

Package ‘lefko3’

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Type Package

Title Historical and Ahistorical Population Projection Matrix Analysis

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Description Creates matrix population models for use in population ecological analyses. Specializes on the construction of historical matrices, which are 2d matrices comprising 3 time intervals of demographic information. Estimates both raw and function-based forms of historical and standard ahistorical matrices. Methodology based on Ehrlen (2000) <doi:10.1890/0012-9658(2000)081[1675:TDOPPD]2.0.CO;2>.

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License GPL (>= 2)

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Author Richard P. Shefferson [aut, cre]
(<<https://orcid.org/0000-0002-5234-3131>>),
Johan Ehrlen [aut] (<<https://orcid.org/0000-0001-8539-8967>>)

Maintainer Richard P. Shefferson <cdorm@e.ecc.u-tokyo.ac.jp>

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R topics documented:

cypdata	2
cypvert	4
flefko2	6
flefko3	11
historicalize3	16
lambda3	22
lambda3.lefkoMat	24
lambda3.matrix	25
lathyrus	27
lefko3	29
lmean	30
modelsearch	32
overwrite	37
repvalue3	39
repvalue3.lefkoMat	41
repvalue3.matrix	42
rlefko2	44
rlefko3	47
sf_create	51
stablestage3	53
stablestage3.lefkoMat	55
stablestage3.matrix	57
summary.lefkoMat	58
summary.lefkoMod	59
verticalize3	61
Index	67

cypdata	<i>Demographic Dataset of Cypripedium candidum Population, in Horizontal Format</i>
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Description

A dataset containing the states and fates of *Cypripedium candidum* (white lady’s slipper orchids), family Orchidaceae, from a population in Illinois, USA, resulting from monitoring that occurred annually between 2004 and 2009.

Usage

data(cypdata)

Format

A data frame with 77 individuals and 27 variables. Each row corresponds to an unique individual, and each variable from size.04 on refers to the state of the individual in a particular year.

plantid A numeric variable giving a unique number to each individual.

patch A variable referring to patch within the population.

sensor A variable coding for whether the data point is valid. An entry of 1 means that it is so.

Inf2.04 Number of double inflorescences in 2004.

Inf.04 Number of inflorescences in 2004.

Veg.04 Number of stems without inflorescences in 2004.

Pod.04 Number of fruits in 2004.

Inf2.05 Number of double inflorescences in 2005.

Inf.05 Number of inflorescences in 2005.

Veg.05 Number of stems without inflorescences in 2005.

Pod.05 Number of fruits in 2005.

Inf2.06 Number of double inflorescences in 2006.

Inf.06 Number of inflorescences in 2006.

Veg.06 Number of stems without inflorescences in 2006.

Pod.06 Number of fruits in 2006.

Inf2.07 Number of double inflorescences in 2007.

Inf.07 Number of inflorescences in 2007.

Veg.07 Number of stems without inflorescences in 2007.

Pod.07 Number of fruits in 2007.

Inf2.08 Number of double inflorescences in 2008.

Inf.08 Number of inflorescences in 2008.

Veg.08 Number of stems without inflorescences in 2008.

Pod.08 Number of fruits in 2008.

Inf2.09 Number of double inflorescences in 2009.

Inf.09 Number of inflorescences in 2009.

Veg.09 Number of stems without inflorescences in 2009.

Pod.09 Number of fruits in 2009.

Source

Shefferson, R.P., R. Mizuta, and M.J. Hutchings. 2017. Predicting evolution in response to climate change: the example of sprouting probability in three dormancy-prone orchid species. *Royal Society Open Science* 4(1):160647.

Examples

```

data(cypdata)

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm",
                 "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
                         repstatus = repvector, obsstatus = obsvector,
                         matstatus = matvector, propstatus = propvector,
                         immstatus = immvector, indataset = indataset,
                         binhalfwidth = binvec)

cypraw_v1 <- verticalize3(data = cypdata, noyears = 6, firstyear = 2004,
                        patchidcol = "patch", individcol = "plantid",
                        blocksize = 4, size1col = "Inf2.04", size2col = "Inf.04",
                        size3col = "Veg.04", repstr1col = "Inf.04",
                        repstr2col = "Inf2.04", fec1col = "Pod.04",
                        stageassign = cypframe_raw, stagesize = "sizeadded",
                        NAas0 = TRUE, NRasRep = TRUE)

rep_cyp_raw <- matrix(0, 11, 11)
rep_cyp_raw[1:2,7:11] <- 0.5

cypover2r <- overwrite(stage3 = c("SD", "P1", "P2", "P3", "SL", "SL", "D",
                                   "XSm", "Sm"), stage2 = c("SD", "SD", "P1", "P2", "P3",
                                   "SL", "SL", "SL", "SL"), eststage3 = c(NA, NA, NA, NA,
                                   NA, NA, "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA, NA,
                                   NA, NA, "XSm", "XSm", "XSm"), givenrate = c(0.1, 0.2,
                                   0.2, 0.2, 0.25, 0.4, NA, NA, NA), type = c("S", "S", "S",
                                   "S", "S", "S", "S", "S"))

cypmatrix2r <- rlefk2(data = cypraw_v1, stageframe = cypframe_raw, year = "all",
                    patch = "all", stages = c("stage3", "stage2"),
                    size = c("size3added", "size2added"),
                    repmatrix = rep_cyp_raw, overwrite = cypover2r,
                    yearcol = "year2", patchcol = "patchid",
                    indivcol = "indiv")

cypmatrix2r$A[[1]]

```

Description

A dataset containing the states and fates of *Cypripedium candidum* (white lady's slipper orchids), family Orchidaceae, from a population in Illinois, USA, resulting from monitoring that occurred annually between 2004 and 2009. Same dataset as cypdata, but arranged in an ahistorical vertical format.

Usage

```
data(cypvert)
```

Format

A data frame with 77 individuals, 331 rows, and 12 variables. Each row corresponds to a specific two-year transition for a specific individual. Variable codes are similar to those for cypdata, but use .2 to identify time t and .3 to identify time $t+1$.

plantid A numeric variable giving a unique number to each individual.

patch A variable referring to patch within the population.

sensor A variable coding for whether the data point is valid. An entry of 1 means that it is so.

year2 Year in time t .

Inf2.2 Number of double inflorescences in time t .

Inf.2 Number of inflorescences in time t .

Veg.2 Number of stems without inflorescences in time t .

Pod.2 Number of fruits in time t .

Inf2.3 Number of double inflorescences in time $t+1$.

Inf.3 Number of inflorescences in time $t+1$.

Veg.3 Number of stems without inflorescences in time $t+1$.

Pod.3 Number of fruits in time $t+1$.

Source

Shefferson, R.P., R. Mizuta, and M.J. Hutchings. 2017. Predicting evolution in response to climate change: the example of sprouting probability in three dormancy-prone orchid species. *Royal Society Open Science* 4(1):160647.

Examples

```
data(cypvert)
```

```
sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm", "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
```

```

indataset <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
  repstatus = repvector, obsstatus = obsvector,
  matstatus = matvector, propstatus = propvector,
  immstatus = immvector, indataset = indataset,
  binhalfwidth = binvec)

cypframe_raw

cypraw_v2 <- historicalize3(data = cypvert, patchidcol = "patch", individcol = "plantid",
  year2col = "year2", sizea2col = "Inf2.2", sizea3col = "Inf2.3",
  sizeb2col = "Inf.2", sizeb3col = "Inf.3", sizec2col = "Veg.2",
  sizec3col = "Veg.3", repstra2col = "Inf2.2", repstra3col = "Inf2.3",
  repstrb2col = "Inf.2", repstrb3col = "Inf.3", fec2col = "Pod.2",
  fec3col = "Pod.3", repstrrel = 2, stageassign = cypframe_raw,
  stagesize = "sizeadded", censorcol = "censor", censor = FALSE,
  NAas0 = TRUE, NRasRep = TRUE, reduce = TRUE)

summary(cypraw_v2)

```

fleeko2

Create Function-based Ahistorical Population Projection Matrices

Description

Function `fleeko2()` returns a list of ahistorical population projection matrices corresponding to the patches and years given, as well as the associated component transition and fecundity matrices, a data frame detailing the characteristics of ahistorical stages, and a data frame characterizing the patch and year combinations corresponding to these matrices. Note that, unlike `rlfeko2()`, this function currently does not currently distinguish populations.

Usage

```

fleeko2(
  year = "all",
  patch = "all",
  stageframe,
  repmatrix = NA,
  data = NA,
  modelsuite = NA,
  surv_model = NA,
  obs_model = NA,
  size_model = NA,
  repst_model = NA,
  fec_model = NA,
  jsurv_model = NA,
  jobs_model = NA,

```

```

    jsize_model = NA,
    jrepst_model = NA,
    paramnames = NA,
    surv_dev = 0,
    obs_dev = 0,
    size_dev = 0,
    repst_dev = 0,
    fec_dev = 0,
    jsurv_dev = 0,
    jobs_dev = 0,
    jsize_dev = 0,
    jrepst_dev = 0,
    repmod = 1,
    overwrite = NA,
    yearcol = NA,
    patchcol = NA,
    year.as.random = FALSE,
    patch.as.random = FALSE,
    randomseed = 0,
    negfec = FALSE,
    reduce = FALSE
  )

```

Arguments

year	A variable corresponding to year or observation time, or a set of such values, given in values associated with the year term used in linear model development. Can also equal <code>all</code> , in which case matrices will be estimated for all years. Defaults to <code>all</code> .
patch	A variable designating which patches or subpopulations will have matrices estimated. Should be set to specific patch names, or to <code>"all"</code> if all patches should have matrices estimated. Defaults to <code>all</code> .
stageframe	A stageframe object that includes information on the size, observation status, propagule status, immaturity status, and maturity status of each ahistorical stage. Should also incorporate bin widths if size is continuous.
repmatrix	A matrix composed mostly of 0s, with non-zero values for each potentially new individual (row) born to each reproductive stage (column). Non-zero entries correspond to multipliers for fecundity, with 1 equaling full fecundity.
data	The original historical demographic data frame used to estimate vital rates (class <code>hfvdata</code>). The original data frame is required in order to initialize years and patches properly.
modelsuite	An optional suite of models of class <code>lefkMod</code> . If given, then <code>surv_model</code> , <code>obs_model</code> , <code>size_model</code> , <code>repst_model</code> , <code>fec_model</code> , <code>paramnames</code> , <code>yearcol</code> , and <code>patchcol</code> are not required. Note that the modeling exercise used to develop the models must have tested only the impact of time t for this to work properly.

surv_model	A linear model predicting survival probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any survival probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
obs_model	A linear model predicting sprouting or observation probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any observation probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
size_model	A linear model predicting size. This can be a model of class <code>glm</code> or <code>glmer</code> , both of which require a predicted poisson variable under a log link, or a model of class <code>lm</code> or <code>lmer</code> , in which a Gaussian response is assumed. If given, then will overwrite any size model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
repst_model	A linear model predicting reproduction probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any reproduction probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
fec_model	A linear model predicting fecundity. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted poisson variable under a log link. If given, then will overwrite any fecundity model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
jsurv_model	A linear model predicting juvenile survival probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any juvenile survival probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
jobs_model	A linear model predicting juvenile sprouting or observation probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any juvenile observation probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
jsize_model	A linear model predicting juvenile size. This can be a model of class <code>glm</code> or <code>glmer</code> , both of which require a predicted poisson variable under a log link, or a model of class <code>lm</code> or <code>lmer</code> , in which a Gaussian response is assumed. If given, then will overwrite any juvenile size model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .
jrepst_model	A linear model predicting reproduction probability of a mature individual that was immature in the previous year. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any reproduction probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing only the impacts of time t .

paramnames	A dataframe with two columns, the first showing the general model terms that will be used in matrix creation, and the second showing the equivalent terms used in modeling. Only required if <code>modelsuite</code> is not supplied.
surv_dev	A numeric value to be added to the y-intercept in the linear model for survival probability.
obs_dev	A numeric value to be added to the y-intercept in the linear model for observation probability.
size_dev	A numeric value to be added to the y-intercept in the linear model for size.
repst_dev	A numeric value to be added to the y-intercept in the linear model for probability of reproduction.
fec_dev	A numeric value to be added to the y-intercept in the linear model for fecundity.
jsurv_dev	A numeric value to be added to the y-intercept in the linear model for juvenile survival probability.
jobs_dev	A numeric value to be added to the y-intercept in the linear model for juvenile observation probability.
jsize_dev	A numeric value to be added to the y-intercept in the linear model for juvenile size.
jrepst_dev	A numeric value to be added to the y-intercept in the linear model for juvenile reproduction probability.
repmo	A scalar multiplier of fecundity. Defaults to 1.
overwrite	A data frame developed with the 'overwrite' function, describing transitions to be overwritten either with given values or with other estimated transitions.
yearcol	The variable name or column number corresponding to year in time t in the dataset. Not needed if a <code>modelsuite</code> is supplied.
patchcol	The variable name or column number corresponding to patch in the dataset. Not needed if a <code>modelsuite</code> is supplied.
year.as.random	A logical term indicating whether coefficients for missing patches within vital rate models should be estimated as random intercepts. Defaults to FALSE, in which case missing time step coefficients are set to 0.
patch.as.random	A logical term indicating whether coefficients for missing patches within vital rate models should be estimated as random intercepts. Defaults to FALSE, in which case missing patch coefficients are set to 0.
randomseed	A numeric value used as a seed to generate random estimates for missing time step and patch coefficients, if either 'year.as.random' or 'patch.as.random' is set to TRUE.
negfec	A logical value denoting whether fecundity values estimated to be negative should be reset to 0. Defaults to FALSE.
reduce	A logical value denoting whether to remove ahistorical stages associated solely with 0 transitions. These are only removed in cases where the associated row and column sums in ALL matrices estimated equal 0. Defaults to FALSE.

