

# Package 'lsmeans'

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**Type** Package

**Title** Least-Squares Means

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**Imports** estimability, graphics, stats, utils, nlme, coda (>= 0.17), multcomp, plyr, mvtnorm, xtable (>= 1.8-2)

**Additional\_repositories** <http://glmmadmb.r-forge.r-project.org/repos>

**BugReports** <https://github.com/rvlenth/lsmeans/issues>

**LazyData** yes

**ByteCompile** yes

**Description** Obtain least-squares means for many linear, generalized linear, and mixed models. Compute contrasts or linear functions of least-squares means, and comparisons of slopes. Plots and compact letter displays. Least-squares means were proposed in Harvey, W (1960) "Least-squares analysis of data with unequal subclass numbers", Tech Report ARS-20-8, USDA National Agricultural Library, and discussed further in Searle, Speed, and Milliken (1980) "Population marginal means in the linear model: An alternative to least squares means", The American Statistician 34(4), 216-221 <doi:10.1080/00031305.1980.10483031>. NOTE: Users are encouraged to switch to the 'emmeans' package, as 'lsmeans' will be archived in the not-too-distant future.

**License** GPL-2 | GPL-3

**NeedsCompilation** no

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lsmeans-package	<i>Least-squares means</i>
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## Description

This package provides methods for obtaining so-called least-squares means for factor combinations in a variety of fitted linear models. It can also compute contrasts or linear combinations of these least-squares means, (several standard contrast families are provided), and in addition can estimate and contrast slopes of trend lines. Popular adjustments for multiple-comparisons are provided, as well as graphical ways of displaying the results.

## Details

Package:	lsmeans
Type:	Package
License:	GPL-2
Other information:	See DESCRIPTION

## Overview

**Concept** Least-squares means (see Searle *et al.* 1980, who prefer the term “predicted marginal means” (PMM)) are popular for summarizing linear models that include factors. For balanced experimental designs, they are just the marginal means. For unbalanced data, they in essence estimate what you *would* have observed that the data arisen from a balanced experiment.

**Reference grids** The implementation in **lsmeans** relies on our own concept of a *reference grid*, which is an array of factor and predictor levels. Predictions are made on this grid, and least-squares means are defined as averages of these predictions over zero or more dimensions of the grid. The function `ref.grid` explicitly creates a reference grid (`ref.grid` object) that can subsequently be used to obtain least-squares means. The `update` method is used to change its properties.

Our reference-grid framework expands slightly upon Searle *et al.*'s definitions of PMMs, in that it is possible to include multiple levels of covariates in the grid.

**Models supported** Many linear models are supported by the package, including `lm`, `glm`, `avList`, and `mlm` in the **stats** package, as well as fitted-model objects from several contributed packages including **nlme**, **lme4**, **survival**, and **geepack**. The help page for `models` provides more details, including, in some cases, additional `ref.grid` arguments that might affect the subsequent analysis. Also, some models require other packages be installed in order to obtain all the available features.

**Least-squares means** The `lsmeans` function computes least-squares means given a `ref.grid` object or a fitted model, and a specification indicating what factors to include. The `lstrends` function creates the same sort of results for estimating and comparing slopes of fitted lines. Both return an `lsmobj` object very much like a reference grid, but with possibly fewer factors involved.

**Summaries and analysis** The `summary` method may be used to display a `ref.grid` or an `lsmobj`. Special-purpose summaries are available via `confint` and `test`, the latter of which can also do a joint test of several estimates. The user may specify by variables, multiplicity-adjustment methods, confidence levels, etc., and if a transformation or link function is involved, may reverse-transform the results to the response scale.

**Contrasts and comparisons** The `contrast` method is used to obtain contrasts among the estimates; several standard contrast families are available such as deviations from the mean, polynomial contrasts, and comparisons with one or more controls. Another `lsmobj` object is returned, which can be summarized or further analyzed. For convenience, a `pairs` method is provided for the case of pairwise comparisons. Related to this is the `cld` method, which provides a compact letter display for grouping pairs of means that are not significantly different. `cld` requires the **multcompView** package.

**Graphs** The `plot` method will display side-by-side confidence intervals for the estimates, and/or ‘comparison arrows’ whereby the significance of pairwise differences can be judged by how much they overlap. The `lsmip` function displays estimates like an interaction plot, multi-paneled if there are by variables. These graphics capabilities require the **lattice** package be installed.

**multcomp interface** The `as.glht` function and `glht` method for `lsmobjs` provide an interface to the `glht` function in the **multcomp** package, thus providing for more exacting simultaneous

estimation or testing. The package also provides an `lsm` method that works as an alternative to `mcp` in a call to `glht`.

### Additional information

Examples and discussion are available via `vignette("using-lsmeans", package="lsmeans")`.

Some features of the **lsmeans** require (or are enhanced by) additional packages that are loaded when needed. Since they are not “required” packages, they are not automatically installed with **lsmeans**. We highly recommend that users also install the following packages: **multcomp** (if `cld`, `glht`, or `as.glht` are to be used), **multcompView** (for `cld`), **lattice** (for `plot` and `lsmip`), and **lmerTest** or **pbkrtest** (for models fitted by the **lme4** package).

Starting with **lsmeans** version 2, a new object framework based on *reference grids* is used that increases flexibility and provides for extending its capabilities to additional model objects. Use `vignette("lsmeans-changes")` for information on the user impact of these changes.

It is possible to write your own interfaces for models not yet supported by **lsmeans**. See the help page `extending-lsmeans` and `vignette("extending")` for details on how to do this.

### Author(s)

Russell V. Lenth (author), Maxime Hervé (contributor)

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### References

Russell V. Lenth (2016) Least-Squares Means: The R Package `lsmeans`. *Journal of Statistical Software*, 69(1), 1-33. doi:10.18637/jss.v069.i01

Searle S.R. Speed F.M. Milliken G.A. (1980) Population marginal means in the linear model: An alternative to least squares means. *The American Statistician* **34**(4), 216-221.

---

add\_grouping

*Create a grouping factor*

---

### Description

A new factor `G` can be defined having levels based on those of an existing factor `A`. This adds `G` to the reference grid and redefines `A` as being nested in `G`.

### Usage

```
add_grouping(object, newname, refname, newlevs)
```

**Arguments**

object	A <a href="#">ref.grid</a> object
newname	Character name of the grouping factor to be created
refname	Character name of an existing factor in object whose levels are to be grouped
newlevs	Character vector or factor of the same length as the levels for refname. Each element specifies the corresponding level for newname

**Details**

This function is useful when one wants to group certain levels of some treatment factor together and summarize by those groups – without fitting a new model. For example, suppose a factor `hosp` refers to five hospitals. A call like `newgrid <- add_grouping(refgrid, "envir", "hosp", c("rural", "urban", "urban", "urban", "urban"))` would add a two-level grouping factor named `envir` in which the first and fourth hospitals are rural and the others are urban. Subsequently, we may use `lsmeans(newgrid, "envir")` to obtain the marginal means for the rural and urban environments.

If `newlevs` is specified as a factor, the user can use its `levels` attribute to control the order in which levels are presented. Otherwise, it will be alphabetical.

**Value**

A `ref.grid` object with the factor `newname` added. It will include a nesting structure such that `refname` is nested in `newname`, and with `newname` added to any existing nesting that involves `refname`.

**Note**

If object already has `refname` nested in some other factors, this creates a conflict and therefore it is not allowed; an error is returned.

**Author(s)**

Russell V. Lenth

**See Also**

[ref.grid](#)

**Examples**

```
require("lsmeans")

fiber.lm <- lm(strength ~ diameter + machine, data = fiber)
frg <- ref.grid(fiber.lm)

## Suppose the machines are of two types
gfrg <- add_grouping(frg, newname = "type", refname = "machine",
                    newlevs = c("computerized", "computerized", "manual"))
gfrg
```

```
lsmeans(gfrg, "type", contr = "pairwise")
```

---

auto.noise

*Auto Pollution Filter Noise*

---

### Description

Three-factor experiment comparing pollution-filter noise for two filters, three sizes of cars, and two sides of the car.

### Usage

```
auto.noise
```

### Format

A data frame with 36 observations on the following 4 variables.

noise Noise level in decibels - a numeric vector.

size The size of the vehicle - an ordered factor with levels S, M, L.

type Type of anti-pollution filter - a factor with levels Std and Octel

side The side of the car where measurement was taken – a factor with levels L and R.

### Details

The data are from a statement by Texaco, Inc., to the Air and Water Pollution Subcommittee of the Senate Public Works Committee on June 26, 1973. Mr. John McKinley, President of Texaco, cited an automobile filter developed by Associated Octel Company as effective in reducing pollution. However, questions had been raised about the effects of filters on vehicle performance, fuel consumption, exhaust gas back pressure, and silencing. On the last question, he referred to the data included here as evidence that the silencing properties of the Octel filter were at least equal to those of standard silencers.

### Source

The dataset was imported from the Data and Story Library - <http://lib.stat.cmu.edu/DASL/Datafiles/airpullutionfiltersdat.html> (sic). However, the factor levels were assigned meaningful names, and the observations were sorted in random order as if this were the run order of the experiment.

### References

A.Y. Lewin and M.F. Shakun (1976) *Policy Sciences: Methodology and Cases*. Pergammon Press. p.313.

## Examples

```
require(lsmmeans)
noise.lm <- lm(noise ~ size * type * side, data = auto.noise)

# Interaction plot of predictions
lsmip(noise.lm, type ~ size | side)

# Confidence intervals
plot(lsmmeans(noise.lm, ~ size | side*type))
```

---

cld

*Compact letter display of pairwise comparisons*


---

## Description

Extract and display information on all pairwise comparisons of least-squares means.

## Usage

```
## S3 method for class 'ref.grid'
cld(object, details = FALSE, sort = TRUE, by, alpha = 0.05,
     Letters = c("1234567890", LETTERS, letters), reversed = FALSE, ...)
## S3 method for class 'lsm.list'
cld(object, ..., which = 1)
```

## Arguments

object	An object of class <code>ref.grid</code>
details	Logical value determining whether detailed information on tests of pairwise comparisons is displayed
sort	Logical value determining whether the LS means are sorted before the comparisons are produced. When <code>sort</code> is <code>TRUE</code> , the results are displayed in increasing order if <code>reversed</code> is <code>FALSE</code> (the default), or in decreasing order if <code>reversed</code> is <code>TRUE</code> .
by	Character value giving the name or names of variables by which separate families of comparisons are tested. If <code>NULL</code> , all means are compared. If missing, and a <code>by</code> variable was used in creating object, it is used as the <code>by</code> variable in <code>cld</code> .
alpha	Numeric value giving the significance level for the comparisons
Letters	Character vector of letters to use in the display. Any strings of length greater than 1 are expanded into individual characters
reversed	Logical value (passed to <code>multcompLetters</code> in the <code>multcompView</code> package.) If <code>TRUE</code> , the order of use of the letters is reversed. In addition, if both <code>sort</code> and <code>reversed</code> are <code>TRUE</code> , the sort order of results is reversed.
...	Arguments passed to <code>contrast</code> (for example, an <code>adjust</code> method)
which	When object is a list, this determines which element is analyzed.

## Details

This function uses the Piepho (2004) algorithm (as implemented in the **multcompView** package) to generate a compact letter display of all pairwise comparisons of least-squares means. The function obtains (possibly adjusted)  $P$  values for all pairwise comparisons of means, using the `contrast` function with `method = "pairwise"`. When a  $P$  value exceeds  $\alpha$ , then the two means have at least one letter in common.

## Value

When `details == FALSE`, an object of class `summary.ref.grid` (which inherits from `data.frame`) showing the summary of LS means with an added column named `.groups` with the `cld` information. When `details == TRUE`, a list the object just described, as well as the summary of the contrast results showing each comparison, its estimate, standard error,  $t$  ratio, and adjusted  $P$  value.

## Note

This function requires the **multcompView** package to be installed. Otherwise an error message is produced.

## Author(s)

Russell V. Lenth

## References

Hans-Peter Piepho (2004) An algorithm for a letter-based representation of all pairwise comparisons, *Journal of Computational and Graphical Statistics*, 13(2), 456-466.

## See Also

`cld` in the **multcomp** package

## Examples

```
warp.lm <- lm(breaks ~ wool * tension, data = warpbreaks)
warp.lsm <- lsmeans(warp.lm, ~ tension | wool)
cld(warp.lsm) # implicitly uses by = "wool"
cld(warp.lsm, by = "tension") # overrides implicit 'by'

# Mimic grouping bars and compare all 6 means
cld(warp.lsm, by = NULL, Letters = "||||||", alpha = .01)
```



---

contrast                      *Methods for obtaining analyses ref.grid and lsmobj objects*

---

## Description

These methods provide for analyses of `ref.grid` objects, or follow-up analyses of `lsmobj` objects: Contrasts, pairwise comparisons, tests, and confidence intervals.

## Usage

```
## S3 method for class 'ref.grid'
contrast(object, method = "eff", interaction = FALSE,
         by, offset = NULL, name = "contrast",
         options = getOption("lsmeans")$contrast, adjust, ...)
## S3 method for class 'lsm.list'
contrast(object, ..., which = 1)

## S3 method for class 'ref.grid'
test(object, null = 0, joint = FALSE,
     verbose = FALSE, rows, by, ...)

## S3 method for class 'ref.grid'
confint(object, parm, level = 0.95, ...)

## S3 method for class 'ref.grid'
pairs(x, reverse = FALSE, ...)

## S3 method for class 'ref.grid'
coef(object, ...)
```

## Arguments

<code>object, x</code>	An object of class <code>"ref.grid"</code> or its extension, <code>"lsmobj"</code> .
<code>method</code>	Character value giving the root name of a contrast method (e.g. <code>"pairwise"</code> ). Alternatively, a named list of contrast coefficients that must each conform to the number of least-squares means in each by group. This is just like the <code>contr</code> argument in <code>lsmeans</code> . To identify the available methods, see <code>ls("package:lsmeans", pat=".lsmc")</code> . You may define your own <code>.lsmc</code> function and use its root name as <code>method</code> . If <code>interaction</code> is of character type, this argument is ignored.
<code>interaction</code>	Character vector or logical value. In multi-factor situations with <code>interaction = FALSE</code> , the factor combinations are treated as levels of a single "uber-factor", and the contrast specified in <code>method</code> is applied to it. Otherwise, interaction contrasts are computed: Contrasts are generated for each factor separately, one at a time; and these contrasts are applied to the object (the first time around) or to the

previous result (subsequently). (Any factors specified in `by` are skipped.) The final result comprises contrasts of contrasts, or, equivalently, products of contrasts for the factors involved. Processing is done in the order of appearance in `object@levels`. With `interaction = TRUE`, `method` (if specified as character) is used for each contrast. If `interaction` is a character vector, the elements specify the respective contrast method(s); they are recycled as needed.

