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Description A comprehensive collection of functions for conducting meta-analyses in R. The package includes functions to calculate various effect sizes or outcome measures, fit equal-, fixed-, random-, and mixed-effects models to such data, carry out moderator and meta-regression analyses, and create various types of meta-analytical plots (e.g., forest, funnel, radial, L’Abbe, B aujat, bubble, and GOSH plots). For meta-analyses of binomial and person-time data, the package also provides functions that implement specialized methods, including the Mantel-Haenszel method, Peto's method, and a variety of suitable generalized linear (mixed-effects) models (i.e., mixed-effects logistic and Poisson regression models). Finally, the package provides functionality for fitting meta-analytic multivariate/multilevel models that account for non-independent sampling errors and/or true effects (e.g., due to the inclusion of multiple treatment studies, multiple endpoints, or other forms of clustering). Network meta-analyses and meta-analyses accounting for known correlation structures (e.g., due to phylogenetic relatedness) can also be conducted. An introduction to the package can be found in Viechtbauer (2010) <doi:10.18637/jss.v036.i03>.
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BugReports https://github.com/wviechtb/metafor/issues
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Description

The metafor package provides a comprehensive collection of functions for conducting meta-analyses in R. The package can be used to calculate various effect sizes or outcome measures and then allows the user to fit equal-, fixed-, and random-effects models to these data. By including study-level variables (‘moderators’) as predictors in these models, (mixed-effects) meta-regression models can also be fitted. For meta-analyses of $2 \times 2$ tables, proportions, incidence rates, and incidence rate ratios, the package also provides functions that implement specialized methods, including the Mantel-Haenszel method, Peto’s method, and a variety of suitable generalized linear mixed-effects models (i.e., mixed-effects logistic and Poisson regression models). For non-independent effects/outcomes (e.g., due to correlated sampling errors, correlated true effects or outcomes, or other forms of clustering), the package also provides a function for fitting multilevel and multivariate models to meta-analytic data.

Various methods are available to assess model fit, to identify outliers and/or influential studies, and for conducting sensitivity analyses (e.g., standardized residuals, Cook’s distances, leave-one-out analyses). Advanced techniques for hypothesis testing and obtaining confidence intervals (e.g., for the average effect or outcome or for the model coefficients in a meta-regression model) have also been implemented (e.g., the Knapp and Hartung method, permutation tests, cluster-robust inference methods / robust variance estimation).

The package also provides functions for creating forest, funnel, radial (Galbraith), normal quantile-quantile, L’Abbé, Baujat, bubble, and GOSH plots. The presence of publication bias (or more precisely, funnel plot asymmetry or ‘small-study effects’) and its potential impact on the results can be examined via the rank correlation and Egger’s regression test, the trim and fill method, the test of excess significance, and by applying a variety of selection models.

The escalc Function

escalc Before a meta-analysis can be conducted, the relevant results from each study must be quantified in such a way that the resulting values can be further aggregated and compared. The escalc function can be used to compute a wide variety of effect sizes or outcome measures (and the corresponding sampling variances) that are often used in meta-analyses (e.g., risk ratios, odds ratios, risk differences, mean differences, standardized mean differences, response ratios / ratios of means, raw or r-to-z transformed correlation coefficients). Measures for quantifying some characteristic of individual groups (e.g., in terms of means, proportions, or incidence rates and transformations thereof), measures of change (e.g., raw and standardized mean changes), and measures of variability (e.g., variability ratios and coefficient of variation ratios) are also available.

The rma.uni Function

rma.uni The various meta-analytic models that are typically used in practice are special cases of the general linear (mixed-effects) model. The rma.uni function (with alias rma) provides a general framework for fitting such models. The function can be used in combination with any of the effect
sizes or outcome measures computed with the \texttt{escalc} function or, more generally, any set of estimates (with corresponding sampling variances or standard errors) one would like to analyze. The notation and models underlying the \texttt{rma.uni} function are explained below.

For a set of $i = 1, \ldots, k$ independent studies, let $y_i$ denote the observed value of the effect size or outcome measure in the $i$th study. Let $\theta_i$ denote the corresponding (unknown) true effect/outcome, such that

$$y_i | \theta_i \sim N(\theta_i, v_i).$$

In other words, the observed effect sizes or outcomes are assumed to be unbiased and normally distributed estimates of the corresponding true effects/outcomes with sampling variances equal to $v_i$ (where $v_i$ is just the square of the standard errors of the estimates). The $v_i$ values are assumed to be known. Depending on the outcome measure used, a bias correction, normalizing, and/or variance stabilizing transformation may be necessary to ensure that these assumptions are (at least approximately) true (e.g., the log transformation for odds/risk ratios, the bias correction for standardized mean differences, Fisher’s r-to-z transformation for correlations; see \texttt{escalc} for more details).

According to the random-effects model, we further assume that $\theta_i \sim N(\mu, \tau^2)$, that is, the true effects/outcomes are normally distributed with $\mu$ denoting the average true effect/outcome and $\tau^2$ the variance in the true effects/outcomes ($\tau^2$ is therefore often referred to as the amount of ‘heterogeneity’ in the true effects/outcomes). The random-effects model can also be written as

$$y_i = \mu + u_i + \varepsilon_i,$$

where $u_i \sim N(0, \tau^2)$ and $\varepsilon_i \sim N(0, v_i)$. The fitted model provides estimates of $\mu$ and $\tau^2$, that is,

$$\hat{\mu} = \frac{\sum_{i=1}^{k} w_i y_i}{\sum_{i=1}^{k} w_i},$$

where $w_i = 1/(\hat{\tau}^2 + v_i)$ and $\hat{\tau}^2$ denotes an estimate of $\tau^2$ obtained with one of the many estimators that have described in the literature for this purpose (this is the standard ‘inverse-variance’ method for random-effects models).

A special case of the model above is the equal-effects model (also sometimes called the common-effects model) which arises when $\tau^2 = 0$. In this case, the true effects/outcomes are homogeneous (i.e., $\theta_1 = \theta_2 = \ldots = \theta_k \equiv \theta$) and hence we can write the model as

$$y_i = \theta + \varepsilon_i,$$

where $\theta$ denotes the true effect/outcome in the studies, which is estimated with

$$\hat{\theta} = \frac{\sum_{i=1}^{k} w_i y_i}{\sum_{i=1}^{k} w_i},$$

where $w_i = 1/v_i$ (again, this is the standard ‘inverse-variance’ method as described in the meta-analytic literature). Note that the commonly-used term ‘fixed-effects model’ is not used here - for an explanation, see here.

Study-level variables (often referred to as ‘moderators’) can also be included as predictors in meta-analytic models, leading to so-called ‘meta-regression’ analyses (to examine whether the effects/outcomes tend to be larger/smaller under certain conditions or circumstances). When including moderator variables in a random-effects model, we obtain a mixed-effects meta-regression model. This model can be written as

$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \ldots + \beta_p x_{ip} + u_i + \varepsilon_i,$$
where \( u_i \sim N(0, \tau^2) \) and \( \varepsilon_i \sim N(0, \nu_i) \) as before and \( x_{ij} \) denotes the value of the \( j \)th moderator variable for the \( i \)th study (letting \( p = p' + 1 \) denote the total number of coefficients in the model including the model intercept). Therefore, \( \beta_j \) denotes how the average true effect/outcome changes for a one-unit increase in \( x_{ij} \) and the model intercept \( \beta_0 \) denotes the average true effect/outcome when the values of all moderator variables are equal to zero. The value of \( \tau^2 \) in the mixed-effects model denotes the amount of ‘residual heterogeneity’ in the true effects/outcomes (i.e., the amount of variability in the true effects/outcomes that is not accounted for by the moderators included in the model).

The \texttt{rma.mh} Function

\texttt{rma.mh} The Mantel-Haenszel method provides an alternative approach for fitting equal-effects models when dealing with studies providing data in the form of \( 2 \times 2 \) tables or in the form of event counts (i.e., person-time data) for two groups (Mantel & Haenszel, 1959). The method is particularly advantageous when aggregating a large number of studies with small sample sizes (the so-called sparse data or increasing strata case). The Mantel-Haenszel method is implemented in the \texttt{rma.mh} function. It can be used in combination with risk ratios, odds ratios, risk differences, incidence rate ratios, and incidence rate differences.

The \texttt{rma.peto} Function

\texttt{rma.peto} Yet another method that can be used in the context of a meta-analysis of \( 2 \times 2 \) table data is Peto’s method (see Yusuf et al., 1985), implemented in the \texttt{rma.peto} function. The method provides an estimate of the (log) odds ratio under an equal-effects model. The method is particularly advantageous when the event of interest is rare, but see the documentation of the function for some caveats.

The \texttt{rma.glmm} Function

\texttt{rma.glmm} Dichotomous outcomes and event counts (based on which one can calculate outcome measures such as odds ratios, incidence rate ratios, proportions, and incidence rates) are often assumed to arise from binomial and Poisson distributed data. Meta-analytic models that are directly based on such distributions are implemented in the \texttt{rma.glmm} function. These models are essentially special cases of generalized linear mixed-effects models (i.e., mixed-effects logistic and Poisson regression models). For \( 2 \times 2 \) table data, a mixed-effects conditional logistic model (based on the non-central hypergeometric distribution) is also available. Random/mixed-effects models with dichotomous data are often referred to as ‘binomial-normal’ models in the meta-analytic literature. Analogously, for event count data, such models could be referred to as ‘Poisson-normal’ models.

The \texttt{rma.mv} Function

\texttt{rma.mv} Standard meta-analytic models assume independence between the observed effect sizes or outcomes obtained from a set of studies. This assumption is often violated in practice. Dependencies can arise for a variety of reasons. For example, the sampling errors and/or true effects/outcomes may be correlated in multiple treatment studies (e.g., when multiple treatment groups are compared with a common control/reference group, such that the data from the control/reference group is used multiple times to compute the observed effect sizes or outcomes) or in multiple endpoint studies (e.g., when more than one effect size estimate or outcome is calculated based on the same sample
of subjects due to the use of multiple endpoints or response variables). Correlations in the true effects/outcomes can also arise due to other forms of clustering (e.g., when multiple effects/outcomes derived from the same author, lab, or research group may be more similar to each other than effects/outcomes derived from different authors, labs, or research groups). In ecology and related fields, the shared phylogenetic history among the organisms studied (e.g., plants, fungi, animals) can also induce correlations among the effects/outcomes. The `rma.mv` function can be used to fit suitable meta-analytic multivariate/multilevel models to such data, so that the non-independence in the effects/outcomes is accounted for. Network meta-analyses (also called multiple/mixed treatment comparisons) can also be carried out with this function.

### Future Plans and Updates

The `metafor` package is a work in progress and is updated on a regular basis with new functions and options. With `metafor.news()`, you can read the ‘NEWS’ file of the package after installation. Comments, feedback, and suggestions for improvements are always welcome.

### Citing the Package

To cite the package, please use the following reference:


### Getting Started with the Package

The paper mentioned above is a good starting place for those interested in using the package. The purpose of the article is to provide a general overview of the package and its capabilities (as of version 1.4-0). Not all of the functions and options are described in the paper, but it should provide a useful introduction to the package. The paper can be freely downloaded from the URL given above or can be directly loaded with the command `vignette("metafor")`. In addition to reading the paper, carefully read this page and then the help pages for the `escalc` and the `rma.uni` functions (or the `rma.mh`, `rma.peto`, `rma.glmm`, and/or `rma.mv` functions if you intend to use these methods). The help pages for these functions provide links to many additional functions, which can be used after fitting a model. You can also read the entire documentation online at [https://wviechtb.github.io/metafor/](https://wviechtb.github.io/metafor/) (where it is nicely formatted and the output from all examples is provided).

A (pdf) diagram showing the various functions in the metafor package (and how they are related to each other) can be opened with the command `vignette("diagram")`. Finally, additional information about the package, several detailed analysis examples, examples of plots and figures provided by the package (with the corresponding code), some additional tips and notes, and a FAQ can be found on the package website at [https://www.metafor-project.org](https://www.metafor-project.org).

### Author(s)

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Suggestions on how to obtain help with using the package can found on the package website at: 
https://www.metafor-project.org/doku.php/help

References


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**addepoly**

*Add Polygons to Forest Plots*

**Description**

The `addepoly` function can be used to add polygons, sometimes called ‘diamonds’, to a forest plot, for example to indicate summary estimates for subgroups of studies or to indicate fitted/predicted values based on models involving moderators.

**Usage**

```r
addepoly(x, ...)  
```

**Arguments**

- `x` either an object of class "rma", an object of class "predict.rma", or the values at which polygons should be drawn. See 'Details'.
- `...` other arguments.

**Details**

Currently, methods exist for three types of situations.

In the first case, object `x` is a fitted model coming from the `rma.uni`, `rma.mh`, `rma.peto`, `rma.glmm`, or `rma.mv` functions. The model must either be an equal- or a random-effects model, that is, the model should not contain any moderators. The corresponding method is called `addepoly.rma`. It can be used to add a polygon to an existing forest plot (usually at the bottom), showing the summary estimate (with its confidence interval) based on the fitted model.
Alternatively, x can be an object of class "predict.rma" obtained with the `predict.rma` function. In this case, polygons based on the predicted values are drawn. The corresponding method is `addpoly.predict.rma`.

Alternatively, object x can be a vector with values at which one or more polygons should be drawn. The corresponding method is then `addpoly.default`.

Author(s)
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References

See Also
`addpoly.rma`, `addpoly.predict.rma`, and `addpoly.default` for the specific method functions. `forest.rma` and `forest.default` for functions to draw forest plots to which polygons can be added.

---

**addpoly.default**

Add Polygons to Forest Plots (Default Method)

Description
Function to add one or more polygons to a forest plot.

Usage
```r
## Default S3 method:
addpoly(x, vi, sei, ci.lb, ci.ub, pi.lb, pi.ub,
  rows=-1, level, annotate, digits, width, mlab,
  transf, atransf, targs, efac, col, border, lty, fonts, cex, ...)
```

Arguments
- **x**: vector with the values at which the polygons should be drawn.
- **vi**: vector with the corresponding variances.
- **sei**: vector with the corresponding standard errors (note: only one of the two, vi or sei, needs to be specified).
- **ci.lb**: vector with the corresponding lower confidence interval bounds. Not needed if vi or sei is specified. See ‘Details’.
- **ci.ub**: vector with the corresponding upper confidence interval bounds. Not needed if vi or sei is specified. See ‘Details’.
- **pi.lb**: optional vector with the corresponding lower prediction interval bounds.
addpoly.default

pi.ub  optional vector with the corresponding upper prediction interval bounds.
rows  vector to specify the rows (or more generally, the horizontal positions) for plotting the polygons (defaults is \(-1\)). Can also be a single value to specify the row (horizontal position) of the first polygon (the remaining polygons are then plotted below this starting row).
level  optional numeric value between 0 and 100 to specify the confidence interval level.
annotate  optional logical to specify whether annotations should be added to the plot for the polygons that are drawn.
digits  optional integer to specify the number of decimal places to which the annotations should be rounded.
width  optional integer to manually adjust the width of the columns for the annotations.
mlab  optional character vector with the same length as \(x\) giving labels for the polygons that are drawn.
transf  optional argument to specify a function to transform the \(x\) values and confidence interval bounds (e.g., \(\text{transf=exp}\); see also \(\text{transf}\)).
atransf  optional argument to specify a function to transform the annotations (e.g., \(\text{atransf=exp}\); see also \(\text{transf}\)).
targs  optional arguments needed by the function specified via \(\text{transf}\) or \(\text{atransf}\).
efac  optional vertical expansion factor for the polygons.
col  optional character string to specify the color to use for the polygons. If unspecified, the function sets a default color.
border  optional character string to specify the color to use for the border of the polygons. If unspecified, the function sets a default color.
lty  optional character string to specify the line type for the prediction interval. If unspecified, the function sets this to "dotted" by default.
fonts  optional character string to specify the font to use for the labels and annotations.
cex  optional symbol expansion factor.
...  other arguments.

Details

The function can be used to add one or more polygons to an existing forest plot created with the \texttt{forest} function. For example, summary estimates based on a model involving moderators can be added to the plot this way (see ‘Examples’).

To use the function, one should specify the values at which the polygons should be drawn (via the \(x\) argument) together with the corresponding variances (via the \(vi\) argument) or with the corresponding standard errors (via the \(sei\) argument). Alternatively, one can specify the values at which the polygons should be drawn together with the corresponding confidence interval bounds (via the \(ci.lb\) and \(ci.ub\) arguments). Optionally, one can also specify the bounds of the corresponding prediction interval bounds via the \(pi.lb\) and \(pi.ub\) arguments.

If unspecified, arguments \texttt{level}, \texttt{annotate}, \texttt{digits}, \texttt{width}, \texttt{transf}, \texttt{atransf}, \texttt{targs}, \texttt{efac} (only if the forest plot was created with \texttt{forest.rma}), \texttt{fonts}, \texttt{cex}, \texttt{annosym}, and \texttt{textpos} are automatically set equal to the same values that were used when creating the forest plot.
Author(s)

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References


See Also

`forest.rma` and `forest.default` for functions to draw forest plots to which polygons can be added.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude as a moderator
res <- rma(yi, vi, mods = ~ ablat, slab=paste(author, year, sep=".", "), data=dat)

### forest plot of the observed risk ratios
forest(res, addfit=FALSE, atransf=exp, xlim=c(-8,5), ylim=c(-4.5,16), cex=.8,
order=ablat, ilab=ablat, ilab.xpos=-4, header="Author(s) and Year")

### predicted average log risk ratios for 10, 30, and 50 degrees absolute latitude
x <- predict(res, newmods=c(10, 30, 50))

### add predicted average risk ratios to forest plot
addpoly(x$pred, sei=x$se, rows=-2, mlab=c("- at 10 Degrees", "- at 30 Degrees", "- at 50 Degrees"))
abline(h=0)
text(-8, -1, "Model-Based Estimates:", pos=4, cex=.8)
text(-4, res$k+2, "Latitude", cex=.8, font=2)
```

Description

Function to add one or more polygons to a forest plot based on an object of class "predict.rma".

Usage

```r
## S3 method for class 'predict.rma'
addpoly(x, rows=-2, annotate,
        addpred=FALSE, digits, width, mlab, transf, atransf, targs,
        efac, col, border, lty, fonts, cex, ...)
```
Arguments

- **x**: an object of class "predict.rma".
- **rows**: vector to specify the rows (or more generally, the horizontal positions) for plotting the polygons (defaults is -2). Can also be a single value to specify the row (horizontal position) of the first polygon (the remaining polygons are then plotted below this starting row).
- **annotate**: optional logical to specify whether annotations should be added to the plot for the polygons that are drawn.
- **addpred**: logical to specify whether the bounds of the prediction interval should be added to the plot (the default is FALSE).
- **digits**: optional integer to specify the number of decimal places to which the annotations should be rounded.
- **width**: optional integer to manually adjust the width of the columns for the annotations.
- **mlab**: optional character vector with the same length as x giving labels for the polygons that are drawn.
- **transf**: optional argument to specify a function to transform the x values and confidence interval bounds (e.g., transf=exp; see also transf).
- **atransf**: optional argument to specify a function to transform the annotations (e.g., atransf=exp; see also transf).
- **targs**: optional arguments needed by the function specified via transf or atransf.
- **efac**: optional vertical expansion factor for the polygons.
- **col**: optional character string to specify the color to use for the polygons. If unspecified, the function sets a default color.
- **border**: optional character string to specify color to use for the border of the polygons. If unspecified, the function sets a default color.
- **lty**: optional character string to specify line type for the prediction interval. If unspecified, the function sets this to "dotted" by default.
- **fonts**: optional character string to specify the font to use for the labels and annotations.
- **cex**: optional symbol expansion factor.
- **...**: other arguments.

Details

The function can be used to add one or more polygons to an existing forest plot created with the forest function. For example, summary estimates based on a model involving moderators can be added to the plot this way (see ‘Examples’).

To use the function, one should specify the values at which the polygons should be drawn (via the x argument) together with the corresponding variances (via the vi argument) or with the corresponding standard errors (via the sei argument). Alternatively, one can specify the values at which the polygons should be drawn together with the corresponding confidence interval bounds (via the ci.lb and ci.ub arguments). Optionally, one can also specify the bounds of the corresponding prediction interval bounds via the pi.lb and pi.ub arguments.

If unspecified, arguments annotate, digits, width, transf, atransf, targs, efac (only if the forest plot was created with forest.rma), fonts, cex, annosym, and textpos are automatically set equal to the same values that were used when creating the forest plot.
addpoly.rma

Author(s)

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References


See Also

*forest.rma* and *forest.default* for functions to draw forest plots to which polygons can be added.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg,
               data=dat.bcg, slab=paste(author, year, sep=","))

### forest plot of the observed risk ratios
with(dat, forest(yi, vi, atransf=exp, xlim=c(-8,4), ylim=c(-4.5,16),
                 at=log(c(.05, .25, 1, 4)), cex=.8, order=alloc,
                 ilab=alloc, ilab.xpos=-4, header="Author(s) and Year"))

### fit mixed-effects model with allocation method as a moderator
res <- rma(yi, vi, mods = ~ 0 + alloc, data=dat)

### predicted log risk ratios for the different allocation methods
x <- predict(res, newmods=diag(3))

### add predicted average risk ratios to forest plot
addpoly(x, efac=1.4, col="gray", addpred=TRUE,
        mlab=c("Alternate Allocation", "Random Allocation", "Systematic Allocation"))
abline(h=0)
text(-8, -1, "Model-Based Estimates:", pos=4, cex=.8)
text(-4, res$K+2, "Allocation", cex=.8, font=2)
```

---

**addpoly.rma**  
Add Polygons to Forest Plots (Method for ‘rma’ Objects)

**Description**

Function to add a polygon to a forest plot showing the summary estimate with corresponding confidence interval based on an object of class “rma”. 

Usage

```r
## S3 method for class 'rma'
addpoly(x, row=-2, level=x$level, annotate,
    addpred=FALSE, digits, width, mlab, transf, atransf, targs,
    efac, col, border, lty, fonts, cex, ...)
```

Arguments

- `x`: an object of class "rma".
- `row`: numeric value to specify the row (or more generally, the horizontal position) for plotting the polygon (the default is -2).
- `level`: numeric value between 0 and 100 to specify the confidence interval level (the default is to take the value from the object).
- `annotate`: optional logical to specify whether annotations for the summary estimate should be added to the plot.
- `addpred`: logical to specify whether the bounds of the prediction interval should be added to the plot (the default is FALSE).
- `digits`: optional integer to specify the number of decimal places to which the annotations should be rounded.
- `width`: optional integer to manually adjust the width of the columns for the annotations.
- `mlab`: optional character string giving a label for the summary estimate polygon. If unspecified, the function sets a default label.
- `transf`: optional argument to specify a function to transform the summary estimate and confidence interval bound (e.g., `transf=exp`; see also `transf`).
- `atransf`: optional argument to specify a function to transform the annotations (e.g., `atransf=exp`; see also `transf`).
- `targs`: optional arguments needed by the function specified via `transf` or `atransf`.
- `efac`: optional vertical expansion factor for the polygon.
- `col`: optional character string to specify color to use for the polygon. If unspecified, the function sets a default color.
- `border`: optional character string to specify the color to use for the border of the polygon. If unspecified, the function sets a default color.
- `lty`: optional character string to specify the line type for the prediction interval. If unspecified, the function sets this to "dotted" by default.
- `fonts`: optional character string to specify the font to use for the label and annotations.
- `cex`: optional character string to specify color to use for the label and annotations.
- `...`: other arguments.

Details

The function can be used to add a four-sided polygon, sometimes called a summary ‘diamond’, to an existing forest plot created with the `forest` function. The polygon shows the summary estimate (with its confidence interval bounds) based on an equal- or a random-effects model. Using this...
function, summary estimates based on different types of models can be shown in the same plot. Also, summary estimates based on a subgrouping of the studies can be added to the plot this way. See ‘Examples’.

If unspecified, arguments annotate, digits, width, transf, atransf, targs, efac (only if the forest plot was created with \texttt{forest.rma}), fonts, cex, annosym, and textpos are automatically set equal to the same values that were used when creating the forest plot.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> \url{https://www.metafor-project.org}

References


See Also

\texttt{forest.rma} and \texttt{forest.default} for functions to draw forest plots to which polygons can be added.

Examples

### meta-analysis of the log risk ratios using the Mantel-Haenszel method
res <- rma.mh(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg,
    slab=paste(author, year, sep=","))

### forest plot of the observed risk ratios with summary estimate
forest(res, atransf=exp, xlim=c(-8,6), ylim=c(-2.5,16), header=TRUE)

### meta-analysis of the log risk ratios using a random-effects model
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### add summary estimate from the random-effects model to the forest plot
addpoly(res)

### forest plot with subgrouping of studies and summaries per subgroup
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg,
    slab=paste(author, year, sep=","))
tmp <- forest(res, xlim=c(-16, 4.6), at=log(c(.05, .25, 1, 4)), atransf=exp,
    ilab=cbind(tpos, tneg, cpos, cneg), ilab.xpos=c(-9.5,-8,-6,-4.5),
    cex=.75, ylim=c(-1, 27), order=alloc, rows=c(3:4,9:15,20:23),
    mlab="RE Model for All Studies", header="Author(s) and Year")
op <- par(cex=.75, font=2)
text(c(-9.5,-8,-6,-4.5), tmp$ylim[2]-1, c("TB+", "TB-", "TB+", "TB-"))
text(-16, c(24,16,5), c("Systematic Allocation", "Random Allocation",
    "Alternate Allocation"), pos=4)
par(op)
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg,
aggregate.escalc

aggregate.escalc

Aggregate Multiple Effect Sizes or Outcomes Within Studies

Description

The function can be used to aggregate multiple effect sizes or outcomes belonging to the same study (or to the same level of some other clustering variable) into a single combined effect size or outcome.

Usage

## S3 method for class 'escalc'
aggregate(x, cluster, time, obs, V, struct="CS", rho, phi,
  weighted=TRUE, checkpd=TRUE, fun, na.rm=TRUE,
  addk=FALSE, subset, select, digits, ...)

Arguments

x
  an object of class "escalc".

cluster
  vector to specify the clustering variable (e.g., study).

time
  optional vector to specify the time points (only relevant when struct="CAR", "CS+CAR", or "CS*CAR").

obs
  optional vector to distinguish different observed effect sizes or outcomes measured at the same time point (only relevant when struct="CS*CAR").

V
  optional argument to specify the variance-covariance matrix of the sampling errors. If not specified, argument struct is used to specify the variance-covariance structure.

struct
  character string to specify the variance-covariance structure of the sampling errors within the same cluster (either "ID", "CS", "CAR", "CS+CAR", or "CS*CAR"). See ‘Details’.

rho
  value of the correlation of the sampling errors within clusters (when struct="CS", "CS+CAR", or "CS*CAR"). Can also be a vector with the value of the correlation for each cluster.

phi
  value of the autocorrelation of the sampling errors within clusters (when struct="CAR", "CS+CAR", or "CS*CAR"). Can also be a vector with the value of the autocorrelation for each cluster.
aggregate.escalc

weighted logical to specify whether estimates within clusters should be aggregated using inverse-variance weighting (the default is TRUE). If set to FALSE, unweighted averages are computed.

checkpd logical to specify whether to check that the variance-covariance matrices of the sampling errors within clusters are positive definite (the default is TRUE).

fun optional list with three functions for aggregating other variables besides the effect sizes or outcomes within clusters (for numeric/integer variables, for logics, and for all other types, respectively).

na.rm logical to specify whether NA values should be removed before aggregating values within clusters. Can also be a vector with two logics (the first pertaining to the effect sizes or outcomes, the second to all other variables).

addk logical to specify whether to add the cluster size as a new variable (called ki) to the dataset (the default is FALSE).

subset optional (logical or numeric) vector to specify the subset of rows to include when aggregating the effect sizes or outcomes.

select optional vector to specify the names of the variables to include in the aggregated dataset.

digits optional integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).

... other arguments.

Details

In many meta-analyses, multiple effect sizes or outcomes can be extracted from the same study. Ideally, such structures should be analyzed using an appropriate multilevel/multivariate model as can be fitted with the rma.mv function. However, there may occasionally be reasons for aggregating multiple effect sizes or outcomes belonging to the same study (or to the same level of some other clustering variable) into a single combined effect size or outcome. The present function can be used for this purpose.

The input must be an object of class "escalc". The error ‘Error in match.fun(FUN): argument “FUN” is missing, with no default’ indicates that a regular data frame was passed to the function, but this does not work. One can turn a regular data frame (containing the effect sizes or outcomes and the corresponding sampling variances) into an "escalc" object with the escalc function. See the ‘Examples’ below for an illustration of this.

The cluster variable is used to specify which estimates/outcomes belong to the same study/cluster. In the simplest case, the estimates/outcomes within clusters (or, to be precise, their sampling errors) are assumed to be independent. This is usually a safe assumption as long as each study participant (or whatever the study units are) only contributes data to a single estimate/outcome. For example, if a study provides effect size estimates for male and female subjects separately, then the sampling errors can usually be assumed to be independent. In this case, one can set struct="ID" and multiple estimates/outcomes within the same cluster are combined using standard inverse-variance weighting (i.e., using weighted least squares) under the assumption of independence.

In other cases, the estimates/outcomes within clusters cannot be assumed to be independent. For example, if multiple effect size estimates are computed for the same group of subjects (e.g., based on different scales to measure some construct of interest), then the estimates are likely to be correlated.
If the actual correlation between the estimates is unknown, one can often still make an educated guess and set argument rho to this value, which is then assumed to be the same for all pairs of estimates within clusters when struct=“CS” (for a compound symmetric structure). Multiple estimates/outcomes within the same cluster are then combined using inverse-variance weighting taking their correlation into consideration (i.e., using generalized least squares). One can also specify a different value of rho for each cluster by passing a vector (of the same length as the number of clusters) to this argument.

If multiple effect size estimates are computed for the same group of subjects at different time points, then it may be more sensible to assume that the correlation between estimates decreases as a function of the distance between the time points. If so, one can specify struct=“CAR” (for a continuous-time autoregressive structure), set phi to the autocorrelation (for two estimates one time-unit apart), and use argument time to specify the actual time points corresponding to the estimates. The correlation between two estimates, \( y_{it} \) and \( y_{it'} \), in the \( i \)th cluster, with time points \( t_i \) and \( t_{i'} \), is then given by \( \rho \left| \alpha \right| \left( \frac{|t_i - t_{i'}|}{\phi} \right)^{\phi} \). One can also specify different values of phi for each cluster by passing a vector (of the same length as the number of clusters) to this argument.

One can also combine the compound symmetric and autoregressive structures if there are multiple time points and multiple observed effect sizes or outcomes at these time points. One option is struct=“CS+CAR”. In this case, one must specify both the time and obs arguments. The correlation between two estimates, \( y_{it} \) and \( y_{ijt'} \), in the \( i \)th cluster, with time points \( t_i \) and \( t_{ijt'} \), is then given by \( \rho + (1 - \rho) \left| \alpha \right| ^{\left| t_i - t_{ijt'} \right|} \).

Alternatively, one can specify struct=“CS*CAR”. In this case, one must specify the time argument and both rho and phi. The correlation between two estimates, \( y_{ijt} \) and \( y_{ijt'} \), with the same value for obs but different values for time, is then given by \( \phi \left| t_{ijt} - t_{ijt'} \right| \), the correlation between two estimates, \( y_{ijt} \) and \( y_{ijt'} \), with different values for obs but the same value for time, is then given by \( \rho \), and the correlation between two estimates, \( y_{ijt} \) and \( y_{ijt'} \), with different values for obs and different values for time, is then given by \( \rho \times \phi \left| t_{ijt} - t_{ijt'} \right| \).

Finally, if one actually knows the correlation (and hence the covariance) between each pair of estimates (or has an approximation thereof), one can also specify the entire variance-covariance matrix of the estimates (or more precisely, their sampling errors) via the V argument (in this case, arguments struct, time, obs, rho, and phi are ignored). Note that the vcalc function can be used to construct such a V matrix and provides even more flexibility for specifying various types of dependencies. See the ‘Examples’ below for an illustration of this.

Instead of using inverse-variance weighting (i.e., weighted/generalized least squares) to combine the estimates within clusters, one can set weighted=FALSE in which case the estimates are averaged within clusters without any weighting (although the correlations between estimates as specified are still taken into consideration).

Other variables (besides the estimates) will also be aggregated to the cluster level. By default, numeric/integer type variables are averaged, logicals are also averaged (yielding the proportion of TRUE values), and for all other types of variables (e.g., character variables or factors) the most frequent category/level is returned. One can also specify a list of three functions via the fun argument for aggregating variables belonging to these three types.

Argument na.rm controls how missing values should be handled. By default, any missing estimates are first removed before aggregating the non-missing values within each cluster. The same applies when aggregating the other variables. One can also specify a vector with two logicals for the na.rm argument to control how missing values should be handled when aggregating the estimates and when aggregating all other variables.
aggregate.escalc

Value

An object of class c("escalc","data.frame") that contains the (selected) variables aggregated to the cluster level.

The object is formatted and printed with the print function.

Author(s)

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References


See Also

escalc for a function to create escalc objects.

Examples

```r
### copy data into 'dat' and examine data
dat <- dat.konstantopoulos2011
head(dat, 11)

### aggregate estimates to the district level, assuming independent sampling
### errors for multiples studies/schools within the same district
agg <- aggregate(dat, cluster=district, struct="ID", addk=TRUE)
agg

### copy data into 'dat' and examine data
dat <- dat.assink2016
head(dat, 19)

### note: 'dat' is a regular data frame
class(dat)

### turn data frame into an 'escalc' object
dat <- escalc(yi=yi, vi=vi, data=dat)
class(dat)

### aggregate the estimates to the study level, assuming a CS structure for
### the sampling errors within studies with a correlation of 0.6
agg <- aggregate(dat, cluster=study, rho=0.6)
agg

### use vcalc() and then the V argument
V <- vcalc(vi, cluster=study, obs=esid, data=dat, rho=0.6)
agg <- aggregate(dat, cluster=study, V=V)
agg

### use a correlation of 0.7 for effect sizes corresponding to the same type of
```
### delinquent behavior and a correlation of 0.5 for effect sizes corresponding
### to different types of delinquent behavior
V <- vcalc(vi, cluster=study, type=deltype, obs=esid, data=dat, rho=c(0.7, 0.5))
agg <- aggregate(dat, cluster=study, V=V)

### reshape 'dat.ishak2007' into long format
dat <- dat.ishak2007
dat <- reshape(dat.ishak2007, direction="long", idvar="study", v.names=c("yi","vi"),
    varying=list(c(2,4,6,8), c(3,5,7,9)))
dat <- dat[order(study, time),]
dat <- dat[!is.na(yi),]
rownames(dat) <- NULL
head(dat, 8)

### aggregate the estimates to the study level, assuming a CAR structure for
### the sampling errors within studies with an autocorrelation of 0.9
agg <- aggregate(dat, cluster=study, struct="CAR", time=time, phi=0.9)
head(agg, 5)

---

**anova.rma**

*Likelihood Ratio and Wald-Type Tests for 'rma' Objects*

**Description**

For two (nested) models of class "rma.uni" or "rma.mv", the function provides a full versus reduced model comparison in terms of model fit statistics and a likelihood ratio test. When a single model is specified, a Wald-type test of one or more model coefficients or linear combinations thereof is carried out.

**Usage**

```r
## S3 method for class 'rma'
anova(object, object2, btt, X, att, Z, rhs, digits, refit=FALSE, ...)
```

**Arguments**

- `object` an object of class "rma.uni" or "rma.mv".
- `object2` an (optional) object of class "rma.uni" or "rma.mv". Only relevant when conducting a model comparison and likelihood ratio test. See ‘Details’.
- `btt` optional vector of indices (or list thereof) to specify which coefficients should be included in the Wald-type test. Can also be a string to `grep` for. See ‘Details’.
- `X` optional numeric vector or matrix to specify one or more linear combinations of the coefficients in the model that should be tested. See ‘Details’.
- `att` optional vector of indices (or list thereof) to specify which scale coefficients should be included in the Wald-type test. Can also be a string to `grep` for. See ‘Details’. Only relevant for location-scale models (see `rma.uni`).
optional numeric vector or matrix to specify one or more linear combinations of the scale coefficients in the model that should be tested. See ‘Details’. Only relevant for location-scale models (see \texttt{rma.uni}).

\texttt{rhs} \hspace{1cm} \text{optional scalar or vector of values for the right-hand side of the null hypothesis when testing a set of coefficients (via \texttt{btt} or \texttt{att}) or linear combinations thereof (via \texttt{X} or \texttt{Z}). If unspecified, this defaults to a vector of zeros of the appropriate length. See ‘Details’.

\texttt{digits} \hspace{1cm} \text{optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.}

\texttt{refit} \hspace{1cm} \text{logical to indicate whether models fitted with REML estimation and differing in their fixed effects should be refitted with ML estimation when conducting a likelihood ratio test (the default is \texttt{FALSE}).}

... \hspace{1cm} \text{other arguments.}

\section*{Details}

The function can be used in three different ways:

1. When a single model is specified (via argument \texttt{object}), the function provides a Wald-type test of one or more model coefficients, that is,

\[ H_0: \beta_{j \in \texttt{btt}} = 0, \]

where \( \beta_{j \in \texttt{btt}} \) is the set of coefficients to be tested (by default whether the set of coefficients is significantly different from zero, but one can specify a different value under the null hypothesis via argument \texttt{rhs}).

In particular, for equal- or random-effects models (i.e., models without moderators), this is just the test of the single coefficient of the model (i.e., \( H_0: \theta = 0 \) or \( H_0: \mu = 0 \)). For models including moderators, an omnibus test of all model coefficients is conducted that excludes the intercept (the first coefficient) if it is included in the model. If no intercept is included in the model, then the omnibus test includes all coefficients in the model including the first.

Alternatively, one can manually specify the indices of the coefficients to test via the \texttt{btt} (‘betas to test’) argument. For example, with \texttt{btt=c(3,4)}, only the third and fourth coefficients from the model are included in the test (if an intercept is included in the model, then it corresponds to the first coefficient in the model). Instead of specifying the coefficient numbers, one can specify a string for \texttt{btt}. In that case, \texttt{grep} will be used to search for all coefficient names that match the string. Using the \texttt{btt} argument, one can for example select all coefficients corresponding to a particular factor to test if the factor as a whole is significant. One can also specify a list of indices/strings, in which case tests of all list elements will be conducted. See ‘Examples’.

For location-scale models fitted with the \texttt{rma.uni} function, one can use the \texttt{att} argument in an analogous manner to specify the indices of the scale coefficients to test (i.e., \( H_0: \alpha_{j \in \texttt{att}} = 0, \) where \( \alpha_{j \in \texttt{att}} \) is the set of coefficients to be tested).

2. When a single model is specified (via argument \texttt{object}), one can use the \texttt{X} argument\(^1\) to specify a linear combination of the coefficients in the model that should be tested using a Wald-type test, that is,

\[ H_0: X \beta = 0, \]

\footnote{The \texttt{X} argument is currently only implemented for the \texttt{rma.uni} function.}
where \( X \) is a (row) vector of the same length as there are coefficients in the model (by default whether the linear combination is significantly different from zero, but one can specify a different value under the null hypothesis via argument \( \text{rhs} \)). If a matrix of linear combinations is specified, each row defines a particular linear combination to be tested (if \( \text{rhs} \) is used, then it should either be a scalar or of the same length as the number of combinations to be tested). If the matrix is of full rank, an omnibus Wald-type test of all linear combinations is also provided. Linear combinations can also be obtained with the \text{predict} function, which provides corresponding confidence intervals.

For location-scale models fitted with the \text{rma.uni} function, one can use the \( Z \) argument in an analogous manner to specify one or multiple linear combinations of the scale coefficients in the model that should be tested (i.e., \( H_0: Z_\alpha = 0 \)).

3. When specifying two models for comparison (via arguments \text{object} and \text{object2}), the function provides a likelihood ratio test (LRT) comparing the two models. The two models must be based on the same set of data, must be of the same class, and should be nested for the LRT to make sense. Also, LRTs are not meaningful when using REML estimation and the two models differ in terms of their fixed effects (setting \text{refit=}TRUE automatically refits the two models using ML estimation). Also, the theory underlying LRTs is only really applicable when comparing models that were fitted with ML/REML estimation, so if some other estimation was used to fit the two models, the results should be treated with caution.

---

1 This argument used to be called \( L \), but was renamed to \( X \) (but using \( L \) in place of \( X \) still works).

**Value**

An object of class "\text{anova.rma}". When a single model is specified (without any further arguments or together with the \text{btt} or \text{att} argument), the object is a list containing the following components:

- \( \text{QM} \): test statistic of the Wald-type test of the model coefficients.
- \( \text{QMdf} \): corresponding degrees of freedom.
- \( \text{QMp} \): corresponding p-value.
- \( \text{btt} \): indices of the coefficients tested by the Wald-type test.
- \( k \): number of outcomes included in the analysis.
- \( p \): number of coefficients in the model (including the intercept).
- \( m \): number of coefficients included in the Wald-type test.
- \( \ldots \): some additional elements/values.

When \text{btt} or \text{att} was a list, then the object is a list of class "\text{list.anova.rma}", where each element is an "\text{anova.rma}" object as described above.

When argument \( X \) is used, the object is a list containing the following components:

- \( \text{QM} \): test statistic of the omnibus Wald-type test of all linear combinations.
- \( \text{QMdf} \): corresponding degrees of freedom.
- \( \text{QMp} \): corresponding p-value.
- \( \text{hyp} \): description of the linear combinations tested.
values of the linear combinations.

se standard errors of the linear combinations.

zval test statistics of the linear combinations.

pval corresponding p-values.

When two models are specified, the object is a list containing the following components:

fit.stats.f log-likelihood, deviance, AIC, BIC, and AICc for the full model.

fit.stats.r log-likelihood, deviance, AIC, BIC, and AICc for the reduced model.

parms.f number of parameters in the full model.

parms.r number of parameters in the reduced model.

LRT likelihood ratio test statistic.

pval corresponding p-value.

QE.f test statistic of the test for (residual) heterogeneity from the full model.

QE.r test statistic of the test for (residual) heterogeneity from the reduced model.

tau2.f estimated \( \tau^2 \) value from the full model. NA for "rma.mv" objects.

tau2.r estimated \( \tau^2 \) value from the reduced model. NA for "rma.mv" objects.

R2 amount (in percent) of the heterogeneity in the reduced model that is accounted for in the full model (NA for "rma.mv" objects). This can be regarded as a pseudo \( R^2 \) statistic (Raudenbush, 2009). Note that the value may not be very accurate unless \( k \) is large (Lopez-Lopez et al., 2014).

... some additional elements/values.

The results are formatted and printed with the print function. To format the results as a data frame, one can use the as.data.frame function.

Notes

The function can also be used to conduct a likelihood ratio test (LRT) for the amount of (residual) heterogeneity in random- and mixed-effects models. The full model should then be fitted with either method="ML" or method="REML" and the reduced model with method="EE" (or with tau2=0). The p-value for the test is based on a chi-square distribution with 1 degree of freedom, but actually needs to be adjusted for the fact that the parameter (i.e., \( \tau^2 \)) falls on the boundary of the parameter space under the null hypothesis (see Viechtbauer, 2007, for more details).

LRTs for variance components in more complex models (as fitted with the rma.mv function) can also be conducted in this manner (see ‘Examples’).

Author(s)

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References


See Also

`rma.uni` and `rma.mv` for functions to fit models for which likelihood ratio and Wald-type tests can be conducted.

`print.anova.rma` for the print method and `as.data.frame.anova.rma` for the method to format the results as a data frame.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res1 <- rma(yi, vi, data=dat, method="ML")

### fit mixed-effects model with two moderators (absolute latitude and publication year)
res2 <- rma(yi, vi, mods = ~ ablat + year, data=dat, method="ML")

### Wald-type test of the two moderators
anova(res2)

### alternative way of specifying the same test
anova(res2, X=rbind(c(0,1,0), c(0,0,1)))

### corresponding likelihood ratio test
anova(res1, res2)

### Wald-type test of a linear combination
anova(res2, X=c(1,35,1970))
```
### use predict() to obtain the same linear combination (with its CI)
```r
predict(res2, newmods=c(35,1970))
```

### mixed-effects model with three moderators
```r
res3 <- rma(yi, vi, mods = ~ ablat + year + alloc, data=dat, method="ML")
```

### Wald-type test of the 'alloc' factor
```r
anova(res3, btt=4:5)
```

### instead of specifying the coefficient numbers, grep for "alloc"
```r
anova(res3, btt="alloc")
```

### specify a list for the 'btt' argument
```r
anova(res3, btt=list(2,3,4:5))
```

########################################################################

### an example of doing LRTs of variance components in more complex models
```r
dat <- dat.konstantopoulos2011
res <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat)
```

### likelihood ratio test of the district-level variance component
```r
res0 <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat, sigma2=c(0,NA))
anova(res, res0)
```

### likelihood ratio test of the school-level variance component
```r
res0 <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat, sigma2=c(NA,0))
anova(res, res0)
```

### likelihood ratio test of both variance components simultaneously
```r
res0 <- rma.mv(yi, vi, data=dat)
anova(res, res0)
```

########################################################################

### an example illustrating a workflow involving cluster-robust inference
```r
dat <- dat.assink2016
```

### assume that the effect sizes within studies are correlated with rho=0.6
```r
V <- vcalc(vi, cluster=study, obs=esid, data=dat, rho=0.6)
```

### fit multilevel model using this approximate V matrix
```r
res <- rma.mv(yi, V, random = ~ 1 | study/esid, data=dat)
```

### likelihood ratio tests of the two variance components
```r
res0 <- rma.mv(yi, V, random = ~ 1 | study/esid, data=dat, sigma2=c(0,NA))
anova(res, res0)
res0 <- rma.mv(yi, V, random = ~ 1 | study/esid, data=dat, sigma2=c(NA,0))
anova(res, res0)
```

### use cluster-robust methods for inferences about the fixed effects
```r
sav <- robust(res, cluster=study, clubSandwich=TRUE)
sav

### examine if 'delttype' is a potential moderator
res <- rma.mv(yi, V, mods = ~ deltype, random = ~ 1 | study/esid, data=dat)
sav <- robust(res, cluster=study, clubSandwich=TRUE)
sav

### note: the (denominator) dfs for the omnibus F-test are very low, so the results
### of this test may not be trustworthy; consider using cluster wild bootstrapping
## Not run:
library(wildmeta)
Wald_test_cwb(res, constraints=constrain_zero(2:3), R=1000, seed=1234)
## End(Not run)
```

### Description

Function to create Baujat plots for objects of class "rma".

### Usage

```r
baujat(x, ...)
```

#### S3 method for class 'rma'

```r
baujat(x, xlim, ylim, xlab, ylab, cex, symbol="ids", grid=TRUE, progbar=FALSE, ...)
```

### Arguments

- `x`: an object of class "rma".
- `xlim`: x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
- `ylim`: y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
- `xlab`: title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
- `ylab`: title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
- `cex`: optional character expansion factor. If unspecified, the function tries to set this to a sensible value.
- `symbol`: either an integer to specify the pch value (i.e., plotting symbol), or "slab" to plot the study labels, or "ids" (the default) to plot the study id numbers.
- `grid`: logical to specify whether a grid should be added to the plot. Can also be a color name.
progress bar logical to specify whether a progress bar should be shown (the default is FALSE).

... other arguments.

Details

The model specified via x must be a model fitted with either the rma.uni, rma.mh, or rma.peto functions.

Baujat et al. (2002) proposed a diagnostic plot to detect sources of heterogeneity in meta-analytic data. The plot shows the contribution of each study to the overall Q-test statistic for heterogeneity on the x-axis versus the influence of each study (defined as the standardized squared difference between the overall estimate based on an equal-effects model with and without the study included in the model fitting) on the y-axis. The same type of plot can be produced by first fitting an equal-effects model with either the rma.uni (using method="EE"), rma.mh, or rma.peto functions and then passing the fitted model object to the baujat function.

For models fitted with the rma.uni function (which may be random-effects or mixed-effects meta-regressions models), the idea underlying this type of plot can be generalized as follows (Viechtbauer, 2021): The x-axis then corresponds to the squared Pearson residual of a study, while the y-axis corresponds to the standardized squared difference between the predicted/fitted value for the study with and without the study included in the model fitting.

By default, the points plotted are the study id numbers, but one can also plot the study labels by setting symbol="slab" (if study labels are available within the model object) or one can specify a plotting symbol via the symbol argument that gets passed to pch (see points for possible options).

Value

A data frame with components:

- x the x-axis coordinates of the points that were plotted.
- y the y-axis coordinates of the points that were plotted.
- ids the study id numbers.
- slab the study labels.

Note that the data frame is returned invisibly.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.uni, rma.mh and rma.peto for functions to fit models for which Baujat plots can be created.
influence.rma.uni for other model diagnostics.

Examples

```r
### copy data from Pignon et al. (2000) into 'dat'
dat <- dat.pignon2000

### calculate estimated log hazard ratios and sampling variances
dat$yi <- with(dat, OmE/V)
dat$vi <- with(dat, 1/V)

### meta-analysis based on all 65 trials
res <- rma(yi, vi, data=dat, method="EE", slab=trial)

### create Baujat plot
baujat(res)

### some variations of the plotting symbol
baujat(res, symbol=19)
baujat(res, symbol="slab")

### label only a selection of the more 'extreme' points
sav <- baujat(res, symbol=19, xlim=c(0,20))
sav <- sav[sav$x >= 10 | sav$y >= 0.10,]
text(sav$x, sav$y, sav$slab, pos=1)
```

bldiag

*Construct Block Diagonal Matrix*

Description

Function to construct a block diagonal matrix from (a list of) matrices.

Usage

```
bldiag(..., order)
```

Arguments

- `...`: individual matrices or a list of matrices.
- `order`: optional argument to specify a variable based on which a square block diagonal matrix should be ordered.

Author(s)

Posted to R-help by Berton Gunter (2 Sep 2005) with some further adjustments by Wolfgang Viechtbauer
See Also

rma.mv for the model fitting function that can take such a block diagonal matrix as input (for the V argument).

blsplit for a function that can split a block diagonal matrix into a list of sub-matrices.

Examples

```r
### copy data into 'dat'
dat <- dat.berkey1998

dat

### construct list with the variance-covariance matrices of the observed outcomes for the studies
V <- lapply(split(dat[,c("v1i","v2i")], dat$trial), as.matrix)
V

### construct block diagonal matrix
V <- bldiag(V)
V

### if we split based on 'author', the list elements in V are in a different order than that data
V <- lapply(split(dat[,c("v1i","v2i")], dat$author), as.matrix)
V

### can use 'order' argument to reorder the block-diagonal matrix into the correct order
V <- bldiag(V, order=dat$author)
V
```

blsplit

---

Split Block Diagonal Matrix

Description

Split a block diagonal matrix into a list of sub-matrices.

Usage

```r
blsplit(x, cluster, fun, args, sort=FALSE)
```

Arguments

- `x` a block diagonal matrix.
- `cluster` vector to specify the clustering variable to use for splitting.
- `fun` optional argument to specify a function to apply to each sub-matrix.
- `args` optional argument to specify any additional argument(s) for the function specified via `fun`.
- `sort` logical to indicate whether to sort the list by the unique cluster values (the default is `FALSE`).
Value
A list of one or more sub-matrices.

Author(s)
Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

See Also
bldiag for a function to create a block diagonal matrix based on sub-matrices.
vcalc for a function to construct a variance-covariance matrix of dependent effect sizes or outcomes, which often has a block diagonal structure.

Examples
### copy data into 'dat'
```
dat <- dat.assink2016
```

### assume that the effect sizes within studies are correlated with rho=0.6
```
V <- vcalc(vi, cluster=study, obs=esid, data=dat, rho=0.6)
```

### split V matrix into list of sub-matrices
```
Vs <- blsplit(V, cluster=dat$study)
Vs[1:2]
lapply(Vs[1:2], cov2cor)
```

### illustrate the use of the fun and args arguments
```
blsplit(V, cluster=dat$study, cov2cor)[1:2]
blsplit(V, cluster=dat$study, round, 3)[1:2]
```

---

**blup**  
Best Linear Unbiased Predictions for 'rma.uni' Objects

Description
The function computes best linear unbiased predictions (BLUPs) of the study-specific true effect sizes or outcomes by combining the fitted values based on the fixed effects and the estimated contributions of the random effects for objects of class "rma.uni". Corresponding standard errors and prediction interval bounds are also provided.

Usage
```
blup(x, ...)
```

## S3 method for class 'rma.uni'
```
blup(x, level, digits, transf, targs, ...)
```
### Arguments

- **x**: An object of class "rma.uni".
- **level**: Numeric value between 0 and 100 to specify the prediction interval level. If unspecified, the default is to take the value from the object.
- **digits**: Optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
- **transf**: Optional argument to specify a function to transform the predicted values and interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.
- **targs**: Optional arguments needed by the function specified under transf.
- **...**: Other arguments.

### Value

An object of class "list.rma". The object is a list containing the following components:

- **pred**: Predicted values.
- **se**: Corresponding standard errors.
- **pi.lb**: Lower bound of the prediction intervals.
- **pi.ub**: Upper bound of the prediction intervals.
- **...**: Some additional elements/values.

The object is formatted and printed with the print function. To format the results as a data frame, one can use the as.data.frame function.

### Note

For best linear unbiased predictions of only the random effects, see ranef.

For predicted/fitted values that are based only on the fixed effects of the model, see fitted and predict.

For conditional residuals (the deviations of the observed effect sizes or outcomes from the BLUPs), see rstandard.rma.uni with type="conditional".

Equal-effects models do not contain random study effects. The BLUPs for these models will therefore be equal to the fitted values, that is, those obtained with fitted and predict.

When using the transf argument, the transformation is applied to the predicted values and the corresponding interval bounds. The standard errors are then set equal to NA and are omitted from the printed output.

By default, a standard normal distribution is used to construct the prediction intervals. When the model was fitted with test="t" or test="knha", then a t-distribution with \( k - p \) degrees of freedom is used.

To be precise, it should be noted that the function actually computes empirical BLUPs (eBLUPs), since the predicted values are a function of the estimated value of \( \tau^2 \).
Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.uni for the function to fit models for which BLUPs can be extracted.
predict.rma and fitted.rma for functions to compute the predicted/fitted values based only on the fixed effects and ranef.rma.uni for a function to compute the BLUPs based only on the random effects.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### meta-analysis of the log risk ratios using a random-effects model
res <- rma(yi, vi, data=dat)

### BLUPs of the true risk ratios for each study
blup(res, transf=exp)

### illustrate shrinkage of BLUPs towards the (estimated) population average
res <- rma(yi, vi, data=dat)
blups <- blup(res)$pred
plot(NA, NA, xlim=c(.8,2.4), ylim=c(-2,0.5), pch=19,
     xaxt="n", bty="n", xlab="", ylab="Log Risk Ratio")
segments(rep(1,13), dat$yi, rep(2,13), blups, col="darkgray")
points(rep(1,13), dat$yi, pch=19)
points(rep(2,13), blups, pch=19)
axis(side=1, at=c(1,2), labels=c("Observed\nValues", "BLUPs"), lwd=0)
segments(0, res$beta, 2.15, res$beta, lty="dotted")
text(2.3, res$beta, substitute(hat(mu)==muhat, list(muhat=round(res$beta[[1]], 2))), cex=1)
```
Extract the Model Coefficient Table from 'permutest.rma.uni' Objects

Description

The function extracts the estimated model coefficients, corresponding standard errors, test statistics, p-values (based on the permutation tests), and confidence interval bounds from objects of class "permutest.rma.uni".

Usage

```r
## S3 method for class 'permutest.rma.uni'
coef(object, ...)  
```

Arguments

- `object`: an object of class "permutest.rma.uni".
- `...`: other arguments.

Value

A data frame with the following elements:

- `estimate`: estimated model coefficient(s).
- `se`: corresponding standard error(s).
- `zval`: corresponding test statistic(s).
- `pval`: p-value(s) based on the permutation test(s).
- `ci.lb`: lower bound of the (permutation-based) confidence interval(s).
- `ci.ub`: upper bound of the (permutation-based) confidence interval(s).

When the model was fitted with test="t" or test="knha", then zval is called tval in the data frame that is returned by the function.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

`permutest.rma.uni` for the function to conduct permutation tests and `rma.uni` for the function to fit models for which permutation tests can be conducted.
Examples

```r
## calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

## fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

## carry out permutation test
## Not run:
set.seed(1234) # for reproducibility
sav <- permutest(res)
coef(sav)

## End(Not run)
```

`coef.rma`

`Extract the Model Coefficients and Coefficient Table from 'rma' and 'summary.rma' Objects`

Description

The `coef` function extracts the estimated model coefficients from objects of class "rma". For objects of class "summary.rma", the model coefficients, corresponding standard errors, test statistics, p-values, and confidence interval bounds are extracted.

Usage

```r
## S3 method for class 'rma'
coef(object, ...)
## S3 method for class 'summary.rma'
coef(object, ...)
```

Arguments

- `object`: an object of class "rma" or "summary.rma".
- `...`: other arguments.

Value

Either a vector with the estimated model coefficient(s) or a data frame with the following elements:

- `estimate`: estimated model coefficient(s).
- `se`: corresponding standard error(s).
- `zval`: corresponding test statistic(s).
- `pval`: corresponding p-value(s).
- `ci.lb`: corresponding lower bound of the confidence interval(s).
ci.ub corresponding upper bound of the confidence interval(s).

When the model was fitted with `test="t"` or `test="knha"`, then `zval` is called `tval` in the data frame that is returned by the function.

### Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

### References


### See Also

`rma.uni`, `rma.mh`, `rma.peto`, `rma.glmm`, and `rma.mv` for functions to fit models for which model coefficients/tables can be extracted.

### Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### extract model coefficients
coef(res)

### extract model coefficient table
coef(summary(res))
```

---

### Description

The function computes confidence intervals for the model coefficients and/or other parameters in the model.

### Usage

```r
### S3 method for class 'rma.uni'
confint(object, parm, level, fixed=FALSE, random=TRUE, type, digits, transf, targs, verbose=FALSE, control, ...)

### S3 method for class 'rma.mh'
confint(object, parm, level, digits, transf, targs, ...)```
## S3 method for class 'rma.peto'
confint(object, parm, level, digits, transf, targs, ...)

## S3 method for class 'rma.glmm'
confint(object, parm, level, digits, transf, targs, ...)

## S3 method for class 'rma.mv'
confint(object, parm, level, fixed=FALSE, sigma2, tau2, rho, gamma2, phi,
       digits, transf, targs, verbose=FALSE, control, ...)

## S3 method for class 'rma.uni.selmodel'
confint(object, parm, level, fixed=FALSE, tau2, delta,
       digits, transf, targs, verbose=FALSE, control, ...)

## S3 method for class 'rma.ls'
confint(object, parm, level, fixed=FALSE, alpha,
       digits, transf, targs, verbose=FALSE, control, ...)

Arguments

- **object**: an object of class "rma.uni", "rma.mh", "rma.peto", "rma.mv", "rma.uni.selmodel", or "rma.ls". The method is not yet implemented for objects of class "rma.glmm".
- **parm**: this argument is here for compatibility with the generic function `confint`, but is (currently) ignored.
- **fixed**: logical to specify whether confidence intervals for the model coefficients should be returned.
- **random**: logical to specify whether a confidence interval for the amount of (residual) heterogeneity should be returned.
- **type**: optional character string to specify the method to use for computing the confidence interval for the amount of (residual) heterogeneity (either "QP", "GENQ", or "PL").
- **sigma2**: integer to specify for which $\sigma^2$ parameter a confidence interval should be obtained.
- **tau2**: integer to specify for which $\tau^2$ parameter a confidence interval should be obtained.
- **rho**: integer to specify for which $\rho$ parameter the confidence interval should be obtained.
- **gamma2**: integer to specify for which $\gamma^2$ parameter a confidence interval should be obtained.
- **phi**: integer to specify for which $\phi$ parameter a confidence interval should be obtained.
- **delta**: integer to specify for which $\delta$ parameter a confidence interval should be obtained.
- **alpha**: integer to specify for which $\alpha$ parameter a confidence interval should be obtained.
level
	numeric value between 0 and 100 to specify the confidence interval level. If unspecified, the default is to take the value from the object.

digits

optional integer to specify the number of decimal places to which the results should be rounded. If unspecified, the default is to take the value from the object.

transf

optional argument to specify a function to transform the model coefficients and interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

targs

optional arguments needed by the function specified under transf.

verbose

logical to specify whether output should be generated on the progress of the iterative algorithms used to obtain the confidence intervals (the default is FALSE). See ‘Details’.

control

list of control values for the iterative algorithms. If unspecified, default values are defined inside the function. See ‘Note’.

... other arguments.

Details

Confidence intervals for the model coefficients can be obtained by setting fixed=TRUE and are simply the usual Wald-type intervals (which are also shown when printing the fitted object).

Other parameter(s) for which confidence intervals can be obtained depend on the model object:

- For objects of class "rma.uni" obtained with the rma.uni function, a confidence interval for the amount of (residual) heterogeneity (i.e., \( \tau^2 \)) can be obtained by setting random=TRUE (which is the default). The interval is obtained iteratively either via the Q-profile method or via the generalized Q-statistic method (Hartung and Knapp, 2005; Viechtbauer, 2007; Jackson, 2013; Jackson et al., 2014). The latter is automatically used when the model was fitted with method="GENQ" or method="GENQM", the former is used in all other cases. Either method provides an exact confidence interval for \( \tau^2 \) in random- and mixed-effects models. The square root of the interval bounds is also returned for easier interpretation. Confidence intervals for \( I^2 \) and \( H^2 \) are also provided (Higgins & Thompson, 2002). Since \( I^2 \) and \( H^2 \) are just monotonic transformations of \( \tau^2 \) (for details, see print), the confidence intervals for \( I^2 \) and \( H^2 \) are also exact. One can also set type="PL" to obtain a profile likelihood confidence interval for \( \tau^2 \) (and corresponding CIs for \( I^2 \) and \( H^2 \)), which would be more consistent with the use of ML/REML estimation, but is not exact (see ‘Note’).

- For objects of class "rma.mv" obtained with the rma.mv function, confidence intervals are obtained by default for all (non-fixed) variance and correlation components of the model. Alternatively, one can use the sigma2, tau2, rho, gamma2, or phi arguments to specify for which variance/correlation parameter a confidence interval should be obtained. Only one of these arguments can be used at a time. A single integer is used to specify the number of the parameter. The function provides profile likelihood confidence intervals for these parameters. It is a good idea to examine the corresponding profile likelihood plots (via the profile function) to make sure that the bounds obtained are sensible.

- For selection model objects of class "rma.uni.selmodel" obtained with the selmodel function, confidence intervals are obtained by default for \( \tau^2 \) (for models where this is an estimated parameter) and all (non-fixed) selection model parameters. Alternatively, one can choose to
obtain a confidence interval only for \( \tau^2 \) by setting \( \text{tau2=TRUE} \) or for one of the selection model parameters by specifying its number via the \text{delta} \ argument. The function provides profile likelihood confidence intervals for these parameters. It is a good idea to examine the corresponding profile likelihood plots (via the \text{profile} \ function) to make sure that the bounds obtained are sensible.

- For location-scale model objects of class "rma.ls" obtained with the \text{rma.uni} \ function, confidence intervals are obtained by default for all (non-fixed) scale parameters. Alternatively, one can choose to obtain a confidence interval for one of the scale parameters by specifying its number via the \text{alpha} \ argument. The function provides profile likelihood confidence intervals for these parameters. It is a good idea to examine the corresponding profile likelihood plots (via the \text{profile} \ function) to make sure that the bounds obtained are sensible.

The methods used to find confidence intervals for these parameters are iterative and require the use of the \text{uniroot} \ function. By default, the desired accuracy (\text{tol}) is set equal to \( \text{.Machine}$double.eps^0.25 \) and the maximum number of iterations (\text{maxiter}) to 1000. These values can be adjusted with \text{control=list(tol=value, maxiter=value)} \, but the defaults should be adequate for most purposes. If \text{verbose=TRUE}, output is generated on the progress of the iterative algorithms. This is especially useful when model fitting is slow, in which case finding the confidence interval bounds can also take considerable amounts of time.

When using the \text{uniroot} \ function, one must also set appropriate end points of the interval to be searched for the confidence interval bounds. The function tries to set some sensible defaults for the end points, but it may happen that the function is only able to determine that a bound is below/above a certain limit (this is indicated in the output accordingly with \( < \) or \( > \) signs). It can also happen that the model cannot be fitted or does not converge especially at the extremes of the interval to be searched. This will result in missing (NA) bounds and corresponding warnings. It may then be necessary to adjust the end points manually (see ‘Note’).

Finally, it is also possible that the lower and upper confidence interval bounds for a variance component both fall below zero. Since both bounds then fall outside of the parameter space, the confidence interval then consists of the null/empty set. Alternatively, one could interpret this as a confidence interval with bounds \([0,0]\) or as indicating ‘highly/overly homogeneous’ data.

**Value**

An object of class "confint.rma". The object is a list with either one or two elements (named \text{fixed} and \text{random}) with the following elements:

- \text{estimate} \: estimate of the model coefficient, variance/correlation component, or selection model parameter.
- \text{ci.lb} \: lower bound of the confidence interval.
- \text{ci.ub} \: upper bound of the confidence interval.

When obtaining confidence intervals for multiple components, the object is a list of class "list.confint.rma", where each element is a "confint.rma" object as described above.

The results are formatted and printed with the \text{print} \ function. To format the results as a data frame, one can use the \text{as.data.frame} \ function.
When computing a CI for $\tau^2$ for objects of class "rma.uni", the estimate of $\tau^2$ will usually fall within the CI bounds provided by the Q-profile method. However, this is not guaranteed. Depending on the method used to estimate $\tau^2$ and the width of the CI, it can happen that the CI does not actually contain the estimate. Using the empirical Bayes or Paule-Mandel estimator of $\tau^2$ when fitting the model (i.e., using method="EB" or method="PM") usually ensures that the estimate of $\tau^2$ falls within the CI (for method="PM", this is guaranteed). When method="GENQ" was used to fit the model, the corresponding CI obtained via the generalized Q-statistic method also usually contains the estimate $\tau^2$ (for method="GENQM", this is guaranteed). When using ML/REML estimation, the profile likelihood CI (obtained when setting type="PL") is guaranteed to contain the estimate of $\tau^2$.

When computing a CI for $\tau^2$ for objects of class "rma.uni", the end points of the interval to be searched for the CI bounds are $[0, 100]$ (or, for the upper bound, ten times the estimate of $\tau^2$, whichever is greater). The upper bound should be large enough for most cases, but can be adjusted with control=list(tau2.max=value). One can also adjust the lower end point with control=list(tau2.min=value). You should only play around with this value if you know what you are doing.

For objects of class "rma.mv", the function provides profile likelihood CIs for the variance/correlation parameters in the model. For variance components, the lower end point of the interval to be searched is set to 0 and the upper end point to the larger of 10 and 100 times the value of the component. For correlations, the function tries to set the lower end point to a sensible default depending on the type of variance structure chosen, while the upper end point is set to 1. One can adjust the lower and/or upper end points with control=list(vc.min=value, vc.max=value). Also, the function tries to adjust the lower/upper end points when the model does not converge at these extremes (the end points are then moved closer to the estimated value of the component). The total number of tries for setting/adjusting the end points in this manner is determined via control=list(eptries=value), with the default being 10 tries.

For objects of class "rma.uni.selmodel" or "rma.ls", the function also sets some sensible defaults for the end points of the interval to be searched for the CI bounds (of the $\tau^2$, $\delta$, and $\alpha$ parameter(s)). One can again adjust the end points and the number of retries (as described above) with control=list(vc.min=value, vc.max=value, eptries=value).

The Q-profile and generalized Q-statistic methods are both exact under the assumptions of the random- and mixed-effects models (i.e., normally distributed observed and true effect sizes or outcomes and known sampling variances). In practice, these assumptions are usually only approximately true, turning CIs for $\tau^2$ also into approximations. Profile likelihood CIs are not exact by construction and rely on the asymptotic behavior of the likelihood ratio statistic, so they may be inaccurate in small samples, but they are inherently consistent with the use of ML/REML estimation.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

**References**

## confint.rma


### See Also

`rma.uni`, `rma.mh`, `rma.peto`, `rma.glmm`, `rma.mv`, and `selmodel.rma.uni` for functions to fit models for which confidence intervals can be computed.

`profile.rma.uni`, `profile.rma.mv`, and `profile.rma.uni.selmodel` for functions to create profile likelihood plots corresponding to profile likelihood confidence intervals.

### Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### meta-analysis of the log risk ratios using a random-effects model
res <- rma(yi, vi, data=dat, method="REML")

### confidence interval for the total amount of heterogeneity
confint(res)

### mixed-effects model with absolute latitude in the model
res <- rma(yi, vi, mods = ~ ablat, data=dat)

### confidence interval for the residual amount of heterogeneity
confint(res)

### multilevel random-effects model
res <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat.konstantopoulos2011)

### profile plots and confidence intervals for the variance components
## Not run:
par(mfrow=c(2,1))
profile(res, sigma2=1, steps=40, cline=TRUE)
sav <- confint(res, sigma2=1)
sav
```
abline(v=sav$random[1,2:3], lty="dotted")
profile(res, sigma2=2, steps=40, cline=TRUE)
sav <- confint(res, sigma2=2)
sav
abline(v=sav$random[1,2:3], lty="dotted")

## End(Not run)

### multivariate parameterization of the model
res <- rma.mv(yi, vi, random = ~ school | district, data=dat.konstantopoulos2011)

### profile plots and confidence intervals for the variance component and correlation
## Not run:
par(mfrow=c(2,1))
profile(res, tau2=1, steps=40, cline=TRUE)
sav <- confint(res, tau2=1)
sav
abline(v=sav$random[1,2:3], lty="dotted")
profile(res, rho=1, steps=40, cline=TRUE)
sav <- confint(res, rho=1)
sav
abline(v=sav$random[1,2:3], lty="dotted")

## End(Not run)

---

**contrmat**

*Construct Contrast Matrix for Two-Group Comparisons*

**Description**

The function constructs a matrix that indicates which two groups have been contrasted against each other in each row of a dataset.

**Usage**

```r
contrmat(data, grp1, grp2, last, shorten=FALSE, minlen=2, check=TRUE, append=TRUE)
```

**Arguments**

- **data**: a data frame in wide format.
- **grp1**: either the name (given as a character string) or the position (given as a single number) of the first group variable in the data frame.
- **grp2**: either the name (given as a character string) or the position (given as a single number) of the second group variable in the data frame.
- **last**: optional character string to specify which group will be placed in the last column of the matrix (must be one of the groups in the group variables). If not given, the most frequently occurring second group is placed last.
shorten: logical to specify whether the variable names corresponding to the group names should be shortened (the default is FALSE).

minlen: integer to specify the minimum length of the shortened variable names (the default is 2).

check: logical to specify whether the variables names should be checked to ensure that they are syntactically valid variable names and if not, they are adjusted (by make.names) so that they are (the default is TRUE).

append: logical to specify whether the contrast matrix should be appended to the data frame specified via the data argument (the default is TRUE). If append=FALSE, only the contrast matrix is returned.

Details

The function can be used to construct a matrix that indicates which two groups have been contrasted against each other in each row of a data frame (with 1 for the first group, -1 for the second group, and 0 otherwise).

The grp1 and grp2 arguments are used to specify the group variables in the dataset (either as character strings or as numbers indicating the column positions of these variables in the dataset). Optional argument last is used to specify which group will be placed in the last column of the matrix.

If shorten=TRUE, the variable names corresponding to the group names are shortened (to at least minlen; the actual length might be longer to ensure uniqueness of the variable names).

The examples below illustrate the use of this function.

Value

A matrix with as many variables as there are groups.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also
to.wide for a function to create ‘wide’ format datasets.

Examples

### restructure to wide format
dat <- dat.senn2013
dat <- dat[c(1,4,3,2,5,6)]
dat <- to.wide(dat, study="study", grp="treatment", ref="placebo", grpvars=4:6)
cumul

### add contrast matrix
dat <- contrmat(dat, grp1="treatment.1", grp2="treatment.2")
dat

### data in long format
dat <- dat.hasselblad1998
dat

### restructure to wide format
dat <- to.wide(dat, study="study", grp="trt", ref="no_contact", grpvars=6:7)
dat

### add contrast matrix
dat <- contrmat(dat, grp1="trt.1", grp2="trt.2", shorten=TRUE, minlen=3)
dat

cumul

Cumulative Meta-Analysis for 'rma' Objects

Description

The functions repeatedly fit the specified model, adding one study at a time to the model.

Usage

cumul(x, ...)

## S3 method for class 'rma.uni'
cumul(x, order, digits, transf, targs, progbar=FALSE, ...)

## S3 method for class 'rma.mh'
cumul(x, order, digits, transf, targs, progbar=FALSE, ...)

## S3 method for class 'rma.peto'
cumul(x, order, digits, transf, targs, progbar=FALSE, ...)

Arguments

x

an object of class "rma.uni", "rma.mh", or "rma.peto".

order

optional argument to specify a variable based on which the studies will be ordered for the cumulative meta-analysis.

digits

optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

transf

optional argument to specify a function to transform the model coefficients and interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.
The function `cumul` takes optional arguments needed by the function specified under `transf`. It also includes a progress bar to specify whether a progress bar should be shown (the default is `FALSE`). Other arguments can also be included.

### Details

For "rma.uni" objects, the model specified via `x` must be a model without moderators (i.e., either an equal- or a random-effects model). If argument `order` is not specified, the studies are added according to their order in the original dataset.

When a variable is specified for `order`, the variable is assumed to be of the same length as the original dataset that was used in the model fitting (and if the `data` argument was used in the original model fit, the variable will be searched for within this data frame first). Any subsetting and removal of studies with missing values that was applied during the model fitting is also automatically applied to the variable specified via the `order` argument. See ‘Examples’.

### Value

An object of class `c("list.rma","cumul.rma")`. The object is a list containing the following components:

- `estimate` estimated (average) outcomes.
- `se` corresponding standard errors.
- `zval` corresponding test statistics.
- `pval` corresponding p-values.
- `ci.lb` lower bounds of the confidence intervals.
- `ci.ub` upper bounds of the confidence intervals.
- `Q` test statistics for the test of heterogeneity.
- `Qp` corresponding p-values.
- `tau2` estimated amount of heterogeneity (only for random-effects models).
- `I2` values of $I^2$.
- `H2` values of $H^2$.
- ... other arguments.

When the model was fitted with `test="t"` or `test="knha"`, then `zval` is called `tval` in the object that is returned by the function.

The object is formatted and printed with the `print` function. To format the results as a data frame, one can use the `as.data.frame` function. A forest plot showing the results from the cumulative meta-analysis can be obtained with `forest`. Alternatively, `plot` can also be used to visualize the results.

### Note

When using the `transf` option, the transformation is applied to the estimated coefficients and the corresponding interval bounds. The standard errors are then set equal to `NA` and are omitted from the printed output.
**cumul**

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

**References**


**See Also**

`forest.cumul.rma` for a function to draw cumulative forest plots and `plot.cumul.rma` for a different visualization of the cumulative results.

**Examples**

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)

### cumulative meta-analysis (in the order of publication year)
cumul(res, transf=exp, order=year)

### meta-analysis of the (log) risk ratios using the Mantel-Haenszel method
res <- rma.mh(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

cumul(res, order=year)
cumul(res, order=year, transf=TRUE)

### meta-analysis of the (log) odds ratios using Peto's method
res <- rma.peto(ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

cumul(res, order=year)
cumul(res, order=year, transf=TRUE)

### make first log risk ratio missing and fit model without study 2; then the
### variable specified via 'order' should still be of the same length as the
### original dataset; subsetting and removal of studies with missing values is
### automatically done by the cumul() function

dat$yi[1] <- NA
res <- rma(yi, vi, data=dat, subset=-2)
cumul(res, transf=exp, order=year)
```
**dfround**

*Round Variables in a Data Frame*

**Description**

Function to round the numeric variables in a data frame.

**Usage**

dfround(x, digits)

**Arguments**

- **x**
  a data frame.
- **digits**
  either a single integer or a numeric vector of the same length as there are columns in \( x \).

**Details**

A simple convenience function to round the numeric variables in a data frame, possibly to different numbers of digits. Hence, **digits** can either be a single integer (which will then be used to round all numeric variables to the specified number of digits) or a numeric vector (of the same length as there are columns in \( x \)) to specify the number of digits to which each variable should be rounded.

Non-numeric variables are skipped. If **digits** is a vector, some arbitrary value (or NA) can be specified for those variables.

**Value**

Returns the data frame with variables rounded as specified.

**Author(s)**

Wolfgang Viechtbauer \(<wvb@metafor-project.org>\) [https://www.metafor-project.org](https://www.metafor-project.org)

**Examples**

dat <- dat.bcg
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat)
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)
coef(summary(res))
dfround(coef(summary(res)), digits=c(2,3,2,3,2,2))
escalc

Calculate Effect Sizes and Outcome Measures

Description

The function can be used to calculate various effect sizes or outcome measures (and the corresponding sampling variances) that are commonly used in meta-analyses.

Usage

```
escalc(measure, ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i,
       m1i, m2i, sd1i, sd2i, xi, mi, ri, ti, sdi, r2i, ni, yi, vi, sei,
       data, slab, subset, include,
       add=1/2, to="only0", drop00=FALSE, vtype="LS",
       var.names=c("yi","vi"), add.measure=FALSE,
       append=TRUE, replace=TRUE, digits, ...)
```

Arguments

- `measure`: a character string to specify which effect size or outcome measure should be calculated. See 'Details' for possible options and how the data needed to compute the selected effect size or outcome measure should then be specified.
- `ai`: vector to specify the $2 \times 2$ table frequencies (upper left cell).
- `bi`: vector to specify the $2 \times 2$ table frequencies (upper right cell).
- `ci`: vector to specify the $2 \times 2$ table frequencies (lower left cell).
- `di`: vector to specify the $2 \times 2$ table frequencies (lower right cell).
- `n1i`: vector to specify the group sizes or row totals (first group/row).
- `n2i`: vector to specify the group sizes or row totals (second group/row).
- `x1i`: vector to specify the number of events (first group).
- `x2i`: vector to specify the number of events (second group).
- `t1i`: vector to specify the total person-times (first group).
- `t2i`: vector to specify the total person-times (second group).
- `m1i`: vector to specify the means (first group or time point).
- `m2i`: vector to specify the means (second group or time point).
- `sd1i`: vector to specify the standard deviations (first group or time point).
- `sd2i`: vector to specify the standard deviations (second group or time point).
- `xi`: vector to specify the frequencies of the event of interest.
- `mi`: vector to specify the frequencies of the complement of the event of interest or the group means.
- `ri`: vector to specify the raw correlation coefficients.
- `ti`: vector to specify the total person-times.
sd1 vector to specify the standard deviations.
ri vector to specify the $R^2$ values.
ni vector to specify the sample/group sizes.
yi vector to specify the observed effect sizes or outcomes.
vi vector to specify the corresponding sampling variances.
sei vector to specify the corresponding standard errors.
data optional data frame containing the variables given to the arguments above.
slab optional vector with labels for the studies.
subset optional (logical or numeric) vector to specify the subset of studies that will be included in the data frame returned by the function.
include optional (logical or numeric) vector to specify the subset of studies for which the measure should be calculated. See the ‘Value’ section for more details.
add a non-negative number to specify the amount to add to zero cells, counts, or frequencies. See ‘Details’.
to a character string to specify when the values under add should be added (either "all", "only0", "if0all", or "none"). See ‘Details’.
drop00 logical to specify whether studies with no cases/events (or only cases) in both groups should be dropped when calculating the observed effect sizes or outcomes. See ‘Details’.
vtype a character string to specify the type of sampling variances to calculate. See ‘Details’.
var.names character string with two elements to specify the name of the variable for the observed effect sizes or outcomes and the name of the variable for the corresponding sampling variances (the defaults are "yi" and "vi").
add.measure logical to specify whether a variable should be added to the data frame (with default name "measure") that indicates the type of outcome measure computed. When using this option, var.names can have a third element to change this variable name.
append logical to specify whether the data frame provided via the data argument should be returned together with the observed effect sizes or outcomes and corresponding sampling variances (the default is TRUE).
replace logical to specify whether existing values for yi and vi in the data frame should be replaced. Only relevant when append=TRUE and the data frame already contains the yi and vi variables. If replace=TRUE (the default), all of the existing values will be overwritten. If replace=FALSE, only NA values will be replaced. See the ‘Value’ section for more details.
digits optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. Note that the values are stored without rounding in the returned object. See also here for further details on how to control the number of digits in the output.
...
other arguments.
Details

Before a meta-analysis can be conducted, the relevant results from each study must be quantified in such a way that the resulting values can be further aggregated and compared. Depending on (a) the goals of the meta-analysis, (b) the design and types of studies included, and (c) the information provided therein, one of the various effect sizes or outcome measures described below may be appropriate for the meta-analysis and can be computed with the escalc function.

The measure argument is a character string to specify the outcome measure that should be calculated (see below for the various options), arguments ai through ni are then used to specify the information needed to calculate the various measures (depending on the chosen outcome measure, different arguments need to be specified), and data can be used to specify a data frame containing the variables given to the previous arguments. The add, to, and drop00 arguments may be needed when dealing with frequency or count data that may need special handling when some of the frequencies or counts are equal to zero (see below for details). Finally, the vtype argument is used to specify how the sampling variances should be estimated (again, see below for details).

To provide a structure to the various effect sizes or outcome measures that can be calculated with the escalc function, we can distinguish between measures that are used to:

- contrast two independent (either experimentally created or naturally occurring) groups,
- describe the direction and strength of the association between two variables,
- summarize some characteristic or attribute of individual groups, or
- quantify change within a single group or the difference between two matched pairs samples.

Furthermore, where appropriate, we can further distinguish between measures that are applicable when the characteristic, response, or dependent variable assessed in the individual studies is:

- a dichotomous (binary) variable (e.g., remission versus no remission),
- a count of events per time unit (e.g., number of migraines per year),
- a quantitative variable (e.g., amount of depression as assessed by a rating scale).

Outcome Measures for Two-Group Comparisons:

In many meta-analyses, the goal is to synthesize the results from studies that compare or contrast two groups. The groups may be experimentally defined (e.g., a treatment and a control group created via random assignment) or may occur naturally (e.g., men and women, employees working under high- versus low-stress conditions, people exposed to some environmental risk factor versus those not exposed).

Measures for Dichotomous Variables:

In various fields (such as the health and medical sciences), the response variable measured is often dichotomous (binary), so that the data from a study comparing two different groups can be expressed in terms of a $2 \times 2$ table, such as:

<table>
<thead>
<tr>
<th></th>
<th>outcome 1</th>
<th>outcome 2</th>
<th>total</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>$a_i$</td>
<td>$b_i$</td>
<td>$n_{1i}$</td>
</tr>
<tr>
<td>group 2</td>
<td>$c_i$</td>
<td>$d_i$</td>
<td>$n_{2i}$</td>
</tr>
</tbody>
</table>

where $a_i$, $b_i$, $c_i$, and $d_i$ denote the cell frequencies (i.e., the number of people falling into a particular category) and $n_{1i}$ and $n_{2i}$ are the row totals (i.e., the group sizes).
For example, in a set of randomized clinical trials, group 1 and group 2 may refer to the treatment and placebo/control group, respectively, with outcome 1 denoting some event of interest (e.g., death, complications, failure to improve under the treatment) and outcome 2 its complement. Similarly, in a set of cohort studies, group 1 and group 2 may denote those who engage in and those who do not engage in a potentially harmful behavior (e.g., smoking), with outcome 1 denoting the development of a particular disease (e.g., lung cancer) during the follow-up period. Finally, in a set of case-control studies, group 1 and group 2 may refer to those with the disease (i.e., cases) and those free of the disease (i.e., controls), with outcome 1 denoting, for example, exposure to some environmental risk factor in the past and outcome 2 non-exposure. Note that in all of these examples, the stratified sampling scheme fixes the row totals (i.e., the group sizes) by design.

A meta-analysis of studies reporting results in terms of $2 \times 2$ tables can be based on one of several different outcome measures, including the risk ratio (also called the relative risk), the odds ratio, the risk difference, and the arcsine square root transformed risk difference (e.g., Fleiss & Berlin, 2009, Rücker et al., 2009). For any of these outcome measures, one needs to specify the cell frequencies via the $a_i$, $b_i$, $c_i$, and $d_i$ arguments (or alternatively, one can use the $a_i$, $c_i$, $n_{1i}$, and $n_{2i}$ arguments).

The options for the `measure` argument are then:

- "RR" for the log risk ratio,
- "OR" for the log odds ratio,
- "RD" for the risk difference,
- "AS" for the arcsine square root transformed risk difference (Rücker et al., 2009),
- "PETO" for the log odds ratio estimated with Peto’s method (Yusuf et al., 1985).

Note that the log is taken of the risk ratio and the odds ratio, which makes these outcome measures symmetric around 0 and yields corresponding sampling distributions that are closer to normality. Also, when multiplied by 2, the arcsine square root transformed risk difference is actually identical to Cohen’s $h$ (Cohen, 1988).

If the $2 \times 2$ table is not available (or cannot be reconstructed) for a study, but measures such as the odds ratio and corresponding confidence interval bounds are reported, one can easily transform these values into the corresponding log odds ratio and sampling variance directly. See here for an illustration/discussion of this.

Cell entries with a zero count can be problematic, especially for the risk ratio and the odds ratio. Adding a small constant to the cells of the $2 \times 2$ tables is a common solution to this problem. When `to="only0"` (the default), the value of `add` (the default is $1/2$; but see ‘Note’) is added to each cell of those $2 \times 2$ tables with at least one cell equal to 0. When `to="all"`, the value of `add` is added to each cell of all $2 \times 2$ tables. When `to="if0all"`, the value of `add` is added to each cell of all $2 \times 2$ tables, but only when there is at least one $2 \times 2$ table with a zero cell. Setting `to="none"` or `add=0` has the same effect: No adjustment to the observed table frequencies is made. Depending on the outcome measure and the data, this may lead to division by zero (when this occurs, the resulting value is recoded to NA). Also, studies where $a_i=c_i=0$ or $b_i=d_i=0$ may be considered to be uninformative about the size of the effect and dropping such studies has sometimes been recommended (Higgins et al., 2019). This can be done by setting `drop00=TRUE`. The values for such studies will then be set to NA.


Assuming that the dichotomous outcome is actually a dichotomized version of the responses on an underlying quantitative scale, it is also possible to estimate the standardized mean difference
based on $2 \times 2$ table data, using either the probit transformed risk difference or a transformation of the odds ratio (e.g., Cox & Snell, 1989; Chinn, 2000; Hasselblad & Hedges, 1995; Sánchez-Meca et al., 2003). The options for the measure argument are then:

- "PBIT" for the **probit transformed risk difference** as an estimate of the standardized mean difference,
- "OR2DN" for the **transformed odds ratio** as an estimate of the standardized mean difference (assuming normal distributions),
- "OR2DL" for the **transformed odds ratio** as an estimate of the standardized mean difference (assuming logistic distributions).

The probit transformation assumes that the responses on the underlying quantitative scale are normally distributed. There are two versions of the odds ratio transformation, the first also assuming normal distributions within the two groups, while the second assumes that the responses within groups follow logistic distributions.

A dataset corresponding to data of this type is provided in `dat.gibson2002`.

**Measures for Event Counts:**

In medical and epidemiological studies comparing two different groups (e.g., treated versus untreated patients, exposed versus unexposed individuals), results are sometimes reported in terms of event counts (i.e., the number of events, such as strokes or myocardial infarctions) over a certain period of time. Data of this type are also referred to as 'person-time data'. Assume that the studies report data in the form:

\[
\begin{array}{c|c|c}
\text{number of events} & \text{total person-time} \\
\hline
\text{group 1} & x_1i & t_{1i} \\
\text{group 2} & x_2i & t_{2i} \\
\end{array}
\]

where $x_1i$ and $x_2i$ denote the number of events in the first and the second group, respectively, and $t_{1i}$ and $t_{2i}$ the corresponding total person-times at risk. Often, the person-time is measured in years, so that $t_{1i}$ and $t_{2i}$ denote the total number of follow-up years in the two groups.

This form of data is fundamentally different from what was described in the previous section, since the total follow-up time may differ even for groups of the same size and the individuals studied may experience the event of interest multiple times. Hence, different outcome measures than the ones described in the previous section need to be considered when data are reported in this format. These include the incidence rate ratio, the incidence rate difference, and the square root transformed incidence rate difference (Bagos & Nikolopoulos, 2009; Rothman et al., 2008). For any of these outcome measures, one needs to specify the total number of events via the $x_1i$ and $x_2i$ arguments and the corresponding total person-time values via the $t_{1i}$ and $t_{2i}$ arguments.

The options for the measure argument are then:

- "IRR" for the **log incidence rate ratio**,
- "IRD" for the **incidence rate difference**,
- "IRSD" for the **square root transformed incidence rate difference**.

Note that the log is taken of the incidence rate ratio, which makes this outcome measure symmetric around 0 and yields a corresponding sampling distribution that is closer to normality.

Studies with zero events in one or both groups can be problematic, especially for the incidence rate ratio. Adding a small constant to the number of events is a common solution to this problem. When `to="only0"` (the default), the value of `add` (the default is $1/2$; but see 'Note') is added to $x_{1i}$ and $x_{2i}$ only in the studies that have zero events in one or both groups. When `to="all"`,
the value of \( \text{add} \) is added to \( x_{1i} \) and \( x_{2i} \) in all studies. When \( \text{to} = \"if0all\" \), the value of \( \text{add} \) is added to \( x_{1i} \) and \( x_{2i} \) in all studies, but only when there is at least one study with zero events in one or both groups. Setting \( \text{to} = \"none\" \) or \( \text{add}=0 \) has the same effect: No adjustment to the observed number of events is made. Depending on the outcome measure and the data, this may lead to division by zero (when this occurs, the resulting value is recoded to NA). Like for \( 2 \times 2 \) table data, studies where \( x_{1i}=x_{2i}=0 \) may be considered to be uninformative about the size of the effect and dropping such studies has sometimes been recommended. This can be done by setting \( \text{drop00}=\text{TRUE} \). The values for such studies will then be set to NA.

Datasets corresponding to data of this type are provided in \texttt{dat.hart1999} and \texttt{dat.nielweise2008}.

**Measures for Quantitative Variables:**

When the response or dependent variable assessed in the individual studies is measured on some quantitative scale, it is customary to report certain summary statistics, such as the mean and standard deviation of the observations. The data layout for a study comparing two groups with respect to such a variable is then of the form:

<table>
<thead>
<tr>
<th></th>
<th>mean</th>
<th>standard deviation</th>
<th>group size</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>( m_{1i} )</td>
<td>( sd_{1i} )</td>
<td>( n_{1i} )</td>
</tr>
<tr>
<td>group 2</td>
<td>( m_{2i} )</td>
<td>( sd_{2i} )</td>
<td>( n_{2i} )</td>
</tr>
</tbody>
</table>

where \( m_{1i} \) and \( m_{2i} \) are the observed means of the two groups, \( sd_{1i} \) and \( sd_{2i} \) are the observed standard deviations, and \( n_{1i} \) and \( n_{2i} \) denote the number of individuals in each group. Again, the two groups may be experimentally created (e.g., a treatment and control group based on random assignment) or naturally occurring (e.g., men and women). In either case, the raw mean difference, the standardized mean difference, and the (log transformed) ratio of means (also called the log 'response ratio') are useful outcome measures when meta-analyzing studies of this type.

The options for the \texttt{measure} argument are then:

- \texttt{"MD"} for the *raw mean difference* (e.g., Borenstein, 2009),
- \texttt{"SMD"} for the *standardized mean difference* (Hedges, 1981),
- \texttt{"SMDH"} for the *standardized mean difference* with heteroscedastic population variances in the two groups (Bonett, 2008, 2009),
- \texttt{"SMD1"} for the *standardized mean difference* where the mean difference is divided by the standard deviation of the second group (and \texttt{"SMD1H"} for the same but with heteroscedastic population variances),
- \texttt{"ROM"} for the *log transformed ratio of means* (Hedges et al., 1999; Lajeunesse, 2011).

The standardized mean difference is computed with \( (m_{1i} - m_{2i}) / \text{sdpi} \). For \texttt{measure="SMD"}, \( \text{sdpi} = sqrt(((n_{1i}-1) * sd_{1i}^2 + (n_{2i}-1) * sd_{2i}^2) / (n_{1i} + n_{2i} - 2)) \) is the pooled standard deviation of the two groups. For \texttt{measure="SMDH"}, \( \text{sdpi} = sqrt((sd_{1i}^2 + sd_{2i}^2) / 2) \) is the square root of the average variance. Finally, for \texttt{measure="SMD1"} and \texttt{measure="SMD1H"}, we simply use \( \text{sdpi} = sd_{2i} \) (note: for \texttt{measure="SMD1"}, only \( sd_{2i} \) needs to be specified and \( sd_{1i} \) is ignored).

For \texttt{measure="SMD"}, the positive bias in the standardized mean difference (i.e., in a Cohen's \( d \) value) is automatically corrected for within the function, yielding Hedges' \( g \) (Hedges, 1981). Similarly, the same bias correction is applied for \texttt{measure="SMDH"} (Bonett, 2009), \texttt{measure="SMD1"} (Hedges, 1981), and \texttt{measure="SMD1H"}.

For \texttt{measure="ROM"}, the log is taken of the ratio of means, which makes this outcome measure symmetric around 0 and yields a corresponding sampling distribution that is closer to normality.
Hence, this measure cannot be computed when \( m_{1i} \) and \( m_{2i} \) have opposite signs (in fact, this measure is only meant to be used for ratio scale measurements, where both means should be positive anyway).

For measure="SMD", if the means and standard deviations are unknown for some studies, but the standardized mean differences (Cohen’s \( d \) values) are directly available (e.g., if they are reported in those studies), then these can be specified via argument \( d_i \). Also, if the t-statistics from an independent samples t-test is available for some studies (or the corresponding p-values, which can be easily transformed into the t-statistics), one can specify those values via argument \( t_i \), which are then transformed into the corresponding standardized mean differences within the function. See here for an illustration/discussion of this.

For measure="MD", one can choose between vtype="LS" (the default) and vtype="HO". The former computes the sampling variances without assuming homoscedasticity (i.e., that the true variances of the measurements are the same in group 1 and group 2 within each study), while the latter assumes homoscedasticity (equations 12.5 and 12.3 in Borenstein, 2009, respectively). For measure="SMD", one can choose between vtype="LS" (the default) for the usual large-sample approximation to compute the sampling variances (equation 8 in Hedges, 1982), vtype="UB" to compute unbiased estimates of the sampling variances (equation 9 in Hedges, 1983), vtype="LS2" to compute the sampling variances as described in Borenstein (2009) (i.e., equation 12.17), and vtype="AV" to compute the sampling variances with the usual large-sample approximation but plugging the sample-size weighted average of the Hedges’ \( g \) values into the equation. The same choices also apply to measure="SMD1". For measure="ROM", one can choose between vtype="LS" (the default) for the usual large-sample approximation to compute the sampling variances (equation 1 in Hedges et al., 1999), vtype="H0" to compute the sampling variances assuming homoscedasticity (the unnumbered equation after equation 1 in Hedges et al., 1999), vtype="AV" to compute the sampling variances assuming homoscedasticity of the coefficient of variation within each group across studies, and vtype="AVHO" to compute the sampling variances assuming homoscedasticity of the coefficient of variation for both groups across studies.

Datasets corresponding to data of this type are provided in dat.normand1999 and dat.curtis1998.

It is also possible to transform standardized mean differences into log odds ratios (e.g., Cox & Snell, 1989; Chinn, 2000; Hasselblad & Hedges, 1995; Sánchez-Meca et al., 2003). The options for the measure argument are then:

- "D2ORN" for the transformed standardized mean difference as an estimate of the log odds ratio (assuming normal distributions),
- "D2ORL" for the transformed standardized mean difference as an estimate of the log odds ratio (assuming logistic distributions).

Both of these transformations provide an estimate of the log odds ratio, the first assuming that the responses within the two groups are normally distributed, while the second assumes that the responses follow logistic distributions.

A dataset illustrating the combined analysis of standardized mean differences and probit transformed risk differences is provided in dat.gibson2002.

Finally, interest may also be focused on differences between the two groups with respect to their variability. Here, the (log transformed) ratio of the coefficient of variation of the two groups (also called the coefficient of variation ratio) can be a useful measure (Nakagawa et al., 2015). If focus is solely on the variability of the measurements within the two groups, then the (log transformed) ratio of the standard deviations (also called the variability ratio) can be used (Nakagawa et al., 2015). For the latter, one only needs to specify \( sd_{1i} \), \( sd_{2i} \), \( n_{1i} \), and \( n_{2i} \). The options for the measure argument are:
• "CVR" for the log transformed coefficient of variation ratio,
• "VR" for the log transformed variability ratio.

Note that a slight bias correction is applied for both of these measures (Nakagawa et al., 2015). Also, the sampling variance for measure="CVR" is computed as given by equation 12 in Nakagawa et al. (2015), but without the ‘−2ρ...’ terms, since for normally distributed data (which we assume here) the mean and variance (and transformations thereof) are independent.

Outcome Measures for Variable Association:
Meta-analyses are often used to synthesize studies that examine the direction and strength of the association between two variables measured concurrently and/or without manipulation by experimenters. In this section, a variety of outcome measures will be discussed that may be suitable for a meta-analyses with this purpose. We can distinguish between measures that are applicable when both variables are measured on quantitative scales, when both variables measured are dichotomous, and when the two variables are of mixed types.

Measures for Two Quantitative Variables:
The (Pearson or product-moment) correlation coefficient quantifies the direction and strength of the (linear) relationship between two quantitative variables and is therefore frequently used as the outcome measure for meta-analyses. Two alternative measures are a bias-corrected version of the correlation coefficient and Fisher’s r-to-z transformed correlation coefficient.

For these measures, one needs to specify ri, the vector with the raw correlation coefficients, and ni, the corresponding sample sizes. The options for the measure argument are then:
• "COR" for the raw correlation coefficient,
• "UCOR" for the raw correlation coefficient corrected for its slight negative bias (based on equation 2.3 in Olkin & Pratt, 1958),
• "ZCOR" for Fisher’s r-to-z transformed correlation coefficient (Fisher, 1921).

For measure="COR" and measure="UCOR", one can choose between vtype="LS" (the default) for the usual large-sample approximation to compute the sampling variances (i.e., plugging the (biased-corrected) correlation coefficients into equation 12.27 in Borenstein, 2009), vtype="UB" to compute unbiased estimates of the sampling variances (see Hedges, 1989, but using the exact equation instead of the approximation), and vtype="AV" to compute the sampling variances with the usual large-sample approximation but plugging the sample-size weighted average of the (bias-corrected) correlation coefficients into the equation.

Datasets corresponding to data of this type are provided in dat.mcdaniel1994 and dat.molloy2014.

For meta-analyses involving multiple correlations extracted from the same sample, see also the rcalc function.

Measures for Two Dichotomous Variables:
When the goal of a meta-analysis is to examine the relationship between two dichotomous variables, the data for each study can again be presented in the form of a 2 × 2 table, except that there may not be a clear distinction between the grouping variable and the outcome variable. Moreover, the table may be a result of cross-sectional (i.e., multinomial) sampling, where none of the table margins (except the total sample size) are fixed by the study design.

The phi coefficient and the odds ratio are commonly used measures of association for 2 × 2 table data (e.g., Fleiss & Berlin, 2009). The latter is particularly advantageous, as it is directly comparable to values obtained from stratified sampling (as described earlier). Yule’s Q and Yule’s Y (Yule, 1912) are additional measures of association for 2 × 2 table data (although they are not typically used in meta-analyses). Finally, assuming that the two dichotomous variables are actually dichotomized versions of the responses on two underlying quantitative scales (and
assuming that the two variables follow a bivariate normal distribution), it is also possible to estimate the correlation between the two variables using the tetrachoric correlation coefficient (Pearson, 1900; Kirk, 1973).

For any of these outcome measures, one needs to specify the cell frequencies via the $a_i$, $b_i$, $c_i$, and $d_i$ arguments (or alternatively, one can use the $a_i$, $c_i$, $n_{1i}$, and $n_{2i}$ arguments). The options for the measure argument are then:

- "OR" for the log odds ratio,
- "PHI" for the phi coefficient,
- "YUQ" for Yule's Q (Yule, 1912),
- "YUY" for Yule's Y (Yule, 1912),
- "RTET" for the tetrachoric correlation coefficient.

Tables with one or more zero counts are handled as described earlier. For measure="PHI", one must indicate via vtype="ST" or vtype="CS" whether the data for the studies were obtained using stratified or cross-sectional (i.e., multinomial) sampling, respectively (it is also possible to specify an entire vector for the vtype argument in case the sampling scheme differed for the various studies).

A dataset corresponding to data of this type is provided in data.bourassa1996.

### Measures for Mixed Variable Types:

Finally, we can consider outcome measures that can be used to describe the relationship between two variables, where one variable is dichotomous and the other variable measures some quantitative characteristic. In that case, it is likely that study authors again report summary statistics, such as the mean and standard deviation of the measurements within the two groups (defined by the dichotomous variable). Based on this information, one can compute the point-biserial correlation coefficient (Tate, 1954) as a measure of association between the two variables. If the dichotomous variable is actually a dichotomized version of the responses on an underlying quantitative scale (and assuming that the two variables follow a bivariate normal distribution), it is also possible to estimate the correlation between the two variables using the biserial correlation coefficient (Pearson, 1909; Soper, 1914; Jacobs & Viechtbauer, 2017).

Here, one again needs to specify $m_1i$ and $m_2i$ for the observed means of the two groups, $sd_1i$ and $sd_2i$ for the observed standard deviations, and $n_{1i}$ and $n_{2i}$ for the number of individuals in each group. The options for the measure argument are then:

- "RPB" for the point-biserial correlation coefficient,
- "RBIS" for the biserial correlation coefficient.

For measure="RPB", one must indicate via vtype="ST" or vtype="CS" whether the data for the studies were obtained using stratified or cross-sectional (i.e., multinomial) sampling, respectively (it is also possible to specify an entire vector for the vtype argument in case the sampling scheme differed for the various studies).

### Outcome Measures for Individual Groups:

In this section, outcome measures will be described which may be useful when the goal of a meta-analysis is to synthesize studies that characterize some property of individual groups. We will again distinguish between measures that are applicable when the characteristic of interest is a dichotomous variable, when the characteristic represents an event count, or when the characteristic assessed is a quantitative variable.

#### Measures for Dichotomous Variables:

A meta-analysis may be conducted to aggregate studies that provide data about individual groups with respect to a dichotomous dependent variable. Here, one needs to specify $x_i$ and $n_i$, denoting the number of individuals experiencing the event of interest and the total number of
individuals within each study, respectively. Instead of specifying $n_i$, one can use $m_i$ to specify the number of individuals that do not experience the event of interest. The options for the measure argument are then:

- "PR" for the raw proportion,
- "PLN" for the log transformed proportion,
- "PLO" for the logit transformed proportion (i.e., log odds),
- "PAS" for the arcsine square root transformed proportion (i.e., the angular transformation),
- "PFT" for the Freeman-Tukey double arcsine transformed proportion (Freeman & Tukey, 1950).

Zero cell entries can be problematic for certain outcome measures. When to="only0" (the default), the value of add (the default is 1/2; but see ‘Note’) is added to $x_i$ and $m_i$ only for studies where $x_i$ or $m_i$ is equal to 0. When to="all", the value of add is added to $x_i$ and $m_i$ in all studies. When to="if0all", the value of add is added in all studies, but only when there is at least one study with a zero value for $x_i$ or $m_i$. Setting to="none" or add=0 has the same effect: No adjustment to the observed values is made. Depending on the outcome measure and the data, this may lead to division by zero (when this occurs, the resulting value is recoded to NA).

Datasets corresponding to data of this type are provided in dat.pritz1997 and dat.debruin2009.

Measures for Event Counts:

Various measures can be used to characterize individual groups when the dependent variable assessed is an event count. Here, one needs to specify $x_i$ and $t_i$, denoting the number of events that occurred and the total person-times at risk, respectively. The options for the measure argument are then:

- "IR" for the raw incidence rate,
- "IRLN" for the log transformed incidence rate,
- "IRS" for the square root transformed incidence rate,
- "IRFT" for the Freeman-Tukey transformed incidence rate (Freeman & Tukey, 1950).

Measures "IR" and "IRLN" can also be used when meta-analyzing standardized incidence ratios (SIRs), where the observed number of events is divided by the expected number of events. In this case, arguments $x_i$ and $t_i$ are used to specify the observed and expected number of events in the studies. Since SIRs are not symmetric around 1, it is usually more appropriate to meta-analyze the log transformed SIRs (i.e., using measure "IRLN"), which are symmetric around 0.

Studies with zero events can be problematic, especially for the log transformed incidence rate. Adding a small constant to the number of events is a common solution to this problem. When to="only0" (the default), the value of add (the default is 1/2; but see ‘Note’) is added to $x_i$ only in the studies that have zero events. When to="all", the value of add is added to $x_i$ in all studies. When to="if0all", the value of add is added to $x_i$ in all studies, but only when there is at least one study with zero events. Setting to="none" or add=0 has the same effect: No adjustment to the observed number of events is made. Depending on the outcome measure and the data, this may lead to division by zero (when this occurs, the resulting value is recoded to NA).

Measures for Quantitative Variables:

The goal of a meta-analysis may also be to characterize individual groups, where the response, characteristic, or dependent variable assessed in the individual studies is measured on some quantitative scale. In the simplest case, the raw mean for the quantitative variable is reported.
for each group, which then becomes the observed outcome for the meta-analysis. Here, one needs to specify \( m_i \), \( sdi \), and \( n_i \) for the observed means, the observed standard deviations, and the sample sizes, respectively. For ratio scale measurements, the log transformed mean or the log transformed coefficient of variation (with bias correction) may also be of interest (Nakagawa et al., 2015). If focus is solely on the variability of the measurements, then the log transformed standard deviation (with bias correction) is a useful measure (Nakagawa et al., 2015; Raudenbush & Bryk, 1987). Here, one only needs to specify \( sdi \) and \( n_i \).

The options for the `measure` argument are:

- "MN" for the raw mean,
- "MNLN" for the log transformed mean,
- "CVLN" for the log transformed coefficient of variation,
- "SDLN" for the log transformed standard deviation.

Note that \( sdi \) is used to specify the standard deviations of the observed values of the response, characteristic, or dependent variable and not the standard errors of the means. Also, the sampling variance for `measure="CVLN"` is computed as given by equation 27 in Nakagawa et al. (2015), but without the ‘\(-2 \rho \ldots\)' term, since for normally distributed data (which we assume here) the mean and variance (and transformations thereof) are independent.

**Outcome Measures for Change or Matched Pairs:**

A more complicated situation arises when the purpose of the meta-analysis is to assess the amount of change within individual groups (e.g., before and after a treatment or under two different treatments) or when dealing with matched pairs designs.

**Measures for Dichotomous Variables:**

For dichotomous variables, the data for a study of this type gives rise to a paired \( 2 \times 2 \) table, which is of the form:

\[
\begin{array}{cccc}
\text{trt 2} & \text{outcome 1} & \text{trt 2} & \text{outcome 2} \\
\text{trt 1} & ai & bi \\
\text{trt 1} & ci & di \\
\end{array}
\]

where \( ai, bi, ci, \) and \( di \) denote the cell frequencies. Note that ‘trt1’ and ‘trt2’ may be applied to a single group of subjects or to matched pairs of subjects. Also, ‘trt1’ and ‘trt2’ might refer to two different time points (e.g., before and after a treatment). In any case, the data from such a study can be rearranged into a marginal table of the form:

\[
\begin{array}{cc}
\text{outcome 1} & \text{outcome 2} \\
\text{trt 1} & ai+bi & ci+di \\
\text{trt 2} & ai+ci & bi+di \\
\end{array}
\]

which is of the same form as a \( 2 \times 2 \) table that would arise in a study comparing/contrasting two independent groups.

The options for the `measure` argument that will compute outcome measures based on the marginal table are:

- "MPRR" for the matched pairs marginal log risk ratio,
- "MPOR" for the matched pairs marginal log odds ratio,
- "MPRD" for the matched pairs marginal risk difference.

See Becker and Balagtas (1993), Curtin et al. (2002), Elbourne et al. (2002), Fagerland et al.
May and Johnson (1997), Newcombe (1998), Stedman et al. (2011), and Zou (2007) for discussions of these measures.

The options for the `measure` argument that will compute outcome measures based on the paired table are:

- "MPORC" for the *conditional log odds ratio*,
- "MPORC" for the *conditional log odds ratio* estimated with Peto’s method.

See Curtin et al. (2002) and Zou (2007) for discussions of these measures.

If only marginal tables are available, then another possibility is to compute the marginal log odds ratios based on these table directly. However, for the correct computation of the sampling variances, the correlations (phi coefficients) from the paired tables must be known (or 'guestimated'). To use this approach, set `measure="MPORM"` and use argument `ri` to specify the correlation coefficients.

**Measures for Quantitative Variables:**

When the response or dependent variable assessed in the individual studies is measured on some quantitative scale, the raw mean change, standardized versions thereof, or the (log transformed) ratio of means (log response ratio) can be used as outcome measures (Becker, 1988; Gibbons et al., 1993; Lajeunesse, 2011; Morris, 2000). Here, one needs to specify `m1i` and `m2i`, the observed means at the two measurement occasions, `sd1i` and `sd2i` for the corresponding observed standard deviations, `ri` for the correlation between the measurements at the two measurement occasions, and `ni` for the sample size. The options for the `measure` argument are then:

- "MC" for the *raw mean change*,
- "SMCC" for the *standardized mean change* using change score standardization (Gibbons et al., 1993),
- "SMCR" for the *standardized mean change* using raw score standardization (Becker, 1988),
- "SMCRH" for the *standardized mean change* using raw score standardization with heteroscedastic population variances at the two measurement occasions (Bonett, 2008),
- "ROMC" for the *log transformed ratio of means* (Lajeunesse, 2011).

See also Morris and DeShon (2002) for a thorough discussion of the difference between the change score measures.

A few notes about the change score measures. In practice, one often has a mix of information available from the individual studies to compute these measures. In particular, if `m1i` and `m2i` are unknown, but the raw mean change is directly reported in a particular study, then one can set `m1i` to that value and `m2i` to 0 (making sure that the raw mean change was computed as `m1i-m2i` within that study and not the other way around). Also, for the raw mean change ("MC") or the standardized mean change using change score standardization ("SMCC"), if `sd1i`, `sd2i`, and `ri` are unknown, but the standard deviation of the change scores is directly reported, then one can set `sd1i` to that value and both `sd2i` and `ri` to 0. Finally, for the standardized mean change using raw score standardization ("SMCR"), argument `sd2i` is actually not needed, as the standardization is only based on `sd1i` (Becker, 1988; Morris, 2000), which is usually the pre-test standard deviation (if the post-test standard deviation should be used, then set `sd1i` to that).

Note that all of these measures are also applicable for matched-pairs designs (subscripts 1 and 2 then simply denote the first and second group that are formed by the matching).

Finally, interest may also be focused on differences in the variability of the measurements at the two measurement occasions (or between the two matched groups). Here, the (log transformed) ratio of the coefficient of variation (also called the coefficient of variation ratio) can be a useful measure (Nakagawa et al., 2015). If focus is solely on the variability of the measurements, then the (log transformed) ratio of the standard deviations (also called the variability ratio) can be
used (Nakagawa et al., 2015). For the latter, one only needs to specify sd1i, sd2i, ni, and ri. The options for the measure argument are:
- "CVRC" for the log transformed coefficient of variation ratio,
- "VRC" for the log transformed variability ratio.

The definitions of these measures are the same as given in Nakagawa et al. (2015) but are here computed for two sets of dependent measurements. Hence, the computation of the sampling variances are adjusted to take the correlation between the measurements into consideration.

**Other Outcome Measures for Meta-Analyses:**

Other outcome measures are sometimes used for meta-analyses that do not directly fall into the categories above. These are described in this section.

**Cronbach’s alpha and Transformations Thereof:**

Meta-analytic methods can also be used to aggregate Cronbach’s alpha values from multiple studies. This is usually referred to as a ‘reliability generalization meta-analysis’ (Vacha-Haase, 1998). Here, one needs to specify ai, mi, and ni for the observed alpha values, the number of items/replications/parts of the measurement instrument, and the sample sizes, respectively. One can either directly analyze the raw Cronbach’s alpha values or transformations thereof (Bonett, 2002, 2010; Hakstian & Whalen, 1976). The options for the measure argument are then:
- "ARAW" for raw alpha values,
- "AHW" for transformed alpha values (Hakstian & Whalen, 1976),
- "ABT" for transformed alpha values (Bonett, 2002).

Note that the transformations implemented here are slightly different from the ones described by Hakstian and Whalen (1976) and Bonett (2002). In particular, for "AHW", the transformation \(1 - (1 - \alpha)^{1/3}\) is used, while for "ABT", the transformation \(-\ln(1 - \alpha)\) is used. This ensures that the transformed values are monotonically increasing functions of \(\alpha\).

A dataset corresponding to data of this type is provided in dat.bonett2010.

**Partial and Semi-Partial Correlations:**

Aloe and Becker (2012), Aloe and Thompson (2013), and Aloe (2014) describe the use of partial and semi-partial correlation coefficients as a method for meta-analyzing the results from regression models (when the focus is on a common regression coefficient of interest across studies). To compute these measures, one needs to specify ti for the test statistics (i.e., t-tests) of the regression coefficient of interest, ni for the sample sizes of the studies, mi for the number of predictors in the regression models, and r2i for the \(R^2\) value of the regression models (the latter is only needed when measure="SPCOR"). The options for the measure argument are then:
- "PCOR" for the partial correlation coefficient,
- "ZPCOR" for Fisher’s r-to-z transformed partial correlation coefficient,
- "SPCOR" for the semi-partial correlation coefficient.

Note that the sign of the (semi-)partial correlation coefficients is determined based on the signs of the values specified via the ti argument. Also, the Fisher transformation can only be applied to partial correlation coefficient, not semi-partial coefficients.

A dataset corresponding to data of this type is provided in dat.aloe2013.

**Relative Excess Heterozygosity:**

Ziegler et al. (2011) describe the use of meta-analytic methods to examine deviations from Hardy-Weinberg equilibrium across multiple studies. The relative excess heterozygosity (REH) is the proposed measure for such a meta-analysis, which can be computed by setting measure="REH". Here, one needs to specify ai for the number of individuals with homozygous dominant alleles,
bi for the number of individuals with heterozygous alleles, and ci for the number of individuals with homozygous recessive alleles.

Note that the log is taken of the REH values, which makes this outcome measure symmetric around 0 and yields a corresponding sampling distribution that is closer to normality.

A dataset corresponding to data of this type is provided in dat.frank2008.

Converting a Data Frame to an 'escalc' Object:
The function can also be used to convert a regular data frame to an ‘escalc’ object. One simply sets the measure argument to one of the options described above (or to measure="GEN" for a generic outcome measure not further specified) and passes the observed effect sizes or outcomes via the yi argument and the corresponding sampling variances via the vi argument (or the standard errors via the sei argument).

Value
An object of class c("escalc","data.frame"). The object is a data frame containing the following components:

yi observed effect sizes or outcomes.
vi corresponding sampling variances.

If append=TRUE and a data frame was specified via the data argument, then yi and vi are appended to this data frame. Note that the var.names argument actually specifies the names of these two variables (yi and vi are the defaults).

If the data frame already contains two variables with names as specified by the var.names argument, the values for these two variables will be overwritten when replace=TRUE (which is the default). By setting replace=FALSE, only values that are NA will be replaced.

The subset argument can be used to select the studies that will be included in the data frame returned by the function. On the other hand, the include argument simply selects for which studies the measure will be computed (if it shouldn’t be computed for all of them).

The object is formatted and printed with the print function. The summary function can be used to obtain confidence intervals for the individual outcomes. See methods.escalc for some additional method functions for "escalc" objects.

With the aggregate function, one can aggregate multiple effect sizes or outcomes belonging to the same study (or some other clustering variable) into a single combined effect size or outcome.

Note
The variable names specified under var.names should be syntactically valid variable names. If necessary, they are adjusted so that they are.

Although the default value for add is 1/2, for certain measures the use of such a bias correction makes little sense and for these measures, the function internally sets add=0. This applies to the following measures: "AS", "PHI", "RTET", "IRSO", "PAS", "PFT", "IRS", and "IRFT". One can still force the use of the bias correction by explicitly setting the add argument to some non-zero value.

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References


Pearson, K. (1909). On a new method of determining correlation between a measured character A, and a character B, of which only the percentage of cases wherein B exceeds (or falls short of) a given intensity is recorded for each grade of A. *Biometrika*, 7(1/2), 96–105. [https://doi.org/10.1093/biomet/7.1-2.96](https://doi.org/10.1093/biomet/7.1-2.96)


See Also

- `print.escalc` and `summary.escalc` for the print and summary methods.
- `rma.uni` and `rma.mv` for model fitting functions that can take the calculated effect sizes or outcomes (and the corresponding sampling variances) as input.
- `rma.mh`, `rma.peto`, and `rma.glmm` for model fitting functions that take similar inputs.
Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)
dat

### suppose that for a particular study, yi and vi are known (i.e., have
### already been calculated) but the 2x2 table counts are not known; with
### replace=FALSE, the yi and vi values for that study are not replaced
dat[1:12,10:11] <- NA
dat[13,4:7] <- NA
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat, replace=FALSE)
dat

### illustrate difference between 'subset' and 'include' arguments
escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, subset=1:6)
escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, include=1:6)

### convert a regular data frame to an 'escalc' object
### dataset from Lipsey & Wilson (2001), Table 7.1, page 130
dat <- data.frame(id = c(100, 308, 1596, 2479, 9021, 9028, 161, 172, 537, 7049),
                  yi = c(-0.33, 0.32, 0.39, 0.31, 0.17, 0.64, -0.33, 0.15, -0.02, 0.00),
                  vi = c(0.084, 0.035, 0.017, 0.034, 0.072, 0.117, 0.102, 0.093, 0.012, 0.067),
                  random = c(0, 0, 0, 0, 0, 0, 1, 1, 1, 1),
                  intensity = c(7, 3, 7, 5, 7, 7, 4, 4, 5, 6))
dat <- escalc(measure="SMD", yi=yi, vi=vi, data=dat, slab=paste("Study ID: ", id), digits=3)
dat
```

---

**fitstats**

*Fit Statistics and Information Criteria for 'rma' Objects*

**Description**

Functions to extract the log-likelihood, deviance, AIC, BIC, and AICc values from objects of class "rma".

**Usage**

```r
fitstats(object, ...)
```

### S3 method for class 'rma'
```r
fitstats(object, ..., REML)
```

### S3 method for class 'rma'
```r
logLik(object, REML, ...)
```

### S3 method for class 'rma'
```r
deviance(object, REML, ...)
```

### S3 method for class 'rma'
```r
```
AIC(object, ..., k=2, correct=FALSE)
## S3 method for class 'rma'
BIC(object, ...)

**Arguments**

- **object**: an object of class "rma".
- **...**: optionally more fitted model objects (only for fitstats(), AIC(), and BIC()).
- **REML**: logical to specify whether the regular or restricted likelihood function should be used to obtain the fit statistics and information criteria. Defaults to the method of estimation used (i.e., TRUE if object was fitted with method="REML" and FALSE otherwise).
- **k**: numeric value to specify the penalty per parameter to use. The default (k=2) is the classical AIC. See AIC for more details.
- **correct**: logical to specify whether the regular (default) or corrected (i.e., AICc) should be extracted.

**Value**

For fitstats, a data frame with the (restricted) log-likelihood, deviance, AIC, BIC, and AICc values for each model passed to the function.

For logLik, an object of class "logLik", providing the (restricted) log-likelihood of the model evaluated at the estimated coefficient(s).

For deviance, a numeric value with the corresponding deviance.

For AIC and BIC, either a numeric value with the corresponding AIC, AICc, or BIC or a data frame with rows corresponding to the models and columns representing the number of parameters in the model (df) and the AIC, AICc, or BIC.

**Note**

Variance components in the model (e.g., $\tau^2$ in random/mixed-effects models fitted with rma.uni) are counted as additional parameters in the calculation of the AIC, BIC, and AICc. Also, the fixed effects are counted as parameters in the calculation of the AIC, BIC, and AICc even when using REML estimation.

**Author(s)**

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**References**

See Also

rma.uni, rma.mh, rma.peto, rma.glmm, and rma.mv for functions to fit models for which fit statistics and information criteria can be extracted.

anova.rma for a function to conduct likelihood ratio tests.

Examples

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### random-effects model
res1 <- rma(yi, vi, data=dat, method="ML")

### mixed-effects model with absolute latitude and publication year as moderators
res2 <- rma(yi, vi, mods = ~ ablat + year, data=dat, method="ML")

### compare fit statistics
fitstats(res1, res2)

### log-likelihoods
logLik(res1)
logLik(res2)

### deviances
deviance(res1)
deviance(res2)

### AIC, AICc, and BIC values
AIC(res1, res2)
AIC(res1, res2, correct=TRUE)
BIC(res1, res2)

---

fitted.rma

Fitted Values for 'rma' Objects

Description

The function computes the fitted values for objects of class "rma".

Usage

## S3 method for class 'rma'
fitted(object, ...)

Arguments

object

an object of class "rma".

... (optional)

other arguments.
The **forest** function can be used to create forest plots.

### Description

The **forest** function can be used to create forest plots.

### Usage

```r
forest(x, ...)
```
Arguments

x either an object of class "rma", a vector with the observed effect sizes or outcomes, or an object of class "cumul.rma". See ‘Details’.

Details

Currently, methods exist for three types of situations.

In the first case, object x is a fitted model object coming from the rma.uni, rma.mh, or rma.peto functions. The corresponding method is then forest.rma.

Alternatively, object x can be a vector with observed effect sizes or outcomes. The corresponding method is then forest.default.

Finally, object x can be an object coming from the cumul.rma.uni, cumul.rma.mh, or cumul.rma.peto functions. The corresponding method is then forest.cumul.rma.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

forest.rma, forest.default, and forest.cumul.rma for the specific method functions.

forecumul.rma  Forest Plots (Method for 'cumul.rma' Objects)

Description

Function to create forest plots for objects of class "cumul.rma".

Usage

```r
# S3 method for class 'cumul.rma'
forest(x, annotate=TRUE, header=FALSE,
       xlim, ylim, at, steps=5,
       level=x$level, reline=0, digits=2L, width,
       xlab, ilab, ilab.xpos, ilab.pos,
       transf, atransf, targs, rows,
       efac=1, pch, psize, col,
       lty, fonts, cex, cex.lab, cex.axis, ...)
```
Arguments

- **x**: an object of class "cumul.rma" obtained with `cumul`.
- **annotate**: logical to specify whether annotations should be added to the plot (the default is TRUE).
- **header**: logical to specify whether column headings should be added to the plot (the default is FALSE). Can also be a character vector to specify the left and right headings (or only the left one).
- **xlim**: horizontal limits of the plot region. If unspecified, the function tries to set the horizontal plot limits to some sensible values.
- **alim**: the x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
- **olim**: optional argument to specify observation/outcome limits. If unspecified, no limits are used.
- **ylim**: the y-axis limits of the plot. If unspecified, the function tries to set the y-axis limits to some sensible values.
- **at**: position of the x-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.
- **steps**: the number of tick marks for the x-axis (the default is 5). Ignored when the positions are specified via the `at` argument.
- **level**: numeric value between 0 and 100 to specify the confidence interval level (the default is to take the value from the object).
- **refline**: numeric value to specify the location of the vertical ‘reference’ line (the default is 0). The line can be suppressed by setting this argument to NA.
- **digits**: integer to specify the number of decimal places to which the tick mark labels of the x-axis and the annotations should be rounded (the default is 2L). Can also be a vector of two integers, the first to specify the number of decimal places for the annotations, the second for the x-axis labels. When specifying an integer (e.g., 2L), trailing zeros after the decimal mark are dropped for the x-axis labels. When specifying a numeric value (e.g., 2), trailing zeros are retained.
- **width**: optional integer to manually adjust the width of the columns for the annotations (either a single integer or a vector of the same length as the number of annotation columns).
- **xlab**: title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
- **ilab**: optional vector, matrix, or data frame providing additional information about the studies that should be added to the plot.
- **ilab.xpos**: numeric vector to specify the horizontal position(s) of the variable(s) given via `ilab` (must be specified if `ilab` is specified).
- **ilab.pos**: integer(s) (either 1, 2, 3, or 4) to specify the alignment of the vector(s) given via `ilab` (2 means right, 4 mean left aligned). If unspecified, the default is to center the labels.
- **transf**: optional argument to specify a function to transform the estimates and confidence interval bounds (e.g., `transf=exp`; see also `transf`). If unspecified, no transformation is used.
atransf optional argument to specify a function to transform the x-axis labels and annotations (e.g., atransf=exp; see also transf). If unspecified, no transformation is used.

targs optional arguments needed by the function specified via transf or atransf.

rows optional vector to specify the rows (or more generally, the horizontal positions) for plotting the outcomes. Can also be a single value to specify the row (horizontal position) of the first outcome (the remaining outcomes are then plotted below this starting row). If unspecified, the function sets this value automatically.

efac vertical expansion factor for confidence interval limits and arrows. The default value of 1 should usually work okay. Can also be a vector of two numbers, the first for CI limits, the second for arrows.

pch plotting symbol to use for the estimates. By default, a filled square is used. See points for other options. Can also be a vector of values.

psize numeric value to specify the point sizes for the estimates (the default is 1). Can also be a vector of values.

col optional character string to specify the color to use for plotting ("black" is used by default if not specified). Can also be a vector.

lty optional character string to specify the line type for the confidence intervals. If unspecified, the function sets this to "solid" by default.

fonts optional character string to specify the font to use for the study labels, annotations, and the extra information (if specified via ilab). If unspecified, the default font is used.

cex optional character and symbol expansion factor. If unspecified, the function tries to set this to a sensible value.

cex.lab optional expansion factor for the x-axis title. If unspecified, the function tries to set this to a sensible value.

cex.axis optional expansion factor for the x-axis labels. If unspecified, the function tries to set this to a sensible value.

... other arguments.

Details

The plot shows the estimated (average) outcome with corresponding confidence interval as one study at a time is added to the analysis.

Note

The function tries to set some sensible values for the optional arguments, but it may be necessary to adjust these in certain circumstances.

The function actually returns some information about the chosen values invisibly. Printing this information is useful as a starting point to make adjustments to the plot.

If the number of studies is quite large, the labels, annotations, and symbols may become quite small and impossible to read. Stretching the plot window vertically may then provide a more readable figure (one should call the function again after adjusting the window size, so that the label/symbol...
sizes can be properly adjusted). Also, the `cex`, `cex.lab`, and `cex.axis` arguments are then useful to adjust the symbol and text sizes.

If the horizontal plot and/or x-axis limits are set manually, then the horizontal plot limits (`xlim`) must be at least as wide as the x-axis limits (`alim`). This restriction is enforced inside the function.

If the outcome measure used for creating the plot is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the `ylim` argument to enforce those limits (the observed outcomes and confidence intervals cannot exceed those bounds then).

The `lty` argument can also be a vector of two elements, the first for specifying the line type of the individual CIs ("solid" by default), the second for the line type of the horizontal line that is automatically added to the plot ("solid" by default; set to "blank" to remove it).

**Author(s)**

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**References**


**See Also**

- `forest` for an overview of the various `forest` functions.
- `cumul` for the function to create `cumul.rma` objects.

**Examples**

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat, slab=paste(author, year, sep=",", "))

### draw cumulative forest plots
x <- cumul(res, order=year)
forest(x, cex=.8, header=TRUE)
forest(x, alim=c(-2,1), cex=.8, header=TRUE)

### meta-analysis of the (log) risk ratios using the Mantel-Haenszel method
res <- rma.mh(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, slab=paste(author, year, sep=",", "))
```
### draw cumulative forest plot

```r
x <- cumul(res, order=year)
forest(x, alim=c(-2,1), cex=.8, header=TRUE)
```

---

**forest.default**

*Forest Plots (Default Method)*

#### Description

Function to create forest plots for a given set of data.

#### Usage

```r
## Default S3 method:
forest(x, vi, sei, ci.lb, ci.ub,
      annotate=TRUE, showweights=FALSE, header=FALSE,
      xlim, alim, olim, at, steps=5,
      level=95, reline=0, digits=2L, width,
      xlab, slab, ilab, ilab.xpos, ilab.pos,
      order, subset, transf, atransf, targs, rows,
      efac=1, pch, psize, plim=c(0.5,1.5), col,
      lty, fonts, cex, cex.lab, cex.axis, ...)
```

#### Arguments

- `x`: vector of length `k` with the observed effect sizes or outcomes.
- `vi`: vector of length `k` with the corresponding sampling variances.
- `sei`: vector of length `k` with the corresponding standard errors (note: only one of the two, `vi` or `sei`, needs to be specified).
- `ci.lb`: vector of length `k` with the corresponding lower confidence interval bounds. Not needed if `vi` or `sei` is specified. See ‘Details’.
- `ci.ub`: vector of length `k` with the corresponding upper confidence interval bounds. Not needed if `vi` or `sei` is specified. See ‘Details’.
- `annotate`: logical to specify whether annotations should be added to the plot (the default is `TRUE`).
- `showweights`: logical to specify whether the annotations should also include the inverse variance weights (the default is `FALSE`).
- `header`: logical to specify whether column headings should be added to the plot (the default is `FALSE`). Can also be a character vector to specify the left and right headings (or only the left one).
- `xlim`: horizontal limits of the plot region. If unspecified, the function tries to set the horizontal plot limits to some sensible values.
- `alim`: the x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
optional argument to specify observation/outcome limits. If unspecified, no limits are used.

the y-axis limits of the plot. If unspecified, the function tries to set the y-axis limits to some sensible values.

position of the x-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.

the number of tick marks for the x-axis (the default is 5). Ignored when the positions are specified via the at argument.

numeric value between 0 and 100 to specify the confidence interval level (the default is 95).

numeric value to specify the location of the vertical ‘reference’ line (the default is 0). The line can be suppressed by setting this argument to NA.

integer to specify the number of decimal places to which the tick mark labels of the x-axis and the annotations should be rounded (the default is 2L). Can also be a vector of two integers, the first to specify the number of decimal places for the annotations, the second for the x-axis labels. When specifying an integer (e.g., 2L), trailing zeros after the decimal mark are dropped for the x-axis labels. When specifying a numeric value (e.g., 2), trailing zeros are retained.

optional integer to manually adjust the width of the columns for the annotations (either a single integer or a vector of the same length as the number of annotation columns).

title for the x-axis. If unspecified, the function tries to set an appropriate axis title.

optional vector with labels for the k studies. If unspecified, the function tries to extract study labels from x and otherwise simple labels are created within the function. To suppress labels, set this argument to NA.

optional vector, matrix, or data frame providing additional information about the studies that should be added to the plot.

numeric vector to specify the horizontal position(s) of the variable(s) given via ilab (must be specified if ilab is specified).

integer(s) (either 1, 2, 3, or 4) to specify the alignment of the vector(s) given via ilab (2 means right, 4 mean left aligned). If unspecified, the default is to center the labels.

optional character string to specify how the studies should be ordered. Can also be a variable based on which the studies will be ordered. See ‘Details’.

optional (logical or numeric) vector to specify the subset of studies that should be included in the plot.

optional argument to specify a function to transform the observed outcomes and corresponding confidence interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

optional argument to specify a function to transform the x-axis labels and annotations (e.g., atransf=exp; see also transf). If unspecified, no transformation is used.
**forest.default**

**targs**
optional arguments needed by the function specified via `transf` or `atransf`.

**rows**
optional vector to specify the rows (or more generally, the horizontal positions) for plotting the outcomes. Can also be a single value to specify the row (horizontal position) of the first outcome (the remaining outcomes are then plotted below this starting row). If unspecified, the function sets this value automatically.

**efac**
vertical expansion factor for confidence interval limits and arrows. The default value of 1 should usually work okay. Can also be a vector of two numbers, the first for CI limits, the second for arrows.

**pch**
plotting symbol to use for the observed outcomes. By default, a filled square is used. See `points` for other options. Can also be a vector of values.

**psize**
optional numeric value to specify the point sizes for the observed outcomes. If unspecified, the point sizes are a function of the precision of the estimates. Can also be a vector of values.

**plim**
numeric vector of length 2 to scale the point sizes (ignored when `psize` is specified). See 'Details'.

**col**
optional character string to specify the color to use for plotting the observed outcomes ("black" is used by default if not specified). Can also be a vector.

**lty**
optional character string to specify the line type for the confidence intervals. If unspecified, the function sets this to "solid" by default.

**fonts**
optional character string to specify the font to use for the study labels, annotations, and the extra information (if specified via `ilab`). If unspecified, the default font is used.

**cex**
optional character and symbol expansion factor. If unspecified, the function tries to set this to a sensible value.

**cex.lab**
optional expansion factor for the x-axis title. If unspecified, the function tries to set this to a sensible value.

**cex.axis**
optional expansion factor for the x-axis labels. If unspecified, the function tries to set this to a sensible value.

... other arguments.

**Details**

The plot shows the observed effect sizes or outcomes with corresponding confidence intervals. To use the function, one should specify the observed outcomes (via the `x` argument) together with the corresponding sampling variances (via the `vi` argument) or with the corresponding standard errors (via the `sei` argument). Alternatively, one can specify the observed outcomes together with the corresponding confidence interval bounds (via the `ci.lb` and `ci.ub` arguments).

With the `transf` argument, the observed outcomes and corresponding confidence interval bounds can be transformed with some suitable function. For example, when plotting log odds ratios, then one could use `transf=exp` to obtain a forest plot showing the odds ratios. Alternatively, one can use the `atransf` argument to transform the x-axis labels and annotations (e.g., `atransf=exp`). See also `transf` for some other useful transformation functions in the context of a meta-analysis. The examples below illustrate the use of these arguments.

By default, the studies are ordered from top to bottom (i.e., the first study in the dataset will be placed in row $k$, the second study in row $k - 1$, and so on, until the last study, which is placed in the first row). The studies can be reordered with the `order` argument:
- **order="obs"**: the studies are ordered by the observed outcomes,
- **order="prec"**: the studies are ordered by their sampling variances.

Alternatively, it is also possible to set `order` equal to a variable based on which the studies will be ordered (see ‘Examples’).

Additional columns with information about the studies can be added to the plot via the `ilab` argument. This can either be a single variable or an entire matrix/data frame (with as many rows as there are studies in the forest plot). The `ilab.xpos` argument must then also be specified to indicate the horizontal position of the variables specified via `ilab`.

Summary estimates can be added to the plot with the `addpoly` function. See the documentation for that function for examples.

By default (i.e., when `psize` is not specified), the point sizes are a function of the precision (i.e., inverse standard errors) of the outcomes. This way, more precise estimates are visually more prominent in the plot. By making the point sizes a function of the inverse standard errors of the estimates, their areas are proportional to the inverse sampling variances, which corresponds to the weights they would receive in an equal-effects model. However, the point sizes are rescaled so that the smallest point size is `plim[1]` and the largest point size is `plim[2]`. As a result, their relative sizes (i.e., areas) no longer exactly correspond to their relative weights in such a model. If exactly relative point sizes are desired, one can set `plim[2]` to `NA`, in which case the points are rescaled so that the smallest point size corresponds to `plim[1]` and all other points are scaled accordingly. As a result, the largest point may be very large. Alternatively, one can set `plim[1]` to `NA`, in which case the points are rescaled so that the largest point size corresponds to `plim[2]` and all other points are scaled accordingly. As a result, the smallest point may be very small and essentially indistinguishable from the confidence interval line. To avoid the latter, one can also set `plim[3]`, which enforces a minimal point size.

**Note**

The function tries to set some sensible values for the optional arguments, but it may be necessary to adjust these in certain circumstances.

The function actually returns some information about the chosen values invisibly. Printing this information is useful as a starting point to make adjustments to the plot.

If the number of studies is quite large, the labels, annotations, and symbols may become quite small and impossible to read. Stretching the plot window vertically may then provide a more readable figure (one should call the function again after adjusting the window size, so that the label/symbol sizes can be properly adjusted). Also, the `cex`, `cex.lab`, and `cex.axis` arguments are then useful to adjust the symbol and text sizes.

If the horizontal plot and/or x-axis limits are set manually, then the horizontal plot limits (`xlim`) must be at least as wide as the x-axis limits (`xlim`). This restriction is enforced inside the function.

If the outcome measure used for creating the plot is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the `olim` argument to enforce those limits (the observed outcomes and confidence intervals cannot exceed those bounds then).

The `lty` argument can also be a vector of two elements, the first for specifying the line type of the individual CIs (“solid” by default), the second for the line type of the horizontal line that is automatically added to the plot (“solid” by default; set to “blank” to remove it).
Additional Arguments

There are some additional arguments that can be passed to the function via ... (hence, they cannot be abbreviated):

- **top** the amount of space to leave empty at the top of the plot (e.g., for adding headers) (the default is 3 rows).
- **annosym** optional vector of length 3 to select the left bracket, separation, and right bracket symbols for the annotations (the default is c(" ", ", ", "]"). Can also include a 4th element to adjust the look of the minus symbol, for example to use a proper minus (−) sign instead of a hyphen-minus (-).
- **textpos** optional vector of length 2 to specify the placement of the study labels and the annotations (the default is to use the horizontal limits of the plot region, i.e., the study labels to the right of xlim[1] and the annotations to the left of xlim[2]).
- **rowadj** optional vector of length 3 to vertically adjust the position of the study labels, the annotations, and the extra information (if specified via ilab). This is useful for fine-tuning the position of text added with different positional alignments (i.e., argument pos in the text function).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

References


See Also

- forest for an overview of the various forest functions and especially forest.rma for the function draw forest plots including a summary polygon.
- addpoly for a function to add polygons to forest plots.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### default forest plot of the observed log risk ratios
forest(dat$yi, dat$vi)

### the with() function can be used to avoid having to retype dat$... over and over
with(dat, forest(yi, vi))

### forest plot of the observed risk ratios (transform outcomes)
with(dat, forest(yi, vi, slab=paste(author, year, sep=" "), transf=exp,
               alim=c(0,2), steps=5, xlim=c(-2.5,4), reflation=1, cex=.9, header=TRUE))
```
### forest plot of the observed risk ratios (transformed x-axis)
with(dat, forest(yi, vi, slab=paste(author, year, sep=" ",), atransf=exp,
at=log(c(.05,.25,1,4,20)), xlim=c(-10,8), cex=.9, header=TRUE))

### forest plot of the observed risk ratios with studies ordered by the RRs
with(dat, forest(yi, vi, slab=paste(author, year, sep=" ",), atransf=exp,
at=log(c(.05,.25,1,4,20)), xlim=c(-10,8), cex=.9, header=TRUE, order="obs"))

### forest plot of the observed risk ratios with studies ordered by absolute latitude
with(dat, forest(yi, vi, slab=paste(author, year, sep=" ",), atransf=exp,
at=log(c(.05,.25,1,4,20)), xlim=c(-10,8), cex=.9, header=TRUE, order=ablat))

### see also examples for the forest.rma function

---

**forest.rma**

**Forest Plots (Method for 'rma' Objects)**

**Description**

Function to create forest plots for objects of class "rma".

**Usage**

```r
## S3 method for class 'rma'
forest(x, annotate=TRUE, addfit=TRUE, addpred=FALSE,
showweights=FALSE, header=FALSE,
xlim, alim, ylim, at, steps=5,
level=x$level, reline=0, digits=2L, width,
xlab, slab, mlab, ilab, ilab.xpos, ilab.pos,
order, transf, atransf, targs, rows,
efac=1, pch, psize, plim=c(0.5,1.5), colout,
col, border, lty, fonts, cex, cex.lab, cex.axis, ...)
```

**Arguments**

- `x` an object of class "rma".
- `annotate` logical to specify whether annotations should be added to the plot (the default is TRUE).
- `addfit` logical to specify whether the summary estimate (for models without moderators) or fitted values (for models with moderators) should be added to the plot (the default is TRUE). See ‘Details’.
- `addpred` logical to specify whether the bounds of the prediction interval should be added to the plot (the default is FALSE). See ‘Details’.
- `showweights` logical to specify whether the annotations should also include the weights given to the observed outcomes during the model fitting (the default is FALSE). See ‘Details’.
<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>header</td>
<td>logical to specify whether column headings should be added to the plot (the default is FALSE). Can also be a character vector to specify the left and right headings (or only the left one).</td>
</tr>
<tr>
<td>xlim</td>
<td>horizontal limits of the plot region. If unspecified, the function tries to set the horizontal plot limits to some sensible values.</td>
</tr>
<tr>
<td>alim</td>
<td>the x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.</td>
</tr>
<tr>
<td>olim</td>
<td>optional argument to specify observation/outcome limits. If unspecified, no limits are used.</td>
</tr>
<tr>
<td>ylim</td>
<td>the y-axis limits of the plot. If unspecified, the function tries to set the y-axis limits to some sensible values.</td>
</tr>
<tr>
<td>at</td>
<td>position of the x-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.</td>
</tr>
<tr>
<td>steps</td>
<td>the number of tick marks for the x-axis (the default is 5). Ignored when the positions are specified via the at argument.</td>
</tr>
<tr>
<td>level</td>
<td>numeric value between 0 and 100 to specify the confidence interval level (the default is to take the value from the object).</td>
</tr>
<tr>
<td>reline</td>
<td>numeric value to specify the location of the vertical ‘reference’ line (the default is 0). The line can be suppressed by setting this argument to NA.</td>
</tr>
<tr>
<td>digits</td>
<td>integer to specify the number of decimal places to which the tick mark labels of the x-axis and the annotations should be rounded (the default is 2L). Can also be a vector of two integers, the first to specify the number of decimal places for the annotations, the second for the x-axis labels. When specifying an integer (e.g., 2L), trailing zeros after the decimal mark are dropped for the x-axis labels. When specifying a numeric value (e.g., 2), trailing zeros are retained.</td>
</tr>
<tr>
<td>width</td>
<td>optional integer to manually adjust the width of the columns for the annotations (either a single integer or a vector of the same length as the number of annotation columns).</td>
</tr>
<tr>
<td>xlab</td>
<td>title for the x-axis. If unspecified, the function tries to set an appropriate axis title.</td>
</tr>
<tr>
<td>slab</td>
<td>optional vector with labels for the $k$ studies. If unspecified, the function tries to extract study labels from x or simple labels are created within the function. To suppress labels, set this argument to NA.</td>
</tr>
<tr>
<td>mlab</td>
<td>optional character string giving a label to the summary estimate from an equal- or a random-effects model. If unspecified, the label is created within the function.</td>
</tr>
<tr>
<td>ilab</td>
<td>optional vector, matrix, or data frame providing additional information about the studies that should be added to the plot.</td>
</tr>
<tr>
<td>ilab.xpos</td>
<td>numeric vector to specify the horizontal position(s) of the variable(s) given via ilab (must be specified if ilab is specified).</td>
</tr>
<tr>
<td>ilab.pos</td>
<td>integer(s) (either 1, 2, 3, or 4) to specify the alignment of the vector(s) given via ilab (2 means right, 4 mean left aligned). If unspecified, the default is to center the labels.</td>
</tr>
</tbody>
</table>
forest.rma

order optional character string to specify how the studies should be ordered. Can also be a variable based on which the studies will be ordered. See ‘Details’.

transf optional argument to specify a function to transform the observed outcomes, summary estimates, fitted values, and confidence interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

atransf optional argument to specify a function to transform the x-axis labels and annotations (e.g., atransf=exp; see also transf). If unspecified, no transformation is used.

targs optional arguments needed by the function specified via transf or atransf.

rows optional vector to specify the rows (or more generally, the horizontal positions) for plotting the outcomes. Can also be a single value to specify the row (horizontal position) of the first outcome (the remaining outcomes are then plotted below this starting row). If unspecified, the function sets this value automatically.

efac vertical expansion factor for confidence interval limits, arrows, and the symbol used to denote summary estimates. The default value of 1 should usually work okay. Can also be a vector of two numbers, the first for CI limits and arrows, the second for summary estimates. Can also be a vector of three numbers, the first for CI limits, the second for arrows, the third for summary estimates.

pch plotting symbol to use for the observed outcomes. By default, a filled square is used. See points for other options. Can also be a vector of values.

psize optional numeric value to specify the point sizes for the observed outcomes. If unspecified, the point sizes are a function of the model weights. Can also be a vector of values.

plim numeric vector of length 2 to scale the point sizes (ignored when psize is specified). See ‘Details’.

colout optional character string to specify the color to use for plotting the observed outcomes ("black" is used by default if not specified). Can also be a vector.

col optional character string to specify the color to use for the summary polygon or fitted values. If unspecified, the function sets a default color.

border optional character string to specify the color to use for the border of the summary polygon or fitted values. If unspecified, the function sets a default color.

lty optional character string to specify the line type for the confidence intervals. If unspecified, the function sets this to "solid" by default.

fonts optional character string to specify the font to use for the study labels, annotations, and the extra information (if specified via ilab). If unspecified, the default font is used.

cex optional character and symbol expansion factor. If unspecified, the function tries to set this to a sensible value.

cex.lab optional expansion factor for the x-axis title. If unspecified, the function tries to set this to a sensible value.

cex.axis optional expansion factor for the x-axis labels. If unspecified, the function tries to set this to a sensible value.

... other arguments.
Details

The plot shows the observed effect sizes or outcomes with corresponding confidence intervals. For an equal- and a random-effects model (i.e., for models without moderators), a four-sided polygon, sometimes called a summary 'diamond', is added to the bottom of the forest plot, showing the summary estimate based on the model (with the center of the polygon corresponding to the estimate and the left/right edges indicating the confidence interval limits). The col and border arguments can be used to adjust the (border) color of the polygon. Drawing of the polygon can be suppressed by setting addfit=FALSE.

For random-effects models and if addpred=TRUE, a dotted line is added to the summary polygon which indicates the (approximate) bounds of the prediction interval (the interval indicates where level % of the true outcomes are expected to fall) (Riley et al., 2011). For random-effects models of class "rma.mv" (see rma.mv) with multiple $\tau^2$ values, the addpred argument can be used to specify for which level of the inner factor the prediction interval should be provided (since the intervals differ depending on the $\tau^2$ value). If the model should also contain multiple $\gamma^2$ values, the addpred argument should then be of length 2 to specify the levels of both inner factors. See also predict.rma, which is used to compute these interval bounds.

For meta-regression models (i.e., models involving moderators), the fitted value for each study is added as a polygon to the plot. By default, the width of the polygons corresponds to the confidence interval limits for the fitted values. By setting addpred=TRUE, the width reflects the prediction interval limits. Again, the col and border arguments can be used to adjust the (border) color of the polygons. These polygons can be suppressed by setting addfit=FALSE.

With the transf argument, the observed outcomes, summary estimate, fitted values, confidence interval bounds, and prediction interval bounds can be transformed with some suitable function. For example, when plotting log odds ratios, one could use transf=exp to obtain a forest plot showing the odds ratios. Alternatively, one can use the atransf argument to transform the x-axis labels and annotations (e.g., atransf=exp). See also transf for some other useful transformation functions in the context of a meta-analysis. The examples below illustrate the use of these arguments.

By default, the studies are ordered from top to bottom (i.e., the first study in the dataset will be placed in row $k$, the second study in row $k-1$, and so on, until the last study, which is placed in the first row). The studies can be reordered with the order argument:

- order="obs": the studies are ordered by the observed outcomes,
- order="fit": the studies are ordered by the fitted values,
- order="prec": the studies are ordered by their sampling variances,
- order="resid": the studies are ordered by the size of their residuals,
- order="rstandard": the studies are ordered by the size of their standardized residuals,
- order="abs.resid": the studies are ordered by the size of their absolute residuals,
- order="abs.rstandard": the studies are ordered by the size of their absolute standardized residuals.

Alternatively, it is also possible to set order equal to a variable based on which the studies will be ordered (see ‘Examples’).

Additional columns with information about the studies can be added to the plot via the ilab argument. This can either be a single variable or an entire matrix / data frame (with as many rows as
there are studies in the forest plot). The `ilab.xpos` argument must then also be specified to indicate the horizontal position of the variables specified via `ilab`.

The figure below illustrates how the elements in a forest plot can be arranged and the meaning of some of the arguments such as `xlim`, `alim` or `at`, `ilab`, and `ilab.xpos`.

