

# Package ‘markovchain’

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**Type** Package

**Title** Easy Handling Discrete Time Markov Chains

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**Description** Functions and S4 methods to create and manage discrete time Markov chains more easily. In addition functions to perform statistical (fitting and drawing random variates) and probabilistic (analysis of their structural proprieties) analysis are provided.

**License** GPL-2

**Depends** R (>= 3.5.0), methods

**Imports** igraph, Matrix, matlab, expm, stats4, parallel, Rcpp (>= 0.12.18), RcppParallel, utils, stats, grDevices

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## R topics documented:

markovchain-package . . . . .	3
absorbingStates . . . . .	4
blanden . . . . .	6
committorAB . . . . .	7
conditionalDistribution . . . . .	8
craigsendi . . . . .	9
createSequenceMatrix . . . . .	9
ctmc-class . . . . .	11
ctmcFit . . . . .	13
expectedRewards . . . . .	14
expectedRewardsBeforeHittingA . . . . .	15
ExpectedTime . . . . .	15
firstPassage . . . . .	16
firstPassageMultiple . . . . .	17
fitHigherOrder . . . . .	18
fitHigherOrderMultivarMC . . . . .	19
freq2Generator . . . . .	20
generatorToTransitionMatrix . . . . .	21
HigherOrderMarkovChain-class . . . . .	22
holson . . . . .	22
hommc-class . . . . .	23
ictmc-class . . . . .	24
impreciseProbabilityatT . . . . .	24
inferHyperparam . . . . .	25
is.accessible . . . . .	26
is.CTMCirreducible . . . . .	27
is.irreducible . . . . .	28
is.TimeReversible . . . . .	29
kullback . . . . .	30
markovchain-class . . . . .	30
markovchainList-class . . . . .	33
markovchainListFit . . . . .	35
markovchainSequence . . . . .	36
meanFirstPassageTime . . . . .	37
multinomialConfidenceIntervals . . . . .	38
name . . . . .	39
name<- . . . . .	40

noofVisitsDist . . . . .	40
predictHommc . . . . .	41
predictiveDistribution . . . . .	42
preproglucacon . . . . .	43
priorDistribution . . . . .	44
probabilityatT . . . . .	45
rain . . . . .	46
rctmc . . . . .	47
rmarkovchain . . . . .	48
sales . . . . .	50
show,hommc-method . . . . .	50
states . . . . .	51
steadyStates . . . . .	52
tm_abs . . . . .	53
transition2Generator . . . . .	53
transitionProbability . . . . .	54
verifyMarkovProperty . . . . .	55

<b>Index</b>	<b>57</b>
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markovchain-package    *Easy Handling Discrete Time Markov Chains*

---

## Description

The package contains classes and method to create and manage (plot, print, export for example) discrete time Markov chains (DTMC). In addition it provide functions to perform statistical (fitting and drawing random variates) and probabilistic (analysis of DTMC proprieties) analysis.

## Details

Package: markovchain  
 Type: Package  
 Version: 0.6.9.10  
 Date: 2018-05-30  
 License: GPL-2  
 Depends: R (>= 3.4.0), methods, expm, matlab, igraph, Matrix

## Author(s)

Giorgio Alfredo Spedicato Maintainer: Giorgio Alfredo Spedicato <spedicato\_giorgio@yahoo.it>

## References

Discrete-Time Markov Models, Bremaud, Springer 1999

**Examples**

```

#create some markov chains
statesNames=c("a","b")
mcA<-new("markovchain", transitionMatrix=matrix(c(0.7,0.3,0.1,0.9),byrow=TRUE,
nrow=2, dimnames=list(statesNames,statesNames)))

statesNames=c("a","b","c")
mcB<-new("markovchain", states=statesNames, transitionMatrix=
      matrix(c(0.2,0.5,0.3,
              0,1,0,
              0.1,0.8,0.1),nrow=3, byrow=TRUE, dimnames=list(statesNames,
statesNames)
      ))

statesNames=c("a","b","c","d")
matrice<-matrix(c(0.25,0.75,0,0,0.4,0.6,0,0,0,0.1,0.9,0,0,0.7,0.3),
nrow=4, byrow=TRUE)
mcC<-new("markovchain", states=statesNames, transitionMatrix=matrice)
mcD<-new("markovchain", transitionMatrix=matrix(c(0,1,0,1), nrow=2,byrow=TRUE))

#operations with S4 methods

mcA^2
steadyStates(mcB)
absorbingStates(mcB)
markovchainSequence(n=20, markovchain=mcC, include=TRUE)

```

---

absorbingStates

*Various function to perform structural analysis of DTMC*


---

**Description**

These functions return absorbing and transient states of the markovchain objects.

**Usage**

```
absorbingStates(object)
```

```
transientStates(object)
```

```
## S4 method for signature 'markovchain'
transientStates(object)
```

```
canonicForm(object)
```

```
communicatingClasses(object)
```

```
recurrentClasses(object)
```

```
period(object)
```

### Arguments

object            A markovchain object.

### Value

vector, matrix or list

### Author(s)

Giorgio Alfredo Spedicato

### References

Feres, Matlab listing for markov chain.

### See Also

[markovchain](#)

### Examples

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
              matrix(c(0.2, 0.5, 0.3,
                      0, 1, 0,
                      0.1, 0.8, 0.1), nrow = 3, byrow = TRUE,
                      dimnames = list(statesNames, statesNames)
              ))
```

```
communicatingClasses(markovB)
recurrentClasses(markovB)
absorbingStates(markovB)
transientStates(markovB)
canonicForm(markovB)
```

```
# periodicity analysis : 1
E <- matrix(c(0, 1, 0, 0, 0.5, 0, 0.5, 0, 0, 0.5, 0, 0.5, 0, 0, 1, 0),
            nrow = 4, ncol = 4, byrow = TRUE)
mcE <- new("markovchain", states = c("a", "b", "c", "d"),
           transitionMatrix = E,
           name = "E")
```

```
is.irreducible(mcE) #true
period(mcE) #2
```

```
# periodicity analysis : 2
```

```

myMatr <- matrix(c(0, 0, 1/2, 1/4, 1/4, 0, 0,
                  0, 0, 1/3, 0, 2/3, 0, 0,
                  0, 0, 0, 0, 0, 1/3, 2/3,
                  0, 0, 0, 0, 0, 1/2, 1/2,
                  0, 0, 0, 0, 0, 3/4, 1/4,
                  1/2, 1/2, 0, 0, 0, 0, 0,
                  1/4, 3/4, 0, 0, 0, 0, 0), byrow = TRUE, ncol = 7)
myMc <- new("markovchain", transitionMatrix = myMatr)
period(myMc)

```

---

blanden

*Mobility between income quartiles*


---

### Description

This table show mobility between income quartiles for father and sons for the 1970 cohort born

### Usage

```
data(blanden)
```

### Format

An object of class `table` with 4 rows and 4 columns.

### Details

The rows represent fathers' income quartile when the son is aged 16, whilst the columns represent sons' income quartiles when he is aged 30 (in 2000).

### Source

Personal reworking

### References

Jo Blanden, Paul Gregg and Stephen Machin, *Intergenerational Mobility in Europe and North America*, Center for Economic Performances (2005)

### Examples

```

data(blanden)
mobilityMc<-as(blanden, "markovchain")

```

---

committorAB	<i>Calculates committor of a markovchain object with respect to set A, B</i>
-------------	--

---

**Description**

Returns the probability of hitting states from set A before set B with different initial states

**Usage**

```
committorAB(object,A,B,p)
```

**Arguments**

object	a markovchain class object
A	a set of states
B	a set of states
p	initial state (default value : 1)

**Details**

The function solves a system of linear equations to calculate probability that the process hits a state from set A before any state from set B

**Value**

Return a vector of probabilities in case initial state is not provided else returns a number

**Examples**

```
transMatr <- matrix(c(0,0,0,1,0.5,
                     0.5,0,0,0,0,
                     0.5,0,0,0,0,
                     0,0.2,0.4,0,0,
                     0,0.8,0.6,0,0.5),
                    nrow = 5)
object <- new("markovchain", states=c("a","b","c","d","e"),transitionMatrix=transMatr)
committorAB(object,c(5),c(3))
```

conditionalDistribution

conditionalDistribution of a Markov Chain

---

### Description

It extracts the conditional distribution of the subsequent state, given current state.

### Usage

```
conditionalDistribution(object, state)
```

### Arguments

object	A markovchain object.
state	Subsequent state.

### Value

A named probability vector

### Author(s)

Giorgio Spedicato, Deepak Yadav

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

[markovchain](#)

### Examples

```
# define a markov chain
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,
    byrow = TRUE, dimnames = list(statesNames, statesNames)))

conditionalDistribution(markovB, "b")
```



---

`craigsendi`*CD4 cells counts on HIV Infected between zero and six month*

---

**Description**

This is the table shown in Craig and Sendi paper showing zero and six month CD4 cells count in six brackets

**Usage**