Value

If all inputs are properly formatted, then this function will return either an object of class `flefkoMat`. Output includes:

<code>A</code>	A list of full projection matrices in order of sorted patches and years.
<code>U</code>	A list of survival-transition matrices sorted as in <code>A</code> .
<code>F</code>	A list of fecundity matrices sorted as in <code>A</code> .
<code>hstages</code>	Null for ahistorical matrices.
<code>ahstages</code>	A data frame detailing the characteristics of associated ahistorical stages.
<code>labels</code>	A data frame giving the patch and year of each matrix in order. In <code>flefko2()</code> , only one population may be analyzed at once, and so 'pop = NA'.
<code>matrixqc</code>	A short vector describing the number of non-zero elements in <code>U</code> and <code>F</code> matrices, and the number of annual matrices.
<code>modelqc</code>	This is the qc portion of the modelsuite input.

Please note that this function will yield incorrect estimates if the models utilized incorporate state in time $t-1$. Only use models developed testing ahistorical effects.

Examples

```
data(lathyrus)

sizevector <- c(0, 4.6, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9)
stagevector <- c("Sd", "Sd1", "Dorm", "Sz1nr", "Sz2nr", "Sz3nr", "Sz4nr", "Sz5nr",
  "Sz6nr", "Sz7nr", "Sz8nr", "Sz9nr", "Sz1r", "Sz2r", "Sz3r", "Sz4r",
  "Sz5r", "Sz6r", "Sz7r", "Sz8r", "Sz9r")
repvector <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1)
obsvector <- c(0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 4.6, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5)

lathframeIn <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvertIn <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "lnVol88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframeIn,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, NAas0 = TRUE, censor = TRUE)
```

```

lathvertln$fece2 <- round(lathvertln$fece2)
lathvertln$fece1 <- round(lathvertln$fece1)
lathvertln$fece3 <- round(lathvertln$fece3)

lathrepmln <- matrix(0, 21, 21)
lathrepmln[1, c(13:21)] <- 0.345
lathrepmln[2, c(13:21)] <- 0.054

lathover2 <- overwrite(stage3 = c("Sd", "Sd1"), stage2 = c("Sd", "Sd"),
                      givenrate = c(0.345, 0.054))

lathmodelsln2 <- modelsearch(lathvertln, historical = FALSE, approach = "lme4", suite = "main",
                           vitalrates = c("surv", "obs", "size", "repst", "fec"),
                           juvestimate = "Sd1", bestfit = "AICc&k", sizedist = "gaussian",
                           fecdist = "poisson", indiv = "indiv", patch = "patchid",
                           year = "year2", year.as.random = TRUE, patch.as.random = TRUE,
                           show.model.tables = TRUE)

lathmat2ln <- flefko2(year = "all", patch = "all", stageframe = lathframeIn,
                    modelsuite = lathmodelsln2, data = lathvertln,
                    repmatrix = lathrepmln, overwrite = lathover2,
                    patchcol = "patchid", yearcol = "year2",
                    year.as.random = FALSE, patch.as.random = FALSE,
                    reduce = FALSE)

summary(lathmat2ln)

```

flefko3

*Create Function-based Historical Population Projection Matrices***Description**

Function `flefko3()` returns a list of historical population projection matrices corresponding to the patches and years given, as well as the associated component transition and fecundity matrices, data frames detailing the characteristics of the ahistorical stages used and the historical stage pairs created, and a data frame characterizing the patch and year combinations corresponding to these matrices. Note that, unlike `rllefko3()`, this function currently does not currently distinguish populations.

Usage

```

flefko3(
  year = "all",
  patch = "all",
  stageframe,

```

```

repmatrix = NA,
data = NA,
modelsuite = NA,
surv_model = NA,
obs_model = NA,
size_model = NA,
repst_model = NA,
fec_model = NA,
jsurv_model = NA,
jobs_model = NA,
jsize_model = NA,
jrepst_model = NA,
paramnames = NA,
surv_dev = 0,
obs_dev = 0,
size_dev = 0,
repst_dev = 0,
fec_dev = 0,
jsurv_dev = 0,
jobs_dev = 0,
jsize_dev = 0,
jrepst_dev = 0,
repmode = 1,
overwrite = NA,
yearcol = NA,
patchcol = NA,
year.as.random = FALSE,
patch.as.random = FALSE,
randomseed = 0,
negfec = FALSE,
reduce = FALSE
)

```

Arguments

year	A variable corresponding to year or observation time, or a set of such values, given in values associated with the year term used in linear model development. Can also equal <code>all</code> , in which case matrices will be estimated for all years. Defaults to <code>all</code> .
patch	A variable designating which patches or subpopulations will have matrices estimated. Should be set to specific patch names, or to <code>all</code> if all patches should have matrices estimated. Defaults to <code>all</code> .
stageframe	A stageframe object that includes information on the size, observation status, propagule status, immaturity status, and maturity status of each ahistorical stage. Should also incorporate bin widths if size is continuous.
repmatrix	A matrix composed mostly of 0s, with non-zero values for each potentially new individual (row) born to each reproductive stage (column). Non-zero entries correspond to multipliers for fecundity, with 1 equaling full fecundity.

<code>data</code>	The original historical demographic data frame used to estimate vital rates (class <code>hfvdata</code>). The original data frame is required in order to initialize years and patches properly.
<code>modelsuite</code>	An optional suite of models of class <code>lefkoMod</code> . If given, then <code>surv_model</code> , <code>obs_model</code> , <code>size_model</code> , <code>repst_model</code> , <code>fec_model</code> , <code>paramnames</code> , <code>yearcol</code> , and <code>patchcol</code> are not required. Note that the modeling exercise used to develop the models must have tested the impact of time $t-1$ for this to work properly.
<code>surv_model</code>	A linear model predicting survival probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any survival probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>obs_model</code>	A linear model predicting sprouting or observation probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any observation probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>size_model</code>	A linear model predicting size. This can be a model of class <code>glm</code> or <code>glmer</code> , both of which require a predicted poisson variable under a log link, or a model of class <code>lm</code> or <code>lmer</code> , in which a Gaussian response is assumed. If given, then will overwrite any size model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>repst_model</code>	A linear model predicting reproduction probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any reproduction probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>fec_model</code>	A linear model predicting fecundity. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted poisson variable under a log link. If given, then will overwrite any fecundity model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>jsurv_model</code>	A linear model predicting juvenile survival probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any juvenile survival probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>jobs_model</code>	A linear model predicting juvenile sprouting or observation probability. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any juvenile observation probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
<code>jsize_model</code>	A linear model predicting juvenile size. This can be a model of class <code>glm</code> or <code>glmer</code> , both of which require a predicted poisson variable under a log link, or a model of class <code>lm</code> or <code>lmer</code> , in which a Gaussian response is assumed. If given, then will overwrite any juvenile size model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.

jrepst_model	A linear model predicting reproduction probability of a mature individual that was immature in the previous year. This can be a model of class <code>glm</code> or <code>glmer</code> , and requires a predicted binomial variable under a logit link. If given, then will overwrite any reproduction probability model given in <code>modelsuite</code> . This model must have been developed in a modeling exercise testing the impacts of times t and $t-1$.
paramnames	A dataframe with two columns, the first showing the general model terms that will be used in matrix creation, and the second showing the equivalent terms used in modeling. Only required if 'modelsuite' is not supplied.
surv_dev	A numeric value to be added to the y-intercept in the linear model for survival probability.
obs_dev	A numeric value to be added to the y-intercept in the linear model for observation probability.
size_dev	A numeric value to be added to the y-intercept in the linear model for size.
repst_dev	A numeric value to be added to the y-intercept in the linear model for probability of reproduction.
fec_dev	A numeric value to be added to the y-intercept in the linear model for fecundity.
jsurv_dev	A numeric value to be added to the y-intercept in the linear model for juvenile survival probability.
jobs_dev	A numeric value to be added to the y-intercept in the linear model for juvenile observation probability.
jsize_dev	A numeric value to be added to the y-intercept in the linear model for juvenile size.
jrepst_dev	A numeric value to be added to the y-intercept in the linear model for juvenile reproduction probability.
repmo	A scalar multiplier of fecundity. Defaults to 1.
overwrite	A data frame developed with the <code>overwrite()</code> function, describing transitions to be overwritten either with given values or with other estimated transitions.
yearcol	The variable name or column number corresponding to year in time t in the dataset. Not needed if a <code>modelsuite</code> is supplied.
patchcol	The variable name or column number corresponding to patch in the dataset. Not needed if a <code>modelsuite</code> is supplied.
year.as.random	A logical term indicating whether coefficients for missing patches within vital rate models should be estimated as random intercepts. Defaults to FALSE, in which case missing time step coefficients are set to 0.
patch.as.random	A logical term indicating whether coefficients for missing patches within vital rate models should be estimated as random intercepts. Defaults to FALSE, in which case missing patch coefficients are set to 0.
randomseed	A numeric value used as a seed to generate random estimates for missing time step and patch coefficients, if either <code>year.as.random</code> or <code>patch.as.random</code> is set to TRUE.
negfec	A logical value denoting whether fecundity values estimated to be negative should be reset to 0. Defaults to FALSE.

reduce A logical value denoting whether to remove historical stages associated solely with 0 transitions. These are only removed in cases where the associated row and column sums in ALL matrices estimated equal 0. Defaults to FALSE.

Value

If all inputs are properly formatted, then this function will return either an object of class `lefkoMat`. Output includes:

A	A list of full projection matrices in order of sorted patches and years.
U	A list of survival-transition matrices sorted as in A.
F	A list of fecundity matrices sorted as in A.
hstages	A data frame matrix showing the pairing of ahistorical stages used to create historical stage pairs.
ahstages	A data frame detailing the characteristics of associated ahistorical stages.
labels	A data frame giving the patch and year of each matrix in order. In <code>flefko3()</code> , only one population may be analyzed at once, and so <code>pop = NA</code> .
matrixqc	A short vector describing the number of non-zero elements in U and F matrices, and the number of annual matrices.
modelqc	This is the qc portion of the <code>modelsuite</code> input.

Examples

```
data(lathyrus)

sizevector <- c(0, 4.6, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9)
stagevector <- c("Sd", "Sd1", "Dorm", "Sz1nr", "Sz2nr", "Sz3nr", "Sz4nr", "Sz5nr",
  "Sz6nr", "Sz7nr", "Sz8nr", "Sz9nr", "Sz1r", "Sz2r", "Sz3r", "Sz4r",
  "Sz5r", "Sz6r", "Sz7r", "Sz8r", "Sz9r")
repvector <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1)
obsvector <- c(0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 4.6, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5,
  0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5)

lathframeIn <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvertIn <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "lnVol88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframeIn,
  stagesize = "sizea", censorcol = "Missing1988",
```

```

censorkeep = NA, NAas0 = TRUE, censor = TRUE)

lathvertln$fece2 <- round(lathvertln$fece2)
lathvertln$fece1 <- round(lathvertln$fece1)
lathvertln$fece3 <- round(lathvertln$fece3)

lathrepmln <- matrix(0, 21, 21)
lathrepmln[1, c(13:21)] <- 0.345
lathrepmln[2, c(13:21)] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

lathmodelsln3 <- modelsearch(lathvertln, historical = TRUE, approach = "lme4", suite = "main",
  vitalrates = c("surv", "obs", "size", "repst", "fec"),
  juvestimate = "Sd1", bestfit = "AICc&k", sizedist = "gaussian",
  fecdist = "poisson", indiv = "indiv", patch = "patchid",
  year = "year2", year.as.random = TRUE, patch.as.random = TRUE,
  show.model.tables = TRUE, quiet = TRUE)

lathmat3ln <- flefko3(year = "all", patch = "all", stageframe = lathframe1ln,
  modelsuite = lathmodelsln3, data = lathvertln,
  repmatrix = lathrepmln, overwrite = lathover3,
  patchcol = "patchid", yearcol = "year2", year.as.random = FALSE,
  patch.as.random = FALSE, reduce = FALSE)

summary(lathmat3ln)

```

historicalize3	<i>Create Historical Vertical Data Frame From Ahistorical Vertical Data Frame</i>
----------------	---

Description

`historicalize3()` returns a vertically formatted demographic data frame organized to create historical projection matrices, given a vertically but ahistorically formatted data frame. This data frame is in standard 'lefko3' format and can be used in all functions in the package.