```
forest(res, addpred=TRUE, xlim=c(-16,7), at=seq(-3,2,by=1),
ilab=cbind(tpos, tneg, cpos, cneg), ilab.xpos=c(-9.5,-8,-6,-4.5),
cex=.75, header="Author(s) and Year")
```

Additional summary estimates can be added to the plot with the `addpoly` function. See the documentation for that function for examples.

When `showweights=TRUE`, the annotations will include information about the weights given to the observed outcomes during the model fitting. For simple models (such as those fitted with the `rma.uni` function), these weights correspond to the 'inverse-variance weights' (but are given in
percent). For models fitted with the \texttt{rma.mv} function, the weights are based on the
diagonal of the weight matrix. Note that the weighting structure is typically more complex in
such models (i.e., the weight matrix is usually not just a diagonal matrix) and the weights shown therefore
do not reflect this complexity. See \texttt{weights.rma} for more details (for the special case that \( x \) is an intercept-only
"rma.mv" model, one can also set \texttt{showweights="rowsum"} to show the 'row-sum weights').

By default (i.e., when \texttt{psize} is not specified), the point sizes are a function of the square root of
the model weights. This way, their areas are proportional to the weights. However, the point sizes are
rescaled so that the smallest point size is \texttt{plim[1]} and the largest point size is \texttt{plim[2]}. As a result,
their relative sizes (i.e., areas) no longer exactly correspond to their relative weights. If exactly
relative point sizes are desired, one can set \texttt{plim[2]} to NA, in which case the points are rescaled
so that the smallest point size corresponds to \texttt{plim[1]} and all other points are scaled accordingly.
As a result, the largest point may be very large. Alternatively, one can set \texttt{plim[1]} to NA, in which
case the points are rescaled so that the largest point size corresponds to \texttt{plim[2]} and all other
points are scaled accordingly. As a result, the smallest point may be very small and essentially
indistinguishable from the confidence interval line. To avoid the latter, one can also set \texttt{plim[3]},
which enforces a minimal point size.

\textbf{Note}

The function tries to set some sensible values for the optional arguments, but it may be necessary to
adjust these in certain circumstances.

The function actually returns some information about the chosen values invisibly. Printing this
information is useful as a starting point to make adjustments to the plot (see ‘Examples’).

Arguments \texttt{slab} and \texttt{i1ab} and when specifying vectors for arguments \texttt{pch}, \texttt{psize}, \texttt{order}, and/or
\texttt{colout}, the variables specified are assumed to be of the same length as the data originally passed
to the model fitting function (and if the \texttt{data} argument was used in the original model fit, then the
variables will be searched for within this data frame first). Any subsetting and removal of studies
with missing values is automatically applied to the variables specified via these arguments.

If the number of studies is quite large, the labels, annotations, and symbols may become quite small
and impossible to read. Stretching the plot window vertically may then provide a more readable
figure (one should call the function again after adjusting the window size, so that the label/symbol
sizes can be properly adjusted). Also, the \texttt{cex}, \texttt{cex.lab}, and \texttt{cex.axis} arguments are then useful
to adjust the symbol and text sizes.

If the horizontal plot and/or x-axis limits are set manually, then the horizontal plot limits (\texttt{xlim})
must be at least as wide as the x-axis limits (\texttt{alim}). This restriction is enforced inside the function.

If the outcome measure used for creating the plot is bounded (e.g., correlations are bounded between
-1 and +1, proportions are bounded between 0 and 1), one can use the \texttt{olim} argument to enforce
those limits (the observed outcomes and confidence/prediction intervals cannot exceed those bounds
then).

The models without moderators, the \texttt{col} argument can also be a vector of two elements, the first for
specifying the color of the summary polygon, the second for specifying the color of the line for the
prediction interval.

The \texttt{lty} argument can also be a vector of up to three elements, the first for specifying the line type
of the individual CIs ("solid" by default), the second for the line type of the prediction interval
("dotted" by default), the third for the line type of the horizontal lines that are automatically added
to the plot ("solid" by default; set to "blank" to remove them).
Additional Arguments

There are some additional arguments that can be passed to the function via ... (hence, they cannot be abbreviated):

- **top** the amount of space to leave empty at the top of the plot (e.g., for adding headers) (the default is 3 rows).
- **annosym** optional vector of length 3 to select the left bracket, separation, and right bracket symbols for the annotations (the default is c(" [", ", ", "]"). Can also include a 4th element to adjust the look of the minus symbol, for example to use a proper minus (−) sign instead of a hyphen-minus (-).
- **textpos** optional vector of length 2 to specify the placement of the study labels and the annotations (the default is to use the horizontal limits of the plot region, i.e., the study labels to the right of xlim[1] and the annotations to the left of xlim[2]).
- **rowadj** optional vector of length 3 to vertically adjust the position of the study labels, the annotations, and the extra information (if specified via ilab). This is useful for fine-tuning the position of text added with different positional alignments (i.e., argument pos in the text function).

Author(s)

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References


See Also

- **forest** for an overview of the various forest functions and **forest.default** for the function draw forest plots without a summary polygon.
- **rma.uni**, **rma.mh**, **rma.peto**, **rma.glmm**, and **rma.mv** for functions to fit models for which forest plots can be drawn.
- **addpoly** for a function to add polygons to forest plots.

Examples

```r
### meta-analysis of the log risk ratios using a random-effects model
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg,
           slab=paste(author, year, sep="", "")

### default forest plot of the log risk ratios and summary estimate
forest(res, header=TRUE)
```
### summary estimate in row -1; studies in rows k=13 through 1; horizontal
### lines in rows 0 and k+1; two extra lines of space at the top for headings,
### and other annotations; headings (if requested) in line k+2
op <- par(xpd=TRUE)
text(x=-8.4, y=-1:16, -1:16, pos=4, cex=.6)
par(op)

### can also inspect defaults chosen
defaults <- forest(res)
defaults

### several forest plots illustrating the use of various arguments
forest(res, cex=.8)
forest(res, cex=.8, addpred=TRUE)
forest(res, cex=.8, alim=c(-3,3))
forest(res, cex=.8, order="prec", alim=c(-3,3))
forest(res, cex=.8, order=ablat, addpred=TRUE)

### adjust xlim values to see how that changes the plot
forest(res)
par("usr")[1:2] ### this shows what xlim values were chosen by default
forest(res, xlim=c(-16,14))
forest(res, xlim=c(-18,10))
forest(res, xlim=c(-10,10))

### illustrate transf argument
forest(res, transf=exp, at=0:7, xlim=c(-8,12), cex=.8, reline=1, header=TRUE)

### illustrate atransf argument
forest(res, atransf=exp, at=log(c(.05,.25,1,4,20)), xlim=c(-8,7), cex=.8, header=TRUE)

### showweights argument
forest(res, atransf=exp, at=log(c(.05,.25,1,4)), xlim=c(-8,8),
       order="prec", showweights=TRUE, cex=.8)

### forest plot with extra annotations
### note: may need to widen plotting device to avoid overlapping text
forest(res, atransf=exp, at=log(c(.05,.25,1,4)), xlim=c(-16,6),
       ilab=cbind(tpos, tneg, cpos, cneg), ilab.xpos=c(-9.5,-8,-6,-4.5),
       cex=.75, header="Author(s) and Year")
op <- par(cex=.75, font=2)
text(c(-9.5,-8,-6,-4.5), res$k+2, c("TB+", "TB-", "TB+", "TB-"))
text(c(-8.75,-5.25), res$k+3, c("Vaccinated", "Control"))
par(op)

### mixed-effects model with absolute latitude in the model
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, mods = ~ ablat,
data=dat.bcg, slab=paste(author, year, sep="", ""))

### forest plot with observed and fitted values
forest(res, xlim=c(-9,5), order="fit", cex=.8, ilab=ablat,
ilab.xpos=-4, atransf=exp, at=log(c(.05,.25,1,4)),
       ilab=cbind(tpos, tneg, cpos, cneg), ilab.xpos=c(-9.5,-8,-6,-4.5),
       cex=.75, header="Author(s) and Year")
header="Author(s) and Year")
text(-4, res$k+2, "Latitude", cex=.8, font=2)

### meta-analysis of the log risk ratios using a random-effects model
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg,
          slab=paste(author, year, sep="", "\r"))

### for more complicated plots, the ylim and rows arguments may be useful
forest(res)
forest(res, ylim=c(-1.5, 16)) ### the default
forest(res, ylim=c(-1.5, 20)) ### extra space in plot
forest(res, ylim=c(-1.5, 20), rows=c(17:15, 12:6, 3:1)) ### set positions

### forest plot with subgrouping of studies
### note: may need to widen plotting device to avoid overlapping text
tmp <- forest(res, xlim=c(-16, 4.6), at=log(c(.05, .25, 1, 4)), atransf=exp,
              ilab=cbind(tpos, tneg, cpos, cneg), ilab.xpos=c(-9.5,-8,-6,-4.5),
              cex=.75, ylim=c(0.5, 21), order=alloc, rows=c(1:2,5:11,14:17),
              header="Author(s) and Year")
op <- par(cex=0.75, font=2)
text(c(-9.5,-8,-6,-4.5), tmp$ylim[2]-1, c("TB+", "TB-", "TB+", "TB-"))
text(c(-8.75,-5.25), tmp$ylim[2], c("Vaccinated", "Control"))
par(font=4)
text(-16, c(18,12,3), c("Systematic Allocation", "Random Allocation",
                        "Alternate Allocation"), pos=4)
par(op)

### see also the addpoly.rma function for an example where summaries
### for the three subgroups are added to such a forest plot

### illustrate use of olim argument with a meta-analysis of raw correlation
### coefficients (data from Pritz, 1997); without olim=c(0,1), some of the
### CIs would have upper bounds larger than 1
dat <- escalc(measure="PR", xi=xi, ni=ni, data=dat.pritz1997)
res <- rma(yi, vi, data=dat, slab=paste0(study, "\r", authors))
forest(res, xlim=c(-0.8,1.6), alim=c(0,1), psize=1, refline=coef(res), olim=c(0,1), header=TRUE)

### an example of a forest plot where the data have a multilevel structure and
### we want to reflect this by grouping together estimates from the same cluster
dat <- dat.konstantopoulos2011
res <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat,
              slab=paste0("District ", district, ", School: ", school))
dd <- c(0,diff(dat$district))
dd[dd > 0] <- 1
rows <- (1:res$k) + cumsum(dd)
op <- par(tck=-.01, mgp = c(1.6,.2,0), mar=c(3.8,1.5))
forest(res, cex=0.5, header=TRUE, rows=rows, ylim=c(0.5,max(rows)+3))
abline(h = rows[c(1,diff(rows)) == 2] - 1, lty="dotted")
par(op)
Extract the Model Formula from `rma` Objects

Description

The function extracts the model formula from objects of class "rma".

Usage

```r
## S3 method for class 'rma'
formula(x, type="mods", ...)
```

Arguments

- `x`: an object of class "rma".
- `type`: the formula which should be returned: either "mods" (default), "yi" (in case argument `yi` was used to specify a formula), or "scale" (only for location-scale models).
- `...`: other arguments.

Value

The requested formula.

Author(s)

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References


See Also

- `rma.uni`, `rma.glmm`, and `rma.mv` for functions to fit models for which a model formula can be extracted.

Examples

```r
### copy BCG vaccine data into 'dat'
dat <- dat.bcg

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat,
             slab=paste(author, ",", year, sep=""))

### mixed-effects meta-regression model
```
res <- rma(yi, vi, mods = ~ ablat + alloc, data=dat)
formula(res, type="mods")

### specify moderators via 'yi' argument
res <- rma(yi ~ ablat + alloc, vi, data=dat)
formula(res, type="yi")

---

**fsn**

*Fail-Safe N Analysis (File Drawer Analysis)*

### Description

Function to compute the fail-safe N (also called a file drawer analysis).

### Usage

```r
fsn(yi, vi, sei, data, type="Rosenthal", alpha=.05,
    target, weighted=FALSE, subset, digits, ...)
```

### Arguments

- `yi`: vector with the observed effect sizes or outcomes.
- `vi`: vector with the corresponding sampling variances.
- `sei`: vector with the corresponding standard errors (note: only one of the two, vi or sei, needs to be specified).
- `data`: optional data frame containing the variables given to the arguments above.
- `type`: character string to specify the method to use for the calculation of the fail-safe N. Possible options are "Rosenthal" (the default), "Orwin", or "Rosenberg". See 'Details'.
- `alpha`: target alpha level to use for the Rosenthal and Rosenberg methods (the default is .05).
- `target`: target average effect size or outcome to use for the Orwin method. If undefined, then the target average effect size or outcome will be equal to the observed average effect size or outcome divided by 2.
- `weighted`: logical to specify whether Orwin’s method should be based on unweighted (the default) or weighted averages (the default is FALSE).
- `subset`: optional (logical or numeric) vector to specify the subset of studies that should be used for the calculations.
- `digits`: optional integer to specify the number of decimal places to which the printed results should be rounded.
- `...`: other arguments.
Details

The function can be used in combination with any of the usual effect sizes / outcome measures used in meta-analyses (e.g., log risk ratios, log odds ratios, risk differences, mean differences, standardized mean differences, raw correlation coefficients, correlation coefficients transformed with Fisher’s r-to-z transformation), or, more generally, any set of estimates (with corresponding sampling variances) one would like to analyze. Simply specify the observed outcomes via the `yi` argument and the corresponding sampling variances via the `vi` argument (instead of specifying `vi`, one can specify the standard errors via the `sei` argument). The `escalc` function can be used to compute a wide variety of effect sizes / outcome measures (and the corresponding sampling variances) based on summary statistics.

The Rosenthal method (sometimes called a ‘file drawer analysis’) calculates the number of studies averaging null results that would have to be added to the given set of observed outcomes to reduce the combined significance level (p-value) to a particular alpha level (e.g., .05). The calculation is based on Stouffer’s method to combine p-values and is described in Rosenthal (1979).

The Orwin method calculates the number of studies averaging null results that would have to be added to the given set of observed outcomes to reduce the (unweighted or weighted) average outcome to a target value (as specified via the `target` argument). The method is described in Orwin (1983). If `weighted=FALSE` (the default), the method does not require (or makes use) of `vi` (or `sei`), so these arguments are then not relevant for this method. If the `target` argument is not specified, then the target average outcome will be equal to the observed average outcome divided by 2 (which is quite arbitrary). One should really set `target` to a value that reflects an outcome one would consider practically irrelevant. Note that if `target` has the opposite sign as the actually observed average outcome, then its sign is automatically flipped.

The Rosenberg method calculates the number of studies averaging null results that would have to be added to the given set of observed outcomes to reduce the significance level (i.e., p-value) of the weighted average outcome (based on an equal-effects model) to a particular alpha level (e.g., .05). The method is described in Rosenberg (2005).

If the combined/observed significance level is above the specified alpha level (for `type = "Rosenthal"` or `type = "Rosenberg"`) or if the observed average outcome is below the target average outcome (for `type = "Orwin"`), then the fail-safe N value will be 0.

Value

An object of class "fsn". The object is a list containing the following components:

- `type`: the method used.
- `fsnum`: the calculated fail-safe N.
- `alpha`: the specified alpha level.
- `pval`: the p-value of the observed results. NA for the Orwin method.
- `meanes`: the average outcome of the observed results. NA for the Rosenthal method.
- `target`: the target value. NA for the Rosenthal and Rosenberg methods.

The results are formatted and printed with the `print` function.

Note

For the Rosenberg method, the p-value is calculated based on a standard normal distribution (instead of a t-distribution, as suggested by Rosenberg, 2005).
funnel

Author(s)

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References


See Also

`ranktest` for the rank correlation test, `regtest` for the regression test, `trimfill` for the trim and fill method, `tes` for the test of excess significance, and `selmodel` for selection models.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit equal-effects model
rma(yi, vi, data=dat, method="EE")

### fail-safe N computations
fsn(yi, vi, data=dat)
fsn(yi, data=dat, type="Orwin", target=log(0.95)) # target corresponds to a 5% risk reduction/fsn(yi, vi, data=dat, type="Orwin", weighted=TRUE, target=log(0.95))
fsn(yi, vi, data=dat, type="Rosenberg")
```

funnel

Funnel Plots

Description

Function to create funnel plots.

Usage

```r
funnel(x, ...)

# S3 method for class 'rma'
funnel(x, yaxis="sei",
      xlim, ylim, xlab, ylab, slab,
      ...)
funnel steps=5, at, atransf, targs, digits, level=x$level, addtau2=FALSE, type="rstandard", back="lightgray", shade="white", hlines="white", reline, lty=3, pch, pch.fill, col, bg, label=FALSE, offset=0.4, legend=FALSE, ...

## Default S3 method:
funnel(x, vi, sei, ni, subset, yaxis="sei", xlim, ylim, xlab, ylab, slab, steps=5, at, atransf, targs, digits, level=95, back="lightgray", shade="white", hlines="white", reline=0, lty=3, pch, col, bg, label=FALSE, offset=0.4, legend=FALSE, ...)

Arguments

- **x**: an object of class "rma" or a vector with the observed effect sizes or outcomes.
- **vi**: vector with the corresponding sampling variances (needed if x is a vector with the observed effect sizes or outcomes).
- **sei**: vector with the corresponding standard errors (note: only one of the two, vi or sei, needs to be specified).
- **ni**: vector with the corresponding sample sizes. Only relevant when passing a vector via x.
- **subset**: optional (logical or numeric) vector to specify the subset of studies that should be included in the plot. Only relevant when passing a vector via x.
- **yaxis**: either "sei", "vi", "seinv", "vinv", "ni", "ninv", "sqrtni", "sqrtninv", "lni", or "wi" to indicate what values should be placed on the y-axis. See 'Details'.
- **xlim**: x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
- **ylim**: y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
- **xlab**: title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
- **ylab**: title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
- **slab**: optional vector with labels for the k studies. If unspecified, the function tries to extract study labels from x.
- **steps**: the number of tick marks for the y-axis (the default is 5).
- **at**: position of the x-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.
- **atransf**: optional argument to specify a function to transform the x-axis labels (e.g., atransf=exp; see also transf). If unspecified, no transformation is used.
- **targs**: optional arguments needed by the function specified via atransf.
digits

optional integer to specify the number of decimal places to which the tick mark labels of the x- and y-axis should be rounded. Can also be a vector of two integers, the first to specify the number of decimal places for the x-axis, the second for the y-axis labels (e.g., digits=c(2,3)). If unspecified, the function tries to set the argument to some sensible values.

level

numeric value between 0 and 100 to specify the level of the pseudo confidence interval region (for "rma" objects, the default is to take the value from the object). May also be a vector of values to obtain multiple regions. See ‘Examples’.

addtau2

logical to indicate whether the amount of heterogeneity should be accounted for when drawing the pseudo confidence interval region (the default is FALSE). Ignored when x is a meta-regression model and residuals are plotted. See ‘Details’.

type

either "rstandard" (default) or "rstudent" to specify whether the usual or deleted residuals should be used in creating the funnel plot when x is a meta-regression model. See ‘Details’.

back

color to use for the background of the plotting region (default is "lightgray").

shade

color to use for shading the pseudo confidence interval region (default is "white"). When level is a vector of values, different shading colors can be specified for each region.

hlines

color of the horizontal reference lines (default is "white").

recline

numeric value to specify the location of the vertical ‘reference’ line and where the pseudo confidence interval should be centered. If unspecified, the reference line is drawn at the equal- or random-effects model estimate and at zero for meta-regression models (in which case the residuals are plotted) or when directly plotting observed outcomes.

lty

line type for the pseudo confidence interval region and the reference line. The default is to draw dotted lines (see par for other options). Can also be a vector to specify the two line types separately.

pch

plotting symbol to use for the observed outcomes. By default, a filled circle is used. Can also be a vector of values. See points for other options.

pch.fill

plotting symbol to use for the outcomes filled in by the trim and fill method. By default, a circle is used. Only relevant when plotting an object created by the trimfill function.

col

optional character string to specify the color to use for the points ("black" is used by default if not specified). Can also be a vector.

bg

optional character string to specify the background color for open plot symbols ("white" is used by default if not specified). Can also be a vector.

label

argument to control the labeling of the points (the default is FALSE). See ‘Details’.

offset

argument to control the distance between the points and the corresponding labels.

legend

logical to indicate whether a legend should be added to the plot (the default is FALSE). Can also be a keyword to indicate the position of the legend (see legend).

...

other arguments.
Details

For equal- and random-effects models (i.e., models not involving moderators), the plot shows the observed effect sizes or outcomes on the x-axis against the corresponding standard errors (i.e., the square root of the sampling variances) on the y-axis. A vertical line indicates the estimate based on the model. A pseudo confidence interval region is drawn around this value with bounds equal to \( \pm 1.96 \text{SE} \), where SE is the standard error value from the y-axis (assuming level=95). If addtau2=TRUE (only for models of class "rma.uni"), then the bounds of the pseudo confidence interval region are equal to \( \pm 1.96 \sqrt{\text{SE}^2 + \hat{\tau}^2} \), where \( \hat{\tau}^2 \) is the amount of heterogeneity as estimated by the model.

For (mixed-effects) meta-regression models (i.e., models involving moderators), the plot shows the residuals on the x-axis against their corresponding standard errors. Either the usual or deleted residuals can be used for that purpose (set via the type argument). See residuals for more details on the different types of residuals.

With the atransf argument, the labels on the x-axis can be transformed with some suitable function. For example, when plotting log odds ratios, one could use transf=exp to obtain a funnel plot with the values on the x-axis corresponding to the odds ratios. See also transf for some other useful transformation functions in the context of a meta-analysis.

Instead of placing the standard errors on the y-axis, several other options are available by setting the yaxis argument to:

- `yaxis="vi"` for the sampling variances,
- `yaxis="seinv"` for the inverse of the standard errors,
- `yaxis="vinv"` for the inverse of the sampling variances,
- `yaxis="ni"` for the sample sizes,
- `yaxis="ninv"` for the inverse of the sample sizes,
- `yaxis="sqrtlni"` for the square root of the sample sizes,
- `yaxis="sqrtlninv"` for the inverse square root of the sample sizes,
- `yaxis="lni"` for the log of the sample sizes,
- `yaxis="wi"` for the weights.

However, only when `yaxis="se"` (the default) will the pseudo confidence region have the expected (upside-down) funnel shape with straight lines. Also, when placing (a function of) the sample sizes on the y-axis or the weights, then the pseudo confidence region cannot be drawn. See Sterne and Egger (2001) for more details on the choice of the y-axis.

If the object passed to the function comes from the trimfill function, the outcomes that are filled in by the trim and fill method are also added to the funnel plot. The symbol to use for plotting the filled in values can be specified via the pch.fill argument.

One can also directly pass a vector with the observed effect sizes or outcomes (via x) and the corresponding sampling variances (via vi), standard errors (via sei), and/or sample sizes (via ni) to the function. By default, the vertical reference line is then drawn at zero.

The arguments back, shade, and hlines can be set to NULL to suppress the shading and the horizontal reference line.

With the label argument, one can control whether points in the plot will be labeled. If label="all" (or label=TRUE), all points in the plot will be labeled. If label="out", points falling outside of
funnel
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the pseudo confidence region will be labeled. Finally, one can also set this argument to a numeric value (between 1 and $k$) to specify how many of the most extreme points should be labeled (e.g., with label=1 only the most extreme point are labeled, while with label=3, the most extreme, and the second and third most extreme points are labeled). With the offset argument, one can adjust the distance between the labels and the corresponding points.

Value

A data frame with components:

- x: the x-axis coordinates of the points that were plotted.
- y: the y-axis coordinates of the points that were plotted.
- slab: the study labels.

Note that the data frame is returned invisibly.

Note

Placing (a function of) the sample sizes on the y-axis (i.e., using yaxis="ni", yaxis="ninv", yaxis="sqrtni", yaxis="sqrtninv", or yaxis="lni") is only possible when information about the sample sizes is actually stored within the object passed to the funnel function. That should automatically be the case when the observed effect sizes or outcomes were computed with the escalc function or when the observed effect sizes or outcomes were computed within the model fitting function. On the other hand, this will not be the case when rma.uni was used together with the yi and vi arguments and the yi and vi values were not computed with escalc. In that case, it is still possible to pass information about the sample sizes to the rma.uni function (e.g., use rma.uni(yi, vi, ni=ni, data=dat), where data frame dat includes a variable called ni with the sample sizes).

When using unweighted estimation, using yaxis="wi" will place all points on a horizontal line. When directly passing a vector with the observed effect sizes or outcomes to the function, yaxis="wi" is equivalent to yaxis="vinv", except that the weights are expressed in percent.

Argument slab and when specifying vectors for arguments pch, col, and/or bg and x is an object of class "rma", the variables specified are assumed to be of the same length as the data passed to the model fitting function (and if the data argument was used in the original model fit, then the variables will be searched for within this data frame first). Any subsetting and removal of studies with missing values is automatically applied to the variables specified via these arguments.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


**See Also**

*rma.uni*, *rma.mh*, *rma.peto*, *rma.glmm*, and *rma.mv* for functions to fit models for which funnel plots can be drawn.

*trimfill* for the trim and fill method and *regtest* for the regression test.

**Examples**

```r
### copy BCG vaccine data into 'dat'
dat <- dat.bcg

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat)

### fit random-effects model
res <- rma(yi, vi, data=dat, slab=paste(author, year, sep="", "))

### draw a standard funnel plot
funnel(res)

### show risk ratio values on x-axis (log scale)
funnel(res, atransf=exp)

### label points outside of the pseudo confidence interval region
funnel(res, atransf=exp, label="out")

### passing log risk ratios and sampling variances directly to the function
### note: same plot, except that reference line is centered at zero
funnel(dat$yi, dat$vi)

### the with() function can be used to avoid having to retype dat$... over and over
with(dat, funnel(yi, vi))

### can accomplish the same thing by setting refline=0
funnel(res, refline=0)

### adjust the position of the x-axis labels, number of digits, and y-axis limits
funnel(res, atransf=exp, at=log(c(.125, .25, .5, 1, 2)), digits=3L, ylim=c(0,.8))

### contour-enhanced funnel plot centered at 0 (see Peters et al., 2008)
funnel(res, level=c(90, 95, 99), shade=c("white", "gray55", "gray75"), refline=0, legend=TRUE)

### same, but show risk ratio values on the x-axis and some further adjustments
funnel(res, level=c(90, 95, 99), shade=c("white", "gray55", "gray75"), digits=3L, ylim=c(0,.8),
       refline=0, legend=TRUE, atransf=exp, at=log(c(.125, .25, .5, 1, 2, 4, 8)))

### illustrate the use of vectors for 'pch' and 'col'
```
gosh

GOSH Plots for 'rma' Objects

Description

Function to create GOSH plots for objects of class "rma".
Usage

gosh(x, ...)

# S3 method for class 'rma'
gosh(x, subsets, progbar=TRUE, parallel="no", ncpus=1, cl, ...)

Arguments

x an object of class "rma".
subsets optional integer to specify the number of subsets.
progbar logical to specify whether a progress bar should be shown (the default is TRUE).
parallel character string to specify whether parallel processing should be used (the default is "no"). For parallel processing, set to either "snow" or "multicore". See ‘Note’.
ncpus integer to specify the number of processes to use in the parallel processing.
cl optional cluster to use if parallel="snow". If unspecified, a cluster on the local machine is created for the duration of the call.
... other arguments.

Details

The model specified via x must be a model fitted with either the rma.uni, rma.mh, or rma.peto function.

Olkin et al. (2012) proposed the GOSH (graphical display of study heterogeneity) plot, which is based on examining the results of an equal-effects model in all possible subsets of size 1, ..., k of the k studies included in a meta-analysis. In a homogeneous set of studies, the model estimates obtained this way should form a roughly symmetric, contiguous, and unimodal distribution. On the other hand, when the distribution is multimodal, then this suggests the presence of heterogeneity, possibly due to outliers and/or distinct subgroupings of studies. Plotting the estimates against some measure of heterogeneity (e.g., I^2, H^2, or the Q-statistic) can also help to reveal subclusters, which are indicative of heterogeneity. The same type of plot can be produced by first fitting an equal-effects model with either the rma.uni (using method="EE"), rma.mh, or rma.peto functions and then passing the fitted model object to the gosh function and then plotting the results.

For models fitted with the rma.uni function (which may be random-effects or mixed-effects meta-regressions models), the idea underlying this type of plot can be generalized (Viechtbauer, 2021) by examining the distribution of all model coefficients, plotting them against each other, and against some measure of (residual) heterogeneity (including the estimate of \( \tau^2 \)).

Note that for models without moderators, application of the method requires fitting a total of \( 2^k - 1 \) models, which could be an excessively large number when k is large. For example, for \( k = 10 \), there are only 1023 possible subsets, but for \( k = 20 \), this number already grows to 1,048,575. For even larger \( k \), it may become computationally infeasible to consider all possible subsets. Instead, we can then examine a (sufficiently large number of) random subsets.

By default, if the number of possible subsets is \( \leq 10^6 \), the function will consider all possible subsets and otherwise \( 10^4 \) random subsets. One can use the subsets argument to specify a different number of subsets to consider. If subsets is specified and it is actually larger than the number of possible
subsets, then the function automatically only considers the possible subsets and does not use random subsets.

When \( x \) is an equal-effects model or a random-effects model fitted using method="DL", provisions have been made to speed up the model fitting to the various subsets. For random-effects models using some other estimator of \( \tau^2 \) (especially an iterative one like method="REML"), the computations will be considerably slower.

Value

An object of class "gosh.rma". The object is a list containing the following components:

- res: a data frame with the results for each subset (various heterogeneity statistics and the model coefficient(s)).
- incl: a matrix indicating which studies were included in which subset.
- ...: some additional elements/values.

The results can be printed with the print function and plotted with the plot function.

Note

On machines with multiple cores, one can try to speed things up by delegating the model fitting to separate worker processes, that is, by setting parallel="snow" or parallel="multicore" and ncpus to some value larger than 1. Parallel processing makes use of the parallel package, using the makePSOCKcluster and parLapply functions when parallel="snow" or using mclapply when parallel=" multicore" (the latter only works on Unix/Linux-alikes). With parallel::detectCores(), one can check on the number of available cores on the local machine.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.uni, rma.mh, and rma.peto for functions to fit models for which GOSH plots can be drawn.
influence.rma.uni for other model diagnostics.
Examples

```r
### calculate log odds ratios and corresponding sampling variances
dat <- escalc(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat.egger2001)

### meta-analysis of all trials including ISIS-4 using an equal-effects model
res <- rma(yi, vi, data=dat, method="EE")

### fit FE model to all possible subsets (65535 models)
## Not run:
sav <- gosh(res, progbar=FALSE)
sav

### create GOSH plot
### red points for subsets that include and blue points
### for subsets that exclude study 16 (the ISIS-4 trial)
plot(sav, out=16, breaks=100)
## End(Not run)
```

---

**hc**  
*Meta-Analysis based on the Method by Henmi and Copas (2010)*

**Description**

The function can be used to obtain an estimate of the average true outcome and corresponding confidence interval under a random-effects model using the method described by Henmi and Copas (2010).

**Usage**

```r
hc(object, ...)
```

## S3 method for class 'rma.uni'

```r
hc(object, digits, transf, targs, control, ...)
```

**Arguments**

- `object` an object of class "rma.uni".
- `digits` optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
- `transf` optional argument to specify a function to transform the estimate and the corresponding interval bounds (e.g., `transf=exp`; see also `transf`). If unspecified, no transformation is used.
- `targs` optional arguments needed by the function specified under `transf`.
- `control` list of control values for the iterative algorithm. If unspecified, default values are defined inside the function. See ‘Note’.
- `...` other arguments.
Details

The model specified via object must be a model without moderators (i.e., either an equal- or a random-effects model).

When using the usual method for fitting a random-effects model (i.e., weighted estimation with inverse-variance weights), the weights assigned to smaller and larger studies become more uniform as the amount of heterogeneity increases. As a consequence, the estimated average outcome could become increasingly biased under certain forms of publication bias (where smaller studies on one side of the funnel plot are missing). The method by Henmi and Copas (2010) tries to counteract this problem by providing an estimate of the average true outcome that is based on inverse-variance weights as used under an equal-effects model (which do not take the amount of heterogeneity into consideration). The amount of heterogeneity is still estimated (with the DerSimonian-Laird estimator) and incorporated into the standard error of the estimated average outcome and the corresponding confidence interval.

Currently, there is only a method for handling objects of class "rma.uni" with the hc function. It therefore provides a method for conducting a sensitivity analysis after the model has been fitted with the rma.uni function.

Value

An object of class "hc.rma.uni". The object is a list containing the following components:

- beta: estimated average true outcome.
- se: corresponding standard error.
- ci.lb: lower bound of the confidence intervals for the average true outcome.
- ci.ub: upper bound of the confidence intervals for the average true outcome.
- ...: some additional elements/values.

The results are formatted and printed with the print function.

Note

The method makes use of the uniroot function. By default, the desired accuracy is set equal to .Machine$double.eps^0.25 and the maximum number of iterations to 1000. The desired accuracy (tol) and the maximum number of iterations (maxiter) can be adjusted with the control argument (i.e., control=list(tol=value, maxiter=value)).

Author(s)

Original code by Henmi and Copas (2010). Corrected for typos by Michael Dewey (<lists@dewey.myzen.co.uk>). Incorporated into the package with some small adjustments for consistency with the other functions in the package by Wolfgang Viechtbauer (<wvb@metafor-project.org>).

References


See Also

rma.uni for the function to fit rma.uni models.

Examples

### calculate log odds ratios and corresponding sampling variances
dat <- escalc(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat.lee2004)
dat

### meta-analysis based on log odds ratios
res <- rma(yi, vi, data=dat)
res

### funnel plot as in Henmi and Copas (2010)
funnel(res, yaxis="seinv", reline=0, xlim=c(-3,3), ylim=c(5,3.5), steps=7, digits=1, back="white")

### use method by Henmi and Copas (2010) as a sensitivity analysis
hc(res)

### back-transform results to odds ratio scale
hc(res, transf=exp)

---

influence.rma.mv Model Diagnostics for 'rma.mv' Objects

Description

The functions can be used to compute various outlier and influential case diagnostics (some of which indicate the influence of deleting one case at a time on the model fit or the fitted/residual values) for objects of class "rma.mv".

Usage

## S3 method for class 'rma.mv'
cooks.distance(model, progbar=FALSE, cluster,
               reestimate=TRUE, parallel="no", ncpus=1, cl, ...)

## S3 method for class 'rma.mv'
dfbetas(model, progbar=FALSE, cluster,
        reestimate=TRUE, parallel="no", ncpus=1, cl, ...)

## S3 method for class 'rma.mv'
hatvalues(model, type="diagonal", ...)

Arguments

model an object of class "rma.mv".
progbar logical to specify whether a progress bar should be shown (the default is FALSE).
cluster: optional vector to specify a clustering variable to use for computing the Cook's distances or DFBETAS values. If not specified, these measures are computed for the individual observed effect sizes or outcomes.

reestimate: logical to specify whether variance/correlation components should be re-estimated after deletion of the i-th case (the default is TRUE).

parallel: character string to specify whether parallel processing should be used (the default is "no"). For parallel processing, set to either "snow" or "multicore". See ‘Note’.

ncpus: integer to specify the number of processes to use in the parallel processing.

c1: optional cluster to use if parallel="snow". If unspecified, a cluster on the local machine is created for the duration of the call.

type: character string to specify whether only the diagonal of the hat matrix ("diagonal") or the entire hat matrix ("matrix") should be returned.

...: other arguments.

Details

The term ‘case’ below refers to a particular row from the dataset used in the model fitting (when argument cluster is not specified) or each level of the variable specified via cluster.

Cook’s distance for the i-th case can be interpreted as the Mahalanobis distance between the entire set of predicted values once with the i-th case included and once with the i-th case excluded from the model fitting.

The DFBETAS value(s) essentially indicate(s) how many standard deviations the estimated coefficient(s) change(s) after excluding the i-th case from the model fitting.

Value

The cooks.distance function returns a vector. The dfbetas function returns a data frame. The hatvalues function returns either a vector with the diagonal elements of the hat matrix or the entire hat matrix.

Note

The variable specified via cluster is assumed to be of the same length as the data originally passed to the rma.mv function (and if the data argument was used in the original model fit, then the variable will be searched for within this data frame first). Any subsetting and removal of studies with missing values that was applied during the model fitting is also automatically applied to the variable specified via the cluster argument.

Leave-one-out diagnostics are calculated by refitting the model k times (where k denotes the number of cases). Depending on how large k is, it may take a few moments to finish the calculations. For complex models fitted with rma.mv, this can become computationally expensive.

On machines with multiple cores, one can try to speed things up by delegating the model fitting to separate worker processes, that is, by setting parallel="snow" or parallel="multicore" and ncpus to some value larger than 1. Parallel processing makes use of the parallel package, using the makePSOCKcluster and parLapply functions when parallel="snow" or using mclapply
when parallel=\texttt{\textasciitilde multicore} (the latter only works on Unix/Linux-alikes). With parallel::detectCores(), one can check on the number of available cores on the local machine.

Alternatively (or in addition to using parallel processing), one can also set \texttt{reestimate=\texttt{FALSE}}, in which case any variance/correlation components in the model are not re-estimated after deleting the $i$th case from the dataset. Doing so only yields an approximation to the Cook’s distances and DFBETAS values that ignores the influence of the $i$th case on the variance/correlation components, but is considerably faster (and often yields similar results).

It may not be possible to fit the model after deletion of the $i$th case from the dataset. This will result in NA values for that case.

\section*{Author(s)}
Wolfgang Viechtbauer \texttt{<wvb@metafor-project.org>} \url{https://www.metafor-project.org}

\section*{References}


\section*{See Also}
\texttt{rstudent.rma.mv} for externally standardized residuals and \texttt{weights.rma.mv} for model fitting weights.

\section*{Examples}

\begin{verbatim}
### copy data from Konstantopoulos (2011) into 'dat'
dat <- dat.konstantopoulos2011

### multilevel random-effects model
res <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat)
print(res, digits=3)

### Cook's distance for each observed outcome
x <- cooks.distance(res)
x
plot(x, type="o", pch=19, xlab="Observed Outcome", ylab="Cook's Distance")

### Cook's distance for each district
x <- cooks.distance(res, cluster=district)
x
plot(x, type="o", pch=19, xlab="District", ylab="Cook's Distance", xaxt="n")
\end{verbatim}
### hat values
hatvalues(res)

---

**Description**

The functions can be used to compute various outlier and influential case diagnostics (some of which indicate the influence of deleting one case at a time on the model fit or the fitted/residual values) for objects of class "rma.uni". For the corresponding documentation for "rma.mv" objects, see `influence.rma.mv`.

**Usage**

```r
## S3 method for class 'rma.uni'
influence(model, digits, progbar=FALSE, ...)
## S3 method for class 'infl.rma.uni'
print(x, digits=x$digits, infonly=FALSE, ...)
## S3 method for class 'rma.uni'
cooks.distance(model, progbar=FALSE, ...)
## S3 method for class 'rma.uni'
dfbetas(model, progbar=FALSE, ...)
## S3 method for class 'rma.uni'
hatvalues(model, type="diagonal", ...)
```

**Arguments**

- **model**: an object of class "rma.uni".
- **x**: an object of class "infl.rma.uni" (for print).
- **digits**: optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
- **progbar**: logical to specify whether a progress bar should be shown (the default is FALSE).
- **infonly**: logical to specify whether only the influential cases should be printed (the default is FALSE).
- **type**: character string to specify whether only the diagonal of the hat matrix ("diagonal") or the entire hat matrix ("matrix") should be returned.
- **...**: other arguments.
Details

The term ‘case’ below refers to a particular row from the dataset used in the model fitting (which is typically synonymous with study).

The `influence` function calculates the following leave-one-out diagnostics for each case:

- externally standardized residual,
- DFFITS value,
- Cook’s distance,
- covariance ratio,
- the leave-one-out amount of (residual) heterogeneity,
- the leave-one-out test statistic of the test for (residual) heterogeneity,
- DFBETAS value(s).

The diagonal elements of the hat matrix and the weights (in %) given to the observed effect sizes or outcomes during the model fitting are also provided (except for their scaling, the hat values and weights are the same for models without moderators, but will differ when moderators are included). For details on externally standardized residuals, see `rstudent.rma.uni`.

The DFFITS value essentially indicates how many standard deviations the predicted (average) effect or outcome for the \( i \)th case changes after excluding the \( i \)th case from the model fitting.

Cook’s distance can be interpreted as the Mahalanobis distance between the entire set of predicted values once with the \( i \)th case included and once with the \( i \)th case excluded from the model fitting.

The covariance ratio is defined as the determinant of the variance-covariance matrix of the parameter estimates based on the dataset with the \( i \)th case removed divided by the determinant of the variance-covariance matrix of the parameter estimates based on the complete dataset. A value below 1 therefore indicates that removal of the \( i \)th case yields more precise estimates of the model coefficients.

The leave-one-out amount of (residual) heterogeneity is the estimated value of \( \tau^2 \) based on the dataset with the \( i \)th case removed. This is always equal to 0 for equal-effects models.

Similarly, the leave-one-out test statistic of the test for (residual) heterogeneity is the value of the test statistic of the test for (residual) heterogeneity calculated based on the dataset with the \( i \)th case removed.

Finally, the DFBETAS value(s) essentially indicate(s) how many standard deviations the estimated coefficient(s) change(s) after excluding the \( i \)th case from the model fitting.

A case may be considered to be ‘influential’ if at least one of the following is true:

- The absolute DFFITS value is larger than \( 3 \times \sqrt{p/(k - p)} \), where \( p \) is the number of model coefficients and \( k \) the number of cases.
- The lower tail area of a chi-square distribution with \( p \) degrees of freedom cut off by the Cook’s distance is larger than 50%.
- The hat value is larger than \( 3 \times (p/k) \).
- Any DFBETAS value is larger than 1.

Cases which are considered influential with respect to any of these measures are marked with an asterisk. Note that the chosen cut-offs are (somewhat) arbitrary. Substantively informed judgment should always be used when examining the influence of each case on the results.
Value

An object of class "infl.rma.uni", which is a list containing the following components:

inf
  an element of class "list.rma" with the externally standardized residuals, DF-FITS values, Cook's distances, covariance ratios, leave-one-out \( \tau^2 \) estimates, leave-one-out (residual) heterogeneity test statistics, hat values, weights, and an indicator whether a case is influential.

dfbs
  an element of class "list.rma" with the DFBETAS values.

... some additional elements/values.

The results are printed with `print.infl.rma.uni` and plotted with `plot.infl.rma.uni`. To format the results as a data frame, one can use the `as.data.frame` function.

Note

Leave-one-out diagnostics are calculated by refitting the model \( k \) times. Depending on how large \( k \) is, it may take a few moments to finish the calculations. There are shortcuts for calculating at least some of these values without refitting the model each time, but these are currently not implemented (and may not exist for all of the leave-one-out diagnostics calculated by the function).

It may not be possible to fit the model after deletion of the \( i \)th case from the dataset. This will result in NA values for that case.

Certain relationships between the leave-one-out diagnostics and the (internally or externally) standardized residuals (Belsley, Kuh, & Welsch, 1980; Cook & Weisberg, 1982) no longer hold for meta-analytic models. Maybe there are other relationships. These remain to be determined.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

plot.infl.rma.uni for a method to plot the outlier and influential case diagnostics.
rstudent.rma.uni for externally standardized residuals and weights.rma.uni for model fitting weights.
Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods ~ ablat + year, data=dat)

### compute the diagnostics
inf <- influence(res)
inf

### plot the values
plot(inf)

### compute Cook's distances, DFBETAS values, and hat values
cooks.distance(res)
dfbetas(res)
hatvalues(res)
```

---

labbe

L'Abbé Plots for 'rma' Objects

Description

Function to create L'Abbé plots for objects of class "rma".

Usage

```r
labbe(x, ...)

## S3 method for class 'rma'
labbe(x, xlim, ylim, xlab, ylab,
      add=x$add, to=x$to, transf, targs,
      pch=21, psize, plim=c(0.5,3.5),
      col, bg, grid=FALSE, lty, ...)
```

Arguments

- `x` an object of class "rma". See ‘Details’.
- `xlim` x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
- `ylim` y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
- `xlab` title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
- `ylab` title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
add See ‘Details’ and the documentation of the escalc function for more details.

to See ‘Details’ and the documentation of the escalc function for more details.

transf optional argument to specify a function to transform the outcomes (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

targs optional arguments needed by the function specified under transf.

pch plotting symbol to use for the outcomes. By default, a filled circle is used. Can also be a vector of values. See points for other options.

psize optional numeric vector to specify the point sizes for the outcomes. If unspecified, the point sizes are a function of the precision of the outcomes. Can also be a vector of values.

plim numeric vector of length 2 to scale the point sizes (ignored when psize is specified). See ‘Details’.

col optional character string to specify the color to use for the points ("black" is used by default if not specified). Can also be a vector.

bg optional character string to specify the background color for open plot symbols ("gray" is used by default if not specified). Can also be a vector. Set to NA to make the plotting symbols transparent.

grid logical to specify whether a grid should be added to the plot. Can also be a color name.

lty optional character vector to specify the line type for the diagonal reference line of no effect and the line that indicates the estimated effect based on the fitted model. If unspecified, the function sets this to c("solid","dashed") by default (use "blank" to suppress a line).

... other arguments.

Details

The model specified via x must be a model without moderators (i.e., either an equal- or a random-effects model) fitted with either the rma.uni, rma.mh, rma.peto, or rma.glmm functions. Moreover, the model must have been fitted with measure set equal to "RD" (for risk differences), "RR" (for risk ratios), "OR" (for odds ratios), "AS" (for arcsine square root transformed risk differences), "IRR" (for incidence rate ratios), "IR0" (for incidence rate differences), or "IRSD" (for square root transformed incidence rate differences).

The function calculates the arm-level outcomes for the two groups (e.g., treatment and control) and plots them against each other. In particular, the function plots the raw proportions of the two groups against each other when analyzing risk differences, the log of the proportions when analyzing (log) risk ratios, the log odds when analyzing (log) odds ratios, the arcsine square root transformed proportions when analyzing arcsine square root transformed risk differences, the raw incidence rates when analyzing incidence rate differences, the log of the incidence rates when analyzing (log) incidence rate ratios, and the square root transformed incidence rates when analyzing square root transformed incidence rate differences. The transf argument can be used to transform these values (e.g., transf=exp to transform the log of the proportions back to raw proportions; see also transf).

As described under the documentation for the escalc function, zero cells can lead to problems when calculating particular outcomes. Adding a small constant to the cells of the $2 \times 2$ tables is a
common solution to this problem. By default, the functions adopts the same method for handling
zero cells as was used when fitting the model.

By default (i.e., when psize is not specified), the point sizes are a function of the precision (i.e.,
inverse standard errors) of the outcomes. This way, more precise estimates are visually more promi-
nent in the plot. By making the point sizes a function of the inverse standard errors of the estimates,
their areas are proportional to the inverse sampling variances, which corresponds to the weights they
would receive in an equal-effects model. However, the point sizes are rescaled so that the smallest
point size is plim[1] and the largest point size is plim[2]. As a result, their relative sizes (i.e.,
areas) no longer exactly correspond to their relative weights in such a model. If exactly relative
point sizes are desired, one can set plim[2] to NA, in which case the points are rescaled so that the
smallest point size corresponds to plim[1] and all other points are scaled accordingly. As a result,
the largest point may be very large. Alternatively, one can set plim[1] to NA, in which case the
points are rescaled so that the largest point size corresponds to plim[2] and all other points are
scaled accordingly.

The solid line corresponds to identical outcomes in the two groups (i.e., the absence of a difference
between the two groups). The dashed line indicates the estimated effect based on the fitted model.

Value
A data frame with components:

- x: the x-axis coordinates of the points that were plotted.
- y: the y-axis coordinates of the points that were plotted.
- cex: the point sizes.
- pch: the plotting symbols.
- col: the point colors.
- bg: the background colors.
- ids: the study id numbers.
- slab: the study labels.

Note that the data frame is returned invisibly.

Author(s)
Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References

See Also
rma.uni, rma.mh, rma.peto, and rma.glmm for functions to fit models for which L’Abbé plots can
be drawn.
### Examples

```r
### meta-analysis of the log risk ratios using a random-effects model
res <- rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### default plot
labbe(res)

### funnel plot with risk values on the x- and y-axis and add grid
labbe(res, transf=exp, grid=TRUE)
```

---

**leave1out**  
*Leave-One-Out Diagnostics for 'rma' Objects*

**Description**

The functions repeatedly fit the specified model, leaving out one observation/study at a time.

**Usage**

```r
leave1out(x, ...)
```

```
## S3 method for class 'rma.uni'
leave1out(x, digits, transf, targs, progbar=FALSE, ...)
## S3 method for class 'rma.mh'
leave1out(x, digits, transf, targs, progbar=FALSE, ...)
## S3 method for class 'rma.peto'
leave1out(x, digits, transf, targs, progbar=FALSE, ...)
```

**Arguments**

- `x`  
  an object of class "rma.uni", "rma.mh", or "rma.peto".

- `digits`  
  optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

- `transf`  
  optional argument to specify a function to transform the model coefficients and interval bounds (e.g., transf=exp; see also `transf`). If unspecified, no transformation is used.

- `targs`  
  optional arguments needed by the function specified under `transf`.

- `progbar`  
  logical to specify whether a progress bar should be shown (the default is FALSE).

- `...`  
  other arguments.

**Details**

For "rma.uni" objects, the model specified via `x` must be a model without moderators (i.e., either an equal- or a random-effects model).
Value

An object of class "list.rma". The object is a list containing the following components:

- `estimate` estimated (average) outcomes.
- `se` corresponding standard errors.
- `zval` corresponding test statistics.
- `pval` corresponding p-values.
- `ci.lb` lower bounds of the confidence intervals.
- `ci.ub` upper bounds of the confidence intervals.
- `Q` test statistics for the test of heterogeneity.
- `Qp` corresponding p-values.
- `tau2` estimated amount of heterogeneity (only for random-effects models).
- `I2` values of $I^2$.
- `H2` values of $H^2$.

When the model was fitted with `test="t"` or `test="knha"`, then `zval` is called `tval` in the object that is returned by the function.

The object is formatted and printed with the `print` function. To format the results as a data frame, one can use the `as.data.frame` function.

Note

When using the `transf` option, the transformation is applied to the estimated coefficients and the corresponding interval bounds. The standard errors are then set equal to `NA` and are omitted from the printed output.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

`rma.uni`, `rma.mh`, and `rma.peto` for functions to fit models for which leave-one-out diagnostics can be computed.
Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### random-effects model
res <- rma(yi, vi, data=dat)

### leave-one-out analysis
leave1out(res)
leave1out(res, transf=exp)

### meta-analysis of the (log) risk ratios using the Mantel-Haenszel method
res <- rma.mh(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### leave-one-out analysis
leave1out(res)
leave1out(res, transf=exp)

### meta-analysis of the (log) odds ratios using Peto's method
res <- rma.peto(ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### leave-one-out analysis
leave1out(res)
leave1out(res, transf=exp)
```

llplot

Plot of Likelihoods for Individual Studies

Description

Function to plot the likelihood of a certain parameter corresponding to an effect size or outcome measure given the study data.

Usage

```r
llplot(measure, yi, vi, sei, ai, bi, ci, di, n1i, n2i, data, subset, drop00=TRUE,
xvals=1000, xlim, ylim, xlab, ylab, scale=TRUE,
lty, lwd, col, level=99.99, refline=0, ...)
```

Arguments

- `measure` a character string to specify for which effect size or outcome measure the likelihoods should be calculated. See ‘Details’ for possible options and how the data should then be specified.
- `yi` vector with the observed effect sizes or outcomes.
- `vi` vector with the corresponding sampling variances.
- `se` vector to specify the corresponding standard.
ai vector to specify the $2 \times 2$ table frequencies (upper left cell).
bi vector to specify the $2 \times 2$ table frequencies (upper right cell).
ci vector to specify the $2 \times 2$ table frequencies (lower left cell).
di vector to specify the $2 \times 2$ table frequencies (lower right cell).
n1i vector to specify the group sizes or row totals (first group/row).
n2i vector to specify the group sizes or row totals (second group/row).
data optional data frame containing the variables given to the arguments above.
subset optional (logical or numeric) vector to specify the subset of studies that should be included in the plot.
drop00 logical to specify whether studies with no cases (or only cases) in both groups should be dropped. See ‘Details’.
xvals integer to specify for how many distinct values the likelihood should be evaluated.
xlim x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
ylim y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
xlab title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
ylab title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
scale logical to specify whether the likelihood values should be scaled, so that the total area under each curve is (approximately) equal to 1.
lty the line types (either a single value or a vector of length $k$). If unspecified, the function sets the line types according to some characteristics of the likelihood function. See ‘Details’.
lwd the line widths (either a single value or a vector of length $k$). If unspecified, the function sets the widths according to the sampling variances (so that the line is thicker for more precise studies and vice-versa).
col the line colors (either a single value or a vector of length $k$). If unspecified, the function uses various shades of gray according to the sampling variances (so that darker shades are used for more precise studies and vice-versa).
level numeric value between 0 and 100 to specify the plotting limits for each likelihood line in terms of the confidence interval (the default is 99.99).
recline numeric value to specify the location of the vertical ‘reference’ line (the default is 0). The line can be suppressed by setting this argument to NA.
... other arguments.

Details

At the moment, the function only accepts measure="GEN" or measure="OR".

For measure="GEN", one must specify arguments yi for the observed effect sizes or outcomes and vi for the corresponding sampling variances (instead of specifying vi, one can specify the
standard errors via the sei argument). The function then plots the likelihood of the true effect size or outcome based on a normal sampling distribution with observed outcome as given by $y_i$ and variance as given by $v_i$ for each study.

For measure="OR", one must specify arguments $a_i$, $b_i$, $c_i$, and $d_i$, which denote the cell frequencies of the $2 \times 2$ tables. Alternatively, one can specify $a_i$, $c_i$, $n_{1i}$, and $n_{2i}$. See escalc function for more details. The function then plots the likelihood of the true log odds ratio based on the non-central hypergeometric distribution for each $2 \times 2$ table. Since studies with no cases (or only cases) in both groups have a flat likelihood and are not informative about the odds ratio, they are dropped by default (i.e., drop00=TRUE) and are hence not drawn (if drop00=FALSE, these likelihood are indicated by dotted lines). For studies that have a single zero count, the MLE of the odds ratio is infinite and these likelihoods are indicated by dashed lines.

### Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

### References


### See Also

rma.uni and rma.glmm for model fitting functions that are based on corresponding likelihood functions.

### Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### draw likelihoods
llplot(measure="GEN", yi=yi, vi=vi, data=dat, lwd=1, refline=NA, xlim=c(-3,2))

### create plot (Figure 2 in van Houwelingen, Zwinderman, & Stijnen, 1993)
llplot(measure="OR", ai=b.xci, n1i=nci, ci=b.xti, n2i=nti, data=dat.collins1985a, lwd=1, refline=NA, xlim=c(-4,4), drop00=FALSE)
```

---

**matreg**

*Fit Regression Models based on Correlation and Covariance Matrices*

### Description

Function to fit regression models based on correlation and covariance matrices.
Usage

matreg(y, x, R, n, V, cov=FALSE, means, ztor=FALSE, nearpd=FALSE, level=95, digits, ...)

Arguments

y
index (or name given as a character string) of the outcome variable.
x
indices (or names given as a character vector) of the predictor variables.
R
correlation or covariance matrix (or only the lower triangular part including the diagonal).
n
sample size based on which the elements in the correlation/covariance matrix were computed.
V
variance-covariance matrix of the lower triangular elements of the correlation/covariance matrix. Either V or n should be specified, not both. See ‘Details’.
cov
logical to specify whether R is a covariance matrix (the default is FALSE).
means
optional vector to specify the means of the variables (only relevant when cov=TRUE).
ztor
logical to specify whether R is a matrix of r-to-z transformed correlations and hence should be back-transformed to raw correlations (the default is FALSE). See ‘Details’.
nearpd
logical to specify whether the nearPD function from the Matrix package should be used when the $R_{x,x}$ matrix cannot be inverted. See ‘Note’.
level
numeric value between 0 and 100 to specify the confidence interval level (the default is 95).
digits
optional integer to specify the number of decimal places to which the printed results should be rounded.
...
other arguments.

Details

Let $R$ be a $p \times p$ correlation or covariance matrix. Let $y$ denote the row/column of the outcome variable and $x$ the row(s)/column(s) of the predictor variable(s) in this matrix. Let $R_{x,x}$ and $R_{x,y}$ denote the corresponding submatrices of $R$. Then

$$b = R_{x,x}^{-1}R_{x,y}$$

yields the standardized or raw regression coefficients (depending on whether $R$ is a correlation or covariance matrix, respectively) when regressing the outcome variable on the predictor variable(s).

The $R$ matrix may be computed based on a single sample of $n$ subjects. In this case, one should specify the sample size via argument $n$. The variance-covariance matrix of the standardized regression coefficients is then given by $\text{Var}(b) = \text{MSE} \times R_{x,x}^{-1}$, where $\text{MSE} = (1 - b' R_{x,y})/(n - m)$ and $m$ denotes the number of predictor variables. The standard errors are then given by the square root of the diagonal elements of $\text{Var}(b)$. Test statistics (in this case, t-statistics) and the corresponding p-values can then be computed as in a regular regression analysis. When $R$ is a covariance matrix, one should set cov=TRUE and specify the means of the $p$ variables via argument means to obtain raw regression coefficients including the intercept and corresponding standard errors.
Alternatively, \( R \) may be the result of a meta-analysis of correlation coefficients. In this case, the elements in \( R \) are pooled correlation coefficients and the variance-covariance matrix of these pooled coefficients should be specified via argument \( V \). The order of elements in \( V \) should correspond to the order of elements in the lower triangular part of \( R \) column-wise. For example, if \( R \) is a \( 4 \times 4 \) matrix of the form:

\[
\begin{bmatrix}
1 & r_{21} & r_{31} & r_{41} \\
r_{21} & 1 & r_{32} & r_{42} \\
r_{31} & r_{32} & 1 & r_{43} \\
r_{41} & r_{42} & r_{43} & 1
\end{bmatrix}
\]

then the elements are \( r_{21}, r_{31}, r_{41}, r_{32}, r_{42}, \) and \( r_{43} \) and hence \( V \) should be a \( 6 \times 6 \) variance-covariance matrix of these elements in this order. The variance-covariance matrix of the standardized regression coefficients (i.e., \( \text{Var}[\hat{b}] \)) is then computed as a function of \( V \) as described in Becker (1992) using the multivariate delta method. The standard errors are then again given by the square root of the diagonal elements of \( \text{Var}[\hat{b}] \). Test statistics (in this case, z-statistics) and the corresponding p-values can then be computed in the usual manner.

In case \( R \) is the result of a meta-analysis of Fisher r-to-z transformed correlation coefficients (and hence \( V \) is then the corresponding variance-covariance matrix of these pooled transformed coefficients), one should set argument \( ztor=TRUE \), so that the appropriate back-transformation is then applied to \( R \) (and \( V \)) within the function.

Finally, \( R \) may be a covariance matrix based on a meta-analysis (e.g., the estimated variance-covariance matrix of the random effects in a multivariate model). In this case, one should set \( cov=TRUE \) and \( V \) should again be the variance-covariance matrix of the elements in \( R \), but now including the diagonal. Hence, if \( R \) is a \( 4 \times 4 \) matrix of the form:

\[
\begin{bmatrix}
\tau_1^2 & \tau_{21} & \tau_{31} & \tau_{41} \\
\tau_{21} & \tau_2^2 & \tau_{32} & \tau_{42} \\
\tau_{31} & \tau_{32} & \tau_3^2 & \tau_{43} \\
\tau_{41} & \tau_{42} & \tau_{43} & \tau_4^2
\end{bmatrix}
\]

then the elements are \( \tau_1^2, \tau_{21}, \tau_{31}, \tau_{41}, \tau_2^2, \tau_{32}, \tau_{42}, \tau_3^2, \tau_{43}, \) and \( \tau_4^2 \), and hence \( V \) should be a \( 10 \times 10 \) variance-covariance matrix of these elements in this order. Argument \( \text{means} \) can then again be used to specify the means of the variables.

**Value**

An object of class “matreg”. The object is a list containing the following components:

- **tab**
  a data frame with the estimated model coefficients, standard errors, test statistics, degrees of freedom (only for t-tests), p-values, and lower/upper confidence interval bounds.

- **vb**
  the variance-covariance matrix of the estimated model coefficients.

- **...**
  some additional elements/values.

The results are formatted and printed with the **print** function.

**Note**

Only the lower triangular part of \( R \) (and \( V \) if it is specified) is used in the computations.
If $R_{x,x}$ is not invertible, an error will be issued. In this case, one can set argument nearpd=TRUE, in which case the nearPD function from the Matrix package will be used to find the nearest positive semi-definite matrix, which should be invertible. The results should be treated with caution when this is done.

When $R$ is a covariance matrix with $V$ and means specified, the means are treated as known constants when estimating the standard error of the intercept.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.mv for a function to meta-analyze multiple correlation coefficients that can be used to construct an $R$ matrix.

calc for a function to construct the variance-covariance matrix of dependent correlation coefficients.

Examples

```r
### copy data into 'dat'
dat <- dat.craft2003

### construct dataset and var-cov matrix of the correlations
tmp <- rcalc(ri ~ var1 + var2 | study, ni=ni, data=dat)
V <- tmp$V
dat <- tmp$dat

### turn var1.var2 into a factor with the desired order of levels
dat$var1.var2 <- factor(dat$var1.var2,
  levels=c("acog.perf", "asom.perf", "conf.perf", "acog.asom", "acog.conf", "asom.conf"))

### multivariate random-effects model
res <- rma.mv(yi, V, mods = ~ var1.var2 - 1, random = ~ var1.var2 | study, struct="UN", data=dat)
res

### restructure estimated mean correlations into a 4x4 matrix
R <- vec2mat(coef(res))
rownames(R) <- colnames(R) <- c("perf", "acog", "asom", "conf")
round(R, digits=3)
```
### check that order in vcov(res) corresponds to order in R
round(vcov(res), digits=4)

### fit regression model with 'perf' as outcome and 'acog', 'asom', and 'conf' as predictors
\[ \text{matreg}(1, 2:4, R=R, V=\text{vcov(res)}) \]

### can also specify variable names
\[ \text{matreg}(\text{"perf"}, c(\text{"acog"}, \text{"asom"}, \text{"conf"}), R=R, V=\text{vcov(res)}) \]

### Not run:
### repeat the above but with r-to-z transformed correlations
\[ \text{dat <- dat.craft2003} \]
\[ \text{tmp <- rcalc(ri ~ var1 + var2 | study, ni=ni, data=dat, rtoz=TRUE)} \]
\[ \mbox{\small V <- tmp$V} \]
\[ \mbox{\small dat <- tmp$dat} \]
\[ \text{dat$var1.var2 <- factor(dat$var1.var2, levels=c(\"acog.perf", \"asom.perf", \"conf.perf", \"acog.asom", \"acog.conf", \"asom.conf\")} \]
\[ \text{res <- rma.mv(yi, V, mods = ~ var1.var2 - 1, random = ~ var1.var2 | study, struct="UN", data=dat)} \]
\[ \mbox{\small R <- vec2mat(coef(res))} \]
\[ \text{rownames(R) <- colnames(R) <- c(\"perf", \"acog", \"asom", \"conf\")} \]
\[ \text{matreg(1, 2:4, R=R, V=\text{vcov(res)}, ztor=TRUE)} \]

### End(Not run)

### a different example based on van Houwelingen et al. (2002)

### create dataset in long format
\[ \text{dat.long <- to.long(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.colditz1994)} \]
\[ \text{dat.long <- escalc(measure="PLO", xi=out1, mi=out2, data=dat.long)} \]
\[ \text{dat.long$tpos <- dat.long$tneg <- dat.long$cpos <- dat.long$cneg <- NULL} \]
\[ \text{levels(dat.long$group) <- c("CON", "EXP")} \]

### fit bivariate model
\[ \text{res <- rma.mv(yi, vi, mods = ~ group - 1, random = ~ group | trial, struct="UN", data=dat.long, method="ML"} \]
\[ \text{res} \]

### regression of log(odds)_EXP on log(odds)_CON
\[ \text{matreg(y=2, x=1, R=\text{res$G}, cov=TRUE, means=coef(res), n=\text{res$g.levels.comb.k})} \]

### but the SE of the CON coefficient is not computed correctly, since above we treat \text{res$G} as if
### it was a var-cov matrix computed from raw data based on \text{res$g.levels.comb.k} (= 13) data points

### fit bivariate model and get the var-cov matrix of the estimates in \text{res$G}
\[ \text{res <- rma.mv(yi, vi, mods = ~ group - 1, random = ~ group | trial, struct="UN", data=dat.long, method="ML", cvvc="varcov", control=list(nearpd=TRUE))} \]

### now use \text{res$vcv} as the var-cov matrix of the estimates in \text{res$G}
\[ \text{matreg(y=2, x=1, R=\text{res$G}, cov=TRUE, means=coef(res), V=\text{res$vcv})} \]
metafor.news  
Read News File of the Metafor Package

Description
Read the news file of the metafor-package.

Usage
metafor.news()

Details
The function is just a wrapper for news(package="metafor") which parses and displays the ‘NEWS’ file of the package.