<code>by</code>	Character names of variable(s) to be used for “by” groups. The contrasts or joint tests will be evaluated separately for each combination of these variables. If <code>object</code> was created with <code>by</code> groups, those are used unless overridden. Use <code>by = NULL</code> to use no by groups at all.
<code>offset</code>	Numeric vector of the same length as each by group. These values are added to their respective linear estimates. This argument is ignored when <code>interaction</code> is not <code>FALSE</code> .
<code>name</code>	Name to use to label the contrasts in table headings or subsequent contrasts of the returned object. This argument is ignored when <code>interaction</code> is not <code>FALSE</code> .
<code>options</code>	If non-NULL, a named list of arguments to pass to <code>update</code> , just after the object is constructed.
<code>adjust</code>	Method to use for adjusting $P$ values. This is passed to <code>summary</code> . This argument is available in <code>contrast</code> for historical reasons; but it is better style to specify the adjustment method, along with other testing options such as <code>side</code> , as part of <code>options</code> .
<code>joint</code>	Logical value. If <code>FALSE</code> , the arguments are passed to <code>summary</code> with <code>infer=c(FALSE, TRUE)</code> . If <code>TRUE</code> , a joint test of the hypothesis $L\beta = \text{null}$ is performed, where $L$ is <code>object@linfct</code> and $\beta$ is the vector of fixed effects estimated by <code>object@betahat</code> . This will be either an $F$ test or a chi-square (Wald) test depending on whether degrees of freedom are available.
<code>rows</code>	Integer values. The rows of $L$ to be tested in the joint test. If missing, all rows of $L$ are used. If not missing, by variables are ignored.
<code>null</code>	Numeric value specifying the null value(s) being tested against. It may be either a single value, in which case it is used as the null value for all linear functions under test; or a numeric vector of length equal to the number of linear functions.
<code>parm</code>	This is ignored, but it is a required argument of the generic <code>confint</code> method.)
<code>verbose</code>	Logical value. If <code>TRUE</code> and <code>joint==TRUE</code> , a table of the effects being tested is printed.
<code>level</code>	Numeric value of the desired confidence level.
<code>which</code>	When <code>object</code> is a list of <code>lsmobj</code> objects, this specifies which member of the list is analyzed.
<code>reverse</code>	Logical value determining whether “pairwise” or “revpairwise” pairwise comparisons are generated.
<code>...</code>	Additional arguments passed to <code>summary</code> or to a contrast function.

### Details

Though `contrast` is ordinarily used to create true contrasts (whose coefficients sum to zero), it may be used to estimate any linear function of the LS means; and `offset` expands this capability further by allowing additive constants. `pairs` is equivalent to `contrast` with `method = "pairwise"`.

`confint` and `test` (when `JOINT==FALSE`) are equivalent to calling `summary` with `infer=c(TRUE,FALSE)` and `infer=c(FALSE,TRUE)`, respectively.

When using `test` to do a joint test of  $L\beta = \text{null}$ , an error is thrown if any row of  $L$  is non-estimable. It is permissible for the rows of  $L$  to be linearly dependent as long as `null == 0`; a reduced set of contrasts is tested. Linear dependence and nonzero `null` cause an error.

## Value

`contrast` and `pairs` return an object of class `"lsmobj"`, which is an extension of `"ref.grid"`. Consequently, they may be used as arguments to other `"lsmobj"` or `"ref.grid"` methods. The user may, for example, compute contrasts of contrasts, or re-summarize a set of confidence intervals with a different by grouping or confidence level. The "grid" for the returned value is simply the set of variables that identify the results. For example, `contrast`'s return value is a reference grid for one factor named `contrast`.

`confint` and `test` (when `Joint==FALSE`) return an object of class `summary.ref.grid`. When `JOINT==TRUE`, `test` returns a `"summary.ref.grid"` object (extends `"data.frame"`) with the test statistic, degrees of freedom, and  $P$  value for each by group.

When object is the result of a call to `contrast` or `pairs`, the `coef` method returns a `data.frame`. The initial columns are the factor combinations that were contrasted (i.e. the grid for the object originally specified in the call to `contrast`), and the remaining columns (named `c.1`, `c.2`, ...) contain the contrast coefficients that were applied to the corresponding predictions. If object was not produced via `contrast`, `NULL` is returned, along with a message.

## Author(s)

Russell V. Lenth

## See Also

Additional `"lsmobj"` methods having their own help pages are `cld` and `glht`. Also, the `summary` and other methods for `"ref.grid"` objects also work for `"lsmobj"` objects.

## Examples

```
require(lsmmeans)
warp.lm <- lm(breaks ~ wool*tension, data = warpbreaks)
warp.lsm <- lsmmeans(warp.lm, ~ tension | wool)

# Polynomial contrasts of tension, by wool
(warp.pl <- contrast(warp.lsm, "poly", name = "order"))
# Same results with a different adjustment
summary(warp.pl, adjust = "fdr")

# Jointly test the tension effects for each wool
test(warp.pl, joint = TRUE, by = "wool")

# Compare the two contrasts for each order
contrast(warp.pl, "revpairwise", by = "order")

# User-provided contrasts, ignoring the previous by grouping
```

```

contrast(warp.lsm,
  list(c1=c(1,0,0,-1,0,0), c2=c(1,1,1,-1,-1,-1)/3),
  by = NULL)

# Compare consecutive tension*wool comb's as treatment with 6 levels
contrast(warp.lsm, "consec", by = NULL)

# Interaction contrasts (comparisons of linear and quadratic contrasts)
(int.con <- contrast(warp.lsm, interaction = c("poly", "consec"), by = NULL))

# See the contrast coefficients used by the previous call
coef(int.con)

```

---

feedlot

*Feedlot data*

---

### Description

This is an unbalanced analysis-of-covariance example, where one covariate is affected by a factor. Feeder calves from various herds enter a feedlot, where they are fed one of three diets. The weight of the animal at entry is the covariate, and the weight at slaughter is the response.

### Usage

```
data(feedlot)
```

### Format

A data frame with 67 observations on the following 4 variables.

**herd** a factor with levels 9 16 3 32 24 31 19 36 34 35 33, designating the herd that a feeder calf came from.

**diet** a factor with levels Low Medium High: the energy level of the diet given the animal.

**swt** a numeric vector: the weight of the animal at slaughter.

**ewt** a numeric vector: the weight of the animal at entry to the feedlot.

### Details

The data arise from a Western Regional Research Project conducted at New Mexico State University. Calves born in 1975 in commercial herds entered a feedlot as yearlings. Both diets and herds are of interest as factors. The covariate, ewt, is thought to be dependent on herd due to different genetic backgrounds, breeding history, etc. The levels of herd ordered to similarity of genetic background.

Note: There are some empty cells in the cross-classification of herd and diet.

**Source**

Urquhart NS (1982) Adjustment in covariates when one factor affects the covariate. *Biometrics* 38, 651-660.

**Examples**

```
require(lsmmeans)
feedlot.lm <- lm(swt ~ ewt + herd*diet, data = feedlot)

# Obtain LSmeans with a separate reference value of ewt for each
# herd. This reproduces the last part of Table 2 in the reference
lsmmeans(feedlot.lm, ~ diet | herd, cov.reduce = ewt ~ herd)
```

---

fiber

*Fiber data*

---

**Description**

Fiber data from Montgomery Design (8th ed.), p.656 (Table 15.10). Useful as a simple analysis-of-covariance example.

**Usage**

```
fiber
```

**Format**

A data frame with 15 observations on the following 3 variables.

`machine` a factor with levels A B C. The primary factor of interest.

`strength` a numeric vector. The response variable.

`diameter` a numeric vector. A covariate.

**Details**

The goal of the experiment is to compare the mean breaking strength of fibers produced by the three machines. When testing this, the technician also measured the diameter of each fiber, and this measurement may be used as a concomitant variable to improve precision of the estimates.

**Source**

Montgomery, D. C. (2013) *Design and Analysis of Experiments* (8th ed.). John Wiley and Sons, ISBN 978-1-118-14692-7.

## Examples

```
require(lsmmeans)
fiber.lm <- lm(strength ~ diameter + machine, data=fiber)
ref.grid(fiber.lm)

# Covariate-adjusted means and comparisons
lsmmeans(fiber.lm, pairwise ~ machine)
```

---

glht

*lsmmeans support for glht*


---

## Description

These functions and methods provide an interface between **lsmmeans** and the [glht](#) function for simultaneous inference in the **multcomp** package.

## Usage

```
## S3 method for class 'ref.grid'
as.glht(object, ...)
## S3 method for class 'lsm.list'
as.glht(object, ..., which = 1)

## S3 method for class 'glht.list'
coef(object, ...)
## S3 method for class 'glht.list'
confint(object, ...)
## S3 method for class 'glht.list'
plot(x, ...)
## S3 method for class 'glht.list'
summary(object, ...)
## S3 method for class 'glht.list'
vcov(object, ...)

lsm(...)
pmm(...)
```

## Arguments

object, x	An object of the required class.
which	Numeric index of which element of the <code>lsm.list</code> to use.
...	Additional arguments to other methods.

## Details

lsm (and pmm, which is identical) are meant to be called only *from* "glht" as its second (linfct) argument. It works similarly to [mcp](#) except with specs (and optionally by and contr arguments) provided as in a call to [lsmeans](#) or [pmmmeans](#).

When there is a non-NULL by variable (either explicitly or implicitly), each "by" group is passed separately to glht and returned as a list of "glht" objects. For convenience, this is classed as "glht.list", and appropriate methods coef, confint, plot, summary, and vcov are provided.

## Value

as.glht returns an object of class [glht](#), or of class `glht.list` if by is non-NULL. The latter is simply a list of glht objects, and the provided methods coef, confint, plot, summary, and vcov simply [lapply](#) the corresponding methods for class "glht".

## Note

There is also a glht method for class `ref.grid`, but it is far preferable to use `as.glht` instead, as its `model` argument is redundant.

## Author(s)

Russell V. Lenth

## See Also

[lsmeans](#), [glht](#)

## Examples

```
require(lsmeans)
require(multcomp)

warp.lm <- lm(breaks ~ wool*tension, data = warpbreaks)

# Using 'lsm'
summary(glht(warp.lm, lsm(pairwise ~ tension | wool)))

# Same, but using an existing 'lsmeans' result
warp.lsmobj <- lsmeans(warp.lm, ~ tension | wool)
summary(as.glht(pairs(warp.lsmobj)))

# Same contrasts, but treat as one family
summary(as.glht(pairs(warp.lsmobj), by = NULL))
```

---

lsmeans	<i>Least-squares means (or predicted marginal means)</i>
---------	--

---

## Description

Compute least-squares means (predicted marginal means) for specified factors or factor combinations in a linear model, and optionally comparisons or contrasts among them.

## Usage

```
## S3 method for class 'character'
lsmeans(object, specs, ...)
## (used when 'specs' is 'character')

## S3 method for class 'character.ref.grid'
lsmeans(object, specs, by = NULL,
         fac.reduce = function(coefs) apply(coefs, 2, mean), contr,
         options = getOption("lsmeans")$lsmeans, weights, trend, ...)
## (used when 'object' is a 'ref.grid' and 'specs' is 'character')

## S3 method for class 'list'
lsmeans(object, specs, ...)
## (used when 'specs' is a 'list')

## S3 method for class 'formula'
lsmeans(object, specs, contr.list, trend, ...)
## (used when 'specs' is a 'formula')

lstrends(model, specs, var, delta.var = 0.01 * rng, data,
         transform = c("none", "response"), ...)

lsmobj(bhat, V, levels, linfct, df = NA, post.beta = matrix(NA), ...)

pmmeans(...)
pmtrends(...)
pmmobj(...)
```

## Arguments

object	An object of class <code>ref.grid</code> ; or a fitted model object that is supported, such as the result of a call to <code>lm</code> or <code>lmer</code> . Many fitted-model objects are supported; see <code>link{models}</code> for details.
specs	A character vector specifying the names of the predictors over which LS-means are desired. <code>specs</code> may also be a formula or a list (optionally named) of valid specs. Use of formulas is described in the Details section below.
by	A character vector specifying the names of predictors to condition on.



fac.reduce	A function that combines the rows of a matrix into a single vector. This implements the “marginal averaging” aspect of least-squares means. The default is the mean of the rows. Typically if it is overridden, it would be some kind of weighted mean of the rows. If fac.reduce is nonlinear, bizarre results are likely, and LS means will not be interpretable. If the weights argument is non-missing, fac.reduce is ignored.
contr	A list of contrast coefficients to apply to the least-squares means – or the root name of an .lsmc function that returns such coefficients. In addition, contr = "cld" is an alternative way to invoke the <a href="#">cld</a> function. See <a href="#">contrast</a> for more details on contrasts. NOTE: contr is ignored when specs is a formula.
contr.list	A named list of lists of contrast coefficients, as for contr. This is used only in the formula method; see Details below.
options	If non-NULL, a named list of arguments to pass to <a href="#">update</a> , just after the object is constructed.
weights	Numeric vector, numeric matrix, or character string specifying weights to use in averaging predictions. If a vector, its length must equal the number of predictions to be averaged to obtain each least-squares mean. If a matrix, each row of the matrix is used in turn, wrapping back to the first row as needed. When in doubt about what is being averaged (or how many), first call with weights = "show.levels". If a string, it should partially match one of the following: <ul style="list-style-type: none"> <li>"equal" Use an equally weighted average.</li> <li>"proportional" Weight in proportion to the frequencies (in the original data) of the factor combinations that are averaged over.</li> <li>"outer" Weight in proportion to each individual factor's marginal frequencies. Thus, the weights for a combination of factors are the outer product of the one-factor margins</li> <li>"cells" Weight according to the frequencies of the cells being averaged.</li> <li>"flat" Give equal weight to all cells with data, and ignore empty cells.</li> <li>"show.levels" This is a convenience feature for understanding what is being averaged over. Instead of a table of LS means, this causes the function to return a table showing the levels that are averaged over, in the order they appear.</li> </ul> <p>Outer weights are like the 'expected' counts in a chi-square test of independence, and will yield the same results as those obtained by proportional averaging with one factor at a time. All except "cells" uses the same set of weights for each mean. In a model where the predicted values are the cell means, cell weights will yield the raw averages of the data for the factors involved. Using "flat" is similar to "cells", except nonempty cells are weighted equally and empty cells are ignored.</p> <p>Note: If a nested structure exists (see the nests argument in <a href="#">ref.grid</a>), then averaging is done separately over each nesting group; thus, these groups are potentially of different sizes. Accordingly, it is unsafe to specify numerical weights.</p> <p>Note: If weights were used in fitting the model, then weight totals are used in place of frequencies in these schemes.</p>