Usage

```

historicalize3(
  data,
  popidcol = 0,
  patchidcol = 0,
  individcol,
  year2col = 0,
  year3col = 0,
  xcol = 0,

```



```

    ycol = 0,
    sizea2col = 0,
    sizea3col = 0,
    sizeb2col = 0,
    sizeb3col = 0,
    sizec2col = 0,
    sizec3col = 0,
    repstra2col = 0,
    repstra3col = 0,
    repstrb2col = 0,
    repstrb3col = 0,
    fecal2col = 0,
    fecal3col = 0,
    fecb2col = 0,
    fecb3col = 0,
    alive2col = 0,
    alive3col = 0,
    dead2col = 0,
    dead3col = 0,
    obs2col = 0,
    obs3col = 0,
    nonobs2col = 0,
    nonobs3col = 0,
    repstrrel = 1,
    fecrel = 1,
    stage2col = 0,
    stage3col = 0,
    juv2col = 0,
    juv3col = 0,
    stageassign = NA,
    stagesize = NA,
    censor = FALSE,
    censorcol = 0,
    censorkeep = 0,
    spacing = NA,
    NAas0 = FALSE,
    NRasRep = FALSE,
    reduce = TRUE
  )

```

Arguments

<code>data</code>	The horizontal data file.
<code>popidcol</code>	A variable name or column number corresponding to the identity of the population for each individual.
<code>patchidcol</code>	A variable name or column number corresponding to the identity of the patch for each individual, if patches have been designated within populations.

individcol	A variable name or column number corresponding to the identity of each individual.
year2col	A variable name or column number corresponding to the year or time step in time t .
year3col	A variable name or column number corresponding to the year or time step in time $t+1$.
xcol	A variable name or column number corresponding to the x coordinate of each individual in Cartesian space.
ycol	A variable name or column number corresponding to the y coordinate of each individual in Cartesian space.
sizea2col	A variable name or column number corresponding to the primary size entry in time t .
sizea3col	A variable name or column number corresponding to the primary size entry in time $t+1$.
sizeb2col	A variable name or column number corresponding to the secondary size entry in time t .
sizeb3col	A variable name or column number corresponding to the secondary size entry in time $t+1$.
sizec2col	A variable name or column number corresponding to the tertiary size entry in time t .
sizec3col	A variable name or column number corresponding to the tertiary size entry in time $t+1$.
repstra2col	A variable name or column number corresponding to the production of reproductive structures, such as flowers, in time t . This can be binomial or count data, and is used to in analysis of the probability of reproduction.
repstra3col	A variable name or column number corresponding to the production of reproductive structures, such as flowers, in time $t+1$. This can be binomial or count data, and is used to in analysis of the probability of reproduction.
repstrb2col	A second variable name or column number corresponding to the production of reproductive structures, such as flowers, in time t . This can be binomial or count data.
repstrb3col	A second variable name or column number corresponding to the production of reproductive structures, such as flowers, in time $t+1$. This can be binomial or count data.
feca2col	A variable name or column number corresponding to fecundity in time t . This may represent egg counts, fruit counts, seed production, etc.
feca3col	A variable name or column number corresponding to fecundity in time $t+1$. This may represent egg counts, fruit counts, seed production, etc.
fecb2col	A second variable name or column number corresponding to fecundity in time t . This may represent egg counts, fruit counts, seed production, etc.
fecb3col	A second variable name or column number corresponding to fecundity in time $t+1$. This may represent egg counts, fruit counts, seed production, etc.

alive2col	A variable name or column number that provides information an whether an individual is alive in time t . If used, living status must be designated as binomial (living = 1, dead = 0).
alive3col	A variable name or column number that provides information an whether an individual is alive in time $t+1$. If used, living status must be designated as binomial (living = 1, dead = 0).
dead2col	A variable name or column number that provides information an whether an individual is dead in time t . If used, dead status must be designated as binomial (living = 0, dead = 1).
dead3col	A variable name or column number that provides information an whether an individual is dead in time $t+1$. If used, dead status must be designated as binomial (living = 0, dead = 1).
obs2col	A variable name or column number providing information on whether an individual is in an observable stage in time t . If used, observation status must be designated as binomial (observed = 1, not observed = 0).
obs3col	A variable name or column number providing information on whether an individual is in an observable stage in time $t+1$. If used, observation status must be designated as binomial (observed = 1, not observed = 0).
nonobs2col	A variable name or column number providing information on whether an individual is in an unobservable stage in time t . If used, observation status must be designated as binomial (observed = 0, not observed = 1).
nonobs3col	A variable name or column number providing information on whether an individual is in an unobservable stage in time $t+1$. If used, observation status must be designated as binomial (observed = 0, not observed = 1).
repstrrel	This is a scalar modifier for that makes the variable in repstrb2col equivalent to repstra2col. This can be useful if two reproductive status variables have related but unequal units, for example if repstrb2col refers to one-flowered stems while repstra2col refers to two-flowered stems.
fecrel	This is a scalar modifier for that makes the variable in fecb2col equivalent to feca2col. This can be useful if two fecundity variables have related but unequal units.
stage2col	Optional variable name or column number corresponding to life history stage in time t .
stage3col	Optional variable name or column number corresponding to life history stage in time $t+1$.
juv2col	A variable name or column number that marks individuals in immature stages in time t . The <code>historicalize3()</code> function assumes that immature individuals are identified in this variable marked with a number equal to or greater than 1, and that mature individuals are marked as 0 or NA.
juv3col	A variable name or column number that marks individuals in immature stages in time $t+1$. The <code>historicalize3()</code> function assumes that immature individuals are identified in this variable marked with a number equal to or greater than 1, and that mature individuals are marked as 0 or NA.

stageassign	The stageframe object identifying the life history model being operationalized. Note that if stage2col is provided, then this stageframe is not utilized in stage designation.
stagesize	A variable name or column number describing which size variable to use in stage estimation. Defaults to NA, and can also take sizea, sizeb, sizec, or sizeadded, depending on which size variable is chosen.
censor	A logical variable determining whether the output data should be censored using the variable defined in censorcol. Defaults to FALSE.
censorcol	A variable name or column number corresponding to a censor variable within the dataset, used to distinguish between entries to use and those to discard from analysis, or to designate entries with special issues that require further attention.
censorkeep	The value of the censoring variable identifying data that should be included in analysis. Defaults to 0, but may take any value including NA.
spacing	The spacing at which density should be estimated, if density estimation is desired and x and y coordinates are supplied. Given in the same units as those used in the x and y coordinates given in xcol and ycol. Defaults to NA.
NAas0	If TRUE, then all NA entries for size and fecundity variables will be set to 0. This can help increase the sample size analyzed by <code>modelsearch()</code> , but should only be used when it is clear that this substitution is biologically realistic. Defaults to FALSE.
NRasRep	If TRUE, then will treat non-reproductive but mature individuals as reproductive during stage assignment. This can be useful, for example, when a matrix is desired without separation of reproductive and non-reproductive but mature stages of the same size. Only used if stageassign is set to a stageframe. Defaults to FALSE.
reduce	A logical variable determining whether invariant state variables should be removed from the output dataset. For example, if all living individuals are always observable, then variables identifying observation status are invariant and can be removed. Defaults to TRUE.

Value

If all inputs are properly formatted, then this function will output a historical vertical data frame (class `hfvdata`), meaning that the output data frame will have three consecutive years of size and reproductive data per individual per row. Note that determination of state in times t^*-1 and t^*+1 gives preference to condition in time t^* within the input dataset. So, conflicts in condition in input datasets that have both times t^* and t^*+1 listed per row are resolved by using condition in time t^* .

popid	Unique identifier for the population, if given.
patchid	Unique identifier for the patch within the population, if given.
year1, year2, year3	Year or time step at times $t-1$, t , and $t+1$.
xpos, ypos	X and Y position in Cartesian space, if given.
sizea1, sizea2, sizea3	Main size measurement in times $t-1$, t , and $t+1$, respectively.

sizeb1,sizeb2,sizeb3	Secondary size measurement in times $t-1$, t , and $t+1$, respectively.
sizec1,sizec2,sizec3	Tertiary size measurement in times $t-1$, t , and $t+1$, respectively.
censor1,censor2,censor3	Censor state values in times $t-1$, t , and $t+1$.
repstra1,repstrb1,repstrc1	Main, secondary, and tertiary numbers of reproductive structures in time $t-1$.
repstra2,repstrb2,repstrc2	Main, secondary, and tertiary numbers of reproductive structures in time t .
repstra3,repstrb3,repstrc3	Main, secondary, and tertiary numbers of reproductive structures in time $t+1$.
feca1,feceb1	Main, secondary, and tertiary numbers of offspring in time $t-1$.
feca2,feceb2	Main, secondary, and tertiary numbers of offspring in time t .
feca3,feceb3	Main, secondary, and tertiary numbers of offspring in time $t+1$.
size1added,size2added,size3added	Sum of primary, secondary, and tertiary size measurements in times $t-1$, t , and $t+1$, respectively.
repstr1added,repstr2added,repstr3added	Sum of primary, secondary, and tertiary reproductive structures in times $t-1$, t , and $t+1$, respectively.
fec1added,fec2added,fec3added	Sum of primary, secondary, and tertiary offspring numbers in times $t-1$, t , and $t+1$, respectively.
obsstatus1,obsstatus2,obsstatus3	Binomial observation state in times $t-1$, t , and $t+1$, respectively.
repstatus1,repstatus2,repstatus3	Binomial reproductive state in times $t-1$, t , and $t+1$, respectively.
fecstatus1,fecstatus2,fecstatus3	Binomial offspring production state in times $t-1$, t , and $t+1$, respectively.
firstseen	Year or time step of first observation.
lastseen	Year or time step of last observation.
xcorr,ycorr	Overall x and y coordinates of individual in Cartesian space.
alive1,alive2,alive3	Binomial state as alive in times $t-1$, t , and $t+1$, respectively.
obsage	Observed age in time t , assuming first observation corresponds to age = 0.
obs lifespan	Observed lifespan, given as 'lastseen - firstseen + 1'.
indiv id	Unique identifier for the individual.
density	Density of individuals per unit designated in 'spacing'. Only given if spacing is not NA.

Examples

```
data(cypvert)

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm", "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
  repstatus = repvector, obsstatus = obsvector,
  matstatus = matvector, propstatus = propvector,
  immstatus = immvector, indataset = indataset,
  binhalfwidth = binvec)

cypframe_raw

cypraw_v2 <- historicalize3(data = cypvert, patchidcol = "patch", individcol = "plantid",
  year2col = "year2", sizea2col = "Inf2.2", sizea3col = "Inf2.3",
  sizeb2col = "Inf.2", sizeb3col = "Inf.3", sizec2col = "Veg.2",
  sizec3col = "Veg.3", repstra2col = "Inf2.2", repstra3col = "Inf2.3",
  repstrb2col = "Inf.2", repstrb3col = "Inf.3", fec2col = "Pod.2",
  fec3col = "Pod.3", repstrrel = 2, stageassign = cypframe_raw,
  stagesize = "sizeadded", censorcol = "censor", censor = FALSE,
  NAas0 = TRUE, NRasRep = TRUE, reduce = TRUE)

summary(cypraw_v2)
```

lambda3

Dominant Eigenvalue and Deterministic Population Growth Rate Estimation

Description

`lambda3()` is a generic function that returns the dominant eigenvalue of a matrix, and set of dominant eigenvalues of a set of matrices. Unlike the 'popbio' package's `lambda()` function, it is particularly made to handle very large and sparse matrices supplied as `lefkoMat` objects or as individual matrices. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
lambda3(mats)
```

Arguments

mats A lefkoMat object, or a population projection matrix, for which the dominant eigenvalue is desired.

Value

The value returned depends on the class of the **mats** argument.

See Also

[lambda3.lefkoMat\(\)](#)

[lambda3.matrix\(\)](#)

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "indiv")
```

```
ehrlen3mean <- lmean(ehrlen3)
lambda3(ehrlen3mean)
```

lambda3.lefkoMat	<i>Estimate Deterministic Population Growth Rate for a lefkoMat Object</i>
------------------	--

Description

lambda3.lefkoMat() returns the dominant eigenvalues of projection matrices supplied as lefkoMat objects. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
## S3 method for class 'lefkoMat'
lambda3(mats)
```

Arguments

mats An object of class lefkoMat.

Value

This function returns the dominant eigenvalue of each \$A matrix in the lefkoMat object input. This is given as the largest real part of all eigenvalues estimated via the [eigs\(\)](#) function in package 'RSpectra'. The output includes a data frame showing the population, patch, and lambda estimate for each \$A matrix within the object. Row names correspond to the number of the matrix within the \$A element of the lefkoMat object.

See Also

[lambda3\(\)](#)
[lambda3.matrix\(\)](#)

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VLa", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)
```



```

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "individ")

ehrlen3mean <- lmean(ehrlen3)
lambda3(ehrlen3mean)

```

lambda3.matrix	<i>Estimate Deterministic Population Growth Rate of a Projection Matrix</i>
----------------	---

Description

lambda3.matrix() returns the dominant eigenvalues of a single projection matrix. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```

## S3 method for class 'matrix'
lambda3(mats)

```

Arguments

mats A population projection matrix of class matrix.

Value

This function returns the dominant eigenvalue of the matrix. This is given as the largest real part of all eigenvalues estimated via the `eigs()` function in package 'RSpectra'.

See Also

`lambda3()`
`lambda3.lefkoMat()`

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  individcol = "individ")

ehrlen3mean <- lmean(ehrlen3)
lambda3(ehrlen3mean$A[[1]])
```

lathyrus

*Demographic Dataset of Lathyrus vernus Population***Description**

A dataset containing the states and fates of *Lathyrus vernus* (spring vetch), family Fabaceae, from a population in Sweden monitored annually from 1988 to 1991 in six study plots.

Usage

```
data(lathyrus)
```

Format

A data frame with 1119 individuals and 34 variables. Each row corresponds to a unique individual, and each variable from Volume88 on refers to the state of the individual in a given year.

SUBPLOT A variable referring to patch within the population.

GENET A numeric variable giving a unique number to each individual.

Volume88 Aboveground volume in cubic mm in 1988.

lnVol88 Natural logarithm of Volume88.

FCODE88 Equals 1 if flowering and 0 if not flowering in 1988.

Flow88 Number of flowers in 1988.

Intactseed88 Number of intact mature seeds produced in 1988. Not always an integer, as in some cases seed number was estimated via linear modeling.

Dead1988 Marked as 1 if known to be dead in 1988.

Dormant1988 Marked as 1 if known to be alive but vegetatively dormant in 1988.

Missing1988 Marked as 1 if not found in 1988.