Author(s)
Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References

Examples
## Not run:
metafor.news()
## End(Not run)

misc-models  
Fixed-Effects and Random-Effects Models in Meta-Analysis

Description
Books and articles about meta-analysis often describe and discuss the difference between the so-called ‘fixed-effects model’ and the ‘random-effects model’ (e.g., Cooper et al., 2009). The former term is (mostly) avoided throughout the documentation of the metafor package. The term ‘equal-effects model’ is used instead, since it more concretely describes the main assumption underlying this model (i.e., that the underlying true effects/outcomes are homogeneous, or in other words, that they are all equal to each other). The terms ‘common-effect(s) model’ or ‘homogenous-effect(s) model’ have also sometimes been used in the literature to describe this model and are equally descriptive.
Moreover, the term ‘fixed-effects model’ creates a bit of a conundrum. When authors use this term, they are really typically referring to the equal-effects model. There is however another type of model, the ‘real’ fixed-effects model, that is different from the equal-effects model, but now we would need to invent (unnecessarily) a different term to refer to this model. Some have done so or tried to make a distinction between the ‘fixed-effect model’ (without the s!) and the ‘fixed-effects model’, but this subtle difference in terminology is easily overlooked/missed. Using the term ‘equal-effects model’ avoids this confusion and is more informative.

However, the question then remains what the real fixed-effects model is all about. The purpose of this page is to describe this model and to contrast it with the well-known random-effects model.

**Details**

**Fixed-Effects Model:**

Assume we have a set of \( i = 1, \ldots, k \) independent studies and let \( y_i \) denote the observed value of the effect size or outcome measure in the \( i \)th study. Let \( \theta_i \) denote the corresponding (unknown) true effect/outcome, such that

\[
y_i | \theta_i \sim N(\theta_i, v_i).
\]

In other words, the observed effect sizes or outcomes are assumed to be unbiased and normally distributed estimates of the corresponding true effects/outcomes with sampling variances equal to \( v_i \). The \( v_i \) values are assumed to be known.

The fixed-effects model is simply given by

\[
y_i = \theta_i + \varepsilon_i,
\]

where the \( \theta_i \) values are the (fixed) true effects/outcomes of the \( k \) studies. Therefore, the model ‘conditions’ on the true effects/outcomes and provides a *conditional inference* about the \( k \) studies included in the meta-analysis.

When using weighted estimation (the default in `rma.uni` when `method="FE"`), this implies that the fitted model provides an estimate of

\[
\hat{\theta}_w = \frac{\sum_{i=1}^{k} w_i \theta_i}{\sum_{i=1}^{k} w_i},
\]

that is, the *weighted average* of the true effects/outcomes in the \( k \) studies, with weights equal to \( w_i = 1/v_i \).

As an example, consider the meta-analysis by Bangert-Drowns et al. (2004) on the effectiveness of writing-to-learn interventions on academic achievement. The dataset (`dat.bangertdrowns2004`) includes the observed standardized mean differences (variable \( y_i \)) and the corresponding sampling variances (variable \( v_i \)) of the 48 studies. We can fit a fixed-effects model to these data with:

```r
# copy data into 'dat'
dat <- dat.bangertdrowns2004

# fit a fixed-effects model
res <- rma(yi, vi, data=dat, method="FE")
res
```

# Fixed-Effects Model (k = 48)
The Q-test suggests that the underlying true standardized mean differences are heterogeneous ($Q(df = 47) = 107.111, p < .0001$). Therefore, if we believe this to be true, then the value shown under estimate is an estimate of the inverse-variance weighted average of the true standardized mean differences of these 48 studies (i.e., $\hat{\theta}_w = 0.17$).

One can also employ an unweighted estimation method (by setting weighted=FALSE in rma.uni), which provides an estimate of the unweighted average of the true effects/outcomes in the $k$ studies, that is, an estimate of $\bar{\theta}_u = \sum_{i=1}^{k} \theta_i / k$.

Returning to the example, we then find:

```r
# fit a fixed-effects model using unweighted estimation
res <- rma(yi, vi, data=dat, method="FE", weighted=FALSE)
res
# Fixed-Effects Model (k = 48)
#
# I^2 (total heterogeneity / total variability): 56.12%
# H^2 (total variability / sampling variability): 2.28
#
# Test for Heterogeneity:
# Q(df = 47) = 107.1061, p-val < .0001
#
# Model Results:
#
# estimate se  zval  pval ci.lb  ci.ub
# 0.2598 0.0380 6.8366 <.0001 0.1853 0.3343
```

Therefore, the estimate value is now an estimate of the average of the true standardized mean differences of these 48 studies (i.e., $\hat{\theta}_u = 0.26$).

For weighted estimation, one could also choose to estimate $\hat{\theta}_w$, where the $w_i$ values are user-defined weights (via argument weights in rma.uni). Hence, using inverse-variance weights or unit weights (as in unweighted estimation) are just special cases. It is up to the user to decide to what extent $\hat{\theta}_w$ is a meaningful parameter to estimate (regardless of the weights used).

For example, we could use the sample sizes as weights:

```r
# fit a fixed-effects model using the sample sizes as weights
```
We therefore obtain an estimate of the sample-size weighted average of the true standardized mean differences of these 48 studies (i.e., \( \hat{\theta}_w = 0.17 \)). Since the sample sizes and the inverse sampling variances are highly correlated (\( \text{cor}(\text{dat$ni}, 1/\text{dat$vi}) \) yields 0.999), the results are almost identical to the ones we obtained earlier using inverse-variance weighting.

**Random-Effects Model:**

The random-effects model does not condition on the true effects/outcomes. Instead, the \( k \) studies included in the meta-analysis are assumed to be a random sample from a larger population of studies. In rare cases, the studies included in a meta-analysis are actually sampled from a larger collection of studies. More typically, all efforts have been made to find and include all relevant studies providing evidence about the phenomenon of interest and hence the population of studies is a hypothetical population of an essentially infinite set of studies comprising all of the studies that have been conducted, that could have been conducted, or that may be conducted in the future.

We assume that \( \theta_i \sim N(\mu, \tau^2) \), that is, the true effects/outcomes in the population of studies are normally distributed with \( \mu \) denoting the average true effect/outcome and \( \tau^2 \) the variance of the true effects/outcomes in the population (\( \tau^2 \) is therefore often referred to as the amount of ‘heterogeneity’ in the true effects/outcomes). The random-effects model can also be written as

\[
y_i = \mu + u_i + \varepsilon_i,
\]

where \( u_i \sim N(0, \tau^2) \) and \( \varepsilon_i \sim N(0, v_i) \). The fitted model provides estimates of \( \mu \) and \( \tau^2 \). Consequently, the random-effects model provides an **unconditional inference** about the average true effect/outcome in the population of studies (from which the \( k \) studies included in the meta-analysis are assumed to be a random sample).

Fitting a random-effects model to the example data yields:

```r
res <- rma(yi, vi, data=dat)
res
```

**Random-Effects Model (k = 48; \( \tau^2 \) estimator: REML)**

\#
\# \( \tau^2 \) (estimated amount of total heterogeneity): 0.0499 (SE = 0.0197)
\# \( \tau \) (square root of estimated \( \tau^2 \) value): 0.2235
# I^2 (total heterogeneity / total variability): 58.37%
# H^2 (total variability / sampling variability): 2.40

# Test for Heterogeneity:
# Q(df = 47) = 107.1061, p-val < .0001

# Model Results:
#
# estimate  se   zval  pval  ci.lb  ci.ub
# 0.2219 0.0460 4.8209 <.0001 0.1317 0.3122

The value shown under estimate is now an estimate of the average true standardized mean difference of studies in the population of studies from which the 48 studies included in this dataset have come (i.e., \( \hat{\mu}_w = 0.22 \)).

When using weighted estimation in the context of a random-effects model, the model is fitted with weights equal to \( w_i = 1/(\tau^2 + v_i) \), with \( \tau^2 \) replaced by its estimate (the default in \texttt{rma.uni} when method is set to one of the possible choices for estimating \( \tau^2 \)). One can also choose unweighted estimation in the context of the random-effects model (\texttt{weighted=FALSE}) or specify user-defined weights (via \texttt{weights}), although the parameter that is estimated (i.e., \( \mu \)) remains the same regardless of the estimation method and weights used (as opposed to the fixed-effect model, where the parameter estimated is different for weighted versus unweighted estimation or when using different weights than the standard inverse-variance weights). Since weighted estimation with inverse-variance weights is most efficient, it is usually to be preferred for random-effects models (while in the fixed-effect model case, we must carefully consider whether \( \bar{\theta}_w \) or \( \bar{\theta}_u \) is the more meaningful parameter to estimate).

**Conditional versus Unconditional Inferences:**

Contrary to what is often stated in the literature, it is important to realize that the fixed-effects model does not assume that the true effects/outcomes are homogeneous (i.e., that \( \theta_i \) is equal to some common value \( \theta \) in all \( k \) studies). In other words, the fixed-effects model provides perfectly valid inferences under heterogeneity, as long as one is restricting these inferences to the set of studies included in the meta-analysis and one realizes that the model does not provide an estimate of \( \theta \) or \( \mu \), but of \( \bar{\theta}_w \) or \( \bar{\theta}_u \) (depending on the estimation method used).

However, such inferences are conditional on the included studies. It is therefore not permissible to generalize those inferences beyond the set of studies included in a meta-analysis. In contrast, a random-effects model provides unconditional inferences and therefore allows a generalization beyond the set of included studies, although the population of studies to which we can generalize is typically only vaguely defined (since the included studies are not a proper random sample from a specified sampling frame). Instead, we simply must assume that the included studies are a representative sample of some population and it is to that population to which we are generalizing.

Leaving aside this issue, the above implies that there is nothing wrong with fitting both the fixed- and random-effects models to the same data, since these models address inherently different questions (i.e., what was the average effect in the studies that have been conducted and are included in this meta-analysis versus what is the average effect in the larger population of studies?).

**Equal-Effects Model:**

In the special case that the true effects/outcomes are actually homogeneous (the equal-effects case), the distinction between the fixed- and random-effects models disappears, since homogeneity implies that \( \mu = \bar{\theta}_w = \bar{\theta}_u \equiv \theta \). Therefore, if one believes that the true effects/outcomes are
homogeneous, then one can fit an equal-effects model (using weighted estimation), since this will provide the most efficient estimate of \( \theta \) (note that if the true effects/outcomes are really homogeneous but we fit a random-effects model, it can happen that the estimate of \( \tau^2 \) is actually larger than 0, which then leads to a loss of efficiency).

However, since there is no infallible method to test whether the true effects/outcomes are really homogeneous or not, a researcher should decide on the type of inference desired before examining the data and choose the model accordingly.

Note that fitting an equal-effects model (with \texttt{method="EE"}) yields the exact same output as fitting a fixed-effects model, since the equations used to fit these two models are identical. However, the interpretation of the results is different. If we fit an equal-effects model, we make the assumption that the true effects are homogeneous and, if we believe this assumption to be justified, can interpret the estimate as an estimate of the true effect. On the other hand, if we reject the homogeneity assumption, then we should reject the model altogether. In contrast, if we fit a fixed-effects model, we do not assume homogeneity and instead interpret the estimate as an estimate of the (weighted) average true effect of the included studies.

For further discussions of the distinction between the equal-, fixed-, and random-effects models, see Laird and Mosteller (1990) and Hedges and Vevea (1998).

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References


Description

This page documents some miscellaneous options and features that do not fit very well elsewhere.
Details

Controlling the Number of Digits in the Output:

Many functions in the `metafor` package have a `digits` argument, which can be used to control the number of digits that are displayed in the output when printing numeric values. For more control over the displayed output, one can set this argument to a named vector of the form:

```r
digits=c(est=2, se=3, test=2, pval=3, ci=2, var=3, sevar=3, fit=3, het=3)
```

where the elements control the displayed number of digits for various aspects of the output, namely:

- `est` for estimates (e.g., effect sizes, model coefficients, predicted values),
- `se` for standard errors,
- `test` for test statistics,
- `pval` for p-values,
- `ci` for confidence/prediction interval bounds,
- `var` for sampling variances and variance components,
- `sevar` for standard errors thereof,
- `fit` for fit statistics,
- `het` for heterogeneity statistics.

Instead of setting this argument in each function call (which would be tedious), one can also create a vector named `.digits` in the workspace (at the beginning of an analysis script) with:

```r
.digits <- c(est=2, se=3, test=2, pval=3, ci=2, var=3, sevar=3, fit=3, het=3)
```

which then controls the displayed output. The values for the elements shown above could be a sensible choice when analyzing various types of standardized effect size measures.

Styled Output with the crayon Package:

The `crayon` package provides a way to create colored output. The `metafor` package is designed to automatically make use of this feature when the `crayon` package is installed (`install.packages("crayon")`) and loaded (`library(crayon)`). Note that this only works on terminals that support ‘ANSI’ color and highlight codes (e.g., not under RGui on Windows or R.app on macOS, but the RStudio console and all modern terminals should support this).

The default color theme that is used is quite plain, but should work with a light or dark colored background. One can modify the color theme by creating an object in the workspace named `.mtheme`, which should be a list whose elements specify the styles for various parts of the output (see below for some examples and the documentation of the `crayon` package for the syntax to specify styles). The following elements are recognized:

- `header` for the header of tables (underlined by default),
- `body1` for odd numbered rows in the body of tables,
- `body2` for even numbered rows in the body of tables,
- `na` for missing values in tables,
- `section` for section headers (bold by default),
- `text` for descriptive text in the output,
- `result` for the corresponding result(s),
- `stop` for errors (bold red by default),
- warning for warnings (yellow by default),
- message for messages (green by default),
- verbose for the text in verbose output (cyan by default),
- legend for legends (gray by default).

Elements not specified are styled according to their defaults. For example, one could use:

```r
.mstyle <- list(header=combine_styles("gray20", "underline"),
               body1=make_style("gray40"),
               body2=make_style("gray40"),
               na=bold,
               section=combine_styles("gray15", "bold"),
               text=make_style("gray50"),
               result=make_style("gray30"))
```

or

```r
.mstyle <- list(header=combine_styles("gray80", "underline"),
               body1=make_style("gray60"),
               body2=make_style("gray60"),
               na=bold,
               section=combine_styles("gray85", "bold"),
               text=make_style("gray50"),
               result=make_style("gray70"))
```

for a light or dark colored background, respectively. A slightly more colorful theme could be:

```r
.mstyle <- list(header=combine_styles("snow", make_style("royalblue4", bg=TRUE)),
               body1=combine_styles("gray20", make_style("gray95", bg=TRUE)),
               body2=combine_styles("gray20", make_style("gray85", bg=TRUE)),
               na=combine_styles("red4", "bold"),
               section=combine_styles("black", "bold", make_style("lightskyblue", bg=TRUE)),
               text=make_style("gray50"),
               result=make_style("blue"))
```

or

```r
.mstyle <- list(header=combine_styles("snow", make_style("royalblue4", bg=TRUE)),
               body1=combine_styles("gray95", make_style("gray20", bg=TRUE)),
               body2=combine_styles("gray95", make_style("gray30", bg=TRUE)),
               na=combine_styles("orange1", "bold"),
               section=combine_styles("white", "bold", make_style("blue", bg=TRUE)),
               text=make_style("steelblue4"),
               result=make_style("steelblue1"))
```

for a light and dark colored background, respectively.

The following code snippet includes all output elements (except for an error) and can be used to test out a chosen color theme:

```r
# calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg,
              ci=cpos, di=cneg, data=dat.bcg)
dat$yi[1] <- NA # set one estimate to missing so we get a warning below
```
dat

# fit random-effects model
res <- rma(yi, vi, mods = ~ ablat, data=dat, verbose=3)
summary(res)

Note that support for 256 different colors and text formatting (such as underlined and bold text) differs across terminals.

Removing Empty Lines Before and After the Output:

When printing output, an empty line is usually added before and after the output. For more compact output, this can be suppressed by creating an object named .rmspace in the workspace. For example, running the following code:

# calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, 
              ci=cpos, di=cneg, data=dat.bcg)

# fit random-effects model
res <- rma(yi, vi, data=dat)
res

.rmspace <- TRUE
res

shows the difference.

Version Check:

When loading the metafor package in an interactive session, an automatic check is run to compare the version number of the installed package with the one available on CRAN. If the installed version is older than the one available at CRAN, the user is notified that a new version is available. This check can be suppressed by setting the environment variable METAFOR_VERSION_CHECK to FALSE (e.g., with Sys.setenv(METAFOR_VERSION_CHECK=FALSE)).

By setting the environment variable to "devel" (e.g., with Sys.setenv(METAFOR_VERSION_CHECK="devel")), the version check is run against the 'development version' available on GitHub.

Model Fitting / Processing Time:

The various model fitting functions (i.e., rma.uni, rma.mh, rma.peto, rma.glmm, rma.mv, and selmodel) and various other functions (e.g., confint, cumul, leave1out, profile, rstudent) automatically keep track of the model fitting / processing time. This information is stored as element time (in seconds) in the object that is returned. One can also use argument time=TRUE to nicely print this information. For example:

# fit multilevel mixed-effects meta-regression model and print processing time
res <- rma.mv(yi, vi, mods = ~ condition, 
              random = list(~ 1 | article/experiment/sample/id, ~ 1 | pairing), 
              data=dat.mccurdy2020, sparse=TRUE, digits=3, time=TRUE)

# extract processing time (should take somewhere around 10-20 seconds on a modern CPU)
res$time
Load Balancing:
Several functions in the metafor package can make use of parallel processing (e.g., profile) to speed up intensive computations on machines with multiple cores. When using parallel="snow", the default is to use the parLapply function from the parallel package for this purpose. In some cases (especially when the parallelized computations take up quite variable amounts of time to complete), using ‘load balancing’ may help to speed things up further (by using the parLapplyLB function). This can be enabled with pbapply::pboptions(use_lb=TRUE) before running the function that makes use of parallel processing. Whether this really does speed things up depends on many factors and is hard to predict.

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References

Description
This page documents some recommended practices when working with the metafor package (and more generally when conducting meta-analyses).

Details
Restricted Maximum Likelihood Estimation:
When fitting models with the rma.uni and rma.mv functions, use of restricted maximum likelihood (REML) estimation is generally recommended. This is also the default setting (i.e., method="REML"). Various simulation studies have indicated that REML estimation tends to provide approximately unbiased estimates of the amount of heterogeneity (e.g., Langan et al., 2019; Veroniki et al., 2016; Viechtbauer, 2005), or more generally, of the variance components in more complex mixed-effects models (Harville, 1977).

For models fitted with the rma.uni function, the empirical Bayes / Paule-Mandel estimators (i.e., method="EB" / method="PM"), which can actually be shown to be identical to each other despite their different derivations (Viechtbauer et al., 2015), also have some favorable properties. However, these estimators do not generalize in a straightforward manner to more complex models, such as those that can be fitted with the rma.mv function.

Improved Inference Methods:
When fitting models with the rma.uni function, tests of individual model coefficients and the corresponding confidence intervals are by default (i.e., when test="z") based on a standard normal distribution, while the omnibus test is based on a chi-square distribution. These inference methods may not perform nominally (i.e., the Type I error rate of tests and the coverage rate of
confidence intervals may deviate from the chosen level), especially when the number of studies, \(k\), is low. Therefore, it is highly recommended to use the method by Hartung (1999), Sidik and Jonkman (2002), and Knapp and Hartung (2003) (the Knapp-Hartung method; also referred to as the Hartung-Knapp-Sidik-Jonkman method) by setting test="knha". Then tests of individual coefficients and confidence intervals are based on a \(t\)-distribution with \(k - p\) degrees of freedom, while the omnibus test then uses an \(F\)-distribution with \(m\) and \(k - p\) degrees of freedom (with \(m\) denoting the number of coefficients tested and \(p\) the total number of model coefficients). Various simulation studies have shown that this method works very well in providing tests and confidence intervals with close to nominal performance (e.g., Sánchez-Meca & Marín-Martínez, 2008; Viechtbauer et al., 2015).

Alternatively, one can also conduct permutation tests using the permute function. These also perform very well (and are, in a certain sense, ‘exact’ tests), but are computationally expensive. For models fitted with the rma.mv and rma.glmm functions, the Knapp-Hartung method and permutation tests are not available. Instead, one can set test="t" to also use \(t\)- and \(F\)-distributions for making inferences (although this does not involve the adjustment to the standard errors of the estimated model coefficients that is made as part of the Knapp-Hartung method). For rma.mv, one should also set dfs="contain", which uses an improved method for approximating the degrees of freedom of the \(t\)- and \(F\)-distributions.

Note that test="z" is the default for the rma.uni, rma.mv, and the rma.glmm functions. While the improved inference methods described above should ideally be the default, changing this now would break backwards compatibility.

**General Workflow for Meta-Analyses Involving Complex Dependency Structures:**

Many meta-analyses involve observed outcomes / effect size estimates that cannot be assumed to be independent, because some estimates were computed based on the same sample of subjects (or at least a partially overlapping set). In this case, one should compute the covariances for any pair of estimates that involve (fully or partially) overlapping subjects. Doing so is difficult, but we can often construct an approximate variance-covariance matrix (say \(V\)) of such dependent estimates. This can be done with the vcalc function. We can then fit a multivariate/multilevel model to the estimates with the rma.mv function, using \(V\) as the approximate var-cov matrix of the estimates and adding fixed and random effects to the model as deemed necessary. However, since \(V\) is often just a rough approximation (and since the random effects structure may not fully capture all dependencies in the underlying true outcomes/effects), we can then apply cluster-robust inference methods (also known as robust variance estimation) to the model. This can be done with the robust function, which also interfaces with the improved inference methods implemented in the clubSandwich package to obtain the cluster-robust tests and confidence intervals. Finally, we can compute predicted outcomes (with corresponding confidence intervals) and test sets of coefficients or linear combinations thereof using the predict and anova functions. See Pustejovsky and Tipton (2022) for a paper describing such a workflow for various cases.

To summarize, the general workflow therefore will often consist of these steps:

```r
# construct/approximate the var-cov matrix of dependent estimates
V <- vcalc(...)  
# fit multivariate/multilevel model with appropriate fixed/random effects
res <- rma.mv(yi, V, mods = ~ ..., random = ~ ...)  
# apply cluster-robust inference methods (robust variance estimation)
```

1 See Pustejovsky and Tipton (2022) for a paper describing such a workflow for various cases.
# note: use the improved methods from the clubSandwich package
sav <- robust(res, cluster = ..., clubSandwich = TRUE)
sav

# compute predicted outcomes (with corresponding CIs) as needed
predict(sav, ...)

# test sets of coefficients / linear combinations as needed
anova(sav, ...)

The details of how \texttt{vcalc} and \texttt{rma.mv} are used (and the clustering variable specified for \texttt{robust})
will depend on the specifics of the application.
See \texttt{dat.knapp2017} and \texttt{dat.tannersmith2016} for some examples illustrating this workflow.

**Profile Likelihood Plots to Check Parameter Identifiability:**

When fitting complex models, it is not guaranteed that all parameters of the model are identifiable (i.e., that there is a unique set of values for the parameters that maximizes the (restricted) likelihood function). For models fitted with the \texttt{rma.mv} function, this pertains especially to the variance/correlation components of the model (i.e., what is specified via the \texttt{random} argument).

Therefore, it is strongly advised in general to do post model fitting checks to make sure that the likelihood surface around the ML/REML estimates is not flat for some combination of the parameter estimates (which would imply that the estimates are essentially arbitrary). For example, one can plot the (restricted) log-likelihood as a function of each variance/correlation component in the model to make sure that each profile plot shows a clear peak at the corresponding ML/REML estimate. The \texttt{profile} function can be used for this purpose. See also Raue et al. (2009) for some further discussion of parameter identifiability and the use of profile likelihoods to check for this.

The \texttt{profile} function should also be used after fitting location-scale models with the \texttt{rma.uni} function and after fitting selection models with the \texttt{selmodel} function.

---

1 In small meta-analyses, the (denominator) degrees of freedom for the approximate t- and F-tests provided by the cluster-robust inference methods might be very low, in which case the tests may not be trustworthy and overly conservative (Joshi et al., in press). Under these circumstances, one can consider the use of cluster wild bootstrapping (as implemented in the \texttt{wildmeta} package) as an alternative method for making inferences.

**Author(s)**

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**References**


---

model.matrix.rma Extract the Model Matrix from 'rma' Objects

**Description**

The function extracts the model matrix from objects of class "rma".

**Usage**

```r
## S3 method for class 'rma'
model.matrix(object, ...)  
```

**Arguments**

- `object` an object of class "rma".
- `...` other arguments.

---

model.matrix.rma

Extract the Model Matrix from 'rma' Objects

**Description**

The function extracts the model matrix from objects of class "rma".

**Usage**

```r
## S3 method for class 'rma'
model.matrix(object, ...)  
```

**Arguments**

- `object` an object of class "rma".
- `...` other arguments.
Value

The model matrix.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.uni, rma.glmm, and rma.mv for functions to fit models for which a model matrix can be extracted.

fitted.rma for a function to extract the fitted values.

Examples

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### extract the model matrix
model.matrix(res)
Arguments

- **x**: an object of class "rma.uni".
- **exact**: logical to specify whether an exact permutation test should be carried out (the default is FALSE). See ‘Details’.
- **iter**: integer to specify the number of iterations for the permutation test when not doing an exact test (the default is 1000).
- **permci**: logical to specify whether permutation-based confidence intervals (CIs) should also be constructed (the default is FALSE). Can also be a vector of indices to specify for which coefficients a permutation-based CI should be obtained.
- **progbar**: logical to specify whether a progress bar should be shown (the default is TRUE).
- **digits**: optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
- **control**: list of control values for numerical comparisons (comptol) and for uniroot (i.e., tol and maxiter). The latter is only relevant when permci=TRUE. See ‘Note’.
- **...**: other arguments.

Details

For models without moderators, the permutation test is carried out by permuting the signs of the observed effect sizes or outcomes. The (two-sided) p-value of the permutation test is then equal to the proportion of times that the absolute value of the test statistic under the permuted data is as extreme or more extreme than under the actually observed data. See Follmann and Proschan (1999) for more details.

For models with moderators, the permutation test is carried out by permuting the rows of the model matrix (i.e., X). The (two-sided) p-value for a particular model coefficient is then equal to the proportion of times that the absolute value of the test statistic for the coefficient under the permuted data is as extreme or more extreme than under the actually observed data. Similarly, for the omnibus test, the p-value is the proportion of times that the test statistic for the omnibus test is as extreme or more extreme than the actually observed one. See Higgins and Thompson (2004) and Viechtbauer et al. (2015) for more details.

Exact versus Approximate Permutation Tests:

If exact=TRUE, the function will try to carry out an exact permutation test. An exact permutation test requires fitting the model to each possible permutation. However, the number of possible permutations increases rapidly with the number of outcomes/studies (i.e., k). For models without moderators, there are \(2^k\) possible permutations of the signs. Therefore, for \(k = 5\), there are 32 possible permutations, for \(k = 10\), there are already 1024, and for \(k = 20\), there are over one million such permutations.

For models with moderators, the increase in the number of possible permutations may be even more severe. The total number of possible permutations of the model matrix is \(k!\). Therefore, for \(k = 5\), there are 120 possible permutations, for \(k = 10\), there are 3,628,800, and for \(k = 20\), there are over \(10^{18}\) permutations of the model matrix.
Therefore, going through all possible permutations may become infeasible. Instead of using an exact permutation test, one can set `exact=FALSE` (which is also the default). In that case, the function approximates the exact permutation-based p-value(s) by going through a smaller number (as specified by the `iter` argument) of random permutations. Therefore, running the function twice on the same data can yield (slightly) different p-values. Setting `iter` sufficiently large ensures that the results become stable. For full reproducibility, one can also set the seed of the random number generator before running the function (see ‘Examples’). Note that if `exact=FALSE` and `iter` is actually larger than the number of iterations required for an exact permutation test, then an exact test will automatically be carried out.

For models with moderators, the exact permutation test actually only requires fitting the model to each unique permutation of the model matrix. The number of unique permutations will be smaller than $k!$ when the model matrix contains recurring rows. This may be the case when only including categorical moderators (i.e., factors) in the model or when any quantitative moderators included in the model can only take on a small number of unique values. When `exact=TRUE`, the function therefore uses an algorithm to restrict the test to only the unique permutations of the model matrix, which may make the use of the exact test feasible even when $k$ is large.

When using random permutations, the function ensures that the very first permutation will always correspond to the original data. This avoids p-values equal to 0.

Permutation-Based Confidence Intervals:
When `permci=TRUE`, the function also tries to obtain permutation-based confidence intervals (CIs) of the model coefficient(s). This is done by shifting the observed effect sizes or outcomes by some amount and finding the most extreme values for this amount for which the permutation-based test would just lead to non-rejection. This is computationally expensive and may take a long time to complete. For models with moderators, one can also set `permci` to a vector of indices to specify for which coefficient(s) a permutation-based CI should be obtained. When the algorithm fails to determine a particular CI bound, it will be shown as NA in the output.

Permutation Tests for Location-Scale Models:
The function also works with location-scale models (see `rma.uni` for details on such models). Permutation tests will then be carried out for both the location and scale parts of the model. However, note that permutation-based CIs are not available for location-scale models.

Value
An object of class "permutest.rma.uni". The object is a list containing the following components:

- `pval`: p-value(s) based on the permutation test.
- `QMp`: p-value for the omnibus test of moderators based on the permutation test.
- `zval.perm`: values of the test statistics of the coefficients under the various permutations.
- `b.perm`: the model coefficients under the various permutations.
- `QM.perm`: the test statistic of the omnibus test of moderators under the various permutations.
- `ci.lb`: lower bound of the confidence intervals for the coefficients (permutation-based when `permci=TRUE`).
- `ci.ub`: upper bound of the confidence intervals for the coefficients (permutation-based when `permci=TRUE`).
The results are formatted and printed with the `print` function. One can also use `coef` to obtain the table with the model coefficients, corresponding standard errors, test statistics, p-values, and confidence interval bounds. The permutation distribution(s) can be plotted with the `plot` function.

**Note**

The p-values obtained with permutation tests cannot reach conventional levels of statistical significance (i.e., $p \leq .05$) when $k$ is very small. In particular, for models without moderators, the smallest possible (two-sided) p-value is .0625 when $k = 5$ and .03125 when $k = 6$. Therefore, the permutation test is only able to reject the null hypothesis at $\alpha = .05$ when $k$ is at least equal to 6. For models with moderators, the smallest possible (two-sided) p-value for a particular model coefficient is .0833 when $k = 4$ and .0167 when $k = 5$ (assuming that each row in the model matrix is unique). Therefore, the permutation test is only able to reject the null hypothesis at $\alpha = .05$ when $k$ is at least equal to 5. Consequently, permutation-based CIs can also only be obtained when $k$ is sufficiently large.

When the number of permutations required for the exact test is so large as to be essentially indistinguishable from infinity (e.g., `factorial(200)`), the function will terminate with an error.

Determining whether a test statistic under the permuted data is as extreme or more extreme than under the actually observed data requires making $\geq$ or $\leq$ comparisons. To avoid problems due to the finite precision with which computers generally represent numbers (see this FAQ for details), the function uses a numerical tolerance (control argument `comptol`, which is set equal to `.Machine$double.eps^0.5` by default) when making such comparisons (e.g., instead of $\sqrt{3}^2 \geq 3$, which may evaluate to `FALSE`, we use $\sqrt{3}^2 \geq 3 - .Machine$double$\cdot$eps$^0.5$, which should evaluate to `TRUE`).

When obtaining permutation-based CIs, the function makes use of `uniroot`. By default, the desired accuracy is set equal to `.Machine$double$\cdot$eps$^0.25` and the maximum number of iterations to 100. The desired accuracy and the maximum number of iterations can be adjusted with the control argument (i.e., `control=list(tol=value, maxiter=value)`). Also, the interval searched for the CI bounds may be too narrow, leading to `NA` for a bound. In this case, one can try setting `control=list(distfac=value)` with a value larger than 1 to extend the interval (the value indicating a multiplicative factor by which to extend the width of the interval searched) or `control=list(extendInt="yes")` to allow `uniroot` to extend the interval dynamically.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

**References**


See Also

rma.uni for the function to fit models for which permutation tests can be conducted.
print.permutest.rma.uni and plot.permutest.rma.uni for the print and plot methods and
coefficients.permutest.rma.uni for a method to extract the model results table.

Examples

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### random-effects model
res <- rma(yi, vi, data=dat)
res

## Not run:
### permutation test (approximate and exact)
set.seed(1234) # for reproducibility
permutest(res)
permutest(res, exact=TRUE)

## End(Not run)

### mixed-effects model with two moderators (absolute latitude and publication year)
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)
res

### permutation test (approximate only; exact not feasible)
## Not run:

### permutation test (approximate)
set.seed(1234) # for reproducibility
permres <- permutest(res, iter=10000)
permres

### plot of the permutation distribution for absolute latitude
### dashed horizontal line: the observed value of the test statistic (in both tails)
### black curve: standard normal density (theoretical reference/null distribution)
### blue curve: kernel density estimate of the permutation distribution
### note: the tail area under the permutation distribution is larger
### than under a standard normal density (hence, the larger p-value)
plot(permres, beta=2, lwd=c(2,3,3,4), xlim=c(-5,5), ylim=c(0,.4))

## End(Not run)
plot.cumul.rma  

Plot Method for 'cumul.rma' Objects

Description

Plot method for objects of class "cumul.rma".

Usage

## S3 method for class 'cumul.rma'
plot(x, yaxis, xlim, ylim, xlab, ylab,
    at, transf, atransf, targs, digits, cols=c("gray80","gray10"),
    grid=TRUE, pch=19, cex=1, lwd=2, ...)

Arguments

x  an object of class "cumul.rma" obtained with cumul.
yaxis  either "tau2", "I2", or "H2" to indicate what values should be placed on the y-axis. See ‘Details’.
xlim  x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
ylim  y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
xlab  title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
ylab  title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
at  position of the x-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.
transf optional argument to specify a function to transform the summary estimates (e.g., transf=exp; see also transf). If unspecified, no transformation is used.
transf optional argument to specify a function to transform the x-axis labels (e.g., transf=exp; see also transf). If unspecified, no transformation is used.
targs optional arguments needed by the function specified via transf or atransf.
digits optional integer to specify the number of decimal places to which the tick mark labels of the x- and y-axis should be rounded. Can also be a vector of two integers, the first to specify the number of decimal places for the x-axis, the second for the y-axis labels (e.g., digits=c(2, 3)). If unspecified, the function tries to set the argument to some sensible values.
cols vector with two or more colors to use for visualizing the order of the cumulative results.
grid logical to specify whether a grid should be added to the plot. Can also be a color name.
plot.cumul.rma

pch       plotting symbol to use. By default, a filled circle is used. See points for other options.
cex       symbol expansion factor.
lwd       line width.
...       other arguments.

Details

The function can be used to visualize the results from a cumulative meta-analysis as obtained with the cumul function.

The plot shows the model estimate (i.e., the estimated overall/average outcome) on the x-axis and some measure of heterogeneity on the y-axis in the cumulative order of the results in the "cumul.rma" object. By default, $\tau^2$ is shown on the y-axis for a random-effects model and $I^2$ otherwise, but one can also use argument yaxis to specify the measure of heterogeneity to place on the y-axis.

The color gradient of the points/lines indicates the order of the cumulative results (by default, light gray at the beginning, dark gray at the end). A different set of colors can be chosen via the cols argument. See ‘Examples’.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

cumul.rma.uni for the function to conduct a cumulative meta-analysis.

Examples

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### random-effects model
res <- rma(yi, vi, data=dat)

### cumulative meta-analysis (in the order of publication year)
sav <- cumul(res, transf=exp, order=year)

### plot of model estimate and tau^2 over time
plot(sav)

### illustrate some other plot options
plot(sav, yaxis=12, ylim=c(0,100), atransf=exp, at=log(seq(1.3, 1.6, by=.1)),
     lwd=5, cex=1.5, cols=c("green","blue","red"))
plot.gosh.rma

Plot Method for 'gosh.rma' Objects

Description

Plot method for objects of class "gosh.rma".

Usage

## S3 method for class 'gosh.rma'
plot(x, het="I2", pch=16, cex=0.5, out, col, alpha, border,
xlim, ylim, xhist=TRUE, yhist=TRUE, hh=0.3, breaks,
adjust, lwd, labels, ...)

Arguments

x
an object of class "gosh.rma" obtained with gosh.

het
character string to specify the heterogeneity measure to plot. Either "I2", "H2",
"QE", or "tau2" (the last only for random/mixed-effects models).

pch
plotting symbol to use. By default, a borderless filled circle is used. See points
for other options.

cex
symbol expansion factor.

out
optional integer to specify the number of a study that may be a potential outlier.
If specified, subsets containing the specified study are drawn in a different color
than those not containing the study.

col
optional character string to specify the color to use for the points (if not provided,
points are drawn in black). When out is used, two colors should be specified
(if not provided, red is used for subsets containing the specified study and blue
otherwise).

alpha
optional alpha transparency value for the points (0 means fully transparent and
1 means opaque). If unspecified, the function tries to set this to a sensible value.

border
optional character string to specify the color to use for the borders of the his-
togram (if not provided, borders are drawn in white). Set to FALSE to omit the
borders.

xlim
x-axis limits. If unspecified, the function tries to set the x-axis limits to some
sensible values.

ylim
y-axis limits. If unspecified, the function tries to set the y-axis limits to some
sensible values.

xhist
logical to specify whether a histogram should be drawn for the x-axis (the default
is TRUE).

yhist
logical to specify whether a histogram should be drawn for the y-axis (the default
is TRUE).
optional numeric value (or vector of two values) to adjust the height of the histogram(s). Must be between 0 and 1, but should not be too close to 0 or 1, as otherwise the plot cannot be drawn.

breaks
optional argument passed on to `hist` for choosing the (number of) breakpoints of the histogram(s).

adjust
optional argument passed on to `density` for adjusting the bandwidth of the kernel density estimate(s) (values larger than 1 result in more smoothing).

lwd
optional numeric value to specify the line width of the estimated densities. Set to 0 to omit the line(s).

labels
optional argument to specify the x-axis and y-axis labels (or passed on to `pairs` to specify the names of the variables in the scatter plot matrix).

... other arguments.

Details
For models without moderators, the function draws a scatter plot of the model estimates on the x-axis against the chosen measure of heterogeneity on the y-axis. Histograms of the respective distributions (with kernel density estimates superimposed) are shown in the margins (when `xhist=TRUE` and `yhist=TRUE`).

For models with moderators, the function draws a scatter plot matrix (with the `pairs` function) of the chosen measure of heterogeneity and each of the model coefficients. Histograms of the variables plotted are shown along the diagonal, with kernel density estimates of the distributions superimposed. Arguments `xlim`, `ylim`, `xhist`, and `yhist` are then ignored (argument `hh` can then be used to compress/stretch the height of the distributions shown along the diagonal).

Author(s)
Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also
gosh.rma for the function to create the input to a GOSH plot.

Examples
```r
### calculate log odds ratios and corresponding sampling variances
dat <- escalc(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat.egger2001)
```

### meta-analysis of all trials including ISIS-4 using an equal-effects model
res <- rma(yi, vi, data=dat, method="EE")

### fit FE model to all possible subsets (65535 models)
## Not run:
sav <- gosh(res, progbar=FALSE)

### create GOSH plot
### red points for subsets that include and blue points
### for subsets that exclude study 16 (the ISIS-4 trial)
plot(sav, out=16, breaks=100)

## End(Not run)

---

### plot.infl.rma.uni

Plot Method for 'infl.rma.uni' Objects

#### Description
Plot method for objects of class "infl.rma.uni".

#### Usage
```r
## S3 method for class 'infl.rma.uni'
plot(x, plotinf=TRUE, plotdfbs=FALSE, dfbsnew=FALSE, logcov=TRUE,
     layout, slab.style=1, las=0, pch=21, bg="black",
     bg.infl="red", col.na="lightgray", ...)
```

#### Arguments
- **x**: an object of class "infl.rma.uni" obtained with `influence`
- **plotinf**: logical to specify whether the various case diagnostics should be plotted (the default is TRUE). Can also be a vector of up to 8 integers to specify which plots to draw. See ‘Details’ for the numbers corresponding to the various plots.
- **plotdfbs**: logical to specify whether the DFBETAS values should be plotted (the default is FALSE). Can also be a vector of integers to specify for which coefficient(s) to plot the DFBETAS values.
- **dfbsnew**: logical to specify whether a new device should be opened for plotting the DFBETAS values (the default is FALSE).
- **logcov**: logical to specify whether the covariance ratios should be plotted on a log scale (the default is TRUE).
- **layout**: optional vector of two numbers to specify the number of rows and columns for the layout of the figure.
- **slab.style**: integer to indicate the style of the x-axis labels: 1 = study number, 2 = study label, 3 = abbreviated study label. Note that study labels, even when abbreviated, may be too long to fit in the margins.)
plot.infl.rma.uni

las  integer between 0 and 3 to specify the alignment of the axis labels (see \texttt{par}). The most useful alternative to 0 is 3, so that the x-axis labels are drawn vertical to the axis.

pch  plotting symbol to use. By default, a filled circle is used. See \texttt{points} for other options.

bg   color to use for filling the plotting symbol (the default is "black").

bg.infl  color to use for filling the plotting symbol when the point is considered influential (the default is "red").

col.na  color to use for lines connecting two points with NA values in between (the default is "lightgray").

\ldots  other arguments.

Details

When \texttt{plotinf=TRUE}, the function plots the (1) externally standardized residuals, (2) DFFITS values, (3) Cook’s distances, (4) covariance ratios, (5) leave-one-out $\tau^2$ estimates, (6) leave-one-out (residual) heterogeneity test statistics, (7) hat values, and (8) weights. If \texttt{plotdfbss=TRUE}, the DFBETAS values are also plotted either after confirming the page change (if \texttt{dfbssnew=FALSE}) or on a separate device (if \texttt{dfbssnew=TRUE}).

A case (which is typically synonymous with study) may be considered to be ‘influential’ if at least one of the following is true:

- The absolute DFFITS value is larger than $3 \times \sqrt{p/(k - p)}$, where $p$ is the number of model coefficients and $k$ the number of cases.
- The lower tail area of a chi-square distribution with $p$ degrees of freedom cut off by the Cook’s distance is larger than 50%.
- The hat value is larger than $3 \times (p/k)$.
- Any DFBETAS value is larger than 1.

Cases which are considered influential with respect to any of these measures are indicated by the color specified for the \texttt{bg.infl} argument (the default is "red").

The cut-offs described above are indicated in the plot with horizontal reference lines. In addition, on the plot of the externally standardized residuals, horizontal reference lines are drawn at -1.96, 0, and 1.96. On the plot of the hat values, a horizontal reference line is drawn at $p/k$. Since the sum of the hat values is equal to $p$, the value $p/k$ indicates equal hat values for all $k$ cases. Finally, on the plot of weights, a horizontal reference line is drawn at $100/k$, corresponding to the value for equal weights (in %) for all $k$ cases. Note that all weights will automatically be equal to each other when using unweighted model fitting. Also, the hat values will be equal to the weights values (except for their scaling) in models without moderators.

The chosen cut-offs are (somewhat) arbitrary. Substantively informed judgment should always be used when examining the influence of each case on the results.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> \url{https://www.metafor-project.org}
References


See Also

[influence.rma.uni](#) for the function to compute the various model diagnostics.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### compute the diagnostics
inf <- influence(res)

### plot the values
plot(inf)

### select which plots to show
plot(inf, plotinf=1:4)
plot(inf, plotinf=1:4, layout=c(4,1))

### plot the DFBETAS values
plot(inf, plotinf=FALSE, plotdfbs=TRUE)
```

---

**plot.permutest.rma.uni**

*Plot Method for 'permutest.rma.uni' Objects*

Description

Plot method for objects of class "permutest.rma.uni".

Usage

```r
## S3 method for class 'permutest.rma.uni'
plot(x, beta, alpha, QM=FALSE, QS=FALSE,
     breaks="Scott", freq=FALSE, col="gray", border="white", trim=0,
     col.out=rgb(1,0,0,0.5), col.ref="black", col.density="blue",
     adjust=1, lwd=c(2,0,0,4), layout, ...)
```
Arguments

- **x**: an object of class "permutest.rma.uni" obtained with `permutest`.
- **beta**: optional vector of indices to specify which (location) coefficients should be plotted.
- **alpha**: optional vector of indices to specify which scale coefficients should be plotted. Only relevant for location-scale models (see `rma.uni`).
- **QM**: logical to specify whether the permutation distribution of the omnibus test of the (location) coefficients should be plotted (the default is FALSE).
- **QS**: logical to specify whether the permutation distribution of the omnibus test of the scale coefficients should be plotted (the default is FALSE). Only relevant for location-scale models (see `rma.uni`).
- **breaks**: argument to be passed on to the corresponding argument of `hist` to set (the method for determining) the (number of) breakpoints.
- **freq**: logical to indicate whether frequencies or probability densities should be plotted (the default is FALSE to plot densities).
- **col**: character string to specify the color for the bars (the default is gray).
- **border**: character string to specify the color for the border around the bars (the default is white).
- **trim**: the fraction (up to 0.5) of observations to be trimmed from the tails of each permutation distribution before its histogram is plotted.
- **col.out**: character string to specify the color for the bars that are more extreme than the observed test statistic (the default is a semi-transparent shade of red).
- **col.ref**: character string to specify the color of the theoretical reference/null distribution that is superimposed on top of the histogram (the default is black).
- **col.density**: character string to specify the color of the kernel density estimate of the permutation distribution that is superimposed on top of the histogram (the default is blue).
- **adjust**: numeric value to be passed on to the corresponding argument of `density` (for adjusting the bandwidth of the kernel density estimate).
- **lwd**: numeric vector to specify the width of the vertical lines corresponding to the value of the observed test statistic, of the reference/null distribution, of the density estimate, and of the vertical line at 0 (note: by default, the reference/null distribution and the density estimate both have a line width of 0 and are therefore not plotted).
- **layout**: optional vector of two numbers to specify the number of rows and columns for the layout of the figure.
- `...`: other arguments.

Details

The function plots the permutation distribution of each model coefficient as a histogram.

For models with moderators, one can choose via argument `beta` which coefficients to plot (by default, all permutation distributions except that of the intercept are plotted). One can also choose to plot the permutation distribution of the omnibus test of the model coefficients (by setting `QM=TRUE`).
Arguments `breaks`, `freq`, `col`, and `border` are passed on to the `hist` function for the plotting. Argument `trim` can be used to trim away a certain fraction of observations from the tails of each permutation distribution before its histogram is plotted. By setting this to a value above 0, one can quickly remove some of the extreme values that might lead to the bulk of the distribution getting squished together at the center (typically, a small value such as `trim=.01` is sufficient for this purpose).

The observed test statistic is indicated as a vertical dashed line (in both tails for a two-sided test). Argument `col.out` is used to specify the color for the bars in the histogram that are more extreme than the observed test statistic. The p-value of a permutation test corresponds to the area of these bars.

One can superimpose the theoretical reference/null distribution on top of the histogram (i.e., the distribution as assumed by the model). The p-value for the standard (i.e., non-permutation) test is the area that is more extreme than the observed test statistic under this reference/null distribution.

A kernel density estimate of the permutation distribution can also be superimposed on top of the histogram (as a smoothed representation of the permutation distribution).

Note that the theoretical reference/null distribution and the kernel density estimate of the permutation distribution are only shown when setting the line width for these elements greater than 0 via the `lwd` argument (e.g., `lwd=c(2,2,2,4)`).

For location-scale models (see `rma.uni` for details), one can also use arguments `alpha` and `QS` to specify which scale coefficients to plot and whether to also plot the permutation distribution of the omnibus test of the scale coefficients (by setting `QS=TRUE`).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

`permutest.rma.uni` for the function to create `permutest.rma.uni` objects.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### random-effects model
res <- rma(yi, vi, data=dat)
res

### Not run:
### permutation test (exact)
set.seed(1234) # for reproducibility
permres <- permutest(res, exact=TRUE)
```
### Mixed-effects model with two moderators (absolute latitude and publication year)

```
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)
```

### Permutation test (approximate)

```
set.seed(1234) # for reproducibility
permres <- permutest(res, iter=10000)
```

### Plot of the permutation distribution for absolute latitude

```
plot(permres, beta=2, lwd=c(2,3,3,4), xlim=c(-5,5))
```

## End(Not run)

---

### Description

Plot method for objects of class "rma.uni", "rma.mh", "rma.peto", and "rma.glmm".

### Usage

```
## S3 method for class 'rma.uni'
plot(x, qqplot=FALSE, ...)

## S3 method for class 'rma.mh'
plot(x, qqplot=FALSE, ...)

## S3 method for class 'rma.peto'
plot(x, qqplot=FALSE, ...)

## S3 method for class 'rma.glmm'
plot(x, qqplot=FALSE, ...)
```

### Arguments

- **x**: an object of class "rma.uni", "rma.mh", or "rma.peto". The method is not yet implemented for objects of class "rma.glmm".
qqplot logical to specify whether a normal QQ plot should be drawn (the default is FALSE).

... other arguments.

Details

Four plots are produced. If the model does not contain any moderators, then a forest plot, funnel plot, radial plot, and a plot of the standardized residuals is provided. If qqplot=TRUE, the last plot is replaced by a normal QQ plot of the standardized residuals.

If the model contains moderators, then a forest plot, funnel plot, plot of the standardized residuals against the fitted values, and a plot of the standardized residuals is provided. If qqplot=TRUE, the last plot is replaced by a normal QQ plot of the standardized residuals.

Note

If the number of studies is large, the forest plot may become difficult to read due to the small font size. Stretching the plotting device vertically should provide more space.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

*forest* for forest plots, *funnel* for funnel plots, *radial* for radial plots, and *qqnorm.rma.uni* for normal QQ plots.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)

### plot results
plot(res, qqplot=TRUE)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### plot results
plot(res, qqplot=TRUE)
```
**plot.rma.uni.selmodel**  
*Plot Method for 'plot.rma.uni.selmodel' Objects*

**Description**

Plot method for objects of class "plot.rma.uni.selmodel".

**Usage**

```r
## S3 method for class 'rma.uni.selmodel'
plot(x, xlim, ylim, n=1000, prec="max", scale=FALSE,
     ci=FALSE, reps=1000, rug=TRUE, add=FALSE,
     lty=c("solid","dotted"), lwd=c(2,1), ...)
```

**Arguments**

- `x`: an object of class "rma.uni.selmodel" obtained with `selmodel`.
- `xlim`: x-axis limits. Essentially the range of p-values for which the selection function should be drawn. If unspecified, the function sets the limits automatically.
- `ylim`: y-axis limits. If unspecified, the function sets the limits automatically.
- `n`: numeric value to specify for how many p-values within the x-axis limits the function value should be computed (the default is 1000).
- `prec`: either a character string (with options "max", "min", "mean", or "median") or a numeric value. See 'Details'.
- `scale`: logical to specify whether the function values should be rescaled to a 0 to 1 range (the default is FALSE).
- `ci`: logical to specify whether a confidence interval should be drawn around the selection function (the default is FALSE). Can also be a string (with options "boot" or "wald"). See 'Details'.
- `reps`: numeric value to specify the number of bootstrap samples to draw for generating the confidence interval bounds (the default is 1000).
- `rug`: logical to specify whether the observed p-values should be added as tick marks on the x-axis (the default is TRUE).
- `add`: logical to specify whether the function should be added to an existing plot (the default is FALSE).
- `lty`: the line types for the selection function and the confidence interval bounds.
- `lwd`: the line widths for the selection function and the confidence interval bounds.
- `...`: other arguments.
Details

The function can be used to draw the estimated selection function based on objects of class "plot.rma.uni.selmodel". When the selection function incorporates a measure of precision (which, strictly speaking, is really a measure of imprecision), one can specify for which level of precision the selection function should be drawn. When prec="max", then the function is drawn for the least precise study (maximum imprecision), when prec="min", then the function is drawn for the most precise study (minimum imprecision), while prec="mean" and prec="median" will show the function for the mean and median level of imprecision, respectively. Alternatively, one can specify a numeric value for argument prec to specify the precision value (where prec="max" corresponds to prec=1 and higher levels of precision to prec values below 1).

When ci=TRUE (or equivalently, ci="boot"), a confidence interval is drawn around the selection function. The bounds of this interval are generated using parametric bootstrapping, with argument reps controlling the number of bootstrap samples to draw for generating the confidence interval bounds. When both n and reps are large, constructing the confidence interval can take a few moments to complete.

For models where the selection function involves a single $\delta$ parameter, one can also set ci="wald", in which case the confidence interval will be constructed based on the Wald-type CI of the $\delta$ parameter (doing so is much quicker than using parametric bootstrapping). This option is also available for step function models (even if they involve multiple $\delta$ parameters).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

selmodel.rma.uni for the function to fit models for which the estimated selection function can be drawn.

Examples

```r
# copy data into 'dat' and examine data
dat <- dat.hackshaw1998

# fit random-effects model using the log odds ratios
res <- rma(yi, vi, data=dat, method="ML")
res

# fit step selection model
sel1 <- selmodel(res, type="stepfun", steps=c(0.05, 0.10, 0.50, 1.00))

# plot selection function
plot(sel1, scale=TRUE)
```
### fit negative exponential selection model
sel2 <- selmodel(res, type="negexp")

### add selection function to the existing plot
plot(sel2, add=TRUE, col="blue")

### plot selection function with CI
plot(sel1, ci="wald")

---

**Description**

Plot method for objects of class "vif.rma".

**Usage**

```r
## S3 method for class 'vif.rma'
plot(x, breaks="Scott", freq=FALSE, col="gray", border="white", trim=0,
     col.out=rgb(1,0,0,0.5), col.density="blue", adjust=1, lwd=c(2,0), layout, ...)
```

**Arguments**

- `x`: an object of class "vif.rma" obtained with `vif`.
- `breaks`: argument to be passed on to the corresponding argument of `hist` to set the (number of) breakpoints.
- `freq`: logical to indicate whether frequencies or probability densities should be plotted (the default is `FALSE` to plot densities).
- `col`: character string to specify the color for the bars (the default is gray).
- `border`: character string to specify the color for the border around the bars (the default is white).
- `trim`: the fraction (up to 0.5) of observations to be trimmed from the upper tail of each distribution before its histogram is plotted.
- `col.out`: character string to specify the color for the bars that are more extreme than the observed (G)VIF value (the default is a semi-transparent shade of red).
- `col.density`: character string to specify the color of the kernel density estimate of the distribution that is superimposed on top of the histogram (the default is blue).
- `adjust`: numeric value to be passed on to the corresponding argument of `density` (for adjusting the bandwidth of the kernel density estimate).
- `lwd`: numeric vector to specify the width of the vertical lines corresponding to the value of the observed (G)VIFs and of the density estimate (note: by default, the density estimate has a line width of 0 and is therefore not plotted).
- `layout`: optional vector of two numbers to specify the number of rows and columns for the layout of the figure.
- `...`: other arguments.
Details

The function plots the distribution of each (G)VIF as simulated under independence as a histogram. Arguments breaks, freq, col, and border are passed on to the hist function for the plotting. Argument trim can be used to trim away a certain fraction of observations from the upper tail of each distribution before its histogram is plotted. By setting this to a value above 0, one can quickly remove some of the extreme values that might lead to the bulk of the distribution getting squished together at the left (typically, a small value such as trim=.01 is sufficient for this purpose). The observed (G)VIF value is indicated as a vertical dashed line. If the observed exceeds the upper plot limit, then this is indicated by an arrow pointing to the line.

Argument col.out is used to specify the color for the bars in the histogram that are more extreme than the observed (G)VIF value.

A kernel density estimate of the distribution can be superimposed on top of the histogram (as a smoothed representation of the distribution). Note that the kernel density estimate of the distribution is only shown when setting the line width for this element greater than 0 via the lwd argument (e.g., lwd=c(2,2)).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

vif.rma for the function to create vif.rma objects.

Examples

### copy data from Bangert-Drowns et al. (2004) into 'dat'
dat <- dat.bangertdrowns2004

### fit mixed-effects meta-regression model
res <- rma(yi, vi, mods = ~ length + wic + feedback + info + pers + imag + meta, data=dat)

### use the simulation approach to analyze the size of the VIFs
## Not run:
vifs <- vif(res, sim=TRUE)
vifs

### plot the simulated distributions of the VIFs
plot(vifs)

### add densities, trim away some extremes, and set break points
plot(vifs, lwd=c(2,2), trim=.01, breaks=seq(1,2.2,by=.05), adjust=1.5)

## End(Not run)
predict.rma

Predicted Values for 'rma' Objects

Description

The function computes predicted values, corresponding standard errors, confidence intervals, and prediction intervals for objects of class "rma".

Usage

## S3 method for class 'rma'
predict(object, newmods, intercept, tau2.levels, gamma2.levels, addx=FALSE, level, digits, transf, targs, vcov=FALSE, ...)

## S3 method for class 'rma.ls'
predict(object, newmods, intercept, addx=FALSE, newscale, addz=FALSE, level, digits, transf, targs, vcov=FALSE, ...)

Arguments

- **object**
  - an object of class "rma" or "rma.ls".

- **newmods**
  - optional vector or matrix to specify the values of the moderator values for which the predicted values should be calculated. See 'Details'.

- **intercept**
  - logical to specify whether the intercept should be included when calculating the predicted values for newmods. If unspecified, the intercept is automatically added when the original model also included an intercept.

- **tau2.levels**
  - vector to specify the levels of the inner factor when computing prediction intervals. Only relevant for models of class "rma.mv" (see rma.mv) and when the model includes more than a single \( \tau^2 \) value. See 'Details'.

- **gamma2.levels**
  - vector to specify the levels of the inner factor when computing prediction intervals. Only relevant for models of class "rma.mv" (see rma.mv) and when the model includes more than a single \( \gamma^2 \) value. See 'Details'.

- **addx**
  - logical to specify whether the values of the moderator variables should be added to the returned object. See 'Examples'.

- **newscale**
  - optional vector or matrix to specify the values of the scale variables for which the predicted values should be calculated. Only relevant for location-scale models (see rma.uni). See 'Details'.

- **addz**
  - logical to specify whether the values of the scale variables should be added to the returned object.

- **level**
  - numeric value between 0 and 100 to specify the confidence and prediction interval level. If unspecified, the default is to take the value from the object.

- **digits**
  - optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
predict.rma

transf
optional argument to specify a function to transform the predicted values and interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

targs
optional arguments needed by the function specified under transf.

vcov
logical to specify whether the variance-covariance matrix of the predicted values should also be returned (the default is FALSE).

Details

For an equal-effects model, predict(object) returns the estimated (average) outcome in the set of studies included in the meta-analysis. This is the same as the estimated intercept in the equal-effects model (i.e., \( \hat{\theta} \)).

For a random-effects model, predict(object) returns the estimated (average) outcome in the hypothetical population of studies from which the set of studies included in the meta-analysis are assumed to be a random selection. This is the same as the estimated intercept in the random-effects model (i.e., \( \hat{\mu} \)).

For models including one or more moderators, predict(object) returns the estimated (average) outcomes for values of the moderator(s) equal to those of the \( k \) studies included in the meta-analysis (i.e., the ‘fitted values’ for the \( k \) studies).

For models including \( p' \) moderator variables, new moderator values (for \( k_{\text{new}} \) hypothetical new studies) can be specified by setting newmods equal to a \( k_{\text{new}} \times p' \) matrix with the corresponding new moderator values. If the model object included an intercept, then it should not be explicitly specified under newmods, as it will be added by default (unless one sets intercept=FALSE). Also, any factors in the original model get turned into the appropriate contrast variables within the rma function, so that newmods should actually include the values for the contrast variables. Examples are shown below.

For random/mixed-effects models, an approximate prediction interval is also constructed (Riley et al., 2011). The interval estimates where level % of the true effect sizes or outcomes fall in the hypothetical population of studies (and hence where the true effect or outcome of a new study from the population of studies should fall in level % of the cases).

For random-effects models that were fitted with the rma.mv function, the model may actually include multiple \( \tau^2 \) values (i.e., when the random argument includes an ‘~ inner | outer’ term and struct="HCS", struct="DIAG", struct="HAR", or struct="UN"). In that case, the function will provide prediction intervals for each level of the inner factor (since the prediction intervals differ depending on the \( \tau^2 \) value). Alternatively, one can use the tau2.levels argument to specify for which level(s) the prediction interval should be provided. If the model includes a second ‘~ inner | outer’ term with multiple \( \gamma^2 \) values, prediction intervals for each combination of levels of the inner factors will be provided. Alternatively, one can use the tau2.levels and gamma2.levels arguments to specify for which level combination(s) the prediction interval should be provided.

When using the newmods argument for mixed-effects models that were fitted with the rma.mv function, if the model includes multiple \( \tau^2 \) (and multiple \( \gamma^2 \)) values, then one must use the tau2.levels (and gamma2.levels) argument to specify the levels of the inner factor(s) (i.e., a vector of length \( k_{\text{new}} \)) to obtain the appropriate prediction interval(s).

For location-scale models fitted with the rma.uni function, one can use newmods to specify the values of the \( p' \) moderator variables included in the model and newscale to specify the values of the \( q' \)
scale variables included in the model. Whenever newmods is specified, the function computes predicted effects/outcomes for the specified moderators values. To obtain the corresponding prediction intervals, one must also specify the corresponding newscale values. If only newscale is specified (and not newmods), the function computes the predicted log-transformed \( \tau^2 \) values (when using a log link) for the specified scale values. By setting transf=exp, one can then obtain the predicted \( \tau^2 \) values.

Value

An object of class c("predict.rma","list.rma"). The object is a list containing the following components:

- pred: predicted value(s).
- se: corresponding standard error(s).
- ci.lb: lower bound of the confidence interval(s).
- ci.ub: upper bound of the confidence interval(s).
- pi.lb: lower bound of the prediction interval(s) (only for random/mixed-effects models).
- pi.ub: upper bound of the prediction interval(s) (only for random/mixed-effects models).
- tau2.level: the level(s) of the inner factor (only for models of class "rma.mv" with multiple \( \tau^2 \) values).
- gamma2.level: the level(s) of the inner factor (only for models of class "rma.mv" with multiple \( \gamma^2 \) values).
- X: the moderator value(s) used to calculate the predicted values (only when addx=TRUE).
- Z: the scale value(s) used to calculate the predicted values (only when addz=TRUE and only for location-scale models).
- ...: some additional elements/values.

If vcov=TRUE, then the returned object is a list with the first element equal to the one as described above and the second element equal to the variance-covariance matrix of the predicted values.

The object is formatted and printed with the print function. To format the results as a data frame, one can use the as.data.frame function.

Note

Confidence and prediction intervals are constructed based on the critical values from a standard normal distribution (i.e., \( \pm 1.96 \) for level=95). When the model was fitted with test="t" or test="knha", then a t-distribution with \( k - p \) degrees of freedom is used.

For a random-effects model (where \( p = 1 \)) fitted with the rma.uni function, note that this differs slightly from Riley et al. (2001), who suggest to use a t-distribution with \( k - 2 \) degrees of freedom for constructing the prediction interval. Neither a normal, nor a t-distribution with \( k - 1 \) or \( k - 2 \) degrees of freedom is correct; all of these are approximations. The computations are done in the way described above, so that the prediction interval is identical to the confidence interval when \( \hat{\tau}^2 = 0 \), which could be argued is the logical thing that should happen. If the prediction interval should be computed exactly as described by Riley et al. (2001), then one can use argument pi.type="riley".
The predicted values are based only on the fixed effects of the model. Best linear unbiased predictions (BLUPs) that combine the fitted values based on the fixed effects and the estimated contributions of the random effects can be obtained with `blup` (currently only for objects of class "rma.uni").

When using the `transf` option, the transformation is applied to the predicted values and the corresponding interval bounds. The standard errors are omitted from the printed output. Also, `vcov=TRUE` is ignored when using the `transf` option.

### Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

### References


Riley, R. D., Higgins, J. P. T., & Deeks, J. J. (2011). Interpretation of random effects meta-analyses. *British Medical Journal, 342*, d549. [https://doi.org/10.1136/bmj.d549](https://doi.org/10.1136/bmj.d549)


### See Also

`fitted.rma` for a function to extract the fitted values, `blup.rma.uni` for a function to compute BLUPs that combine the fitted values and predicted random effects, and `addpoly.predict.rma` to add polygons based on predicted values to a forest plot.

### Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)

### average risk ratio with 95% CI
predict(res, transf=exp)

### fit mixed-effects model with absolute latitude as a moderator
res <- rma(yi, vi, mods = ~ ablat, data=dat)

### predicted average risk ratios for given absolute latitude values
predict(res, transf=exp, addx=TRUE)

### predicted average risk ratios for 10-60 degrees absolute latitude
predict(res, newmods=c(10, 20, 30, 40, 50, 60), transf=exp, addx=TRUE)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)
```
### predicted average risk ratios for 10 and 60 degrees latitude in 1950 and 1980
predict(res, newmods=cbind(c(10,60,10,60),c(1950,1950,1980,1980)), transf=exp, addx=TRUE)

### fit mixed-effects model with two moderators (one of which is a factor)
res <- rma(yi, vi, mods = ~ ablat + factor(alloc), data=dat)

### examine how the factor was actually coded for the studies in the dataset
predict(res, addx=TRUE)

### predicted average risk ratios at 30 degrees for the three factor levels
### note: the contrast (dummy) variables need to specified explicitly here
predict(res, newmods=c(30, 0, 0), addx=TRUE)  # for alternate allocation
predict(res, newmods=c(30, 1, 0), addx=TRUE)  # for random allocation
predict(res, newmods=c(30, 0, 1), addx=TRUE)  # for systematic allocation

### can also use named vector with arbitrary order and abbreviated variable names
predict(res, newmods=c(sys=0, ran=0, abl=30))
predict(res, newmods=c(sys=0, ran=1, abl=30))
predict(res, newmods=c(sys=1, ran=0, abl=30))

---

**print.anova.rma**

**Print Method for 'anova.rma' and 'list.anova.rma' Objects**

**Description**

Print method for objects of class "anova.rma".

**Usage**

```r
## S3 method for class 'anova.rma'
print(x, digits=x$digits, ...)
## S3 method for class 'list.anova.rma'
print(x, digits=x[[1]]$digits, ...)
```

**Arguments**

- `x` an object of class "anova.rma" or "list.anova.rma" obtained with `anova`.
- `digits` integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `...` other arguments.

**Details**

For a Wald-type test of one or multiple model coefficients, the output includes the test statistic (either a chi-square or F-value) and the corresponding p-value.

When testing one or multiple contrasts, the output includes the estimated value of the contrast, its standard error, test statistic (either a z- or a t-value), and the corresponding p-value.

When comparing two model objects, the output includes:
- the number of parameters in the full and the reduced model.
- the AIC, BIC, AICc, and log-likelihood of the full and the reduced model.
- the value of the likelihood ratio test statistic.
- the corresponding p-value.
- the test statistic of the test for (residual) heterogeneity for the full and the reduced model.
- the estimate of \( \tau^2 \) from the full and the reduced model. Suppressed for equal-effects models.
- amount (in percent) of heterogeneity in the reduced model that is accounted for in the full model (NA for "rma.mv" objects). This can be regarded as a pseudo \( R^2 \) statistic (Raudenbush, 2009). Note that the value may not be very accurate unless \( k \) is large (Lopez-Lopez et al., 2014).

The last two items are not provided when comparing "rma.mv" models.

**Value**

The function does not return an object.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

**References**


**See Also**

anova.rma for the function to create anova.rma objects.
Print Methods for 'confint.rma' and 'list.confint.rma' Objects

Description

Print methods for objects of class "confint.rma" and "list.confint.rma".

Usage

## S3 method for class 'confint.rma'
print(x, digits=x$digits, ...)
## S3 method for class 'list.confint.rma'
print(x, digits=x$digits, ...)

Arguments

x
  an object of class "confint.rma" or "list.confint.rma" obtained with confint.
digits
  integer to specify the number of decimal places to which the printed results
  should be rounded (the default is to take the value from the object).
...
  other arguments.

Details

The output includes:

- estimate of the model coefficient or variance/correlation parameter
- lower bound of the confidence interval
- upper bound of the confidence interval

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

confint.rma.uni and confint.rma.mv for the functions to create confint.rma and list.confint.rma objects.
Description

Print and summary methods for objects of class "escalc".

Usage

## S3 method for class 'escalc'
print(x, digits=attr(x,"digits"), ...)

## S3 method for class 'escalc'
summary(object, out.names=c("sei","zi","pval","ci.lb","ci.ub"), var.names,
         H0=0, append=TRUE, replace=TRUE, level=95, olim, digits, transf, ...)

Arguments

x an object of class "escalc" obtained with escalc.
object an object of class "escalc" obtained with escalc.
digits integer to specify the number of decimal places to which the printed results
should be rounded (the default is to take the value from the object).
oun.names character string with four elements to specify the variable names for the standard
effects, test statistics, and lower/upper confidence interval bounds.
var.names character string with two elements to specify the variable names for the observed
effect sizes or outcomes and the sampling variances (the default is to take the
value from the object if possible).
H0 numeric value to specify the value of the effect size or outcome under the null hypothesis (the default is 0).
append logical to specify whether the data frame specified via the object argument
should be returned together with the additional variables that are calculated by
the summary function (the default is TRUE).
replace logical to specify whether existing values for sei, zi, ci.lb, and ci.ub in the
data frame should be replaced. Only relevant when the data frame already
contains these variables. If replace=TRUE (the default), all of the existing values
will be overwritten. If replace=FALSE, only NA values will be replaced.
level numeric value between 0 and 100 to specify the confidence interval level (the
default is 95).
olim optional argument to specify observation/outcome limits. If unspecified, no lim-
its are used.
transf optional argument to specify a function to transform the observed effect sizes or
outcomes and interval bounds (e.g., transf=exp; see also transf). If unspecified,
no transformation is used. Any additional arguments needed for the function
specified here can be passed via ...

... other arguments.
Value

The `print.escalc` function formats and prints the data frame, so that the observed effect sizes or outcomes and sampling variances are rounded (to the number of digits specified).

The `summary.escalc` function creates an object that is a data frame containing the original data (if `append=TRUE`) and the following components:

- `yi`: observed effect sizes or outcomes (transformed if `transf` is specified).
- `vi`: corresponding sampling variances.
- `sei`: corresponding standard errors.
- `zi`: test statistics for testing $H_0: \theta_i = H_0$ (i.e., $(yi-H0)/sei$).
- `pval`: corresponding p-values.
- `ci.lb`: lower confidence interval bounds (transformed if `transf` is specified).
- `ci.ub`: upper confidence interval bounds (transformed if `transf` is specified).

When the `transf` argument is specified, elements `vi`, `sei`, `zi`, and `pval` are not included (since these only apply to the untransformed effect sizes or outcomes).

Note that the actual variable names above depend on the `out.names` (and `var.names`) arguments. If the data frame already contains variables with names as specified by the `out.names` argument, the values for these variables will be overwritten when `replace=TRUE` (which is the default). By setting `replace=FALSE`, only values that are `NA` will be replaced.

The `print.escalc` function again formats and prints the data frame, rounding the added variables to the number of digits specified.

Note

If some transformation function has been specified for the `transf` argument, then `yi`, `ci.lb`, and `ci.ub` will be transformed accordingly. However, `vi` and `sei` then still reflect the sampling variances and standard errors of the untransformed values.

The `summary.escalc` function computes level % Wald-type confidence intervals, which may or may not be the most accurate method for computing confidence intervals for the chosen effect size or outcome measure.