```
data(craigsendi)
```

**Format**

The format is: table [1:3, 1:3] 682 154 19 33 64 19 25 47 43 - attr(\*, "dimnames")=List of 2 ..\$ : chr [1:3] "0-49" "50-74" "75-UP" ..\$ : chr [1:3] "0-49" "50-74" "75-UP"

**Details**

Rows represent counts at the beginning, cols represent counts after six months.

**Source**

Estimation of the transition matrix of a discrete time Markov chain, Bruce A. Craig and Peter P. Sendi, Health Economics 11, 2002.

**References**

see source

**Examples**

```
data(craigsendi)
csMc<-as(craigsendi, "markovchain")
steadyStates(csMc)
```

---

`createSequenceMatrix` *Function to fit a discrete Markov chain*

---

**Description**

Given a sequence of states arising from a stationary state, it fits the underlying Markov chain distribution using either MLE (also using a Laplacian smoother), bootstrap or by MAP (Bayesian) inference.

**Usage**

```
createSequenceMatrix(stringchar, toRowProbs = FALSE, sanitize = FALSE,
  possibleStates = character())
```

```
markovchainFit(data, method = "mle", byrow = TRUE, nboot = 10L,
  laplacian = 0, name = "", parallel = FALSE,
  confidencelevel = 0.95, confint = TRUE, hyperparam = matrix(),
  sanitize = FALSE, possibleStates = character())
```

**Arguments**

stringchar	It can be a nx2 matrix or a character vector or a list
toRowProbs	converts a sequence matrix into a probability matrix
sanitize	put 1 in all rows having rowSum equal to zero
possibleStates	Possible states which are not present in the given sequence
data	It can be a character vector or a nx2 matrix or a nx2 data frame or a list
method	Method used to estimate the Markov chain. Either "mle", "map", "bootstrap" or "laplace"
byrow	it tells whether the output Markov chain should show the transition probabilities by row.
nboot	Number of bootstrap replicates in case "bootstrap" is used.
laplacian	Laplacian smoothing parameter, default zero. It is only used when "laplace" method is chosen.
name	Optional character for name slot.
parallel	Use parallel processing when performing Bootstrap estimates.
confidencelevel	

$\alpha$

confint	level for confidence intervals width. Used only when method equal to "mle". a boolean to decide whether to compute Confidence Interval or not.
hyperparam	Hyperparameter matrix for the a priori distribution. If none is provided, default value of 1 is assigned to each parameter. This must be of size kxk where k is the number of states in the chain and the values should typically be non-negative integers.

**Details**

Disabling confint would lower the computation time on large datasets. If data or stringchar contain NAs, the related NA containing transitions will be ignored.

**Value**

A list containing an estimate, log-likelihood, and, when "bootstrap" method is used, a matrix of standards deviations and the bootstrap samples. When the "mle", "bootstrap" or "map" method is used, the lower and upper confidence bounds are returned along with the standard error. The "map" method also returns the expected value of the parameters with respect to the posterior distribution.

**Note**

This function has been rewritten in Rcpp. Bootstrap algorithm has been defined "heuristically". In addition, parallel facility is not complete, involving only a part of the bootstrap process. When data is either a `data.frame` or a `matrix` object, only MLE fit is currently available.

**Author(s)**

Giorgio Spedicato, Tae Seung Kang, Sai Bhargav Yalamanchi

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010  
 Inferring Markov Chains: Bayesian Estimation, Model Comparison, Entropy Rate, and Out-of-Class Modeling, Christopher C. Strelhoff, James P. Crutchfield, Alfred Hubler, Santa Fe Institute  
 Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

**See Also**

[markovchainSequence](#), [markovchainListFit](#)

**Examples**

```
sequence <- c("a", "b", "a", "a", "a", "a", "b", "a", "b", "a", "b", "a", "a",
             "b", "b", "b", "a")
sequenceMatr <- createSequenceMatrix(sequence, sanitize = FALSE)
mcFitMLE <- markovchainFit(data = sequence)
mcFitBSP <- markovchainFit(data = sequence, method = "bootstrap", nboot = 5, name = "Bootstrap Mc")

na.sequence <- c("a", NA, "a", "b")
# There will be only a (a,b) transition
na.sequenceMatr <- createSequenceMatrix(na.sequence, sanitize = FALSE)
mcFitMLE <- markovchainFit(data = na.sequence)

# data can be a list of character vectors
sequences <- list(x = c("a", "b", "a"), y = c("b", "a", "b", "a", "c"))
mcFitMap <- markovchainFit(sequences, method = "map")
mcFitMle <- markovchainFit(sequences, method = "mle")
```

---

ctmc-class

*Class "ctmc"*


---

**Description**

The S4 class that describes `ctmc` (continuous time Markov chain) objects.

**Objects from the Class**

Objects can be created by calls of the form `new("ctmc", states, byrow, generator, ...)`.



```
steadyStates(molecularCTMC)
## Not run: plot(molecularCTMC)
```

---

ctmcFit *Function to fit a CTMC*

---

### Description

This function fits the underlying CTMC give the state transition data and the transition times using the maximum likelihood method (MLE)

### Usage

```
ctmcFit(data, byrow = TRUE, name = "", confidencelevel = 0.95)
```

### Arguments

data	It is a list of two elements. The first element is a character vector denoting the states. The second is a numeric vector denoting the corresponding transition times.
byrow	Determines if the output transition probabilities of the underlying embedded DTMC are by row.
name	Optional name for the CTMC.
confidencelevel	Confidence level for the confidence interval construction.

### Details

Note that in data, there must exist an element wise corresponding between the two elements of the list and that `data[[2]][1]` is always 0.

### Value

It returns a list containing the CTMC object and the confidence intervals.

### Author(s)

Sai Bhargav Yalamanchi

### References

Continuous Time Markov Chains (vignette), Sai Bhargav Yalamanchi, Giorgio Alfredo Spedicato 2015

### See Also

[rctmc](#)

**Examples**

```
data <- list(c("a", "b", "c", "a", "b", "a", "c", "b", "c"), c(0, 0.8, 2.1, 2.4, 4, 5, 5.9, 8.2, 9))  
ctmcFit(data)
```

---

expectedRewards	<i>Expected Rewards for a markovchain</i>
-----------------	---

---

**Description**

Given a markovchain object and reward values for every state, function calculates expected reward value after n steps.

**Usage**

```
expectedRewards(markovchain,n,rewards)
```

**Arguments**

markovchain	the markovchain-class object
n	no of steps of the process
rewards	vector depicting rewards coresponding to states

**Details**

the function uses a dynamic programming approach to solve a recursive equation described in reference.

**Value**

returns a vector of expected rewards for different initial states

**Author(s)**

Vandit Jain

**References**

Stochastic Processes: Theory for Applications, Robert G. Gallager, Cambridge University Press

**Examples**

```
transMatr<-matrix(c(0.99,0.01,0.01,0.99),nrow=2,byrow=TRUE)  
simpleMc<-new("markovchain", states=c("a","b"),  
            transitionMatrix=transMatr)  
expectedRewards(simpleMc,1,c(0,1))
```

---

expectedRewardsBeforeHittingA

*Expected first passage Rewards for a set of states in a markovchain*

---

### Description

Given a markovchain object and reward values for every state, function calculates expected reward value for a set A of states after n steps.

### Usage

expectedRewardsBeforeHittingA(markovchain, A, state, rewards, n)

### Arguments

markovchain	the markovchain-class object
A	set of states for first passage expected reward
state	initial state
rewards	vector depicting rewards coressponding to states
n	no of steps of the process

### Details

The function returns the value of expected first passage rewards given rewards coressponding to every state, an initial state and number of steps.

### Value

returns a expected reward (numerical value) as described above

### Author(s)

Sai Bhargav Yalamanchi, Vandit Jain

---

ExpectedTime

*Returns expected hitting time from state i to state j*

---

### Description

Returns expected hitting time from state i to state j

### Usage

ExpectedTime(C, i, j, useRCpp)

**Arguments**

C	A CTMC S4 object
i	Initial state i
j	Final state j
useRCpp	logical whether to use Rcpp

**Details**

According to the theorem, holding times for all states except j should be greater than 0.

**Value**

A numerical value that returns expected hitting times from i to j

**Author(s)**

Vandit Jain

**References**

Markovchains, J. R. Norris, Cambridge University Press

**Examples**

```
states <- c("a","b","c","d")
byRow <- TRUE
gen <- matrix(data = c(-1, 1/2, 1/2, 0, 1/4, -1/2, 0, 1/4, 1/6, 0, -1/3, 1/6, 0, 0, 0, 0),
  nrow = 4,byrow = byRow, dimnames = list(states,states))
ctmc <- new("ctmc",states = states, byrow = byRow, generator = gen, name = "testctmc")
ExpectedTime(ctmc,1,4,TRUE)
```

---

firstPassage

*First passage across states*

---

**Description**

This function compute the first passage probability in states

**Usage**