Seedling1988 Marked as 1, 2, or 3 if observed as a seedling in year t . Numbers refer to certainty of assignment: 1 = certain that plant is a seedling in 1988, 2 = likely that plant is a seedling in 1988, 3 = probable that plant is a seedling in 1988.

Volume89 Aboveground volume in cubic mm in 1989.

lnVol89 Natural logarithm of Volume89.

FCODE89 Equals 1 if flowering and 0 if not flowering in 1989.

Flow89 Number of flowers in 1989.

Intactseed89 Number of intact mature seeds produced in 1989. Not always an integer, as in some cases seed number was estimated via linear modeling.

Dead1989 Marked as 1 if known to be dead in 1989.

Dormant1989 Marked as 1 if known to be alive but vegetatively dormant in 1989.

Missing1989 Marked as 1 if not found in 1989.

Seedling1989 Marked as 1, 2, or 3 if observed as a seedling in year t . Numbers refer to certainty of assignment: 1 = certain that plant is a seedling in 1989, 2 = likely that plant is a seedling in 1989, 3 = probable that plant is a seedling in 1989.

Volume90 Aboveground volume in mm^3 in 1990.

lnVol90 Natural logarithm of Volume90.

FCODE90 Equals 1 if flowering and 0 if not flowering in 1990.

Flow90 Number of flowers in 1990.

Intactseed90 Number of intact mature seeds produced in 1990. Not always an integer, as in some cases seed number was estimated via linear modeling.

Dead1990 Marked as 1 if known to be dead in 1990.

Dormant1990 Marked as 1 if known to be alive but vegetatively dormant in 1990.

Missing1990 Marked as 1 if not found in 1990.

Seedling1990 Marked as 1, 2, or 3 if observed as a seedling in year t . Numbers refer to certainty of assignment: 1 = certain that plant is a seedling in 1990, 2 = likely that plant is a seedling in 1990, 3 = probable that plant is a seedling in 1990.

Volume91 Aboveground volume in mm^3 in 1991.

lnVol91 Natural logarithm of Volume91.

FCODE91 Equals 1 if flowering and 0 if not flowering in 1991.

Flow91 Number of flowers in 1991.

Intactseed91 Number of intact mature seeds produced in 1991. Not always an integer, as in some cases seed number was estimated via linear modeling.

Dead1991 Marked as 1 if known to be dead in 1991.

Dormant1991 Marked as 1 if known to be alive but vegetatively dormant in 1991.

Missing1991 Marked as 1 if not found in 1991.

Seedling1991 Marked as 1, 2, or 3 if observed as a seedling in year t . Numbers refer to certainty of assignment: 1 = certain that plant is a seedling in 1991, 2 = likely that plant is a seedling in 1991, 3 = probable that plant is a seedling in 1991.

Source

Ehrlén, J. 2000. The dynamics of plant populations: does the history of individuals matter? *Ecology* 81(6):1675-1684.

Examples

```
data(lathyrus)

sizevector <- c(0, 4.6, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9)
stagevector <- c("Sd", "Sd1", "Dorm", "Sz1nr", "Sz2nr", "Sz3nr", "Sz4nr", "Sz5nr",
                 "Sz6nr", "Sz7nr", "Sz8nr", "Sz9nr", "Sz1r", "Sz2r", "Sz3r", "Sz4r",
                 "Sz5r", "Sz6r", "Sz7r", "Sz8r", "Sz9r")
repvector <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1)
obsvector <- c(0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
```

```

immvector <- c(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 4.6, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5,
            0.5, 0.5, 0.5, 0.5, 0.5, 0.5)

lathframeIn <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
                        obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
                        indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvertIn <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
                          individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
                          size1col = "lnVol88", repstr1col = "FCODE88",
                          fec1col = "Intactseed88", dead1col = "Dead1988",
                          nonobs1col = "Dormant1988", stageassign = lathframeIn,
                          stagesize = "sizea", censorcol = "Missing1988",
                          censorkeep = NA, NAas0 = TRUE, censor = TRUE)

summary(lathvertIn)

```

Description

This package creates population projection matrices for use in population ecological analyses. The particular specialty of the package is the construction of historical matrices, which are 2-dimensional matrices comprising 3 time intervals of demographic information. The package is robust and can produce function-based and raw matrices for both standard ahistorical (i.e. 2 time interval) and historical analyses.

Package lefko3

Details

The lefko package provides five categories of functions: 1. Data transformation and handling functions 2. Functions determining population characteristics from vertical data 3. Model building and selection 4. Matrix / integral projection model creation functions 5. Population dynamics analysis functions

It also includes example datasets complete with sample code.

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The lefko package provides five categories of functions: 1. Data transformation and handling functions 2. Functions determining population characteristics from vertical data 3. Model building and

selection 4. Matrix / integral projection model creation functions 5. Population dynamics analysis functions

It also includes example datasets complete with sample code.

Author(s)

Richard P. Shefferson <cdorm@g.ecc.u-tokyo.ac.jp>

Johan Ehrlén

Richard P. Shefferson <cdorm@g.ecc.u-tokyo.ac.jp>

Johan Ehrlén

References

Shefferson, R.P., J. Ehrlén, and S. Kurokawa. *In review*. Package lefko3: individual history in population projection matrix modeling.

Shefferson, R.P., J. Ehrlén, and S. Kurokawa. *In review*. Package lefko3: individual history in population projection matrix modeling.

lmean

Estimate Mean Projection Matrices

Description

lmean() estimates mean projection matrices. The function differs from a typical element-by-element mean matrix estimator through two options. First, it allows mean matrix elements to be estimated as geometric means across time. Spatial means are always developed as arithmetic means. Second, it allows element means to be estimated ignoring 0s in cases where some elements are not zero. The function takes lefkoMat objects as input, and returns the same class of object.

Usage

```
lmean(mats, time = "arithmetic", sparse = FALSE, AasSum = TRUE)
```

Arguments

mats	A lefkoMat object holding population projection matrices.
time	A variable designating whether element means be computed as geometric (geometric or g) or arithmetic (arithmetic or a) across time. Please note that using the geometric option does not yield a geometric mean matrix - it yields a matrix of geometric mean elements, which is theoretically different. Defaults to arithmetic.
sparse	If TRUE, then all 0s will be ignored in elements that include other numbers across matrices. Only elements that equal 0 in all matrices (structural zeroes) will be exempt. Defaults to FALSE.

AasSum If TRUE, then lefkoMat matrix means are estimated as means of U and F matrices, and then summed to estimate A matrices. If FALSE, then mean A matrices are estimated as means of A matrices within lefkoMat objects. Defaults to TRUE.

Value

Yields a lefkoMat object with the following characteristics:

A	A list of full mean projection matrices in order of sorted populations, patches, and years. These are typically estimated as the sums of associated mean U and F matrices.
U	A list of mean survival-transition matrices sorted as in A.
F	A list of mean fecundity matrices sorted as in A.
hstages	A data frame matrix showing the pairing of ahistorical stages used to create historical stage pairs.
ahstages	A data frame detailing the characteristics of associated ahistorical stages.
labels	A data frame giving the population, patch, and year of each mean matrix in order. If pop, patch, or year2 are all NA in the original labels set, then these will be re-labeled as A, 1, or 1, respectively.
matrixqc	A short vector describing the number of non-zero elements in U and F mean matrices, and the number of annual matrices.
modelqc	The qc portion of the modelsuite input, if used.
dataqc	A vector showing the numbers of individuals and rows in the vertical dataset used as input.

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
```

```

nonobs1col = "Dormant1988", stageassign = lathframe,
stagesize = "sizea", censorcol = "Missing1988",
censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
                      stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
                 stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
                 overwrite = lathover3, yearcol = "year2",
                 indivcol = "individ")

ehrlen3mean <- lmean(ehrlen3)
ehrlen3mean$A[[1]]

```

modelsearch

Develop Best-fit Vital Rate Estimation Models For Matrix Develop-
ment

Description

modelsearch() returns both a table of vital rate estimating models and a best-fit model for each major vital rate estimated. The final output can be used as input in other functions within this package.

Usage

```

modelsearch(
  data,
  historical = TRUE,
  approach = "lme4",
  suite = "size",
  vitalrates = c("surv", "size", "fec"),
  juvestimate = NA,
  juvsize = FALSE,
  bestfit = "AICc&k",
  sizedist = "gaussian",
  fecdist = "gaussian",
  fectime = 2,
  censor = NA,
  indiv = "individ",
  patch = NA,
  year = "year2",

```



```

surv = c("alive3", "alive2", "alive1"),
obs = c("obsstatus3", "obsstatus2", "obsstatus1"),
size = c("sizea3", "sizea2", "sizea1"),
repst = c("repstatus3", "repstatus2", "repstatus1"),
fec = c("feca3", "feca2", "feca1"),
stage = c("stage3", "stage2", "stage1"),
age = NA,
year.as.random = TRUE,
patch.as.random = TRUE,
show.model.tables = TRUE,
quiet = FALSE
)

```

Arguments

data	The vertical dataset to be used for analysis. The dataset should ideally be of class <code>hfvdata</code> , but will also work with data frames formatted similarly to the output format provided by functions <code>verticalize3()</code> or <code>historicalize3()</code> , as long as all needed variables are properly designated.
historical	A logical variable denoting whether to assess the effects of state in time $t-1$ in addition to state in time t . Defaults to <code>TRUE</code> .
approach	Designates the approach to be taken for model building. The default is <code>lme4</code> , which uses the mixed model approach utilized in package 'lme4'. Other options include <code>glm</code> , which uses the <code>lm</code> , <code>glm</code> , and related functions in base R.
suite	This describes the global model for each vital rate estimation and has the following possible values: <code>full</code> , includes main effects and all two-way interactions of size and reproductive status; <code>main</code> , includes main effects only of size and reproductive status; <code>size</code> , includes only size (also interactions between size in historical model); <code>rep</code> , includes only reproductive status (also interactions between status in historical model); <code>cons</code> , all vital rates estimated only as y-intercepts. If <code>approach = "glm"</code> and <code>year.as.random = FALSE</code> , then <code>year</code> is also included as a fixed effect, and, in the case of <code>full</code> , included in two-way interactions. Defaults to <code>size</code> .
vitalrates	A vector describing which vital rates will be estimated via linear modeling, with the following options: <code>surv</code> , survival probability; <code>obs</code> , observation probability; <code>size</code> , overall size; <code>repst</code> , probability of reproducing; and <code>fec</code> , amount of reproduction (overall fecundity). Defaults to <code>c("surv", "size", "fec")</code> .
juvestimate	An optional variable denoting the stage name of the juvenile stage in the vertical dataset. If not <code>NA</code> , and <code>stage</code> is also given (see below), then vital rates listed in <code>vitalrates</code> other than <code>fec</code> will also be estimated from the juvenile stage to all adult stages. Defaults to <code>NA</code> , in which case juvenile vital rates are not estimated.
juvsize	A logical variable denoting whether size should be used as a term in models involving transition from the juvenile stage. Defaults to <code>FALSE</code> , and is only used if <code>juvestimate</code> does not equal <code>NA</code> .
bestfit	A variable indicating the model selection criterion for the choice of best-fit model. The default is <code>AICc&k</code> , which chooses the best-fit model as the model

with the lowest AICc or, if not the same model, then the model that has the lowest degrees of freedom among models with $\Delta \text{AICc} \leq 2.0$. Alternatively, AICc may be chosen, in which case the best-fit model is simply the model with the lowest AICc value.

sizedist	The probability distribution used to model size. Options include gaussian for the Normal distribution (default), poisson for the Poisson distribution, and negbin for the negative binomial distribution.
fecdist	The probability distribution used to model fecundity. Options include gaussian for the Normal distribution (default), poisson for the Poisson distribution, and negbin for the negative binomial distribution.
fectime	A variable indicating which year of fecundity to use as the response term in fecundity models. Options include 2, which refers to time t , and 3, which refers to time $t+1$. Defaults to 2.
censor	A vector denoting the names of censoring variables in the dataset, in order from time $t+1$, followed by time t , and lastly followed by time $t-1$. Defaults to NA.
indiv	A variable indicating the variable name coding individual identity. Defaults to individ.
patch	A variable indicating the variable name coding for patch, where patches are defined as permanent subgroups within the study population. Defaults to NA.
year	A variable indicating the variable coding for observation time in time t . Defaults to year2.
surv	A vector indicating the variable names coding for status as alive or dead in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("alive3", "alive2", "alive1")</code> .
obs	A vector indicating the variable names coding for observation status in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("obsstatus3", "obsstatus2", "obsstatus1")</code> .
size	A vector indicating the variable names coding for size in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("sizea3", "sizea2", "sizea1")</code> .
repst	A vector indicating the variable names coding for reproductive status in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("repstatus3", "repstatus2", "repstatus1")</code> .
fec	A vector indicating the variable names coding for fecundity in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("feca3", "feca2", "feca1")</code> .
stage	A vector indicating the variables coding for stage in times $t+1$, t , and $t-1$. Defaults to <code>c("stage3", "stage2", "stage1")</code> .
age	Designates the name of the variable corresponding to age in the vertical dataset. Defaults to NA, in which case age is not included in linear models. Should only be used if building age x stage matrices.
year.as.random	If set to TRUE and approach = "lme4", then year is included as a random factor. If set to FALSE, then year is included as a fixed factor. All other combinations of logical value and approach lead to year not being included in modeling.
patch.as.random	If set to TRUE and approach = "lme4", then patch is included as a random factor. If set to FALSE and approach = "glm", then patch is included as a fixed factor. All other combinations of logical value and approach lead to patch not being included in modeling.

<code>show.model.tables</code>	If set to TRUE, then includes full modeling tables in the output. Defaults to TRUE.
<code>quiet</code>	If set to TRUE, then model building and selection will proceed without warnings and diagnostic messages being issued. Note that this will not affect warnings and messages generated during global model development. Defaults to FALSE.

Value

This function yields an object of class `lefkoMod`, which is a list in which the first 8 elements are the best-fit models for survival, observation status, size, reproductive status, fecundity, juvenile survival, juvenile observation, and juvenile size, respectively, followed by eight elements corresponding to the model tables for each of these vital rates, in order, followed by a single character element denoting the criterion used for model selection, as follows:

<code>survival_model</code>	Best-fit model of the binomial probability of survival from time t to time $t+1$. Defaults to 1.
<code>observation_model</code>	Best-fit model of the binomial probability of observation in time $t+1$ given survival to that time. Defaults to 1.
<code>size_model</code>	Best-fit model of size in time $t+1$ given survival to and observation in that time. Defaults to 1.
<code>repstatus_model</code>	Best-fit model of the binomial probability of reproduction in time $t+1$, given survival to and observation in that time. Defaults to 1.
<code>fecundity_model</code>	Best-fit model of fecundity in time $t+1$ given survival to, and observation and reproduction in that time. Defaults to 1.
<code>juv_survival_model</code>	Best-fit model of the binomial probability of survival from time t to time $t+1$ of an immature individual. Defaults to 1.
<code>juv_observation_model</code>	Best-fit model of the binomial probability of observation in time $t+1$ given survival to that time of an immature individual. Defaults to 1.
<code>juv_size_model</code>	Best-fit model of size in time $t+1$ given survival to and observation in that time of an immature individual. Defaults to 1.
<code>juv_reproduction_model</code>	Best-fit model of the binomial probability of reproduction in time $t+1$, given survival to and observation in that time of an individual that was immature in time t . This model is technically not a model of reproduction probability for individuals that are immature, rather reproduction probability here is given for individuals that are mature in time $t+1$ but were immature in time t . Defaults to 1.
<code>survival_table</code>	Full dredge model table of survival probability.
<code>observation_table</code>	Full dredge model table of observation probability.
<code>size_table</code>	Full dredge model table of size.

repstatus_table	Full dredge model table of reproduction probability.
fecundity_table	Full dredge model table of fecundity.
juv_survival_table	Full dredge model table of immature survival probability.
juv_observation_table	Full dredge model table of immature observation probability.
juv_size_table	Full dredge model table of immature size.
juv_reproduction_table	Full dredge model table of immature reproduction probability.
criterion	Character variable denoting the criterion used to determine the best-fit model.
qc	Data frame with three variables: 1) Name of vital rate, 2) number of individuals used to model that vital rate, and 3) number of individual transitions used to model that vital rate.

The mechanics governing model building are fairly robust to errors and exceptions. The function attempts to build global models, and simplifies models automatically via several steps should model building fail. Model selection proceeds via the [dredge](#) function in package 'MuMIn', and defaults to the global model should that fail.

This function is set to run in a verbose fashion, so that any errors and warnings developed during model building, model analysis, and model selection can be seen and, if necessary, dealt with. Interpretations of errors during global model analysis may be found in documentation in base R for functions `lm` and `glm` used in analysis of models without random terms, and packages 'lme4' and 'glmmTMB' for mixed models (see [glmer](#) and [glmmTMB](#), respectively). Package 'MuMIn' is used for model dredging (see [dredge](#)), and errors and warnings during dredging can be interpreted using the documentation for that package. The `quiet = TRUE` option can be used to silence dredging warnings, but users should note that automated model selection can be viewed as mindless, and so great care should be taken to ensure that the models run are sensible, and that issues of model quality are properly dealt with.

Note that care must be taken to build models that test the impacts of state in time $t-1$ for historical models, and that do not test these impacts for ahistorical models. Ahistorical matrix modeling particularly will yield transition estimates biased low if historical terms from models are ignored. This can be at the start of modeling by setting `historical = FALSE` for the ahistorical case, and `historical = TRUE` for the historical case.

Model building and selection may fail if NAs exist within variables used in modeling. If NAs represent 0 entries, then please change all NAs to 0, as with the `NAas0 = TRUE` option in function [verticalize3\(\)](#).

Examples