If the outcome measure used is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the `olim` argument to enforce those observation/outcome limits (the observed outcomes and confidence intervals cannot exceed those bounds then).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References

See Also

`escalc` for the function to create `escalc` objects.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)
dat

### apply summary function
summary(dat)
summary(dat, transf=exp)
```

---

print.fsn

*Print Method for 'fsn' Objects*

Description

Print method for objects of class "fsn".

Usage

```r
## S3 method for class 'fsn'
print(x, digits=x$digits, ...)
```

Arguments

- `x` an object of class "fsn" obtained with `fsn`.
- `digits` integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `...` other arguments.

Details

The output shows the results from the fail-safe N calculation.

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer `<wvb@metafor-project.org>` [https://www.metafor-project.org]

References

print.gosh.rma

See Also

gosh for the function to create gosh objects.

print.gosh.rma Print Method for 'gosh.rma' Objects

Description

Print method for objects of class "gosh.rma".

Usage

## S3 method for class 'gosh.rma'
print(x, digits=x$digits, ...)

Arguments

x an object of class "gosh.rma" obtained with gosh.
digits integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
... other arguments.

Details

The output shows how many model fits were attempted, how many succeeded, and summary statistics (i.e., the mean, minimum, first quartile, median, third quartile, and maximum) for the various measures of (residual) heterogeneity and the model coefficient(s) computed across all of the subsets.

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

gosh.rma for the function to create gosh.rma objects.
Print Method for 'hc.rma.uni' Objects

Description

Print method for objects of class "hc.rma.uni".

Usage

```r
## S3 method for class 'hc.rma.uni'
print(x, digits=x$digits, ...)
```

Arguments

- `x` an object of class "hc.rma.uni" obtained with `hc`.
- `digits` integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `...` other arguments.

Details

The output is a data frame with two rows, the first (labeled `rma`) corresponding to the results based on the usual estimation method, the second (labeled `hc`) corresponding to the results based on the method by Henmi and Copas (2010). The data frame includes the following variables:

- the method used to estimate $\tau^2$ (always DL for `hc`)
- the estimated amount of heterogeneity
- the estimated average true outcome
- the corresponding standard error (NA when `transf` argument has been used)
- the lower and upper confidence interval bounds

Value

The function returns the data frame invisibly.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

- `hc.rma.uni` for the function to create `hc.rma.uni` objects.
print.list.rma

Description

Print method for objects of class "list.rma".

Usage

## S3 method for class 'list.rma'
print(x, digits=x$digits, ...)

Arguments

x an object of class "list.rma".
digits integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
...
other arguments.

Value

See the documentation of the function that creates the "list.rma" object for details on what is printed. Regardless of what is printed, a data frame with the results is also returned invisibly. See methods.list.rma for some additional method functions for "list.rma" objects.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


print.matreg

Print Method for 'matreg' Objects

Description

Print method for objects of class "matreg".

Usage

## S3 method for class 'matreg'
print(x, digits=x$digits,
    signif.stars=getOption("show.signif.stars"), signif.legend=signif.stars, ...)

print.matreg

Print Method for 'matreg' Objects

Description

Print method for objects of class "matreg".

Usage

## S3 method for class 'matreg'
print(x, digits=x$digits,
    signif.stars=getOption("show.signif.stars"), signif.legend=signif.stars, ...)

print.matreg

Print Method for 'matreg' Objects

Description

Print method for objects of class "matreg".

Usage

## S3 method for class 'matreg'
print(x, digits=x$digits,
    signif.stars=getOption("show.signif.stars"), signif.legend=signif.stars, ...)
Arguments

x

an object of class "matreg" obtained with \texttt{matreg}.

digits

integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

signif.stars

logical to specify whether p-values should be encoded visually with ‘significance stars’. Defaults to the \texttt{show.signif.stars} slot of \texttt{options}.

signif.legend

logical to specify whether the legend for the ‘significance stars’ should be printed. Defaults to the value for \texttt{signif.stars}.

...

other arguments.

Details

The output is a table with the estimated coefficients, corresponding standard errors, test statistics, p-values, and confidence interval bounds.

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

See Also

\texttt{matreg} for the function to create \texttt{matreg} objects.
**Arguments**

- `x` : an object of class "permutest.rma.uni" obtained with `permutest`.
- `digits` : integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `signif.stars` : logical to specify whether p-values should be encoded visually with 'significance stars'. Defaults to the show.signif.stars slot of `options`.
- `signif.legend` : logical to specify whether the legend for the 'significance stars' should be printed. Defaults to the value for `signif.stars`.
- `...` : other arguments.

**Details**

The output includes:

- the results of the omnibus test of moderators. Suppressed if the model includes only one coefficient (e.g., only an intercept, like in the equal- and random-effects models). The p-value is based on the permutation test.
- a table with the estimated coefficients, corresponding standard errors, test statistics, p-values, and confidence interval bounds. The p-values are based on permutation tests. If `permci` was set to `TRUE`, then the permutation-based CI bounds are shown.

**Value**

The function does not return an object.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

**References**


**See Also**

`permutest.rma.uni` for the function to create `permutest.rma.uni` objects.
Print Method for 'ranktest' Objects

Description

Print method for objects of class "ranktest".

Usage

```r
# S3 method for class 'ranktest'
print(x, digits=x$digits, ...)
```

Arguments

- `x` an object of class "ranktest" obtained with `ranktest`.
- `digits` integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `...` other arguments.

Details

The output includes:

- the estimated value of Kendall’s tau rank correlation coefficient
- the corresponding p-value for the test that the true tau is equal to zero

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

References


See Also

`ranktest` for the function to create `ranktest` objects.
Description

Print method for objects of class "regtest".

Usage

```r
## S3 method for class 'regtest'
print(x, digits=x$digits, ret.fit=x$ret.fit, ...)
```

Arguments

- `x`: an object of class "regtest" obtained with `regtest`.
- `digits`: integer to specify the number of decimal places to which the printed results should be rounded (the default is to take the value from the object).
- `ret.fit`: logical to specify whether the full results from the fitted model should also be returned. If unspecified, the default is to take the value from the object.
- `...`: other arguments.

Details

The output includes:

- the model used for the regression test
- the predictor used for the regression test
- the results from the fitted model (only when `ret.fit=TRUE`)
- the test statistic of the test that the predictor is unrelated to the outcomes
- the degrees of freedom of the test statistic (only if the test statistic follows a t-distribution)
- the corresponding p-value
- the ‘limit estimate’ and its corresponding CI (only for predictors "sei", "vi", "ninv", or "sqrtinv" and when the model does not contain any additional moderators)

Value

The function does not return an object.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References

See Also

`regtest` for the function to create `regtest` objects.

**Description**

Print and summary methods for objects of class "rma.uni", "rma.mh", "rma.peto", "rma.glmm", "rma.glmm", and "rma.mv".

**Usage**

```r
## S3 method for class 'rma.uni'
print(x, digits, showfit=FALSE, signif.stars=getOption("show.signif.stars"),
      signif.legend=signif.stars, ...)

## S3 method for class 'rma.mh'
print(x, digits, showfit=FALSE, ...)

## S3 method for class 'rma.peto'
print(x, digits, showfit=FALSE, ...)

## S3 method for class 'rma.glmm'
print(x, digits, showfit=FALSE, signif.stars=getOption("show.signif.stars"),
      signif.legend=signif.stars, ...)

## S3 method for class 'rma.mv'
print(x, digits, showfit=FALSE, signif.stars=getOption("show.signif.stars"),
      signif.legend=signif.stars, ...)

## S3 method for class 'summary.rma'
print(x, digits, showfit=TRUE, signif.stars=getOption("show.signif.stars"),
      signif.legend=signif.stars, ...)
```

**Arguments**

- `x` an object of class "rma.uni", "rma.mh", "rma.peto", "rma.glmm", "rma.glmm", or "rma.mv" (for `print`).
- `object` an object of class "rma" (for `summary`).
- `digits` integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object. See also [here](#) for further details on how to control the number of digits in the output.
showfit logical to specify whether the fit statistics and information criteria should be printed (the default is FALSE for print and TRUE for summary).

signif.stars logical to specify whether p-values should be encoded visually with 'significance stars'. Defaults to the show.signif.stars slot of options.

signif.legend logical to specify whether the legend for the 'significance stars' should be printed. Defaults to the value for signif.stars.

... other arguments.

Details

The output includes:

- the log-likelihood, deviance, AIC, BIC, and AICc value (when setting showfit=TRUE or by default for summary).

- for objects of class "rma.uni" and "rma.glmm", the amount of (residual) heterogeneity in the random/mixed-effects model (i.e., the estimate of $\tau^2$ and its square root). Suppressed for equal-effects models. The (asymptotic) standard error of the estimate of $\tau^2$ is also provided (where possible).

- for objects of "rma.mv", a table providing information about the variance components and correlations in the model. For $\sigma^2$ components, the estimate and its square root are provided, in addition to the number of values/levels, whether the component was fixed or estimated, and the name of the grouping variable/factor. If the R argument was used to specify known correlation matrices, this is also indicated. For models with an '~ inner | outer' formula term, the name of the inner and outer grouping variable/factor are given and the number of values/levels of these variables/factors. In addition, for each $\tau^2$ component, the estimate and its square root are provided, the number of effects or outcomes observed at each level of the inner grouping variable/factor (only for struct="HCS", struct="DIAG", struct="HAR", and struct="UN"), and whether the component was fixed or estimated. Finally, either the estimate of $\rho$ (for struct="CS", struct="AR", struct="CAR", struct="HAR", or struct="HCS") or the entire estimated correlation matrix (for struct="UN") between the levels of the inner grouping variable/factor is provided, again with information whether a particular correlation was fixed or estimated, and how often each combination of levels of the inner grouping variable/factor was observed across the levels of the outer grouping variable/factor. If there is a second '~ inner | outer' formula term, the same information as described above will be provided, but now for the $\gamma^2$ and $\phi$ components.

- the $I^2$ statistic, which estimates (in percent) how much of the total variability in the observed effect sizes or outcomes (which is composed of heterogeneity plus sampling variability) can be attributed to heterogeneity among the true effects. For a meta-regression model, $I^2$ estimates how much of the unaccounted variability (which is composed of residual heterogeneity plus sampling variability) can be attributed to residual heterogeneity. See ‘Note’ for how $I^2$ is computed.

- the $H^2$ statistic, which estimates the ratio of the total amount of variability in the observed effect sizes or outcomes to the amount of sampling variability. For a meta-regression model, $H^2$ estimates the ratio of the unaccounted variability in the observed effect sizes or outcomes to the amount of sampling variability. See ‘Note’ for how $H^2$ is computed.

- for objects of class "rma.uni", the $R^2$ statistic, which estimates the amount of heterogeneity accounted for by the moderators included in the model and can be regarded as a pseudo $R^2$
statistic (Raudenbush, 2009). Only provided when fitting a model including moderators. This is suppressed (and set to NULL) for models without moderators or if the model does not contain an intercept. See ‘Note’ for how $R^2$ is computed.

- for objects of class "rma.glmm", the amount of study level variability (only when using a model that models study level differences as a random effect).
- the results of the test for (residual) heterogeneity. This is the usual $Q$-test for heterogeneity when not including moderators in the model and the $Q_E$-test for residual heterogeneity when moderators are included. For objects of class "rma.glmm", the results from a Wald-type test and a likelihood ratio test are provided (see rma.glmm for more details).
- the results of the omnibus (Wald-type) test of the coefficients in the model (the indices of the coefficients tested are also indicated). Suppressed if the model includes only one coefficient (e.g., only an intercept, like in the equal- and random-effects models).
- a table with the estimated coefficients, corresponding standard errors, test statistics, p-values, and confidence interval bounds.
- the Cochran-Mantel-Haenszel test and Tarone’s test for heterogeneity (only when analyzing odds ratios using the Mantel-Haenszel method, i.e., "rma.mh").

See also here for details on the option to create styled/colored output with the help of the crayon package.

**Value**

The print functions do not return an object. The summary function returns the object passed to it (with additional class "summary.rma").

**Note**

For random-effects models, the $I^2$ statistic is computed with

$$I^2 = 100\% \times \frac{\hat{\tau}^2}{\hat{\tau}^2 + \tilde{v}},$$

where $\hat{\tau}^2$ is the estimated value of $\tau^2$ and

$$\tilde{v} = \frac{(k - 1) \sum w_i}{(\sum w_i)^2 - \sum w_i^2},$$

where $w_i = 1/\sigma^2_i$ is the inverse of the sampling variance of the $i$th study ($\tilde{v}$ is equation 9 in Higgins & Thompson, 2002, and can be regarded as the ‘typical’ within-study variance of the observed effect sizes or outcomes). The $H^2$ statistic is computed with

$$H^2 = \frac{\hat{\tau}^2 + \tilde{v}}{\tilde{v}}.$$

Analogous equations are used for mixed-effects models.

Therefore, depending on the estimator of $\tau^2$ used, the values of $I^2$ and $H^2$ will change. For random-effects models, $I^2$ and $H^2$ are often computed with $I^2 = (Q - (k - 1))/Q$ and $H^2 = Q/(k - 1)$, where $Q$ denotes the statistic of the test for heterogeneity and $k$ the number of studies (i.e., observed effect sizes or outcomes) included in the meta-analysis. The equations used in the metafor package

\[
\hat{\tau}^2 = \frac{I^2 \cdot \tilde{v}}{100 - I^2}.
\]
to compute these statistics are more general and have the advantage that the values of $I^2$ and $H^2$ will be consistent with the estimated value of $\tau^2$ (i.e., if $\hat{\tau}^2 = 0$, then $I^2 = 0$ and $H^2 = 1$ and if $\hat{\tau}^2 > 0$, then $I^2 > 0$ and $H^2 > 1$).

The two definitions of $I^2$ and $H^2$ actually coincide when using the DerSimonian-Laird estimator of $\tau^2$ (i.e., the commonly used equations are actually special cases of the more general definitions given above). Therefore, if you prefer the more conventional definitions of these statistics, use method="DL" when fitting the random/mixed-effects model with the rma.uni function. The conventional definitions are also automatically used when fitting an equal-effects models.

For mixed-effects models, the pseudo $R^2$ statistic (Raudenbush, 2009) is computed with

$$R^2 = \frac{\hat{\tau}^2_{RE} - \hat{\tau}^2_{ME}}{\hat{\tau}^2_{RE}},$$

where $\hat{\tau}^2_{RE}$ denotes the estimated value of $\tau^2$ based on the random-effects model (i.e., the total amount of heterogeneity) and $\hat{\tau}^2_{ME}$ denotes the estimated value of $\tau^2$ based on the mixed-effects model (i.e., the residual amount of heterogeneity). It can happen that $\hat{\tau}^2_{RE} < \hat{\tau}^2_{ME}$, in which case $R^2$ is set to zero (and also if $\hat{\tau}^2_{RE} = 0$). Again, the value of $R^2$ will change depending on the estimator of $\tau^2$ used. This statistic is only computed when the mixed-effects model includes an intercept (so that the random-effects model is clearly nested within the mixed-effects model). You can also use the anova function to compute $R^2$ for any two models that are known to be nested. Note that the pseudo $R^2$ statistic may not be very accurate unless $k$ is large (Lopez-Lopez et al., 2014).

For fixed-effects with moderators models, the $R^2$ statistic is simply the standard $R^2$ statistic (also known as the ‘coefficient of determination’) computed based on weighted least squares estimation. To be precise, the so-called ‘adjusted’ $R^2$ statistic is provided, since $k$ is often relatively small in meta-analyses, in which case the adjustment is relevant.

Author(s)
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References

See Also
rma.uni, rma.mh, rma.peto, rma.glmm, and rma.mv for the corresponding model fitting functions.
Profile Likelihood Plots for 'rma' Objects

Description

Function to profile the (restricted) log-likelihood for objects of class "rma.uni", "rma.mv", "rma.uni.selmodel", and "rma.ls".

Usage

```r
## S3 method for class 'rma.uni'
profile(fitted, xlim, ylim, steps=20, lltol=1e-03, progbar=TRUE, parallel="no", ncpus=1, cl, plot=TRUE, pch=19, refline=TRUE, cline=FALSE, ...)

## S3 method for class 'rma.mv'
profile(fitted, sigma2, tau2, rho, gamma2, phi, xlim, ylim, steps=20, lltol=1e-03, progbar=TRUE, parallel="no", ncpus=1, cl, plot=TRUE, pch=19, refline=TRUE, cline=FALSE, ...)

## S3 method for class 'rma.uni.selmodel'
profile(fitted, tau2, delta, xlim, ylim, steps=20, lltol=1e-03, progbar=TRUE, parallel="no", ncpus=1, cl, plot=TRUE, pch=19, refline=TRUE, cline=FALSE, ...)

## S3 method for class 'rma.ls'
profile(fitted, alpha, xlim, ylim, steps=20, lltol=1e-03, progbar=TRUE, parallel="no", ncpus=1, cl, plot=TRUE, pch=19, refline=TRUE, cline=FALSE, ...)

## S3 method for class 'profile.rma'
print(x, ...)  # S3 method for class 'profile.rma'
plot(x, xlim, ylim, pch=19, xlab, ylab, main, refline=TRUE, cline=FALSE, ...)
```

Arguments

- `fitted`: an object of class "rma.uni", "rma.mv", "rma.uni.selmodel", or "rma.ls".
- `x`: an object of class "profile.rma" (for plot and print).
- `sigma2`: optional integer to specify for which $\sigma^2$ value the likelihood should be profiled.
- `tau2`: optional integer to specify for which $\tau^2$ value the likelihood should be profiled.
- `rho`: optional integer to specify for which $\rho$ value the likelihood should be profiled.
gamma2 optional integer to specify for which $\gamma^2$ value the likelihood should be profiled.
phi optional integer to specify for which $\phi$ value the likelihood should be profiled.
delta optional integer to specify for which $\delta$ value the likelihood should be profiled.
alpha optional integer to specify for which $\alpha$ value the likelihood should be profiled.
xlim optional vector to specify the lower and upper limit of the parameter over which the profiling should be done. If unspecified, the function tries to set these limits automatically.
ylim optional vector to specify the y-axis limits when plotting the profiled likelihood. If unspecified, the function tries to set these limits automatically.
steps number of points between xlim[1] and xlim[2] (inclusive) for which the likelihood should be evaluated (the default is 20).
lltol numerical tolerance used when comparing values of the profiled log-likelihood with the log-likelihood of the fitted model (the default is 1e-03).
progbar logical to specify whether a progress bar should be shown (the default is TRUE).
parallel character string to specify whether parallel processing should be used (the default is "no"). For parallel processing, set to either "snow" or "multicore". See ‘Details’.
ncpus integer to specify the number of processes to use in the parallel processing.
c1 optional cluster to use if parallel="snow". If unspecified, a cluster on the local machine is created for the duration of the call.
plot logical to specify whether the profile plot should be drawn after profiling is finished (the default is TRUE).
pch plotting symbol to use. By default, a filled circle is used. See points for other options.
refline logical to specify whether the value of the parameter estimate should be indicated by a dotted vertical line and its log-likelihood value by a dotted horizontal line (the default is TRUE).
cline logical to specify whether a horizontal reference line should be added to the plot that indicates the log-likelihood value corresponding to the 95% profile confidence interval (the default is FALSE).
xlab title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
ylab title for the y-axis. If unspecified, the function tries to set an appropriate axis title.
main title for the plot. If unspecified, the function tries to set an appropriate title.
... other arguments.

Details
The function fixes a particular parameter of the model and then computes the maximized (restricted) log-likelihood over the remaining parameters of the model. By doing this for a range of values for the parameter that was fixed, a profile of the (restricted) log-likelihood is constructed.
Selecting the Parameter(s) to Profile:

The parameters that can be profiled depend on the model object:

- For objects of class "rma.uni" obtained with the `rma.uni` function, the function profiles over $\tau^2$ (not for equal-effects models).
- For objects of class "rma.mv" obtained with the `rma.mv` function, profiling is done by default over all (non-fixed) variance and correlation components of the model. Alternatively, one can use the `sigma2`, `tau2`, `rho`, `gamma2`, or `phi` arguments to specify over which parameter the profiling should be done. Only one of these arguments can be used at a time. A single integer is used to specify the number of the parameter.
- For selection model objects of class "rma.uni.selmodel" obtained with the `selmodel` function, profiling is done by default over $\tau^2$ (for models where this is an estimated parameter) and all (non-fixed) selection model parameters. Alternatively, one can choose to profile only $\tau^2$ by setting `tau2=TRUE` or one can select one of the selection model parameters to profile by specifying its number via the `delta` argument.
- For location-scale model objects of class "rma.ls" obtained with the `rma.uni` function, profiling is done by default over all (non-fixed) $\alpha$ parameters that are part of the scale model.

Interpreting a Likelihood Profile:

A profile plot should show a single peak at the corresponding ML/REML estimate (assuming that the model was fitted with ML/REML estimation). If `refline=TRUE` (the default), the value of the parameter estimate is indicated by a dotted vertical line and its log-likelihood value by a dotted horizontal line. Hence, the intersection of these two lines should correspond to the peak.

When profiling a variance component (or some other parameter that cannot be negative), the peak may be at zero (if this corresponds to the ML/REML estimate of the parameter). In this case, the profiled log-likelihood should be a monotonically decreasing function of the parameter.

If the profiled log-likelihood has multiple peaks, this indicates that the likelihood surface is not unimodal. In such cases, the ML/REML estimate may correspond to a local optimum (when the intersection of the two dotted lines is not at the highest peak).

If the profile is flat (over the entire parameter space or large portions of it), then this suggests that at least some of the parameters of the model are not identifiable (and the parameter estimates obtained are to some extent arbitrary). See Raue et al. (2009) for some further discussion of parameter identifiability (structurally and practically) and the use of profile likelihoods to check for this.

The function checks whether any profiled log-likelihood value is actually larger than the log-likelihood of the fitted model (using a numerical tolerance of `lltol`). If so, a warning is issued as this might indicate that the optimizer did not identify the actual ML/REML estimate.

Parallel Processing:

Profiling requires repeatedly refitting the model, which can be slow when $k$ is large and/or the model is complex (the latter especially applies to "rma.mv" objects and also to certain "rma.uni.selmodel" or "rma.ls" objects). On machines with multiple cores, one can try to speed things up by delegating the model fitting to separate worker processes, that is, by setting `parallel="snow"` or `parallel="multicore"` and `ncpus` to some value larger than 1. Parallel processing makes use of the `parallel` package, using the `makePSOCKcluster` and `parLapply` functions when `parallel="snow"` or using `mclapply` when `parallel="multicore"` (the latter only works on Unix/Linux-alikes). With `parallel::detectCores()`, one can check on the number of available cores on the local machine.
Value

An object of class "profile.rma". The object is a list (or list of such lists) containing the following components:

One of the following (depending on the parameter that was actually profiled):

- **sigma2**: values of $\sigma^2$ over which the likelihood was profiled.
- **tau2**: values of $\tau^2$ over which the likelihood was profiled.
- **rho**: values of $\rho$ over which the likelihood was profiled.
- **gamma2**: values of $\gamma^2$ over which the likelihood was profiled.
- **phi**: values of $\phi$ over which the likelihood was profiled.
- **delta**: values of $\delta$ over which the likelihood was profiled.
- **alpha**: values of $\alpha$ over which the likelihood was profiled.

In addition, the following components are included:

- **ll**: (restricted) log-likelihood values at the corresponding parameter values.
- **beta**: a matrix with the estimated model coefficients at the corresponding parameter values.
- **ci.lb**: a matrix with the lower confidence interval bounds of the model coefficients at the corresponding parameter values.
- **ci.ub**: a matrix with the upper confidence interval bounds of the model coefficients at the corresponding parameter values.
- **...**: some additional elements/values.

Note that the list is returned invisibly.

Author(s)

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References


See Also

`rma.uni`, `rma.mv`, and `selmodel.rma.uni` for functions to fit models for which profile likelihood plots can be drawn.

`confint.rma.uni`, `confint.rma.mv`, and `confint.rma.uni.selmodel` for functions to compute corresponding profile likelihood confidence intervals.
### calculate log odds ratios and corresponding sampling variances

dat <- escalc(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model using rma.uni()
res <- rma(yi, vi, data=dat)

### profile over tau^2
profile(res, probar=FALSE)

### change data into long format
dat.long <- to.long(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### set levels of group variable ("exp" = experimental/vaccinated; "con" = control/non-vaccinated)
levels(dat.long$group) <- c("exp", "con")

### set "con" to reference level
dat.long$group <- relevel(dat.long$group, ref="con")

### calculate log odds and corresponding sampling variances
dat.long <- escalc(measure="PLO", xi=out1, mi=out2, data=dat.long)

### fit bivariate random-effects model using rma.mv()
res <- rma.mv(yi, vi, mods = ~ group, random = ~ group | study, struct="UN", data=dat.long)

### profile over tau^2_1, tau^2_2, and rho
### note: for rho, adjust region over which profiling is done (’zoom in’ on area around estimate)
### Not run:
par(mfrow=c(2,2))
profile(res, tau2=1)
profile(res, tau2=2)
profile(res, rho=1, xlim=c(.90, .98))

### End(Not run)

### an example where the peak is at 0
dat <- escalc(measure="RD", n1i=n1i, n2i=n2i, ai=ai, ci=ci, data=dat.hine1989)
res <- rma(yi, vi, data=dat)
par(mfrow=c(1,1))
profile(res, probar=FALSE)

---

**Normal QQ Plots for 'rma' Objects**

**Description**

Function to create normal QQ plots for objects of class "rma.uni", "rma.mh", and "rma.peto".
Usage

## S3 method for class 'rma.uni'
qqnorm(y, type="rstandard", pch=19, envelope=TRUE, 
level=y$level, bonferroni=FALSE, reps=1000, smooth=TRUE, bass=0, 
label=FALSE, offset=0.3, pos=13, lty, ...)
## S3 method for class 'rma.mh'
qqnorm(y, type="rstandard", pch=19, label=FALSE, offset=0.3, pos=13, ...)
## S3 method for class 'rma.peto'
qqnorm(y, type="rstandard", pch=19, label=FALSE, offset=0.3, pos=13, ...)
## S3 method for class 'rma.glmm'
qqnorm(y, ...)
## S3 method for class 'rma.mv'
qqnorm(y, ...)

Arguments

y
an object of class "rma.uni", "rma.mh", or "rma.peto". The method is not yet implemented for objects of class "rma.glmm" or "rma.mv".

type
character string (either "rstandard" (default) or "rstudent") to specify whether standardized residuals or studentized deleted residuals should be used in creating the plot. See 'Details'.
pch
plotting symbol to use for the observed outcomes. By default, a filled circle is used. See points for other options.
envelope
logical to specify whether a pseudo confidence envelope should be simulated and added to the plot (the default is TRUE). Only for objects of class "rma.uni". See 'Details'.
level
numeric value between 0 and 100 to specify the level of the pseudo confidence envelope (the default is to take the value from the object).
bonferroni
logical to specify whether the bounds of the envelope should be Bonferroni corrected.
reps
numeric value to specify the number of iterations to use for simulating the pseudo confidence envelope (the default is 1000).
smooth
logical to specify whether the results from the simulation should be smoothed (the default is TRUE).
bass
numeric value that controls the degree of smoothing (the default is 0).
label
argument to control the labeling of the points (the default is FALSE). See 'Details'.
offset
argument to control the distance between the points and the corresponding labels.
pos
argument to control the position of the labels.
lty
optional character string to specify the line type for the diagonal line and the pseudo confidence envelope. If unspecified, the function sets this to c("solid", "dotted") by default.
...
other arguments.
Details

The plot shows the theoretical quantiles of a normal distribution on the horizontal axis against
the observed quantiles for either the standardized residuals (type="rstandard", the default) or
the externally standardized residuals (type="rstudent") on the vertical axis (see residuals for
details on the definition of these residual types).

For reference, a line is added to the plot with slope of 1, going through the (0,0) point.

For objects of class "rma.uni", it is also possible to add a pseudo confidence envelope to the plot.
The envelope is created based on the quantiles of sets of pseudo residuals simulated from the given
model (for details, see Cook & Weisberg, 1982). The number of sets simulated can be controlled
with the reps argument. When smooth=TRUE, the simulated bounds are smoothed with Friedman's
SuperSmoother (see supsmu). The bass argument can be set to a number between 0 and 10, with
higher numbers indicating increasing smoothness. If bonferroni=TRUE, the envelope bounds are
Bonferroni corrected, so that the envelope can be regarded as a confidence region for all k
residuals simultaneously. The default however is bonferroni=FALSE, which makes the plot more sensitive
to deviations from normality.

With the label argument, one can control whether points in the plot will be labeled (e.g., to identify
outliers). If label="all" (or label=TRUE), all points in the plot will be labeled. If label="out".
points falling outside of the confidence envelope will be labeled (only available for objects of class
"rma.uni"). Finally, one can also set this argument to a numeric value (between 1 and k), indicating
how many of the most extreme points should be labeled (for example, with label=1 only the most
extreme point is labeled, while with label=3, the most extreme, and the second and third most
extreme points is labeled). With the offset argument, one can adjust the distance between the
labels and the corresponding points. The pos argument is the position specifier for the labels (1, 2,
3, and 4, respectively indicate positions below, to the left of, above, and to the right of the points; 13
places the labels below the points for points that fall below the reference line and above otherwise;
24 places the labels to the left of the points for points that fall above the reference line and to the
right otherwise).

Value

A list with components:

x  the x-axis coordinates of the points that were plotted.

y  the y-axis coordinates of the points that were plotted.

Note that the list is returned invisibly.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References

Hall.

**radial**

Radial (Galbraith) Plots for 'rma' Objects

**Description**

Function to create radial (also called Galbraith) plots for objects of class "rma".

**Usage**

```r
radial(x, ...) galbraith(x, ...)
```

```r
# S3 method for class 'rma'
radial(x, center=FALSE, xlim, ylim, xlab, ylab,
       atz, aty, steps=7, level=x$level, digits=2, back="lightgray",
       transf, targs, pch=19, arc.res=100, cex, ...)
```

**Examples**

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)

### draw QQ plot
qqnorm(res)

### fit mixed-effects model with absolute latitude as moderator
res <- rma(yi, vi, mods = ~ ablat, data=dat)

### draw QQ plot
qqnorm(res)
```

**See Also**

`rma.uni`, `rma.mh`, and `rma.peto` for functions to fit models for which normal QQ plots can be drawn.


Arguments

- **x**: an object of class "rma".
- **center**: logical to indicate whether the plot should be centered horizontally at the model estimate (the default is FALSE).
- **xlim**: x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
- **zlim**: z-axis limits. If unspecified, the function tries to set the z-axis limits to some sensible values (note that the z-axis limits are the actual vertical limit of the plotting region).
- **xlab**: title for the x-axis. If unspecified, the function tries to set an appropriate axis title.
- **zlab**: title for the z-axis. If unspecified, the function tries to set an appropriate axis title.
- **atz**: position for the z-axis tick marks and labels. If unspecified, these values are set by the function.
- **aty**: position for the y-axis tick marks and labels. If unspecified, these values are set by the function.
- **steps**: the number of tick marks for the y-axis (the default is 7). Ignored when argument aty is used.
- **level**: numeric value between 0 and 100 to specify the level of the z-axis error region (the default is to take the value from the object).
- **digits**: integer to specify the number of decimal places to which the tick mark labels of the y-axis should be rounded (the default is 2).
- **back**: color of the z-axis error region. Set to NA to suppress shading of the region.
- **transf**: optional argument to specify a function to transform the y-axis labels (e.g., transf=exp; see also transf). If unspecified, no transformation is used.
- **targs**: optional arguments needed by the function specified via transf.
- **pch**: plotting symbol. By default, a filled circle is used. See points for other options.
- **arc.res**: integer to specify the number of line segments to use when drawing the y-axis and confidence interval arcs (the default is 100).
- **cex**: optional character and symbol expansion factor. If unspecified, the function tries to set this to a sensible value.
- **...**: other arguments.

Details

For an equal-effects model, the plot shows the inverse of the standard errors on the horizontal axis against the observed effect sizes or outcomes standardized by their corresponding standard errors on the vertical axis. Since the vertical axis corresponds to standardized values, it is referred to as the z-axis within this function. On the right hand side of the plot, an arc is drawn (referred to as the y-axis within this function) corresponding to the observed effect sizes or outcomes. A line projected from (0,0) through a particular point within the plot onto this arc indicates the value of the observed effect size or outcome for that point.
For a random-effects model, the function uses $1/\sqrt{v_i + \tau^2}$ for the horizontal axis, where $v_i$ is the sampling variance of the observed effect size or outcome and $\tau^2$ is the amount of heterogeneity as estimated based on the model. For the z-axis, $\sqrt{v_i + \tau^2}$ is used to standardize the observed effect sizes or outcomes.

If the model contains moderators, the function returns an error.

Value

A data frame with components:

- x: the x-axis coordinates of the points that were plotted.
- y: the y-axis coordinates of the points that were plotted.
- ids: the study id numbers.
- slab: the study labels.

Note that the data frame is returned invisibly.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.uni, rma.mh, rma.peto, rma.glmm, and rma.mv for functions to fit models for which radial plots can be drawn.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)
dat

### fit equal-effects model
res <- rma(yi, vi, data=dat, method="EE")

### draw radial plot
radial(res)
```
### line from (0,0) with slope equal to the log risk ratio from the 4th study

```r
abline(a=0, b=dat$yi[4], lty="dotted")
```

### meta-analysis of the log risk ratios using a random-effects model

```r
res <- rma(yi, vi, data=dat)
```

### draw radial plot

```r
radial(res)
```

---

### ranef

#### Best Linear Unbiased Predictions for 'rma.uni' and 'rma.mv' Objects

**Description**

The function computes best linear unbiased predictions (BLUPs) of the random effects for objects of class "rma.uni" and "rma.mv". Corresponding standard errors and prediction interval bounds are also provided.

**Usage**

```r
## S3 method for class 'rma.uni'
ranef(object, level, digits, transf, targs, ...)
## S3 method for class 'rma.mv'
ranef(object, level, digits, transf, targs, verbose=FALSE, ...)
```

**Arguments**

- `object`: an object of class "rma.uni" or "rma.mv".
- `level`: numeric value between 0 and 100 to specify the prediction interval level. If unspecified, the default is to take the value from the object.
- `digits`: optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
- `transf`: optional argument to specify a function to transform the predicted values and interval bounds (e.g., `transf=exp`; see also `transf`). If unspecified, no transformation is used.
- `targs`: optional arguments needed by the function specified under `transf`.
- `verbose`: logical to specify whether output should be generated on the progress of the computations (the default is `FALSE`).
- `...`: other arguments.
For objects of class "rma.uni", an object of class "list.rma". The object is a list containing the following components:

- **pred**: predicted values.
- **se**: corresponding standard errors.
- **pi.lb**: lower bound of the prediction intervals.
- **pi.ub**: upper bound of the prediction intervals.
- **...**: some additional elements/values.

The object is formatted and printed with the `print` function. To format the results as a data frame, one can use the `as.data.frame` function.

For objects of class "rma.mv", a list of data frames with the same components as described above.

**Note**

For best linear unbiased predictions that combine the fitted values based on the fixed effects and the estimated contributions of the random effects, see `blup`.

For predicted/fitted values that are based only on the fixed effects of the model, see `fitted` and `predict`.

Equal-effects models do not contain random study effects. The BLUPs for these models will therefore be 0.

When using the `transf` argument, the transformation is applied to the predicted values and the corresponding interval bounds. The standard errors are then set equal to NA and are omitted from the printed output.

By default, a standard normal distribution is used to construct the prediction intervals. When the model was fitted with `test="t"` or `test="knha"`, then a t-distribution with $k-p$ degrees of freedom is used.

To be precise, it should be noted that the function actually computes empirical BLUPs (eBLUPs), since the predicted values are a function of the estimated variance component(s).

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> [https://www.metafor-project.org](https://www.metafor-project.org)

**References**


Rank Correlation Test for Funnel Plot Asymmetry

The function can be used to carry out the rank correlation test for funnel plot asymmetry.

### Usage

```r
ranktest(x, vi, sei, subset, data, digits, ...)
```

### Arguments

- `x`: a vector with the observed effect sizes or outcomes or an object of class "rma".
- `vi`: vector with the corresponding sampling variances (ignored if `x` is an object of class "rma").
- `sei`: vector with the corresponding standard errors (note: only one of the two, `vi` or `sei`, needs to be specified).
- `subset`: optional (logical or numeric) vector to specify the subset of studies that should be included in the test (ignored if `x` is an object of class "rma").
- `data`: optional data frame containing the variables given to the arguments above.
- `digits`: optional integer to specify the number of decimal places to which the printed results should be rounded.
- `...`: other arguments.
Details

The function carries out the rank correlation test as described by Begg and Mazumdar (1994). The test can be used to examine whether the observed effect sizes or outcomes and the corresponding sampling variances are correlated. A high correlation would indicate that the funnel plot is asymmetric, which may be a result of publication bias.

One can either pass a vector with the observed effect sizes or outcomes (via x) and the corresponding sampling variances via vi (or the standard errors via sei) to the function or an object of class "rma".

Value

An object of class "ranktest". The object is a list containing the following components:

- tau: the estimated value of Kendall's tau rank correlation coefficient.
- pval: the corresponding p-value for the test that the true tau value is equal to zero.

The results are formatted and printed with the print function.

Note

The method does not depend on the model fitted. Therefore, regardless of the model passed to the function, the results of the rank test will always be the same. See regtest for tests of funnel plot asymmetry that are based on regression models and model dependent.

The function makes use of the cor.test function with method="kendall". If possible, an exact p-value is provided; otherwise, a large-sample approximation is used.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

regtest for the regression test, trimfill for the trim and fill method, tes for the test of excess significance, and selmodel for selection models.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)
```
### carry out the rank correlation test
ranktest(res)

### can also pass the observed outcomes and corresponding sampling variances to the function
ranktest(yi, vi, data=dat)

---

**rcalc**

*Calculate the Variance-Covariance of Dependent Correlation Coefficients*

**Description**

The function can be used to calculate the variance-covariance matrix of correlation coefficients computed based on the same sample of subjects.

**Usage**

```r
rcalc(x, ni, data, rtoz=FALSE, nfun="min", sparse=FALSE, ...)
```

**Arguments**

- `x` a formula of the form `ri ~ var1 + var2 | study`. See ‘Details’.
- `ni` vector to specify the sample sizes based on which the correlations were computed.
- `data` data frame containing the variables specified via the formula (and the sample sizes).
- `rtoz` logical to specify whether to transform the correlations via Fisher’s r-to-z transformation (the default is FALSE).
- `nfun` a character string to specify how the ‘common’ sample size within each study should be computed. Possible options are “min” (for the minimum), “harmonic” (for the harmonic mean), or “mean” (for the arithmetic mean). Can also be a function. See ‘Details’.
- `sparse` logical to specify whether the variance-covariance matrix should be returned as a sparse matrix (the default is FALSE).
- `...` other arguments.

**Details**

A meta-analysis of correlation coefficients may involve multiple correlation coefficients extracted from the same study. When these correlations are computed based on the same sample of subjects, then they are typically not independent. The `rcalc` function can be used to create a dataset with the correlation coefficients (possibly transformed with Fisher’s r-to-z transformation) and the corresponding variance-covariance matrix. The dataset and variance-covariance matrix can then be further meta-analyzed using the `rma.mv` function.

When computing the covariance between two correlation coefficients, we can distinguish two cases:
1. In the first case, one of the variables involved in the two correlation coefficients is the same. For example, in $r_{12}$ and $r_{13}$, variable 1 is common to both correlation coefficients. This is sometimes called the (partially) 'overlapping' case. The covariance between the two correlation coefficients, $\text{Cov}(r_{12}, r_{13})$, then depends on the degree of correlation between variables 2 and 3 (i.e., $r_{23}$).

2. In the second case, none of the variables are common to both correlation coefficients. For example, this would be the case if we have correlations $r_{12}$ and $r_{34}$ based on 4 variables. This is sometimes called the 'non-overlapping' case. The covariance between the two correlation coefficients, $\text{Cov}(r_{12}, r_{34})$, then depends on $r_{13}$, $r_{14}$, $r_{23}$, and $r_{24}$.

Equations to compute these covariances can be found, for example, in Steiger (1980) and Olkin and Finn (1990).

To use the rcalc function, one needs to construct a data frame that contains a study identifier (say study), two variable identifiers (say var1 and var2), the corresponding correlation coefficients (say $r_i$), and the sample sizes based on which the correlation coefficients were computed (say $n_i$). Then the first argument should be a formula of the form $r_i \sim \text{var1} + \text{var2} | \text{study}$, argument $n_i$ is set equal to the variable name containing the sample sizes, and the data frame containing these variables is specified via the data argument. When using the function for a single study, one can leave out the study identifier from the formula.

When argument $r$toz is set to TRUE, then the correlations are transformed with Fisher's r-to-z transformation (Fisher, 1921) and the variance-covariance matrix is computed for the transformed values.

In some cases, the sample size may not be identical within a study (e.g., $r_{12}$ may have been computed based on 120 subjects while $r_{13}$ was computed based on 118 subjects due to 2 missing values in variable 3). For constructing the variance-covariance matrix, we need to assume a 'common' sample size for all correlation coefficients within the study. Argument $nfun$ provides some options for how the common sample size should be computed. Possible options are "min" (for using the minimum sample size within a study as the common sample size), "harmonic" (for using the harmonic mean), or "mean" (for using the arithmetic mean). The default is "min", which is a conservative choice (i.e., it will overestimate the sampling variances of coefficients that were computed based on a sample size that was actually larger than the minimum sample size). One can also specify a function via the $nfun$ argument (which should take a numeric vector as input and return a single value).

**Value**

A list containing the following components:

- **dat**: a data frame with the study identifier, the two variable identifiers, a variable pair identifier, the correlation coefficients (possibly transformed with Fisher’s r-to-z transformation), and the (common) sample sizes.

- **V**: corresponding variance-covariance matrix (given as a sparse matrix when sparse=TRUE).

Note that a particular covariance can only be computed when all of the correlation coefficients involved in the covariance equation are included in the dataset. If one or more coefficients needed for the computation are missing, then the resulting covariance will also be missing (i.e., NA).
Note

For raw correlation coefficients, the variance-covariance matrix is computed with \( n - 1 \) in the denominator (instead of \( n \) as suggested in Steiger, 1980, and Olkin & Finn, 1990). This is more consistent with the usual equation for computing the sampling variance of a correlation coefficient (with \( n - 1 \) in the denominator).

For raw and r-to-z transformed coefficients, the variance-covariance matrix will only be computed when the (common) sample size for a study is at least 5.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

rma.mv for a model fitting function that can be used to meta-analyze dependent correlation coefficients.

dat.craft2003 for an illustrative example.

Examples

```r
### copy data into 'dat'
dat <- dat.craft2003

### construct dataset and var-cov matrix of the correlations
tmp <- rcalc(ri ~ var1 + var2 | study, ni=ni, data=dat)
V <- tmp$V
dat <- tmp$dat

### examine data for study 1
dat[dat$study == 1,]
blsplit(V, dat$study, round, 4)$"6"

### examine data for study 6
dat[dat$study == 6,]
blsplit(V, dat$study, round, 4)$"6"

### examine data for study 17
dat[dat$study == 17,]
blsplit(V, dat$study, round, 4)$"17"
```
Scatter Plots / Bubble Plots

Description
Function to create scatter plots / bubble plots based on meta-regression models.

Usage
regplot(x, ...)

## S3 method for class 'rma'
regplot(x, mod, pred=TRUE, ci=TRUE, pi=FALSE, shade=TRUE,
xlim, ylim, predlim, olim, xlab, ylab, at, digits=2L,
transf, atransf, targs, level=x$level,
pch, psize, plim=c(0.5,3), col, bg, slab,
grid=FALSE, refline, label=FALSE, offset=c(1,1), labsize=1,
lcol, lwd, lty, legend=FALSE, xvals, ...)

## S3 method for class 'regplot'
points(x, ...)

Arguments

x an object of class "rma.uni", "rma.mv", or "rma.glmm" including one or multiple moderators (or an object of class "regplot" for points).
mod either a scalar to specify the position of the moderator variable in the model or a character string to specify the name of the moderator variable.
pred logical to indicate whether the (marginal) regression line based on the moderator should be added to the plot (the default is TRUE). Can also be an object from predict. See ‘Details’.
ci logical to indicate whether the corresponding confidence interval bounds should be added to the plot (the default is TRUE).
pi logical to indicate whether the corresponding prediction interval bounds should be added to the plot (the default is FALSE).
shade logical to indicate whether the confidence/prediction interval regions should be shaded (the default is TRUE). Can also be a two-element character vector to specify the colors for shading the confidence and prediction interval regions (if shading only the former, a single color can also be specified).
xlim x-axis limits. If unspecified, the function tries to set the x-axis limits to some sensible values.
ylim y-axis limits. If unspecified, the function tries to set the y-axis limits to some sensible values.
predlim optional argument to specify the limits of the (marginal) regression line. If unspecified, the limits are based on the range of the moderator variable.
optional argument to specify observation/outcome limits. If unspecified, no limits are used.

title for the x-axis. If unspecified, the function tries to set an appropriate axis title.

title for the y-axis. If unspecified, the function tries to set an appropriate axis title.

position of the y-axis tick marks and corresponding labels. If unspecified, the function tries to set the tick mark positions/labels to some sensible values.

integer to specify the number of decimal places to which the tick mark labels of the y-axis should be rounded. When specifying an integer (e.g., 2L), trailing zeros after the decimal mark are dropped for the y-axis labels. When specifying a numeric value (e.g., 2), trailing zeros are retained.

optional argument to specify a function to transform the observed outcomes, predicted values, and confidence/prediction interval bounds (e.g., transf=exp; see also transf). If unspecified, no transformation is used.

optional argument to specify a function to transform the y-axis labels (e.g., atransf=exp; see also transf). If unspecified, no transformation is used.

optional arguments needed by the function specified via transf or atransf.

numeric value between 0 and 100 to specify the confidence/prediction interval level (the default is to take the value from the object).

plotting symbol to use for the observed outcomes. By default, a filled circle is used. Can also be a vector of values. See points for other options.

optional numeric value to specify the point sizes for the observed outcomes. If unspecified, the point sizes are a function of the model weights. Can also be a vector of values. Can also be a character string (either "seinv" or "vinv") to make the point sizes proportional to the inverse standard errors or inverse sampling variances.

numeric vector of length 2 to scale the point sizes (ignored when a numeric value or vector is specified for psize). See ‘Details’.

character string to specify the color to use for plotting the observed outcomes ("black" is used by default if not specified). Can also be a vector.

character string to specify the background color for open plot symbols ("darkgray" is used by default if not specified). Can also be a vector.

optional vector with labels for the k studies. If unspecified, the function tries to extract study labels from x.

logical to specify whether a grid should be added to the plot. Can also be a color name for the grid.

optional numeric value to specify the location of a horizontal reference line that should be added to the plot.

argument to control the labeling of the points (the default is FALSE). See ‘Details’.

argument to control the distance between the points and the corresponding labels. See ‘Details’.
regplot

**Details**

The function draws a scatter plot of the values of a moderator variable in a meta-regression model (on the x-axis) against the observed effect sizes or outcomes (on the y-axis). The regression line from the model (with corresponding confidence interval bounds) is added to the plot by default. These types of plots are also often referred to as ‘bubble plots’ as the points are typically drawn in different sizes to reflect their precision or weight in the model.

If the model includes multiple moderators, one must specify via argument `mod` either the position (as a number) or the name (as a string) of the moderator variable to place on the x-axis. The regression line then reflects the ‘marginal’ relationship between the chosen moderator and the effect sizes or outcomes (i.e., all other moderators except the one being plotted are held constant at their means).

By default (i.e., when `psize` is not specified), the size of the points is a function of the square root of the model weights. This way, their area is proportional to the weights. However, the point sizes are rescaled so that the smallest point size is `plim[1]` and the largest point size is `plim[2]`. As a result, their relative sizes (i.e., areas) no longer exactly correspond to their relative weights. If exactly relative point sizes are desired, one can set `plim[2]` to `NA`, in which case the points are rescaled so that the smallest point size corresponds to `plim[1]` and all other points are scaled accordingly. As a result, the largest point may be very large. Alternatively, one can set `plim[1]` to `NA`, in which case the points are rescaled so that the largest point size corresponds to `plim[2]` and all other points are scaled accordingly. As a result, the smallest point may be very small. To avoid the latter, one can also set `plim[3]`, which enforces a minimal point size.

One can also set `psize` to a scalar (e.g., `psize=1`) to avoid that the points are drawn in different sizes. One can also specify the point sizes manually by passing a vector of the appropriate length to `psize`. Finally, one can also set `psize` to either "seinv" or "vinv" to make the point sizes proportional to the inverse standard errors or inverse sampling variances.

With the `label` argument, one can control whether points in the plot will be labeled. If `label="all"` (or `label=TRUE`), all points in the plot will be labeled. If `label="ciout"` or `label="piout"`, points falling outside of the confidence/prediction interval will be labeled. Alternatively, one can set this...
argument to a logical or numeric vector to specify which points should be labeled. The labels are placed above the points when they fall above the regression line and otherwise below. With the offset argument, one can adjust the distance between the labels and the corresponding points. This can either be a single numeric value, which is used as a multiplicative factor for the point sizes (so that the distance between labels and points is larger for larger points) or a numeric vector with two values, where the first is used as an additive factor independent of the point sizes and the second again as a multiplicative factor for the point sizes. The values are given as percentages of the y-axis range. It may take some trial and error to find two values for the offset argument so that the labels are placed right next to the boundary of the points. With labsize, one can control the size of the labels.

One can also pass an object from predict to the pred argument. This can be useful when the meta-regression model reflects a more complex relationship between the moderator variable and the effect sizes or outcomes (e.g., when using polynomials or splines) or when the model involves interactions. In this case, one also needs to specify the xvals argument. See ‘Examples’.

Value

An object of class "regplot" with components:

- slab: the study labels
- ids: the study ids
- xi: the x-axis coordinates of the points that were plotted.
- yi: the y-axis coordinates of the points that were plotted.
- pch: the plotting symbols of the points that were plotted.
- psize: the point sizes of the points that were plotted.
- col: the colors of the points that were plotted.
- bg: the background colors of the points that were plotted.
- label: logical vector indicating whether a point was labeled.

Note that the object is returned invisibly. Using points.regplot, one can redraw the points (and labels) in case one wants to superimpose the points on top of any elements that were added manually to the plot (see ‘Examples’).

Note

For certain types of models, it may not be possible to draw the prediction interval bounds (if this is the case, a warning will be issued).

Argument slab and when specifying vectors for arguments pch, psize, col, bg, and/or label (for a logical vector), the variables specified are assumed to be of the same length as the data passed to the model fitting function (and if the data argument was used in the original model fit, then the variables will be searched for within this data frame first). Any subsetting and removal of studies with missing values is automatically applied to the variables specified via these arguments.

If the outcome measure used for creating the plot is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the olim argument to enforce those limits (the observed outcomes and confidence/prediction intervals cannot exceed those bounds then).
Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

`rma.uni`, `rma.glmm`, and `rma.mv` for functions to fit models for which scatter plots / bubble plots can be drawn.

Examples

```r
### copy BCG vaccine data into 'dat'
dat <- dat.bcg
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat)

############################################################################
### fit mixed-effects model with absolute latitude as a moderator
res <- rma(yi, vi, mods = ~ ablat, data=dat)
res
### draw plot
regplot(res, mod="ablat", xlab="Absolute Latitude")

### adjust x-axis limits and back-transform to risk ratios
regplot(res, mod="ablat", xlab="Absolute Latitude", xlim=c(0,60), transf=exp)

### also extend the prediction limits for the regression line
regplot(res, mod="ablat", xlab="Absolute Latitude", xlim=c(0,60), predlim=c(0,60), transf=exp)

### add the prediction interval to the plot, add a reference line at 1, and add a legend
regplot(res, mod="ablat", pi=TRUE, xlab="Absolute Latitude",
        xlim=c(0,60), predlim=c(0,60), transf=exp, refline=1, legend=TRUE)

### label points outside of the prediction interval
regplot(res, mod="ablat", pi=TRUE, xlab="Absolute Latitude",
        xlim=c(0,60), predlim=c(0,60), transf=exp, refline=1, legend=TRUE,
        label="piout", labsize=0.8)

############################################################################
### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)
```
### plot the marginal relationships
regplot(res, mod="ablat", xlab="Absolute Latitude")
regplot(res, mod="year", xlab="Publication Year")

############################################################################
### fit a quadratic polynomial meta-regression model
res <- rma(yi, vi, mods = ~ ablat + I(ablat^2), data=dat)
res

### compute predicted values using predict()
xs <- seq(0,60,length=601)
tmp <- predict(res, newmods=cbind(xs, xs^2))

### can now pass these results to the 'pred' argument (and have to specify xvals accordingly)
regplot(res, mod="ablat", pred=tmp, xlab="Absolute Latitude", xlim=c(0,60), xvals=xs)

### back-transform to risk ratios and add reference line
regplot(res, mod="ablat", pred=tmp, xlab="Absolute Latitude", xlim=c(0,60), xvals=xs, transf=exp, reline=1)

############################################################################
### fit a model with an interaction between a quantitative and a categorical predictor
### (note: just for illustration purposes; this model is too complex for this dataset)
res <- rma(yi, vi, mods = ~ ablat * alloc, data=dat)
res

### draw bubble plot but do not add regression line or CI
tmp <- regplot(res, mod="ablat", xlab="Absolute Latitude", xlim=c(0,60), pred=FALSE, ci=FALSE)

### add regression lines for the three alloc levels
xs <- seq(0, 60, length=100)
preds <- predict(res, newmods=cbind(xs, 0, 0, 0, 0))
lines(xs, preds$pred, lwd=3)
preds <- predict(res, newmods=cbind(xs, 1, 0, xs, 0))
lines(xs, preds$pred, lwd=3)
preds <- predict(res, newmods=cbind(xs, 0, 1, 0, xs))
lines(xs, preds$pred, lwd=3)

### add points back to the plot (so they are on top of the lines)
points(tmp)
**Description**

The function can be used to carry out (various versions of) Egger's regression test for funnel plot asymmetry.

**Usage**

```r
regtest(x, vi, sei, ni, subset, data, 
    model="rma", predictor="sei", ret.fit=FALSE, digits, ...)
```

**Arguments**

- `x`: a vector with the observed effect sizes or outcomes or an object of class "rma".
- `vi`: vector with the corresponding sampling variances (ignored if `x` is an object of class "rma").
- `sei`: vector with the corresponding standard errors (note: only one of the two, `vi` or `sei`, needs to be specified).
- `ni`: optional vector with the corresponding sample sizes (only relevant when using the sample sizes (or a transformation thereof) as predictor).
- `subset`: optional (logical or numeric) vector to specify the subset of studies that should be included in the test (ignored if `x` is an object of class "rma").
- `data`: optional data frame containing the variables given to the arguments above.
- `model`: either "rma" or "lm" to indicate the type of model to use for the regression test. See 'Details'.
- `predictor`: either "sei", "vi", "ni", "ninv", "sqrtni", or "sqrtninv" to indicate the predictor to use for the regression test. See 'Details'.
- `ret.fit`: logical to specify whether the full results from the fitted model should also be returned.
- `digits`: optional integer to specify the number of decimal places to which the printed results should be rounded.
- `...`: other arguments.

**Details**

Various tests for funnel plot asymmetry have been suggested in the literature, including the rank correlation test by Begg and Mazumdar (1994) and the regression test by Egger et al. (1997). Extensions, modifications, and further developments of the regression test are described (among others) by Macaskill, Walter, and Irwig (2001), Sterne and Egger (2005), Harbord, Egger, and Sterne (2006), Peters et al. (2006), Rücker et al. (2008), and Moreno et al. (2009). The various versions of the regression test differ in terms of the model (either a weighted regression model with a multiplicative dispersion term or a fixed/mixed-effects meta-regression model is used), in terms of the predictor variable that the observed effect sizes or outcomes are hypothesized to be related to when publication bias is present (suggested predictors include the standard error, the sampling variance, and the sample size or transformations thereof), and in terms of the outcome measure used (e.g., for $2 \times 2$ table data, one has the choice between various outcome measures). The idea behind the various tests is the same though: If there is a relationship between the observed effect sizes or
outcomes and the chosen predictor, then this usually implies asymmetry in the funnel plot, which in turn may be an indication of publication bias.

The `regtest` function can be used to carry out various versions of the regression test. One can either pass a vector with the observed effect sizes or outcomes (via `x`) and the corresponding sampling variances via `vi` (or the standard errors via `sei`) to the function or an object of class "rma".

The model type for the regression test is chosen via the `model` argument, with `model="lm"` for a weighted regression model with a multiplicative dispersion term or `model="rma"` for a (mixed-effects) meta-regression model (the default).

The predictor for the test is chosen via the `predictor` argument:

- `predictor="sei"` for the standard errors (the default),
- `predictor="vi"` for the sampling variances,
- `predictor="ni"` for the sample sizes,
- `predictor="ninv"` for the inverse of the sample sizes,
- `predictor="sqrtni"` for the square root of the sample sizes, or
- `predictor="sqrtninv"` for the inverse square root of the sample sizes.

The outcome measure used for the regression test is simply determined by the values passed to the function or the measure that was used in fitting the original model (when passing an object of class "rma" to the function).

When using the sample sizes (or a transformation thereof) as the predictor, one can use the `ni` argument to specify the sample sizes. When `x` is a vector with the observed effect sizes or outcomes and it was computed with `escalc`, then the sample sizes should automatically be stored as an attribute of `x` and `ni` does not need to be specified. This should also be the case when passing an object of class "rma" to the function and the input to the model fitting function came from `escalc`.

When passing an object of class "rma" to the function, arguments such as `method`, `weighted`, and `test` as used during the initial model fitting are also used for the regression test. If the model already included one or more moderators, then `regtest` will add the chosen predictor to the moderator(s) already included in the model. This way, one can test for funnel plot asymmetry after accounting first for the influence of the moderator(s) already included in the model.

The model used for conducting the regression test can also be used to obtain a ‘limit estimate’ of the (average) true effect or outcome. In particular, when the standard errors, sampling variances, or inverse (square root) sample sizes are used as the predictor, the model intercept in essence reflects the estimate under infinite precision. This is sometimes (cautiously) interpreted as an estimate of the (average) true effect or outcome that is adjusted for publication bias.

Value

An object of class "regtest". The object is a list containing the following components:

- `model` the model used for the regression test.
- `predictor` the predictor used for the regression test.
- `zval` the value of the test statistic.
- `pval` the corresponding p-value.
- `df` the degrees of freedom of the test statistic (if the test is based on a t-distribution).
fit the full results from the fitted model.
est the limit estimate (only for predictors "sei", "vi", "ninv", or "sqrtinv" and when the model does not contain any additional moderators; NULL otherwise).
ci.lb lower bound of the confidence interval for the limit estimate.
ci.ub upper bound of the confidence intervals for the limit estimate.

The results are formatted and printed with the `print` function.

Note

The classical ‘Egger test’ is obtained by setting `model='lm'` and `predictor='sei'`. For the random/mixed-effects version of the test, set `model='rma'` (this is the default). See Sterne and Egger (2005) for details on these two types of models/tests.

When conducting a classical ‘Egger test’, the test of the limit estimate is the same as the ‘precision-effect test’ (PET) of Stanley and Doucouliagos (2014). The limit estimate when using the sampling variance as predictor is sometimes called the ‘precision-effect estimate with SE’ (PEESE) (Stanley & Doucouliagos, 2014). A conditional procedure where we use the limit estimate when PET is not significant (i.e., when using the standard error as predictor) and the PEESE (i.e., when using the sampling variance as predictor) when PET is significant is sometimes called the PET-PEESE procedure (Stanley & Doucouliagos, 2014).

All of the tests do not directly test for publication bias, but for a relationship between the observed effect sizes or outcomes and the chosen predictor. If such a relationship is present, then this usually implies asymmetry in the funnel plot, which in turn may be an indication of publication bias. However, it is important to keep in mind that there can be other reasons besides publication bias that could lead to asymmetry in the funnel plot.

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References


See Also

*ranktest* for the rank test, *trimfill* for the trim and fill method, *tes* for the test of excess significance, and *selmodel* for selection models.

Examples

```r
### copy data into 'dat' and examine data
dat <- dat.egger2001

### calculate log odds ratios and corresponding sampling variances (but remove ISIS-4 trial)
dat <- escalc(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat, subset=-16)

### fit random-effects model
res <- rma(yi, vi, data=dat)
res

### classical Egger test
regtest(res, model="lm")

### mixed-effects meta-regression version of the Egger test
regtest(res)

### same tests, but passing outcomes directly
regtest(yi, vi, data=dat, model="lm")
regtest(yi, vi, data=dat)

### if dat$yi is computed with escalc(), sample size information is stored in attributes
dat$yi

### then this will also work
regtest(yi, vi, data=dat, predictor="ni")

### similarly when passing a model object to the function
regtest(res, model="lm", predictor="ni")
regtest(res, model="lm", predictor="ninv")
regtest(res, predictor="ni")
regtest(res, predictor="ninv")

### otherwise have to supply sample sizes manually
dat$yi <- c(dat$yi) # this removes the 'ni' attribute from 'yi'
```
dat$nitotal <- with(dat, n1i + n2i)
regtest(yi, vi, ni=nitotal, data=dat, predictor="ni")
res <- rma(yi, vi, data=dat)
regtest(res, predictor="ni", ni=nitotal, data=dat)

### standard funnel plot (with standard errors on the y-axis)
funnel(res, refline=0)

### regression test (by default the standard errors are used as predictor)
reg <- regtest(res)
reg

### add regression line to funnel plot
se <- seq(0,1.8,length=100)
lines(coef(reg$fit)[1] + coef(reg$fit)[2]*se, se, lwd=3)

### regression test (using the sampling variances as predictor)
reg <- regtest(res, predictor="vi")

### add regression line to funnel plot (using the sampling variances as predictor)
lines(coef(reg$fit)[1] + coef(reg$fit)[2]*se^2, se, lwd=3, lty="dotted")

### add legend
legend("bottomright", inset=.02, lty=c("solid","dotted"), lwd=3, cex=0.9, bg="white",
  legend=c("Standard Errors as Predictor",
            "Sampling Variances as Predictor"))

### testing for asymmetry after accounting for the influence of a moderator
res <- rma(yi, vi, mods = ~ year, data=dat)
regtest(res, model="lm")
regtest(res)

---

**replmiss**

*Replace Missing Values in a Vector*

**Description**

Function to replace missing (NA) values in a vector.

**Usage**

replmiss(x, y, data)

**Arguments**

- **x** : vector that may include one or more missing values.
- **y** : either a scalar or a vector of the same length as x with the value(s) to replace missing values with.
- **data** : optional data frame containing the variables given to the arguments above.
Value

Vector x with the missing values replaced based on the scalar or vector y.

Author(s)

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Examples

```r
x <- c(4,2,7,NA,1,NA,5)
x <- replmiss(x,0)
x

x <- c(4,2,7,NA,1,NA,5)
y <- c(2,3,6,5,8,1,2)
x <- replmiss(x,y)
x
```

Description

The function dynamically generates analysis reports for objects of class "rma.uni".

Usage

```r
reporter(x, ...)
```

## S3 method for class 'rma.uni'

```r
reporter(x, dir, filename, format="html_document", open=TRUE,
digits, forest, funnel, footnotes=FALSE, verbose=TRUE, ...)
```

Arguments

- `x`: an object of class "rma.uni".
- `dir`: optional character string to specify the directory for creating the report. If unspecified, `tempdir` will be used.
- `filename`: optional character string to specify the filename (without file extension) for the report. If unspecified, the function sets a filename automatically.
- `format`: output format for the report (either `html_document`, `pdf_document`, or `word_document`). Can be abbreviated. See ‘Note’.
- `open`: logical to specify whether the report should be opened after it has been generated (the default is `TRUE`). See ‘Note’.
- `digits`: optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
forest

funnel

footnotes

verbose

Details

The function dynamically generates an analysis report based on the model object. The report includes information about the model that was fitted, the distribution of the observed effect sizes or outcomes, the estimate of the average outcome based on the fitted model, tests and statistics that are informative about potential (residual) heterogeneity in the outcomes, checks for outliers and/or influential studies, and tests for funnel plot asymmetry. By default, a forest plot and a funnel plot are also provided (these can be suppressed by setting forest=FALSE and/or funnel=FALSE).

Value

The function generates either a html, pdf, or docx file and returns (invisibly) the path to the generated document.

Note

Since the report is created based on an R markdown document that is generated by the function, the rmarkdown package and pandoc must be installed.

To render the report into a pdf document (i.e., using format="pdf_document") requires a LaTeX installation. If LaTeX is not already installed, you could try using the tinytex package to install a lightweight LaTeX distribution based on TeX Live.

Once the report is generated, the function tries to open the output file (either a .html, .pdf, or .docx file) with an appropriate application (if open=TRUE). This will only work when an appropriate application for the file type is installed and associated with the extension.

If filename is unspecified, the default is to use report, followed by an underscore (i.e., _) and the name of the object passed to the function. Both the R markdown file (with extension .rmd) and the actual report (with extension .html, .pdf, or .docx) are named accordingly. To generate the report, the model object is also saved to a file (with the same filename as above, but with extension .rdata). Also, files references.bib and apa.csl are copied to the same directory (these files are needed to generate the references in APA format).

Since the report is put together based on predefined text blocks, the writing is not very elegant. Also, using personal pronouns (‘I’ or ‘we’) does not make sense for such a report, so a lot of passive voice is used.

The generated report provides an illustration of how the results of the model can be reported, but is not a substitute for a careful examination of the results.
residuals.rma

Residual Values based on 'rma' Objects

Description

The residuals, rstandard, and rstudent functions compute residuals, corresponding standard errors, and standardized residuals for models fitted with the rma.uni, rma.mh, rma.peto, and rma.mv functions.

Usage

```r
## S3 method for class 'rma'
residuals(object, type="response", ...)

## S3 method for class 'rma.uni'
rstandard(model, digits, type="marginal", ...)
## S3 method for class 'rma.mh'
rstandard(model, digits, ...)
```

Examples

```r
### copy BCG vaccine data into 'dat'
dat <- dat.bcg

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat,
              slab=paste(author, ",", year, sep=""))

### fit random-effects model
res <- rma(yi, vi, data=dat)

## Not run:
### generate report
reporter(res)
## End(Not run)
```
Arguments

object an object of class "rma" (for residuals).

type the type of residuals which should be returned. For residuals, the alternatives are: "response" (default), "rstandard", "rstudent", and "pearson". For rstandard.rma.uni, the alternatives are: "marginal" (default) and "conditional". See 'Details'.

model an object of class "rma" (for residuals) or an object of class "rma.uni", "rma.mh", "rma.peto", or "rma.mv" (for rstandard and rstudent).

cluster optional vector to specify a clustering variable to use for computing cluster-level multivariate standardized residuals (only for "rma.mv" objects).

reestimate logical to specify whether variance/correlation components should be re-estimated after deletion of the i\textsuperscript{th} case when computing externally standardized residuals for "rma.mv" objects (the default is TRUE).

parallel character string to specify whether parallel processing should be used (the default is "no"). For parallel processing, set to either "snow" or "multicore". See 'Note'.

ncpus integer to specify the number of processes to use in the parallel processing.

cl optional cluster to use if parallel="snow". If unspecified, a cluster on the local machine is created for the duration of the call.

digits optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

progbar logical to specify whether a progress bar should be shown (only for rstudent) (the default is FALSE).

Details

The observed residuals (obtained with residuals) are simply equal to the 'observed - fitted' values. These can be obtained with residuals(object) (using the default type="response").
Dividing the observed residuals by the model-implied standard errors of the observed effect sizes or outcomes yields Pearson (or semi-standardized) residuals. These can be obtained with `residuals(object, type="pearson")`.

Dividing the observed residuals by their corresponding standard errors yields (internally) standardized residuals. These can be obtained with `rstandard(model)` or `residuals(object, type="rstandard")`.

With `rstudent(model)` (or `residuals(object, type="rstudent")`), one can obtain the externally standardized residuals (also called standardized deleted residuals or (externally) studentized residuals). The externally standardized residual for the $i$th case is obtained by deleting the $i$th case from the dataset, fitting the model based on the remaining cases, calculating the predicted value for the $i$th case based on the fitted model, taking the difference between the observed and the predicted value for the $i$th case (which yields the deleted residual), and then standardizing the deleted residual based on its standard error.

If a particular case fits the model, its standardized residual follows (asymptotically) a standard normal distribution. A large standardized residual for a case therefore may suggest that the case does not fit the assumed model (i.e., it may be an outlier).

For "rma.uni" objects, `rstandard(model, type="conditional")` computes conditional residuals, which are the deviations of the observed effect sizes or outcomes from the best linear unbiased predictions (BLUPs) of the study-specific true effect sizes or outcomes (see `blup`).

For "rma.mv" objects, one can specify a clustering variable (via the `cluster` argument). If specified, `rstandard(model)` and `rstudent(model)` also compute cluster-level multivariate (internally or externally) standardized residuals. If all outcomes within a cluster fit the model, then the multivariate standardized residual for the cluster follows (asymptotically) a chi-square distribution with $k_i$ degrees of freedom (where $k_i$ denotes the number of outcomes within the cluster).

See also `influence.rma.uni` and `influence.rma.mv` for other leave-one-out diagnostics that are useful for detecting influential cases in models fitted with the `rma.uni` and `rma.mv` functions.

**Value**

Either a vector with the residuals of the requested type (for `residuals`) or an object of class "list.rma", which is a list containing the following components:

- `resid` observed residuals (for `rstandard`) or deleted residuals (for `rstudent`).
- `se` corresponding standard errors.
- `z` standardized residuals (internally standardized for `rstandard` or externally standardized for `rstudent`).

When a clustering variable is specified for "rma.mv" objects, the returned object is a list with the first element (named `obs`) as described above and a second element (named `cluster` of class "list.rma" with:

- `X2` cluster-level multivariate standardized residuals.
- `k` number of observed effect sizes or outcomes within the clusters.

The object is formatted and printed with `print.list.rma`. To format the results as a data frame, one can use the `as.data.frame` function.
Note

The externally standardized residuals (obtained with rstudent) are calculated by refitting the model \( k \) times (where \( k \) denotes the number of cases). Depending on how large \( k \) is, it may take a few moments to finish the calculations. For complex models fitted with rma.mv, this can become computationally expensive.

On machines with multiple cores, one can try to speed things up by delegating the model fitting to separate worker processes, that is, by setting parallel="snow" or parallel="multicore" and ncpus to some value larger than 1 (only for objects of class "rma.mv"). Parallel processing makes use of the parallel package, using the makePSOCKcluster and parLapply functions when parallel="snow" or using mclapply when parallel="multicore" (the latter only works on Unix/Linux-alikes). With parallel::detectCores(), one can check on the number of available cores on the local machine.

Alternatively (or in addition to using parallel processing), one can also set reestimate=FALSE, in which case any variance/correlation components in the model are not re-estimated after deleting the \( i \)th case from the dataset. Doing so only yields an approximation to the externally standardized residuals (and the cluster-level multivariate standardized residuals) that ignores the influence of the \( i \)th case on the variance/correlation components, but is considerably faster (and often yields similar results).

It may not be possible to fit the model after deletion of the \( i \)th case from the dataset. This will result in NA values for that case when calling rstudent.

Also, for "rma.mv" objects with a clustering variable specified, it may not be possible to compute the cluster-level multivariate standardized residual for a particular cluster (if the var-cov matrix of the residuals within a cluster is not of full rank). This will result in NA for that cluster.

The variable specified via cluster is assumed to be of the same length as the data originally passed to the rma.mv function (and if the data argument was used in the original model fit, then the variable will be searched for within this data frame first). Any subsetting and removal of studies with missing values that was applied during the model fitting is also automatically applied to the variable specified via the cluster argument.

For objects of class "rma.mh" and "rma.peto", rstandard actually computes Pearson (or semi-standardized) residuals.