	If <code>weights</code> is used, <code>fac.reduce</code> is ignored.
<code>trend</code>	Including this argument is an alternative way of calling <code>lstrends</code> with <code>trend</code> as its <code>var</code> argument and object as its <code>model</code> .
<code>model</code>	A supported model object ( <i>not</i> a <code>ref.grid</code> ).
<code>var</code>	Character giving the name of a variable with respect to which a difference quotient of the linear predictors is computed. In order for this to be useful, <code>var</code> should be a numeric predictor that interacts with at least one factor in <code>specs</code> . Then instead of computing least-squares means, we compute and compare the slopes of the <code>var</code> trend over levels of the specified other predictor(s). As in least-squares means, marginal averages are computed when some variables in the reference grid are excluded for the specification.  The user may specify some monotone function of one variable, e.g., <code>var = "log(dose)"</code> . If so, the chain rule is applied. Note that, in this example, if <code>model</code> contains <code>log(dose)</code> as a predictor, we will be comparing the slopes estimated by that model, whereas specifying <code>var = "dose"</code> would perform a transformation of those slopes.
<code>delta.var</code>	The value of $h$ to use in forming the difference quotient $(f(x+h) - f(x))/h$ . Changing it (especially changing its sign) may be necessary to avoid numerical problems such as logs of negative numbers. The default value is 1/100 of the range of <code>var</code> over the dataset.
<code>data</code>	As in <a href="#">ref.grid</a> , you may use this argument to supply the dataset used in fitting the model, for situations where it is not possible to reconstruct the data. Otherwise, leave it missing.
<code>transform</code>	In <code>lstrends</code> , if object has a response transformation, then specifying <code>transform = "response"</code> will cause <code>lstrends</code> to calculate the trends after back-transforming to the response scale. This is done using the chain rule, and standard errors are estimated via the delta method. With <code>transform = "none"</code> (the default), the trends are calculated on the scale of the linear predictor, without back-transforming it. This argument works similarly to the <code>transform</code> argument in <a href="#">ref.grid</a> (but without a "log" option), in that the returned object is re-gridded to the new scale (see also <a href="#">regrid</a> ).
<code>bhat</code>	Numeric. Vector of regression coefficients.
<code>V</code>	Square matrix. Covariance matrix of <code>bhat</code>
<code>levels</code>	Named list or vector. Levels of factor(s) that define the estimates defined by <code>linfct</code> . If not a list, we assume one factor named "level"
<code>linfct</code>	Matrix. Linear functions of <code>bhat</code> for each combination of <code>levels</code>
<code>df</code>	Numeric or function with arguments $(x, \text{dfargs})$ . If a number, that is used for the degrees of freedom. If a function, it should return the degrees of freedom for <code>sum(x*bhat)</code> ; if additional parameters are needed, include them in <code>...</code> as <code>dfargs</code> (not abbreviated).
<code>post.beta</code>	Matrix whose columns comprise a sample from the posterior distribution of the regression coefficients (so that typically, the column averages will be <code>bhat</code> ). A 1 x 1 matrix of NA indicates that such a sample is unavailable.

... Additional arguments passed to other methods or to `ref.grid`. For example, `vcov` may be used to override the default covariance estimate, and some models allow additional options. Some models require data to be given explicitly. See the help pages for `ref.grid` and `models`. In addition, if the model formula contains references to variables that are not predictors, you must provide a `params` argument with a list of their names; see the example below for `Oatsq.lm`.

## Details

Least-squares means (also called predicted marginal means) are predictions from a linear model over a *reference grid*, or marginal averages thereof. They have been popularized by **SAS** (SAS Institute, 2012). The `ref.grid` function identifies/creates the reference grid upon which `lsmeans` is based.

For those who prefer the term “predicted marginal means”, courtesy wrappers `pmmeans`, `pmtrends`, and `pmmobj` are provided that behave identically to those that start with `ls`, except that estimates are relabeled accordingly (e.g., `lsmean` becomes `pmmean`).

If `specs` is a formula, it should be of the form `~ specs`, `~ specs | by`, `contr ~ specs`, or `contr ~ specs | by`. The formula is parsed and the variables therein are used as the arguments `specs`, `by`, and `contr` as indicated. The left-hand side is optional, but if specified it should be the name of a contrast family (e.g., `pairwise`) or of a sub-list of `contr.list`. Operators like `*` or `:` are necessary to delineate names in the formulas, but otherwise are ignored.

In the special case where the mean (or weighted mean) of all the predictions is desired, specify `specs` as `~ 1` or `"1"`.

A number of standard contrast families are provided. They can be identified as functions having names ending in `.lsmc` – use

```
ls("package:lsmeans", pat=".lsmc")
```

to list them. See the documentation for `pairwise.lsmc` and its siblings for details. You may write your own `.lsmc` function for custom contrasts.

The function `lsmobj` may be used to construct an object just like one returned by `lsmeans` from user-specified coefficients, covariance matrix, levels (or row labels), linear functions for each row, and degrees of freedom. After the object is constructed, it is `updateed` with any additional arguments in ...

## Value

When `specs` is a character vector or one-sided formula, an object of class `lsmobj`. A number of methods are provided for further analysis, including `summary`, `confint`, `test`, `contrast`, `pairs`, and `cld`.

When `specs` is a list or a formula having a left-hand side, the return value is an `lsm.list` object, which is simply a list of `lsmobj` objects. Methods for `lsm.list` objects are the same as those for `lsmobj`, but they apply to only one member of the list, determined by its `which` argument.

**Side effect:** When object is a model, a reference grid is constructed and it is saved as `.Last.ref.grid` in the user’s environment (unless this is disabled via `lsm.option(save.ref.grid = FALSE)`). This makes it possible to check what reference grid was used, or to use it as the object in future `lsmeans` calls (and bypass reconstructing it). Similarly, `lstrends` also saves its reference grid (but for predicting difference quotients) as `.Last.ref.grid`.

**Note**

If the model formula contains variables that are not predictors (e.g., degree of a polynomial, knots for a spline, etc.), you must add a `params` argument to the call

**Note**

While using `specs` as a two-sided formula or a list is a convenient way to get a lot of results with minimal effort, it can also create confusion when additional arguments are provided, because not all arguments may be applied to all the results produced (see examples). Thus, the safer route is to do things incrementally.

**Note**

`lsmeans` and its relatives can produce fatal errors or incorrect results with models containing splines (e.g., `ns`) and other smoothers because the required information to reconstruct their basis is not always available. A model with `poly` involving two or more predictors will almost always produce misleading results without any warning; but `poly(..., raw = TRUE)` will work correctly.

**Note**

For a `ref.grid` or `lsmobj` object created in `lsmeans` version 2.10 or earlier, the information needed by the `weights` argument is not present; so a message is displayed and averaging is done using `fac.reduce`.

**Author(s)**

Russell V. Lenth

**References**

SAS Institute Inc. (2012) Online documentation; Shared concepts; LSMEANS statement, [http://support.sas.com/documentation/cdl/en/statug/63962/HTML/default/viewer.htm#statug\\_introcom\\_a0000003362.htm](http://support.sas.com/documentation/cdl/en/statug/63962/HTML/default/viewer.htm#statug_introcom_a0000003362.htm), accessed August 15, 2012.

**See Also**

[ref.grid](#), [.Last.ref.grid](#), [models](#), [pairwise.lsmc](#), [glht](#), [lsm.options](#)

**Examples**

```
require(lsmeans)

### Covariance example (from Montgomery Design (8th ed.), p.656)
# Uses supplied dataset 'fiber'
fiber.lm <- lm(strength ~ diameter + machine, data = fiber)

# adjusted means and comparisons, treating machine C as control
( fiber.lsm <- lsmeans (fiber.lm, "machine") )
contrast(fiber.lsm, "trt.vs.ctrlk")
# Or get both at once using
```

```

# lsmeans (fiber.lm, "machine", contr = "trt.vs.ctrlk")

### Factorial experiment
warp.lm <- lm(breaks ~ wool * tension, data = warpbreaks)
( warp.lsm <- lsmeans (warp.lm, ~ wool | tension,
  options = list(estName = "pred.breaks")) )
pairs(warp.lsm) # remembers 'by' structure
contrast(warp.lsm, method = "poly", by = "wool")

### Unbalanced split-plot example ###
#-- The imbalance is imposed deliberately to illustrate that
#-- the variance estimates become biased
require(nlme)
Oats.lme <- lme(yield ~ factor(nitro) + Variety,
  random = ~1 | Block/Variety,
  subset = -c(1,2,3,5,8,13,21,34,55), data = Oats)
(Oats.anal <- lsmeans(Oats.lme, list(poly ~ nitro, pairwise ~ Variety)))

### Issues with lists of specs
test(Oats.anal) # Uses 1st element by default
confint(Oats.anal, which = 4) # or confint(Oats.anal[[4]])

# Using 'pmmeans' wrapper ...
pmmeans(warp.lm, ~ wool,
  options = list(infer = c(TRUE, TRUE), null = 22, side = ">"))

### Weights
# See what's being averaged over in the above
lsmeans(Oats.lme, ~ nitro, cov.reduce = FALSE, weights = "show.levels")

# Give three times the weight to Marvellous
lsmeans(Oats.lme, ~ nitro, cov.reduce = FALSE, weights = c(1,3,1))

# Overall mean
lsmeans(Oats.lme, ~ 1, weights = "equal")
lsmeans(Oats.lme, "1", weights = "cells")

### Model with a quadratic trend for 'nitro'
# Also illustrates use of `params` argument to list non-predictors
deg = 2
Oatsq.lm <- lm(yield ~ Block + poly(nitro, deg) + Variety, data = Oats)
# Predictions at each unique 'nitro' value in the dataset
lsmeans(Oatsq.lm, ~ nitro, cov.reduce = FALSE, params = "deg")

### Trends
fiber.lm <- lm(strength ~ diameter*machine, data=fiber)
# Obtain slopes for each machine ...
( fiber.lst <- lstrends(fiber.lm, "machine", var="diameter") )

```

```

# ... and pairwise comparisons thereof
pairs(fiber.lst)

# Suppose we want trends relative to sqrt(diameter)...
lstrends(fiber.lm, ~ machine | diameter, var = "sqrt(diameter)",
  at = list(diameter = c(20,30)))

# Given summary statistics for 4 cities computed elsewhere,
# obtain multiple comparisons of their means using the
# Satterthwaite method
ybar <- c(47.6, 53.2, 88.9, 69.8)
s <- c(12.1, 19.5, 22.8, 13.2)
n <- c(44, 11, 37, 24)
se2 = s^2 / n
Satt.df <- function(x, dfargs)
  sum(x * dfargs$v)^2 / sum((x * dfargs$v)^2 / (dfargs$n - 1))
city.pmm <- pmmobj(bhat = ybar, V = diag(se2),
  levels = list(city = LETTERS[1:4]), linfct = diag(c(1,1,1,1)),
  df = Satt.df, dfargs = list(v = se2, n = n), estName = "mean")
city.pmm
contrast(city.pmm, "revpairwise")

# See also many other examples in documentation for
# 'contrast', 'cld', 'glht', 'lsmip', 'ref.grid', 'MOats',
# 'nutrition', etc., and in the vignettes

```

---

lsmip

*Least-squares (predicted marginal) means interaction plot*


---

## Description

This function creates an interaction plot of the least-squares means based on a fitted model and a simple formula specification.

## Usage

```

## Default S3 method:
lsmip(object, formula, type,
  pch = c(1,2,6,7,9,10,15:20),
  lty = 1, col = NULL, plotit = TRUE, ...)

pmmip(...)

```

## Arguments

**object** An object of class `lsmobj`, or a fitted model of a class supported by [lsmmeans](#).

formula	Formula of the form <code>trace.factors ~ x.factors   by.factors</code> . The least-squares means are plotted against <code>x.factor</code> for each level of <code>trace.factors</code> . <code>by.factors</code> is optional, but if present, it determines separate panels. Each element of this formula may be a single factor in the model, or a combination of factors using the <code>*</code> operator.
type	As in <a href="#">predict</a> , this determines whether we want to inverse-transform the predictions ( <code>"type="response"</code> ) or not (any other choice). The default is <code>"link"</code> , unless the <code>"predict.type"</code> option is in force; see <a href="#">lsm.options</a> .
pch	The plotting characters to use for each group (i.e., levels of <code>trace.factors</code> ). They are recycled as needed.
lty	The line types to use for each group. Recycled as needed.
col	The colors to use for each group, recycled as needed. If not specified, the default trellis colors are used.
plotit	If TRUE, the plot is displayed. Otherwise, one may use the <code>"lattice"</code> attribute of the returned object and print it, perhaps after additional manipulation.
...	Additional arguments passed to <a href="#">lsmeans</a> or to <a href="#">xyplot</a> .

### Details

If `object` is a fitted model, [lsmeans](#) is called with an appropriate specification to obtain least-squares means for each combination of the factors present in `formula` (in addition, any arguments in `...` that match `at`, `trend`, `cov.reduce`, or `fac.reduce` are passed to [lsmeans](#)). Otherwise, if `object` is an `lsmobj` object, its first element is used, and it must contain one `lsmean` value for each combination of the factors present in `formula`.

The wrapper `pmmip` is provided for those who prefer the term ‘predicted marginal means’.

### Value

(Invisibly), a `data.frame` with the table of least-squares means that were plotted, with an additional `"lattice"` attribute containing the trellis object for the plot.

### Note

This function uses the [xyplot](#) function in the `lattice` package (an error is returned if `lattice` is not installed). Conceptually, it is equivalent to [interaction.plot](#) where the summarization function is the least-squares means.