```
data(lathyrus)

sizevector <- c(0, 4.6, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9)
stagevector <- c("Sd", "Sd1", "Dorm", "Sz1nr", "Sz2nr", "Sz3nr", "Sz4nr", "Sz5nr",
  "Sz6nr", "Sz7nr", "Sz8nr", "Sz9nr", "Sz1r", "Sz2r", "Sz3r", "Sz4r",
```

```

      "Sz5r", "Sz6r", "Sz7r", "Sz8r", "Sz9r")
repvector <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1)
obsvector <- c(0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 4.6, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5,
            0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5)

lathframeIn <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
                        obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
                        indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvertIn <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
                          individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
                          size1col = "lnVol88", repstr1col = "FCODE88",
                          fec1col = "Intactseed88", dead1col = "Dead1988",
                          nonobs1col = "Dormant1988", stageassign = lathframeIn,
                          stagesize = "sizea", censorcol = "Missing1988",
                          censorkeep = NA, NAas0 = TRUE, censor = TRUE)

lathvertIn$feca2 <- round(lathvertIn$feca2)
lathvertIn$feca1 <- round(lathvertIn$feca1)
lathvertIn$feca3 <- round(lathvertIn$feca3)

lathmodelsIn2 <- modelsearch(lathvertIn, historical = FALSE, approach = "lme4", suite = "main",
                             vitalrates = c("surv", "obs", "size", "repst", "fec"),
                             juvestimate = "Sd1", bestfit = "AICc&k", sizedist = "gaussian",
                             fecdist = "poisson", indiv = "indiv", patch = "patchid",
                             year = "year2", year.as.random = TRUE, patch.as.random = TRUE,
                             show.model.tables = TRUE)

lathmodelsIn2

```

 overwrite

Create an Overwrite Table for Population Matrix Development

Description

`overwrite()` returns a data frame describing which particular transitions within an ahistorical or historical projection matrix to overwrite with either given rates and probabilities, or other estimated transitions.

Usage

```

overwrite(
  stage3,

```

```

    stage2,
    stage1 = NA,
    eststage3 = NA,
    eststage2 = NA,
    eststage1 = NA,
    givenrate = NA,
    type = NA
  )

```

Arguments

stage3	The name of the stage in time $t+1$ in the transition to be replaced.
stage2	The name of the stage in time t in the transition to be replaced.
stage1	The name of the stage in time $t-1$ in the transition to be replaced. Only needed if a historical matrix is to be produced. Use rep if all reproductive stages are to be used, and leave empty or use all if all stages in stageframe are to be used.
eststage3	The name of the stage to replace stage3. Only needed if a transition will be replaced by another estimated transition.
eststage2	The name of the stage to replace stage2. Only needed if a transition will be replaced by another estimated transition.
eststage1	The name of the stage to replace stage1. Only needed if a transition will be replaced by another estimated transition, and the matrix to be estimated is a historical matrix.
givenrate	A fixed rate or probability to replace for the transition described by stage3, stage2, and stage1.
type	A vector denoting the kind of transition that will be replaced. Should be entered as 1, S, or s for survival, or 2, F, or f for fecundity. Defaults to 1, for survival transition.

Value

A data frame that puts the above vectors together and can be used as input in [fleeko3](#), [fleeko2](#), [rleeko3](#), and [rleeko2](#).

Variables in this data frame include the following:

stage3	Stage at time $t+1$ in the transition to be replaced.
stage2	Stage at time t in the transition to be replaced.
stage1	Stage at time $t-1$ in the transition to be replaced.
eststage3	Stage at time $t+1$ in the transition to replace the transition designated by stage3, stage2, and stage1.
eststage2	Stage at time t in the transition to replace the transition designated by stage3, stage2, and stage1.
eststage1	Stage at time $t-1$ in the transition to replace the transition designated by stage3, stage2, and stage1.
givenrate	A constant to be used as the value of the transition.
convtype	Designates whether the transition is a survival-transition probability (1) or a fecundity rate (2).

Examples

```
cypover2r <- overwrite(stage3 = c("SD", "P1", "P2", "P3", "SL", "SL", "D",
  "XSm", "Sm"), stage2 = c("SD", "SD", "P1", "P2", "P3",
  "SL", "SL", "SL", "SL"), eststage3 = c(NA, NA, NA, NA,
  NA, NA, "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA, NA,
  NA, NA, "XSm", "XSm", "XSm"), givenrate = c(0.1, 0.2,
  0.2, 0.2, 0.25, 0.4, NA, NA, NA), type = c("S", "S", "S",
  "S", "S", "S", "S", "S"))
```

```
cypover2r
```

```
cypover3r <- overwrite(stage3 = c("SD", "SD", "P1", "P1", "P2", "P3", "SL",
  "SL", "SL", "D", "XSm", "Sm", "D", "XSm", "Sm"),
  stage2 = c("SD", "SD", "SD", "SD", "P1", "P2", "P3",
  "SL", "SL", "SL", "SL", "SL", "SL", "SL", "SL"),
  stage1 = c("SD", "rep", "SD", "rep", "SD", "P1", "P2",
  "P3", "SL", "P3", "P3", "P3", "SL", "SL", "SL"),
  eststage3 = c(NA, NA, NA, NA, NA, NA, NA, NA, "D",
  "XSm", "Sm", "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA,
  NA, NA, NA, NA, NA, "XSm", "XSm", "XSm", "XSm", "XSm",
  "XSm"), eststage1 = c(NA, NA, NA, NA, NA, NA, NA, NA,
  "XSm", "XSm", "XSm", "XSm", "XSm", "XSm"),
  givenrate = c(0.1, 0.1, 0.2, 0.2, 0.2, 0.2, 0.25, 0.4,
  0.4, NA, NA, NA, NA, NA, NA), type = c("S", "S", "S",
  "S", "S", "S", "S", "S", "S", "S", "S", "S", "S",
  "S"))
```

```
cypover3r
```

repvalue3

Reproductive Value Estimation

Description

repvalue3() is a generic function that estimates returns the reproductive values of stages in a population projection matrix or a set of matrices. The specifics of estimation vary with the class of input object. However, unlike the 'popbio' package's [reproductive.value\(\)](#) function, it is particularly made to handle very large and sparse matrices supplied as `lefkMat` objects or as individual matrices. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
repvalue3(mats)
```

Arguments

`mats` A `lefkMat` object, or population projection matrix.

Value

The value returned depends on the class of the `mat`s argument.

See Also

```
repvalue3.lefkoMat()
repvalue3.matrix()
```

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VLa", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "individ", reduce = TRUE)

ehrlen3mean <- lmean(ehrlen3)
repvalue3(ehrlen3mean)
```

repvalue3.lefkoMat	<i>Estimate Reproductive Value for a lefkoMat Object</i>
--------------------	--

Description

repvalue3.lefkoMat() returns the reproductive values for stages in a set of population projection matrices. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
## S3 method for class 'lefkoMat'  
repvalue3(mats)
```

Arguments

mats An object of class lefkoMat object.

Value

This function returns the reproductive values for stages of a population projection matrix. The nature of the output depends on whether the lefkoMat object used as input is ahistorical or historical. In both cases, raw reproductive values are estimated as the left eigenvector associated with the largest real part of the dominant eigenvalue estimated via the [eigs\(\)](#) function in package 'RSpecTra', divided either by the first non-zero element of the left eigenvector.

If an ahistorical matrix set is used as input, then the output is a data frame that includes the number of the matrix within the '\$A' element of the input lefkoMat object, followed by the original stage id, the new stage id (numeric and assigned through [sf_create\(\)](#)), the original given size, and the reproductive value estimate within a variable called repvalue.

If a historical matrix set is used as input, then a list with two elements is output. The first element is a data frame showing the reproductive values given in terms of across-year stage pairs, as estimated in the procedure described above. The second element is another data frame showing the reproductive values of the basic stages in the associated stageframe. The reproductive values in this second data frame are estimated via the approach developed in Ehrlén (2000), in which each ahistorical stage's reproductive value is the average of the RVs summed by stage at time t weighted by the proportion of that stage pair within the historical stable stage distribution associated with the matrix.

See Also

[repvalue3\(\)](#)
[repvalue3.matrix\(\)](#)

Examples

```

data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VLa", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefk3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "indiv", reduce = TRUE)

ehrlen3mean <- lmean(ehrlen3)
repvalue3(ehrlen3mean)

```

repvalue3.matrix

Estimate Reproductive Value for a Population Projection Matrix

Description

repvalue3.matrix() returns the reproductive values for stages in a population projection matrix. The function assumes that the matrix is ahistorical and provides standard reproductive values, meaning that the overall reproductive values of basic life history stages in a historical matrix are

not provided (the `repvalue3.lefkoMat()` function estimates these on the basis of stage description information provided in the `lefkoMat` object used as input in that function). This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
## S3 method for class 'matrix'
repvalue3(mats)
```

Arguments

`mats` A population projection matrix.

Value

This function returns a vector data frame characterizing the reproductive values for stages of a population projection matrix. This is given as the left eigenvector associated with largest real part of the dominant eigenvalue estimated via the `eigs()` function in package 'RSpectra', divided by the first non-zero element of the left eigenvector.

See Also

`repvalue3()`
`repvalue3.lefkoMat()`

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)
```

```

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
                      stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefko3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
                  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
                  overwrite = lathover3, yearcol = "year2",
                  indivcol = "individ", reduce = TRUE)

ehrlen3mean <- lmean(ehrlen3)
repvalue3(ehrlen3mean$A[[1]])

```

rlefko2

Create Raw Ahistorical Population Projection Matrices

Description

`rlefko2()` returns an ahistorical population projection matrix or, if multiple years are given, then a list of such matrices, as well as the associated component transition and fecundity matrices, a data frame showing the pairing of single ahistorical stages used to create historical paired stages, a dataframe detailing the associated ahistorical stages, and a vector of years corresponding to the matrices (time t).

