls(rate ~ Vm * conc/(K + conc), data = Puromycin2,
start = c(Vm = 200, K = 0.05))
conc <- seq(from = 0.02, to = 1.10, length = 101)
pred <- predFit(Puro.nls, newdata = data.frame(conc), interval = "prediction")
plot(Puromycin2, ylim = c(min(pred[, "lwr"]), max(pred[, "upr"])))
lines(conc, pred[, "fit"], lwd = 2)
lines(conc, pred[, "lwr"], lty = 2)
lines(conc, pred[, "upr"], lty = 2)

whisky

<table>
<thead>
<tr>
<th>Whisky data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Description</td>
</tr>
<tr>
<td>The data give the proof (measured as twice the percentage of alcohol by volume, denoted 2ABV) of whiskey stored in a charred oak barrel against time in years.</td>
</tr>
<tr>
<td>Format</td>
</tr>
<tr>
<td>A data frame with 10 rows and 2 columns.</td>
</tr>
</tbody>
</table>
Details

- age The age of the whisky (years).
- proof The proof of the whisky (2ABV).

Source

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