### Author(s)

Russell V. Lenth

### See Also

[interaction.plot](#)

## Examples

```
require(lsmmeans)
require(lattice)

#--- Two-factor example
warp.lm <- lm(breaks ~ wool * tension, data = warpbreaks)

# Following plot is the same as the usual interaction plot of the data
lsmip(warp.lm, wool ~ tension)

#--- Three-factor example
noise.lm = lm(noise ~ size * type * side, data = auto.noise)

# Separate interaction plots of size by type, for each side
lsmip(noise.lm, type ~ size | side)

# One interaction plot, using combinations of size and side as the x factor
lsmip(noise.lm, type ~ side * size)

# One interaction plot using combinations of type and side as the trace factor
# customize the colors, line types, and symbols to suggest these combinations
lsmip(noise.lm, type * side ~ size, lty=1:2, col=1:2, pch=c(1,1,2,2))

# 3-way interaction is significant, but doesn't make a lot of visual difference...
noise.lm2 = update(noise.lm, . ~ . - size:type:side)
lsmip(noise.lm2, type * side ~ size, lty=1:2, col=1:2, pch=c(1,1,2,2))
```

---

make.tran

*Response transformations*

---

## Description

Create the needed information to perform transformations of the response variable, including inverting the transformation and estimating variances of back-transformed predictions via the delta method. `make.tran` is similar to `make.link`, but it covers additional transformations. The result can be used as an environment in which the model is fitted, or as the `tran` argument in `update.ref.grid` (when the given transformation was already applied in an existing model).

## Usage

```
make.tran(type = c("genlog", "power", "boxcox", "sympower", "asin.sqrt"), param = 1)

# See Details for additional auto-detected transformations
```

## Arguments

<code>type</code>	The name of the transformation. See Details.
<code>param</code>	Numeric parameter for the transformation. Optionally, it may be a vector of two numeric values; the second element specifies an alternative base or origin for certain transformations. See Details.



## Details

The functions `lsmeans`, `ref.grid`, and related ones automatically detect response transformations that are recognized by examining the model formula. These are `log`, `log2`, `log10`, `sqrt`, `logit`, `probit`, `cauchit`, `cloglog`; as well as (for a response variable  $y$ ) `asin(sqrt(y))`, `asinh(sqrt(y))`, and `sqrt(y) + sqrt(y+1)`. In addition, any constant multiple of these (e.g., `2*sqrt(y)`) is auto-detected and appropriately scaled (see also the `tran.mult` argument in `update.ref.grid`).

A few additional character strings may be supplied as the `tran` argument in `update.ref.grid`: "identity", "1/mu^2", "inverse", "reciprocal", "asin.sqrt", and "asinh.sqrt".

More general transformations may be provided as a list of functions and supplied as the `tran` argument as documented in `update.ref.grid`. The `make.tran` function returns a suitable list of functions for several popular transformations. Besides being usable with `update`, the user may use this list as an enclosing environment in fitting the model itself, in which case the transformation is auto-detected when the special name `linkfun` (the transformation itself) is used as the response transformation in the call. See the examples below.

Most of the transformations available in "make.tran" require a parameter, specified in `param`; we use  $p$  to denote this parameter, and  $y$  to denote the response variable, in subsequent expressions. The `type` argument specifies the following transformations:

"genlog" Generalized logarithmic transformation:  $\log(y + p)$ , where  $y > -p$

"power" Power transformation:  $y^p$ , where  $y > 0$ . When  $p = 0$ , "log" is used instead

"boxcox" The Box-Cox transformation (unscaled by the geometric mean):  $(y^p - 1)/p$ , where  $y > 0$ . When  $p = 0$ ,  $\log(y)$  is used.

"sympower" A symmetrized power transformation on the whole real line:  $\text{abs}(y)^p * \text{sign}(y)$ . There are no restrictions on  $y$ , but we require  $p > 0$  in order for the transformation to be monotone and continuous.

"asin.sqrt" Arcsin-square-root transformation:  $\sin^{-1}(y/p)^{1/2}$ . Typically, the parameter  $p$  equals to 1 for a fraction,

The user may include a second element in `param` to specify an alternative origin (other than zero) for the "power", "boxcox", or "sympower" transformations. For example, `'type = "power", param = c(1.5, 4)` specifies the transformation  $(y - 4)^{1.5}$ . In the "genpower" transformation, a second `param` element may be used to specify a base other than the default natural logarithm. For example, `'type = "genlog", param = c(.5, 10)`' specifies the  $\log_{10}(y + .5)$  transformation.

For purposes of back-transformation, the `'sqrt(y) + sqrt(y+1)'` transformation is treated exactly the same way as `'2*sqrt(y)'`, because both are regarded as estimates of  $2\sqrt{\mu}$ .

## Value

A list having at least the same elements as that returned by `make.link`. The `linkfun` component is the transformation itself.

## Note

We modify certain `make.link` results in transformations where there is a restriction on valid prediction values, so that reasonable inverse predictions are obtained for no matter what. For example, if a `sqrt` transformation was used but a predicted value is negative, the inverse transformation is zero rather than the square of the prediction. A side effect of this is that it is possible for one or both confidence limits, or even a standard error, to be zero.

**Author(s)**

Russell V. Lenth

**See Also**[make.link](#), [update](#)**Examples**

```
require("lsmeans")

# Fit a model using an oddball transformation:
bctran <- make.tran("boxcox", 0.368)
warp.bc <- with(bctran,
  lm(linkfun(breaks) ~ wool * tension, data = warpbreaks))
# Obtain back-transformed LS means:
lsmeans(warp.bc, ~ tension | wool, type = "response")

## Not run:
# An existing model 'mod' was fitted with a log(y + 1) transformation...
mod.rg <- update(ref.grid(mod), tran = make.tran("genlog", 1))
lsmeans(mod.rg, "treatment")

## End(Not run)
```

---

MOats

*Oats data in multivariate form*

---

**Description**

This is the Oats dataset provided in the **nlme** package, but it is rearranged as one multivariate observation per plot.

**Usage**

```
data(MOats)
```

**Format**

A data frame with 18 observations on the following 3 variables.

Variety a factor with levels Golden Rain, Marvellous, Victory

Block an ordered factor with levels VI < V < III < IV < II < I

yield a matrix with 4 columns, giving the yields with nitrogen concentrations of 0, .2, .4, and .6.

## Details

These data arise from a split-plot experiment reported by Yates (1935) and used as an example in Pinheiro and Bates (2000) and other texts. Six blocks were divided into three whole plots, randomly assigned to the three varieties of oats. The whole plots were each divided into 4 split plots and randomized to the four concentrations of nitrogen.

## Source

The dataset `Oats` in the `nlme` package.

## References

- Pinheiro, J. C. and Bates D. M. (2000) *Mixed-Effects Models in S and S-PLUS*, Springer, New York. (Appendix A.15)
- Yates, F. (1935) Complex experiments, *Journal of the Royal Statistical Society Suppl.* 2, 181-247

## Examples

```
require(lsmeans)
MOats.lm <- lm (yield ~ Block + Variety, data = MOats)
MOats.rg <- ref.grid (MOats.lm, mult.name = "nitro")
lsmeans(MOats.rg, ~ nitro | Variety)
```

---

models

*Models supported in lsmeans*

---

## Description

Here we document what model objects may be used with `lsmeans`, and some special features of some of them. We start with those in the `stats` package; the other packages follow in alphabetical order.

Certain objects are affected by optional arguments to functions that construct `ref.grid` or `lsmobj` objects, including `ref.grid`, `lsmeans`, `lstrends`, and `lsmip`. When “arguments” are mentioned in the subsequent object-by-object documentation, we are talking about arguments in these constructors.

Additional models can be supported by writing appropriate `recover.data` and `lsm.basis` methods. See `extending-lsmeans` and `vignette("extending")` for details.

## stats package

**lm**, **aov**, **glm** No extended features. Note that the `lm` support often extends to a number of model objects that inherit from it, such as `r1m` in the `MASS` package and `rsm` in the `rsm` package.

**mlm**, **maov**, **manova** When there is a multivariate response, the different responses are treated as if they were levels of a factor – named `rep.meas` by default. The `mult.name` argument may be used to change this name. The `mult.levs` argument may specify a named list of one or more sets of levels. If this has more than one element, then the multivariate levels are expressed as combinations of the named factor levels via the function `expand.grid`.

**aovlist** Support for these objects is limited. To avoid strong biases in the predictions, the contrasts attribute of all factors should be of a type that sums to zero – for example, "contr.sum", "contr.poly", or "contr.helmert" but *not* "contr.treatment". Only intra-block estimates of covariances are used. That is, if a factor appears in more than one error stratum, only the covariance structure from its lowest stratum is used in estimating standard errors. Degrees of freedom are obtained using the Satterthwaite method. In general, aovList support is best with balanced designs, and due caution in the use of contrasts. If a vcov. argument is supplied, it must yield a single covariance matrix for the unique fixed effects, and the degrees of freedom are set to NA.

#### **afex package**

**mixed** Support for mixed objects has been removed. Version 0.14 and later of **afex** provides new object classes with their own **lsmeans** support.

#### **betareg package**

**betareg** The additional mode argument has possible values of "response", "link", "precision", "phi.link", "variance", and "quantile", which have the same meaning as the type argument in predict.betareg – with the addition that "phi.link" is like "link", but for the precision portion of the model. When mode = "quantile" is specified, the additional argument quantile (a numeric scalar or vector) specifies which quantile(s) to compute; the default is 0.5 (the median). Also in "quantile" mode, an additional variable quantile is added to the reference grid, and its levels are the values supplied.

#### **CARBayes package**

**carbays** The user *must* supply (via the data argument) the dataset used in fitting the model. As with other MCMC-based objects, the summaries and such are frequentist, but the as.mcmc method provides a posterior sample of the desired quantities.

#### **coxme package**

**coxme** No additional options. Support for these models is experimental; may throw errors or incorrect results.

#### **gam package**

**gam** Currently, gam objects are not supported. Past versions of **lsmeans** appeared to support gam models owing to inheritance from lm, but the results were incorrect because spline features were ignored. We now explicitly trap gam objects to avoid these misleading analyses.

#### **gee and geepack packages**

These models all have more than one covariance estimate available, and it may be selected by supplying a string as the vcov.method argument. It is partially matched with the available choices; thus, for example, 'vcov = "n"' translates to 'vcov.method = "naive"'

**gee** Available covariance estimates are specified in vcov.method as "robust" (the default) and "naive".

**geeglm**, **geese** Available covariance estimates are specified in `vcov.method` as "vbeta" (the default), "vbeta.naiv", "vbeta.jls", or "vbeta.fij". The aliases "robust" (for "vbeta") and "naive" (for "vbeta.naiv") are also accepted.

If a matrix or function is supplied as `vcov.method`, it is interpreted as a `vcov.` specification as described for . . . in [ref.grid](#).

### glmmADMB package

**glmmadmb** No extended features.

### lme4 package

**lmerMod** There is an optional `mode` argument that defaults to `get.lsm.option("lmer.df")` (which in turn defaults to "satterthwaite"). The possible values are "satterthwaite", "kenward-roger", and "asymptotic" (these are partially matched and case-insensitive). With "satterthwaite", d.f. are obtained using code from the **lmerTest** package, if installed. With "kenward-roger", d.f. are obtained using code from the **pbkrtest** package, if installed. With "asymptotic", or if the needed package is not installed, d.f. are set to NA.

A by-product of the Kenward-Roger method is that the covariance matrix is adjusted using [vcovAdj](#). This can require considerable computation; so to avoid that overhead, the user should opt for the Satterthwaite or asymptotic method; or, for backward compatibility, may disable the use of **pbkrtest** via `'lsm.options(disable.pbkrtest=TRUE)'` (this does not disable the **pbkrtest** package entirely, just its use in **lsmeans**). The computation time required depends roughly on the number of observations,  $N$ , in the design matrix (because a major part of the computation involves inverting an  $N \times N$  matrix). Thus, **pbkrtest** is automatically disabled if  $N$  exceeds the value of `get.lsm.option("pbkrtest.limit")`. If desired, the user may use `lsm.options` to adjust this limit from the default of 3000.

The `df` argument may be used to specify some other degrees of freedom. Note that if `df` and `method = "satterthwaite"` are both specified, the covariance matrix is adjusted but the K-R degrees of freedom are not used.

**glmerMod** No degrees of freedom are available for these objects, so tests and confidence intervals are asymptotic.

### lme4.0 package

**mer** Only asymptotic results are available (no d.f.).

### MASS package

**glmmPQL** Supported by virtue of inheritance from `lme` in the **nlme** package.

**glm.nb** Supported by virtue of inheritance from `glm`.

**polr** There are two optional arguments: `mode` and `rescale` (which defaults to `'c(0,1)'`). For details, see the documentation below regarding the support for the **ordinal** package, which produces comparable objects (but since `polr` does not support scale models, `mode="scale"` is not supported). Tests and confidence intervals are asymptotic.

**rlm** Supported by virtue of inheritance from `lm`.

### MCMCglmm package

**MCMCglmm** Currently, I have found no way to reconstruct the data based on information in the object; thus, you *must* provide the dataset via the `data` argument. In addition, the contrasts specifications are not recoverable from the object, so the system default must match what was actually used in fitting the model. The usual `summary`, `test`, etc. methods provide frequentist analyses of the results based on the posterior means and covariances. However, an `as.mcmc` method is provided that creates an `mcmc` object that can be summarized or plotted using the **coda** package. It provides a posterior sample of `lsmeans` for the given reference grid, based on the posterior sample of the fixed effects from the `MCMCglmm` object.

### MCMCpack package (and perhaps others)

**mcmc** Certain linear-model or mixed-model objects are of class `mcmc`, and contain a sample from the posterior distribution of fixed-effect coefficients. In some cases (e.g., results of `MCMCregress` and `MCMCpoisson`), the object may include a `"call"` attribute that `lsmeans` can use to reconstruct the data and obtain a basis for the least-squares means. If not, a formula and data argument are provided that may help produce the right results. In addition, the contrasts specifications are not recoverable from the object, so the system default must match what was actually used in fitting the model. As for other MCMC-based objects, the summaries and such are frequentist, but the `as.mcmc` method provides a posterior sample of the desired quantities.

### nlme package

**gls** No additional features. Degrees of freedom are computed using  $N - p$  in `object$df.residual`. This is consistent with `nlme::summary.gls` but seems questionable.

**lme** Degrees of freedom are obtained using a containment method, i.e., the minimum of those elements of `object$fixDF` receiving nonzero weight (but with a correction to the `lme` object's intercept df). (This is similar to SAS's containment method, but I believe SAS does it incorrectly when the estimands are not contrasts.) The optional argument `sigmaAdjust` (defaults to `TRUE`) will adjust standard errors like in `summary.lme` when the model is fitted using the "ML" method. **Note:** `sigmaAdjust` is comparable to `adjustSigma` in `summary.lme` but it is renamed to avoid conflicting with `adjust`.

**nlme** Support is provided for inferences on parameters named in the fixed part of the model. The user *must* specify `param` in the call and give the name of a parameter that appears in the right-hand side of a fixed formula. Degrees of freedom are obtained using the containment-like method described above for `lme`.