```
firstPassage(object, state, n)
```

**Arguments**

object	A markovchain object
state	Initial state
n	Number of rows on which compute the distribution



**Details**

Based on Feres' Matlab listings

**Value**

A matrix of size 1:n x number of states showing the probability of the first time of passage in states to be exactly the number in the row.

**Author(s)**

Giorgio Spedicato

**References**

Renaldo Feres, Notes for Math 450 Matlab listings for Markov chains

**See Also**

[conditionalDistribution](#)

**Examples**

```
simpleMc <- new("markovchain", states = c("a", "b"),
              transitionMatrix = matrix(c(0.4, 0.6, .3, .7),
                                       nrow = 2, byrow = TRUE))
firstPassage(simpleMc, "b", 20)
```

---

firstPassageMultiple *function to calculate first passage probabilities*

---

**Description**

The function calculates first passage probability for a subset of states given an initial state.

**Usage**

```
firstPassageMultiple(object, state, set, n)
```

**Arguments**

object	a markovchain-class object
state	intital state of the process (charactervector)
set	set of states A, first passage of which is to be calculated
n	Number of rows on which compute the distribution

**Value**

A vector of size n showing the first time probabilities

**Author(s)**

Vandit Jain

**References**

Renaldo Feres, Notes for Math 450 Matlab listings for Markov chains; MIT OCW, course - 6.262, Discrete Stochastic Processes, course-notes, chap -05

**See Also**

[firstPassage](#)

**Examples**

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
matrix(c(0.2, 0.5, 0.3,
        0, 1, 0,
        0.1, 0.8, 0.1), nrow = 3, byrow = TRUE,
        dimnames = list(statesNames, statesNames)
))
firstPassageMultiple(markovB, "a", c("b", "c"), 4)
```

---

fitHigherOrder

*Functions to fit a higher order Markov chain*

---

**Description**

Given a sequence of states arising from a stationary state, it fits the underlying Markov chain distribution with higher order.

**Usage**

```
fitHigherOrder(sequence, order = 2)
seq2freqProb(sequence)
seq2matHigh(sequence, order)
```

**Arguments**

sequence	A character list.
order	Markov chain order

**Value**

A list containing lambda, Q, and X.

**Note**

This function is written in Rcpp.

**Author(s)**

Giorgio Spedicato, Tae Seung Kang

**References**

Ching, W. K., Huang, X., Ng, M. K., & Siu, T. K. (2013). Higher-order markov chains. In Markov Chains (pp. 141-176). Springer US.

Ching, W. K., Ng, M. K., & Fung, E. S. (2008). Higher-order multivariate Markov chains and their applications. Linear Algebra and its Applications, 428(2), 492-507.

package version 0.2.5

**See Also**

[markovchain](#)

**Examples**

```
sequence<-c("a", "a", "b", "b", "a", "c", "b", "a", "b", "c", "a", "b", "c", "a",
            , "b", "c", "a", "b", "a", "b")
fitHigherOrder(sequence)
```

---

```
fitHigherMultivarMC
```

*Function to fit Higher Order Multivariate Markov chain*

---

**Description**

Given a matrix of categorical sequences it fits Higher Order Multivariate Markov chain.

**Usage**

```
fitHigherMultivarMC(seqMat, order = 2, Norm = 2)
```

**Arguments**

seqMat	a matrix or a data frame where each column is a categorical sequence
order	Multivariate Markov chain order. Default is 2.
Norm	Norm to be used. Default is 2.

**Value**

an hommc object

**Author(s)**

Giorgio Spedicato, Deepak Yadav

**References**

W.-K. Ching et al. / Linear Algebra and its Applications

**Examples**

```
data <- matrix(c('2', '1', '3', '3', '4', '3', '2', '1', '3', '3', '2', '1',
                c('2', '4', '4', '4', '4', '2', '3', '3', '1', '4', '3', '3')),
              ncol = 2, byrow = FALSE)

fitHighOrderMultivarMC(data, order = 2, Norm = 2)
```

---

freq2Generator

*Returns a generator matrix corresponding to frequency matrix*

---

**Description**

The function provides interface to calculate generator matrix corresponding to a frequency matrix and time taken

**Usage**

```
freq2Generator(P, t = 1, method = "QO", logmethod = "Eigen")
```

**Arguments**

P	relative frequency matrix
t	(default value = 1)
method	one among "QO"(Quasi optimisation), "WA"(weighted adjustment), "DA"(diagonal adjustment)
logmethod	method for computation of matrix algorithm (by default : Eigen)

**Value**

returns a generator matrix with same dimnames

**References**

E. Kreinin and M. Sidelnikova: Regularization Algorithms for Transition Matrices. Algo Research Quarterly 4(1):23-40, 2001

**Examples**

```
sample <- matrix(c(150,2,1,1,1,200,2,1,2,1,175,1,1,1,1,150),nrow = 4,byrow = TRUE)
sample_rel = rbind((sample/rowSums(sample))[1:dim(sample)[1]-1,],c(rep(0,dim(sample)[1]-1),1))
freq2Generator(sample_rel,1)

data(tm_abs)
tm_rel=rbind((tm_abs/rowSums(tm_abs))[1:7,],c(rep(0,7),1))
## Derive quasi optimization generator matrix estimate
freq2Generator(tm_rel,1)
```

---

generatorToTransitionMatrix

*Function to obtain the transition matrix from the generator.*

---

**Description**

The transition matrix of the embedded DTMC is inferred from the CTMC's generator.

**Usage**

```
generatorToTransitionMatrix(gen, byrow = TRUE)
```

**Arguments**

gen	The generator matrix.
byrow	Flag to determine if rows (columns) sum to 0.

**Value**

Returns the transition matrix.

**Author(s)**

Sai Bhargav Yalamanchi

**References**

Introduction to Stochastic Processes with Applications in the Biosciences (2013), David F. Anderson, University of Wisconsin at Madison

**See Also**

[rctmc,ctmc-class](#)

**Examples**

```
energyStates <- c("sigma", "sigma_star")
byRow <- TRUE
gen <- matrix(data = c(-3, 3,
                      1, -1), nrow = 2,
              byrow = byRow, dimnames = list(energyStates, energyStates))
generatorToTransitionMatrix(gen)
```

---

```
HigherOrderMarkovChain-class
      Class "HigherOrderMarkovChain"
```

---

**Description**

The S4 class that describes HigherOrderMarkovChain objects.

---

```
holson          Holson data set
```

---

**Description**

A data set containing 1000 life histories trajectories and a categorical status (1,2,3) observed on eleven evenly spaced steps.

**Usage**

```
data(holson)
```

**Format**

A data frame with 1000 observations on the following 12 variables.

```
id unique id
time1 observed status at i-th time
time2 observed status at i-th time
time3 observed status at i-th time
time4 observed status at i-th time
time5 observed status at i-th time
time6 observed status at i-th time
time7 observed status at i-th time
time8 observed status at i-th time
time9 observed status at i-th time
time10 observed status at i-th time
time11 observed status at i-th time
```

**Details**

The example can be used to fit a markovchain or a markovchainList object.

**Source**

Private communications

**References**

Private communications

**Examples**

```
data(holson)
head(holson)
```

---

hommc-class	<i>An S4 class for representing High Order Multivariate Markovchain (HOMMC)</i>
-------------	---

---

**Description**

An S4 class for representing High Order Multivariate Markovchain (HOMMC)

**Slots**

order an integer equal to order of Multivariate Markovchain  
 states a vector of states present in the HOMMC model  
 P array of transition matrices  
 Lambda a vector which stores the weightage of each transition matrices in P  
 byrow if FALSE each column sum of transition matrix is 1 else row sum = 1  
 name a name given to hommc

**Author(s)**

Giorgio Spedicato, Deepak Yadav

**Examples**

```
statesName <- c("a", "b")

P <- array(0, dim = c(2, 2, 4), dimnames = list(statesName, statesName))
P[,1] <- matrix(c(0, 1, 1/3, 2/3), byrow = FALSE, nrow = 2)
P[,2] <- matrix(c(1/4, 3/4, 0, 1), byrow = FALSE, nrow = 2)
P[,3] <- matrix(c(1, 0, 1/3, 2/3), byrow = FALSE, nrow = 2)
P[,4] <- matrix(c(3/4, 1/4, 0, 1), byrow = FALSE, nrow = 2)
```

```
Lambda <- c(0.8, 0.2, 0.3, 0.7)

ob <- new("hommc", order = 1, states = statesName, P = P,
         Lambda = Lambda, byrow = FALSE, name = "FOMMC")
```