Usage

```

rlefko2(
  data,
  stageframe,
  year = "all",
  pop = NA,
  patch = NA,
  censor = FALSE,
  stages = NA,
  alive = c("alive3", "alive2"),
  size = c("sizea3", "sizea2"),
  repst = c("repstatus3", "repstatus2"),
  matst = c("matstatus3", "matstatus2"),
  fec = c("feca3", "feca2"),
  repmatrix = NA,
  overwrite = NA,
  yearcol = NA,
  popcol = NA,

```

```

    patchcol = NA,
    indivcol = NA,
    censorcol = NA,
    reduce = FALSE
  )

```

Arguments

data	A vertical demographic data frame, with variables corresponding to the naming conventions in <code>verticalize3()</code> .
stageframe	A stageframe object that includes information on the size, observation status, propagule status, immaturity status, and maturity status of each ahistorical stage. Should also incorporate bin widths if size is continuous.
year	A variable corresponding to year or observation time, or a set of such values, given in values associated with the year term used in linear model development. Can also equal <code>all</code> , in which case matrices will be estimated for all years. Defaults to <code>all</code> .
pop	A variable designating which populations will have matrices estimated. Should be set to specific population names, or to <code>all</code> if all populations should have matrices estimated.
patch	A variable designating which patches or subpopulations will have matrices estimated. Should be set to specific patch names, or to <code>all</code> if all patches should have matrices estimated.
censor	If TRUE, then data will be removed according to the variable set in <code>censorcol</code> , such that only data with censor values equal to 1 will remain. Defaults to FALSE.
stages	An optional but important vector denoting the names of the variables within the main vertical dataset coding for the names of the stages of each individual in times $t+1$ and t , respectively. The names of the stages in these variables should match those used in the <code>stageframe</code> input for this analysis exactly. If left blank, then <code>rlefk2()</code> will attempt to infer stages by matching values of <code>alive</code> , <code>size</code> , <code>repst</code> , and <code>matst</code> to characteristics noted in the associated <code>stageframe</code> .
alive	A vector of names of binomial variables corresponding to status as alive (1) or dead (0) in times $t+1$, t , and $t-1$, respectively.
size	A vector of names of variables coding size in times $t+1$ and t , respectively. Defaults to <code>c("sizea3", "sizea2")</code> .
repst	A vector of names of variables coding reproductive status in times $t+1$ and t , respectively. Defaults to <code>c("repstatus3", "repstatus2")</code> .
matst	A vector of names of variables coding maturity status in times $t+1$ and t , respectively. Defaults to <code>c("matstatus3", "matstatus2")</code> . Must be supplied if stages is not provided.
fec	A vector of names of variables coding fecundity in times $t+1$ and t , respectively. Defaults to <code>c("feca3", "feca2")</code> .
repmatrix	A matrix composed mostly of 0s, with non-zero values for each potentially new individual (row) born to each reproductive stage (column). Non-zero entries correspond to multipliers for fecundity, with 1 equaling full fecundity.

overwrite	A data frame developed with the <code>overwrite()</code> function, describing transitions to be overwritten either with given values or with other estimated transitions.
yearcol	The variable name or column number corresponding to year in time t in the dataset.
popcol	The variable name or column number corresponding to the identity of the population.
patchcol	The variable name or column number corresponding to patch in the dataset.
indivcol	The variable name or column number coding individual identity.
sensorcol	The variable name or column number denoting the censor status. Only needed if <code>censor = TRUE</code> .
reduce	A logical value denoting whether to remove historical stages associated with only zero transitions. These are removed only if all row and column sums in ALL matrices estimated equal 0. Defaults to FALSE.

Value

If all inputs are properly formatted, then this function will return an object of class `lefkMat`. This includes:

A	A list of full projection matrices in order of sorted populations, patches, and years.
U	A list of survival-transition matrices sorted as in A.
F	A list of fecundity matrices sorted as in A.
hstages	Null for ahistorical matrices.
ahstages	A data frame detailing the characteristics of associated ahistorical stages.
labels	A data frame giving the population, patch, and year of each matrix in order.
matrixqc	A short vector describing the number of non-zero elements in U and F matrices, and the number of annual matrices.
dataqc	A vector showing the numbers of individuals and rows in the vertical dataset used as input.

Examples

```
data(cypdata)

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm",
               "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)
```

```

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
  repstatus = repvector, obsstatus = obsvector,
  matstatus = matvector, propstatus = propvector,
  immstatus = immvector, indataset = indataset,
  binhalfwidth = binvec)

cypraw_v1 <- verticalize3(data = cypdata, noyears = 6, firstyear = 2004,
  patchidcol = "patch", individcol = "plantid",
  blocksize = 4, size1col = "Inf2.04", size2col = "Inf.04",
  size3col = "Veg.04", repstr1col = "Inf.04",
  repstr2col = "Inf2.04", fec1col = "Pod.04",
  stageassign = cypframe_raw, stagesize = "sizeadded",
  NAas0 = TRUE, NRasRep = TRUE)

rep_cyp_raw <- matrix(0, 11, 11)
rep_cyp_raw[1:2,7:11] <- 0.5

cypover2r <- overwrite(stage3 = c("SD", "P1", "P2", "P3", "SL", "SL", "D",
  "XSm", "Sm"), stage2 = c("SD", "SD", "P1", "P2", "P3",
  "SL", "SL", "SL", "SL"), eststage3 = c(NA, NA, NA, NA,
  NA, NA, "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA, NA,
  NA, NA, "XSm", "XSm", "XSm"), givenrate = c(0.1, 0.2,
  0.2, 0.2, 0.25, 0.4, NA, NA, NA), type = c("S", "S", "S",
  "S", "S", "S", "S", "S", "S"))

cypmatrix2r <- rlefk2(data = cypraw_v1, stageframe = cypframe_raw, year = "all",
  patch = "all", stages = c("stage3", "stage2", "stage1"),
  size = c("size3added", "size2added"),
  repmatrix = rep_cyp_raw, overwrite = cypover2r,
  yearcol = "year2", patchcol = "patchid",
  individcol = "individ")

cypmatrix2r$A[[1]]

```

rlefk3

Create Raw Historical Population Projection Matrices

Description

`rlefk3()` returns a list of raw historical population projection matrices, as well as the associated component transition and fecundity matrices, data frames describing the ahistorical stages used and the pairing of ahistorical stages used to create historical paired stages, and a data frame describing the population, patch, and year associated with each matrix.

Usage

```

rlefk3(
  data,
  stageframe,
  year = "all",
  pop = NA,

```

```

patch = NA,
censor = FALSE,
stages = NA,
alive = c("alive3", "alive2", "alive1"),
size = c("sizea3", "sizea2", "sizea1"),
repst = c("repstatus3", "repstatus2", "repstatus1"),
matst = c("matstatus3", "matstatus2", "matstatus1"),
fec = c("feca3", "feca2", "feca1"),
repmatrix = NA,
overwrite = NA,
yearcol = NA,
popcol = NA,
patchcol = NA,
indivcol = NA,
censorcol = NA,
reduce = FALSE
)

```

Arguments

data	A vertical demographic data frame, with variables corresponding to the naming conventions in verticalize3() .
stageframe	A stageframe object that includes information on the size, observation status, propagule status, immaturity status, and maturity status of each ahistorical stage. Should also incorporate bin widths if size is continuous.
year	A variable corresponding to year or observation time, or a set of such values, given in values associated with the year term used in linear model development. Can also equal <code>all</code> , in which case matrices will be estimated for all years. Defaults to <code>all</code> .
pop	A variable designating which populations will have matrices estimated. Should be set to specific population names, or to <code>all</code> if all populations should have matrices estimated.
patch	A variable designating which patches or subpopulations will have matrices estimated. Should be set to specific patch names, or to <code>all</code> if all patches should have matrices estimated.
censor	If TRUE, then data will be removed according to the variable set in <code>censorcol</code> , such that only data with censor values equal to 1 will remain. Defaults to FALSE.
stages	An optional but important vector denoting the names of the variables within the main vertical dataset coding for the names of the stages of each individual in times $t+1$, t , and $t-1$, respectively. The names of the stages in these variables should match those used in the <code>stageframe</code> input for this analysis exactly. If left blank, then <code>rlefk3()</code> will attempt to infer stages by matching values of <code>alive</code> , <code>size</code> , <code>repst</code> , and <code>matst</code> to characteristics noted in the associated <code>stageframe</code> .
alive	A vector of names of binomial variables corresponding to status as alive (1) or dead (0) in times $t+1$, t , and $t-1$, respectively.

size	A vector of names of variables coding size in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("sizea3", "sizea2", "sizea1")</code> .
repst	A vector of names of variables coding reproductive status in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("repstatus3", "repstatus2", "repstatus1")</code> .
matst	A vector of names of variables coding maturity status in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("matstatus3", "matstatus2", "matstatus1")</code> . Must be supplied if stages is not provided.
fec	A vector of names of variables coding fecundity in times $t+1$, t , and $t-1$, respectively. Defaults to <code>c("feca3", "feca2", "feca1")</code> .
repmatrix	A matrix composed mostly of 0s, with non-zero values for each potentially new individual (row) born to each reproductive stage (column). Non-zero entries correspond to multipliers for fecundity, with 1 equaling full fecundity.
overwrite	A data frame developed with the <code>overwrite()</code> function, describing transitions to be overwritten either with given values or with other estimated transitions.
yearcol	The variable name or column number corresponding to year in time t in the dataset.
popcol	The variable name or column number corresponding to the identity of the population.
patchcol	The variable name or column number corresponding to patch in the dataset.
indivcol	The variable name or column number coding individual identity.
sensorcol	The variable name or column number denoting the censor status. Only needed if <code>censor = TRUE</code> .
reduce	A logical value denoting whether to remove historical stages associated with only zero transitions. These are removed only if all row and column sums in ALL matrices estimated equal 0. Defaults to <code>FALSE</code> .

Value

If all inputs are properly formatted, then this function will return either an object of class `lefkMat`. Output includes:

A	A list of full projection matrices in order of sorted populations, patches, and years.
U	A list of survival-transition matrices sorted as in A.
F	A list of fecundity matrices sorted as in A.
hstages	A data frame matrix showing the pairing of ahistorical stages used to create historical stage pairs.
ahstages	A data frame detailing the characteristics of associated ahistorical stages.
labels	A data frame giving the population, patch, and year of each matrix in order.
matrixqc	A short vector describing the number of non-zero elements in U and F matrices, and the number of annual matrices.
dataqc	A vector showing the numbers of individuals and rows in the vertical dataset used as input.

Examples

```

data(cypdata)

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm",
                 "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
                          repstatus = repvector, obsstatus = obsvector,
                          matstatus = matvector, propstatus = propvector,
                          immstatus = immvector, indataset = indataset,
                          binhalfwidth = binvec)

cypraw_v1 <- verticalize3(data = cypdata, noyears = 6, firstyear = 2004,
                          patchidcol = "patch", individcol = "plantid",
                          blocksize = 4, size1col = "Inf2.04", size2col = "Inf.04",
                          size3col = "Veg.04", repstr1col = "Inf.04",
                          repstr2col = "Inf2.04", fec1col = "Pod.04",
                          stageassign = cypframe_raw, stagesize = "sizeadded",
                          NAas0 = TRUE, NRasRep = TRUE)

rep_cyp_raw <- matrix(0, 11, 11)
rep_cyp_raw[1:2,7:11] <- 0.5

cypover3r <- overwrite(stage3 = c("SD", "SD", "P1", "P1", "P2", "P3", "SL",
                                   "SL", "SL", "D", "XSm", "Sm", "D", "XSm", "Sm"),
                       stage2 = c("SD", "SD", "SD", "SD", "P1", "P2", "P3",
                                   "SL", "SL", "SL", "SL", "SL", "SL", "SL", "SL"),
                       stage1 = c("SD", "rep", "SD", "rep", "SD", "P1", "P2",
                                   "P3", "SL", "P3", "P3", "SL", "SL", "SL"),
                       eststage3 = c(NA, NA, NA, NA, NA, NA, NA, NA, NA, "D",
                                      "XSm", "Sm", "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA,
                                      NA, NA, NA, NA, NA, "XSm", "XSm", "XSm", "XSm", "XSm",
                                      "XSm"), eststage1 = c(NA, NA, NA, NA, NA, NA, NA, NA,
                                      "XSm", "XSm", "XSm", "XSm", "XSm", "XSm"),
                       givenrate = c(0.1, 0.1, 0.2, 0.2, 0.2, 0.2, 0.25, 0.4,
                                      0.4, NA, NA, NA, NA, NA, NA), type = c("S", "S", "S",
                                      "S", "S", "S", "S", "S", "S", "S", "S", "S",
                                      "S"))

cypmatrix3r <- rlefk3(data = cypraw_v1, stageframe = cypframe_raw, year = "all",
                      patch = "all", stages = c("stage3", "stage2", "stage1"),
                      size = c("size3added", "size2added", "size1added"),
                      repmatrix = rep_cyp_raw, overwrite = cypover3r,
                      yearcol = "year2", patchcol = "patchid", indivcol = "individ")

```

```
summary(cypmatrix3r)
```

sf_create

Create a Stageframe for Population Matrix Projection Analysis

Description

sf_create() returns a data frame describing each ahistorical life history stage. This data frame can be used as input into matrix-estimating functions such as [fleeko3\(\)](#), where it instructs the function as to the treatment of each stage during matrix creation.