### nnet package

**multinom** The reference grid includes a pseudo-factor with the same name and levels as the multinomial response. There is an optional `mode` argument which should match "prob" or "latent". With `mode = "prob"`, the reference-grid predictions consist of the estimated multinomial probabilities. The "latent" mode returns the linear predictor, recentered so that it averages to zero over the levels of the response variable (similar to sum-to-zero contrasts). Thus each latent variable can be regarded as the log probability at that level minus the average log probability over all levels.

Please note that, because the probabilities sum to 1 (and the latent values sum to 0) over the multivariate-response levels, all sensible results from `lsmeans` must involve that response as

one of the factors. For example, if `resp` is a response with  $k$  levels, `lsmeans(model, ~ resp | trt)` will yield the estimated multinomial distribution for each `trt`; but `lsmeans(model, ~ trt)` will just yield the average probability of  $1/k$  for each `trt`.

### ordinal package

**clm, clmm** The reference grid will include all variables that appear in the main model as well as those in the scale or nominal models. There are two optional arguments: `mode` (a character string) and `rescale` (which defaults to `c(0,1)`). `mode` should match one of `"latent"` (the default), `"linear.predictor"`, `"cum.prob"`, `"exc.prob"`, `"prob"`, `"mean.class"`, or `"scale"`.

With `mode = "latent"`, the reference-grid predictions are made on the scale of the latent variable implied by the model. The scale and location of this latent variable are arbitrary, and may be altered via `rescale`. The predictions are multiplied by `rescale[2]`, then `rescale[1]` is added. Keep in mind that the scaling is related to the link function used in the model; for example, changing from a probit link to a logistic link will inflate the latent values by around  $\pi/\sqrt{3}$ , all other things being equal. `rescale` has no effect for other values of `mode`.

With `mode = "linear.predictor"`, `mode = "cum.prob"`, and `mode = "exc.prob"`, the boundaries between categories (i.e., thresholds) in the ordinal response are included in the reference grid as a pseudo-factor named `cut`. The reference-grid predictions are then of the cumulative probabilities at each threshold (for `mode = "cum.prob"`), exceedance probabilities (one minus cumulative probabilities, for `mode = "exc.prob"`), or the link function thereof (for `mode = "linear.predictor"`).

With `mode = "prob"`, a pseudo-factor with the same name as the model's response variable is created, and the grid predictions are of the probabilities of each class of the ordinal response. With `"mean.class"`, the returned results are means of the ordinal response, interpreted as a numeric value from 1 to the number of classes, using the `"prob"` results as the estimated probability distribution for each case.

With `mode = "scale"`, and the fitted object incorporates a scale model, least-squares means are obtained for the factors in the scale model instead of the response model. The grid is constructed using only the factors in the scale model.

Any grid point that is non-estimable by either the location or the scale model (if present) is set to NA, and any LS-means involving such a grid point will also be non-estimable. A consequence of this is that if there is a rank-deficient scale model, and then *all* latent responses become non-estimable because the predictions are made using the average log-scale estimate. Tests and confidence intervals are asymptotic.

### pscl package

**hurdle, zeroinfl** Two optional arguments – `mode` and `lin.pred` – are provided. The `mode` argument has possible values `"response"` (the default), `"count"`, `"zero"`, or `"prob0"`. `lin.pred` is logical and defaults to FALSE.

With `lin.pred = FALSE`, the results are comparable to those returned by `predict(..., type = "response")`, `predict(..., type = "count")`, `predict(..., type = "zero")`, or `predict(..., type = "prob0")[, 1]`. See the documentation for [predict.hurdle](#) and [predict.zeroinfl](#).

The option `lin.pred = TRUE` only applies to `mode = "count"` and `mode = "zero"`. The results returned are on the linear-predictor scale, with the same transformation as the link function in that part of the model. The predictions for a reference grid with `mode = "count"`,

`lin.pred = TRUE`, and `type = "response"` will be the same as those obtained with `lin.pred = FALSE` and `mode = "count"`; however, any LS means derived from these grids will be different, because the averaging is done on the log-count scale and the actual count scale, respectively – thereby producing geometric means versus arithmetic means of the predictions.

If the `vcov.` argument is used (see details in [ref.grid](#)), it must yield a matrix of the same size as would be obtained using `vcov.hurdle` or `vcov.zeroinfl` with its `model` argument set to (`"full"`, `"count"`, `"zero"`) in respective correspondence with `mode` of (`"mean"`, `"count"`, `"zero"`). If `vcov.` is a function, it must support the `model` argument.

### rms package

**Potential masking issue** Both **rms** and **lsmeans** offer contrast methods, and whichever package is loaded later masks the other. Thus, you may need to call `lsmeans::contrast` or `rms::contrast` explicitly to access the one you want.

**Objects inheriting from rms** Standard support is provided. However, with models having more than one intercept (e.g. from **orm**), a `mode` argument is provided that works similarly to that for the **ordinal** package. The available modes are `"middle"` (the default), `"latent"`, `"linear.predictor"`, `"cum.prob"`, `"exc.prob"`, `"prob"`, and `"mean.class"`. All are as described for the **ordinal** package, except as noted below.

With `mode = "middle"` (this is the default), the middle intercept is used, comparable to the default for **rms**'s `Predict` function. This is quite similar in concept to `mode = "latent"`, where all intercepts are averaged together.

Results for `mode = "linear.predictor"` are reversed from those in the **ordinal** package, because **orm** models predict the link function of the *upper*-tail (exceedance) probabilities.

With `mode = "prob"`, a pseudo-factor is created having the same name as the model response variable, but its levels are always integers `'1, 2, ...'` regardless of the levels of the original response.

### rstanarm package

**stanreg** Support for models fitted using `stan_xxx` is similar to that for models fitted by `xxx`, where supported, except that posterior samples are also available. For example, `stan_glm` models are treated like `stats::glm`, and `stan_polr` results are similar to those for `MASS::polr` (including its available `mode` and `rescale` options). Models fitted using `stan_biglm`, `stan_betareg`, and `stan_gamm4` are currently not supported. The user may use `as.mcmc`, `as.mcmc.list`, or `as.stanfit` on the `ref.grid` or `lsmobj` produced to obtain posterior samples of LS means, contrasts, etc.

### survival package

**survreg**, **coxph** No extended features.

### Author(s)

Russell V. Lenth



**See Also**

[ref.grid](#), [lsm.basis](#)

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nutrition	<i>Nutrition data</i>
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---

**Description**

This observational dataset involves three factors, but where several factor combinations are missing. It is used as a case study in Milliken and Johnson, Chapter 17, p.202. (You may also find it in the second edition, p.278.)

**Usage**

```
nutrition
```

**Format**

A data frame with 107 observations on the following 4 variables.

age a factor with levels 1, 2, 3, 4. Mother's age group.

group a factor with levels FoodStamps, NoAid. Whether or not the family receives food stamp assistance.

race a factor with levels Black, Hispanic, White. Mother's race.

gain a numeric vector (the response variable). Gain score (posttest minus pretest) on knowledge of nutrition.

**Details**

A survey was conducted by home economists "to study how much lower-socioeconomic-level mothers knew about nutrition and to judge the effect of a training program designed to increase their knowledge of nutrition." This is a messy dataset with several empty cells.

**Source**

Milliken, G. A. and Johnson, D. E. (1984) *Analysis of Messy Data – Volume I: Designed Experiments*. Van Nostrand, ISBN 0-534-02713-7.

**Examples**

```
require(lsmmeans)
nutr.aov <- aov(gain ~ (group + age + race)^2, data = nutrition)

# Summarize predictions for age group 3
nutr.lsm <- lsmmeans(nutr.aov, ~ race * group,
  at = list(age="3"))
```

```

lsmip(nutr.lsm, race ~ group)

# Hispanics seem exceptional; but, this doesn't test out due to very sparse data
cld(nutr.lsm, by = "group")
cld(nutr.lsm, by = "race")

```

---

oranges

*Orange sales*


---

### Description

This example dataset on sales of oranges has two factors, two covariates, and two responses. There is one observation per factor combination.

### Usage

```
data(oranges)
```

### Format

A data frame with 36 observations on the following 6 variables.

store a factor with levels 1 2 3 4 5 6. The store that was observed.

day a factor with levels 1 2 3 4 5 6. The day the observation was taken (same for each store).

price1 a numeric vector. Price of variety 1.

price2 a numeric vector. Price of variety 2.

sales1 a numeric vector. Sales (per customer) of variety 1.

sales2 a numeric vector. Sales (per customer) of variety 2.

### Source

Download from <http://ftp.sas.com/samples/A56655>.

### References

Littell, R., Stroup W., Freund, R. (2002) *SAS For Linear Models* (4th edition). SAS Institute. ISBN 1-59047-023-0.

### Examples

```

require(lsmmeans)

# Example on p.244 of Littell et al.
oranges.lm <- lm(sales1 ~ price1*day, data = oranges)
lsmmeans(oranges.lm, "day")

# Example on p.246
lsmmeans(oranges.lm, "day", at = list(price1 = 0))

```

---

pairwise.lsmc	<i>Contrast families</i>
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---

### Description

These functions return standard sets of contrast coefficients. The name of any of these functions (with the `.lsmc` omitted) may be used as the method argument in `contrast`, or as the `contr` argument or left-hand side of a spec formula in `lsmeans`.

### Usage

```
pairwise.lsmc(levs, ...)
revpairwise.lsmc(levs, ...)
tukey.lsmc(levs, reverse = FALSE)

poly.lsmc(levs, max.degree = min(6, k - 1))

trt.vs.ctrl1.lsmc(levs, ref = 1)
trt.vs.ctrl11.lsmc(levs, ...)
trt.vs.ctrlk.lsmc(levs, ...)
dunnett.lsmc(levs, ref = 1)

consec.lsmc(levs, reverse = FALSE, ...)
mean_chg.lsmc(levs, reverse = FALSE, ...)

eff.lsmc(levs, ...)
del.eff.lsmc(levs, ...)
```

### Arguments

<code>levs</code>	Vector of factor levels
<code>...</code>	Additional arguments, ignored but needed to make these functions interchangeable
<code>max.degree</code>	The maximum degree of the polynomial contrasts in <code>poly.lsmc</code>
<code>reverse</code>	Logical value to determine the direction of comparisons, e.g., pairwise (if TRUE) or reverse-pairwise (if FALSE) comparisons.
<code>ref</code>	Reference level (or control group) in <code>trt.vs.ctrl1.lsmc</code>

### Details

Each contrast family has a default multiple-testing adjustment as noted below. These adjustments are often only approximate; for a more exacting adjustment, use the interfaces provided to `glht` in the **multcomp** package.

`pairwise.lsmc`, `revpairwise.lsmc`, and `tukey.lsmc` generate contrasts for all pairwise comparisons among least-squares means at the levels in `levs`. The distinction is in which direction they are subtracted. For factor levels A, B, C, D, `pairwise.lsmc` generates the comparisons A-B, A-C,

A-D, B-C, B-D, and C-D, whereas `revpairwise.lsmc` generates B-A, C-A, C-B, D-A, D-B, and D-C. `tukey.lsmc` invokes `pairwise.lsmc` or `revpairwise.lsmc` depending on `reverse`. The default multiplicity adjustment method is "tukey", which is approximate when the standard errors differ.

`poly.lsmc` generates orthogonal polynomial contrasts, assuming equally-spaced factor levels. These are derived from the `poly` function, but an ad hoc algorithm is used to scale them to integer coefficients that are (usually) the same as in published tables of orthogonal polynomial contrasts. The default multiplicity adjustment method is "none".

`trt.vs.ctrl.lsmc` and its relatives generate contrasts for comparing one level (or the average over specified levels) with each of the other levels. The argument `ref` should be the *index(es)* (not the labels) of the reference level(s). `trt.vs.ctrl1.lsmc` is the same as `trt.vs.ctrl` with a reference value of 1, and `trt.vs.ctrlk.lsmc` is the same as `trt.vs.ctrl` with a reference value of `length(levs)`. `dunnett.lsmc` is the same as `trt.vs.ctrl`. The default multiplicity adjustment method is "dunnett", a close approximation to the Dunnett adjustment.

`consec.lsmc` and `mean_chg.lsmc` are useful for contrasting treatments that occur in sequence. For a factor with levels A, B, C, D, E, `consec.lsmc` generates the comparisons B-A, C-B, and D-C, while `mean_chg.lsmc` generates the contrasts  $(B+C+D)/3 - A$ ,  $(C+D)/2 - (A+B)/2$ , and  $D - (A+B+C)/3$ . With `reverse = TRUE`, these differences go in the opposite direction.

`eff.lsmc` and `del.eff.lsmc` generate contrasts that compare each level with the average over all levels (in `eff.lsmc`) or over all other levels (in `del.eff.lsmc`). These differ only in how they are scaled. For a set of  $k$  lsmeans, `del.eff.lsmc` gives weight 1 to one lsmean and weight  $-1/(k-1)$  to the others, while `eff.lsmc` gives weights  $(k-1)/k$  and  $-1/k$  respectively, as in subtracting the overall lsmean from each lsmean. The default multiplicity adjustment method is "fdr". This is a Bonferroni-based method and is slightly conservative; see [p.adjust](#)

### Value

A data.frame, each column containing contrast coefficients for `levs`. The "desc" attribute is used to label the results in `lsmeans`, and the "adjust" attribute gives the default adjustment method for multiplicity.

### Note

You may create your own contrast functions, using these as guides. A function named `mycontr.lsmc` may be invoked in `lsmeans` via, e.g.,

```
lsmeans(\var{object}, mycontr ~ \var{factor})
```

The "desc", "adjust", and "offset" attributes are optional; if present, these are passed to `contrast`. If absent, the root name of the function is used as "desc", and no adjustment is requested for p values. See the examples.

### Author(s)

Russell V. Lenth

### See Also

[lsmeans](#), [glht](#)

**Examples**

```
### View orthogonal polynomials for 4 levels
poly.lsmc(1:4)

### Setting up a custom contrast function
helmert.lsmc <- function(levs, ...) {
  M <- as.data.frame(contr.helmert(levs))
  names(M) <- paste(levs[-1], "vs earlier")
  attr(M, "desc") <- "Helmert contrasts"
  M
}
warp.lm <- lm(breaks ~ wool*tension, data = warpbreaks)
lsmeans(warp.lm, helmert ~ tension | wool)
```

---

 recover.data

*Support functions for creating a reference grid*


---

**Description**

This documents the methods used to create a [ref.grid](#) object from a fitted model.