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References


### rma.glmm

#### Meta-Analysis via Generalized Linear (Mixed-Effects) Models

#### Description

Function to fit meta-analytic equal-, fixed-, and random-effects models and (mixed-effects) meta-regression models using a generalized linear (mixed-effects) model framework. See below and the introduction to the metafor-package for more details on these models.

#### Usage

```
rma.glmm(ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i, xi, ti, mi, ti, ni, 
  mods, measure, intercept=TRUE, data, slab, subset, 
  add=1/2, to="only0", drop00=TRUE, vtype="LS", 
  model="UM.FS", method="ML", coding=1/2, cor=FALSE, test="z", 
  level=95, btt, nAGQ=7, verbose=FALSE, digits, control, ...)
```

#### Arguments

- `ai`: see below and the documentation of the escalc function for more details.
- `bi`: see below and the documentation of the escalc function for more details.
- `ci`: see below and the documentation of the escalc function for more details.
- `di`: see below and the documentation of the escalc function for more details.
- `n1i`: see below and the documentation of the escalc function for more details.

#### See Also

rma.uni, rma.mh, rma.peto, rma.glmm, and rma.mv for functions to fit models for which the various types of residuals can be computed.

influence.rma.uni and influence.rma.mv for other model diagnostics.

#### Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model
res <- rma(yi, vi, data=dat)

### compute the studentized residuals
rstudent(res)

### fit mixed-effects model with absolute latitude as moderator
res <- rma(yi, vi, mods = ~ ablat, data=dat)

### compute the studentized residuals
rstudent(res)
```
see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

see below and the documentation of the escalc function for more details.

optional argument to include one or more moderators in the model. A single moderator can be given as a vector of length \( k \) specifying the values of the moderator. Multiple moderators are specified by giving a matrix with \( k \) rows and as many columns as there are moderator variables. Alternatively, a model formula can be used to specify the model. See ‘Details’.

character string to specify the outcome measure to use for the meta-analysis. Possible options are "OR" for the (log transformed) odds ratio, "IRR" for the (log transformed) incidence rate ratio, "PLO" for the (logit transformed) proportion, or "IRLN" for the (log transformed) incidence rate.

logical to specify whether an intercept should be added to the model (the default is TRUE).

optional data frame containing the data supplied to the function.

optional vector with labels for the \( k \) studies.

optional (logical or numeric) vector to specify the subset of studies that should be used for the analysis.

non-negative number to specify the amount to add to zero cells, counts, or frequencies when calculating the observed effect sizes or outcomes of the individual studies. See below and the documentation of the escalc function for more details.

character string to specify when the values under add should be added (either "only0", "all", "if0all", or "none"). See below and the documentation of the escalc function for more details.

logical to specify whether studies with no cases/events (or only cases) in both groups should be dropped. See the documentation of the escalc function for more details.

character string to specify the type of sampling variances to calculate when calculating the observed effect sizes or outcomes. See the documentation of the escalc function for more details.

character string to specify the general model type to use for the analysis. Either "UM.FS" (the default), "UM.RS", "CM.EL", or "CM.AL". See ‘Details’.

character string to specify whether an equal- or a random-effects model should be fitted. An equal-effects model is fitted when using method="EE". A random-effects model is fitted by setting method="ML" (the default). See ‘Details’.
coding numeric scalar to indicate how the group variable should be coded in the random effects structure for random/mixed-effects models (the default is \(1/2\)). See ‘Note’.
cor logical to indicate whether the random study effects should be allowed to be correlated with the random group effects for random/mixed-effects models when model="UM.RS" (the default is FALSE). See ‘Note’.
test character string to specify how test statistics and confidence intervals for the fixed effects should be computed. By default (test="z"), Wald-type tests and CIs are obtained, which are based on a standard normal distribution. When test="t", a t-distribution is used instead. See ‘Details’ and also here for some recommended practices.
level numeric value between 0 and 100 to specify the confidence interval level (the default is 95).
btt optional vector of indices to specify which coefficients to include in the omnibus test of moderators. Can also be a string to grep for. See ‘Details’.
nAGQ positive integer to specify the number of points per axis for evaluating the adaptive Gauss-Hermite approximation to the log-likelihood. The default is 7. Setting this to 1 corresponds to the Laplacian approximation. See ‘Note’.
verbose logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE). Can also be an integer. Values > 1 generate more verbose output. See ‘Note’.
digits optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. See also here for further details on how to control the number of digits in the output.
control optional list of control values for the estimation algorithms. If unspecified, default values are defined inside the function. See ‘Note’.

... additional arguments.

Details

Specifying the Data:
The function can be used in combination with the following effect sizes or outcome measures:
- measure="OR" for (log transformed) odds ratios,
- measure="IRR" for (log transformed) incidence rate ratios,
- measure="PLO" for (logit transformed) proportions (i.e., log odds),
- measure="IRLN" for (log transformed) incidence rates.
The escalc function describes the data/arguments that should be specified/used for these measures.

Specifying the Model:
A variety of model types are available when analyzing \(2 \times 2\) table data (i.e., when measure="OR") or two-group event count data (i.e., when measure="IRR"):
- model="UM.FS" for an unconditional generalized linear mixed-effects model with fixed study effects,
• model="UM.RS" for an unconditional generalized linear mixed-effects model with random study effects,
• model="CM.AL" for a conditional generalized linear mixed-effects model (approximate likelihood),
• model="CM.EL" for a conditional generalized linear mixed-effects model (exact likelihood).

For measure="OR", models "UM.FS" and "UM.RS" are essentially (mixed-effects) logistic regression models, while for measure="IRR", these models are (mixed-effects) Poisson regression models. The difference between "UM.FS" and "UM.RS" is how study level variability (i.e., differences in outcomes across studies irrespective of group membership) is modeled. One can choose between using fixed study effects (which means that $k$ dummy variables are added to the model) or random study effects (which means that random effects corresponding to the levels of the study factor are added to the model).

The conditional model (model="CM.EL") avoids having to model study level variability by conditioning on the total numbers of cases/events in each study. For measure="OR", this leads to a non-central hypergeometric distribution for the data within each study and the corresponding model is then a (mixed-effects) conditional logistic model. Fitting this model can be difficult and computationally expensive. When the number of cases in each study is small relative to the group sizes, one can approximate the exact likelihood by a binomial distribution, which leads to a regular (mixed-effects) logistic regression model (model="CM.AL"). For measure="IRR", the conditional model leads directly to a binomial distribution for the data within each study and the resulting model is again a (mixed-effects) logistic regression model (no approximate likelihood model is needed here).

When analyzing proportions (i.e., measure="PLO") or incidence rates (i.e., measure="IRLN") of individual groups, the model type is always a (mixed-effects) logistic or Poisson regression model, respectively (i.e., the model argument is not relevant here).

Aside from choosing the general model type, one has to decide whether to fit an equal- or a random-effects model to the data. An equal-effects model is fitted by setting method="EE". A random-effects model is fitted by setting method="ML" (the default). Note that random-effects models with dichotomous data are often referred to as ‘binomial-normal’ models in the meta-analytic literature. Analogously, for event count data, such models could be referred to as ‘Poisson-normal’ models.

One or more moderators can be included in a model via the mods argument. A single moderator can be given as a (row or column) vector of length $k$ specifying the values of the moderator. Multiple moderators are specified by giving an appropriate model matrix (i.e., $X$) with $k$ rows and as many columns as there are moderator variables (e.g., mods = cbind(mod1, mod2, mod3), where mod1, mod2, and mod3 correspond to the names of the variables for three moderator variables). The intercept is added to the model matrix by default unless intercept=FALSE.

Alternatively, one can use standard formula syntax to specify the model. In this case, the mods argument should be set equal to a one-sided formula of the form mods = ~ model (e.g., mods = ~ mod1 + mod2 + mod3). Interactions, polynomial terms, and factors can be easily added to the model in this manner. When specifying a model formula via the mods argument, the intercept argument is ignored. Instead, the inclusion/exclusion of the intercept is controlled by the specified formula (e.g., mods = ~ mod1 + mod2 + mod3 - 1 would lead to the removal of the intercept).

Equal-, Saturated-, and Random/Mixed-Effects Models:
When fitting a particular model, actually up to three different models are fitted within the function:
• the equal-effects model (i.e., where $\tau^2$ is set to 0),
• the saturated model (i.e., the model with a deviance of 0), and
• the random/mixed-effects model (i.e., where $\tau^2$ is estimated) (only if method="ML").

The saturated model is obtained by adding as many dummy variables to the model as needed so that the model deviance is equal to zero. Even when method="ML", the equal- and saturated models are also fitted, as they are used to compute the test statistics for the Wald-type and likelihood ratio tests for (residual) heterogeneity (see below).

Omnibus Test of Moderators:
For models including moderators, an omnibus test of all model coefficients is conducted that excludes the intercept (the first coefficient) if it is included in the model. If no intercept is included in the model, then the omnibus test includes all of the coefficients in the model including the first. Alternatively, one can manually specify the indices of the coefficients to test via the btt ("betas to test") argument (i.e., to test $H_0: \beta_{j\in btt} = 0$, where $\beta_{j\in btt}$ is the set of coefficients to be tested). For example, with btt=c(3,4), only the third and fourth coefficients from the model are included in the test (if an intercept is included in the model, then it corresponds to the first coefficient in the model). Instead of specifying the coefficient numbers, one can specify a string for btt. In that case, grep will be used to search for all coefficient names that match the string. The omnibus test is called the $Q_M$-test and follows asymptotically a chi-square distribution with $m$ degrees of freedom (with $m$ denoting the number of coefficients tested) under the null hypothesis (that the true value of all coefficients tested is equal to 0).

Categorical Moderators:
Categorical moderator variables can be included in the model via the mods argument in the same way that appropriately (dummy) coded categorical variables can be included in linear models. One can either do the dummy coding manually or use a model formula together with the factor function to automate the coding (note that string/character variables in a model formula are automatically converted to factors).

Tests and Confidence Intervals:
By default, tests of individual coefficients in the model (and the corresponding confidence intervals) are based on a standard normal distribution, while the omnibus test is based on a chi-square distribution (see above). As an alternative, one can set test="t", in which case tests of individual coefficients and confidence intervals are based on a t-distribution with $k - p$ degrees of freedom, while the omnibus test then uses an F-distribution with $m$ and $k - p$ degrees of freedom (with $k$ denoting the total number of estimates included in the analysis and $p$ the total number of model coefficients including the intercept if it is present). Note that test="t" is not the same as test="knha" in rma.uni, as no adjustment to the standard errors of the estimated coefficients is made.

Tests for (Residual) Heterogeneity:
Two different tests for (residual) heterogeneity are automatically carried out by the function. The first is a Wald-type test, which tests the coefficients corresponding to the dummy variables added in the saturated model for significance. The second is a likelihood ratio test, which tests the same set of coefficients, but does so by computing $-2$ times the difference in the log-likelihoods of the equal-effects and the saturated models. These two tests are not identical for the types of models fitted by the rma.glmm function and may even lead to conflicting conclusions.

Observed Effect Sizes or Outcomes of the Individual Studies:
The various models do not require the calculation of the observed effect sizes or outcomes of the individual studies (e.g., the observed log odds ratios of the \( k \) studies) and directly make use of the table/event counts. Zero cells/events are not a problem (except in extreme cases, such as when one of the two outcomes never occurs or when there are no events in any of the studies). Therefore, it is unnecessary to add some constant to the cell/event counts when there are zero cells/events. However, for plotting and various other functions, it is necessary to calculate the observed effect sizes or outcomes for the \( k \) studies. Here, zero cells/events can be problematic, so adding a constant value to the cell/event counts ensures that all \( k \) values can be calculated. The \texttt{add} and \texttt{to} arguments are used to specify what value should be added to the cell/event counts and under what circumstances when calculating the observed effect sizes or outcomes. The documentation of the \texttt{escalc} function explains how the \texttt{add} and \texttt{to} arguments work. Note that \texttt{drop00} is set to \texttt{TRUE} by default, since studies where \( ai=ci=0 \) or \( bi=di=0 \) or studies where \( x1i=x2i=0 \) are uninformative about the size of the effect.

\section*{Value}

An object of class \texttt{c("rma.glmm","rma")}. The object is a list containing the following components:

- \texttt{beta} estimated coefficients of the model.
- \texttt{se} standard errors of the coefficients.
- \texttt{zval} test statistics of the coefficients.
- \texttt{pval} corresponding p-values.
- \texttt{ci.lb} lower bound of the confidence intervals for the coefficients.
- \texttt{ci.ub} upper bound of the confidence intervals for the coefficients.
- \texttt{vb} variance-covariance matrix of the estimated coefficients.
- \texttt{tau2} estimated amount of (residual) heterogeneity. Always 0 when \texttt{method="EE"}.
- \texttt{sigma2} estimated amount of study level variability (only for \texttt{model="UM.RS"}).
- \texttt{k} number of studies included in the analysis.
- \texttt{p} number of coefficients in the model (including the intercept).
- \texttt{m} number of coefficients included in the omnibus test of moderators.
- \texttt{QE.Wld} Wald-type test statistic of the test for (residual) heterogeneity.
- \texttt{QEp.Wld} corresponding p-value.
- \texttt{QE.LRT} likelihood ratio test statistic of the test for (residual) heterogeneity.
- \texttt{QEp.LRT} corresponding p-value.
- \texttt{QM} test statistic of the omnibus test of moderators.
- \texttt{QMp} corresponding p-value.
- \texttt{I2} value of \( I^2 \).
- \texttt{H2} value of \( H^2 \).
- \texttt{int.only} logical that indicates whether the model is an intercept-only model.
- \texttt{yi, vi, X} the vector of outcomes, the corresponding sampling variances, and the model matrix.
- \texttt{fit.stats} a list with the log-likelihood, deviance, AIC, BIC, and AICc values.
- \texttt{...} some additional elements/values.
Methods

The results of the fitted model are formatted and printed with the `print` function. If fit statistics should also be given, use `summary` (or use the `fitstats` function to extract them).

Note

When `measure="OR"` or `measure="IRR"`, `model="UM.FS"` or `model="UM.RS"`, and `method="ML"`, one has to choose a coding scheme for the group variable in the random effects structure. When `code=1/2` (the default), the two groups are coded with $+1/2$ and $-1/2$ (i.e., contrast coding), which is invariant under group label switching.

When `code=1`, the first group is coded with 1 and the second group with 0. Finally, when `code=0`, the first group is coded with 0 and the second group with 1. Note that these coding schemes are not invariant under group label switching.

When `model="UM.RS"` and `method="ML"`, one has to decide whether the random study effects are allowed to be correlated with the random group effects. By default (i.e., when `cor=FALSE`), no such correlation is allowed (which is typically an appropriate assumption when `code=1/2`). When using a different coding scheme for the group variable (i.e., `code=1` or `code=0`), allowing the random study and group effects to be correlated (i.e., using `cor=TRUE`) is usually recommended.

Fitting the various types of models requires several different iterative algorithms:

- For `model="UM.FS"` and `model="CM.AL"`, iteratively reweighted least squares (IWLS) as implemented in the `glm` function is used for fitting the equal-effects and the saturated models. For `method="ML"`, adaptive Gauss-Hermite quadrature as implemented in the `glmer` function is used. The same applies when `model="CM.EL"` is used in combination with `measure="IRR"` or when `measure="PL0"` or `measure="IRLN"` (regardless of the model type).
- For `model="UM.RS"`, adaptive Gauss-Hermite quadrature as implemented in the `glmer` function is used to fit all of the models.
- For `model="CM.EL"` and `measure="OR"`, the quasi-Newton method optimizer as implemented in the `nlminb` function is used by default for fitting the equal-effects and the saturated models. For `method="ML"`, the same algorithm is used, together with adaptive quadrature as implemented in the `integrate` function (for the integration over the density of the non-central hypergeometric distribution). Standard errors of the parameter estimates are obtained by inverting the Hessian, which is numerically approximated using the `hessian` function from the `numDeriv` package.

One can also choose a different optimizer from `optim` via the `control` argument (e.g., `control=list(optimizer="BFGS")` or `control=list(optimizer="Nelder-Mead")`). Besides `nlminb` and one of the methods from `optim`, one can also choose one of the optimizers from the `minqa` package (i.e., `uobyqa`, `newuoa`, or `bobyqa`), one of the (derivative-free) algorithms from the `nloptr` package, the Newton-type algorithm implemented in `nlm`, the various algorithms implemented in the `dfoptim` package (i.e., `nmk` for the Nelder-Mead, and `mads` for the Mesh Adaptive Direct Searches algorithm), the quasi-Newton type optimizers `scipy.optimize.minimize`, and the subspace-searching simplex algorithm `subplex` from the packages of the same name, the Barzilai-Borwein gradient decent method implemented in `BBoptim`, or the parallelized version of the L-BFGS-B algorithm implemented in `optimParallel` from the package of the same name.

The optimizer name must be given as a character string (i.e., in quotes). Additional control parameters can be specified via the `optCtrl` elements of the `control` argument (e.g.,...
control=list(optCtrl=list(iter.max=1000, rel.tol=1e-8)). For \texttt{nloptr}, the default is to use the BOBYQA implementation from that package with a relative convergence criterion of 1e-8 on the function value (i.e., log-likelihood), but this can be changed via the \texttt{algorithm} and \texttt{ftol_rel} arguments (e.g., \texttt{control=list(optimizer="nloptr", optCtrl=list(algorithm="NLOPT_LN_SBPLX", ftol_rel=1e-6))}). For \texttt{optimParallel}, the control argument \texttt{ncpus} can be used to specify the number of cores to use for the parallelization (e.g., \texttt{control=list(optimizer="optimParallel", ncpus=2)}). With \texttt{parallel::detectCores()}, one can check on the number of available cores on the local machine.

When \texttt{model="CM.EL"} and \texttt{measure="OR"}, actually \texttt{model="CM.AL"} is used first to obtain starting values for \texttt{optim}, so either 4 (if \texttt{method="EE"}) or 6 (if \texttt{method="ML"}) models need to be fitted in total.

Various additional control parameters can be adjusted via the \texttt{control} argument:

- \texttt{glmCtrl} is a list of named arguments to be passed on to the \texttt{control} argument of the \texttt{glm} function,
- \texttt{glmerCtrl} is a list of named arguments to be passed on to the \texttt{control} argument of the \texttt{glmer} function,
- \texttt{intCtrl} is a list of named arguments (i.e., \texttt{rel.tol} and \texttt{subdivisions}) to be passed on to the \texttt{integrate} function, and
- \texttt{hessianCtrl} is a list of named arguments to be passed on to the \texttt{method.args} argument of the \texttt{hessian} function. Most important is the \texttt{r} argument, which is set to 16 by default (i.e., \texttt{control=list(hessianCtrl=list(r=16))}). If the Hessian cannot be inverted, it may be necessary to adjust the \texttt{r} argument to a different number (e.g., try \texttt{r=4}, \texttt{r=6}, or \texttt{r=8}).

Also, for \texttt{glmer}, the \texttt{nAGQ} argument is used to specify the number of quadrature points. The default value is 7, which should provide sufficient accuracy in the evaluation of the log-likelihood in most cases, but at the expense of speed. Setting this to 1 corresponds to the Laplacian approximation (which is faster, but less accurate). Note that \texttt{glmer} does not allow values of \texttt{nAGQ > 1} when \texttt{model="UM.RS"} and \texttt{method="ML"}, so this value is automatically set to 1 for this model.

Instead of \texttt{glmer}, one can also choose to use \texttt{mixed_model} from the \texttt{GLMMadaptive} package or \texttt{glmmTMB} from the \texttt{glmmTMB} package for the model fitting. This is done by setting \texttt{control=list(package="GLMMadaptive")} or \texttt{control=list(package="glmmTMB")}, respectively.

Information on the progress of the various algorithms can be obtained by setting \texttt{verbose=TRUE}. Since fitting the various models can be computationally expensive, this option is useful to determine how the model fitting is progressing. One can also set \texttt{verbose} to an integer (\texttt{verbose=2} yields even more information and \texttt{verbose=3} also sets \texttt{option(warn=1)} temporarily).

For \texttt{model="CM.EL"} and \texttt{measure="OR"}, optimization involves repeated calculation of the density of the non-central hypergeometric distribution. When \texttt{method="ML"}, this also requires integration over the same density. This is currently implemented in a rather brute-force manner and may not be numerically stable, especially when models with moderators are fitted. Stability can be improved by scaling the moderators in a similar manner (i.e., don’t use a moderator that is coded 0 and 1, while another uses values in the 1000s). For models with an intercept and moderators, the function actually rescales (non-dummy) variables to z-scores during the model fitting (results are given after back-scaling, so this should be transparent to the user). For models without an intercept, this is not done, so sensitivity analyses are highly recommended here (to ensure that the results do not depend on the scaling of the moderators).

Finally, there is also (highly experimental!) support for the following measures:
• measure="RR" for log transformed risk ratios,
• measure="RD" for raw risk differences,
• measure="PLN" for log transformed proportions,
• measure="PR" for raw proportions,

(the first two only for models "UM.FS" and "UM.RS") by using log and identity links for the binomial models. However, model fitting with these measures is often going to lead to numerical problems.

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Code for computing the density of the non-central hypergeometric distribution comes from the MCMCpack package, which in turn is based on Liao and Rosen (2001).

References


See Also

*rma.uni*, *rma.mh*, *rma.peto*, and *rma.mv* for other model fitting functions.

### Examples

#### random-effects model using rma.uni() (standard RE model analysis)
```
rma(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, method="ML")
```

#### random-effects models using rma.glmm() (require ‘lme4’ package)

#### unconditional model with fixed study effects
```
## Not run:
rma.glmm(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, model="UM.FS")
## End(Not run)
```

#### unconditional model with random study effects
```
## Not run:
rma.glmm(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, model="UM.RS")
## End(Not run)
```

#### conditional model with approximate likelihood
```
## Not run:
rma.glmm(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, model="CM.AL")
## End(Not run)
```

#### conditional model with exact likelihood
```
### note: fitting this model may take a bit of time, so be patient
## Not run:
rma.glmm(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, model="CM.EL")
## End(Not run)
```

---

**rma.mh**

*Meta-Analysis via the Mantel-Haenszel Method*

---

**Description**

Function to fit equal-effects models to $2 \times 2$ table and person-time data via the Mantel-Haenszel method. See below and the introduction to the **metafor-package** for more details on these models.

**Usage**

```
rma.mh(ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i,
measure="OR", data, slab, subset,
add=1/2, to="only0", drop00=TRUE,
correct=TRUE, level=95, verbose=FALSE, digits, ...)
```
Arguments

ai vector to specify the $2 \times 2$ table frequencies (upper left cell). See below and the documentation of the escalc function for more details.

bi vector to specify the $2 \times 2$ table frequencies (upper right cell). See below and the documentation of the escalc function for more details.

ci vector to specify the $2 \times 2$ table frequencies (lower left cell). See below and the documentation of the escalc function for more details.

di vector to specify the $2 \times 2$ table frequencies (lower right cell). See below and the documentation of the escalc function for more details.

n1i vector to specify the group sizes or row totals (first group). See below and the documentation of the escalc function for more details.

n2i vector to specify the group sizes or row totals (second group). See below and the documentation of the escalc function for more details.

x1i vector to specify the number of events (first group). See below and the documentation of the escalc function for more details.

x2i vector to specify the number of events (second group). See below and the documentation of the escalc function for more details.

t1i vector to specify the total person-times (first group). See below and the documentation of the escalc function for more details.

t2i vector to specify the total person-times (second group). See below and the documentation of the escalc function for more details.

measure character string to specify the outcome measure to use for the meta-analysis. Possible options are "RR" for the (log transformed) risk ratio, "OR" for the (log transformed) odds ratio, "RD" for the risk difference, "IRR" for the (log transformed) incidence rate ratio, or "IRD" for the incidence rate difference.

data optional data frame containing the data supplied to the function.

slab optional vector with labels for the $k$ studies.

subset optional (logical or numeric) vector to specify the subset of studies that should be used for the analysis.

add non-negative number to specify the amount to add to zero cells, counts, or frequencies when calculating the observed effect sizes or outcomes of the individual studies. Can also be a vector of two numbers, where the first number is used in the calculation of the observed effect sizes or outcomes and the second number is used when applying the Mantel-Haenszel method. See below and the documentation of the escalc function for more details.

to character string to specify when the values under add should be added (either "only0", "all", "if0all", or "none"). Can also be a character vector, where the first string again applies when calculating the observed effect sizes or outcomes and the second string when applying the Mantel-Haenszel method. See below and the documentation of the escalc function for more details.

drop00 logical to specify whether studies with no cases/events (or only cases) in both groups should be dropped when calculating the observed effect sizes or outcomes (the outcomes for such studies are set to NA). Can also be a vector of two
logicals, where the first applies to the calculation of the observed effect sizes or outcomes and the second when applying the Mantel-Haenszel method. See below and the documentation of the escalc function for more details.

correct
logical to specify whether to apply a continuity correction when computing the Cochran-Mantel-Haenszel test statistic.

level
numeric value between 0 and 100 to specify the confidence interval level (the default is 95).

verbose
logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE).

digits
optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. See also here for further details on how to control the number of digits in the output.

... additional arguments.

Details

Specifying the Data:

When the outcome measure is either the risk ratio (measure="RR"), odds ratio (measure="OR"), or risk difference (measure="RD"), the studies are assumed to provide data in terms of 2 × 2 tables of the form:

<table>
<thead>
<tr>
<th></th>
<th>outcome 1</th>
<th>outcome 2</th>
<th>total</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>ai</td>
<td>bi</td>
<td>n1i</td>
</tr>
<tr>
<td>group 2</td>
<td>ci</td>
<td>di</td>
<td>n2i</td>
</tr>
</tbody>
</table>

where ai, bi, ci, and di denote the cell frequencies and n1i and n2i the row totals. For example, in a set of randomized clinical trials (RCTs) or cohort studies, group 1 and group 2 may refer to the treatment (exposed) and placebo/control (not exposed) group, with outcome 1 denoting some event of interest (e.g., death) and outcome 2 its complement. In a set of case-control studies, group 1 and group 2 may refer to the group of cases and the group of controls, with outcome 1 denoting, for example, exposure to some risk factor and outcome 2 non-exposure. For these outcome measures, one needs to specify either ai, bi, ci, and di or alternatively ai, ci, n1i, and n2i.

Alternatively, when the outcome measure is the incidence rate ratio (measure="IRR") or the incidence rate difference (measure="IRD"), the studies are assumed to provide data in terms of tables of the form:

<table>
<thead>
<tr>
<th></th>
<th>events</th>
<th>person-time</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>x1i</td>
<td>t1i</td>
</tr>
<tr>
<td>group 2</td>
<td>x2i</td>
<td>t2i</td>
</tr>
</tbody>
</table>

where x1i and x2i denote the number of events in the first and the second group, respectively, and t1i and t2i the corresponding total person-times at risk.

Mantel-Haenszel Method:

An approach for aggregating data of these types was suggested by Mantel and Haenszel (1959) and later extended by various authors (see references). The Mantel-Haenszel method provides a...
weighted estimate under an equal-effects model. The method is particularly advantageous when aggregating a large number of studies with small sample sizes (the so-called sparse data or increasing strata case).

When analyzing odds ratios, the Cochran-Mantel-Haenszel (CMH) test (Cochran, 1954; Mantel & Haenszel, 1959) and Tarone’s test for heterogeneity (Tarone, 1985) are also provided (by default, the CMH test statistic is computed with the continuity correction; this can be switched off with `correct=FALSE`). When analyzing incidence rate ratios, the Mantel-Haenszel (MH) test (Rothman et al., 2008) for person-time data is also provided (again, the `correct` argument controls whether the continuity correction is applied). When analyzing risk ratios, odds ratios, or incidence rate ratios, the printed results are given both in terms of the log and the raw units (for easier interpretation).

**Observed Effect Sizes or Outcomes of the Individual Studies:**
The Mantel-Haenszel method itself does not require the calculation of the observed effect sizes or outcomes of the individual studies (e.g., the observed log odds ratios of the \( k \) studies) and directly makes use of the table/event counts. Zero cells/events are not a problem (except in extreme cases, such as when one of the two outcomes never occurs in any of the \( 2 \times 2 \) tables or when there are no events for one of the two groups in any of the tables). Therefore, it is unnecessary to add some constant to the cell/event counts when there are zero cells/events.

However, for plotting and various other functions, it is necessary to calculate the observed effect sizes or outcomes for the \( k \) studies. Here, zero cells/events can be problematic, so adding a constant value to the cell/event counts ensures that all \( k \) values can be calculated. The `add` and `to` arguments are used to specify what value should be added to the cell/event counts and under what circumstances when calculating the observed effect sizes or outcomes and when applying the Mantel-Haenszel method. Similarly, the `drop00` argument is used to specify how studies with no cases/events (or only cases) in both groups should be handled. The documentation of the `escalc` function explains how the `add`, `to`, and `drop00` arguments work. If only a single value for these arguments is specified (as per default), then these values are used when calculating the observed effect sizes or outcomes and no adjustment to the cell/event counts is made when applying the Mantel-Haenszel method. Alternatively, when specifying two values for these arguments, the first value applies when calculating the observed effect sizes or outcomes and the second value when applying the Mantel-Haenszel method.

Note that `drop00` is set to `TRUE` by default. Therefore, the observed effect sizes or outcomes for studies where \( a_i=c_i=0 \) or \( b_i=d_i=0 \) or studies where \( x_{1i}=x_{2i}=0 \) are set to `NA`. When applying the Mantel-Haenszel method, such studies are not explicitly dropped (unless the second value of `drop00` argument is also set to `TRUE`), but this is practically not necessary, as they do not actually influence the results (assuming no adjustment to the cell/event counts are made when applying the Mantel-Haenszel method).

**Value**
An object of class `c("rma.mh", "rma")`. The object is a list containing the following components:

- `beta`: aggregated log risk ratio, log odds ratio, risk difference, log rate ratio, or rate difference.
- `se`: standard error of the aggregated value.
- `zval`: test statistics of the aggregated value.
- `pval`: corresponding p-value.
ci.lb lower bound of the confidence interval.
ci.ub upper bound of the confidence interval.
QE test statistic of the test for heterogeneity.
QEp corresponding p-value.
MH Cochran-Mantel-Haenszel test statistic (measure="OR") or Mantel-Haenszel test statistic (measure="IRR").
MHp corresponding p-value.
TA test statistic of Tarone's test for heterogeneity (only when measure="OR").
TAp corresponding p-value (only when measure="OR").
k number of studies included in the analysis.
yi, vi the vector of outcomes and corresponding sampling variances.
fit.stats a list with the log-likelihood, deviance, AIC, BIC, and AICc values under the unrestricted and restricted likelihood.
... some additional elements/values.

Methods
The results of the fitted model are formatted and printed with the print function. If fit statistics should also be given, use summary (or use the fitstats function to extract them).
The residuals, rstandard, and rstudent functions extract raw and standardized residuals. Leave-one-out diagnostics can be obtained with leavelout.
Forest, funnel, radial, L'Abbé, and Baujat plots can be obtained with forest, funnel, radial, labbe, and baujat. The qqnorm function provides normal QQ plots of the standardized residuals. One can also just call plot on the fitted model object to obtain various plots at once.
A cumulative meta-analysis (i.e., adding one observation at a time) can be obtained with cumul.
Other extractor meta-analysis functions include coef, vcov, logLik, deviance, AIC, and BIC.

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References
See Also

rma.uni, rma.glmm, rma.peto, and rma.mv for other model fitting functions.

Examples

### meta-analysis of the (log) odds ratios using the Mantel-Haenszel method
rma.mh(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### meta-analysis of the (log) risk ratios using the Mantel-Haenszel method
rma.mh(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

---

**rma.mv**

*Meta-Analysis via Multivariate/Multilevel Linear (Mixed-Effects) Models*

**Description**

Function to fit meta-analytic multivariate/multilevel fixed- and random/mixed-effects models with or without moderators via linear (mixed-effects) models. See below and the introduction to the metafor-package for more details on these models.

**Usage**

`rma.mv(yi, V, W, mods, random, struct="CS", intercept=TRUE, data, slab, subset, method="REML", test="z", dfs="residual", level=95, btt, R, Rscale="cor", sigma2, tau2, rho, gamma2, phi, cvvc=FALSE, sparse=FALSE, verbose=FALSE, digits, control, ...)`

**Arguments**

- `yi` vector of length `k` with the observed effect sizes or outcomes. See ‘Details’.
- `V` vector of length `k` with the corresponding sampling variances or a `k x k` variance-covariance matrix of the sampling errors. See ‘Details’.
optional argument to specify a vector of length \( k \) with user-defined weights or a \( k \times k \) user-defined weight matrix. See ‘Details’.

.mods

optional argument to include one or more moderators in the model. A single moderator can be given as a vector of length \( k \) specifying the values of the moderator. Multiple moderators are specified by giving a matrix with \( k \) rows and as many columns as there are moderator variables. Alternatively, a model formula can be used to specify the model. See ‘Details’.

.random

either a single one-sided formula or list of one-sided formulas to specify the random-effects structure of the model. See ‘Details’.

.struct

character string to specify the variance structure of an ~ inner | outer formula in the random argument. Either "CS" for compound symmetry, "HCS" for heteroscedastic compound symmetry, "UN" or "GEN" for an unstructured variance-covariance matrix, "ID" for a scaled identity matrix, "DIAG" for a diagonal matrix, "AR" for an AR(1) autoregressive structure, "HAR" for a heteroscedastic AR(1) autoregressive structure, "CAR" for a continuous-time autoregressive structure, or one of "SPEXP", "SPGAU", "SPLIN", "SPRAT", or "SPSPH" for one of the spatial correlation structures. See ‘Details’.

.intercept

logical to specify whether an intercept should be added to the model (the default is TRUE). Ignored when mods is a formula.

data

optional data frame containing the data supplied to the function.

.slab

optional vector with labels for the \( k \) outcomes/studies.

.subset

optional (logical or numeric) vector to specify the subset of studies (or more precisely, rows of the dataset) that should be used for the analysis.

.method

character string to specify whether the model should be fitted via maximum likelihood ("ML") or via restricted maximum likelihood ("REML") estimation. Default is "REML".

test

character string to specify how test statistics and confidence intervals for the fixed effects should be computed. By default (test="z"), Wald-type tests and CIs are obtained, which are based on a standard normal distribution. When test="t", a t-distribution is used instead. See ‘Details’ and also here for some recommended practices.

dfs

character string to specify how the (denominator) degrees of freedom should be calculated when test="t". Either dfs="residual" or dfs="contain". Can also be a numeric vector with the degrees of freedom for each model coefficient. See ‘Details’.

.level

numeric value between 0 and 100 to specify the confidence interval level (the default is 95).

.btt

optional vector of indices to specify which coefficients to include in the omnibus test of moderators. Can also be a string to grep for. See ‘Details’.

.R

an optional named list of known correlation matrices corresponding to (some of) the components specified via the random argument. See ‘Details’.

.Rscale

character string, integer, or logical to specify how matrices specified via the R argument should be scaled. See ‘Details’.
**sigma2**  
optional numeric vector (of the same length as the number of random intercept components specified via the random argument) to fix the corresponding \( \sigma^2 \) value(s). A specific \( \sigma^2 \) value can be fixed by setting the corresponding element of this argument to the desired value. A specific \( \sigma^2 \) value will be estimated if the corresponding element is set equal to NA. See ‘Details’.

**tau2**  
optional numeric value (for struct="CS", "AR", "CAR", or a spatial correlation structure) or vector (for struct="HCS", "UN", or "HAR") to fix the amount of (residual) heterogeneity for the levels of the inner factor corresponding to an \( \sim \) inner | outer formula specified in the random argument. A numeric value fixes a particular \( \tau^2 \) value, while NA means that the value should be estimated. See ‘Details’.

**rho**  
optional numeric value (for struct="CS", "HCS", "AR", "HAR", "CAR", or a spatial correlation structure) or vector (for struct="UN") to fix the correlation between the levels of the inner factor corresponding to an \( \sim \) inner | outer formula specified in the random argument. A numeric value fixes a particular \( \rho \) value, while NA means that the value should be estimated. See ‘Details’.

**gamma2**  
as tau2 argument, but for a second \( \sim \) inner | outer formula specified in the random argument. See ‘Details’.

**phi**  
as rho argument, but for a second \( \sim \) inner | outer formula specified in the random argument. See ‘Details’.

**cvvc**  
logical to specify whether to calculate the variance-covariance matrix of the variance/correlation component estimates (can also be set to "varcov" or "varcor"). See ‘Details’.

**sparse**  
logical to specify whether the function should use sparse matrix objects to the extent possible (can speed up model fitting substantially for certain models). See ‘Note’.

**verbose**  
logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE). Can also be an integer. Values > 1 generate more verbose output. See ‘Note’.

**digits**  
optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. See also here for further details on how to control the number of digits in the output.

**control**  
optional list of control values for the estimation algorithms. If unspecified, default values are defined inside the function. See ‘Note’.

...  
additional arguments.

### Details

#### Specifying the Data:

The function can be used in combination with any of the usual effect sizes or outcome measures used in meta-analyses (e.g., log risk ratios, log odds ratios, risk differences, mean differences, standardized mean differences, log transformed ratios of means, raw correlation coefficients, correlation coefficients transformed with Fisher’s r-to-z transformation), or, more generally, any set of estimates (with corresponding sampling variances) one would like to meta-analyze. Simply specify the observed effect sizes or outcomes via the \( y_1 \) argument and the corresponding sampling variances via the \( v_1 \) argument (or via the weights argument if you want to directly specify the weights).
variances via the \( V \) argument. In case the sampling errors are correlated, then one can specify the entire variance-covariance matrix of the sampling errors via the \( V \) argument.

The `escalc` function can be used to compute a wide variety of effect sizes or outcome measures (and the corresponding sampling variances) based on summary statistics. Equations for computing the covariance between the sampling errors for a variety of different effect sizes or outcome measures can be found, for example, in Gleser and Olkin (2009), Lajeunesse (2011), and Wei and Higgins (2013). For raw and Fisher r-to-z transformed correlations, one can find suitable equations, for example, in Steiger (1980). The latter are implemented in the `rcalc` function. See also `vcalc` for a function that can be used to construct or approximate the variance-covariance matrix of dependent effect sizes or outcomes for a wide variety of circumstances. See also here for some recommendations on a general workflow for meta-analyses involving complex dependency structures.

Specifying Fixed Effects:
With `rma.mv(yi, V)`, a fixed-effects model is fitted to the data (note: arguments `struct`, `sigma2`, `tau2`, `rho`, `gamma2`, `phi`, `R`, and `Rscale` are not relevant then and are ignored). The model is then simply given by \( y \sim N(\theta, V) \), where \( y \) is a (column) vector with the observed outcomes, \( \theta \) is the (average) true outcome, and \( V \) is the variance-covariance matrix of the sampling errors (if a vector of sampling variances is provided via the \( V \) argument, then \( V \) is assumed to be diagonal). Note that the argument is \( V \), not \( v \) (\( R \) is case sensitive!).

One or more moderators can be included in the model via the `mods` argument. A single moderator can be given as a (row or column) vector of length \( k \) specifying the values of the moderator. Multiple moderators are specified by giving an appropriate model matrix (i.e., \( X \)) with \( k \) rows and as many columns as there are moderator variables (e.g., `mods = cbind(mod1, mod2, mod3)`, where `mod1`, `mod2`, and `mod3` correspond to the names of the variables for the three moderator variables). The intercept is added to the model matrix by default unless `intercept=FALSE`.

Alternatively, one can use standard `formula` syntax to specify the model. In this case, the `mods` argument should be set equal to a one-sided formula of the form `mods = ~ model` (e.g., `mods = ~ mod1 + mod2 + mod3`). Interactions, polynomial terms, and factors can be easily added to the model in this manner. When specifying a model formula via the `mods` argument, the `intercept` argument is ignored. Instead, the inclusion/exclusion of the intercept is controlled by the specified formula (e.g., `mods = ~ mod1 + mod2 + mod3 - 1` would lead to the removal of the intercept). One can also directly specify moderators via the `yi` argument (e.g., `rma.mv(yi ~ mod1 + mod2 + mod3, V)`). In that case, the `mods` argument is ignored and the inclusion/exclusion of the intercept again is controlled by the specified formula.

With moderators included, the model is then given by \( y \sim N(X\beta, V) \), where \( X \) denotes the model matrix containing the moderator values (and possibly the intercept) and \( \beta \) is a column vector containing the corresponding model coefficients. The model coefficients (i.e., \( \beta \)) are then estimated with \( \hat{b} = (X'WX')^{-1}X'Wy \), where \( W = V^{-1} \) is the weight matrix (without moderators, \( X \) is just a column vector of 1’s). With the `W` argument, one can also specify user-defined weights (or a weight matrix).

Specifying Random Effects:
One can fit random/mixed-effects models to the data by specifying the desired random effects structure via the `random` argument. The `random` argument is either a single one-sided formula or a list of one-sided formulas. One formula type that can be specified via this argument is of the form `random = ~ 1 | id`. Such a formula adds a random effect corresponding to the grouping variable `id` to the model. Outcomes with the same value of the `id` variable receive the same
value of the random effect, while outcomes with different values of the id variable are assumed to be independent. The variance component corresponding to such a formula is denoted by \( \sigma^2 \). An arbitrary number of such formulas can be specified as a list of formulas (e.g., \( \text{random} = \text{list}(\sim 1 | \text{id1}, \sim 1 | \text{id2}) \)), with variance components \( \sigma^2_1, \sigma^2_2 \), and so on. Nested random effects of this form can also be added using \( \text{random} = \sim 1 | \text{id1/id2} \), which adds a random effect corresponding to the grouping variable \( \text{id1} \) and a random effect corresponding to \( \text{id2} \) within \( \text{id1} \) to the model. This can be extended to models with even more levels of nesting (e.g., \( \text{random} = \sim 1 | \text{id1/id2/id3} \)).

Random effects of this form are useful to model clustering (and hence non-independence) induced by a multilevel structure in the data (e.g., outcomes derived from the same paper, lab, research group, or species may be more similar to each other than outcomes derived from different papers, labs, research groups, or species). See, for example, Konstantopoulos (2011) and Nakagawa and Santos (2012) for more details.


In addition or alternatively to specifying one or multiple \( \sim 1 | \text{id} \) terms, the \texttt{random} argument can also contain a formula of the form \( \sim \text{inner} | \text{outer} \). Outcomes with the same value of the outer grouping variable share correlated random effects corresponding to the levels of the inner grouping variable, while outcomes with different values of the outer grouping variable are assumed to be independent (note that the inner variable is automatically treated as a factor). The \texttt{struct} argument is used to specify the variance structure corresponding to the inner variable. With \texttt{struct="CS"}, a compound symmetric structure is assumed (i.e., a single variance component \( \tau^2 \) corresponding to the \( j = 1, \ldots, J \) levels of the inner variable and a single correlation coefficient \( \rho \) for the correlation between the different levels). With \texttt{struct="HCS"}, a heteroscedastic compound symmetric structure is assumed (with \( \tau^2_j \) denoting the variance component corresponding to the \( j \)th level of the inner variable and a single correlation coefficient \( \rho \) for the correlation between the different levels). With \texttt{struct="UN"}, an unstructured (but positive definite) variance-covariance matrix is assumed (with \( \tau^2_{jj} \) as described above and correlation coefficient \( \rho_{jj'} \) for the combination of the \( j \)th and \( j' \)th level of the inner variable). For example, for an inner variable with four levels, the three structures correspond to variance-covariance matrices of the form:

\[
\begin{bmatrix}
\tau^2 & \rho \tau^2 & \tau^2 \\
\rho \tau^2 & \tau^2 & \tau^2 \\
\rho \tau^2 & \rho \tau^2 & \tau^2
\end{bmatrix}
\quad
\begin{bmatrix}
\tau^2_1 & \rho_{21} \tau^2_1 & \tau^2_2 \\
\rho_{31} \tau^2_1 & \tau^2_3 & \tau^2_4 \\
\rho_{41} \tau^2_1 & \rho_{42} \tau^2_1 & \tau^2_4
\end{bmatrix}
\quad
\begin{bmatrix}
\tau^2_1 & \rho_{21} \tau^2_1 & \rho_{31} \tau^2_1 & \rho_{41} \tau^2_1 \\
\rho_{21} \tau^2_1 & \tau^2_2 & \rho_{32} \tau^2_2 & \rho_{42} \tau^2_2 \\
\rho_{31} \tau^2_1 & \rho_{32} \tau^2_2 & \tau^2_3 & \rho_{43} \tau^2_3 \\
\rho_{41} \tau^2_1 & \rho_{42} \tau^2_2 & \rho_{43} \tau^2_3 & \tau^2_4
\end{bmatrix}
\]

Structures \texttt{struct="ID"} and \texttt{struct="DIAG"} are just like \texttt{struct="CS"} and \texttt{struct="HCS"}, respectively, except that \( \rho \) is set to 0, so that we either get a scaled identity matrix or a diagonal matrix.

With the outer term corresponding to a study identification variable and the inner term to a variable indicating the treatment type or study arm, such a random effect could be used to estimate how strongly different treatment effects or outcomes within the same study are correlated and/or whether the amount of heterogeneity differs across different treatment types/arms. Network meta-analyses (also known as mixed treatment comparisons) will also typically require such a random effect (e.g., Salanti et al., 2008). The meta-analytic bivariate model (e.g., van Houwelingen, Arends, & Stijnen, 2002) can also be fitted in this manner (see the examples below). The inner term could also correspond to a variable indicating different types of outcomes measured within the same study, which allows for fitting multivariate models with multiple correlated effects/outcomes per study (e.g., Berkey et al., 1998; Kalaian & Raudenbush, 1996).

For meta-analyses of studies reporting outcomes at multiple time points, it may also be reasonable to assume that the true effects/outcomes are correlated over time according to an autoregressive structure (Ishak et al., 2007; Trikalinos & Olkin, 2012). For this purpose, one can choose `struct="AR"`, corresponding to a structure with a single variance component \( \tau^2 \) and AR(1) autocorrelation among the values of the random effect. The values of the \( \text{inner} \) variable should then reflect the various time points, with increasing values reflecting later time points. This structure assumes equally spaced time points, so the actual values of the \( \text{inner} \) variable are not relevant, only their ordering. One can also use `struct="HAR"`, which allows for fitting a heteroscedastic AR(1) structure (with \( \tau_j^2 \) denoting the variance component of the \( j \)th measurement occasion). Finally, when time points are not evenly spaced, one might consider using `struct="CAR"` for a continuous-time autoregressive structure, in which case the values of the \( \text{inner} \) variable should reflect the exact time points of the measurement occasions. For example, for an \( \text{inner} \) variable with four time points, these structures correspond to variance-covariance matrices of the form:

\[
\begin{bmatrix}
\tau^2 & \rho \tau^2 & \rho^2 \tau^2 & \rho^3 \tau^2 \\
\rho \tau^2 & \tau^2 & \rho \tau^2 & \rho^2 \tau^2 \\
\rho^2 \tau^2 & \rho \tau^2 & \tau^2 & \rho \tau^2 \\
\rho^3 \tau^2 & \rho^2 \tau^2 & \rho \tau^2 & \tau^2 \\
\end{bmatrix}
\]

\[
\begin{bmatrix}
\tau_1^2 & \rho \tau_1 \tau_2 & \rho^2 \tau_1 \tau_2 & \rho^3 \tau_1 \tau_2 \\
\rho \tau_1 \tau_2 & \tau_2^2 & \rho \tau_2 \tau_3 & \rho^2 \tau_2 \tau_3 \\
\rho^2 \tau_1 \tau_2 & \rho \tau_2 \tau_3 & \tau_3^2 & \rho \tau_3 \tau_4 \\
\rho^3 \tau_1 \tau_2 & \rho^2 \tau_2 \tau_3 & \rho \tau_3 \tau_4 & \tau_4^2 \\
\end{bmatrix}
\]

\[
\begin{bmatrix}
\tau_j^2 & \rho \tau_{j-1-5} \tau_{j-4-5} & \rho^2 \tau_{j-1-5} \tau_{j-4-5} & \rho^3 \tau_{j-1-5} \tau_{j-4-5} \\
\rho \tau_{j-1-5} \tau_{j-4-5} & \tau_{j-4-5}^2 & \rho \tau_{j-4-5} \tau_{j-3-5} & \rho^2 \tau_{j-4-5} \tau_{j-3-5} \\
\rho^2 \tau_{j-1-5} \tau_{j-4-5} & \rho \tau_{j-4-5} \tau_{j-3-5} & \tau_{j-3-5}^2 & \rho \tau_{j-3-5} \tau_{j-2-5} \\
\rho^3 \tau_{j-1-5} \tau_{j-4-5} & \rho^2 \tau_{j-4-5} \tau_{j-3-5} & \rho \tau_{j-3-5} \tau_{j-2-5} & \tau_{j-2-5}^2 \\
\end{bmatrix}
\]

See `dat.fine1993` and `dat.ishak2007` for examples involving such structures.

For outcomes that have a known spatial configuration, various spatial correlation structures are also available. For these structures, the formula is of the form `random ~ var1 + var2 + \ldots | outer`, where `var1`, `var2`, and so on are variables to indicate the spatial coordinates (e.g., longitude and latitude) based on which distances (by default Euclidean) will be computed. Let \( d \) denote the distance between two points that share the same value of the outer variable (if all true effects/outcomes are allowed to be spatially correlated, simply set outer to a variable that is a constant). Then the correlation between the true effects/outcomes corresponding to these two points is a function of \( d \) and the parameter \( \rho \). The following table shows the types of spatial correlation structures that can be specified and the equations for the correlation. The covariance between the true effects/outcomes is then the correlation times \( \tau^2 \).

<table>
<thead>
<tr>
<th>structure</th>
<th>struct</th>
<th>correlation</th>
</tr>
</thead>
<tbody>
<tr>
<td>exponential</td>
<td>&quot;SPEXP&quot;</td>
<td>( \exp(-d/\rho) )</td>
</tr>
<tr>
<td>Gaussian</td>
<td>&quot;SPGAU&quot;</td>
<td>( \exp(-d^2/\rho^2) )</td>
</tr>
<tr>
<td>linear</td>
<td>&quot;SPLIN&quot;</td>
<td>( (1 - d/\rho) I(d &lt; \rho) )</td>
</tr>
<tr>
<td>rational quadratic</td>
<td>&quot;SPRAT&quot;</td>
<td>( 1 - (d/\rho)^2/(1 + (d/\rho)^2) )</td>
</tr>
<tr>
<td>spherical</td>
<td>&quot;SPSPH&quot;</td>
<td>( (1 - 1.5(d/\rho) + 0.5(d/\rho)^3)I(d &lt; \rho) )</td>
</tr>
</tbody>
</table>

Note that \( I(d < \rho) \) is equal to 1 if \( d < \rho \) and 0 otherwise. The parameterization of the various structures is based on Pinheiro and Bates (2000). Instead of Euclidean distances, one can also use other distance measures by setting (the undocumented) argument `dist` to either "maximum"
for the maximum distance between two points (supremum norm), to "manhattan" for the absolute distance between the coordinate vectors (L1 norm), or to "gcd" for the great-circle distance (WGS84 ellipsoid method). In the latter case, only two variables, namely the longitude and latitude (in decimal degrees, with minus signs for West and South), must be specified.

If a distance matrix has already been computed, one can also pass this matrix as a list element to the dist argument. In this case, one should use a formula of the form random = ~ id | outer, where id are location identifiers, with corresponding row/column names in the distance matrix specified via the dist argument.

See dat.maire2019 for an example of a meta-analysis with a spatial correlation structure.

An ~ inner | outer formula can also be used to add random effects to the model corresponding to a set of predictor variables when struct="GEN". Here, the inner term is used to specify one or multiple variables (e.g., random = ~ var1 + var2 | outer) and corresponding ‘random slopes’ are added to the model (and a ‘random intercept’ unless the intercept is removed from the inner term). The variance-covariance matrix of the random effects added in this manner is assumed to be a general unstructured (but positive definite) matrix. Such a random effects structure may be useful in a meta-analysis examining the dose-response relationship between a moderator variable and the size of the true effects/outcomes (sometimes called a ‘dose-response meta-analysis’).

See dat.obrien2003 for an example of a meta-analysis examining a dose-response relationship. The random argument can also contain a second formula of the form ~ inner | outer (but no more!). A second formula of this form works exactly described as above, but its variance components are denoted by $\gamma^2$ and its correlation components by $\phi$. The struct argument should then be of length 2 to specify the variance-covariance structure for the first and second component, respectively.

When the random argument contains a formula of the form ~ 1 | id, one can use the (optional) argument R to specify a corresponding known correlation matrix for the random effect (i.e., $R = \text{list}(id = \text{Cor})$, where Cor is the correlation matrix). In that case, outcomes with the same value of the id variable receive the same value for the random effect, while outcomes with different values of the id variable receive values that are correlated as specified in the corresponding correlation matrix given via the R argument. The column/row names of the correlation matrix given via the R argument must therefore correspond to the unique values of the id variable. When the random argument contains multiple formulas of the form ~ 1 | id, one can specify known correlation matrices for none, some, or all of those terms (e.g., with random = list(~ 1 | id1, ~ 1 | id2), one could specify $R = \text{list}(id1 = \text{Cor1})$ or $R = \text{list}(id1 = \text{Cor1}, id2 = \text{Cor2})$, where Cor1 and Cor2 are the correlation matrices corresponding to the grouping variables id1 and id2, respectively).

Such a random effect with a known (or at least approximately known) correlation structure is useful in a variety of contexts. For example, such a component can be used to account for the correlations induced by the shared phylogenetic history among organisms (e.g., plants, fungi, animals). In that case, ~ 1 | species is used to specify the species and argument R is used to specify the phylogenetic correlation matrix of the species studied in the meta-analysis. The corresponding variance component then indicates how much variance/heterogeneity is attributable to the specified phylogeny. See Nakagawa and Santos (2012) for more details. As another example, in a genetic meta-analysis studying disease association for several single nucleotide polymorphisms (SNPs), linkage disequilibrium (LD) among the SNPs can induce an approximately known degree of correlation among the effects/outcomes. In that case, ~ 1 | snp could be used to specify the SNPs and R the corresponding LD correlation matrix for the SNPs included in the meta-analysis.

The Rscale argument controls how matrices specified via the R argument are scaled. With Rscale="none" (or Rscale=0 or Rscale=FALSE), no scaling is used. With Rscale="cor" (or
Rs2 = 1 or Rs2 = TRUE, the cov2cor function is used to ensure that the matrices are correlation matrices (assuming they were covariance matrices to begin with). With Rs2 = "cor0" (or Rs2 = 2), first cov2cor is used and then the elements of each correlation matrix are scaled with \((R - \min(R))/\(1 - \min(R))\) (this ensures that a correlation of zero in a phylogenetic correlation matrix corresponds to the split at the root node of the tree comprising the species that are actually analyzed). Finally, Rs2 = "cov0" (or Rs2 = 3) only rescales with \(R - \min(R)\) (which ensures that a phylogenetic covariance matrix is rooted at the lowest split).

See dat.moura2021 and dat.lim2014 for examples of meta-analyses with phylogenetic correlation structures.

Together with the variance-covariance matrix of the sampling errors (i.e., \(V\)), the specified random effects structure of the model implies a particular ‘marginal’ variance-covariance matrix of the observed effect sizes or outcomes. Once estimates of the variance components (i.e., of the \(\sigma^2\), \(\tau^2\), \(\phi\), \(\gamma^2\), and/or \(\phi\) values) have been obtained (either using maximum likelihood or restricted maximum likelihood estimation), the estimated marginal variance-covariance matrix can be constructed (denoted by \(M\)). The model coefficients (i.e., \(\beta\)) are then estimated with \(b = (X'WX)^{-1}X'Wy\), where \(W = M^{-1}\) is the weight matrix. With \(W\) argument, one can again specify user-defined weights (or a weight matrix).

Fixing Variance/Correlation Components:
Arguments sigma2, tau2, rho, gamma2, and phi can be used to fix particular variance/correlation components at a given value. This is useful for sensitivity analyses (e.g., for plotting the regular/restricted log-likelihood as a function of a particular variance/correlation component), likelihood ratio tests, or for imposing a desired variance-covariance structure on the data.

For example, if random = list(~ 1 | id1, ~ 1 | id2) or random = ~ 1 | id1/id2, then sigma2 must be of length 2 (corresponding to \(\sigma_1^2\) and \(\sigma_2^2\)) and a fixed value can be assigned to either or both variance components. Setting a particular component to \(\text{NA}\) means that the component will be estimated by the function (e.g., sigma2 = c(\(\text{NA}\), \(\text{NA}\))) will fix \(\sigma_1^2\) to 0 and estimate \(\sigma_2^2\).

Argument tau2 is only relevant when the random argument contains an \(~ \text{inner} | \text{outer}\) formula. In that case, if the tau2 argument is used, it must be either of length 1 (for "CS", "ID", "AR", "CAR", or one of the spatial correlation structures) or of the same length as the number of unique values of the inner variable (for "HCS", "DIAG", "UN", or "HAR"). A numeric value in the tau2 argument then fixes the corresponding variance component to that value, while \(\text{NA}\) means that the component will be estimated. Similarly, if argument rho is used, it must be either of length 1 (for "CS", "HCS", "AR", "HAR", or one of the spatial correlation structures) or of length \(J(J - 1)/2\) (for "UN"), where \(J\) denotes the number of unique values of the inner variable. Again, a numeric value fixes the corresponding correlation, while \(\text{NA}\) means that the correlation will be estimated. For example, with struct="CS" and rho=\(\text{NA}\), the variance-covariance matrix of the inner variable will be diagonal with \(\tau^2\) along the diagonal. For struct="UN", the values specified under rho should be given in column-wise order (e.g., for an inner variable with four levels, the order would be \(\rho_{21}, \rho_{31}, \rho_{41}, \rho_{32}, \rho_{42}, \rho_{43}\)).

Similarly, arguments gamma2 and phi are only relevant when the random argument contains a second \(~ \text{inner} | \text{outer}\) formula. The arguments then work exactly as described above.

Omnibus Test of Moderators:
For models including moderators, an omnibus test of all model coefficients is conducted that excludes the intercept (the first coefficient) if it is included in the model. If no intercept is included in the model, then the omnibus test includes all coefficients in the model including the first. Alternatively, one can manually specify the indices of the coefficients to test via the btt ("betas to
test') argument (i.e., to test $H_0: \beta_j \in btt = 0$, where $\beta_j \in btt$ is the set of coefficients to be tested). For example, with $btt=c(3,4)$, only the third and fourth coefficients from the model are included in the test (if an intercept is included in the model, then it corresponds to the first coefficient in the model). Instead of specifying the coefficient numbers, one can specify a string for $btt$. In that case, `grep` will be used to search for all coefficient names that match the string. The omnibus test is called the $Q_M$-test and follows asymptotically a chi-square distribution with $m$ degrees of freedom (with $m$ denoting the number of coefficients tested) under the null hypothesis (that the true value of all coefficients tested is equal to 0).

**Categorical Moderators:**

Categorical moderator variables can be included in the model via the `mods` argument in the same way that appropriately (dummy) coded categorical variables can be included in linear models. One can either do the dummy coding manually or use a model formula together with the `factor` function to automate the coding (note that string/character variables in a model formula are automatically converted to factors).

**Tests and Confidence Intervals:**

By default, tests of individual coefficients in the model (and the corresponding confidence intervals) are based on a standard normal distribution, while the omnibus test is based on a chi-square distribution (see above). As an alternative, one can set `test="t"`, in which case tests of individual coefficients and confidence intervals are based on a t-distribution with $k - p$ degrees of freedom, while the omnibus test then uses an F-distribution with $m$ and $k - p$ degrees of freedom (with $k$ denoting the total number of estimates included in the analysis and $p$ the total number of model coefficients including the intercept if it is present). Note that `test="t"` is not the same as `test="knha"` in `rma.uni`, as no adjustment to the standard errors of the estimated coefficients is made.

The method for calculating the (denominator) degrees of freedom described above (which corresponds to `dfs="residual"`) is quite simplistic and may lead to tests with inflated Type I error rates and confidence intervals that are too narrow on average. As an alternative, one can set `dfs="contain"` (which automatically also sets `test="t"`), in which case the degrees of freedom for the test of a particular model coefficient, $b_j$, are determined by checking whether $x_j$, the corresponding column of the model matrix $X$, varies at the level corresponding to a particular random effect in the model. If such a random effect can be found, then the degrees of freedom are set to $l - p$, where $l$ denotes the number of unique values of this random effect (i.e., for an ~ 1 | id term, the number of unique values of the id variable and for an ~ inner | outer term, the number of unique values of the outer variable). If no such random effect can be found, then $k - p$ is used as the degrees of freedom. For the omnibus F-test, the minimum of the degrees of freedom of all coefficients involved in the test is used as the denominator degrees of freedom. This approach for calculating the degrees of freedom should often lead to tests with better control of the Type I error rate and confidence intervals with closer to nominal coverage rates (see also here).

One can also set `dfs` to a numeric vector with the desired values for the degrees of freedom for testing the model coefficients (e.g., if some other method for determining the degrees of freedom was used).

**Tests and Confidence Intervals for Variance/Correlation Components:**

Depending on the random effects structure specified, the model may include one or multiple variance/correlation components. Profile likelihood confidence intervals for such components can be obtained using the `confint` function. Corresponding likelihood ratio tests can be obtained
using the \texttt{anova} function (by comparing two models where the size of the component to be tested is constrained to some null value in the reduced model). It is also always a good idea to examine plots of the (restricted) log-likelihood as a function of the variance/correlation components in the model using the \texttt{profile} function to check for parameter identifiability (see ‘Note’).

**Test for (Residual) Heterogeneity:**
A test for (residual) heterogeneity is automatically carried out by the function. Without moderators in the model, this test is the generalized/weighted least squares extension of Cochran’s $Q$-test, which tests whether the variability in the observed effect sizes or outcomes is larger than one would expect based on sampling variability (and the given covariances among the sampling errors) alone. A significant test suggests that the true effects/outcomes are heterogeneous. When moderators are included in the model, this is the $Q_E$-test for residual heterogeneity, which tests whether the variability in the observed effect sizes or outcomes that is not accounted for by the moderators included in the model is larger than one would expect based on sampling variability (and the given covariances among the sampling errors) alone.

**Var-Cov Matrix of the Variance/Correlation Component Estimates:**
In some cases, one might want to obtain the variance-covariance matrix of the variance/correlation component estimates (i.e., of the estimated $\sigma^2$, $\tau^2$, $\rho$, $\gamma^2$, $\phi$ values). The function will try to calculate this matrix when \texttt{cvvc=TRUE} (or equivalently, when \texttt{cvvc="varcor"}). This is done by inverting the Hessian, which is numerically approximated using the \texttt{hessian} function from the \texttt{numDeriv} package. Note that these computations may not be numerically stable, especially when the estimates are close to their parameter bounds and/or the likelihood surface is relatively flat around its maximum. When \texttt{struct="UN"}, one can also set \texttt{cvvc="varcov"} in which case the variance-covariance matrix is given for the variance and covariance components (instead of the correlation components).

**Value**
An object of class \texttt{c("rma.mv","rma")}. The object is a list containing the following components:

- \texttt{beta} estimated coefficients of the model.
- \texttt{se} standard errors of the coefficients.
- \texttt{zval} test statistics of the coefficients.
- \texttt{pval} corresponding p-values.
- \texttt{ci.lb} lower bound of the confidence intervals for the coefficients.
- \texttt{ci.ub} upper bound of the confidence intervals for the coefficients.
- \texttt{vb} variance-covariance matrix of the estimated coefficients.
- \texttt{sigma2} estimated $\sigma^2$ value(s).
- \texttt{tau2} estimated $\tau^2$ value(s).
- \texttt{rho} estimated $\rho$ value(s).
- \texttt{gamma2} estimated $\gamma^2$ value(s).
- \texttt{phi} estimated $\phi$ value(s).
- \texttt{k} number of observed effect sizes or outcomes included in the analysis.
- \texttt{p} number of coefficients in the model (including the intercept).
m  number of coefficients included in the omnibus test of moderators.
QE  test statistic of the test for (residual) heterogeneity.
QE_p  corresponding p-value.
QM  test statistic of the omnibus test of moderators.
QM_p  corresponding p-value.
int.only  logical that indicates whether the model is an intercept-only model.
yi, V, X  the vector of outcomes, the corresponding variance-covariance matrix of the sampling errors, and the model matrix.
M  the estimated marginal variance-covariance matrix of the observed effect sizes or outcomes.
fit.stats  a list with the log-likelihood, deviance, AIC, BIC, and AICc values.
vvc  variance-covariance matrix of the variance/correlation component estimates (NA when cvvc=FALSE).
...  some additional elements/values.

Methods

The results of the fitted model are formatted and printed with the print function. If fit statistics should also be given, use summary (or use the fitstats function to extract them). Full versus reduced model comparisons in terms of fit statistics and likelihood ratio tests can be obtained with anova. Wald-type tests for sets of model coefficients or linear combinations thereof can be obtained with the same function. Tests and confidence intervals based on (cluster) robust methods can be obtained with robust.

Predicted/fitted values can be obtained with predict and fitted. For best linear unbiased predictions, see ranef.

The residuals, rstandard, and rstudent functions extract raw and standardized residuals. See influence for additional model diagnostics (e.g., to determine influential studies). For models with moderators, variance inflation factors can be obtained with vif.

Confidence intervals for any variance/correlation components in the model can be obtained with confint.

For random/mixed-effects models, the profile function can be used to obtain a plot of the (restricted) log-likelihood as a function of a specific variance/correlation component of the model. For models with moderators, regplot draws scatter plots / bubble plots, showing the (marginal) relationship between the observed outcomes and a selected moderator from the model.

Other extractor functions include coef, vcov, logLik, deviance, AIC, BIC, hatvalues, and weights.

Note

Argument V also accepts a list of variance-covariance matrices for the observed effect sizes or outcomes. From the list elements, the full (block diagonal) variance-covariance matrix is then automatically constructed. For this to work correctly, the list elements must be in the same order as the observed outcomes.

Model fitting is done via numerical optimization over the model parameters. By default, nlminb is used for the optimization. One can also choose a different optimizer from optim via the control argument (e.g., control=list(optimizer="BFGS") or control=list(optimizer="Nelder-Mead").
Besides `nlminb` and one of the methods from `optim`, one can also choose one of the optimizers from the `minqa` package (i.e., `uobyqa`, `newuoa`, or `bobyqa`), one of the (derivative-free) algorithms from the `nloptr` package, the Newton-type algorithm implemented in `nlm`, the various algorithms implemented in the `dfoptim` package (`hjk` for the Hooke-Jeeves, `nmk` for the Nelder-Mead, and `mads` for the Mesh Adaptive Direct Searches algorithm), the quasi-Newton type optimizers `ucminf` and `lbfgsb3c` and the subspace-searching simplex algorithm `subplex` from the packages of the same name, the Barzilai-Borwein gradient decent method implemented in `BBoptim`, or the parallelized version of the L-BFGS-B algorithm implemented in `optimParallel` from the package of the same name.

The optimizer name must be given as a character string (i.e., in quotes). Additional control parameters can be specified via the `control` argument (e.g., `control=list(iter.max=1000, rel.tol=1e-8)`). For `nloptr`, the default is to use the BOBYQA implementation from that package with a relative convergence criterion of $1e^{-8}$ on the function value (i.e., log-likelihood), but this can be changed via the `algorithm` and `ftop_rel` arguments (e.g., `control=list(optimizer="nloptr", algorithm="NLOPT_LN_SBPLX", ftol_rel=1e-6)`). For `optimParallel`, the control argument `ncpus` can be used to specify the number of cores to use for the parallelization (e.g., `control=list(optimizer="optimParallel", ncpus=2)`). With `parallel::detectCores()`, one can check on the number of available cores on the local machine.

At the moment, the starting values are not chosen in a terribly clever way and could be far off. As a result, the optimizer may be slow to converge or may even get stuck at a local maximum. One can set the starting values manually for the various variance/correlation components in the model via the `control` argument by specifying the vectors `sigma2.init`, `tau2.init`, `rho.init`, `gamma2.init`, and/or `phi.init` as needed. Especially for complex models, it is a good idea to try out different starting values to make sure that the same estimates are obtained.

Information on the progress of the optimization algorithm can be obtained by setting `verbose=TRUE` (this won’t work when using parallelization). Since fitting complex models with many random effects can be computationally expensive, this option is useful to determine how the model fitting is progressing. One can also set `verbose` to an integer (`verbose=2` yields even more information and `verbose=3` also sets `option(warn=1)` temporarily).

Whether a particular variance/correlation component is actually identifiable needs to be carefully examined when fitting complex models. The function does some limited checking internally to fix variances and/or correlations at zero when it is clear that insufficient information is available to estimate a particular parameter (e.g., if a particular factor has only a single level, the corresponding variance component cannot be estimated). However, it is strongly advised in general to do post model fitting checks to make sure that the likelihood surface around the ML/REML estimates is not flat for some combination of the parameter estimates (which would imply that the estimates are essentially arbitrary). For example, one can plot the (restricted) log-likelihood as a function of each variance/correlation component in the model to make sure that each profile plot shows a clear peak at the corresponding ML/REML estimate. The `profile` function can be used for this purpose.

Finally, note that the model fitting is not done in a very efficient manner at the moment, which is partly a result of allowing for crossed random effects and correlations across the entire dataset (e.g., when using the `R` argument). As a result, the function works directly with the entire $k \times k$ (marginal) variance-covariance matrix of the observed effect sizes or outcomes (instead of working with smaller blocks in a block diagonal structure). As a result, model fitting can be slow for large $k$. However, when the variance-covariance structure is actually sparse, a lot of speed can be gained by setting `sparse=TRUE`, in which case sparse matrix objects are used (via the `Matrix` package). Also, when model fitting appears to be slow, setting `verbose=TRUE` is useful to obtain information
on how the model fitting is progressing.

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**References**


**See Also**

*rma.uni, rma.mh, rma.peto, and rma.glmm* for other model fitting functions.
### Examples

```r
### calculate log odds ratios and corresponding sampling variances
dat <- escalc(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model using rma.uni()
rma(yi, vi, data=dat)

### fit random-effects model using rma.mv()
### note: sigma^2 in this model is the same as tau^2 from the previous model
rma.mv(yi, vi, random = ~ 1 | trial, data=dat)

### change data into long format
dat.long <- to.long(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### set levels of group variable ("exp" = experimental/vaccinated; "con" = control/non-vaccinated)
levels(dat.long$group) <- c("exp", "con")

### set "con" to reference level
dat.long$group <- relevel(dat.long$group, ref="con")

### calculate log odds and corresponding sampling variances
dat.long <- escalc(measure="PLO", xi=out1, mi=out2, data=dat.long)

### fit bivariate random-effects model using rma.mv()
res <- rma.mv(yi, vi, mods = ~ group, random = ~ group | study, struct="UN", data=dat.long)
res
```

---

### rma.peto

**Meta-Analysis via Peto's Method**

### Description

Function to fit equal-effects models to $2 \times 2$ table data via Peto's method. See below and the introduction to the *metafor-package* for more details on these models.

### Usage