---

ictmc-class	<i>An S4 class for representing Imprecise Continuous Time Markovchains</i>
-------------	--

---

### Description

An S4 class for representing Imprecise Continuous Time Markovchains

### Slots

states a vector of states present in the ICTMC model  
 Q matrix representing the generator demonstrated in the form of variables  
 range a matrix that stores values of range of variables  
 name name given to ICTMC

---

impreciseProbabilityatT	<i>Calculating full conditional probability using lower rate transition matrix</i>
-------------------------	--

---

### Description

This function calculates full conditional probability at given time s using lower rate transition matrix

### Usage

```
impreciseProbabilityatT(C,i,t,s,error,useRCpp)
```

### Arguments

C	a ictmc class object
i	initial state at time t
t	initial time t. Default value = 0
s	final time
error	error rate. Default value = 0.001
useRCpp	logical whether to use RCpp implementation; by default TRUE



**Author(s)**

Vandit Jain

**References**

Imprecise Continuous-Time Markov Chains, Thomas Krak et al., 2016

**Examples**

```

states <- c("n","y")
Q <- matrix(c(-1,1,1,-1),nrow = 2,byrow = TRUE,dimnames = list(states,states))
range <- matrix(c(1/52,3/52,1/2,2),nrow = 2,byrow = 2)
name <- "testictmc"
ictmc <- new("ictmc",states = states,Q = Q,range = range,name = name)
impreciseProbabilityatT(ictmc,2,0,1,10^-3,TRUE)

```

---

inferHyperparam	<i>Function to infer the hyperparameters for Bayesian inference from an a priori matrix or a data set</i>
-----------------	---

---

**Description**

Since the Bayesian inference approach implemented in the package is based on conjugate priors, hyperparameters must be provided to model the prior probability distribution of the chain parameters. The hyperparameters are inferred from a given a priori matrix under the assumption that the matrix provided corresponds to the mean (expected) values of the chain parameters. A scaling factor vector must be provided too. Alternatively, the hyperparameters can be inferred from a data set.

**Usage**

```
inferHyperparam(transMatr = matrix(), scale = numeric(),
  data = character())
```

**Arguments**

transMatr	A valid transition matrix, with dimension names.
scale	A vector of scaling factors, each element corresponds to the row names of the provided transition matrix transMatr, in the same order.
data	A data set from which the hyperparameters are inferred.

**Details**

transMatr and scale need not be provided if data is provided.

**Value**

Returns the hyperparameter matrix in a list.

**Note**

The hyperparameter matrix returned is such that the row and column names are sorted alphanumerically, and the elements in the matrix are correspondingly permuted.

**Author(s)**

Sai Bhargav Yalamanchi, Giorgio Spedicato

**References**

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

**See Also**

[markovchainFit](#), [predictiveDistribution](#)

**Examples**

```
data(rain, package = "markovchain")
inferHyperparam(data = rain$rain)

weatherStates <- c("sunny", "cloudy", "rain")
weatherMatrix <- matrix(data = c(0.7, 0.2, 0.1,
                                0.3, 0.4, 0.3,
                                0.2, 0.4, 0.4),
                        byrow = TRUE, nrow = 3,
                        dimnames = list(weatherStates, weatherStates))
inferHyperparam(transMatr = weatherMatrix, scale = c(10, 10, 10))
```

---

is.accessible

*Verify if a state j is reachable from state i.*

---

**Description**

This function verifies if a state is reachable from another, i.e., if there exists a path that leads to state j leaving from state i with positive probability

**Usage**

```
is.accessible(object, from, to)
```

**Arguments**

object	A markovchain object.
from	The name of state "i" (beginning state).
to	The name of state "j" (ending state).

**Details**

It wraps an internal function named `.commStatesFinder`.

**Value**

A boolean value.

**Author(s)**

Giorgio Spedicato

**References**

James Montgomery, University of Madison

**See Also**

`is.irreducible`

**Examples**

```

statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames,
              transitionMatrix = matrix(c(0.2, 0.5, 0.3,
                                         0, 1, 0,
                                         0.1, 0.8, 0.1), nrow = 3, byrow = TRUE,
                                         dimnames = list(statesNames, statesNames)
              )
is.accessible(markovB, "a", "c")

```

---

`is.CTMCirreducible`      *Check if CTMC is irreducible*

---

**Description**

This function verifies whether a CTMC object is irreducible

**Usage**

```
is.CTMCirreducible(ctmc)
```

**Arguments**

ctmc                    a ctmc-class object

**Value**

a boolean value as described above.

**Author(s)**

Vandit Jain

**References**

Continuous-Time Markov Chains, Karl Sigman, Columbia University

**Examples**

```
energyStates <- c("sigma", "sigma_star")
byRow <- TRUE
gen <- matrix(data = c(-3, 3,
                      1, -1), nrow = 2,
              byrow = byRow, dimnames = list(energyStates, energyStates))
molecularCTMC <- new("ctmc", states = energyStates,
                    byrow = byRow, generator = gen,
                    name = "Molecular Transition Model")
is.CTMCirreducible(molecularCTMC)
```

---

is.irreducible                    *Function to check if a Markov chain is irreducible*

---

**Description**

This function verifies whether a markovchain object transition matrix is composed by only one communicating class.

**Usage**

```
is.irreducible(object)
```

**Arguments**

object                    A markovchain object

**Details**

It is based on .communicatingClasses internal function.

**Value**

A boolean values.

**Author(s)**

Giorgio Spedicato

**References**

Feres, Matlab listings for Markov Chains.

**See Also**

[summary](#)

**Examples**

```
statesNames <- c("a", "b")
mcA <- new("markovchain", transitionMatrix = matrix(c(0.7,0.3,0.1,0.9),
                                                    byrow = TRUE, nrow = 2,
                                                    dimnames = list(statesNames, statesNames)
                                                    ))
is.irreducible(mcA)
```

---

*is.TimeReversible*      *checks if ctmc object is time reversible*

---

**Description**

The function returns checks if provided function is time reversible

**Usage**

```
is.TimeReversible(ctmc)
```

**Arguments**

ctmc                    a ctmc-class object

**Value**

Returns a boolean value stating whether ctmc object is time reversible  
a boolean value as described above

**Author(s)**

Vandit Jain

**References**

INTRODUCTION TO STOCHASTIC PROCESSES WITH R, ROBERT P. DOBROW, Wiley

**Examples**

```
energyStates <- c("sigma", "sigma_star")
byRow <- TRUE
gen <- matrix(data = c(-3, 3,
                      1, -1), nrow = 2,
              byrow = byRow, dimnames = list(energyStates, energyStates))
molecularCTMC <- new("ctmc", states = energyStates,
                    byrow = byRow, generator = gen,
                    name = "Molecular Transition Model")
is.TimeReversible(molecularCTMC)
```

---

kullback

*Example from Kullback and Kupperman Tests for Contingency Tables*

---

**Description**

A list of two matrices representing raw transitions between two states

**Usage**

```
data(kullback)
```

**Format**

A list containing two 6x6 non - negative integer matrices

---

markovchain-class

*Class "markovchain"*

---

**Description**

The S4 class that describes markovchain objects.

**Objects from the Class**

Objects can be created by calls of the form `new("markovchain", states, byrow, transitionMatrix, ...)`.

**Slots**

**states:** Name of the states. Must be the same of colnames and rownames of the transition matrix  
**byrow:** Binary flag.  
**transitionMatrix:** Square transition matrix  
**name:** Optional character name of the Markov chain

**Methods**

\* `signature(e1 = "markovchain", e2 = "markovchain")`: multiply two markovchain objects  
 \* `signature(e1 = "markovchain", e2 = "matrix")`: markovchain by matrix multiplication  
 \* `signature(e1 = "markovchain", e2 = "numeric")`: markovchain by numeric vector multiplication  
 \* `signature(e1 = "matrix", e2 = "markovchain")`: matrix by markov chain  
 \* `signature(e1 = "numeric", e2 = "markovchain")`: numeric vector by markovchain multiplication  
 [ `signature(x = "markovchain", i = "ANY", j = "ANY", drop = "ANY")`: ...  
 ^ `signature(e1 = "markovchain", e2 = "numeric")`: power of a markovchain object  
 == `signature(e1 = "markovchain", e2 = "markovchain")`: equality of two markovchain object  
 != `signature(e1 = "markovchain", e2 = "markovchain")`: non-equality of two markovchain object  
**absorbingStates** `signature(object = "markovchain")`: method to get absorbing states  
**canonicForm** `signature(object = "markovchain")`: return a markovchain object into canonic form  
**coerce** `signature(from = "markovchain", to = "data.frame")`: coerce method from markovchain to data.frame  
**conditionalDistribution** `signature(object = "markovchain")`: returns the conditional probability of subsequent states given a state  
**coerce** `signature(from = "data.frame", to = "markovchain")`: coerce method from data.frame to markovchain  
**coerce** `signature(from = "table", to = "markovchain")`: coerce method from table to markovchain  
**coerce** `signature(from = "msm", to = "markovchain")`: coerce method from msm to markovchain  
**coerce** `signature(from = "msm.est", to = "markovchain")`: coerce method from msm.est (but only from a Probability Matrix) to markovchain  
**coerce** `signature(from = "etm", to = "markovchain")`: coerce method from etm to markovchain  
**coerce** `signature(from = "sparseMatrix", to = "markovchain")`: coerce method from sparseMatrix to markovchain  
**coerce** `signature(from = "markovchain", to = "igraph")`: coercing to igraph objects  
**coerce** `signature(from = "markovchain", to = "matrix")`: coercing to matrix objects