**Usage**

```
recover.data(object, ...)
## S3 method for class 'call'
recover.data(object, trms, na.action,
             data = NULL, params = NULL, ...)

lsm.basis(object, trms, xlev, grid, ...)
```

**Arguments**

object	An object returned from a model-fitting function.
trms	The <a href="#">terms</a> component of object
xlev	Named list of levels of factors in the model frame. This should <i>not</i> include levels of factors created in the model itself, e.g., by including a factor call in the model formula.
grid	A data.frame containing predictor values at which predictions are needed.
na.action	Integer vector of indices of observations to ignore; or NULL if none
data	Data frame. Usually, this is NULL. However, if non-null, this is used in place of the reconstructed dataset. It must have all of the predictors used in the model, and any factor levels must match those used in fitting the model.
params	Character vector giving the names of any variables in the model formula that are <i>not</i> predictors. An example would be a variable knots specifying the knots to use in a spline model.
...	Additional arguments passed to other methods.

## Details

To create a reference grid, the `ref.grid` function needs to reconstruct the data used in fitting the model, and then obtain a matrix of linear functions of the regression coefficients for a given grid of predictor values. These tasks are performed by calls to `recover.data` and `lsm.basis` respectively.

To extend **lsmeans**'s support to additional model types, one need only write S3 methods for these two functions. The existing methods serve as helpful guidance for writing new ones. Most of the work for `recover.data` can be done by its method for class "call", providing the terms component and `na.action` data as additional arguments. Writing an `lsm.basis` method is more involved, but the existing methods (e.g., `lsmeans::lsm.basis.lm`) can serve as models. See the "Value" section below for details on what it needs to return. Also, certain `recover.data` and `lsm.basis` methods are exported from **lsmeans**, so if your object is based on another model-fitting object, it may be that all that is needed is to call one of these exported methods and perhaps make modifications to the results. Contact the developer if you need others of these exported.

If the model has a multivariate response, `bhat` needs to be "flattened" into a single vector, and `X` and `V` must be constructed consistently.

In models where a non-full-rank result is possible (often you can tell by seeing if there is a `singular.ok` argument in the model-fitting function), `summary` and `predict` check the estimability of each prediction, using the `nonest.basis` function in the **estimability** package.

The models already supported are detailed in `models`. Some packages may provide additional **lsmeans** support for its object classes.

## Value

`recover.data` should return a `data.frame` containing all the variables in the original data that appear as predictors in the model. Several attributes need to be included as well; see the code for `lsmeans::recover.data.lm`.

`lsm.basis` should return a `list` with the following elements:

<code>X</code>	The matrix of linear functions over <code>grid</code> , having the same number of rows as <code>grid</code> and the number of columns equal to the length of <code>bhat</code> .
<code>bhat</code>	The vector of regression coefficients for fixed effects. This should <i>include</i> any NAs that result from rank deficiencies.
<code>nbasis</code>	A matrix whose columns form a basis for non-estimable functions of beta, or a 1x1 matrix of NA if there is no rank deficiency.
<code>V</code>	The estimated covariance matrix of <code>bhat</code> .
<code>dffun</code>	A function of <code>(k, dfargs)</code> that returns the degrees of freedom associated with <code>sum(k * bhat)</code> .
<code>dfargs</code>	A <code>list</code> containing additional arguments needed for <code>dffun</code> .

## Optional hooks

Some models may need something other than standard linear estimates and standard errors. If so, custom functions may be pointed to via the items `misc$estHook`, `misc$vcovHook` and `misc$postGridHook`. If just the name of the hook function is provided as a character string, then it is retrieved using `get`.

The `estHook` function should have arguments `'(object, do.se, tol, ...)'` where `object` is the `ref.grid` or `lsmobj` object, `do.se` is a logical flag for whether to return the standard error,

and `tol` is the tolerance for assessing estimability. It should return a matrix with 3 columns: the estimates, standard errors (NA when `do.se==FALSE`), and degrees of freedom (NA for asymptotic). The number of rows should be the same as `'object@linfct'`. The `vcovHook` function should have arguments `'(object, tol, ...)'` as described. It should return the covariance matrix for the estimates. Finally, `postGridHook`, if present, is called at the very end of `ref.grid`; it takes one argument, the constructed object, and should return a suitably modified `ref.grid` object.

### Additional functions

A few additional functions used in the **lsmeans** codebase are exported as they may be useful to package developers. See details near the end of the vignette "extending".

### Author(s)

Russell V. Lenth

### See Also

[models](#), [ref.grid](#), [ref.grid-class](#)

### Examples

```
## Not run:
  require(lsmeans)

  # Fit a 2-factor model with two empty cells
  warpsing.lm <- lm(breaks ~ wool*tension,
    data = warpbreaks, subset = -(16:40))

  lsmeans::recover.data.lm(warpsing.lm, data = NULL)
  grid = with(warpbreaks,
    expand.grid(wool = levels(wool), tension = levels(tension)))
  lsmeans::lsm.basis.lm(warpsing.lm, delete.response(terms(warpsing.lm)),
    warpsing.lm$xlevels, grid)

## End(Not run)
```

---

ref.grid

*Create a reference grid from a fitted model*

---

### Description

Using a fitted model object, determine a reference grid for which least-squares means are defined. The resulting `ref.grid` object encapsulates all the information needed to calculate LS means and make inferences on them.

**Usage**

```
ref.grid(object, at, cov.reduce = mean, mult.name, mult.levs,
         options = get.lsm.option("ref.grid"), data, df, type,
         transform = c("none", "response", "mu", "unlink", "log"),
         nesting, ...)
```

```
.Last.ref.grid
```

**Arguments**

object	An object produced by a supported model-fitting function, such as <code>lm</code> . Many models are supported. See <a href="#">models</a> .
at	Optional named list of levels for the corresponding variables
cov.reduce	A function, logical value, or formula; or a named list of these. Each covariate <i>not specified in</i> at is reduced according to these specifications. If a single function, it is applied to each covariate. If logical and TRUE, mean is used. If logical and FALSE, it is equivalent to specifying ‘function(x) sort(unique(x))’, and these values are considered part of the reference grid; thus, it is a handy alternative to specifying these same values in at. If a formula (which must be two-sided), then a model is fitted to that formula using <code>lm</code> ; then in the reference grid, its response variable is set to the results of <code>predict</code> for that model, with the reference grid as newdata. (This is done <i>after</i> the reference grid is determined.) A formula is appropriate here when you think experimental conditions affect the covariate as well as the response. If cov.reduce is a named list, then the above criteria are used to determine what to do with covariates named in the list. (However, formula elements do not need to be named, as those names are determined from the formulas’ left-hand sides.) Any unresolved covariates are reduced using “mean”. Any cov.reduce specification for a covariate also named in at is ignored.
mult.name	Character, the name to give to the “factor” whose levels delineate the elements of a multivariate response. If this is provided, it overrides the default name, e.g., “rep.meas” for an <code>mlm</code> object or “cut” for a <code>polr</code> object.
mult.levs	A named list of levels for the dimensions of a multivariate response. If there is more than one element, the combinations of levels are used, in <code>expand.grid</code> order. The (total) number of levels must match the number of dimensions. If mult.name is specified, this argument is ignored.
options	If non-NULL, a named list of arguments to pass to <code>update</code> , just after the object is constructed.
data	A data.frame to use to obtain information about the predictors (e.g. factor levels). If missing, then <code>recover.data</code> is used to attempt to reconstruct the data.
df	This is a courtesy shortcut, equivalent to specifying <code>options(df = df)</code> . See <a href="#">update</a> .
type	If provided, this is saved as the “predict.type” setting. See <a href="#">update</a>



transform	If other than "none", the reference grid is reconstructed via <code>regrid</code> with the given transform argument. See Details.
nesting	If the model has nested fixed effects, this may be specified here via a character vector or named list specifying the nesting structure. Specifying nesting overrides any nesting structure that is automatically detected. See Details.
...	Optional arguments passed to <code>lsm.basis</code> , such as <code>vcov</code> . (see Details below) or options for certain models (see <code>models</code> ).

## Details

The reference grid consists of combinations of independent variables over which predictions are made. Least-squares means are defined as these predictions, or marginal averages thereof. The grid is determined by first reconstructing the data used in fitting the model (see `recover.data`), or by using the `data.frame` provided in context. The default reference grid is determined by the observed levels of any factors, the ordered unique values of character-valued predictors, and the results of `cov.reduce` for numeric predictors. These may be overridden using `at`.

Ability to support a particular class of object depends on the existence of `recover.data` and `lsm.basis` methods – see [extending-lsmeans](#) for details. The call `methods("recover.data")` will help identify these.

In certain models, (e.g., results of `glmer.nb`), it is not possible to identify the original dataset. In such cases, we can work around this by setting `data` equal to the dataset used in fitting the model, or a suitable subset. Only the complete cases in `data` are used, so it may be necessary to exclude some unused variables. Using `data` can also help save computing, especially when the dataset is large. In any case, `data` must represent all factor levels used in fitting the model. It *cannot* be used as an alternative to `at`. (Note: If there is a pattern of NAs that caused one or more factor levels to be excluded when fitting the model, then `data` should also exclude those levels.)

By default, the variance-covariance matrix for the fixed effects is obtained from `object`, usually via its `vcov` method. However, the user may override this via a `vcov` argument, specifying a matrix or a function. If a matrix, it must be square and of the same dimension and parameter order of the fixed effects. If a function, must return a suitable matrix when it is called with `object` as its only argument.

**Nested factors:** Having a nesting structure affects marginal averaging in `lsmeans` in that it is done separately for each level (or combination thereof) of the grouping factors. `ref.grid` tries to discern which factors are nested in other factors, but it is not always obvious, and if it misses some, the user must specify this structure via `nesting`; or later using `update`. `nesting` may be a character vector or a named list. If a list, each name should be the name of a single factor in the grid, and its entry a character vector of the name(s) of its grouping factor(s). `nested` may also be a character value of the form `"factor1 %in% (factor2*factor3)"`. If there is more than one such specification, they may be appended separated by commas, or as a character vector. For example, these specifications are equivalent: `nesting = list(state = "country", city = c("state", "country"))`, `nesting = "state %in% country, city %in% (state*country)"`, and `nesting = c("state %in% country", "city %in% (state*country)")`.

There is a subtle difference between specifying `'type = "response"'` and `'transform = "response"'`. While the summary statistics for the grid itself are the same, subsequent use in `lsmeans` will yield different results if there is a response transformation. With `'type = "response"'`, LS means are computed by averaging together predictions on the *linear-predictor* scale and then back-transforming to the response scale; while with `'transform = "response"'`, the predictions are

already on the response scale so that the LS means will be the arithmetic means of those response-scale predictions. To add further to the possibilities, *geometric* means of the response-scale predictions are obtainable via `'transform = "log", type = "response"`.

The most recent result of `ref.grid`, whether called directly or indirectly via `lsmeans`, `lstrends`, or some other function that calls one of these, is saved in the user's environment as `.Last.ref.grid`. This facilitates checking what reference grid was used, or reusing the same reference grid for further calculations. This automatic saving is enabled by default, but may be disabled via `'lsm.options(save.ref.grid = FALSE)` and re-enabled by specifying `TRUE`.

### Value

An S4 object of class `"ref.grid"` (see [ref.grid-class](#)). These objects encapsulate everything needed to do calculations and inferences for least-squares means, and contain nothing that depends on the model-fitting procedure. As a side effect, the result is also saved as `.Last.ref.grid` (in the global environment, unless this variable is found in another position).

### Author(s)

Russell V. Lenth

### See Also

See also [summary](#) and other methods for the returned objects. Reference grids are fundamental to [lsmeans](#). Click here for more on the [ref.grid](#) class. Supported models are detailed in [models](#).

### Examples

```
require(lsmeans)

fiber.lm <- lm(strength ~ machine*diameter, data = fiber)
ref.grid(fiber.lm)
summary(ref.grid(fiber.lm))

ref.grid(fiber.lm, at = list(diameter = c(15, 25)))

## Not run:
# We could substitute the sandwich estimator vcovHAC(fiber.lm)
# as follows:
require(sandwich)
summary(ref.grid(fiber.lm, vcov. = vcovHAC))

## End(Not run)

# If we thought that the machines affect the diameters
# (admittedly not plausible in this example), then we should use:
ref.grid(fiber.lm, cov.reduce = diameter~machine)

# Multivariate example
MOats.lm = lm(yield ~ Block + Variety, data = MOats)
ref.grid(MOats.lm, mult.name = "nitro")
# silly illustration of how to use 'mult.levs'
```

```
ref.grid(MOats.lm, mult.levs = list(T=LETTERS[1:2], U=letters[1:2]))
```

---

ref.grid-class                    *Classes "ref.grid" and "lsmobj"*

---

## Description

A reference grid encapsulates everything needed to compute least-squares means, independently of the underlying model object. The "lsmobj" class is a minor extension of "ref.grid" where the linear predictors for the reference grid are transformed in some linear way such as marginal averages or contrasts.

## Objects from the Classes

Objects of class "ref.grid" are most commonly created by calling the `ref.grid` function.

Objects of class "lsmobj" are created by calling `lsmeans` or a related function such as `contrast`.

## Slots

**model.info:** Object of class "list" containing the elements `call` (the call that produced the model), `terms` (its terms object), and `xlev` (factor-level information)

**roles:** Object of class "list" containing at least the elements `predictors`, `responses`, and `multresp`. These are character vectors of names of these variables.

**grid:** Object of class "data.frame" containing the combinations of the variables that define the reference grid. In addition, there is an auxiliary column named ".wgt." holding the observed frequencies or weights for each factor combination (excluding covariates). If the model has one or more `offset()` calls, there is an another auxiliary column named ".offset.". Auxiliary columns are not considered part of the reference grid. (However, any variables included in `offset` calls *are* in the reference grid.)

**levels:** Object of class "list" with each entry containing the distinct levels of variables in the reference grid. Note that `grid` is obtained by applying the function `expand.grid` to this list

**matlevs:** Object of class "list" Like `levels` but has the levels of any matrices in the original dataset. Matrix columns must always be reduced to a single value for purposes of the reference grid

**linfct:** Object of class "matrix" giving the linear functions of the regression coefficients for predicting each element of the reference grid. The rows of this matrix go in one-to-one correspondence with the rows of `grid`, and the columns with elements of `bhat`

**bhat:** Object of class "numeric" with the regression coefficients. If there is a multivariate response, this must be flattened to a single vector, and `linfct` and `V` redefined appropriately. Important: `bhat` must *include* any NA values produced by collinearity in the predictors. These are taken care of later in the estimability check.