```r
rma.peto(ai, bi, ci, di, n1i, n2i,
data, slab, subset,
add=1/2, to="only0", drop00=TRUE,
level=95, verbose=FALSE, digits, ...)
```

### Arguments

- **ai**: vector to specify the $2 \times 2$ table frequencies (upper left cell). See below and the documentation of the `escalc` function for more details.
- **bi**: vector to specify the $2 \times 2$ table frequencies (upper right cell). See below and the documentation of the `escalc` function for more details.
ci vector to specify the $2 \times 2$ table frequencies (lower left cell). See below and the documentation of the escalc function for more details.
di vector to specify the $2 \times 2$ table frequencies (lower right cell). See below and the documentation of the escalc function for more details.
n1i vector to specify the group sizes or row totals (first group). See below and the documentation of the escalc function for more details.
n2i vector to specify the group sizes or row totals (second group). See below and the documentation of the escalc function for more details.
data optional data frame containing the data supplied to the function.
slab optional vector with labels for the $k$ studies.
subset optional (logical or numeric) vector to specify the subset of studies that should be used for the analysis.
add non-negative number to specify the amount to add to zero cells, counts, or frequencies when calculating the observed effect sizes or outcomes of the individual studies. Can also be a vector of two numbers, where the first number is used in the calculation of the observed effect sizes outcomes and the second number is used when applying Peto’s method. See below and the documentation of the escalc function for more details.
to character string to specify when the values under add should be added (either "only0", "all", "if0all", or "none"). Can also be a character vector, where the first string again applies when calculating the observed effect sizes outcomes and the second string when applying Peto’s method. See below and the documentation of the escalc function for more details.
drop00 logical to specify whether studies with no cases (or only cases) in both groups should be dropped when calculating the observed effect sizes or outcomes (the outcomes for such studies are set to NA). Can also be a vector of two logicals, where the first applies to the calculation of the observed effect sizes outcomes and the second when applying Peto’s method. See below and the documentation of the escalc function for more details.
level numeric value between 0 and 100 to specify the confidence interval level (the default is 95).
verbose logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE).
digits optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. See also here for further details on how to control the number of digits in the output.
... additional arguments.

Details

**Specifying the Data:**
The studies are assumed to provide data in terms of $2 \times 2$ tables of the form:

<table>
<thead>
<tr>
<th></th>
<th>outcome 1</th>
<th>outcome 2</th>
<th>total</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>ai</td>
<td>bi</td>
<td>n1i</td>
</tr>
<tr>
<td>group 2</td>
<td>ci</td>
<td>di</td>
<td>n2i</td>
</tr>
</tbody>
</table>
where \( a_i, b_i, c_i, \) and \( d_i \) denote the cell frequencies and \( n_1i \) and \( n_2i \) the row totals. For example, in a set of randomized clinical trials (RCTs) or cohort studies, group 1 and group 2 may refer to the treatment (exposed) and placebo/control (not exposed) group, with outcome 1 denoting some event of interest (e.g., death) and outcome 2 its complement. In a set of case-control studies, group 1 and group 2 may refer to the group of cases and the group of controls, with outcome 1 denoting, for example, exposure to some risk factor and outcome 2 non-exposure.

**Peto’s Method:**
An approach for aggregating data of this type was suggested by Peto (see Yusuf et al., 1985). The method provides a weighted estimate of the (log) odds ratio under an equal-effects model. The method is particularly advantageous when the event of interest is rare, but it should only be used when the group sizes within the individual studies are not too dissimilar and the effect sizes are generally small (Greenland & Salvan, 1990; Sweeting et al., 2004; Bradburn et al., 2007). Note that the printed results are given both in terms of the log and the raw units (for easier interpretation).

**Observed Effect Sizes or Outcomes of the Individual Studies:**
Peto’s method itself does not require the calculation of the observed log odds ratios of the individual studies and directly makes use of the \( 2 \times 2 \) table counts. Zero cells are not a problem (except in extreme cases, such as when one of the two outcomes never occurs in any of the tables). Therefore, it is unnecessary to add some constant to the cell counts when there are zero cells. However, for plotting and various other functions, it is necessary to calculate the observed (log) odds ratios for the \( k \) studies. Here, zero cells can be problematic, so adding a constant value to the cell counts ensures that all \( k \) values can be calculated. The \( \text{add} \) and \( \text{to} \) arguments are used to specify what value should be added to the cell frequencies and under what circumstances when calculating the observed (log) odds ratios and when applying Peto’s method. Similarly, the \( \text{drop00} \) argument is used to specify how studies with no cases (or only cases) in both groups should be handled. The documentation of the \text{escalc} \) function explains how the \( \text{add} \), \( \text{to} \), and \( \text{drop00} \) arguments work. If only a single value for these arguments is specified (as per default), then these values are used when calculating the observed (log) odds ratios and no adjustment to the cell counts is made when applying Peto’s method. Alternatively, when specifying two values for these arguments, the first value applies when calculating the observed (log) odds ratios and the second value when applying Peto’s method.

Note that \( \text{drop00} \) is set to \text{TRUE} by default. Therefore, the observed (log) odds ratios for studies where \( a_i=c_i=0 \) or \( b_i=d_i=0 \) are set to \text{NA}. When applying Peto’s method, such studies are not explicitly dropped (unless the second value of \( \text{drop00} \) argument is also set to \text{TRUE}), but this is practically not necessary, as they do not actually influence the results (assuming no adjustment to the cell/event counts are made when applying Peto’s method).

**Value**
An object of class \text{c("rma.peto","rma")}. The object is a list containing the following components:

- \text{beta} \quad \text{aggregated log odds ratio.}
- \text{se} \quad \text{standard error of the aggregated value.}
- \text{zval} \quad \text{test statistics of the aggregated value.}
- \text{pval} \quad \text{corresponding p-value.}
- \text{ci.lb} \quad \text{lower bound of the confidence interval.}
**Methods**

The results of the fitted model are formatted and printed with the `print` function. If fit statistics should also be given, use `summary` (or use the `fitstats` function to extract them).

The `residuals`, `rstandard`, and `rstudent` functions extract raw and standardized residuals. Leave-one-out diagnostics can be obtained with `leave1out`.

Forest, funnel, radial, L’Abbé, and Baujat plots can be obtained with `forest`, `funnel`, `radial`, `labbe`, and `baujat`. The `qqnorm` function provides normal QQ plots of the standardized residuals. One can also just call `plot` on the fitted model object to obtain various plots at once.

A cumulative meta-analysis (i.e., adding one observation at a time) can be obtained with `cumul`.

Other extractor functions include `coef`, `vcov`, `logLik`, `deviance`, `AIC`, and `BIC`.

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**References**


**See Also**

`rma.uni`, `rma.glmm`, `rma.mh`, and `rma.mv` for other model fitting functions.

`dat.collins1985a`, `dat.collins1985b`, and `dat.yusuf1985` for further examples of the use of the `rma.peto` function.
Examples

```r
## meta-analysis of the (log) odds ratios using Peto’s method
rma.peto(ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)
```

Description

Function to fit meta-analytic equal-, fixed-, and random-effects models and (mixed-effects) meta-regression models using a linear (mixed-effects) model framework. See below and the introduction to the `metafor-package` for more details on these models.

Usage

```r
rma.uni(yi, vi, sei, weights, ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i, m1i, m2i, sd1i, sd2i, xi, mi, ri, ti, sd1i, r2i, n1i, mods, scale, measure="GEN", intercept=TRUE, data, slab, subset, add=1/2, to="only0", drop00=FALSE, vtype="LS", method="REML", weighted=TRUE, test="z", level=95, btt, att, tau2, verbose=FALSE, digits, control, ...)
```

Arguments

- `yi` vector of length `k` with the observed effect sizes or outcomes. See ‘Details’.
- `vi` vector of length `k` with the corresponding sampling variances. See ‘Details’.
- `sei` vector of length `k` with the corresponding standard errors (only relevant when not using `vi`). See ‘Details’.
- `weights` optional argument to specify a vector of length `k` with user-defined weights. See ‘Details’.
- `ai` see below and the documentation of the `escalc` function for more details.
- `bi` see below and the documentation of the `escalc` function for more details.
- `ci` see below and the documentation of the `escalc` function for more details.
- `di` see below and the documentation of the `escalc` function for more details.
- `n1i` see below and the documentation of the `escalc` function for more details.
- `n2i` see below and the documentation of the `escalc` function for more details.
- `x1i` see below and the documentation of the `escalc` function for more details.
x2i see below and the documentation of the escalc function for more details.
t1i see below and the documentation of the escalc function for more details.
t2i see below and the documentation of the escalc function for more details.
m1i see below and the documentation of the escalc function for more details.
m2i see below and the documentation of the escalc function for more details.
sd1i see below and the documentation of the escalc function for more details.
sd2i see below and the documentation of the escalc function for more details.
x see below and the documentation of the escalc function for more details.
m see below and the documentation of the escalc function for more details.
ri see below and the documentation of the escalc function for more details.
t see below and the documentation of the escalc function for more details.
sdi see below and the documentation of the escalc function for more details.
r2i see below and the documentation of the escalc function for more details.
ni see below and the documentation of the escalc function for more details.
mods optional argument to include one or more moderators in the model. A single moderator can be given as a vector of length $k$ specifying the values of the moderator. Multiple moderators are specified by giving a matrix with $k$ rows and as many columns as there are moderator variables. Alternatively, a model formula can be used to specify the model. See ‘Details’.
scale optional argument to include one or more predictors for the scale part in a location-scale model. See ‘Details’.
measure character string to specify the type of data supplied to the function. When measure="GEN" (default), the observed effect sizes or outcomes and corresponding sampling variances (or standard errors) should be supplied to the function via the yi, vi, and sei arguments (only one of the two, vi or sei, needs to be specified). Alternatively, one can set measure to one of the effect sizes or outcome measures described under the documentation for the escalc function in which case one must specify the required data via the appropriate arguments.
intercept logical to specify whether an intercept should be added to the model (the default is TRUE). Ignored when mods is a formula.
data optional data frame containing the data supplied to the function.
slab optional vector with labels for the $k$ studies.
subset optional (logical or numeric) vector to specify the subset of studies that should be used for the analysis.
add see the documentation of the escalc function.
to see the documentation of the escalc function.
drop00 see the documentation of the escalc function.
vtype see the documentation of the escalc function.
method character string to specify whether an equal- or a random-effects model should be fitted. An equal-effects model is fitted when using method="EE". A random-effects model is fitted by setting method equal to one of the following: "DL", "HE", "HS", "HSk", "SJ", "ML", "REML", "EB", "PM", "GENQ", "PMM", or "GENQM". Default is "REML". See ‘Details’.
weighted  logical to specify whether weighted (default) or unweighted estimation should be used to fit the model (the default is TRUE).

test  character string to specify how test statistics and confidence intervals for the fixed effects should be computed. By default (test="z"), Wald-type tests and CIs are obtained, which are based on a standard normal distribution. When test="t", a t-distribution is used instead. When test="knha", the method by Knapp and Hartung (2003) is used. See ‘Details’ and also here for some recommended practices.

level  numeric value between 0 and 100 to specify the confidence interval level (the default is 95).

btt  optional vector of indices to specify which coefficients to include in the omnibus test of moderators. Can also be a string to grep for. See ‘Details’.

att  optional vector of indices to specify which scale coefficients to include in the omnibus test. Only relevant for location-scale models. See ‘Details’.

tau2  optional numeric value to specify the amount of (residual) heterogeneity in a random- or mixed-effects model (instead of estimating it). Useful for sensitivity analyses (e.g., for plotting results as a function of $\tau^2$). When unspecified, the value of $\tau^2$ is estimated from the data.

verbose  logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE). Can also be an integer. Values > 1 generate more verbose output. See ‘Note’.

digits  optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is 4. See also here for further details on how to control the number of digits in the output.

control  optional list of control values for the iterative estimation algorithms. If unspecified, default values are defined inside the function. See ‘Note’.

...  additional arguments.

Details

Specifying the Data:

The function can be used in combination with any of the usual effect sizes or outcome measures used in meta-analyses (e.g., log risk ratios, log odds ratios, risk differences, mean differences, standardized mean differences, log transformed ratios of means, raw correlation coefficients, correlation coefficients transformed with Fisher’s r-to-z transformation), or, more generally, any set of estimates (with corresponding sampling variances) one would like to analyze. Simply specify the observed effect sizes or outcomes via the yi argument and the corresponding sampling variances via the vi argument. Instead of specifying vi, one can specify the standard errors (the square root of the sampling variances) via the sei argument. The escalc function can be used to compute a wide variety of effect sizes or outcome measures (and the corresponding sampling variances) based on summary statistics.

Alternatively, the function can automatically calculate the values of a chosen effect size or outcome measure (and the corresponding sampling variances) when supplied with the necessary data. The escalc function describes which effect sizes or outcome measures are currently implemented and what data/arguments should then be specified/used. The measure argument should then be set to the desired effect size or outcome measure.
Specifying the Model:
The function can be used to fit equal-, fixed-, and random-effects models, as well as (mixed-effects) meta-regression models including one or multiple moderators (the difference between the various models is described in detail on the introductory metafor-package help page).

Assuming the observed effect sizes or outcomes and corresponding sampling variances are supplied via the yi and vi arguments, an equal-effects model can be fitted with rma(yi, vi, method="EE"). Setting method="FE" fits a fixed-effects model (see here for a discussion of this model). Weighted estimation (with inverse-variance weights) is used by default. User-defined weights can be supplied via the weights argument. Unweighted estimation can be used by setting weighted=FALSE (which is the same as setting the weights equal to a constant).

A random-effects model can be fitted with the same code but setting the method argument to one of the various estimators for the amount of heterogeneity:

- method="DL" = DerSimonian-Laird estimator (DerSimonian & Laird, 1986; Raudenbush, 2009),
- method="HE" = Hedges estimator (Hedges, 1983, 1992),
- method="HS" = Hunter-Schmidt estimator (Hunter & Schmidt, 1990; Viechtbauer et al., 2015),
- method="HSk" = Hunter-Schmidt estimator with a small sample-size correction (Brannick et al., 2019),
- method="SJ" = Sidik-Jonkman estimator (Sidik & Jonkman, 2005b, 2007),
- method="ML" = maximum likelihood estimator (Hardy & Thompson, 1996; Raudenbush, 2009),
- method="REML" = restricted maximum likelihood estimator (Viechtbauer, 2005; Raudenbush, 2009)
- method="EB" = empirical Bayes estimator (Morris, 1983; Berkey et al. 1995),
- method="PM" = Paule-Mandel estimator (Paule & Mandel, 1982; Viechtbauer et al., 2015),
- method="GENQ" = generalized Q-statistic estimator (DerSimonian & Kacker, 2007; Jackson et al., 2014),
- method="PMm" = median-unbiased Paule-Mandel estimator (Viechtbauer, 2021),
- method="GENQM" = median-unbiased generalized Q-statistic estimator (Viechtbauer, 2021).

For a description of the various estimators, see Brannick et al. (2019), DerSimonian and Kacker (2007), Raudenbush (2009), Veroniki et al. (2016), Viechtbauer (2005), and Viechtbauer et al. (2015). Note that the Hedges estimator is also called the ‘variance component estimator’ or ‘Cochran estimator’, the Sidik-Jonkman estimator is also called the ‘model error variance estimator’, the empirical Bayes estimator is actually identical to the Paule-Mandel estimator (Viechtbauer et al., 2015), and the generalized Q-statistic estimator is a general method-of-moments estimator (DerSimonian & Kacker, 2007) requiring the specification of weights (the HE and DL estimators are just special cases with equal and inverse sampling variance weights, respectively). Finally, the two median-unbiased estimators are versions of the Paule-Mandel and generalized Q-statistic estimators that equate the respective estimating equations not to their expected values, but to the medians of their theoretical distributions (Viechtbauer, 2021).

One or more moderators can be included in a model via the mods argument. A single moderator can be given as a (row or column) vector of length k specifying the values of the moderator. Multiple moderators are specified by giving an appropriate model matrix (i.e., X) with k rows and as many columns as there are moderator variables (e.g., mods = cbind(mod1, mod2, mod3), where
mod1, mod2, and mod3 correspond to the names of the variables for three moderator variables. The intercept is added to the model matrix by default unless intercept=FALSE.

Alternatively, one can use standard formula syntax to specify the model. In this case, the mods argument should be set equal to a one-sided formula of the form mods = ~ model (e.g., mods = ~ mod1 + mod2 + mod3). Interactions, polynomial terms, and factors can be easily added to the model in this manner. When specifying a model formula via the mods argument, the intercept argument is ignored. Instead, the inclusion/exclusion of the intercept is controlled by the specified formula (e.g., mods = ~ mod1 + mod2 + mod3 - 1 would lead to the removal of the intercept).

When the observed effect sizes or outcomes and corresponding sampling variances are supplied via the yi and vi (or sei) arguments, one can also specify moderators via the yi argument (e.g., rma(yi ~ mod1 + mod2 + mod3, vi)). In that case, the mods argument is ignored and the inclusion/exclusion of the intercept again is controlled by the specified formula.

Omnibus Test of Moderators:
For models including moderators, an omnibus test of all model coefficients is conducted that excludes the intercept (the first coefficient) if it is included in the model. If no intercept is included in the model, then the omnibus test includes all coefficients in the model including the first. Alternatively, one can manually specify the indices of the coefficients to test via the btt (‘betas to test’) argument (i.e., to test $H_0: \beta_{j \in \text{btt}} = 0$, where $\beta_{j \in \text{btt}}$ is the set of coefficients to be tested). For example, with btt=c(3,4), only the third and fourth coefficients from the model are included in the test (if an intercept is included in the model, then it corresponds to the first coefficient in the model). Instead of specifying the coefficient numbers, one can specify a string for btt. In that case, grep will be used to search for all coefficient names that match the string. The omnibus test is called the $Q_M$-test and follows asymptotically a chi-square distribution with $m$ degrees of freedom (with $m$ denoting the number of coefficients tested) under the null hypothesis (that the true value of all coefficients tested is equal to 0).

Categorical Moderators:
Categorical moderator variables can be included in the model via the mods argument in the same way that appropriately (dummy) coded categorical variables can be included in linear models. One can either do the dummy coding manually or use a model formula together with the factor function to automate the coding (note that string/character variables in a model formula are automatically converted to factors). An example to illustrate these different approaches is provided below.

Tests and Confidence Intervals:
By default, tests of individual coefficients in the model (and the corresponding confidence intervals) are based on a standard normal distribution, while the omnibus test is based on a chi-square distribution (see above). As an alternative, one can set test="t", in which case tests of individual coefficients and confidence intervals are based on a t-distribution with $k - p$ degrees of freedom, while the omnibus test then uses an F-distribution with $m$ and $k - p$ degrees of freedom (with $k$ denoting the total number of estimates included in the analysis and $p$ the total number of model coefficients including the intercept if it is present). Furthermore, when test="knha", the method by Hartung (1999), Sidik and Jonkman (2002), and Knapp and Hartung (2003) (the Knapp-Hartung method; also referred to as the Hartung-Knapp-Sidik-Jonkman method) is used, which applies an adjustment to the standard errors of the estimated coefficients (to account for the uncertainty in the estimate of the amount of (residual) heterogeneity) and uses t- and F-distributions as described above (see also here). Finally, one can set test="adhoc", in which case the Knapp-Hartung
method is used, but with the restriction that the adjustment to the standard errors can never result in adjusted standard errors that are smaller than the unadjusted ones (see Jackson et al., 2017, section 4.3).

**Test for (Residual) Heterogeneity:**
A test for (residual) heterogeneity is automatically carried out by the function. Without moderators in the model, this is simply Cochran’s $Q$-test (Cochran, 1954), which tests whether the variability in the observed effect sizes or outcomes is larger than would be expected based on sampling variability alone. A significant test suggests that the true effects/outcomes are heterogeneous. When moderators are included in the model, this is the $Q_E$-test for residual heterogeneity, which tests whether the variability in the observed effect sizes or outcomes not accounted for by the moderators included in the model is larger than would be expected based on sampling variability alone.

**Location-Scale Models:**
The function can also be used to fit so-called ‘location-scale models’ (Viechtbauer & López-López, in press). In such models, one can specify not only predictors for the size of the average true outcome (i.e., for their ‘location’), but also predictors for the amount of heterogeneity in the outcomes (i.e., for their ‘scale’). The model is given by

\[ y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \ldots + \beta_{p'} x_{ip'} + u_i + \varepsilon_i, \]

\[ u_i \sim N(0, \tau_i^2), \varepsilon_i \sim N(0, v_i), \]

\[ \ln(\tau_i^2) = \alpha_0 + \alpha_1 z_{i1} + \alpha_2 z_{i2} + \ldots + \alpha_{q'} z_{iq'}, \]

where $x_{i1}, \ldots, x_{ip'}$ are the values of the $p'$ predictor variables that may be related to the size of the average true outcome (letting $p = p' + 1$ denote the total number of location coefficients in the model including the model intercept $\beta_0$) and $z_{i1}, \ldots, z_{iq'}$ are the values of the $q'$ scale variables that may be related to the amount of heterogeneity in the outcomes (letting $q = q' + 1$ denote the total number of scale coefficients in the model including the model intercept $\alpha_0$). Location variables can be specified via the `.mods` argument as described above (e.g., `mods = ~ mod1 + mod2 + mod3`). Scale variables can be specified via the `scale` argument (e.g., `scale = ~ var1 + var2 + var3`). A log link is used for specifying the relationship between the scale variables and the amount of heterogeneity so that $\tau_i^2$ is guaranteed to be non-negative (one can also set the (undocumented) argument `link="identity"` to use an identity link, but this is more likely to lead to estimation problems). Estimates of the location and scale coefficients can be obtained either with maximum likelihood (`method="ML"`) or restricted maximum likelihood (`method="REML"`) estimation. An omnibus test of the scale coefficients is conducted as described above (where the `att` argument can be used to specify which scale coefficients to include in the test).

**Value**
An object of class `c("rma.uni","rma")`. The object is a list containing the following components:

- `beta` estimated coefficients of the model.
- `se` standard errors of the coefficients.
- `zval` test statistics of the coefficients.
- `pval` corresponding p-values.
- `ci.lb` lower bound of the confidence intervals for the coefficients.
ci.ub upper bound of the confidence intervals for the coefficients.
vb variance-covariance matrix of the estimated coefficients.
tau2 estimated amount of (residual) heterogeneity. Always 0 when method="EE".
se.tau2 standard error of the estimated amount of (residual) heterogeneity.
k number of studies included in the analysis.
p number of coefficients in the model (including the intercept).
m number of coefficients included in the omnibus test of moderators.
QE test statistic of the test for (residual) heterogeneity.
QEp corresponding p-value.
QM test statistic of the omnibus test of moderators.
QMp corresponding p-value.
I2 value of $I^2$. See print for more details.
H2 value of $H^2$. See print for more details.
R2 value of $R^2$. See print for more details.
int.only logical that indicates whether the model is an intercept-only model.
i1, vi, X the vector of outcomes, the corresponding sampling variances, and the model matrix.
fit.stats a list with the log-likelihood, deviance, AIC, BIC, and AICc values under
unrestricted and restricted likelihood.
... some additional elements/values.

For location-scale models, the object is of class c("rma.ls","rma.uni","rma") and includes the
following components in addition to the ones listed above:

alpha estimated scale coefficients of the model.
se.alpha standard errors of the coefficients.
zval.alpha test statistics of the coefficients.
pval.alpha corresponding p-values.
ci.lb.alpha lower bound of the confidence intervals for the coefficients.
ci.ub.alpha upper bound of the confidence intervals for the coefficients.
va variance-covariance matrix of the estimated coefficients.
tau2 as above, but now a vector of values.
q number of scale coefficients in the model (including the intercept).
QS test statistic of the omnibus test of the scale coefficients.
QS a corresponding p-value.
... some additional elements/values.
Methods

The results of the fitted model are formatted and printed with the \texttt{print} function. If fit statistics should also be given, use \texttt{summary} (or use the \texttt{fitstats} function to extract them). Full versus reduced model comparisons in terms of fit statistics and likelihood ratio tests can be obtained with \texttt{anova}. Wald-type tests for sets of model coefficients or linear combinations thereof can be obtained with the same function. Permutation tests for the model coefficient(s) can be obtained with \texttt{permutest}. Tests and confidence intervals based on (cluster) robust methods can be obtained with \texttt{robust}.

Predicted/fitted values can be obtained with \texttt{predict} and \texttt{fitted}. For best linear unbiased predictions, see \texttt{blup} and \texttt{ranef}.

The \texttt{residuals}, \texttt{rstandard}, and \texttt{rstudent} functions extract raw and standardized residuals. Additional model diagnostics (e.g., to determine influential studies) can be obtained with the \texttt{influence} function. For models without moderators, leave-one-out diagnostics can also be obtained with \texttt{leave1out}. For models with moderators, variance inflation factors can be obtained with \texttt{vif}.

A confidence interval for the amount of (residual) heterogeneity in the random/mixed-effects model can be obtained with \texttt{confint}. For location-scale models, \texttt{confint} can provide confidence intervals for the scale coefficients.

Forest, funnel, radial, L’Abbé, and Baujat plots can be obtained with \texttt{forest}, \texttt{funnel}, \texttt{radial}, \texttt{labbe}, and \texttt{baujat} (radial and L’Abbé plots only for models without moderators). The \texttt{qqnorm} function provides normal QQ plots of the standardized residuals. One can also just call \texttt{plot} on the fitted model object to obtain various plots at once. For random/mixed-effects models, the \texttt{profile} function can be used to obtain a plot of the (restricted) log-likelihood as a function of $\tau^2$. For location-scale models, \texttt{profile} draws analogous plots based on the scale coefficients. For models with moderators, \texttt{regplot} draws scatter plots / bubble plots, showing the (marginal) relationship between the observed outcomes and a selected moderator from the model.

Tests for funnel plot asymmetry (which may be indicative of publication bias) can be obtained with \texttt{ranktest} and \texttt{regtest}. For models without moderators, the \texttt{trimfill} method can be used to carry out a trim and fill analysis and \texttt{hc} provides a random-effects model analysis that is more robust to publication bias (based on the method by Henmi & Copas, 2010). The test of ‘excess significance’ can be carried out with the \texttt{tes} function. Selection models can be fitted with the \texttt{selmodel} function.

For models without moderators, a cumulative meta-analysis (i.e., adding one observation at a time) can be obtained with \texttt{cumul}.

Other extractor functions include \texttt{coef}, \texttt{vcov}, \texttt{logLik}, \texttt{deviance}, \texttt{AIC}, \texttt{BIC}, \texttt{hatvalues}, and \texttt{weights}.

Note

While the HS, HSk, HE, DL, SJ, and GENQ estimators of $\tau^2$ are based on closed-form solutions, the ML, REML, and EB estimators must be obtained iteratively. For this, the function makes use of the Fisher scoring algorithm, which is robust to poor starting values and usually converges quickly (Harville, 1977; Jennrich & Sampson, 1976). By default, the starting value is set equal to the value of the Hedges (HE) estimator and the algorithm terminates when the change in the estimated value of $\tau^2$ is smaller than $10^{-5}$ from one iteration to the next. The maximum number of iterations is 100 by default (which should be sufficient in most cases). Information on the progress of the algorithm can be obtained by setting \texttt{verbose=TRUE}. One can also set \texttt{verbose} to an integer (\texttt{verbose=2} yields even more information and \texttt{verbose=3} also sets \texttt{option(warn=1)} temporarily).
A different starting value, threshold, and maximum number of iterations can be specified via the control argument by setting control=list(tau2.init=value, threshold=value, maxiter=value).

The step length of the Fisher scoring algorithm can also be adjusted by a desired factor with control=list(stepadj=value) (values below 1 will reduce the step length). If using verbose=TRUE shows the estimate jumping around erratically (or cycling through a few values), decreasing the step length (and increasing the maximum number of iterations) can often help with convergence (e.g., control=list(stepadj=0.5, maxiter=1000)).

The step length of the Fisher scoring algorithm can also be adjusted by a desired factor with control=list(stepadj=value) (values below 1 will reduce the step length). If using verbose=TRUE shows the estimate jumping around erratically (or cycling through a few values), decreasing the step length (and increasing the maximum number of iterations) can often help with convergence (e.g., control=list(stepadj=0.5, maxiter=1000)).

The PM, PMM, and GENQM estimators also involve iterative algorithms, which make use of the uniroot function. By default, the desired accuracy (tol) is set equal to .Machine$double.eps^0.25 and the maximum number of iterations (maxiter) to 100 (as above). The upper bound of the interval searched (tau2.max) is set to the larger of 100 and 10*mad(yi)^2 (i.e., 10 times the squared median absolute deviation of the observed effect sizes or outcomes computed with the mad function). These values can be adjusted with control=list(tol=value, maxiter=value, tau2.max=value).

All of the heterogeneity estimators except SJ can in principle yield negative estimates for the amount of (residual) heterogeneity. However, negative estimates of $\tau^2$ are outside of the parameter space. For the HS, HSk, HE, DL, and GENQ estimators, negative estimates are therefore truncated to zero. For the ML, REML, and EB estimators, the Fisher scoring algorithm makes use of step halving (Jennrich & Sampson, 1976) to guarantee a non-negative estimate. Finally, for the PM, PMM, and GENQM estimators, the lower bound of the interval searched is set to zero by default. For those brave enough to step into risky territory, there is the option to set the lower bound for all these estimators to some other value besides zero (even a negative one) with control=list(tau2.min=value), but the lowest value permitted is -min(vi) (to ensure that the marginal variances are always non-negative).

The Hunter-Schmidt estimator for the amount of heterogeneity is defined in Hunter and Schmidt (1990) only in the context of the random-effects model when analyzing correlation coefficients. A general version of this estimator for random- and mixed-effects models not specific to any particular outcome measure is described in Viechtbauer (2005) and Viechtbauer et al. (2015) and is implemented here.

The Sidik-Jonkman estimator starts with a crude estimate of $\tau^2$, which is then updated as described in Sidik and Jonkman (2005b, 2007). If, instead of the crude estimate, one wants to use a better a priori estimate, one can do so by passing this value via control=list(tau2.init=value).

One can also specify a vector of estimators via the method argument (e.g., rma(yi, vi, method=c("REML","DL"))). The various estimators are then applied in turn until one converges. This is mostly useful for simulation studies where an estimator (like the REML estimator) is not guaranteed to converge and one can then substitute one (like the DL estimator) that does not involve iterative methods and is guaranteed to provide an estimate.

Outcomes with non-positive sampling variances are problematic. If a sampling variance is equal to zero, then its weight will be $1/0$ for equal-effects models when using weighted estimation. Switching to unweighted estimation is a possible solution then. For random/mixed-effects model, some estimators of $\tau^2$ are undefined when there is at least one sampling variance equal to zero. Other estimators may work, but it may still be necessary to switch to unweighted model fitting, especially when the estimate of $\tau^2$ converges to zero.

When including moderators in the model, it is possible that the model matrix is not of full rank (i.e., there is a linear relationship between the moderator variables included in the model). The function automatically tries to reduce the model matrix to full rank by removing redundant predictors, but if this fails the model cannot be fitted and an error will be issued. Deleting (redundant) moderator variables from the model as needed should solve this problem.
Some general words of caution about the assumptions underlying the models:

- The sampling variances (i.e., the $v_i$ values) are treated as if they are known constants, even though in practice they are usually estimates themselves. This implies that the distributions of the test statistics and corresponding confidence intervals are only exact and have nominal coverage when the within-study sample sizes are large (i.e., when the error in the sampling variance estimates is small). Certain outcome measures (e.g., the arcsine square root transformed risk difference and Fisher's $r$-to-$z$ transformed correlation coefficient) are based on variance stabilizing transformations that also help to make the assumption of known sampling variances much more reasonable.

- When fitting a mixed/random-effects model, $\tau^2$ is estimated and then treated as a known constant thereafter. This ignores the uncertainty in the estimate of $\tau^2$. As a consequence, the standard errors of the parameter estimates tend to be too small, yielding test statistics that are too large and confidence intervals that are not wide enough. The Knapp and Hartung (2003) adjustment (i.e., using test="knha") can be used to counter this problem, yielding test statistics and confidence intervals whose properties are closer to nominal.

- Most effect sizes or outcome measures do not have exactly normal sampling distributions as assumed under the various models. However, the normal approximation usually becomes more accurate for most effect sizes or outcome measures as the within-study sample sizes increase. Therefore, sufficiently large within-study sample sizes are (usually) needed to be certain that the tests and confidence intervals have nominal levels/coverage. Again, certain outcome measures (e.g., Fisher's $r$-to-$z$ transformed correlation coefficient) may be preferable from this perspective as well.

For location-scale models, model fitting is done via numerical optimization over the model parameters. By default, nlminb is used for the optimization. One can also choose a different optimizer from optim via the control argument (e.g., control=list(optimizer="BFGS") or control=list(optimizer="Nelder-Mead") besides nlminb and one of the methods from optim, one can also choose one of the optimizers from the minqa package (i.e., uobyqa, newuoa, or bobyqa), one of the (derivative-free) algorithms from the nloptr package, the Newton-type algorithm implemented in nlm, the various algorithms implemented in the dfoptim package (hjk for the Hooke-Jeeves, nmk for the Nelder-Mead, and mads for the Mesh Adaptive Direct Searches algorithm), the quasi-Newton type optimizers ucminf and lbfgsbf3c and the subspace-searching simplex algorithm subplex from the packages of the same name, the Barzilai-Borwein gradient decent method implemented in BBoptim, or the parallelized version of the L-BFGS-B algorithm implemented in optimParallel from the package of the same name. When using an identity link with link="identity", constrained optimization (to ensure non-negative $\tau^2_i$ values) as implemented in constrOptim is used by default. Alternative optimizers in this case are the solnp solver from the Rsolnp package, nloptr, or the augmented Lagrangian adaptive barrier minimization algorithm constrOptim.nl from the alabama package.

The optimizer name must be given as a character string (i.e., in quotes). Additional control parameters can be specified via the control argument (e.g., control=list(iter.max=1000, rel.tol=1e-8)). For nloptr, the default is to use the BOBYQA implementation from that package with a relative convergence criterion of 1e-8 on the function value (i.e., log-likelihood), but this can be changed via the algorithm and ftol_rel arguments (e.g., control=list(optimizer="nloptr", algorithm="NLOPT_LN_SBPLX", ftol_rel=1e-6)) (note: when using optimizer="nloptr" in combination with an identity link, the "NLOPT_LN_COByla" algorithm is automatically used, since this one allows for inequality constraints). For optimParallel, the control argument ncpus can be used to specify the number of cores to use for the parallelization (e.g., control=list(optimizer="optimParallel",nloptr, Ramlau tolerate unusually large variations in the data (e.g., outliers) and may not be appropriate for the data at hand.

For certain outcome measures, it is possible to use a different link function to improve the fit of the model. One common approach is to use a log-link function, which is often effective for count data or proportions. For example, the function$log(x)$ can be used as the link function, where $x$ is the outcome measure. This can be achieved by specifying the link argument in the model fitting function, e.g., link="log". Other potential link functions include the probit link, which is often used for binary outcome measures. The choice of link function should be guided by the characteristics of the data and the specific research question at hand.

Another important consideration is the assumption of normality for the sampling distribution of the test statistics. When the sampling distribution is not normal, it may be necessary to use non-parametric methods or transform the data to improve normality. For example, the data may be transformed using a Box-Cox transformation or a log-transformation. The choice of transformation should be guided by the characteristics of the data and the specific research question at hand.

Finally, it is important to consider the robustness of the results to violations of the assumptions. For example, the results may be sensitive to outliers or influential observations. Robust methods such as the Huber or the Hampel robust estimators can be used to handle these issues. The choice of robust method should be guided by the characteristics of the data and the specific research question at hand.
ncpus=2)). With parallel::detectCores(), one can check on the number of available cores on the local machine.

Under certain circumstances (e.g., when the amount of heterogeneity is very small for certain combinations of values for the scale variables and scale coefficients), the values of the scale coefficients may try to drift towards minus or plus infinity, which can lead to problems with the optimization. One can impose constraints on the scale coefficients via control=list(alpha.min=minval, alpha.max=maxval) where minval and maxval are either scalars or vectors of the appropriate length.

Finally, for location-scale models, the standard errors of the scale coefficients are obtained by inverting the Hessian, which is numerically approximated using the hessian function from the numDeriv package. This may fail (especially when using an identity link), leading to NA values for the standard errors and hence test statistics, p-values, and confidence interval bounds. One can set control argument hessianCtrl to a list of named arguments to be passed on to the method.args argument of the hessian function (the default is control=list(hessianCtrl=list(r=8))). Even if the Hessian can be approximated and inverted, the standard errors may be unreasonably large when the likelihood surface is very flat around the estimated scale coefficients. This is more likely to happen when k is small and when the amount of heterogeneity is very small under some conditions as defined by the scale coefficients/variables. Setting constraints on the scale coefficients as described above can also help to mitigate this issue.

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References


See Also

*rma.mh, rma.peto, rma.glmm*, and *rma.mv* for other model fitting functions.

Examples

### calculate log risk ratios and corresponding sampling variances

dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit a random-effects model using the log risk ratios and sampling variances as input
### note: method="REML" is the default, so one could leave this out
rma(yi, vi, data=dat, method="REML")

### fit a random-effects model using the log risk ratios and standard errors as input
### note: the second argument of rma() is for the *sampling variances*, so we use the
### named argument 'sei' to supply the standard errors to the function

dat$sei <- sqrt(dat$vi)
rma(yi, sei=sei, data=dat)

### fit a random-effects model supplying the 2x2 table cell frequencies to the function
rma(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat)

### fit a mixed-effects model with two moderators (absolute latitude and publication year)
rma(yi, vi, mods=cbind(ablat, year), data=dat)

### using a model formula to specify the same model
rma(yi, vi, mods = ~ ablat + year, data=dat)

### using a model formula as part of the yi argument
rma(yi ~ ablat + year, vi, data=dat)

### manual dummy coding of the allocation factor
alloc.random <- ifelse(dat$alloc == "random", 1, 0)
alloc.alternate <- ifelse(dat$alloc == "alternate", 1, 0)
alloc.systematic <- ifelse(dat$alloc == "systematic", 1, 0)

### test the allocation factor (in the presence of the other moderators)
### note: 'alternate' is the reference level of the allocation factor,
### since this is the dummy/level we leave out of the model
### note: the intercept is the first coefficient, so with btt=2:3 we test
### coefficients 2 and 3, corresponding to the coefficients for the
### allocation factor
rma(yi, vi, mods = ~ alloc.random + alloc.systematic + year + ablat, data=dat, btt=2:3)

### using a model formula to specify the same model
rma(yi, vi, mods = ~ factor(alloc) + year + ablat, data=dat, btt=2:3)

### factor() is not needed as character variables are automatically converted to factors
rma(yi, vi, mods = ~ alloc + year + ablat, data=dat, btt=2:3)

### test all pairwise differences with Holm's method (using the 'multcomp' package if installed)
res <- rma(yi, vi, mods = ~ factor(alloc) - 1, data=dat)
if (require(multcomp))
  summary(glht(res, linfct=contrMat(c("alternate"=1,"random"=1,"systematic"=1), type="Tukey")), test=adjusted("holm"))

### subgrouping versus using a single model with a factor (subgrouping provides
### an estimate of tau^2 within each subgroup, but the number of studies in each
### subgroup is quite small; the model with the allocation factor provides a
### single estimate of tau^2 based on a larger number of studies, but assumes
### that tau^2 is the same within each subgroup)
res.a <- rma(yi, vi, data=dat, subset=(alloc=="alternate"))
res.r <- rma(yi, vi, data=dat, subset=(alloc=="random"))
res.s <- rma(yi, vi, data=dat, subset=(alloc=="systematic"))
res.a
res.r
res.s

### demonstrating that Q_E + Q_M = Q_Total for fixed-effects models
### note: this does not work for random/mixed-effects models, since Q_E and
### Q_Total are calculated under the assumption that tau^2 = 0, while the
### calculation of Q_M incorporates the estimate of tau^2
res <- rma(yi, vi, data=dat, method="FE")
res ### this gives Q_Total
res <- rma(yi, vi, mods = ~ ablat + year, data=dat, method="FE")
res ### this gives Q_E and Q_M
res$QE + res$QM

### decomposition of Q_E into subgroup Q-values
res <- rma(yi, vi, mods = ~ factor(alloc), data=dat)
res
res.a <- rma(yi, vi, data=dat, subset=(alloc=="alternate"))
res.r <- rma(yi, vi, data=dat, subset=(alloc=="random"))
res.s <- rma(yi, vi, data=dat, subset=(alloc=="systematic"))

res.a$QE ### Q-value within subgroup "alternate"
res.r$QE ### Q-value within subgroup "random"
res.s$QE ### Q-value within subgroup "systematic"

res$QE
res.a$QE + res.r$QE + res.s$QE

### an example of a location-scale model
### Code

```r
dat <- dat.bangertdrowns2004

### fit a standard random-effects model
res <- rma(yi, vi, data=dat)
res

### fit the same model as a location-scale model
res <- rma(yi, vi, scale = ~ 1, data=dat)
res

### check that we obtain the same estimate for tau^2
predict(res, newscale=1, transf=exp)

### add the total sample size (per 100) as a location and scale predictor
dat$ni100 <- dat$ni/100
res <- rma(yi, vi, mods = ~ ni100, scale = ~ ni100, data=dat)
res

### variables in the location and scale parts can differ
res <- rma(yi, vi, mods = ~ ni100 + meta, scale = ~ ni100 + imag, data=dat)
res
```

---

**robust**

*Cluster-Robust Tests and Confidence Intervals for 'rma' Objects*

---

**Description**

The function provides cluster-robust tests and confidence intervals (also known as robust variance estimation) of the model coefficients for objects of class "rma".

**Usage**

```r
robust(x, cluster, ...) 
```

### S3 method for class 'rma.uni'

```r
robust(x, cluster, adjust=TRUE, clubSandwich=FALSE, digits, ...)
```

### S3 method for class 'rma.mv'

```r
robust(x, cluster, adjust=TRUE, clubSandwich=FALSE, digits, ...)
```

**Arguments**

- `x` : an object of class "rma.uni" or "rma.mv".
- `cluster` : vector to specify the clustering variable to use for constructing the sandwich estimator of the variance-covariance matrix.
- `adjust` : logical to specify whether a small-sample correction should be applied to the variance-covariance matrix.
- `clubSandwich` : logical to specify whether the clubSandwich package should be used to obtain the cluster-robust tests and confidence intervals.
digits optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

Details

The function constructs a cluster-robust estimate of the variance-covariance matrix of the model coefficients based on a sandwich-type estimator and then computes tests and confidence intervals of the model coefficients. This function will often be part of a general workflow for meta-analyses involving complex dependency structures as described here.

By default, tests of individual coefficients and confidence intervals are based on a t-distribution with \( n - p \) degrees of freedom, while the omnibus test uses an F-distribution with \( m \) and \( n - p \) degrees of freedom, where \( n \) is the number of clusters, \( p \) denotes the total number of model coefficients (including the intercept if it is present), and \( m \) denotes the number of coefficients tested by the omnibus test. This is sometimes called the ‘residual’ method for approximating the (denominator) degrees of freedom.

When \( \text{adjust}=\text{TRUE} \) (the default), the cluster-robust estimate of the variance-covariance matrix is multiplied by the factor \( n/(n-p) \), which serves as a small-sample adjustment that tends to improve the performance of the method when the number of clusters is small. This is sometimes called the ‘CR1’ adjustment/estimator (in contrast to ‘CR0’ when \( \text{adjust}=\text{FALSE} \)).

For an even better small-sample adjustment, one can set \( \text{clubSandwich}=\text{TRUE} \) in which case the \text{clubSandwich} package is used to obtain the cluster-robust tests and confidence intervals. The variance-covariance matrix of the model coefficients is then estimated using the ‘bias-reduced linearization’ adjustment proposed by Bell and McCaffrey (2002) and further developed in Tipton (2015) and Pustejovsky and Tipton (2018). This is sometimes called the ‘CR2’ adjustment/estimator. The degrees of freedom of the t-tests are then estimated using a Satterthwaite approximation. F-tests are then based on an approximate Hotelling’s T-squared reference distribution, with denominator degrees of freedom estimated using a method by Zhang (2012, 2013), as further described in Tipton and Pustejovsky (2015).

Value

An object of class "\text{robust.rma}". The object is a list containing the following components:

- \text{beta} estimated coefficients of the model.
- \text{se} robust standard errors of the coefficients.
- \text{zval} test statistics of the coefficients.
- \text{pval} corresponding p-values.
- \text{ci.lb} lower bound of the confidence intervals for the coefficients.
- \text{ci.ub} upper bound of the confidence intervals for the coefficients.
- \text{vb} robust variance-covariance matrix of the estimated coefficients.
- \text{QM} test statistic of the omnibus test of moderators.
- \text{QMp} corresponding p-value.

... some additional elements/values.
The results are formatted and printed with the `print.rma.uni` and `print.rma.mv` functions (depending on the type of model).

Predicted/fitted values based on "robust.rma" objects can be obtained with the `predict` function. Tests for sets of model coefficients or linear combinations thereof can be obtained with the `anova` function.

**Note**

The variable specified via `cluster` is assumed to be of the same length as the data originally passed to the `rma.uni` or `rma.mv` functions (and if the `data` argument was used in the original model fit, then the variable will be searched for within this data frame first). Any subsetting and removal of studies with missing values that was applied during the model fitting is also automatically applied to the variable specified via the `cluster` argument.

The idea of the robust (sandwich-type) estimator for models with unspecified heteroscedasticity can be traced back to Eicker (1967), Huber (1967), and White (1980, 1984). Hence, the method in general is often referred to as the Eicker-Huber-White method. Some small-sample improvements to the method are described by MacKinnon and White (1985). The extension to the cluster-robust estimator can be found in Froot (1989) and Williams (2000), which is also related to the GEE approach by Liang and Zeger (1986). Cameron and Miller (2015) provide an extensive overview of cluster-robust methods. Sidik and Jonkman (2005, 2006) introduced robust methods in the meta-analytic context for standard random/mixed-effects models. The use of cluster-robust methods for multivariate/multilevel meta-analytic models was introduced by Hedges, Tipton, and Johnson (2010).

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**References**


See Also

`rma.uni` and `rma.mv` for functions to fit models for which cluster-robust tests and confidence intervals can be obtained.

Examples

```
### copy data from Bangert-Drowns et al. (2004) into 'dat'
dat <- dat.bangertdrowns2004

### fit random-effects model
res <- rma(yi, vi, data=dat)
res

### use cluster-robust inference methods
robust(res, cluster=id)

### use methods from the clubSandwich package
robust(res, cluster=id, clubSandwich=TRUE)

### fit meta-regression model
```
res <- rma(yi, vi, mods = ~ length, data=dat)
res

### use cluster-robust inference methods
robust(res, cluster=id)

### use methods from the clubSandwich package
robust(res, cluster=id, clubSandwich=TRUE)

############################################################################

### copy data from Konstantopoulos (2011) into 'dat'
dat <- dat.konstantopoulos2011

### fit multilevel random-effects model
res <- rma.mv(yi, vi, random = ~ 1 | district/school, data=dat)
res

### use cluster-robust inference methods
robust(res, cluster=district)

### use methods from the clubSandwich package
robust(res, cluster=district, clubSandwich=TRUE)

############################################################################

### copy data from Berkey et al. (1998) into 'dat'
dat <- dat.berkey1998

### variables v1i and v2i correspond to the 2x2 var-cov matrices of the studies;
### so use these variables to construct the V matrix (note: since v1i and v2i are
### var-cov matrices and not correlation matrices, set vi=1 for all rows)
V <- vcalc(vi=1, cluster=author, rvars=c(v1i, v2i), data=dat)

### fit multivariate model
res <- rma.mv(yi, V, mods = ~ outcome - 1, random = ~ outcome | trial, struct="UN", data=dat)
res

### use cluster-robust inference methods
robust(res, cluster=trial)

### use methods from the clubSandwich package
robust(res, cluster=trial, clubSandwich=TRUE)

############################################################################

---

### Description

Function to fit selection models.
selmodel

Usage

selmodel(x, ...)

## S3 method for class 'rma.uni'
selmodel(x, type, alternative="greater", prec,
delta, steps, verbose=FALSE, digits, control, ...)

Arguments

x        an object of class "rma.uni".
type     character string to specify the type of selection model. Possible options are "beta", "halfnorm", "negexp", "logistic", "power", "negexp_pow", or "stepfun". Can be abbreviated. See ‘Details’.
alternative character string to specify the sidedness of the hypothesis when testing the observed outcomes. Possible options are "greater" (the default), "less", or "two.sided". Can be abbreviated.
p prec     optional character string to specify the measure of precision (only relevant for selection models that can incorporate this into the selection function). Possible options are "sei", "vi", "ninv", or "sqrtfinv". See ‘Details’.
delta     optional numeric vector (of the same length as the number of selection model parameters) to fix the corresponding \( \delta \) value(s). A specific \( \delta \) value can be fixed by setting the corresponding element of this argument to the desired value. A specific \( \delta \) value will be estimated if the corresponding element is set equal to \( \text{NA} \). See ‘Details’.
steps     numeric vector of one or more values between 0 and 1 that can or must be specified for certain selection functions. See ‘Details’.
verbose   logical to specify whether output should be generated on the progress of the model fitting (the default is FALSE). Can also be an integer. Values > 1 generate more verbose output. See ‘Note’.
digits    optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.
control   optional list of control values for the estimation algorithm. If unspecified, default values are defined inside the function. See ‘Note’.
...       other arguments.

Details

Selection models are a general class of models that attempt to model the process by which the studies included in a meta-analysis may have been influenced by some form of publication bias. If a particular selection model is an adequate approximation for the underlying selection process, then the model provides estimates of the parameters of interest (e.g., the average true outcome and the amount of heterogeneity in the true outcomes) that are ‘corrected’ for this selection process (i.e., they are estimates of the parameters in the population of studies before any selection has taken place). The present function fits a variety of such selection models. To do so, one should pass an object fitted with the rma.uni function to the first argument. The model that will then be fitted
is of the same form as the original model combined with the specific selection model chosen (see below for possible options). For example, if the original model was a random-effects model, then a random-effects selection model will be fitted. Similarly, if the original model included moderators, then they will also be included in the selection model. Model fitting is done via maximum likelihood (ML) estimation over the fixed- and random-effects parameters (e.g., $\mu$ and $\tau^2$ in a random-effects model) and the selection model parameters.

Argument type determines the specific type of selection model that should be fitted. All selection models that can be fitted are based on the idea that selection may have taken place based on the p-values of the studies. In particular, let $y_i$ and $v_i$ denote the observed outcome and the corresponding sampling variance of the $i$th study. Then $z_i = y_i / \sqrt{v_i}$ is the (Wald-type) test statistic for testing the null hypothesis $H_0: \theta_i = 0$ and $p_i = 1 - \Phi(z_i)$ (if alternative="greater"), $p_i = \Phi(z_i)$ (if alternative="less"), or $p_i = 2(1 - \Phi(|z_i|))$ (if alternative="two.sided") the corresponding (one- or two-sided) p-value, where $\Phi()$ denotes the cumulative distribution function of a standard normal distribution. Finally, let $w(p_i)$ denote some function that specifies the relative likelihood of selection given the p-value of a study.

If $w(p_i) > w(p_i')$ when $p_i < p_i'$ (i.e., $w(p_i)$ is larger for smaller p-values), then alternative="greater" implies selection in favor of increasingly significant positive outcomes, alternative="less" implies selection in favor of increasingly significant negative outcomes, and alternative="two.sided" implies selection in favor of increasingly significant outcomes regardless of their direction.

**Beta Selection Model:**

When type="beta", the function can be used to fit the ‘beta selection model’ by Cítkowicz and Vevea (2017). For this model, the selection function is given by

$$w(p_i) = p_i^{\delta_1 - 1} \times (1 - p_i)^{\delta_2 - 1}$$

where $\delta_1 > 0$ and $\delta_2 > 0$. The null hypothesis $H_0: \delta_1 = \delta_2 = 1$ represents the case where there is no selection (at least not depending on the p-values). The figure below illustrates with some examples how the relative likelihood of selection can depend on the p-value for various combinations of $\delta_1$ and $\delta_2$. Note that the model allows for a non-monotonic selection function.
Half-Normal, Negative-Exponential, Logistic, and Power Selection Models:

Preston et al. (2004) suggested the first three of the following selection functions:

<table>
<thead>
<tr>
<th>name</th>
<th>type</th>
<th>selection function</th>
</tr>
</thead>
<tbody>
<tr>
<td>half-normal</td>
<td>&quot;halfnorm&quot;</td>
<td>( w(p_i) = \exp(-\delta \times p_i^2) )</td>
</tr>
<tr>
<td>negative-exponential</td>
<td>&quot;negexp&quot;</td>
<td>( w(p_i) = \exp(-\delta \times p_i) )</td>
</tr>
<tr>
<td>logistic</td>
<td>&quot;logistic&quot;</td>
<td>( w(p_i) = 2 \times \exp(-\delta \times p_i)/(1 + \exp(-\delta \times p_i)) )</td>
</tr>
<tr>
<td>power</td>
<td>&quot;power&quot;</td>
<td>( w(p_i) = (1 - p_i)^\delta )</td>
</tr>
</tbody>
</table>

The power selection model is added here as it has similar properties as the models suggested by Preston et al. (2004). For all models, assume \( \delta \geq 0 \), so that all functions imply a monotonically decreasing relationship between the p-value and the selection probability. For all functions, \( H_0: \delta = 0 \) implies no selection. The figure below shows the relative likelihood of selection as a function of the p-value for \( \delta = 0 \) and for the various selection functions when \( \delta = 6 \).
Here, these functions are extended to allow for the possibility that \( w(p_i) = 1 \) for p-values below a certain significance threshold denoted by \( \alpha \) (e.g., to model the case that the relative likelihood of selection is equally high for all significant studies but decreases monotonically for p-values above the significance threshold). To fit such a selection model, one should specify the \( \alpha \) value (with \( 0 < \alpha < 1 \)) via the steps argument. There must be at least one observed p-value below and above the chosen threshold to fit these models. The figure below shows some examples of the relative likelihood of selection when \texttt{steps}=.05.
Preston et al. (2004) also suggested selection functions where the relatively likelihood of selection not only depends on the p-value, but also the precision (e.g., standard error) of the estimate (if two studies have similar p-values, it may be plausible to assume that the larger / more precise study has a higher probability of selection). These selection functions plus the corresponding power functions are given by:

<table>
<thead>
<tr>
<th>name</th>
<th>type</th>
<th>selection function</th>
</tr>
</thead>
<tbody>
<tr>
<td>half-normal</td>
<td>&quot;halfnorm&quot;</td>
<td>( w(p_i) = \exp(-\delta \times \text{prec}_i \times p_i^2) )</td>
</tr>
<tr>
<td>negative-exponential</td>
<td>&quot;negexp&quot;</td>
<td>( w(p_i) = \exp(-\delta \times \text{prec}_i \times p_i) )</td>
</tr>
<tr>
<td>logistic</td>
<td>&quot;logistic&quot;</td>
<td>( w(p_i) = 2 \times \exp(-\delta \times \text{prec}_i \times p_i)/(1 + \exp(-\delta \times \text{prec}_i \times p_i)) )</td>
</tr>
<tr>
<td>power</td>
<td>&quot;power&quot;</td>
<td>( w(p_i) = (1 - p_i)^{\delta \times \text{prec}_i} )</td>
</tr>
</tbody>
</table>

where \( \text{prec}_i = \sqrt{v_i} \) (i.e., the standard error of the \( i \)th study) according to Preston et al. (2004). Here, this idea is generalized to allow the user to specify the specific measure of precision to use (via the prec argument). Possible options are:

- prec="sei" for the standard errors,
- prec="vi" for the sampling variances,
- prec="ninv" for the inverse of the sample sizes,
- prec="sqrtninv" for the inverse square root of the sample sizes.

Using some function of the sample sizes as a measure of precision is only possible when information about the sample sizes is actually stored within the object passed to the selmodel function. See ‘Note’.
Note that \( p_{\text{prec}} \) is really a measure of imprecision (with higher values corresponding to lower precision). Also, regardless of the specific measure chosen, the values are actually rescaled with \( \text{prec}_i = \frac{\text{prec}_i}{\max(\text{prec}_i)} \) inside of the function, such that \( \text{prec}_i = 1 \) for the least precise study and \( \text{prec}_i < 1 \) for the remaining studies (the rescaling does not actually change the fit of the model, it only helps to improve the stability of model fitting algorithm). The figure below shows some examples of the relative likelihood of selection using these selection functions for two different precision values.

One can also use the \texttt{steps} argument as described above in combination with these selection functions (studies with \( p \)-values below the chosen threshold then have \( w(p_i) = 1 \) regardless of their exact \( p \)-value or precision).

**Negative Exponential Power Selection Model:**

As an extension of the half-normal and negative-exponential models, one can also choose \texttt{type=}“negexppow” for a ‘negative exponential power selection model’. The selection function is then given by

\[
    w(p_i) = \exp\left(-\delta_1 \times p_i^{1/\delta_2}\right)
\]

where \( \delta_1 \geq 0 \) and \( \delta_2 \geq 0 \) (see Begg & Mazumdar, 1994, although here a different parameterization is used, such that increasing \( \delta_2 \) leads to more severe selection). The figure below shows some examples of this selection function when holding \( \delta_1 \) constant while increasing \( \delta_2 \).
This model affords greater flexibility in the shape of the selection function, but requires the estimation of the additional power parameter (the half-normal and negative-exponential models are therefore special cases when fixing $\delta_2$ to 0.5 or 1, respectively). $H_0$: $\delta_1 = 0$ again implies no selection, but so does $H_0$: $\delta_2 = 0$.

One can again use the steps argument to specify a single significance threshold, $\alpha$, so that $w(p_i) = 1$ for p-values below this threshold and otherwise $w(p_i)$ follows the selection function as given above. One can also use the prec argument to specify a measure of precision in combination with this model, which leads to the selection function

$$w(p_i) = \exp(-\delta_1 \times \text{prec}_i \times p_i^{1/\delta_2})$$

and hence is the logical extension of the negative exponential power selection model that also incorporates some measure of precision into the selection process.

**Step Function Selection Models:**

When type="stepfun", the function can be used to fit ‘step function models’ as described by Iyengar and Greenhouse (1988), Hedges (1992), Vevea and Hedges (1995), and Vevea and Woods (2005). For these models, one must specify one or multiple values via the steps argument, which define intervals in which the relative likelihood of selection is constant. Let

$$\alpha_1 < \alpha_2 < \ldots < \alpha_c$$

denote these cutpoints sorted in increasing order, with the constraint that $\alpha_c = 1$ (if the highest value specified via steps is not 1, the function will automatically add this cutpoint), and define $\alpha_0 = 0$. The selection function is then given by $w(p_i) = \delta_j$ if $\alpha_{j-1} < p_i \leq \alpha_j$. To make the
model identifiable, we set $\delta_1 = 1$. The $\delta_j$ values therefore denote the likelihood of selection in the various intervals relative to the interval for $p$-values between 0 and $\alpha_1$. Hence, the null hypothesis $H_0: \delta_j = 1$ for $j = 1, \ldots, c$ implies no selection.

For example, if steps=c(.05, .10, .50, 1), then $\delta_2$ is the likelihood of selection for $p$-values between .05 and .10, $\delta_3$ is the likelihood of selection for $p$-values between .10 and .50, and $\delta_4$ is the likelihood of selection for $p$-values between .50 and 1 relative to the likelihood of selection for $p$-values between 0 and .05. The figure below shows the corresponding selection function for some arbitrarily chosen $\delta_j$ values.

There must be at least one observed $p$-value within each interval to fit this model. If this is not the case, an error will be issued (setting verbose=TRUE provides information about the number of $p$-values falling into each interval).

When specifying a single cutpoint in the context of a random-effects model, this model is sometimes called the ‘three-parameter selection model’ (3PSM), corresponding to the parameters $\mu$, $\tau^2$, and $\delta_2$ (e.g., Carter et al., 2019; McShane et al., 2016; Pustejovsky & Rodgers, 2019). The same idea but in the context of an equal-effects model was also described by Iyengar and Greenhouse (1988).

Note that when alternative="greater" or alternative="less" (i.e., when we assume that the relative likelihood of selection is not only related to the $p$-values of the studies, but also the directionality of the outcomes), then it would usually make sense to divide conventional levels of significance (e.g., .05) by 2 before passing these values to the steps argument. For example, if we think that studies were selected for positive outcomes that are significant at two-tailed $\alpha = .05$, then we should use alternative="greater" in combination with steps=c(.025, 1).

One of the challenges when fitting this model with many cutpoints is the large number of pa-
rameters that need to be estimated (which is especially problematic when the number of studies is small). An alternative approach suggested by Vevea and Woods (2005) is to fix the $\delta_j$ values to some a priori chosen values instead of estimating them. One can then conduct a sensitivity analysis by examining the results (e.g., the estimates of $\mu$ and $\tau^2$ in a random-effects model) for a variety of different sets of $\delta_j$ values (reflecting more or less severe forms of selection). This can be done by specifying the $\delta_j$ values via the `delta` argument. Table 1 in Vevea and Woods (2005) provides some illustrative examples of moderate and severe selection functions for one- and two-tailed selection. The code below creates a data frame that contains these functions.

```r
tab <- data.frame(
  steps = c(0.005, 0.01, 0.05, 0.10, 0.25, 0.35, 0.50, 0.65, 0.75, 0.90, 0.95, 0.99, 0.995, 1),
  delta.mod.1 = c(1, 0.99, 0.95, 0.80, 0.75, 0.65, 0.50, 0.50, 0.50, 0.50, 0.50, 0.50, 0.50, 0.50),
  delta.sev.1 = c(1, 0.99, 0.90, 0.75, 0.60, 0.50, 0.40, 0.35, 0.30, 0.25, 0.10, 0.10, 0.10, 0.10),
  delta.mod.2 = c(1, 0.99, 0.95, 0.90, 0.80, 0.75, 0.60, 0.50, 0.40, 0.35, 0.30, 0.25, 0.25, 0.25, 0.25, 0.25),
  delta.sev.2 = c(1, 0.99, 0.90, 0.75, 0.60, 0.50, 0.25, 0.25, 0.50, 0.60, 0.75, 0.90, 0.99, 1.00))
```

The figure below shows the corresponding selection functions.

These four functions are “merely examples and should not be regarded as canonical” (Vevea & Woods, 2005).

Value

An object of class `c("rma.uni","rma")`. The object is a list containing the same components as a regular `c("rma.uni","rma")` object, but the parameter estimates are based on the selection model. Most importantly, the following elements are modified based on the selection model:
beta estimated coefficients of the model.
se standard errors of the coefficients.
zval test statistics of the coefficients.
pval corresponding p-values.
ci.lb lower bound of the confidence intervals for the coefficients.
ci.ub upper bound of the confidence intervals for the coefficients.
vb variance-covariance matrix of the estimated coefficients.
tau2 estimated amount of (residual) heterogeneity. Always 0 when method="EE".
se.tau2 standard error of the estimated amount of (residual) heterogeneity.

In addition, the object contains the following additional elements:
delta estimated selection model parameter(s).
se.delta corresponding standard error(s).
zval.delta corresponding test statistic(s).
pval.delta corresponding p-value(s).
ci.lb.delta lower bound of the confidence intervals for the parameter(s).
ci.ub.delta upper bound of the confidence intervals for the parameter(s).
LRT test statistic of the likelihood ratio test for the selection model parameter(s).
LRTdf degrees of freedom for the likelihood ratio test.
LRTp p-value for the likelihood ratio test.
LRT.tau2 test statistic of the likelihood ratio test for testing H_0: \tau^2 = 0 (NA when fitting an equal-effects model).
LRTp.tau2 p-value for the likelihood ratio test.
... some additional elements/values.

Methods

The results of the fitted model are formatted and printed with the print function. The estimated selection function can be drawn with plot.

The profile function can be used to obtain a plot of the log-likelihood as a function of \tau^2 and/or the selection model parameter(s) of the model. Corresponding confidence intervals can be obtained with the confint function.

Note

Model fitting is done via numerical optimization over the model parameters. By default, optim with method "BFGS" is used for the optimization. One can also chose a different optimizer from optim via the control argument (e.g., control=list(optimizer="Nelder-Mead")). Besides one of the methods from optim, one can also choose the quasi-Newton algorithm in nlmib, one of the optimizers from the minqa package (i.e., uobyqa, newuoa, or bobyqa), one of the (derivative-free) algorithms from the nloptr package, the Newton-type algorithm implemented in nlm, the various algorithms implemented in the dfoptim package (hjk for the Hooke-Jeeves, nmk for the
Nelder-Mead, and mads for the Mesh Adaptive Direct Searches algorithm), the quasi-Newton type optimizers ucminf and lbfgsb3c and the subspace-searching simplex algorithm subplex from the packages of the same name, the Barzilai-Borwein gradient decent method implemented in BBoptim, or the parallelized version of the L-BFGS-B algorithm implemented in optimParallel from the package of the same name.

The optimizer name must be given as a character string (i.e., in quotes). Additional control parameters can be specified via the control argument (e.g., control=list(maxit=1000, reltol=1e-8)). For nloptr, the default is to use the BOBYQA implementation from that package with a relative convergence criterion of 1e-8 on the function value (i.e., log-likelihood), but this can be changed via the algorithm and ftol_rel arguments (e.g., control=list(optimizer="nloptr", algorithm="NLOPT_LN_SBPLX", ftol_rel=1e-6)). For optimParallel, the control argument ncpus can be used to specify the number of cores to use for the parallelization (e.g., control=list(optimizer="optimParallel", ncpus=2)). With parallel::detectCores(), one can check on the number of available cores on the local machine.

All selection models (except for type="stepfun") require repeated evaluations of an integral, which is done via adaptive quadrature as implemented in the integrate function. One can adjust the arguments of the integrate function via control element intCtrl, which is a list of named arguments (e.g., control = list(intCtrl = list(rel.tol=1e-4, subdivisions=100))).

The starting values for the fixed effects, the $\tau^2$ value (only relevant in random/mixed-effects models), and the $\delta$ parameter(s) are chosen automatically by the function, but one can also set the starting values manually via the control argument by specifying a vector of the appropriate length for beta.init, a single value for tau2.init, and a vector of the appropriate length for delta.init.

By default, the $\delta$ parameter(s) are constrained to a certain range, which improves the stability of the optimization algorithm. For all models, the maximum is set to 100 and the minimum to 0 (except for type="beta", where the minimum for both parameters is 1e-05). These defaults can be changed via the control argument by specifying a vector of the appropriate length for delta.min and/or delta.max.

A difficulty with fitting the beta selection model (i.e., type="beta") is the behavior of $w(p_i)$ when $p_i = 0$ or $p_i = 1$. When $\delta_1 < 1$ or $\delta_2 < 1$, then this leads to selection weights equal to infinity, which causes problems when computing the likelihood function. Following Citkowicz and Vevea (2017), this problem can be avoided by censoring p-values too close to 0 or 1. The specific censoring point can be set via the pval.min element of the control argument. The default for this selection model is control=list(pval.min=1e-5). A similar issues arises for the power selection model (i.e., type="power") when $p_i = 1$. Again, pval.min=1e-5 is used to circumvent this issue. For all other selection models, the default is pval.min=0.

The variance-covariance matrix corresponding to the estimates of the fixed effects, the $\tau^2$ value (only relevant in random/mixed-effects models), and the $\delta$ parameter(s) is obtained by inverting the Hessian, which is numerically approximated using the hessian function from the numDeriv package. This may fail, leading to NA values for the standard errors and hence test statistics, p-values, and confidence interval bounds. One can set control argument hessianCtrl to a list of named arguments to be passed on to the method.args argument of the hessian function (the default is control=list(hessianCtrl=list(r=6))).

Information on the progress of the optimization algorithm can be obtained by setting verbose=TRUE (this won’t work when using parallelization). This option is useful to determine how the model fitting is progressing. One can also set verbose to an integer (verbose=2 yields even more information and verbose=3 also show the progress visually by drawing the selection function as the optimization proceeds).
For selection functions where the `prec` argument is relevant, using (a function of) the sample sizes as the measure of precision (i.e., `prec="ninv"` or `prec="sqrtninv"`) is only possible when information about the sample sizes is actually stored within the object passed to the `selmodel` function. That should automatically be the case when the observed effect sizes or outcomes were computed with the `escalc` function or when the observed effect sizes or outcomes were computed within the model fitting function. On the other hand, this will not be the case when `rma.uni` was used together with the `yi` and `vi` arguments and the `yi` and `vi` values were not computed with `escalc`. In that case, it is still possible to pass information about the sample sizes to the `rma.uni` function (e.g., use `rma.uni(yi, vi, ni=ni, data=dat)` where data frame `dat` includes a variable called `ni` with the sample sizes).

Finally, the automatic rescaling of the chosen precision measure can be switched off by setting `scaleprec=FALSE`.

**Author(s)**

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**References**


**See Also**

`rma.uni` for the function to fit models which can be extended with selection models.
Examples

############################################################################
### example from Citkowicz and Vevea (2017) for beta selection model
#
# copy data into 'dat' and examine data
dat <- dat.baskerville2012

dat
#
# fit random-effects model
res <- rma(smd, se^2, data=dat, method="ML", digits=3)
res
#
# funnel plot
funnel(res, ylim=c(0,0.6), xlab="Standardized Mean Difference")
#
# fit beta selection model
## Not run:
sel <- selmodel(res, type="beta")

# plot selection function
plot(sel, ylim=c(0,40))
## End(Not run)
#
# fit mixed-effects meta-regression model with 'blind' dummy variable as moderator
res <- rma(smd, se^2, data=dat, mods = ~ blind, method="ML", digits=3)
res
#
# predicted average effect for studies that do not and that do use blinding
predict(res, newmods=c(0,1))
#
# fit beta selection model
## Not run:
sel <- selmodel(res, type="beta")

# End(Not run)

### example from Preston et al. (2004)
#
# copy data into 'dat' and examine data
dat <- dat.hahn2001

dat
#
### meta-analysis of (log) odds rations using the Mantel-Haenszel method
res <- rma.mh(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat, digits=2, slab=study)
res
# calculate log odds ratios and corresponding sampling variances
dat <- escalc(measure="OR", ai=ai, n1i=n1i, ci=ci, n2i=n2i, data=dat, drop00=TRUE)
dat

# fit equal-effects model
res <- rma(yi, vi, data=dat, method="EE")

# predicted odds ratio (with 95% CI)
predict(res, transf=exp, digits=2)

# funnel plot
funnel(res, atransf=exp, at=log(c(0.01,0.1,1,10,100)), ylim=c(0,2))

# fit half-normal, negative-exponential, logistic, and power selection models
## Not run:
sel1 <- selmodel(res, type="halfnorm", alternative="less")
sel2 <- selmodel(res, type="negexp", alternative="less")
sel3 <- selmodel(res, type="logistic", alternative="less")
sel4 <- selmodel(res, type="power", alternative="less")

# plot selection functions
plot(sel1)
plot(sel2, add=TRUE, col="blue")
plot(sel3, add=TRUE, col="red")
plot(sel4, add=TRUE, col="green")

# add legend
legend("topright", inset=.02, lty="solid", lwd=2, col=c("black","blue","red","green"),
  legend=c("Half-normal", "Negative-exponential", "Logistic", "Power"))

# show estimates of delta (and corresponding SEs)
tab <- data.frame(delta = c(sel1$delta, sel2$delta, sel3$delta, sel4$delta),
  se = c(sel1$se.delta, sel2$se.delta, sel3$se.delta, sel4$se.delta))
rownames(tab) <- c("Half-normal", "Negative-exponential", "Logistic", "Power")
round(tab, 2)

# predicted odds ratios (with 95% CI)
predict(res, transf=exp, digits=2)
predict(sel1, transf=exp, digits=2)
predict(sel2, transf=exp, digits=2)
predict(sel3, transf=exp, digits=2)
predict(sel4, transf=exp, digits=2)

## End(Not run)

# fit selection models including standard error as precision measure (note: using
# scaleprec=FALSE here since Preston et al. (2004) did not use the rescaling)
## Not run:
sel1 <- selmodel(res, type="halfnorm", prec="sei", alternative="less", scaleprec=FALSE)
sel2 <- selmodel(res, type="negexp", prec="sei", alternative="less", scaleprec=FALSE)
sel3 <- selmodel(res, type="logistic", prec="sei", alternative="less", scaleprec=FALSE)
sel4 <- selmodel(res, type="power", prec="sei", alternative="less", scaleprec=FALSE)
# show estimates of delta (and corresponding SEs)
tab <- data.frame(delta = c(sel1$delta, sel2$delta, sel3$delta, sel4$delta),
                 se = c(sel1$se.delta, sel2$se.delta, sel3$se.delta, sel4$se.delta))
rownames(tab) <- c("Half-normal", "Negative-exponential", "Logistic", "Power")
round(tab, 2)

# predicted odds ratio (with 95% CI)
predict(res, transf=exp, digits=2)
predict(sel1, transf=exp, digits=2)
predict(sel2, transf=exp, digits=2)
predict(sel3, transf=exp, digits=2)
predict(sel4, transf=exp, digits=2)

## End(Not run)

############################################################################
### meta-analysis on the effect of environmental tobacco smoke on lung cancer risk

# copy data into 'dat' and examine data
dat <- dat.hackshaw1998
dat

# fit random-effects model
res <- rma(yi, vi, data=dat, method="ML")
res

# funnel plot
funnel(res, atransf=exp, at=log(c(0.25,0.5,1,2,4,8)), ylim=c(0,0.8))

# step function selection model
## Not run:
sel <- selmodel(res, type="stepfun", alternative="greater", steps=c(.025,.10,.50,1))

# plot selection function
plot(sel)

## End(Not run)

############################################################################
### validity of student ratings example from Vevea & Woods (2005)

# copy data into 'dat' and examine data
dat <- dat.cohen1981
dat[c(1,4,5)]

# calculate r-to-z transformed correlations and corresponding sampling variances
dat <- escalc(measure="ZCOR", ri=ri, ni=ni, data=dat[c(1,4,5)])

dat
# fit random-effects model
res <- rma(yi, vi, data=dat, method="ML", digits=3)
res

# predicted average correlation (with 95% CI)
predict(res, transf=transf.ztor)

# funnel plot
funnel(res, ylim=c(0,0.4))

# selection functions from Vevea & Woods (2005)
tab <- data.frame(
  steps = c(0.005, 0.01, 0.05, 0.10, 0.25, 0.35, 0.50, 0.65, 0.75, 0.90, 0.95, 0.99, 0.995, 1),
  delta.mod.1 = c(1, 0.99, 0.95, 0.80, 0.75, 0.65, 0.60, 0.55, 0.50, 0.50, 0.50, 0.50, 0.50, 0.50),
  delta.sev.1 = c(1, 0.99, 0.90, 0.75, 0.60, 0.50, 0.40, 0.35, 0.30, 0.25, 0.20, 0.10, 0.10, 0.10),
  delta.mod.2 = c(1, 0.99, 0.95, 0.90, 0.80, 0.75, 0.60, 0.50, 0.75, 0.80, 0.90, 0.95, 0.99, 1.00),
  delta.sev.2 = c(1, 0.99, 0.90, 0.75, 0.60, 0.50, 0.25, 0.25, 0.50, 0.50, 0.75, 0.90, 0.99, 1.00))

# apply step function model with a priori chosen selection weights
## Not run:
sel <- lapply(tab[-1], function(delta) selmodel(res, type="stepfun", steps=tab$steps, delta=delta))

# estimates (transformed correlation) and tau^2 values
sav <- data.frame(estimate = round(c(res$beta, sapply(sel, function(x) x$beta)), 2),
  varcomp = round(c(res$tau2, sapply(sel, function(x) x$tau2)), 3))
sav

## End(Not run)

~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~

---

**simulate.rma**  
*Simulate Method for 'rma' Objects*

**Description**

The function simulates effect sizes or outcomes based on "rma" model object.

**Usage**