Usage

```
sf_create(
  sizes,
  stagenames = NA,
  repstatus = 1,
  obsstatus = 1,
  propstatus = NA,
  immstatus = NA,
  matstatus = 1,
  minage = NA,
  maxage = NA,
  indataset = NA,
  binhalfwidth = 0.5,
  ipmbins = 100,
  roundsize = 5
)
```

Arguments

sizes	A numeric vector of the typical or representative size of each life history stage.
stagenames	An optional vector of stage names, in the same order as elements in sizes. If an IPM or function-based matrix with many stages is desired, then two stages that occur within the dataset and represent the lower and upper size limits of the IPM must be marked as ipm in this vector. Note that these stages must be mature stages, and should have all characteristics besides size equal. If two or more groups of stages, each with its own characteristics, are to be developed for IPM or function-based matrix development, then an even number of stages with two stages marking the minimum and maximum size of each group should be marked, with all other characteristics equal within each group.
repstatus	A vector denoting the binomial reproductive status of each life history stage. Defaults to 1.
obsstatus	A vector denoting the binomial observation status of each life history stage. Defaults to 1, but may be changed for unobservable stages.

propstatus	A vector denoting whether each life history stage is a propagule. Such stages are generally only used in fecundity estimation. Defaults to NA.
immstatus	A vector denoting whether each stage is immature. Must be composed of binomial values if given. Defaults to NA.
matstatus	A vector denoting whether each stage is mature. Must be composed of binomial values if given. Defaults to 1 for all stages defined in sizes.
minage	An optional vector denoting the minimum age at which a stage can begin. Only used in age x stage matrix development. Defaults to NA.
maxage	An optional vector denoting the maximum age at which a stage should end. Only used in age x stage matrix development. Defaults to NA.
indataset	A vector designating which stages are found within the dataset. While <code>rlefk2()</code> and <code>rlefk3()</code> can use all stages in the input dataset, <code>flefk3()</code> and <code>flefk2()</code> can only handle size-classified stages with non-overlapping combinations of size and reproductive status, plus one immature stage. In the latter scenario, other stages should be excluded by marking them as 0 in this vector.
binhalfwidth	A numeric vector giving the half-width of size bins. Used and required to classify individuals appropriately within size classes. Defaults to 0.5 for all sizes.
ipmbins	If an IPM is desired, then this parameter sets the number of stages to create for that IPM. This number is in addition to any stages that are not size-classified. Defaults to 100, and numbers greater than this yield a warning about the loss of statistical power and increasing chance of matrix over-parameterization resulting from increasing numbers of stages.
roundsize	This parameter sets the precision of size classification, and equals the number of digits used in rounding sizes. Defaults to 5.

Value

A stageframe object, which is a data frame that includes information on the stage name, size, reproductive status, observation status, propagule status, immaturity status, maturity status, presence within the core dataset, counts of similarly sized stages, raw bin half-width, and the minimum, center, and maximum of each size bin, as well as its width. If minimum and maximum ages were specified, then these are also included. Also includes an empty string variable that can be used to describe stages meaningfully. This object can be used as the stageframe input for `flefk3()`, `flefk2()`, `rlefk3()`, and `rlefk2()`.

Variables in this data frame include the following:

stagenames	The unique names of the stages to be analyzed.
size	The typical or representative size at which the stage occurs.
repstatus	A binomial variable designating whether the stage occurs is reproductive.
obsstatus	A binomial variable designating whether the stage occurs is observable.
propstatus	A binomial variable designating whether the stage occurs as a propagule.
immstatus	A binomial variable designating whether the stage occurs in immaturity.
matstatus	A binomial variable designating whether the stage occurs in maturity.
indataset	A binomial variable describing whether the stage occurs in the input dataset.

binhalfwidth_raw	The half-width input for the size bin corresponding to the stage.
sizebin_min	The minimum size at which the stage may occur.
sizebin_max	The maximum size at which the stage may occur.
sizebin_center	The centroid of the size bin at which the stage may occur.
sizebin_width	The width of the size bin corresponding to the stage.
min_age	The minimum age at which the stage may occur.
max_age	The maximum age at which the stage may occur.
comments	A text field to hold verbal stage descriptions.

Examples

```

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm", "Sm", "Md", "Lg",
                 "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
                        repstatus = repvector, obsstatus = obsvector,
                        matstatus = matvector, propstatus = propvector,
                        immstatus = immvector, indataset = indataset,
                        binhalfwidth = binvec)

cypframe_raw$comments[(cypframe_raw$stagenames == "SD")] <- "Dormant seed"
cypframe_raw$comments[(cypframe_raw$stagenames == "P1")] <- "1st yr protocorm"
cypframe_raw$comments[(cypframe_raw$stagenames == "P2")] <- "2nd yr protocorm"
cypframe_raw$comments[(cypframe_raw$stagenames == "P3")] <- "3rd yr protocorm"
cypframe_raw$comments[(cypframe_raw$stagenames == "SL")] <- "Seedling"
cypframe_raw$comments[(cypframe_raw$stagenames == "D")] <- "Dormant adult"
cypframe_raw$comments[(cypframe_raw$stagenames == "XSm")] <- "Extra small adult (1 shoot)"
cypframe_raw$comments[(cypframe_raw$stagenames == "Sm")] <- "Small adult (2-3 shoots)"
cypframe_raw$comments[(cypframe_raw$stagenames == "Md")] <- "Medium adult (4-5 shoots)"
cypframe_raw$comments[(cypframe_raw$stagenames == "Lg")] <- "Large adult (6-10 shoots)"
cypframe_raw$comments[(cypframe_raw$stagenames == "XLg")] <- "Extra large adult (>10 shoots)"

cypframe_raw

```

Description

stablestage3() is a generic function that returns the stable stage distribution for a population projection matrix or set of matrices. Unlike the 'popbio' package's [stable.stage\(\)](#) function, it is particularly made to handle very large and sparse matrices supplied as lefkoMat objects or as individual matrices. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
stablestage3(mats)
```

Arguments

mats A lefkoMat object, or population projection matrix, for which the stable stage distribution is desired.

Value

The value returned depends on the class of the mats argument.

See Also

[stablestage3.lefkoMat\(\)](#)
[stablestage3.matrix\(\)](#)

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)
```

```

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
                      stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefko3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
                  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
                  overwrite = lathover3, yearcol = "year2",
                  indivcol = "individ")

ehrlen3mean <- lmean(ehrlen3)
stablestage3(ehrlen3mean)

```

stablestage3.lefkoMat *Estimate Stable Stage Distribution for a lefkoMat Object*

Description

stablestage3.lefkoMat() returns the stable stage distributions for all \$A matrices in an object of class lefkoMat. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```

## S3 method for class 'lefkoMat'
stablestage3(mats)

```

Arguments

mats An object of class lefkoMat.

Value

This function returns the stable stage distributions corresponding to the matrices in a lefkoMat object. The stable stage distribution is given as the right eigenvector associated with largest real part of all eigenvalues estimated via the [eigs\(\)](#) function in package 'RSpectra' divided by the sum of the associated right eigenvector.

The actual output depends on whether the lefkoMat object used as input is ahistorical or historical. If the former, then a single data frame is output. This data frame includes the number of the matrix within the \$A element of the input lefkoMat object, followed by the original stage id, the new stage id (numeric and assigned through [sf_create\(\)](#)), the original given size, and the estimated proportion of the stable stage distribution within a variable called ss_prop.

If a historical matrix is used as input, then two data frames are output into a list object. The \$hist element contains a data frame where the stable stage distribution is given in terms of across-year

stage pairs. The structure includes the matrix number, the original and new designations for stages in times t and $t-1$, respectively, followed by the estimated proportion of the stable stage distribution for that matrix. The `$ahist` element contains the stable stage distribution in stages as given in the original stageframe. It includes a data frame with the new stage designation from the associated stageframe for the `lefkoMat` object, the corresponding matrix, and the stable stage distribution estimated as the sum of distribution elements from `$hist` corresponding to the equivalent stage in time t , irrespective of stage in time $t-1$.

See Also

`stablestage3()`
`stablestage3.matrix()`

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefko3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "indiv")

ehrlen3mean <- lmean(ehrlen3)
```



```
stablestage3(ehrlen3mean)
```

stablestage3.matrix	<i>Estimate Stable Stage Distribution for a Population Projection Matrix</i>
---------------------	--

Description

stablestage3.matrix() returns the stable stage distribution for a population projection matrix. This function can handle large and sparse matrices, and so can be used with large historical matrices, IPMs, age x stage matrices, as well as smaller ahistorical matrices.

Usage

```
## S3 method for class 'matrix'
stablestage3(mats)
```

Arguments

mats A population projection matrix of class matrix.

Value

This function returns the stable stage distribution corresponding to the input matrix. The stable stage distribution is given as the right eigenvector associated with largest real part of the eigenvalues estimated for the matrix via the [eigs\(\)](#) function in package 'RSpectra', divided by the sum of the associated right eigenvector.

See Also

[stablestage3\(\)](#)
[stablestage3.lefkoMat\(\)](#)

Examples

```
data(lathyrus)
sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VLa", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
```

```

      obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
      indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "Volume88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe,
  stagesize = "sizea", censorcol = "Missing1988",
  censorkeep = NA, censor = TRUE)

lathrepm <- matrix(0, 7, 7)
lathrepm[1, 6] <- 0.345
lathrepm[2, 6] <- 0.054

lathover3 <- overwrite(stage3 = c("Sd", "Sd", "Sd1"), stage2 = c("Sd", "Sd", "Sd"),
  stage1 = c("Sd", "rep", "rep"), givenrate = c(0.345, 0.054))

ehrlen3 <- rlefko3(data = lathvert, stageframe = lathframe, year = c(1989, 1990),
  stages = c("stage3", "stage2", "stage1"), repmatrix = lathrepm,
  overwrite = lathover3, yearcol = "year2",
  indivcol = "individ")

ehrlen3mean <- lmean(ehrlen3)
stablestage3(ehrlen3mean$A[[1]])

```

summary.lefkoMat

Summary of Class "lefkoMat"

Description

A function to simplify the viewing of basic information describing the matrices produced through functions `flefko3()`, `flefko2()`, `rlefko3()`, and `rlefko2()`.

Usage

```
## S3 method for class 'lefkoMat'
summary(object, ...)
```

Arguments

<code>object</code>	An object of class <code>lefkoMat</code> .
<code>...</code>	Other parameters.

Value

A summary of the object, showing the number of each type of matrix, the number of annual matrices, the number of estimated (non-zero) elements across all matrices and per matrix, the number of unique transitions in the dataset, and the number of individuals.

Examples

```

data(cypdata)

sizevector <- c(0, 0, 0, 0, 0, 0, 1, 2.5, 4.5, 8, 17.5)
stagevector <- c("SD", "P1", "P2", "P3", "SL", "D", "XSm",
                 "Sm", "Md", "Lg", "XLg")
repvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
obsvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
immvector <- c(0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1)
binvec <- c(0, 0, 0, 0, 0, 0, 0.5, 0.5, 1, 1, 2.5, 7)

cypframe_raw <- sf_create(sizes = sizevector, stagenames = stagevector,
                         repstatus = repvector, obsstatus = obsvector,
                         matstatus = matvector, propstatus = propvector,
                         immstatus = immvector, indataset = indataset,
                         binhalfwidth = binvec)

cypraw_v1 <- verticalize3(data = cypdata, noyears = 6, firstyear = 2004,
                        patchidcol = "patch", individcol = "plantid",
                        blocksize = 4, size1col = "Inf2.04", size2col = "Inf.04",
                        size3col = "Veg.04", repstr1col = "Inf.04",
                        repstr2col = "Inf2.04", fec1col = "Pod.04",
                        stageassign = cypframe_raw, stagesize = "sizeadded",
                        NAas0 = TRUE, NRasRep = TRUE)

rep_cyp_raw <- matrix(0, 11, 11)
rep_cyp_raw[1:2,7:11] <- 0.5

cypover2r <- overwrite(stage3 = c("SD", "P1", "P2", "P3", "SL", "SL", "D",
                                   "XSm", "Sm"), stage2 = c("SD", "SD", "P1", "P2", "P3",
                                   "SL", "SL", "SL", "SL"), eststage3 = c(NA, NA, NA, NA,
                                   NA, NA, "D", "XSm", "Sm"), eststage2 = c(NA, NA, NA, NA,
                                   NA, NA, "XSm", "XSm", "XSm"), givenrate = c(0.1, 0.2,
                                   0.2, 0.2, 0.25, 0.4, NA, NA, NA), type = c("S", "S", "S",
                                   "S", "S", "S", "S", "S"))

cypmatrix2r <- rlefko2(data = cypraw_v1, stageframe = cypframe_raw, year = "all",
                      patch = "all", stages = c("stage3", "stage2", "stage1"),
                      size = c("size3added", "size2added"),
                      repmatrix = rep_cyp_raw, overwrite = cypover2r,
                      yearcol = "year2", patchcol = "patchid",
                      indivcol = "indiv")

summary(cypmatrix2r)

```

Description

A function to simplify the immediate viewable output for an R object of class `lefkoMod`. This function shows the best-fit models, summarizes the numbers of models in the model tables, shows the criterion used to determine the best-fit models, and provides some basic quality control information about the models.

Usage

```
## S3 method for class 'lefkoMod'
summary(object, ...)
```

Arguments

`object` An R object of class `lefkoMod` resulting from `modelsearch()`.
`...` Other parameters.

Value

A summary of the object, showing the best-fit models for all vital rates, with constants of 0 or 1 used for unestimated models. This is followed by a summary of the number of models tested per vital rate, and a table showing the names of the parameters used to model vital rates and represent tested factors. At the end is a section describing the number of individuals and individual transitions used to estimate each vital rate.