**nbasis:** Object of class "matrix" with the basis for the non-estimable functions of the regression coefficients. Every LS mean will correspond to a linear combination of rows of `linfct`, and that result must be orthogonal to all the columns of `nbasis` in order to be estimable. This will be NULL if everything is estimable

**V:** Object of class "matrix", the symmetric variance-covariance matrix of `bhat`

**dfun, dfargs:** Objects of class "function" and "list" respectively. `dfun(k, dfargs)` should return the degrees of freedom for the linear function `sum(k*bhat)`, or NA if unavailable

**misc:** A list containing additional information used by methods. These include at least the following: `estName` (the label for the estimates of linear functions), and the default values of `infer`, `level`, and `adjust` to be used in the `summary` method. Elements in this slot may be modified if desired using the `update` method.

**post.beta:** A matrix containing a sample from the posterior distribution of the regression coefficients; or a 1 x 1 matrix of NA if this is not available. When it is non-trivial, the `as.mcmc` method returns `post.beta` times `t(linfct)`, which is a sample from the posterior distribution of the LS means.

### Extends

Class "lsmobj" extends Class "ref.grid", directly. There is hardly a difference between these classes except for how the slots `linfct` and `grid` are obtained, and their show methods.

### Methods

All methods for these objects are S3 methods except for `show`.

**show:** Prints the results of `str` for `ref.grid` objects, and `summary` for `lsmobj` objects.

**str:** Displays a brief listing of the variables and levels defining the grid.

**summary:** Displays a summary of estimates, standard errors, degrees of freedom, and optionally, tests and/or confidence intervals.

**lsmeans:** Computes least-squares means and creates an "lsmobj" object.

**confint:** Confidence intervals for `lsmeans`.

**test:** Hypothesis tests.

**cld:** Compact-letter display for tests of pairwise comparisons

**contrast:** Contrasts among `lsmeans`.

**pairs:** A special case of contrasts for pairwise comparisons.

**update:** Change defaults used primarily by `summary`, such as transformation, p-value adjustment, and confidence level.

### Author(s)

Russell V. Lenth

### See Also

[ref.grid](#), [lsmeans](#)

### Examples

```
showClass("ref.grid")
showClass("lsmobj")
```

---

summary

*Methods for ref.grid objects*


---

## Description

Use these methods to summarize, print, plot, or examine objects of class "ref.grid". They also apply to the class "lsmobj", which is an extension of "ref.grid".

## Usage

```
## S3 method for class 'ref.grid'
summary(object, infer, level, adjust, by, type, df,
        null, delta, side, ...)

## S3 method for class 'ref.grid'
predict(object, type, ...)

## S3 method for class 'ref.grid'
str(object, ...)

## S3 method for class 'ref.grid'
rbind(..., deparse.level = 1, adjust = "bonferroni")

## S3 method for class 'ref.grid'
x[i, adjust, drop.levels = TRUE, ...]

## S3 method for class 'ref.grid'
print(x, ...)
## S3 method for class 'summary.ref.grid'
print(x, ..., digits = NULL, quote = FALSE, right = TRUE)

## S3 method for class 'ref.grid'
xtable(x, caption = NULL, label = NULL, align = NULL,
       digits = 4, display = NULL, auto = FALSE, ...)
## S3 method for class 'summary.ref.grid'
xtable(x, caption = NULL, label = NULL, align = NULL,
       digits = 4, display = NULL, auto = FALSE, ...)
## S3 method for class 'xtable.lsm'
print(x, type = getOption("xtable.type", "latex"),
      include.rownames = FALSE, sanitize.message.function = footnotesize,
      ...)

## S3 method for class 'lsmobj'
plot(x, y, type, intervals = TRUE, comparisons = FALSE,
     alpha = 0.05, adjust = "tukey", int.adjust, ...)
## S3 method for class 'summary.ref.grid'
plot(x, y, horizontal = TRUE,
```

```

    xlab, ylab, layout, ...)

## S3 method for class 'ref.grid'
vcov(object, ...)

regrid (object, transform = c("response", "mu", "unlink", "log", "none"),
        inv.log.lbl = "response", predict.type)

## S3 method for class 'ref.grid'
as.mcmc(x, names = TRUE, sep.chains = TRUE, ...)
## S3 method for class 'ref.grid'
as.mcmc.list(x, names = TRUE, ...)

as.stanfit(object, names = TRUE, ...)

```

### Arguments

<code>object</code>	An object of class "ref.grid".
<code>infer</code>	A vector of two logical values. The first determines whether confidence intervals are displayed, and the second determines whether $t$ tests and $P$ values are displayed. If only one value is provided, it is used for both.
<code>level</code>	Confidence level for confidence intervals, if <code>infer[1]</code> is TRUE.
<code>adjust</code>	Character value naming the method used to adjust $p$ values or confidence limits; or to adjust comparison arrows in plot. See Details.
<code>by</code>	Character name(s) of variables to use for grouping. This affects the family of tests considered in adjusted $P$ values. The printed display of the summary is grouped by the <code>by</code> variables.
<code>type</code>	Type of prediction desired (except in <code>print.xtable</code> ). This only has an effect if there is a known transformation or link function. "response" specifies that the inverse transformation be applied. "mu" (or equivalently, "unlink" is usually the same as "response", but in the case where the model has both a link function and a response transformation, only the link part is back-transformed. Other valid values are "link", "lp", and "linear"; these are equivalent, and request that results be shown for the linear predictor, with no back-transformation. The default is "link", unless the "predict.type" option is in force; see <a href="#">lsm.options</a> . Note that <code>type</code> is also an argument for the <code>print.xtable</code> method; it is passed to <code>print.xtableList</code> in the <b>xtable</b> package.
<code>df</code>	If non-missing a constant number of degrees of freedom to use in constructing confidence intervals and $P$ values (NA specifies asymptotic results).
<code>null</code>	Null hypothesis value(s) against which estimates are tested. May be a single value used for all, or a numeric vector of length equal to the number of tests in each family (i.e., by group in the displayed table).
<code>delta</code>	Numeric value. If zero, ordinary tests of significance are performed. If positive, this specifies a threshold for testing equivalence (using the TOST or two-one-sided-test method), non-inferiority, or non-superiority, depending on side. See Details for how the test statistics are defined.

side	Numeric or character value specifying whether the test is left-tailed (-1, "-", code "<", "left", or "noninferiority"); right-tailed (1, "+", ">", "right", or "noninferiority"); or two-sided (0, 2, "!=", "two-sided", "both", "equivalence", or "=").
deparse.level	This argument is needed by the generic <code>rbind</code> method, but ignored by its <code>ref.grid</code> method.
drop.levels	Logical value to specify whether or not the <code>levels</code> slot should be recomputed based on a possibly reduced number of levels of factors in the grid.
x	The object to be subsetted, printed, plotted, or converted.
y	This argument is ignored.
i	Integer index(es) of which linear functions to extract.
horizontal	Determines orientation of plotted confidence intervals.
intervals	If TRUE, confidence intervals are plotted for each estimate
comparisons	If TRUE, "comparison arrows" are added to the plot, in such a way that the degree to which arrows overlap reflects as much as possible the significance of the comparison of the two estimates.
alpha	The alpha argument to use in constructing comparison arrows.
int.adjust	the multiplicity adjustment method for the plotted confidence intervals; if missing, it defaults to the object's internal <code>adjust</code> setting (see <a href="#">update</a> ). (Note: the <code>adjust</code> argument in <code>plot</code> sets the <code>adjust</code> method for the comparison arrows, not the confidence intervals.)
transform	Character value. If "response" or "mu", the inverse transformation is applied to the estimates in the grid (but if there is both a link function and a response transformation, "mu" back-transforms only the link part); if "log", the results are formulated as if the response had been log-transformed; if "none", predictions thereof are on the same scale as in object, and any internal transformation information is preserved. For compatibility with past versions, <code>transform</code> may also be logical; TRUE is taken as "response", and FALSE as "none".
inv.log.lbl	Character value. This applies only when <code>transform = "log"</code> , and is used to label the predictions if subsequently summarized with <code>type = "response"</code> .
predict.type	Character value. If provided, the returned object is first <a href="#">updated</a> with the given type, e.g., "response".
names	Logical scalar or vector specifying whether variable names are appended to levels in the column labels for the <code>as.mcmc</code> or <code>as.mcmc.list</code> result – e.g., column names of <code>treat A</code> and <code>treat B</code> versus just A and B. When there is more than one variable involved, the elements of <code>names</code> are used cyclically.
sep.chains	Logical value. If TRUE, and there is more than one MCMC chain available, an <code>mcmc.list</code> object is returned by <code>as.mcmc</code> , with separate <code>lsmeans</code> posteriors in each chain.
..., digits, quote, right, caption, label, align, display, auto, include.rownames, sanitize.message	For summaries, these are additional arguments passed to other methods including <a href="#">print.data.frame</a> , <a href="#">xtableList</a> , <a href="#">print.xtableList</a> , <a href="#">update</a> , or <a href="#">dotplot</a> as appropriate. If not specified, appropriate defaults are used. For example, the default layout is one column of horizontal panels or one row of vertical panels.

## Details

**Defaults for summarization, etc.:** The misc slot in object contains default values for by, infer, level, adjust, type, null, side, and delta. These defaults vary depending on the code that created the object. The `update` method may be used to change these defaults. In addition, any options set using `'lsm.options(summary=...)` will trump those stored in the object's misc slot.

**Transformations and links:** With `type="response"`, the transformation assumed can be found in `'object@misc$tran'`, and its label, for the summary is in `'object@misc$inv.lbl'`. Any *t* or *z* tests are still performed on the scale of the linear predictor, not the inverse-transformed one. Similarly, confidence intervals are computed on the linear-predictor scale, then inverse-transformed.

**Confidence-limit and P-value adjustments:** The `adjust` argument specifies a multiplicity adjustment for tests or confidence intervals. This adjustment always is applied *separately* to each table or sub-table that you see in the printed output (see the details on `rbind` below for how to combine tables). The valid values of `adjust` are as follows:

`"tukey"` Uses the Studentized range distribution with the number of means in the family. (Available for two-sided cases only.)

`"scheffe"` Computes *p* values from the *F* distribution, according to the Scheffe critical value of  $\sqrt{kF(k, d)}$ , where *d* is the error degrees of freedom and *k* is (family size minus 1) for contrasts, and (number of estimates) otherwise. (Available for two-sided cases only.)

`"sidak"` Makes adjustments as if the estimates were independent (a conservative adjustment in many cases).

`"bonferroni"` Multiplies *p* values, or divides significance levels by the number of estimates. This is a conservative adjustment.

`"dunnett"` Uses an approximation to the Dunnett distribution for a family of estimates having pairwise correlations of 0.5 (as is true when comparing treatments with a control with equal sample sizes). The accuracy of the approximation improves with the number of simultaneous estimates, and is much faster than `"mvt"`. (Available for two-sided cases only.)

`"mvt"` Uses the multivariate *t* distribution to assess the probability or critical value for the maximum of *k* estimates. This method produces the same *p* values and intervals as the default summary or `confint` methods to the results of `as.glht`. In the context of pairwise comparisons or comparisons with a control, this produces "exact" Tukey or Dunnett adjustments, respectively. However, the algorithm (from the `mvtnorm` package) uses a Monte Carlo method, so results are not exactly repeatable unless the random-number seed is used (see `set.seed`). As the family size increases, the required computation time will become noticeable or even intolerable, making the `"tukey"`, `"dunnett"`, or others more attractive.

`"none"` Makes no adjustments to the *p* values.

For P-value adjustments only, the Bonferroni-inequality-based adjustment methods in `p.adjust` are also available (currently, these include `"holm"`, `"hochberg"`, `"hommel"`, `"bonferroni"`, `"BH"`, `"BY"`, `"fdr"`, and `"none"`). If a `p.adjust.methods` method other than `"bonferroni"` or `"none"` is specified for confidence limits, the straight Bonferroni adjustment is used instead. Also, if an adjustment method is not appropriate (e.g., using `"tukey"` with one-sided tests, or with results that are not pairwise comparisons), a more appropriate method (usually `"sidak"`) is substituted.

In some cases, confidence and *p*-value adjustments are only approximate – especially when the degrees of freedom or standard errors vary greatly within the family of tests. The `"mvt"` method is



always the correct one-step adjustment, but it can be very slow. One may use `as.glht` with methods in the **multcomp** package to obtain non-conservative multi-step adjustments to tests.

**Information:** The `str` method outputs a very brief summary of the object, whereas `levels` produces a `data.frame` containing the combinations of levels of predictor values that define the reference grid.

**xtable-related methods:** The `xtable` methods actually use `xtableList`, because of the ability to display messages such as those for P-value adjustments. These methods return an object of class `"xtable.lsm"` – an extension of `"xtableList"`. Unlike other `xtable` methods, the number of digits defaults to 4; and degrees of freedom and *t* ratios are always formatted independently of digits. The `print` method uses `print.xtableList`, and any `...` arguments are passed there.

**rbind and [ methods:** `rbind` can be used to combine two or more reference grids into one. The `"["` method for `ref.grid`s may be used to obtain a subset. The primary reason for doing this would be to redefine the family of tests to which a P-value adjustment method applies. In `rbind`, the variables defined in the objects' `grid`s are merged into one grid, and the returned object has no "by" variables and the multiplicity adjustment method set to `"mvt"` (as this is likely the only appropriate one). `rbind` throws an error if there are any mismatches among the dimensions, fixed-effect coefficients, or covariance matrices.

**Non-estimable cases:** When the model is rank-deficient, each row *x* of object's `linfct` slot is each checked for estimability. If `sum(x*bhat)` is found to be non-estimable, then an NA is displayed for the estimate (as well as any associated statistics). This check is performed using the orthonormal basis *N* in the `nbasis` slot for the null space of the rows of the model matrix. Estimability fails when  $\|Nx\|^2/\|x\|^2$  exceeds `tol`, which by default is `1e-8`. You may change it via `lsm.options` by setting `estble.tol` to the desired value.

**More on tests:** When  $\delta = 0$ , test statistics are of the usual form  $(\text{estimate} - \text{null})/SE$ , or notationally,  $t = (Q - \theta_0)/SE$  where *Q* is our estimate of  $\theta$ ; then left, right, or two-sided *p* values are produced.

When  $\delta$  is positive, the test statistic depends on `side` as follows.

Left-sided (nonsuperiority,  $H_0 : \theta \geq \theta_0 + \delta$  versus  $H_1 : \theta < \theta_0 + \delta$ ):  $t = (Q - \theta_0 - \delta)/SE$ . The *p* value is the lower-tail probability.