**coerce** signature(from = "markovchain", to = "sparseMatrix"): coercing to sparseMatrix objects

**coerce** signature(from = "matrix", to = "markovchain"): coercing to markovchain objects from matrix one

**dim** signature(x = "markovchain"): method to get the size

**names** signature(x = "markovchain"): method to get the names of states

**names<-** signature(x = "markovchain", value = "character"): method to set the names of states

**initialize** signature(.Object = "markovchain"): initialize method

**plot** signature(x = "markovchain", y = "missing"): plot method for markovchain objects

**predict** signature(object = "markovchain"): predict method

**print** signature(x = "markovchain"): print method.

**show** signature(object = "markovchain"): show method.

**sort** signature(x = "markovchain", decreasing=FALSE): sorting the transition matrix.

**states** signature(object = "markovchain"): returns the names of states (as names).

**steadyStates** signature(object = "markovchain"): method to get the steady vector.

**summary** signature(object = "markovchain"): method to summarize structure of the markov chain

**transientStates** signature(object = "markovchain"): method to get the transient states.

**t** signature(x = "markovchain"): transpose matrix

**transitionProbability** signature(object = "markovchain"): transition probability

### Warning

Validation method is used to assess whether either columns or rows totals to one. Rounding is used up to 5th decimal. If state names are not properly defined for a probability matrix, coercing to markovchain object leads to overriding states name with artificial "s1", "s2", ... sequence. In addition, operator overloading has been applied for +, \*, '==', != operators.

### Note

markovchain object are written in S4 Classes.

### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

[markovchainSequence](#), [markovchainFit](#)



**Examples**

```

#show markovchain definition
showClass("markovchain")
#create a simple Markov chain
transMatr<-matrix(c(0.4,0.6,.3,.7),nrow=2,byrow=TRUE)
simpleMc<-new("markovchain", states=c("a","b"),
transitionMatrix=transMatr,
name="simpleMc")
#power
simpleMc^4
#some methods
steadyStates(simpleMc)
absorbingStates(simpleMc)
simpleMc[2,1]
t(simpleMc)
is.irreducible(simpleMc)
#conditional distributions
conditionalDistribution(simpleMc, "b")
#example for predict method
sequence<-c("a", "b", "a", "a", "a", "a", "b", "a", "b", "a", "b", "a", "a", "b", "b", "b", "a")
mcFit<-markovchainFit(data=sequence)
predict(mcFit$estimate, newdata="b",n.ahead=3)
#direct conversion
myMc<-as(transMatr, "markovchain")

#example of summary
summary(simpleMc)
## Not run: plot(simpleMc)

```

---

```
markovchainList-class Class "markovchainList"
```

---

**Description**

A class to handle non - homogeneous Markov chains

**Objects from the Class**

A markovchainlist is a list of markovchain objects. They can be used to model non - homogeneous discrete time Markov Chains, when transition probabilities (and possible states) change by time.

**Slots**

markovchains: Object of class "list": a list of markovchains

name: Object of class "character": optional name of the class

**Methods**

**[[** signature(x = "markovchainList"): extract the i-th markovchain  
**dim** signature(x = "markovchainList"): number of markovchain underlying the matrix  
**predict** signature(object = "markovchainList"): predict from a markovchainList  
**print** signature(x = "markovchainList"): prints the list of markovchains  
**show** signature(object = "markovchainList"): same as print

**Note**

The class consists in a list of markovchain objects. It can help to deal with non - homogeneous Markov chains.

**Author(s)**

Giorgio Spedicato

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

**See Also**

[markovchain](#)

**Examples**

```
showClass("markovchainList")
#define a markovchainList
statesNames=c("a","b")

mcA<-new("markovchain",name="MCA", transitionMatrix=matrix(c(0.7,0.3,0.1,0.9),
byrow=TRUE, nrow=2, dimnames=list(statesNames,statesNames)))

mcB<-new("markovchain", states=c("a","b","c"), name="MCB",
transitionMatrix=matrix(c(0.2,0.5,0.3,0,1,0,0.1,0.8,0.1),
nrow=3, byrow=TRUE))

mcC<-new("markovchain", states=c("a","b","c","d"), name="MCC",
transitionMatrix=matrix(c(0.25,0.75,0,0,0.4,0.6,
0,0,0,0,0.1,0.9,0,0,0.7,0.3), nrow=4, byrow=TRUE)
)
mcList<-new("markovchainList",markovchains=list(mcA, mcB, mcC),
name="Non - homogeneous Markov Chain")
```

---

markovchainListFit     *markovchainListFit*

---

## Description

Given a data frame or a matrix (rows are observations, by cols the temporal sequence), it fits a non-homogeneous discrete time markov chain process (storing row). In particular a markovchainList of size = ncol - 1 is obtained estimating transitions from the n samples given by consecutive column pairs.

## Usage

```
markovchainListFit(data, byrow = TRUE, laplacian = 0, name)
```

## Arguments

data	Either a matrix or a data.frame or a list object.
byrow	Indicates whether distinct stochastic processes trajectories are shown in distinct rows.
laplacian	Laplacian correction (default 0).
name	Optional name.

## Details

If data contains NAs then the transitions containing NA will be ignored.

## Value

A list containing two slots: estimate (the estimate) name

## Examples

```
# using holson dataset
data(holson)
# fitting a single markovchain
singleMc <- markovchainFit(data = holson[,2:12])
# fitting a markovchainList
mclistFit <- markovchainListFit(data = holson[, 2:12], name = "holsonMcList")
```

markovchainSequence     *Function to generate a sequence of states from homogeneous Markov chains.*

---

### Description

Provided any markovchain object, it returns a sequence of states coming from the underlying stationary distribution.

### Usage

```
markovchainSequence(n, markovchain, t0 = sample(markovchain@states, 1),  
  include.t0 = FALSE, useRCpp = TRUE)
```

### Arguments

n	Sample size
markovchain	markovchain object
t0	The initial state
include.t0	Specify if the initial state shall be used
useRCpp	Boolean. Should RCpp fast implementation being used? Default is yes.

### Details

A sequence of size n is sampled.

### Value

A Character Vector

### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

[markovchainFit](#)

**Examples**

```
# define the markovchain object
statesNames <- c("a", "b", "c")
mcB <- new("markovchain", states = statesNames,
  transitionMatrix = matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1),
  nrow = 3, byrow = TRUE, dimnames = list(statesNames, statesNames)))

# show the sequence
outs <- markovchainSequence(n = 100, markovchain = mcB, t0 = "a")
```

---

meanFirstPassageTime    *Mean First Passage Time for markovchain*

---

**Description**

Given a markovchain object, this function calculates the expected steps to go from state  $i$  to  $j$

**Usage**

```
meanFirstPassageTime(markovchain, destination_set)
```

**Arguments**

markovchain    the markovchain-class object  
destination\_set  
                  the set of destination states or NULL (all states)

**Details**

if destination\_set is one or more states, the mean first passage time from each remaining state to the given set is computed. If NULL, the full MFPT matrix is computed (with a different algorithm).

**Value**

a vector (if destination\_set given) or a matrix (otherwise) of mean passage times

**Author(s)**

Toni Giorgino

**References**

C. M. Grinstead and J. L. Snell. Introduction to Probability. American Mathematical Soc., 2012.

**Examples**

```

Pmat <- matrix( c(6,3,1, 2,3,5, 4,1,5)/10, ncol=3, byrow=TRUE)
P <- new("markovchain", states=c("s","c","r"), transitionMatrix=Pmat)
meanFirstPassageTime(P,"r")
meanFirstPassageTime(P)

# Grinstead and Snell's "Oz weather" worked out example
Poz <- new("markovchain", states=c("s","c","r"),
           transitionMatrix=matrix(c(2,1,1, 2,0,2, 1,1,2)/4, byrow=TRUE, ncol=3))
meanFirstPassageTime(Poz)

```

---

multinomialConfidenceIntervals

*A function to compute multinomial confidence intervals of DTMC*

---

**Description**

Return estimated transition matrix assuming a Multinomial Distribution

**Usage**

```

multinomialConfidenceIntervals(transitionMatrix, countsTransitionMatrix,
                                confidencelevel = 0.95)

```

**Arguments**

```

transitionMatrix
    An estimated transition matrix.
countsTransitionMatrix
    Empirical (conts) transition matrix, on which the transitionMatrix was performed.
confidencelevel
    confidence interval level.