Examples

```
data(lathyrus)

sizevector <- c(0, 4.6, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9)
stagevector <- c("Sd", "Sd1", "Dorm", "Sz1nr", "Sz2nr", "Sz3nr", "Sz4nr", "Sz5nr",
  "Sz6nr", "Sz7nr", "Sz8nr", "Sz9nr", "Sz1r", "Sz2r", "Sz3r", "Sz4r",
  "Sz5r", "Sz6r", "Sz7r", "Sz8r", "Sz9r")
repvector <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1)
obsvector <- c(0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
matvector <- c(0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)
binvec <- c(0, 4.6, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5,
  0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5)

lathframe1n <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
  obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
  indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert1n <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
  individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
  size1col = "lnVol88", repstr1col = "FCODE88",
  fec1col = "Intactseed88", dead1col = "Dead1988",
  nonobs1col = "Dormant1988", stageassign = lathframe1n,
```

```

      stagesize = "sizea", censorcol = "Missing1988",
      censorkeep = NA, NAas0 = TRUE, censor = TRUE)

lathvertln$feca2 <- round(lathvertln$feca2)
lathvertln$feca1 <- round(lathvertln$feca1)
lathvertln$feca3 <- round(lathvertln$feca3)

lathmodelsln2 <- modelsearch(lathvertln, historical = FALSE, approach = "lme4", suite = "main",
  vitalrates = c("surv", "obs", "size", "repst", "fec"),
  juvestimate = "Sd1", bestfit = "AICc&k", sizedist = "gaussian",
  fecdist = "poisson", indiv = "individ", patch = "patchid",
  year = "year2", year.as.random = TRUE, patch.as.random = TRUE,
  show.model.tables = TRUE)

summary(lathmodelsln2)

```

verticalize3

Create Historical Vertical Data Frames From Horizontal Data Frames

Description

verticalize3() returns a vertically formatted demographic data frame organized to create historical projection matrices, given a horizontally formatted input data frame.

Usage

```

verticalize3(
  data,
  noyears,
  firstyear,
  popidcol = 0,
  patchidcol = 0,
  individcol = 0,
  blocksize,
  xcol = 0,
  ycol = 0,
  juvcol = 0,
  size1col,
  size2col = 0,
  size3col = 0,
  repstr1col = 0,
  repstr2col = 0,
  fec1col = 0,
  fec2col = 0,
  alive1col = 0,
  dead1col = 0,

```

```

obs1col = 0,
nonobs1col = 0,
censorcol = 0,
repstrrel = 1,
fecrel = 1,
stagecol = 0,
stageassign = NA,
stagesize = NA,
censorkeep = 0,
censor = FALSE,
spacing = NA,
NAas0 = FALSE,
NRasRep = FALSE,
reduce = TRUE
)

```

Arguments

<code>data</code>	The horizontal data file.
<code>noyears</code>	The number of years or observation periods in the dataset.
<code>firstyear</code>	The first year or time of observation.
<code>popidcol</code>	A variable name or column number corresponding to the identity of the population for each individual.
<code>patchidcol</code>	A variable name or column number corresponding to the identity of the patch for each individual, if patches have been designated within populations.
<code>individcol</code>	A variable name or column number corresponding to the identity of each individual.
<code>blocksize</code>	The number of variables corresponding to each time step in the input dataset designated in data.
<code>xcol</code>	A variable name or column number corresponding to the x coordinate of each individual in Cartesian space.
<code>ycol</code>	A variable name or column number corresponding to the y coordinate of each individual in Cartesian space.
<code>juvcol</code>	A variable name or column number that marks individuals in immature stages within the dataset. The <code>verticalize3()</code> function assumes that immature individuals are identified in this variable marked with a number equal to or greater than 1, and that mature individuals are marked as 0 or NA.
<code>size1col</code>	A variable name or column number corresponding to the size entry associated with the first year or observation time in the dataset.
<code>size2col</code>	A second variable name or column number corresponding to the size entry associated with the first year or observation time in the dataset.
<code>size3col</code>	A third variable name or column number corresponding to the size entry associated with the first year or observation time in the dataset.

repstr1col	A variable name or column number corresponding to the production of reproductive structures, such as flowers, associated with the first year or observation period in the input dataset. This can be binomial or count data, and is used to in analysis of the probability of reproduction.
repstr2col	A second variable name or column number corresponding to the production of reproductive structures, such as flowers, associated with the first year or observation period in the input dataset. This can be binomial or count data, and is used to in analysis of the probability of reproduction.
fec1col	A variable name or column number denoting fecundity associated with the first year or observation time in the input dataset. This may represent egg counts, fruit counts, seed production, etc.
fec2col	A second variable name or column number denoting fecundity associated with the first year or observation time in the input dataset. This may represent egg counts, fruit counts, seed production, etc.
alive1col	A variable name or column number that provides information an whether an individual is alive at a given time. If used, living status must be designated as binomial (living = 1, dead = 0).
dead1col	A variable name or column number that provides information an whether an individual is alive at a given time. If used, dead status must be designated as binomial (dead = 1, living = 0).
obs1col	A variable name or column number providing information on whether an individual is in an observable stage at a given time. If used, observation status must be designated as binomial (observed = 1, not observed = 0).
nonobs1col	A variable name or column number providing information on whether an individual is in an unobservable stage at a given time. If used, observation status must be designated as binomial (observed = 0, not observed = 1).
censorcol	A variable name or column number corresponding to the first entry of a censor variable, used to distinguish between entries to use and entries not to use, or to designate entries with special issues that require further attention. If used, this should be associated with the first year or observation time, and all other years or times must also have censor columns.
repstrrel	This is a scalar modifier for that makes the variable in repstr2col equivalent to repstr1col. This can be useful if two reproductive status variables have related but unequal units, for example if repstr1col refers to one-flowered stems while repstr2col refers to two-flowered stems. Defaults to 1.
fecrel	This is a scalar modifier for that makes the variable in fec2col equivalent to fec1col. This can be useful if two fecundity variables have related but unequal units. Defaults to 1.
stagecol	Optional variable name or column number corresponding to life history stage at a given time.
stageassign	The stageframe object identifying the life history model being operationalized. Note that if stagecol is provided, then this stageframe is not used for stage designation.
stagesize	A variable name or column number describing which size variable to use in stage estimation. Defaults to NA, and can also take sizea, sizeb, sizec, or sizeadded, depending on which size variable is chosen.

sensorkeep	The value of the censoring variable identifying data that should be included in analysis. Defaults to 0, but may take any value including NA.
censor	A logical variable determining whether the output data should be censored using the variable defined in <code>censorcol</code> . Defaults to FALSE.
spacing	The spacing at which density should be estimated, if density estimation is desired and x and y coordinates are supplied. Given in the same units as those used in the x and y coordinates given in <code>xcol</code> and <code>ycol</code> . Defaults to NA.
NAas0	If TRUE, then all NA entries for size and fecundity variables will be set to 0. This can help increase the sample size analyzed by <code>modelsearch()</code> , but should only be used when it is clear that this substitution is biologically realistic. Defaults to FALSE.
NRasRep	If TRUE, then will treat non-reproductive but mature individuals as reproductive during stage assignment. This can be useful, for example, when a matrix is desired without separation of reproductive and non-reproductive but mature stages of the same size. Only used if <code>stageassign</code> is set to a stageframe. Defaults to FALSE.
reduce	A logical variable determining whether invariant state variables should be removed from the output dataset. For example, if all living individuals are always observable, then variables identifying observation status are invariant and can be removed. Defaults to TRUE.

Value

If all inputs are properly formatted, then this function will output a historical vertical data frame, meaning that the output data frame will have three consecutive years of size and reproductive data per individual per row. This data frame is in standard format for all functions used in `lefko3`, and so can be used without further modification.

Variables in this data frame include the following:

rowid	Unique identifier for the row of the data frame.
popid	Unique identifier for the population, if given.
patchid	Unique identifier for patch within population, if given.
individ	Unique identifier for the individual.
year2	Year or time step at time t .
xpos, ypos	X and Y position in Cartesian space, if given.
sizea1, sizea2, sizea3	Main size measurement in times $t-1$, t , and $t+1$, respectively.
sizeb1, sizeb2, sizeb3	Secondary size measurement in times $t-1$, t , and $t+1$, respectively.
sizec1, sizec2, sizec3	Tertiary measurement in times $t-1$, t , and $t+1$, respectively.
sensor1, sensor2, sensor3	Sensor state values in times $t-1$, t , and $t+1$.
repstra1, repstrb1, repstrc1	Main, secondary, and tertiary numbers of reproductive structures in time $t-1$.

repstra2, repstrb2, repstrc2	Main, secondary, and tertiary numbers of reproductive structures in time t .
repstra3, repstrb3, repstrc3	Main, secondary, and tertiary numbers of reproductive structures in time $t+1$.
feca1, fecb1	Main and secondary numbers of offspring in time $t-1$.
feca2, fecb2	Main and secondary numbers of offspring in time t .
feca3, fecb3	Main and secondary numbers of offspring in time $t+1$.
size1added, size2added, size3added	Sum of primary, secondary, and tertiary size measurements in times $t-1$, t , and $t+1$, respectively.
repstr1added, repstr2added, repstr3added	Sum of primary, secondary, and tertiary reproductive structures in times $t-1$, t , and $t+1$, respectively.
fec1added, fec2added, fec3added	Sum of primary and secondary fecundity in times $t-1$, t , and $t+1$, respectively.
obsstatus1, obsstatus2, obsstatus3	Binomial observation state in times $t-1$, t , and $t+1$, respectively.
repstatus1, repstatus2, repstatus3	Binomial reproductive state in times $t-1$, t , and $t+1$, respectively.
fecstatus1, fecstatus2, fecstatus3	Binomial offspring production state in times $t-1$, t , and $t+1$, respectively.
firstseen	Year or time step of first observation.
lastseen	Year or time step of last observation.
xcorr, ycorr	Overall x and y coordinates of individual in Cartesian space.
alive1, alive2, alive3	Binomial state as alive in times $t-1$, t , and $t+1$, respectively.
obsage	Observed age in time t , assuming first observation corresponds to age = 0.
obslifespan	Observed lifespan, given as 'lastseen - firstseen + 1'.
matstatus1, matstatus2, matstatus3	Binomial state as mature.
density	Density of individuals per unit designated in 'spacing'. Only given if spacing is not NA.

Examples

```
data(lathyrus)

sizevector <- c(0, 100, 13, 127, 3730, 3800, 0)
stagevector <- c("Sd", "Sd1", "VSm", "Sm", "VL", "Flo", "Dorm")
repvector <- c(0, 0, 0, 0, 0, 1, 0)
obsvector <- c(0, 1, 1, 1, 1, 1, 0)
matvector <- c(0, 0, 1, 1, 1, 1, 1)
immvector <- c(1, 1, 0, 0, 0, 0, 0)
propvector <- c(1, 0, 0, 0, 0, 0, 0)
indataset <- c(0, 1, 1, 1, 1, 1, 1)
```

```
binvec <- c(0, 100, 11, 103, 3500, 3800, 0.5)

lathframe <- sf_create(sizes = sizevector, stagenames = stagevector, repstatus = repvector,
                      obsstatus = obsvector, matstatus = matvector, immstatus = immvector,
                      indataset = indataset, binhalfwidth = binvec, propstatus = propvector)

lathvert <- verticalize3(lathyrus, noyears = 4, firstyear = 1988, patchidcol = "SUBPLOT",
                        individcol = "GENET", blocksize = 9, juvcol = "Seedling1988",
                        size1col = "Volume88", repstr1col = "FCODE88",
                        fec1col = "Intactseed88", dead1col = "Dead1988",
                        nonobs1col = "Dormant1988", stageassign = lathframe,
                        stagesize = "sizea", censorcol = "Missing1988",
                        censorkeep = NA, censor = TRUE)

summary(lathvert)
```

Index

- * **datasets**
 - cypdata, [2](#)
 - cypvert, [4](#)
 - lathyrus, [27](#)
- cypdata, [2](#)
- cypvert, [4](#)
- dredge, [36](#)
- eigs, [24](#), [26](#), [41](#), [43](#), [55](#), [57](#)
- flefko2, [6](#), [38](#), [52](#), [58](#)
- flefko3, [11](#), [38](#), [51](#), [52](#), [58](#)
- glmer, [36](#)
- glmmTMB, [36](#)
- historicalize3, [16](#), [33](#)
- lambda, [22](#)
- lambda3, [22](#), [24](#), [26](#)
- lambda3.lefkoMat, [23](#), [24](#), [36](#)
- lambda3.matrix, [23](#), [24](#), [25](#)
- lathyrus, [27](#)
- lefko3, [29](#)
- lmean, [30](#)
- modelsearch, [20](#), [32](#), [60](#), [64](#)
- overwrite, [14](#), [37](#), [46](#), [49](#)
- reproductive.value, [39](#)
- repvalue3, [39](#), [41](#), [43](#)
- repvalue3.lefkoMat, [40](#), [41](#), [43](#)
- repvalue3.matrix, [40](#), [41](#), [42](#)
- rlefko2, [6](#), [38](#), [44](#), [52](#), [58](#)
- rlefko3, [11](#), [38](#), [47](#), [52](#), [58](#)
- sf_create, [41](#), [51](#), [55](#)
- stable.stage, [54](#)
- stablestage3, [53](#), [56](#), [57](#)
- stablestage3.lefkoMat, [54](#), [55](#), [57](#)
- stablestage3.matrix, [54](#), [56](#), [57](#)
- summary.lefkoMat, [58](#)
- summary.lefkoMod, [59](#)
- verticalize3, [33](#), [36](#), [45](#), [48](#), [61](#)