Right-sided (noninferiority):  $H_0 : \theta \leq \theta_0 - \delta$  versus  $H_1 : \theta > \theta_0 - \delta$ :  $t = (Q - \theta_0 + \delta)/SE$ . The *p* value is the upper-tail probability.

Two-sided (equivalence):  $H_0 : |\theta - \theta_0| \geq \delta$  versus  $H_1 : |\theta - \theta_0| < \delta$ :  $t = (|Q - \theta_0| - \delta)/SE$ . The *p* value is the lower-tail probability.

**Plots:** The `plot` method for `"lsmobj"` or `"summary.ref.grid"` objects (but not `"ref.grid"` objects themselves) produces a plot displaying confidence intervals for the estimates. If any `by` variables are in force, the plot is divided into separate panels. These functions use the `dotplot` function, and thus require that the **lattice** package be installed. For `"summary.ref.grid"` objects, the `...` arguments in `plot` are passed *only* to `dotplot`, whereas for `"lsmobj"` objects, the object is updated using `...` before summarizing and plotting.

In plots with `comparisons = TRUE`, the resulting arrows are only approximate, and in some cases may fail to accurately reflect the pairwise comparisons of the estimates – especially when estimates having large and small standard errors are intermingled in just the wrong way.

**Re-gridding:** The `regrid` function reparameterizes an existing `ref.grid` so that its `linfct` slot is the identity matrix and its `bhat` slot consists of the estimates at the grid points. If `transform` is `TRUE`, the inverse transform is applied to the estimates. Outwardly, the summary after applying

regrid is identical to what it was before (using ‘type=“response”’ if transform is TRUE). But subsequent contrasts will be conducted on the transformed scale – which is the reason this function exists. See the example below. In cases where the degrees of freedom depended on the linear function being estimated, the d.f. from the reference grid are saved, and a kind of “containment” method is substituted in the returned object whereby the calculated d.f. for a new linear function will be the minimum d.f. among those having nonzero coefficients. This is kind of an *ad hoc* method, and it can over-estimate the degrees of freedom in some cases.

**MCMC samplers:** When the object’s `post.beta` slot is non-trivial, `as.mcmc` will return an `mcmc` or `mcmc.list` object that can be summarized or plotted using methods in the **coda** package. Alternatively, `as.stanfit` will return a `stanfit` object that can be summarized or plotted using methods in the **rstan** package. You may use any of these functions regardless of what packages were originally used to implement the MCMC method. In these functions, `post.beta` is transformed by post-multiplying it by `t(linfct)`, creating a sample from the posterior distribution of LS means. In `as.mcmc`, if `sep.chains` is TRUE and there is in fact more than one chain, an `mcmc.list` is returned with each chain’s results. The `as.mcmc.list` method is guaranteed to return an `mcmc.list`, even if it comprises just one chain. Note that `stanfit` objects are designed already for multiple chains.

## Value

The `summary` method for “`ref.grid`” objects returns an object of class “`summary.ref.grid`”, which extends “`data.frame`”. `xtable` returns an object of class “`xtable.lsm`”, as explained in details. `plot` returns an object of class “`trellis`”. `vcov` returns the covariance matrix of the product of the object’s `linfct` and `bhat` slots. `as.mcmc` returns a **coda** `mcmc` object.

## Author(s)

Russell V. Lenth

## See Also

Methods for the closely related “`lsmobj`” class can be found in `contrast`, `cld`, and `glht`. For more on Bonferroni-based P-value adjustments, see `p.adjust`. Also, `test` and `confint` are essentially front-ends for `summary`, so additional examples may be found there.

## Examples

```
require(lsmmeans)
warp.lm <- lm(breaks ~ wool * tension, data = warpbreaks)
warp.rg <- ref.grid(warp.lm)
str(warp.rg)
levels(warp.rg)

summary(warp.rg)

summary(warp.rg, by = "wool",
        infer = c(TRUE, FALSE), level = .90, adjust = "sidak")

# Do all pairwise comparisons within rows or within columns,
# all considered as one family of tests:
```

```

w.t <- pairs(lsmmeans(warp.rg, ~ wool | tension))
t.w <- pairs(lsmmeans(warp.rg, ~ tension | wool))
rbind(w.t, t.w)

# Transformed response
sqwarp.rg <- ref.grid(update(warp.lm, sqrt(breaks) ~ .))
summary(sqwarp.rg)

# Back-transformed results - compare with summary of 'warp.rg'
summary(sqwarp.rg, type = "response")

# But differences of sqrts can't be back-transformed
summary(pairs(sqwarp.rg, by = "wool"), type = "response")

# We can do it via regrid
sqwarp.rg2 <- regrid(sqwarp.rg)
summary(sqwarp.rg2) # same as for sqwarp.rg with type = "response"
pairs(sqwarp.rg2, by = "wool")

# Logistic regression
# Reshape the Titanic data
Titan <- do.call("expand.grid", dimnames(Titanic)[-4])
Titan$Died <- matrix(Titanic, ncol=2)
Titan.glm <- glm(Died ~ (Class + Sex + Age)^2,
  family = binomial, data = Titan)
Titan.lsm <- lsmmeans(Titan.glm, ~ Class|Sex, at = list(Age="Adult"))
summary(Titan.lsm, type="response")
summary(pairs(Titan.lsm), type="response")

# Nonsuperiority test: Is any class no more likely to die than
# the 1st class passengers?
summary(contrast(Titan.lsm, "trt.vs.ctrl1"), delta = 1,
  adjust = "none", side = "<")

# Plot 90% CIs on the response scale
plot(Titan.lsm, type = "response", level = .90,
  xlab = "Predicted probability of drowning")

```

---

transition

*Transition to **emmeans***


---

## Description

The **lsmmeans** package is being deprecated and further development will take place in its successor, **emmeans**. Users may use **emmeans** in almost exactly the same way as **lsmmeans**, but a few function names and internal details are changed.

## Details

In transitioning to **emmeans**, users will find that the vignettes are constructed quite differently and that, in those and in the documentation, emphasis is placed on “estimated marginal means” rather than “least-squares means”. The latter term is broader and more appropriate for use with some models, e.g. ordinal regression, that don’t really involve least-squares methods. That is the reason for the change.

Accordingly, **emmeans** users are encouraged to use the functions `emmeans()`, `emtrends()`, `emmip()`, etc. in lieu of `lsmeans()`, etc. The latter functions *are still available* in **emmeans**; they run the corresponding `emmxxx` function and relabel the results.

The **emmeans** package provides some functions that help convert scripts and R Markdown files containing **lsmeans** code so they will work in **emmeans**. There is also a function to convert `ref.grid` and `lsmobj` objects to the `emmGrid` objects used in **emmeans**. More extensive information is given in `vignette("transition-from-lsmeans", package = "emmeans")`.

## Author(s)

Russell V. Lenth

---

update

*Set or retrieve options for objects and summaries in **lsmeans***

---

## Description

Objects of class `ref.grid` or `lsmobj` contain several settings in their “misc” slot that affect primarily the defaults used by `summary`. This `update` method allows them to be changed more safely than by modifying this slot directly.

In addition, the user may set defaults for all objects using `options(lsmeans = ...)`, or more conveniently using the `lsm.options` and `get.lsm.option` functions documented here (or its courtesy wrappers, `pmm.options` and `get.pmm.option` for those who dislike the ‘least-squares means’ terminology).

## Usage

```
## S3 method for class 'ref.grid'
update(object, ..., silent = FALSE)

lsm.options(...)
get.lsm.option(x, default = defaults.lsm[[x]])

pmm.options(...)
get.pmm.option(...)
```

**Arguments**

object	An object of class <code>ref.grid</code> (or its extension, <code>lsmobj</code> )
...	Arguments specifying elements' names and their new values.
silent	If FALSE, a message is displayed for any unmatched names.
x	Character string holding an option name for <code>lsm.options</code> .
default	Return value if x is not found.

**Details**

**Using update:** In `update`, the names in ... are partially matched against those that are valid, and if a match is found, it adds or replaces the current setting. The valid names are

`nesting` (named list) specifies the nesting structure. The names are those of nested factors, and the elements are character vectors of the factors they are nested in. See the `nesting` argument and Details section of `ref.grid`. The current nesting structure is displayed by `link{str}`.

`tran`, `tran2` (list or character) specifies the transformation which, when inverted, determines the results displayed by `summary`, `predict`, or `lsmip` when `type="response"`. The value may be the name of a standard transformation from `make.link` or additional ones supported by name, such as `log2`; or, for a custom transformation, a list containing at least the functions `linkinv` (the inverse of the transformation) and `mu.eta` (the derivative thereof). The `make.tran` function returns such lists for a number of popular transformations. See the help page of `make.tran` for details as well as information on the additional named transformations that are supported. `tran2` is just like `tran` except it is a second transformation (i.e., a response transformation in a generalized linear model).

`tran.mult` Multiple for `tran`. For example, for the response transformation `'2*sqrt(y)'` (or `'sqrt(y) + sqrt(y + 1)'`, for that matter), we should have `tran = "sqrt"` and `tran.mult = 2`. If absent, a multiple of 1 is assumed.

`estName` (character) is the column label used for displaying predictions or LS means.

`inv.lbl` (character) is the column label to use for predictions or LS means when `type="response"`.

`by.vars` (character) vector or NULL) the variables used for grouping in the summary, and also for defining subfamilies in a call to `contrast`.

`pri.vars` (character vector) are the names of the grid variables that are not in `by.vars`. Thus, the combinations of their levels are used as columns in each table produced by `summary`.

`alpha` (numeric) is the default significance level for tests, in `summary` as well as `cld` and `plot` when `'intervals = TRUE'`

`adjust` (character) is the default for the `adjust` argument in `summary`.

`estType` (character) is the type of the estimate. It should match one of `'c("prediction", "contrast", "pairs")'`. This is used along with `"adjust"` to determine appropriate adjustments to P values and confidence intervals.

`famSize` (integer) is the `nmeans` parameter for `ptukey` when `adjust="tukey"`.

`infer` (logical vector of length 2) is the default value of `infer` in `summary`.

`level` (numeric) is the default confidence level, `level`, in `summary`

`df` (numeric) overrides the default degrees of freedom with a specified single value.

`null` (numeric) null hypothesis for `summary` or `test` (taken to be zero if missing).

`side` (numeric or character) side specification for `summary` or `test` (taken to be zero if missing).

`delta` (numeric) delta specification for summary or test (taken to be zero if missing).

`predict.type` (character) sets the default method of displaying predictions in `summary`, `predict`, and `lsmip`. Valid values are "link" (with synonyms "lp" and "linear"), or "response".

`avgd.over` (character) vector) are the names of the variables whose levels are averaged over in obtaining marginal averages of predictions, i.e., LS means. Changing this might produce a misleading printout, but setting it to `character(0)` will suppress the "averaged over" message in the summary.

`initMesg` (character) is a string that is added to the beginning of any annotations that appear below the `summary` display.

`methDesc` (character) is a string that may be used for creating names for a list of `lsmobj` objects.

**(any slot name)** If the name matches an element of `slotNames(object)`, that slot is replaced by the supplied value, if it is of the required class (otherwise an error occurs). Note that all the other possibilities above refer to elements of `misc`; hence, you probably don't want to replace `misc` itself. The user must be very careful in replacing slots because they are interrelated; for example, the `levels` and `grid` slots must involve the same variable names, and the lengths and dimensions of `grid`, `linfct`, `bhat`, and `V` must conform.

**Using `lsm.options`:** In `lsm.options`, we may set or change the default values for the above attributes in the `lsmeans` option list (see `options`). Currently, the following elements of this list are used if specified:

`ref.grid` A named list of defaults for objects created by `ref.grid`. This could affect other objects as well. For example, if `lsmeans` is called with a fitted model object, it calls `ref.grid` and this option will affect the resulting `lsmobj` object.

`lsmeans` A named list of defaults for objects created by `lsmeans` (or `lstrends`).

`contrast` A named list of defaults for objects created by `contrast` (or `pairs`).

`summary` A named list of defaults used by the methods `summary`, `predict`, and `lsmip`. The only option that can affect the latter two is "predict.method".

`estble.tol` Tolerance for determining estimability in rank-deficient cases. If absent, the value in `defaults.lsm$estble.tol` is used.

**(others)** Other options may be accessed by support code for particular model classes (see `models`). For example, the `lmer.df`, `disable.pbkrtest`, and `pbkrtest.limit` options affect how degrees of freedom are computed for `lmerMod` objects (**lme4** package).

## Value

`update` returns a copy of object with its "misc" slot modified (and perhaps other slots). `lsm.options` returns the current options (same as the result of `'getOption("lsmeans")'`) – invisibly, unless called with no arguments.

## Note

If a call to `lsmeans`, `contrast`, or `ref.grid` contains a non-NULL options list, those options are passed in a call to `update` on the constructed object before it is returned. This allows you, for example, to override the defaults used by `summary`. In addition, user defaults may be set using an `link{options}` setting for "lsmeans". It should be a list with one or more named elements `lsmeans`, `contrast`, or `ref.grid`, used for setting the defaults for objects constructed by functions of these same names. Note that options can get "inherited". See the examples.

Unlike the update method for model classes (lm, glm, etc.), this does not re-fit or re-estimate anything; but it does affect how object is treated by other methods for its class.

**Author(s)**

Russell V. Lenth

**See Also**

[summary](#), [make.tran](#)

**Examples**

```
# An altered log transformation

warp.lm1 <- lm(log(breaks + 1) ~ wool*tension, data = warpbreaks)
rg1 <- update(ref.grid(warp.lm1),
             tran = list(linkinv = function(eta) exp(eta) - 1,
                        mu.eta = function(eta) exp(eta)),
             inv.lbl = "pred.breaks")

summary(rg1, type = "response")

## Not run:
lsm.options(ref.grid = list(level = .90),
            contrast = list(infer = c(TRUE,FALSE)),
            estble.tol = 1e-6)
# Sets default confidence level to .90 for objects created by ref.grid
# AS WELL AS lsmeans called with a model object (since it creates a
# reference grid). In addition, when we call 'contrast', 'pairs', etc.,
# confidence intervals rather than tests are displayed by default.

## End(Not run)

## Not run:
lsm.options(disable.pbkrtest = TRUE)
# This forces use of asymptotic methods for lmerMod objects.
# Set to FALSE or NULL to re-enable using pbkrtest.

## End(Not run)

# See tolerance being used for determining estimability
get.lsm.option("estble.tol")
```

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