```r
## S3 method for class 'rma'
simulate(object, nsim=1, seed=NULL, olim, ...)
```

**Arguments**

- `object`  
an object of class "rma".

- `nsim`  
number of response vectors to simulate (defaults to 1).
seed

seeds an object to specify if and how the random number generator should be initialized ("seeded"). Either NULL or an integer that will be used in a call to set.seed before simulating the response vectors. If set, the value is saved as the "seed" attribute of the returned value. The default, NULL will not change the random generator state, and return .Random.seed as the "seed" attribute; see ‘Value’.

olim

optional argument to specify observation/outcome limits for the simulated values. If unspecified, no limits are used.

... other arguments.

Details

The model specified via object must be a model fitted with either the \texttt{rma.uni} or \texttt{rma.mv} function.

Value

A data frame with \texttt{nsim} columns with the simulated effect sizes or outcomes.

The data frame comes with an attribute "seed". If argument seed is NULL, the attribute is the value of \texttt{.Random.seed} before the simulation was started; otherwise it is the value of the seed argument with a "kind" attribute with value as.list(RNGkind()).

Note

If the outcome measure used for the analysis is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the \texttt{olim} argument to enforce those observation/outcome limits when simulating values (simulated values cannot exceed those bounds then).

Author(s)

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References


See Also

\texttt{rma.uni} and \texttt{rma.mv} for functions to fit models for which simulated effect sizes or outcomes can be generated.

Examples

```r
### copy BCG vaccine data into 'dat'
dat <- dat.bcg

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat)
dat
```
### fit random-effects model
res <- rma(yi, vi, data=dat)
res

### simulate 5 sets of new outcomes based on the fitted model
newdat <- simulate(res, nsim=5, seed=1234)
newdat

---

tes  

**Test of Excess Significance**

---

**Description**

Function to conduct the test of excess significance.

**Usage**

```r
tes(x, vi, sei, subset, data, H0=0, alternative="two.sided", alpha=.05, theta, tau2, test, tes.alternative="greater", progbar=TRUE, tes.alpha=.10, digits, ...)
```

## S3 method for class 'tes'

```r
print(x, digits=x$digits, ...)
```

**Arguments**

These arguments pertain to data input:

- `x` vector with the observed effect sizes or outcomes or an object of class "rma".
- `vi` vector with the corresponding sampling variances (ignored if `x` is an object of class "rma").
- `sei` vector with the corresponding standard errors (note: only one of the two, `vi` or `sei`, needs to be specified).
- `subset` optional (logical or numeric) vector to specify the subset of studies that should be included (ignored if `x` is an object of class "rma").
- `data` optional data frame containing the variables given to the arguments above.

These arguments pertain to the tests of the observed effect sizes or outcomes:

- `H0` numeric value to specify the value of the effect size or outcome under the null hypothesis (the default is 0).
- `alternative` character string to specify the sidedness of the hypothesis when testing the observed effect sizes or outcomes. Possible options are "two.sided" (the default), "greater", or "less". Can be abbreviated.
- `alpha` alpha level for testing the observed effect sizes or outcomes (the default is .05).

These arguments pertain to the power of the tests:

- `theta` optional numeric value to specify the value of the true effect size or outcome under the alternative hypothesis. If unspecified, it will be estimated based on the data or the value is taken from the "rma" object.
tau2
optional numeric value to specify the amount of heterogeneity in the true effect sizes or outcomes. If unspecified, the true effect sizes or outcomes are assumed to be homogeneous or the value is taken from the "rma" object.
These arguments pertain to the test of excess significance:

test
optional character string to specify the type of test to use for conducting the test of excess significance. Possible options are "chi2", "binom", or "exact". Can be abbreviated. If unspecified, the function chooses the type of test based on the data.
tes.alternative
character string to specify the sidedness of the hypothesis for the test of excess significance. Possible options are "greater" (the default), "two.sided", or "less". Can be abbreviated.
progbars
logical to specify whether a progress bar should be shown (the default is TRUE). Only relevant when conducting an exact test.
tes.alpha
alpha level for the test of excess significance (the default is .10). Only relevant for finding the 'limit estimate'.

Miscellaneous arguments:
digits
optional integer to specify the number of decimal places to which the printed results should be rounded.
...
other arguments.

Details
The function carries out the test of excess significance described by Ioannidis and Trikalinos (2007). The test can be used to examine whether the observed number of significant findings is greater than the number of significant findings expected given the power of the tests. An overabundance of significant tests may suggest that the collection of studies is not representative of all studies conducted on a particular topic.

One can either pass a vector with the observed effect sizes or outcomes (via x) and the corresponding sampling variances via vi (or the standard errors via sei) to the function or an object of class "rma".

The observed effect sizes or outcomes are tested for significance based on a standard Wald-type test, that is, by comparing

$$ z_i = \frac{y_i - H_0}{\sqrt{v_i}} $$

against the appropriate critical value(s) of a standard normal distribution (e.g., ±1.96 for alternative="two.sided" and alpha=.05, which are the defaults). Let O denote the observed number of significant tests.

Given a particular value for the true effect or outcome denoted by $\theta$ (which, if it is unspecified, is determined by computing the inverse-variance weighted average of the observed effect sizes or outcomes or the value is taken from the model object), let $1 - \beta_i$ denote the power of the $i$th test (where $\beta_i$ denotes the Type II error probability). If $\tau^2 > 0$, let $1 - \beta_i$ denote the expected power (computed based on integrating the power over a normal distribution with mean $\theta$ and variance $\tau^2$). Let $E = \sum_{i=1}^{k} (1 - \beta_i)$ denote the expected number of significant tests.

The test of excess significance then tests if $O$ is significantly greater (if tes.alternative="greater") than $E$. This can be done using Pearson's chi-squared test (if test="chi2"), a binomial test (if test="binomial"), or an exact test (if test="exact"). The latter is described in Francis (2013).
If argument `test` is unspecified, the default is to do an exact test if the number of elements in the
sum that needs to be computed is less than or equal to $10^6$ and to do a chi-square test otherwise.

One can also iteratively find the value of $\theta$ such that the p-value of the test of excess significance is
equal to `tes.alpha` (which is .10 by default). The resulting value is called the ‘limit estimate’ and
is denoted $\theta_{lim}$ by Ioannidis and Trikalinos (2007). Note that the limit estimate is not computable
if the p-value is larger than `tes.alpha` even if $\theta = H_0$.

### Value

An object of class "tes". The object is a list containing the following components:

- `k` the number of studies included in the analysis.
- `O` the observed number of significant tests.
- `E` the expected number of significant tests.
- `OEratio` the ratio of O over E.
- `test` the type of test conducted.
- `pval` the p-value of the test of excess significance.
- `power` the (estimated) power of the tests.
- `sig` logical vector indicating which tests were significant.
- `theta` the value of $\theta$ used for computing the power of the tests.
- `theta.lim` the ‘limit estimate’ (i.e., $\theta_{lim}$).
- `...` some additional elements/values.

The results are formatted and printed with the `print` function.

### Note

When `tes.alternative="greater"` (the default), then the function tests if $O$ is significantly
greater than $E$ and hence this is indeed a test of excess significance. When `tes.alternative="two.sided"`,
then the function tests if $O$ differs significantly from $E$ in either direction and hence it would be
more apt to describe this as a test of (in)consistency (between $O$ and $E$). Finally, one can also
set `tes.alternative="less"`, in which case the function tests if $O$ is significantly lower than $E$,
which could be considered a test of excess non-significance.

When `tes.alternative="two.sided"`, one can actually compute two limit estimates. The function
attempts to compute both.

The function computes the significance and power of the studies based on Wald-type tests regardless
of the effect size or outcome measure used as input. This works as an adequate approximation as
long as the within-study sample sizes are not too small.

Note that the test is not a test for publication bias but a test whether the set of studies includes an
unusual number of significant findings given the power of the studies. The general usefulness of the
test and its usefulness under particular circumstances (e.g., when there is substantial heterogeneity
in the true effect sizes or outcomes) has been the subject of considerable debate. See Francis (2013)
and the commentaries on this article in the same issue of the journal.
Author(s)

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References


See Also

`ranktest` for the rank test, `regtest` for the regression test, `trimfill` for the trim and fill method, and `selmodel` for selection models.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=x.a, n1i=n.a, ci=x.p, n2i=n.p, data=dat.dorn2007)

### conduct test of excess significance (using test="chi2" to speed things up)
tes(yi, vi, data=dat, test="chi2")

### same as fitting an EE model and then passing the object to the function
res <- rma(yi, vi, data=dat, method="EE")
tes(res, test="chi2")

### illustrate limit estimate (value of theta where p-value of test is equal to tes.alpha)
thetas <- seq(0,1,length=101)
pvals <- sapply(thetas, function(theta) tes(yi, vi, data=dat, test="chi2", theta=theta)$pval)
plot(thetas, pvals, type="o", pch=19, ylim=c(0,1))
sav <- tes(yi, vi, data=dat, test="chi2")
abline(h=sav$tes.alpha, lty="dotted")
abline(v=sav$theta.lim, lty="dotted")

### examine significance of test as a function of alpha (to examine 'significance chasing')
alphas <- seq(.01,.99,length=101)
pvals <- sapply(alphas, function(alpha) tes(yi, vi, data=dat, test="chi2", alpha=alpha)$pval)
plot(alphas, pvals, type="o", pch=19, ylim=c(0,1))
abline(v=.05, lty="dotted")
abline(h=.10, lty="dotted")
```
to.long

Convert Data from Vector to Long Format

Description

The function converts summary data in vector format to the corresponding long format.

Usage

to.long(measure, ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i,
m1i, m2i, sd1i, sd2i, xi, mi, ri, ti, sdi, ni, data, slab, subset,
add=1/2, to="none", drop00=FALSE, vlong=FALSE, append=TRUE, var.names)

Arguments

- **measure**: a character string to specify the effect size or outcome measure corresponding to the summary data supplied. See `Details` and the documentation of the `escalc` function for possible options.
- **ai**: vector to specify the $2 \times 2$ table frequencies (upper left cell).
- **bi**: vector to specify the $2 \times 2$ table frequencies (upper right cell).
- **ci**: vector to specify the $2 \times 2$ table frequencies (lower left cell).
- **di**: vector to specify the $2 \times 2$ table frequencies (lower right cell).
- **n1i**: vector to specify the group sizes or row totals (first group/row).
- **n2i**: vector to specify the group sizes or row totals (second group/row).
- **x1i**: vector to specify the number of events (first group).
- **x2i**: vector to specify the number of events (second group).
- **t1i**: vector to specify the total person-times (first group).
- **t2i**: vector to specify the total person-times (second group).
- **m1i**: vector to specify the means (first group or time point).
- **m2i**: vector to specify the means (second group or time point).
- **sd1i**: vector to specify the standard deviations (first group or time point).
- **sd2i**: vector to specify the standard deviations (second group or time point).
- **xi**: vector to specify the frequencies of the event of interest.
- **mi**: vector to specify the frequencies of the complement of the event of interest or the group means.
- **ri**: vector to specify the raw correlation coefficients.
- **ti**: vector to specify the total person-times.
- **sdi**: vector to specify the standard deviations.
- **ni**: vector to specify the sample/group sizes.
- **data**: optional data frame containing the variables given to the arguments above.
slab optional vector with labels for the studies.

subset optional (logical or numeric) vector to specify the subset of studies that should include in the data frame returned by the function.

add see the documentation of the escalc function.

to see the documentation of the escalc function.

drop00 see the documentation of the escalc function.

vlong optional logical whether a very long format should be used (only relevant for 2×2 or 1×2 table data).

append logical to specify whether the data frame specified via the data argument (if one has been specified) should be returned together with the long format data (the default is TRUE).

var.names optional vector with variable names (length depends on the data type). If unspecified, the function sets appropriate variable names by default.

Details

The escalc function describes a wide variety of effect sizes or outcome measures that can be computed for a meta-analysis. The summary data used to compute those measures are typically contained in vectors, each element corresponding to a study. The to.long function takes this information and constructs a long format dataset from these data.

For example, in various fields (such as the health and medical sciences), the response variable measured is often dichotomous (binary), so that the data from a study comparing two different groups can be expressed in terms of a 2×2 table, such as:

<table>
<thead>
<tr>
<th></th>
<th>outcome 1</th>
<th>outcome 2</th>
<th>total</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>ai</td>
<td>bi</td>
<td>n1i</td>
</tr>
<tr>
<td>group 2</td>
<td>ci</td>
<td>di</td>
<td>n2i</td>
</tr>
</tbody>
</table>

where ai, bi, ci, and di denote the cell frequencies (i.e., the number of people falling into a particular category) and n1i and n2i the row totals (i.e., the group sizes).

The cell frequencies in k such 2×2 tables can be specified via the ai, bi, ci, and di arguments (or alternatively, via the ai, ci, n1i, and n2i arguments). The function then creates the corresponding long format dataset. The measure argument should then be set equal to one of the outcome measures that can be computed based on this type of data, such as "RR", "OR", "RD" (it is not relevant which specific measure is chosen, as long as it corresponds to the specified summary data). See the documentation of the escalc function for more details on the types of data formats available.

The long format for data of this type consists of two rows per study, a factor indicating the study (default name study), a dummy variable indicating the group (default name group, coded as 1 and 2), and two variables indicating the number of individuals experiencing outcome 1 or outcome 2 (default names out1 and out2). Alternatively, if vlong=TRUE, then the long format consists of four rows per study, a factor indicating the study (default name study), a dummy variable indicating the group (default name group, coded as 1 and 2), a dummy variable indicating the outcome (default name outcome, coded as 1 and 2), and a variable indicating the frequency of the respective outcome (default name freq).

The default variable names can be changed via the var.names argument (must be of the appropriate
length, depending on the data type).
The examples below illustrate the use of this function.

Value

A data frame with either \( k \), \( 2 \times k \), or \( 4 \times k \) rows and an appropriate number of columns (depending on the data type) with the data in long format. If append=TRUE and a data frame was specified via the data argument, then the data in long format are appended to the original data frame (with rows repeated an appropriate number of times).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

escalc for a function to compute observed effect sizes or outcomes (and corresponding sampling variances) based on similar inputs.
to.table for a function to turn similar inputs into tabular form.

Examples

```r
### convert data to long format
dat <- to.long(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)
dat

### extra long format
dat <- to.long(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, vlong=TRUE)
dat

### convert data to long format
dat <- to.long(measure="IRR", x1i=x1i, x2i=x2i, t1i=t1i, t2i=t2i,
data=dat.hart1999, var.names=c("id", "group", "events", "ptime"))
dat

### convert data to long format
dat <- to.long(measure="MD", m1i=m1i, sd1i=sd1i, n1i=n1i,
m2i=m2i, sd2i=sd2i, n2i=n2i, data=dat.normand1999,
var.names=c("id", "group", "mean", "sd", "n"))
dat
```
**to.table**  
*Convert Data from Vector to Table Format*

**Description**

The function converts summary data in vector format to the corresponding table format.

**Usage**

```r
to.table(measure, ai, bi, ci, di, n1i, n2i, x1i, x2i, t1i, t2i,
         m1i, m2i, sd1i, sd2i, xi, mi, ri, ti, sdi, ni, data, slab, subset,
         add=1/2, to="none", drop00=FALSE, rows, cols)
```

**Arguments**

- `measure`: a character string to specify the effect size or outcome measure corresponding to the summary data supplied. See ‘Details’ and the documentation of the `escalc` function for possible options.
- `ai`: vector to specify the $2 \times 2$ table frequencies (upper left cell).
- `bi`: vector to specify the $2 \times 2$ table frequencies (upper right cell).
- `ci`: vector to specify the $2 \times 2$ table frequencies (lower left cell).
- `di`: vector to specify the $2 \times 2$ table frequencies (lower right cell).
- `n1i`: vector to specify the group sizes or row totals (first group/row).
- `n2i`: vector to specify the group sizes or row totals (second group/row).
- `x1i`: vector to specify the number of events (first group).
- `x2i`: vector to specify the number of events (second group).
- `t1i`: vector to specify the total person-times (first group).
- `t2i`: vector to specify the total person-times (second group).
- `m1i`: vector to specify the means (first group or time point).
- `m2i`: vector to specify the means (second group or time point).
- `sd1i`: vector to specify the standard deviations (first group or time point).
- `sd2i`: vector to specify the standard deviations (second group or time point).
- `xi`: vector to specify the frequencies of the event of interest.
- `mi`: vector to specify the frequencies of the complement of the event of interest or the group means.
- `ri`: vector to specify the raw correlation coefficients.
- `ti`: vector to specify the total person-times.
- `sdi`: vector to specify the standard deviations.
- `ni`: vector to specify the sample/group sizes.
- `data`: optional data frame containing the variables given to the arguments above.
The `to.table` function describes a wide variety of effect sizes or outcome measures that can be computed for a meta-analysis. The summary data used to compute those measures are typically contained in vectors, each element corresponding to a study. The `to.table` function takes this information and constructs an array of $k$ tables from these data.

For example, in various fields (such as the health and medical sciences), the response variable measured is often dichotomous (binary), so that the data from a study comparing two different groups can be expressed in terms of a $2 \times 2$ table, such as:

```
<table>
<thead>
<tr>
<th></th>
<th>outcome 1</th>
<th>outcome 2</th>
<th>total</th>
</tr>
</thead>
<tbody>
<tr>
<td>group 1</td>
<td>ai</td>
<td>bi</td>
<td>n1i</td>
</tr>
<tr>
<td>group 2</td>
<td>ci</td>
<td>di</td>
<td>n2i</td>
</tr>
</tbody>
</table>
```

where $ai$, $bi$, $ci$, and $di$ denote the cell frequencies (i.e., the number of people falling into a particular category) and $n1i$ and $n2i$ the row totals (i.e., the group sizes).

The cell frequencies in $k$ such $2 \times 2$ tables can be specified via the $ai$, $bi$, $ci$, and $di$ arguments (or alternatively, via the $ai$, $ci$, $n1i$, and $n2i$ arguments). The function then creates the corresponding $2 \times 2 \times k$ array of tables. The `measure` argument should then be set equal to one of the outcome measures that can be computed based on this type of data, such as "RR", "OR", "RD" (it is not relevant which specific measure is chosen, as long as it corresponds to the specified summary data). See the documentation of the `escalc` function for more details on the types of data formats available.

The examples below illustrate the use of this function.

**Value**

An array with $k$ elements each consisting of either 1 or 2 rows and an appropriate number of columns.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

**References**

See Also

`escalc` for a function to compute observed effect sizes or outcomes (and corresponding sampling variances) based on similar inputs.

`to.long` for a function to turn similar inputs into a long format dataset.

Examples

```r
### create tables
dat <- to.table(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg,
data=dat.bcg, slab=paste(author, year, sep=" ", 
rows=c("Vaccinated", "Not Vaccinated"), cols=c("TB+", "TB-"))
dat

### create tables
dat <- to.table(measure="IRR", x1i=x1i, x2i=x2i, t1i=t1i, t2i=t2i,
data=dat.hart1999, slab=paste(study, year, sep=" ", 
rows=c("Warfarin Group", "Placebo/Control Group"))
dat

### create tables
dat <- to.table(measure="MD", m1i=m1i, sd1i=sd1i, n1i=n1i,
m2i=m2i, sd2i=sd2i, n2i=n2i, data=dat.normand1999, 
slab=source, rows=c("Specialized Care", "Routine Care"))
dat
```

to.wide

Convert Data from a Long to a Wide Format

Description

The function converts data given in long format to a wide format.

Usage

```r
to.wide(data, study, grp, ref, grpvars, postfix=c(".1",".2"),
        addid=TRUE, addcomp=TRUE, adddesign=TRUE, minlen=2,
        var.names=c("id","comp","design"))
```

Arguments

data a data frame in long format.

study either the name (given as a character string) or the position (given as a single number) of the study variable in the data frame.

grp either the name (given as a character string) or the position (given as a single number) of the group variable in the data frame.

ref optional character string to specify the reference group (must be one of the groups in the group variable). If not given, the most frequently occurring group is used as the reference group.
to.wide

grpvars

postfix

addid

addcomp

adddesign

minlen

var.names

Details

A meta-analytic dataset may be structured in a ‘long’ format, where each row in the dataset corresponds to a particular study group (e.g., treatment arm). Using this function, such a dataset can be restructured into a ‘wide’ format, where each group within a study is contrasted against a particular reference group.

The study and group arguments are used to specify the study and group variables in the dataset (either as character strings or as numbers indicating the column positions of these variables in the dataset). Optional argument ref is used to specify the reference group (this must be one of the groups in the group variable). Argument grpvars is used to specify (either as a character vector or by giving the column positions) of those variables in the dataset that correspond to group-level outcomes (the remaining variables are treated as study-level outcomes).

The dataset is restructured so that a two-group study will yield a single row in the restructured dataset, contrasting the first group against the second/reference group. For studies with more than two groups (often called ‘multiarm’ or ‘multitreatment’ studies in the medical literature), the reference group is repeated as many times as needed (so a three-group study would yield two rows in the restructured dataset, contrasting two groups against a common reference group).

If a study does not include the reference group, then another group from the study will be used as the reference group. This group is chosen based on the factor levels of the grp variable (i.e., the last level that occurs in the study becomes the reference group).

To distinguish the names of the group-level outcome variables for the two first and second group in the restructured dataset, the strings given for the postfix argument are placed after the respective variable names.

If requested, row id, comparison id, and design id variables are added to the restructured dataset. The row id is simply a unique number for each row in the dataset. The comparison id variable indicates which two groups have been compared against each other. The design id variable indicates which groups were included in a particular study. The group names are shortened for the comparison and design variables (to at least minlen; the actual length might be longer to ensure uniqueness of the group names).

The examples below illustrate the use of this function.
Value

A data frame with rows contrasting groups against a reference group and an appropriate number of columns (depending on the number of group-level outcome variables).

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

`contrmat` for a function to construct a contrast matrix based on a dataset in wide format.


Examples

```r
### data in long format
dat <- dat.senn2013
dat <- dat[c(1,4,3,2,5,6)]
dat

### restructure to wide format
dat <- to.wide(dat, study="study", grp="treatment", ref="placebo", grpvars=4:6)
dat

### data in long format
dat <- dat.hasselblad1998
dat

### restructure to wide format
dat <- to.wide(dat, study="study", grp="trt", ref="no_contact", grpvars=6:7)
dat
```

---

**transf**

Transformation Functions

**Description**

A set of transformation functions useful for meta-analyses.
Usage

transf.rtoz(xi, ...)
transf.ztor(xi, ...)
transf.logit(xi, ...)
transf.ilogit(xi, ...)
transf.arcsin(xi, ...)
transf.iarcsin(xi, ...)
transf.pft(xi, ni, ...)
transf.ipft(xi, ni, ...)
transf.ipft.hm(xi, targs, ...)
transf.isqrt(xi, ...)
transf.irft(xi, ti, ...)
transf.iirft(xi, ti, ...)
transf.ahw(xi, ...)
transf.iahw(xi, ...)
transf.abt(xi, ...)
transf.iabt(xi, ...)
transf.ztor.int(xi, targs, ...)
transf.exp.int(xi, targs, ...)
transf.ilogit.int(xi, targs, ...)
transf.dtou1(xi, ...)
transf.dtou2(xi, ...)
transf.dtou3(xi, ...)
transf.dtorpb(xi, n1i, n2i, ...)
transf.dtobesd(xi, ...)
transf.dtomd(xi, targs, ...)
transf.logortord(xi, pc, ...)
transf.logortorr(xi, pc, ...)

Arguments

xi vector of values to be transformed.
ni vector of sample sizes.
n1i vector of sample sizes for the first group.
n2i vector of sample sizes for the second group.
ti vector of person-times at risk.
pc control group risk (either a single value or a vector).
targs list with additional arguments for the transformation function. See ‘Details’.
... other arguments.

Details

The following transformation functions are currently implemented:

- transf.rtoz: Fisher’s r-to-z transformation for correlation coefficients (same as atanh(x)).
- transf.ztor: inverse of Fisher’s r-to-z transformation (i.e., the z-to-r transformation; same as tanh(x)).
• **transf.logit**: logit (log odds) transformation for proportions (same as \texttt{qlogis(x)}).
• **transf.ilogit**: inverse of the logit transformation (same as \texttt{plogis(x)}).
• **transf.arcsin**: arcsine square root transformation for proportions.
• **transf.iarcsin**: inverse of the arcsine transformation.
• **transf.pft**: Freeman-Tukey (double arcsine) transformation for proportions. See Freeman & Tukey (1950). The \texttt{xi} argument is used to specify the proportions and the \texttt{ni} argument the corresponding sample sizes.
• **transf.ipft**: inverse of the Freeman-Tukey (double arcsine) transformation for proportions. See Miller (1978).
• **transf.ipft.hm**: inverse of the Freeman-Tukey (double arcsine) transformation for proportions using the harmonic mean of the sample sizes for the back-transformation. See Miller (1978). The sample sizes are specified via the \texttt{targs} argument (the list element should be called \texttt{ni}).
• **transf.isqrt**: inverse of the square root transformation (i.e., function to square a number).
• **transf.irft**: Freeman-Tukey transformation for incidence rates. See Freeman & Tukey (1950). The \texttt{xi} argument is used to specify the incidence rates and the \texttt{ti} argument the corresponding person-times at risk.
• **transf.iirft**: inverse of the Freeman-Tukey transformation for incidence rates.
• **transf.ahw**: transformation of coefficient alpha as suggested by Hakstian & Whalen (1976), except that \(1-(1-\alpha)^{1/3}\) is used (so that the transformed values are a monotonically increasing function of the \(\alpha\) values).
• **transf.iahw**: inverse of the transformation of coefficient alpha as suggested by Hakstian & Whalen (1976).
• **transf.abt**: transformation of coefficient alpha as suggested by Bonett (2002), except that \(-\ln(1-\alpha)\) is used (so that the transformed values are a monotonically increasing function of the \(\alpha\) values).
• **transf.iabt**: inverse of the transformation of coefficient alpha as suggested by Bonett (2002).
• **transf.ztor.int**: integral transformation method for the z-to-r transformation.
• **transf.exp.int**: integral transformation method for the exponential transformation.
• **transf.ilogit.int**: integral transformation method for the inverse of the logit transformation.
• **transf.dtou1**: transformation of standardized mean differences to Cohen’s \(U_1\) values (Cohen, 1988). Under the assumption that the data for those in the first (say, treated) and second (say, control) group are normally distributed with equal variances but potentially different means, Cohen’s \(U_1\) indicates the proportion of non-overlap between the two distributions (i.e., when \(d = 0\), then \(U_1\) is equal to 0, which goes to 1 as \(d\) increases).
• **transf.dtou2**: transformation of standardized mean differences to Cohen’s \(U_2\) values (Cohen, 1988). Under the same assumptions as above, Cohen’s \(U_2\) indicates the proportion in the first group that exceeds the same proportion in the second group (i.e., when \(d = 0\), then \(U_2\) is equal to 0.5, which goes to 1 as \(d\) increases).
• **transf.dtou3**: transformation of standardized mean differences to Cohen’s \(U_3\) values (Cohen, 1988). Under the same assumptions as above, Cohen’s \(U_3\) indicates the proportion of individuals in the first group that have a higher value than the mean of those in the second group (i.e., when \(d = 0\), then \(U_3\) is equal to 0.5, which goes to 1 as \(d\) increases).
transf

• **transf.dtocles**: transformation of standardized mean differences to common language effect size (CLES) values (McGraw & Wong, 1992) (also called the probability of superiority). A CLES value indicates the probability that a randomly sampled individual from the first group has a higher value than a randomly sampled individual from the second group (i.e., when $d = 0$, then the CLES is equal to 0.5, which goes to 1 as $d$ increases).

• **transf.dtorpb**: transformation of standardized mean differences to point-biserial correlations. If $n_1i$ and $n_2i$ are not specified, the function assumes $n_1i = n_2i$ and uses the approximate formula $r_{pb} = \frac{d}{\sqrt{d^2 + 1}}$. If $n_1i$ and $n_2i$ are specified, uses the exact transformation formula $r_{pb} = \frac{d}{\sqrt{d^2 + h}}$, where $h = \frac{m}{n_1} + \frac{m}{n_2}$ and $m = n_1 + n_2 - 2$.

• **transf.dtobesd**: transformation of standardized mean differences to binomial effect size display values (Rosenthal & Rubin, 1982). Note that the function only provides the proportion in the first group scoring above the median (the proportion in the second group scoring above the median is simply one minus the proportion in the first group scoring above the median).

• **transf.dtomd**: transformation of standardized mean differences to mean differences given a known standard deviation, which must be specified via the `targs` argument.

• **transf.logortord**: transformation of log odds ratios to risk differences, assuming a particular value for the control group risk (which needs to be specified via the `pc` argument).

• **transf.logortorr**: transformation of log odds ratios to risk ratios, assuming a particular value for the control group risk (which needs to be specified via the `pc` argument).

**Value**

A vector with the transformed values.

**Note**

The integral transformation method for a transformation function $h(z)$ is given by

$$\int_{\text{lower}}^{\text{upper}} h(z)f(z)dz$$

using the limits `targs$lower` and `targs$upper`, where $f(z)$ is the density of a normal distribution with mean equal to $xi$ and variance equal to `targs$tau2`. An example is provided below.

**Author(s)**

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

**References**


Trim and Fill Analysis for 'rma.uni' Objects

Description

Carry out a trim and fill analysis for objects of class "rma.uni".

Usage

trimfill(x, ...)

## S3 method for class 'rma.uni'
trimfill(x, side, estimator="L0", maxiter=100, verbose=FALSE, ilim, ...)
trimfill

Arguments

x an object of class "rma.uni".
side optional character string (either "left" or "right") to specify on which side of the funnel plot the missing studies should be imputed. If left unspecified, the side is chosen within the function depending on the results of Egger’s regression test (see regtest for details on this test).
estimator character string (either "L0", "R0", or "Q0") to specify the estimator to use for estimating the number of missing studies (the default is "L0").
maxiter integer to specify the maximum number of iterations to use for the trim and fill method (the default is 100).
verbose logical to specify whether output should be generated on the progress of the iterative algorithm used as part of the trim and fill method (the default is FALSE).
ilim limits for the imputed values. If unspecified, no limits are used.
... other arguments.

Details

The trim and fill method is a nonparametric (rank-based) data augmentation technique proposed by Duval and Tweedie (2000a, 2000b; see also Duval, 2005). The method can be used to estimate the number of studies missing from a meta-analysis due to suppression of the most extreme results on one side of the funnel plot. The method then augments the observed data so that the funnel plot is more symmetric and recomputes the summary estimate based on the complete data. The trim and fill method can only be used in the context of an equal- or a random-effects model (i.e., in models without moderators). The method should not be regarded as a way of yielding a more ‘valid’ estimate of the overall effect or outcome, but as a way of examining the sensitivity of the results to one particular selection mechanism (i.e., one particular form of publication bias).

Value

An object of class c("rma.uni.trimfill","rma.uni","rma"). The object is a list containing the same components as objects created by rma.uni, except that the data are augmented by the trim and fill method. The following components are also added:
k0 estimated number of missing studies.
side either "left" or "right", indicating on which side of the funnel plot the missing studies (if any) were imputed.
se.k0 standard error of k0.
p.k0 p-value for the test of H0: no missing studies on the chosen side (only when estimator="R0"; NA otherwise).
yi the observed effect sizes or outcomes plus the augmented values (if there are any).
vi the corresponding sampling variances
fill a logical vector indicating which of the values in yi are the observed (FALSE) and the augmented (TRUE) data.

The results of the fitted model after the data augmentation are printed with the print function. Calling funnel on the object provides a funnel plot of the observed and augmented data.
Note

Three different estimators for the number of missing studies were proposed by Duval and Tweedie (2000a, 2000b). Based on these articles and Duval (2005), "R0" and "L0" are recommended. An advantage of estimator "R0" is that it provides a test of the null hypothesis that the number of missing studies (on the chosen side) is zero.

If the outcome measure used for the analysis is bounded (e.g., correlations are bounded between -1 and +1, proportions are bounded between 0 and 1), one can use the ilim argument to enforce those limits when imputing values (imputed values cannot exceed those bounds then).

The model used during the trim and fill procedure is the same as used by the original model object. Hence, if an equal-effects model is passed to the function, then an equal-effects model is also used during the trim and fill procedure and the results provided are also based on an equal-effects model. This would be an ‘equal-equal’ approach. Similarly, if a random-effects model is passed to the function, then the same model is used as part of the trim and fill procedure and for the final analysis. This would be a ‘random-random’ approach. However, one can also easily fit a different model for the final analysis than was used for the trim and fill procedure. See ‘Examples’ for an illustration of an ‘equal-random’ approach.

Author(s)

Wolfgang Viechtbauer <wvb@metafor-project.org> https://www.metafor-project.org

References


See Also

funnel.rma for a function to create funnel plots of the observed and augmented data.
ranktest for the rank test, regtest for the regression test, tes for the test of excess significance, and selmodel for selection models.

Examples

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### meta-analysis of the log risk ratios using an equal-effects model
res <- rma(yi, vi, data=dat, method="EE")
res.tf <- trimfill(res)
res.tf
funnel(res.tf, legend=TRUE, cex=1.2)

### estimator "R0" also provides test
res.tf <- trimfill(res, estimator="R0")
res.tf

### meta-analysis of the log risk ratios using a random-effects model
res <- rma(yi, vi, data=dat)
res.tf <- trimfill(res)
res.tf
funnel(res.tf, legend=TRUE, cex=1.2)

### the examples above are equal-equal and random-random approaches

### illustration of an equal-random approach
res <- rma(yi, vi, data=dat, method="EE")
res.tf <- trimfill(res)
filled <- data.frame(yi = res.tf$yi, vi = res.tf$vi, fill = res.tf$fill)
filled
rma(yi, vi, data=filled)

---

**update.rma**

**Model Updating for 'rma' Objects**

**Description**

The function can be used to update and (by default) re-fit "rma" models. It does this by extracting the call stored in the object, updating the call and (by default) evaluating that call.

**Usage**

```r
## S3 method for class 'rma'
update(object, formula., ..., evaluate=TRUE)
```

**Arguments**

- `object` an object of class "rma".
- `formula.` changes to the formula. See ‘Details’.
- `...` additional arguments to the call, or arguments with changed values.
- `evaluate` logical to specify whether to evaluate the new call or just return the call.

**Details**

For objects of class "rma.uni", "rma.glmm", and "rma.mv", the formula. argument can be used to update the set of moderators included in the model (see ‘Examples’).
Value

If `evaluate=TRUE` the fitted object, otherwise the updated call.

Author(s)

The present function is based on `update.default`, with changes made by Wolfgang Viechtbauer (<wvb@metafor-project.org>) so that the formula updating works with the (somewhat non-standard) interface of the `rma.uni`, `rma.glmm`, and `rma.mv` functions.

References


See Also

`rma.uni`, `rma.mh`, `rma.peto`, `rma.glmm`, and `rma.mv` for functions to fit models which can be updated/re-fit.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit random-effects model (method="REML" is default)
res <- rma(yi, vi, data=dat, digits=3)
res

### fit mixed-effects model with two moderators (absolute latitude and publication year)
res <- update(res, ~ ablat + year)
res

### remove 'year' moderator
res <- update(res, ~ . - year)
res

### fit model with ML estimation
update(res, method="ML")

### example with rma.glmm()
res <- rma.glmm(measure="OR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg, digits=3)
res <- update(res, mods = ~ ablat)
res

### fit conditional model with approximate likelihood
update(res, model="CM.AL")
```
Construct or Approximate the Variance-Covariance Matrix of Dependent Effect Sizes or Outcomes

**Description**

The function can be used to construct or approximate the variance-covariance matrix of dependent effect sizes or outcomes, or more precisely, of their sampling errors (i.e., the V matrix in `rma.mv`).

**Usage**

```r
vcalc(vi, cluster, subgroup, obs, type, time1, time2, grp1, grp2, w1, w2, data, rho, phi, rvars, checkpd=TRUE, nearpd=FALSE, ...)
```

**Arguments**

- `vi` numeric vector to specify the sampling variances of the observed effect sizes or outcomes.
- `cluster` vector to specify the clustering variable (e.g., study).
- `subgroup` optional vector to specify different (independent) subgroups within clusters.
- `obs` optional vector to distinguish different observed effect sizes or outcomes corresponding to the same construct or response/dependent variable.
- `type` optional vector to distinguish different types of constructs or response/dependent variables underlying the observed effect sizes or outcomes.
- `time1` optional numeric vector to specify the time points when the observed effect sizes or outcomes were obtained (in the first condition if the observed effect sizes or outcomes represent contrasts between two conditions).
- `time2` optional numeric vector to specify the time points when the observed effect sizes or outcomes were obtained in the second condition (only relevant when the observed effect sizes or outcomes represent contrasts between two conditions).
- `grp1` optional vector to specify the group of the first condition when the observed effect sizes or outcomes represent contrasts between two conditions.
- `grp2` optional vector to specify the group of the second condition when the observed effect sizes or outcomes represent contrasts between two conditions.
- `w1` optional numeric vector to specify the size of the group (or more generally, the inverse-sampling variance weight) of the first condition when the observed effect sizes or outcomes represent contrasts between two conditions.
- `w2` optional numeric vector to specify the size of the group (or more generally, the inverse-sampling variance weight) of the second condition when the observed effect sizes or outcomes represent contrasts between two conditions.
- `data` optional data frame containing the variables given to the arguments above.
- `rho` argument to specify the correlation(s) of observed effect sizes or outcomes measured concurrently. See ‘Details’.
- `phi` argument to specify the correlation(s) of observed effect sizes or outcomes measured concurrently. See ‘Details’.
- `rvars` argument to specify the correlation(s) of observed effect sizes or outcomes measured concurrently. See ‘Details’.
- `checkpd` logical argument indicating whether to check for positive definiteness.
- `nearpd` logical argument indicating whether to attempt to find a positive definite matrix near the input matrix.
- `...` additional arguments passed to other functions.
phi argument to specify the autocorrelation of observed effect sizes or outcomes measured at different time points. See ‘Details’.

rvars optional argument for specifying the variables that correspond to the correlation matrices of the studies (if this is specified, all arguments above except for cluster and subgroup are ignored). See ‘Details’.

checkpd logical to specify whether to check that the variance-covariance matrices within clusters are positive definite (the default is TRUE). See ‘Note’.

nearpd logical to specify whether the nearPD function from the Matrix package should be used on variance-covariance matrices that are not positive definite. See ‘Note’.

... other arguments.

Details

Standard meta-analytic models (such as those that can be fitted with the rma.uni function) assume that the observed effect sizes or outcomes (or more precisely, their sampling errors) are independent. This assumption is typically violated whenever multiple observed effect sizes or outcomes are computed based on the same sample of subjects (or whatever the study units are) or if there is at least partial overlap of subjects that contribute information to the computation of multiple effect sizes or outcomes.

The present function can be used to construct or approximate the variance-covariance matrix of the sampling errors of dependent effect sizes or outcomes for a wide variety of circumstances (this variance-covariance matrix is the so-called $V$ matrix that may be needed as input for multilevel/multivariate meta-analytic models as can be fitted with the rma.mv function; see also here for some recommendations on a general workflow for meta-analyses involving complex dependency structures).

Argument cluster is used to specify the clustering variable. Rows with the same value of this variable are allowed to be dependent, while rows with different values are assumed to be independent. Typically, cluster will be a study identifier.

Within the same cluster, there may be different subgroups with no overlap of subjects across subgroups. Argument subgroup can be used to distinguish such subgroups. Rows with the same value of this variable within a cluster are allowed to be dependent, while rows with different values are assumed to be independent even if they come from the same cluster. Therefore, from hereon, ‘cluster’ really refers to the combination of cluster and subgroup.

Multiple effect sizes or outcomes belonging to the same cluster may be dependent due to a variety of reasons:

1. The same construct of interest (e.g., severity of depression) may have been measured using different scales or instruments within a study (e.g., using the Beck Depression Inventory (BDI) and the Hamilton Depression Rating Scale (HDRS)) based on which multiple effect sizes can be computed for the same group of subjects (e.g., contrasting a treatment versus a control group with respect to each scale). In this case, we have multiple effect sizes that are different ‘observations’ of the effect with respect to the same type of construct.

Argument obs is then used to distinguish different effect sizes corresponding to the same construct. If obs is specified, then argument rho must also be specified to indicate the degree of correlation among the sampling errors of the different effect sizes. Since this correlation is
typically not known, the correlation among the various scales (or a rough ‘guestimate’ thereof) can be used as a proxy (i.e., the (typical) correlation between BDI and HDRS measurements). One can also specify an entire correlation matrix via \( \rho \) to indicate, for each possible pair of \( \text{obs} \) values, the corresponding correlation. The row/column names of the matrix must then correspond to the unique values of the \( \text{obs} \) variable.

2. Multiple types of constructs (or more generally, types of response/dependent variables) may have been measured in the same group of subjects (e.g., severity of depression as measured with the Beck Depression Inventory (BDI) and severity of anxiety as measured with the State-Trait Anxiety Inventory (STAI)). If this is of interest for a meta-analysis, effect sizes can then be computed with respect to each ‘type’ of construct.

Argument \( \text{type} \) is then used to distinguish effect sizes corresponding to these different types of constructs. If \( \text{type} \) is specified, then argument \( \rho \) must also be specified to indicate the degree of correlation among the sampling errors of effect sizes belonging to these different types. As above, the correlation among the various scales is typically used here as a proxy (i.e., the (typical) correlation between BDI and STAI measurements).

One can also specify an entire correlation matrix via \( \rho \) to indicate, for each possible pair of \( \text{type} \) values, the corresponding correlation. The row/column names of the matrix must then correspond to the unique values of the \( \text{type} \) variable.

3. If there are multiple types of constructs, multiple scales or instruments may also have been used (in at least some of the studies) to measure the same construct and hence there may again be multiple effect sizes that are ‘observations’ of the same type of construct. Arguments \( \text{type} \) and \( \text{obs} \) should then be used together to indicate the various construct types and observations thereof. In this case, argument \( \rho \) must be a vector of two values, the first to specify the within-construct correlation and the second to specify the between-construct correlation.

One can also specify a list with two elements for \( \rho \), the first element being either a scalar or an entire correlation matrix for the within-construct correlation(s) and the second element being a scalar or an entire correlation matrix for the between-construct correlation(s). As above, any matrices specified must have row/column names corresponding to the unique values of the \( \text{obs} \) and/or \( \text{type} \) variables.

4. The same construct and scale may have been assessed/used multiple times, allowing the computation of multiple effect sizes for the same group of subjects at different time points (e.g., right after the end of a treatment, at a short-term follow-up, and at a long-term follow-up). Argument \( \text{time1} \) is then used to specify the time points when the observed effect sizes were obtained. Argument \( \phi \) must then also be specified to indicate the autocorrelation among the sampling errors of two effect sizes that differ by one unit on the \( \text{time1} \) variable. As above, the autocorrelation of the measurements themselves can be used here as a proxy.

If multiple constructs and/or multiple scales have also been assessed at the various time points, then arguments \( \text{type} \) and/or \( \text{obs} \) (together with argument \( \rho \)) should be used as needed to differentiate effect sizes corresponding to the different constructs and/or scales.

5. Many effect sizes or outcome measures (e.g., raw or standardized mean differences, log-transformed ratios of means, log risk/odds ratios and risk differences) reflect the difference between two conditions (i.e., a contrast). Within a study, there may be more than two conditions, allowing the computation of multiple such contrasts (e.g., treatment A versus a control condition and treatment B versus the same control condition) and hence corresponding effect sizes. The reuse of information from the ‘shared’ condition (in this example, the control condition) then induces correlation among the effect sizes.
To account for this, arguments `grp1` and `grp2` should be specified to indicate (within each cluster) which two groups were compared in the computation of each effect size (e.g., in the example above, the coding could be `grp1 = c(1,2)` and `grp2 = c(3,3)`; whether numbers or strings are used as identifiers is irrelevant).

The degree of correlation between two contrast-type effect sizes that is induced by the use of a shared condition is a function of the size of the groups involved in the computation of the two effect sizes (or, more generally, the inverse-sampling variance weights of the condition-specific outcomes). By default, the group sizes (weights) are assumed to be identical across conditions, which implies a correlation of 0.5. If the group sizes (weights) are known, they can be specified via arguments `w1` and `w2` (in which case this information is used by the function to calculate a more accurate estimate of the correlation induced by the shared condition).

In fact, a contrast-type effect size can be based on a between- or a within-subjects design. When at least one or more of the contrast-type effect sizes are based on a within-subjects design, then `time1` and `time2` should be used in combination with `grp1` and `grp2` to indicate for each effect size the group(s) and time point(s) involved.

For example, `grp1 = c(1,2)` and `grp2 = c(3,3)` as above in combination with `time1 = c(1,1)` and `time2 = c(1,1)` would imply a between-subjects design involving three groups where two effect sizes were computed contrasting groups 1 and 2 versus group 3 at a single time point. On the other hand, `grp1 = c(1,1)` and `grp2 = c(1,1)` in combination with `time1 = c(2,1)` and `time2 = c(3,1)` would imply a within-subjects design where two effect sizes were computed contrasting time points 2 and 3 versus time point 1 in a single group. Argument `phi` is then used as above to indicate the autocorrelation of the measurements within groups (i.e., for the within-subjects design above, it would be the autocorrelation between time points 2 and 1 or equivalently, between time points 3 and 2).

All of the arguments above can be specified together to account for a fairly wide variety of dependency types.

**Using the rvars Argument:**

The function also provides an alternative approach for constructing the variance-covariance matrix using the `rvars` argument. Here, one must specify the names of the variables in the dataset that correspond to the correlation matrices of the studies (the variables should be specified as a vector; e.g., `c(var1, var2, var3)`).

In particular, let $k_i$ denote the number of rows corresponding to the $i$th cluster. Then the values of the first $k_i$ variables from `rvars` are used to construct the correlation matrix and, together with the sampling variances (specified via `v1`), the variance-covariance matrix. Say there are three studies, the first with two correlated estimates, the second with a single estimate, and the third with four correlated estimates. Then the data structure should look like this:

```
study yi vi r1 r2 r3 r4
-------------------------------
 1 . . 1 NA NA NA
 1 . . 6 1 NA NA
-------------------------------
 2 . . 1 NA NA NA
-------------------------------
 3 . . 1 NA NA NA
 3 . . 8 1 NA NA
 3 . . .5 .5 1 NA
```
with \texttt{rvars = c(r1, r2, r3, r4)}. If the \texttt{rvars} variables are a consecutive set in the data frame (as above), then one can use the shorthand notation \texttt{rvars = c(r1:r4)}, so \texttt{r1} denotes the first and \texttt{r4} the last variable in the set. Note that only the lower triangular part of the submatrices defined by the \texttt{rvars} variables is used.

There must be as many variables specified via \texttt{rvars} as the number of rows in the largest cluster (in smaller clusters, the non-relevant variables can just be set to \texttt{NA}; see above).

**Value**

A $k \times k$ variance-covariance matrix, where $k$ denotes the length of the \texttt{vi} variable (i.e., the number of rows in the dataset).

**Note**

Depending on the data structure, the specified variables, and the specified values for \texttt{rho} and/or \texttt{phi}, it is possible that the constructed variance-covariance matrix is not positive definite within one or more clusters (this is checked when \texttt{checkpd=TRUE}, which is the default). If such non-positive definite submatrices are found, the reasons for this should be carefully checked since this might indicate misapplication of the function and/or the specification of implausible values for \texttt{rho} and/or \texttt{phi}.

When setting \texttt{nearpd=TRUE}, the \texttt{nearPD} function from the \texttt{Matrix} package is used on variance-covariance submatrices that are not positive definite. This should only be used cautiously and after understanding why these matrices are not positive definite.

**Author(s)**

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**References**


**See Also**

\texttt{escalc} for a function to compute the observed effect sizes or outcomes (and corresponding sampling variances) for which a variance-covariance matrix could be constructed.

\texttt{rcalc} for a function to construct the variance-covariance matrix of dependent correlation coefficients.

\texttt{rma.mv} for a model fitting function that can be used to meta-analyze dependent effect sizes or outcomes.
Examples

########################################################################
### see help(dat.assink2016) for further details on this dataset

dat <- dat.assink2016
head(dat, 9)

### assume that the effect sizes within studies are correlated with rho=0.6
V <- vcalc(vi, cluster=study, obs=esid, data=dat, rho=0.6)

### show part of V matrix for studies 1 and 2
round(V[dat$study %in% c(1,2), dat$study %in% c(1,2)], 4)

### or show as list of matrices
blsplit(V, dat$study, round, 4)[1:2]

### use a correlation of 0.7 for effect sizes corresponding to the same type of
delinquent behavior and a correlation of 0.5 for effect sizes corresponding
### to different types of delinquent behavior
V <- vcalc(vi, cluster=study, type=deltype, obs=esid, data=dat, rho=c(0.7, 0.5))
blsplit(V, dat$study, round, 3)[16]

### examine the correlation matrix for study 16
blsplit(V, dat$study, cov2cor)[16]

########################################################################
### see help(dat.ishak2007) for further details on this dataset

dat <- dat.ishak2007
head(dat, 5)

### create long format dataset
dat <- reshape(dat, direction="long", idvar="study", v.names=c("yi","vi"),
varying=list(c(2,4,6,8), c(3,5,7,9)))
dat <- dat[order(study, time),]

### remove missing measurement occasions from dat
dat <- dat[!is.na(yi),]
rownames(dat) <- NULL

### show the data for the first 5 studies
head(dat, 8)

### construct the full (block diagonal) V matrix with an AR(1) structure
### assuming an autocorrelation of 0.97 as estimated by Ishak et al. (2007)
V <- vcalc(vi, cluster=study, time1=time, phi=0.97, data=dat)
V[1:8, 1:8]
cov2cor(V[1:8, 1:8])

### or show as a list of matrices
blsplit(V, dat$study)[1:5]
blsplit(V, dat$study, cov2cor)[1:5]

############################################################################
### see help(dat.kalaian1996) for further details on this dataset

dat <- dat.kalaian1996
head(dat, 12)

### construct the variance-covariance matrix assuming rho = 0.66 for effect sizes
### corresponding to the 'verbal' and 'math' outcome types
V <- vcalc(vi, cluster=study, type=outcome, data=dat, rho=0.66)
round(V[1:12,1:12], 4)

############################################################################
### see help(dat.berkey1998) for further details on this dataset

dat <- dat.berkey1998

### variables v1i and v2i correspond to the 2x2 var-cov matrices of the studies;
### so use these variables to construct the V matrix (note: since v1i and v2i are
### var-cov matrices and not correlation matrices, set vi=1 for all rows)
V <- vcalc(vi=1, cluster=author, rvars=c(v1i, v2i), data=dat)
V
round(cov2cor(V), 2)

### or show as a list of matrices
blsplit(V, dat$author, function(x) round(cov2cor(x), 2))

### construct the variance-covariance matrix assuming rho = 0.4 for effect sizes
### corresponding to the 'PD' and 'AL' outcome types
V <- vcalc(vi=vi, cluster=trial, type=outcome, data=dat, rho=0.4)
round(V,4)
cov2cor(V)

############################################################################
### see help(dat.knapp2017) for further details on this dataset

dat <- dat.knapp2017

data[-c(1:2)]

dat$task.diff <- unlist(lapply(split(dat, dat$study), function(x) {
  task.int <- as.integer(factor(x$task))
  diff.int <- as.integer(factor(x$difficulty))
  diff.int[is.na(diff.int)] <- 1
  paste0(task.int, ".", diff.int))})

### construct correlation matrix for two tasks with four different difficulties where the
### correlation is 0.4 for different difficulties of the same task, 0.7 for the same
### difficulty of different tasks, and 0.28 for different difficulties of different tasks

```r
R <- matrix(0.4, nrow=8, ncol=8)
R[5:8,1:4] <- R[1:4,5:8] <- 0.28
diag(R[1:4,5:8]) <- 0.7
diag(R[5:8,1:4]) <- 0.7
diag(R) <- 1
rownames(R) <- colnames(R) <- paste0(rep(1:2, each=4), ".", 1:4)
R
```

### construct an approximate V matrix accounting for the use of shared groups and
### for correlations among tasks/difficulties as specified in the R matrix above

```r
V <- vcalc(vi, cluster=study, grp1=group1, grp2=group2, w1=n_sz, w2=n_hc,
obs=task.diff, rho=R, data=dat)
Vs <- blsplit(V, dat$study)
cov2cor(Vs[[3]])  # study with multiple SZ groups and a single HC group
cov2cor(Vs[[6]])  # study with two task types and multiple difficulties
```

---

**vcov.rma**  
*Extract Various Types of Variance-Covariance Matrices from 'rma' Objects*

### Description

The function extracts various types of variance-covariance matrices from objects of class "rma". By default, the variance-covariance matrix of the parameter estimates (fixed effects) is returned.

### Usage

```r
## S3 method for class 'rma'
vcov(object, type="fixed", ...)  
```

### Arguments

- **object**: an object of class "rma".
- **type**: character string to specify the type of variance-covariance matrix to return: type="fixed" returns the variance-covariance matrix of the fixed effects (the default), type="obs" returns the marginal variance-covariance matrix of the observed effect sizes or outcomes, type="fitted" returns the variance-covariance matrix of the fitted values, type="resid" returns the variance-covariance matrix of the residuals.
- **...**: other arguments.
Details

Note that type="obs" currently only works for object of class "rma.uni" and "rma.mv".

For objects of class "rma.uni", the marginal variance-covariance matrix of the observed effect sizes or outcomes is just a diagonal matrix with \( \hat{\tau}^2 + v_i \) along the diagonal, where \( \hat{\tau}^2 \) is the estimated amount of (residual) heterogeneity (set to 0 in equal-effects models) and \( v_i \) is the sampling variance of the \( i \)th study.

For objects of class "rma.mv", the structure can be more complex and depends on the random effects included in the model.

Value

A matrix corresponding to the requested variance-covariance matrix.

Author(s)

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References


See Also

rma.uni, rma.mh, rma.peto, rma.glmm, and rma.mv for functions to fit models for which the various types of variance-covariance matrices can be extracted.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### var-cov matrix of the fixed effects (i.e., the model coefficients)
vcov(res)

### marginal var-cov matrix of the observed log risk ratios
round(vcov(res, type="obs"), 3)

### var-cov matrix of the fitted values
round(vcov(res, type="fitted"), 3)

### var-cov matrix of the residuals
round(vcov(res, type="resid"), 3)
```
vec2mat

**Convert a Vector into a Square Matrix**

**Description**

Function to convert a vector into a square matrix by filling up the lower triangular part of the matrix.

**Usage**

```r
vec2mat(x, diag=FALSE, corr=!diag, dimnames)
```

**Arguments**

- `x` a vector of the correct length.
- `diag` logical to specify whether the vector also contains the diagonal values of the lower triangular part of the matrix (the default is `FALSE`).
- `corr` logical to specify whether the diagonal of the matrix should be replaced with 1’s (the default is to do this when `diag=FALSE`).
- `dimnames` optional vector of the correct length with the dimension names of the matrix.

**Details**

The values in `x` are filled into the lower triangular part of a square matrix with the appropriate dimensions (which are determined based on the length of `x`). If `diag=TRUE`, then `x` is assumed to also contain the diagonal values of the lower triangular part of the matrix. If `corr=TRUE`, then the diagonal of the matrix is replaced with 1’s.

**Value**

A matrix.

**Author(s)**

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**Examples**

```r
vec2mat(1:6, corr=FALSE)
vec2mat(seq(0.2, 0.7, by=0.1), corr=TRUE)
vec2mat(1:10, diag=TRUE)
vec2mat(1:6, corr=FALSE, dimnames=c("A","B","C","D"))
```
Description

Compute (generalized) variance inflation factors (VIFs) for objects of class "rma".

Usage

vif(x, ...)

## S3 method for class 'rma'
vif(x, btt, att, table=FALSE, reestimate=FALSE, sim=FALSE, progbar=TRUE,
seed=NULL, parallel="no", ncpus=1, cl, digits, ...)

## S3 method for class 'vif.rma'
print(x, digits=x$digits, ...)

Arguments

x an object of class "rma" (for vif) or "vif.rma" (for print).

btt optional vector of indices (or list thereof) to specify a set of coefficients for
which a generalized variance inflation factor (GVIF) should be computed. Can
also be a string to grep for.

att optional vector of indices (or list thereof) to specify a set of scale coefficients
for which a generalized variance inflation factor (GVIF) should be computed.
Can also be a string to grep for. Only relevant for location-scale models (see
rma.uni).

table logical to specify whether the VIFs should be added to the model coefficient
table (the default is FALSE). Only relevant when btt (or att) is not specified.

reestimate logical to specify whether the model should be reestimated when removing mod-
erator variables from the model for computing a (G)VIF (the default is FALSE).

sim logical to specify whether the distribution of each (G)VIF under independence
should be simulated (the default is FALSE). Can also be an integer to specify how
many values to simulate (when sim=TRUE, the default is 1000).

progbar logical to specify whether a progress bar should be shown when sim=TRUE (the
default is TRUE).

seed optional value to specify the seed of the random number generator when sim=TRUE
(for reproducibility).

parallel character string to specify whether parallel processing should be used (the de-
fault is "no"). For parallel processing, set to either "snow" or "multicore". See ‘Note’.

ncpus integer to specify the number of processes to use in the parallel processing.
optional cluster to use if `parallel=\"snow\"`. If unspecified, a cluster on the local machine is created for the duration of the call.

digits
optional integer to specify the number of decimal places to which the printed results should be rounded. If unspecified, the default is to take the value from the object.

... other arguments.

Details

The function computes (generalized) variance inflation factors (VIFs) for meta-regression models. Hence, the model specified via argument `x` must include moderator variables (and more than one for this to be useful, as the VIF for a model with a single moderator variable will always be equal to 1).

**VIFs for Individual Coefficients:**

By default (i.e., if `btt` is not specified), VIFs are computed for the individual model coefficients. Let \( b_j \) denote the estimate of the \( j \)th model coefficient of a particular meta-regression model and \( \text{Var}[b_j] \) its variance (i.e., the corresponding diagonal element from the matrix obtained with the `vcov` function). Moreover, let \( b'_j \) denote the estimate of the same model coefficient if the other moderator variables in the model had not been included in the model and \( \text{Var}[b'_j] \) the corresponding variance. Then the VIF for the model coefficient is given by

\[
\text{VIF}[b_j] = \frac{\text{Var}[b_j]}{\text{Var}[b'_j]},
\]

which indicates the inflation in the variance of the estimated model coefficient due to potential collinearity of the \( j \)th moderator variable with the other moderator variables in the model. Taking the square root of a VIF gives the corresponding standard error inflation factor (SIF).

**GVIFs for Sets of Coefficients:**

If the model includes factors (coded in terms of multiple dummy variables) or other sets of moderator variables that belong together (e.g., for polynomials or cubic splines), one may want to examine how much the variance in all of the coefficients in the set is jointly impacted by collinearity with the other moderator variables in the model. For this, we can compute a generalized variance inflation factor (GVIF) (Fox & Monette, 1992) by setting the `btt` argument equal to the indices of those coefficients for which the GVIF should be computed. The square root of a GVIF indicates the inflation in the confidence ellipse/(hyper)ellipsoid for the set of coefficients corresponding to the set due to collinearity. However, to make this value more directly comparable to SIFs (based on single coefficients), the function computes the generalized standard error inflation factor (GSIF) by raising the GVIF to the power of \( 1/(2m) \) (where \( m \) denotes the number of coefficients in the set). One can also specify a list of indices/strings, in which case GVIFs/GSIFs of all list elements will be computed. See ‘Examples’.

For location-scale models fitted with the `rma.uni` function, one can use the `att` argument in an analogous manner to specify the indices of the scale coefficients for which a GVIF should be computed.

**Re-Estimating the Model:**

The way the VIF is typically computed for a particular model coefficient (or a set thereof for a GVIF) makes use of some clever linear algebra to avoid having to re-estimate the model when
removing the other moderator variables from the model. This speeds up the computations considerably. However, this assumes that the other moderator variables do not impact other aspects of the model, in particular the amount of residual heterogeneity (or, more generally, any variance/correlation components in a more complex model, such as those that can be fitted with the rma.mv function).

For a more accurate (but slower) computation of each (G)VIF, one can set reestimate=TRUE, in which case the model is refitted to account for the impact that removal of the other moderator variables has on all aspects of the model. Note that refitting may fail, in which case the corresponding (G)VIF will be missing.

**Interpreting the Size of (G)VIFs:**

A large VIF value suggests that the precision with which we can estimate a particular model coefficient (or a set thereof for a GVIF) is negatively impacted by multicollinearity among the moderator variables. However, there is no specific cutoff for determining whether a particular (G)VIF is ‘large’. Sometimes, values such as 5 or 10 have been suggested as rules of thumb, but such cutoffs are essentially arbitrary.

**Simulating the Distribution of (G)VIFs Under Independence:**

As a more principled approach, we can simulate the distribution of a particular (G)VIF under independence and then examine how extreme the actually observed (G)VIF value is under this distribution. The distribution is simulated by randomly reshuffling the columns of the model matrix (to break any dependence between the moderators) and recomputing the (G)VIF. When setting sim=TRUE, this is done 1000 times (but one can also set sim to an integer to indicate how many (G)VIF values should be simulated).

The way the model matrix is reshuffled depends on how the model was fitted. When the model was specified as a formula via the mods argument and the data was supplied via the data argument, then each column of the data frame specified via data is reshuffled and the formula is evaluated within the reshuffled data (creating the corresponding reshuffled model matrix). This way, factor/character variables are properly reshuffled and derived terms (e.g., interactions, polynomials, splines) are correctly constructed. This is the recommended approach.

On the other hand, if the model matrix was directly supplied to the mods argument, then each column of the matrix is directly reshuffled. This is not recommended, since this approach cannot account for any inherent relationships between variables in the model matrix (e.g., an interaction term is the product of two variables and should not be reshuffled by itself).

Once the distribution of a (G)VIF under independence has been simulated, the proportion of simulated values that are smaller than the actually observed (G)VIF value is computed. If the proportion is close to 1, then this indicates that the actually observed (G)VIF value is extreme.

The general principle underlying the simulation approach is the same as that underlying Horn’s parallel analysis (1965) for determining the number of components / factors to keep in a principal component / factor analysis.

**Value**

An object of class "vif.rma". The object is a list containing the following components:

- **vif**: a list of data frames with the (G)VIFs and (G)SIFs and some additional information.
- **vifs**: a vector with just the (G)VIFs.
table the model coefficient table (only when table=TRUE).
sim a matrix with the simulated (G)VIF values (only when sim=TRUE).
prop vector with the proportions of simulated values that are smaller than the actually observed (G)VIF values (only when sim=TRUE).
... some additional elements/values.

When x was a location-scale model object and (G)VIFs can be computed for both the location and the scale coefficients, then the object is a list with elements beta and alpha, where each element is an "vif.rma" object as described above.

The results are formatted and printed with the print function. To format the results as a data frame, one can use the as.data.frame function. When sim=TRUE, the distribution of each (G)VIF can be plotted with the plot function.

Note

When using sim=TRUE, the model needs to be refitted (by default) 1000 times. When sim=TRUE is combined with reestimate=TRUE, then this value needs to be multiplied by the total number of (G)VIF values that are computed by the function. Hence, the combination of sim=TRUE with reestimate=TRUE is computationally expensive, especially for more complex models where model fitting can be slow.

On machines with multiple cores, one can try to speed things up by delegating the model fitting to separate worker processes, that is, by setting parallel="snow" or parallel="multicore" and ncpus to some value larger than 1. Parallel processing makes use of the parallel package, using the makePSOCKcluster and parLapply functions when parallel="snow" or using mclapply when parallel="multicore" (the latter only works on Unix/Linux-alikes). With parallel::detectCores(), one can check on the number of available cores on the local machine.

Author(s)

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References


See Also

*rma.uni*, *rma.glmm*, and *rma.mv* for functions to fit models for which variance inflation factors can be computed.

*plot.vif.rma* for the plot method and *as.data.frame.vif.rma* for the method to format the results as a data frame.

Examples

```r
### copy data from Bangert-Drowns et al. (2004) into 'dat'
dat <- dat.bangertdrowns2004

### fit mixed-effects meta-regression model
res <- rma(yi, vi, mods = ~ length + wic + feedback + info + pers + imag + meta, data=dat)

### get variance inflation factors
vif(res)

### use the simulation approach to analyze the size of the VIFs
## Not run:
vif(res, sim=TRUE)
## End(Not run)

### get variance inflation factors using the re-estimation approach
vif(res, reestimate=TRUE)

### show that VIFs are not influenced by scaling of the predictors
u <- scale # to standardize the predictors
res <- rma(yi, vi, mods = ~ u(length) + u(wic) + u(feedback) + u(info) + u(pers) + u(imag) + u(meta), data=dat)
vif(res, reestimate=TRUE)

### get full table
vif(res, reestimate=TRUE, table=TRUE)

### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit meta-regression model where one predictor (alloc) is a three-level factor
res <- rma(yi, vi, mods = ~ ablat + alloc + year, data=dat)

### get variance inflation factors for all individual coefficients
vif(res, table=TRUE)

### generalized variance inflation factor for the 'alloc' factor
vif(res, btt=3:4)

### can also specify a string to grep for
vif(res, btt="alloc")

### can also specify a list for the 'btt' argument (and use the simulation approach)
```
weights.rma

## Not run:
vif(res, btt=list(2,3:4,5), sim=TRUE)
## End(Not run)

weights.rma          Compute Weights for 'rma' Objects

Description

The function computes the weights given to the observed effect sizes or outcomes during the model fitting for objects of class "rma.uni", "rma.mh", "rma.peto", and "rma.mv".

Usage

## S3 method for class 'rma.uni'
weights(object, type="diagonal", ...)

## S3 method for class 'rma.mh'
weights(object, type="diagonal", ...)

## S3 method for class 'rma.peto'
weights(object, type="diagonal", ...)

## S3 method for class 'rma.glmm'
weights(object, ...)

## S3 method for class 'rma.mv'
weights(object, type="diagonal", ...)

Arguments

object       an object of class "rma.uni", "rma.mh", "rma.peto", or "rma.mv". The method is not yet implemented for objects of class "rma.glmm".

type         character string to specify whether to return only the diagonal of the weight matrix ("diagonal") or the entire weight matrix ("matrix"). For "rma.mv", this can also be "rowsum" for 'row-sum weights' (for intercept-only models).

...           other arguments.

Value

Either a vector with the diagonal elements of the weight matrix or the entire weight matrix. When only the diagonal elements are returned, they are given in % (and they add up to 100%).

When the entire weight matrix is requested, this is always a diagonal matrix for objects of class "rma.uni", "rma.mh", "rma.peto".

For "rma.mv", the structure of the weight matrix depends on the model fitted (i.e., the random effects included and the variance-covariance matrix of the sampling errors) but is often more complex and not just diagonal.

For intercept-only "rma.mv" models, one can also take the sum over the rows in the weight matrix, which are actually the weights assigned to the observed effect sizes or outcomes when estimating the model intercept. These weights can be obtained with type="rowsum" (as with type="diagonal", they are also given in %). See here for a discussion of this.
weights.rma

Author(s)

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References


See Also

*rma.uni*, *rma.mh*, *rma.peto*, and *rma.mv* for functions to fit models for which model fitting weights can be extracted.

*influence.rma.uni* and *influence.rma.mv* for other model diagnostics.

Examples

```r
### calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg)

### fit mixed-effects model with absolute latitude and publication year as moderators
res <- rma(yi, vi, mods = ~ ablat + year, data=dat)

### extract the model fitting weights (in %)
weights(res)

### extract the weight matrix
round(weights(res, type="matrix"), 4)
```
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