```

**Value**

Two matrices containing the confidence intervals.

**References**

Constructing two-sided simultaneous confidence intervals for multinomial proportions for small counts in a large number of cells. *Journal of Statistical Software* 5(6) (2000)

**See Also**

markovchainFit  
[markovchain](#)

**Examples**

```
seq<-c("a", "b", "a", "a", "a", "a", "b", "a", "b", "a", "b", "a", "a", "b", "b", "b", "a")
mcf<-markovchainFit(data=seq,byrow=TRUE)
seqmat<-createSequenceMatrix(seq)
multinomialConfidenceIntervals(mcf$estimate@transitionMatrix, seqmat, 0.95)
```

---

name	<i>Method to retrieve name of markovchain object</i>
------	--

---

**Description**

This method returns the name of markovchain object

**Usage**

```
name(object)

## S4 method for signature 'markovchain'
name(object)
```

**Arguments**

object            A markovchain object

**Author(s)**

Giorgio Spedicato, Deepak Yadav

**Examples**

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames=list(statesNames,statesNames)),
  name = "A markovchain Object"
)
name(markovB)
```

---

name<- *Method to set name of markovchain object*

---

### Description

This method modify the existing name of markovchain object

### Usage

```
name(object) <- value

## S4 replacement method for signature 'markovchain'
name(object) <- value
```

### Arguments

object            A markovchain object  
value             New name of markovchain object

### Author(s)

Giorgio Spedicato, Deepak Yadav

### Examples

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames=list(statesNames,statesNames)),
  name = "A markovchain Object"
)
name(markovB) <- "dangerous mc"
```

---

noofVisitsDist            *return a joint pdf of the number of visits to the various states of the DTMC*

---

### Description

This function would return a joint pdf of the number of visits to the various states of the DTMC during the first N steps.

### Usage

```
noofVisitsDist(markovchain,N,state)
```



**Arguments**

markovchain	a markovchain-class object
N	no of steps
state	the initial state

**Details**

This function would return a joint pdf of the number of visits to the various states of the DTMC during the first N steps.

**Value**

a numeric vector depicting the above described probability density function.

**Author(s)**

Vandit Jain

**Examples**

```
transMatr<-matrix(c(0.4,0.6,.3,.7),nrow=2,byrow=TRUE)
simpleMc<-new("markovchain", states=c("a","b"),
             transitionMatrix=transMatr,
             name="simpleMc")
noofVisitsDist(simpleMc,5,"a")
```

---

predictHommc

*Simulate a higher order multivariate markovchain*

---

**Description**

This function provides a prediction of states for a higher order multivariate markovchain object

**Usage**

```
predictHommc(hommc,t,init)
```

**Arguments**

hommc	a hommc-class object
t	no of iterations to predict
init	matrix of previous states size of which depends on hommc

**Details**

The user is required to provide a matrix of giving  $n$  previous corresponding every categorical sequence. Dimensions of the init are  $s \times n$ , where  $s$  is number of categorical sequences and  $n$  is order of the homc.

**Value**

The function returns a matrix of size  $s \times t$  displaying  $t$  predicted states in each row corresponding to every categorical sequence.

**Author(s)**

Vandit Jain

---

predictiveDistribution

*Function to compute the probability of observing a new data set, given a data set*

---

**Description**

The function computes the probability of observing a new data set using information from a given data set. Additionally, hyperparameters can be provided.

**Usage**

```
predictiveDistribution(stringchar, newData, hyperparam = matrix())
```

**Arguments**

stringchar	This is the data using which the Bayesian inference is performed.
newData	This is the data whose predictive probability is computed.
hyperparam	This determines the shape of the prior distribution of the parameters. If none is provided, default value of 1 is assigned to each parameter. This must be of size $k \times k$ where $k$ is the number of states in the chain and the values should typically be non-negative integers.

**Details**

The underlying method is Bayesian inference. The probability is computed by averaging the likelihood of the new data with respect to the posterior. Since the method assumes conjugate priors, the result can be represented in a closed form (see the vignette for more details), which is what is returned.

**Value**

The log of the probability is returned.

**Author(s)**

Sai Bhargav Yalamanchi

**References**

Inferring Markov Chains: Bayesian Estimation, Model Comparison, Entropy Rate, and Out-of-Class Modeling, Christopher C. Strelhoff, James P. Crutchfield, Alfred Hübner, Santa Fe Institute

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

**See Also**

[markovchainFit](#)

**Examples**

```
sequence<-c("a", "b", "a", "a", "a", "a", "b", "a", "b", "a", "b", "a", "a",  
"b", "b", "b", "a")  
hyperMatrix<-matrix(c(1, 2, 1, 4), nrow = 2,dimnames=list(c("a","b"),c("a","b")))  
predProb <- predictiveDistribution(sequence[1:10], sequence[11:17], hyperparam =hyperMatrix )  
hyperMatrix2<-hyperMatrix[c(2,1),c(2,1)]  
predProb2 <- predictiveDistribution(sequence[1:10], sequence[11:17], hyperparam =hyperMatrix2 )  
predProb2==predProb
```

---

preproglucacon

*Preprogluccacon DNA protein bases sequences*

---

**Description**

Sequence of bases for preproglucacon DNA protein

**Usage**

```
data(preproglucacon)
```

**Format**

A data frame with 1572 observations on the following 2 variables.

V1 a numeric vector, showing original coding

preproglucacon a character vector, showing initial of DNA bases (Adenine, Cytosine, Guanine, Thymine)

**Source**

Avery Henderson

## References

Averuy Henderson, Fitting markov chain models on discrete time series such as DNA sequences

## Examples

```
data(preproglucacon)
preproglucaconMc<-markovchainFit(data=preproglucacon$preproglucacon)
```

---

priorDistribution      *Prior Distribution*

---

## Description

Function to evaluate the prior probability of a transition matrix. It is based on conjugate priors and therefore a Dirichlet distribution is used to model the transitions of each state.

## Usage

```
priorDistribution(transMatr, hyperparam = matrix())
```

## Arguments

transMatr	The transition matrix whose probability is the parameter of interest.
hyperparam	The hyperparam matrix (optional). If not provided, a default value of 1 is assumed for each and therefore the resulting probability distribution is uniform.

## Details

The states (dimnames) of the transition matrix and the hyperparam may be in any order.

## Value

The log of the probabilities for each state is returned in a numeric vector. Each number in the vector represents the probability (log) of having a probability transition vector as specified in corresponding the row of the transition matrix.

## Note

This function can be used in conjunction with inferHyperparam. For example, if the user has a prior data set and a prior transition matrix, he can infer the hyperparameters using inferHyperparam and then compute the probability of their prior matrix using the inferred hyperparameters with priorDistribution.

## Author(s)

Sai Bhargav Yalamanchi, Giorgio Spedicato

## References

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

## See Also

[predictiveDistribution](#), [inferHyperparam](#)

## Examples

```
priorDistribution(matrix(c(0.5, 0.5, 0.5, 0.5),
                        nrow = 2,
                        dimnames = list(c("a", "b"), c("a", "b"))),
matrix(c(2, 2, 2, 2),
      nrow = 2,
      dimnames = list(c("a", "b"), c("a", "b"))))
```

---

probabilityatT

*Calculating probability from a ctmc object*

---

## Description

This function returns the probability of every state at time  $t$  under different conditions

## Usage

```
probabilityatT(C, t, x0, useRCpp)
```

## Arguments

C	A CTMC S4 object
t	final time $t$
x0	initial state
useRCpp	logical whether to use RCpp implementation

## Details

The initial state is not mandatory, In case it is not provided, function returns a matrix of transition function at time  $t$  else it returns vector of probabilities of transition to different states if initial state was  $x_0$

## Value

returns a vector or a matrix in case  $x_0$  is provided or not respectively.

## Author(s)

Vandit Jain

**References**

INTRODUCTION TO STOCHASTIC PROCESSES WITH R, ROBERT P. DOBROW, Wiley

**Examples**

```
states <- c("a", "b", "c", "d")
byRow <- TRUE
gen <- matrix(data = c(-1, 1/2, 1/2, 0, 1/4, -1/2, 0, 1/4, 1/6, 0, -1/3, 1/6, 0, 0, 0, 0),
  nrow = 4, byrow = byRow, dimnames = list(states, states))
ctmc <- new("ctmc", states = states, byrow = byRow, generator = gen, name = "testctmc")
probabilityatT(ctmc, 1, useRCpp = TRUE)
```

---

rain

*Alofi island daily rainfall*

---

**Description**

Rainfall measured in Alofi Island

**Usage**

```
data(rain)
```

**Format**

A data frame with 1096 observations on the following 2 variables.

V1 a numeric vector, showing original coding

rain a character vector, showing daily rainfall millilitres brackets

**Source**

Avery Henderson

**References**

Avery Henderson, Fitting markov chain models on discrete time series such as DNA sequences

**Examples**

```
data(rain)
rainMc<-markovchainFit(data=rain$rain)
```

---

rctmc *Function to generate a sequence of random CTMC transitions.*

---

### Description

The function generates random CTMC transitions as per the provided generator matrix.

### Usage

```
rctmc(n, ctmc, initDist = numeric(), T = 0, include.T0 = TRUE, out.type = "list")
```

### Arguments

n	The number of samples to generate.
ctmc	The CTMC S4 object.
initDist	The initial distribution of states.
T	The time up to which the simulation runs (all transitions after time T are not returned).
include.T0	Flag to determine if start state is to be included.
out.type	"list" or "df"

### Details

In order to use the T0 argument, set n to Inf.

### Value

Based on out.type, a list or a data frame is returned. The returned list has two elements - a character vector (states) and a numeric vector (indicating time of transitions). The data frame is similarly structured.

### Author(s)

Sai Bhargav Yalamanchi

### References

Introduction to Stochastic Processes with Applications in the Biosciences (2013), David F. Anderson, University of Wisconsin at Madison

### See Also

[generatorToTransitionMatrix,ctmc-class](#)

**Examples**

```

energyStates <- c("sigma", "sigma_star")
byRow <- TRUE
gen <- matrix(data = c(-3, 3,
                      1, -1), nrow = 2,
              byrow = byRow, dimnames = list(energyStates, energyStates))
molecularCTMC <- new("ctmc", states = energyStates,
                    byrow = byRow, generator = gen,
                    name = "Molecular Transition Model")

statesDist <- c(0.8, 0.2)
rctmc(n = Inf, ctmc = molecularCTMC, T = 1)
rctmc(n = 5, ctmc = molecularCTMC, initDist = statesDist, include.T0 = FALSE)

```

---

rmarkovchain	<i>Function to generate a sequence of states from homogeneous or non-homogeneous Markov chains.</i>
--------------	---

---

**Description**

Provided any markovchain or markovchainList objects, it returns a sequence of states coming from the underlying stationary distribution.

**Usage**

```
rmarkovchain(n, object, what = "data.frame", useRCpp = TRUE,
             parallel = FALSE, num.cores = NULL, ...)
```

**Arguments**

n	Sample size
object	Either a markovchain or a markovchainList object
what	It specifies whether either a data.frame or a matrix (each rows represent a simulation) or a list is returned.
useRCpp	Boolean. Should RCpp fast implementation being used? Default is yes.
parallel	Boolean. Should parallel implementation being used? Default is yes.
num.cores	Number of Cores to be used
...	additional parameters passed to the internal sampler

**Details**

When a homogeneous process is assumed (markovchain object) a sequence is sampled of size n. When a non - homogeneous process is assumed, n samples are taken but the process is assumed to last from the begin to the end of the non-homogeneous markov process.



**Value**

Character Vector, data.frame, list or matrix

**Note**

Check the type of input

**Author(s)**

Giorgio Spedicato

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

**See Also**

[markovchainFit](#), [markovchainSequence](#)

**Examples**

```
# define the markovchain object
statesNames <- c("a", "b", "c")
mcB <- new("markovchain", states = statesNames,
  transitionMatrix = matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1),
  nrow = 3, byrow = TRUE, dimnames = list(statesNames, statesNames))

# show the sequence
outs <- rmarkovchain(n = 100, object = mcB, what = "list")

#define markovchainList object
statesNames <- c("a", "b", "c")
mcA <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames = list(statesNames, statesNames)))
mcB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames = list(statesNames, statesNames)))
mcC <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames = list(statesNames, statesNames)))
mclist <- new("markovchainList", markovchains = list(mcA, mcB, mcC))

# show the list of sequence
rmarkovchain(100, mclist, "list")
```

---

sales	<i>Sales Demand Sequences</i>
-------	-------------------------------

---

**Description**

Sales demand sequences of five products (A, B, C, D, E). Each row corresponds to a sequence. First row corresponds to Sequence A, Second row to Sequence B and so on.

**Usage**

```
data("sales")
```

**Format**

An object of class `matrix` with 269 rows and 5 columns.

**Details**

The example can be used to fit High order multivariate markov chain.

**Examples**

```
data("sales")
# fitHighOrderMultivarMC(seqMat = sales, order = 2, Norm = 2)
```

---

show,hommc-method	<i>Function to display the details of hommc object</i>
-------------------	--

---

**Description**

This is a convenience function to display the slots of `hommc` object in proper format

**Usage**

```
## S4 method for signature 'hommc'
show(object)
```

**Arguments**

object	An object of class <code>hommc</code>
--------	---------------------------------------

---

states	<i>Defined states of a transition matrix</i>
--------	--

---

**Description**

This method returns the states of a transition matrix.

**Usage**

```
states(object)

## S4 method for signature 'markovchain'
states(object)
```

**Arguments**

object            A discrete markovchain object

**Value**

The character vector corresponding to states slot.

**Author(s)**

Giorgio Spedicato

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

**See Also**

[markovchain](#)

**Examples**

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames=list(statesNames,statesNames)),
  name = "A markovchain Object"
)
states(markovB)
```

---

steadyStates	<i>Stationary states of a markovchain object</i>
--------------	--

---

**Description**

This method returns the stationary vector in matricial form of a markovchain object.

**Usage**

```
steadyStates(object)
```

```
## S4 method for signature 'markovchain'  
steadyStates(object)
```

**Arguments**

object            A discrete markovchain object

**Value**

A matrix corresponding to the stationary states

**Note**

The steady states are identified starting from which eigenvectors correspond to identity eigenvalues and then normalizing them to sum up to unity. When negative values are found in the matrix, the eigenvalues extraction is performed on the recurrent classes submatrix.

**Author(s)**

Giorgio Spedicato

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

**See Also**

[markovchain](#)

**Examples**

```
statesNames <- c("a", "b", "c")  
markovB <- new("markovchain", states = statesNames, transitionMatrix =  
          matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,  
                byrow = TRUE, dimnames=list(statesNames,statesNames)),  
          name = "A markovchain Object")  
)  
steadyStates(markovB)
```

---

tm\_abs

*Single Year Corporate Credit Rating Transitions*


---

**Description**

Matrix of Standard and Poor's Global Corporate Rating Transition Frequencies 2000 (NR Removed)

**Usage**

```
data(tm_abs)
```

**Format**

The format is: num [1:8, 1:8] 17 2 0 0 0 0 0 1 455 ... - attr(\*, "dimnames")=List of 2 ..\$: chr [1:8] "AAA" "AA" "A" "BBB" ... ..\$: chr [1:8] "AAA" "AA" "A" "BBB" ...

**References**

European Securities and Markets Authority, 2016 <https://cerep.esma.europa.eu/cerep-web/statistics/transitionMatrice.xhtml>

**Examples**

```
data(tm_abs)
```

---

transition2Generator

*Return the generator matrix for a corresponding transition matrix*


---

**Description**

Calculate the generator matrix for a corresponding transition matrix

**Usage**

```
transition2Generator(P, t = 1, method = "logarithm")
```

**Arguments**

P transition matrix between time 0 and t  
t time of observation  
method "logarithm" returns the Matrix logarithm of the transition matrix

**Value**

A matrix that represent the generator of P

**See Also**[rctmc](#)**Examples**

```
mymatr <- matrix(c(.4, .6, .1, .9), nrow = 2, byrow = TRUE)
Q <- transition2Generator(P = mymatr)
expm::expm(Q)
```

---

transitionProbability *Function to get the transition probabilities from initial to subsequent states.*

---

**Description**

This is a convenience function to get transition probabilities.

**Usage**

```
transitionProbability(object, t0, t1)

## S4 method for signature 'markovchain'
transitionProbability(object, t0, t1)
```

**Arguments**

object	A markovchain object.
t0	Initial state.
t1	Subsequent state.

**Value**

Numeric Vector

**Author(s)**

Giorgio Spedicato

**References**

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

**See Also**[markovchain](#)

**Examples**

```

statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =
  matrix(c(0.2, 0.5, 0.3, 0, 1, 0, 0.1, 0.8, 0.1), nrow = 3,
  byrow = TRUE, dimnames=list(statesNames,statesNames)),
  name = "A markovchain Object"
)
transitionProbability(markovB,"b", "c")

```

---

verifyMarkovProperty    *Various functions to perform statistical inference of DTMC*

---

**Description**

These functions verify the Markov property, assess the order and stationarity of the Markov chain.

This function tests whether an empirical transition matrix is statistically compatible with a theoretical one. It is a chi-square based test

Verifies that the  $s$  elements in the input list belongs to the same DTMC

**Usage**

```

verifyMarkovProperty(sequence, verbose = TRUE)

assessOrder(sequence, verbose = TRUE)

assessStationarity(sequence, nblocks, verbose = TRUE)

verifyEmpiricalToTheoretical(data, object, verbose = TRUE)

verifyHomogeneity(inputList, verbose = TRUE)

```

**Arguments**

sequence	An empirical sequence.
verbose	Should test results be printed out?
nblocks	Number of blocks.
data	matrix, character or list to be converted in a raw transition matrix
object	a markovchain object
inputList	A list of items that can coerced to transition matrices

**Value**

Verification result

a list with following slots: statistic (the chi - square statistic), dof (degrees of freedom), and corresponding p-value

a list of transition matrices?

**Author(s)**

Tae Seung Kang, Giorgio Alfredo Spedicato

**References**

Anderson and Goodman.

**See Also**

markovchain

**Examples**

```
sequence <- c("a", "b", "a", "a", "a", "a", "b", "a", "b",
             "a", "b", "a", "a", "b", "b", "b", "a")
mcFit <- markovchainFit(data = sequence, byrow = FALSE)
verifyMarkovProperty(sequence)
assessOrder(sequence)
assessStationarity(sequence, 1)
```

#Example taken from Kullback Kupperman Tests for Contingency Tables and Markov Chains

```
sequence<-c(0,1,2,2,1,0,0,0,0,0,1,2,2,2,1,0,0,1,0,0,0,0,0,0,1,1,
2,0,0,2,1,1,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,1,1,1,0,0,0,0,2,1,0,
0,2,1,0,0,0,0,0,0,1,1,1,2,2,0,0,2,1,1,1,1,2,1,1,1,1,1,1,1,1,0,2,
0,1,1,0,0,0,1,2,2,0,0,0,0,0,0,2,2,2,1,1,1,1,0,1,1,1,1,0,0,2,1,1,
0,0,0,0,0,2,2,1,1,1,1,1,2,1,2,0,0,0,1,2,2,2,0,0,0,1,1)

mc=matrix(c(5/8,1/4,1/8,1/4,1/2,1/4,1/4,3/8,3/8),byrow=TRUE, nrow=3)
rownames(mc)<-colnames(mc)<-0:2; theoreticalMc<-as(mc, "markovchain")

verifyEmpiricalToTheoretical(data=sequence,object=theoreticalMc)

data(kullback)
verifyHomogeneity(inputList=kullback,verbose=TRUE)
```



# Index

- !=, markovchain, markovchain-method  
(markovchain-class), 30
- \*Topic **classes**
  - ctmc-class, 11
  - markovchain-class, 30
  - markovchainList-class, 33
- \*Topic **datasets**
  - blanden, 6
  - craigsendi, 9
  - holson, 22
  - kullback, 30
  - preproglucacon, 43
  - rain, 46
  - sales, 50
  - tm\_abs, 53
- \*Topic **package**
  - markovchain-package, 3
- \*, markovchain, markovchain-method  
(markovchain-class), 30
- \*, markovchain, matrix-method  
(markovchain-class), 30
- \*, markovchain, numeric-method  
(markovchain-class), 30
- \*, matrix, markovchain-method  
(markovchain-class), 30
- \*, numeric, markovchain-method  
(markovchain-class), 30
- ==, markovchain, markovchain-method  
(markovchain-class), 30
- [, markovchain, ANY, ANY, ANY-method  
(markovchain-class), 30
- [[, markovchainList-method  
(markovchainList-class), 33
- ^, markovchain, numeric-method  
(markovchain-class), 30
  
- absorbingStates, 4
- absorbingStates, markovchain-method  
(markovchain-class), 30
- assessOrder (verifyMarkovProperty), 55
  
- assessStationarity  
(verifyMarkovProperty), 55
  
- blanden, 6
  
- canonicForm (absorbingStates), 4
- canonicForm, markovchain-method  
(markovchain-class), 30
- coerce, data.frame, markovchain-method  
(markovchain-class), 30
- coerce, etm, markovchain-method  
(markovchain-class), 30
- coerce, markovchain, data.frame-method  
(markovchain-class), 30
- coerce, markovchain, igrph-method  
(markovchain-class), 30
- coerce, markovchain, matrix-method  
(markovchain-class), 30
- coerce, markovchain, sparseMatrix-method  
(markovchain-class), 30
- coerce, matrix, markovchain-method  
(markovchain-class), 30
- coerce, msm, markovchain-method  
(markovchain-class), 30
- coerce, msm.est, markovchain-method  
(markovchain-class), 30
- coerce, sparseMatrix, markovchain-method  
(markovchain-class), 30
- coerce, table, markovchain-method  
(markovchain-class), 30
- committorAB, 7
- communicatingClasses (absorbingStates),  
4
- conditionalDistribution, 8, 17
- conditionalDistribution, markovchain-method  
(markovchain-class), 30
- craigsendi, 9
- createSequenceMatrix, 9
- ctmc-class, 11
- ctmcFit, 13

- dim,ctmc-method (ctmc-class), 11
- dim,markovchain-method
  - (markovchain-class), 30
- dim,markovchainList-method
  - (markovchainList-class), 33
- expectedRewards, 14
- expectedRewardsBeforeHittingA, 15
- ExpectedTime, 15
- firstPassage, 16, 18
- firstPassageMultiple, 17
- fitHigherOrder, 18
- fitHighOrderMultivarMC, 19
- freq2Generator, 20
- generatorToTransitionMatrix, 12, 21, 47
- HigherOrderMarkovChain-class, 22
- holson, 22
- hommc (hommc-class), 23
- hommc-class, 23
- ictmc (ictmc-class), 24
- ictmc-class, 24
- impreciseProbabilityatT, 24
- inferHyperparam, 25, 45
- initialize,ctmc-method (ctmc-class), 11
- initialize,markovchain-method
  - (markovchain-class), 30
- is.accessible, 26
- is.CTMCirreducible, 27
- is.irreducible, 28
- is.TimeReversible, 29
- kullback, 30
- markovchain, 5, 8, 19, 34, 38, 51, 52, 54
- markovchain (markovchain-package), 3
- markovchain-class, 30
- markovchain-package, 3
- markovchainFit, 26, 32, 36, 43, 49
- markovchainFit (createSequenceMatrix), 9
- markovchainList-class, 33
- markovchainListFit, 11, 35
- markovchainSequence, 11, 32, 36, 49
- meanFirstPassageTime, 37
- multinomialConfidenceIntervals, 38
- name, 39
- name,markovchain-method (name), 39
- name<-, 40
- name<-,markovchain-method (name<-), 40
- names,markovchain-method
  - (markovchain-class), 30
- names<-,markovchain-method
  - (markovchain-class), 30
- noofVisitsDist, 40
- period (absorbingStates), 4
- plot,ctmc,missing-method (ctmc-class), 11
- plot,markovchain,missing-method
  - (markovchain-class), 30
- predict,markovchain-method
  - (markovchain-class), 30
- predict,markovchainList-method
  - (markovchainList-class), 33
- predictHommc, 41
- predictiveDistribution, 26, 42, 45
- preproglucacon, 43
- print,markovchain-method
  - (markovchain-class), 30
- print,markovchainList-method
  - (markovchainList-class), 33
- priorDistribution, 44
- probabilityatT, 45
- rain, 46
- rctmc, 12, 13, 21, 47, 54
- recurrentClasses (absorbingStates), 4
- rmarkovchain, 48
- sales, 50
- seq2freqProb (fitHigherOrder), 18
- seq2matHigh (fitHigherOrder), 18
- show, hommc-method, 50
- show,markovchain-method
  - (markovchain-class), 30
- show,markovchainList-method
  - (markovchainList-class), 33
- sort,markovchain-method
  - (markovchain-class), 30
- states, 51
- states,ctmc-method (ctmc-class), 11
- states,markovchain-method (states), 51
- steadyStates, 52
- steadyStates,ctmc-method (ctmc-class), 11

steadyStates,markovchain-method  
    (steadyStates), 52  
summary, 29  
summary,markovchain-method  
    (markovchain-class), 30

t,markovchain-method  
    (markovchain-class), 30  
tm\_abs, 53  
transientStates (absorbingStates), 4  
transientStates,markovchain-method  
    (absorbingStates), 4  
transition2Generator, 53  
transitionProbability, 54  
transitionProbability,markovchain-method  
    (transitionProbability), 54

verifyEmpiricalToTheoretical  
    (verifyMarkovProperty), 55  
verifyHomogeneity  
    (verifyMarkovProperty), 55  
verifyMarkovProperty, 55