Package ‘mpt’

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Title Multinomial Processing Tree Models
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Imports graphics, utils
Description Fitting and testing multinomial processing tree (MPT) models, a
class of nonlinear models for categorical data. The parameters are the
link probabilities of a tree-like graph and represent the latent cognitive
processing steps executed to arrive at observable response categories
(Batchelder & Riefer, 1999 <doi:10.3758/bf03210812>; Erdfelder et al., 2009
<doi:10.1027/0044-3409.217.3.108>; Riefer & Batchelder, 1988
<doi:10.1037/0033-295x.95.3.318>).
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Description

Thirty-seven participants performed a city-size paired-comparison task. On each trial, participants indicated which of two cities was more populous. After the paired comparisons, participants were asked for each city if they recognized its name, knew in which country it is, and how many inhabitants it has. The study was designed to be similar to Experiment 6 in Hilbig, Erdfelder, and Pohl (2010).


Usage

data(citysize)

Format

A data frame consisting of six components:

- gender factor. Participant gender.
- age Participant age.
- country Number of cities whose country was correctly identified.
- rt Median response time (in seconds) across paired comparisons.
- instr factor. When none, no additional instructions were given; when recog, participants were instructed to choose the city they recognized whenever possible.
- y a matrix of aggregate response frequencies per participant. The column names indicate each of eight response categories: correct/false responses when both cities were recognized (KC, KF), when both were unrecognized (GC, GF), when only one was recognized and the recognized city was chosen (RC, RF), and when only one was recognized and the unrecognized city was chosen (UF, UC).

Source

Data were collected at the Department of Psychology, University of Tuebingen, in June/July 2016.
References


See Also

mpt.

Examples

data(citysize)

## Fit r-model separately for each instruction type
mpt(mptspec("rmodel"), unname(citysize[citysize$instr == "none", "y"]))
mpt(mptspec("rmodel"), unname(citysize[citysize$instr == "recog", "y"]))

## Test instruction effect on r parameter
city.agg <- aggregate(y ~ instr, citysize, sum)
y <- as.vector(t(city.agg[, -1]))

m1 <- mpt(mptspec("rmodel", .replicates=2), y)
m2 <- mpt(update(m1$spec, .restr=list(r2=r1)), y)
anova(m2, m1)  # more use of RH with recognition instruction

## Plot parameter estimates
dotchart(coef(m1)[c(4, 1:3)], xlim=0:1, labels=c("a", "b", "g", "r"), xlab="Parameter estimate (r-model)", main="Recognition heuristic use by instruction type")
points(coef(m1)[c(8, 5:7)], 1:4, pch=16)
legend(0, 1, c("none", "recognition"), pch=c(1, 16), title="Instruction", bty="n")

logLik.mpt  

Log-Likelihood of an mpt Object

Description

Returns the log-likelihood value of the (joint) multinomial processing tree model represented by object evaluated at the estimated parameters.

Usage

## S3 method for class 'mpt'
logLik(object, ...)
Arguments

object: an object inheriting from class mpt, representing a fitted multinomial processing tree model.

... some methods for this generic require additional arguments. None are used in this method.

Value

The log-likelihood of the model represented by object evaluated at the estimated parameters.

See Also

mpt, logLik.lm, AIC, deviance, nobs.

Examples

m <- mpt(mptspec("SR2"), c(243, 64, 58, 55))  # from Riefer et al. (2002)

logLik(m)
deviance(m)
AIC(m)
AIC(m, k = log(sum(m$y)))  # BIC w/total number of data points
BIC(m)  # BIC using nobs()
nobs(m)  # number of non-redundant response categories
Arguments

- **spec**: an object of class `mptspec`: typically result of a call to `mptspec`. A symbolic description of the model to be fitted. (See Details and Examples.)
- **data**: a data frame consisting at least of one variable that contains the absolute response frequencies. Alternatively, a (named) vector or matrix of frequencies.
- **start**: a vector of starting values for the parameter estimates between zero and one.
- **method**: optimization method. Implemented are `optim(..., method = "BFGS")` and the EM algorithm.
- **treeid**: name of the variable that identifies the processing trees of a joint multinomial model. Alternatively, a vector that identifies each tree.
- **freqvar**: if `data` is a data frame, name of the variable that holds the response frequencies; else ignored.
- **logit**: logical. Parameter estimates on logit or probability scale.
- **optimargs**: a list of arguments passed to the optimization function, either `optim` or `mptEM`.
- **object**: an object of class `mpt`, typically the result of a call to `mpt`.
- **test**: should the p-values of the chi-square distributions be reported?
- **parm, level**: See `confint.default`.
- **newdata**: a vector of response frequencies.
- **type**: predicted frequencies or probabilities.
- **...**: additional arguments passed to other methods.

Details

Multinomial processing tree models (Batchelder & Riefer, 1999; Erdfelder et al., 2009; Riefer & Batchelder, 1988) seek to represent the categorical responses of a group of subjects by a small number of latent (psychological) parameters. These models have a tree-like graph, the links being the parameters, the leaves being the response categories. The path from the root to one of the leaves represents the cognitive processing steps executed to arrive at a given response.

If `data` is a data frame, each row corresponds to one response category. If `data` is a vector or matrix, each element or column corresponds to one response category. The order of response categories and of model equations specified in `mptspec` should match.

Joint (or product) multinomial models consist of more than one processing tree. The `treeid` should uniquely identify each tree.

Per default, parameter estimation is carried out by `optim`’s BFGS method on the logit scale with analytical gradients; it can be switched to `mptEM` which implements the EM algorithm.
Value

An object of class `mpt` containing the following components:

- **coefficients**: a vector of parameter estimates. For extraction, the `coef` function is preferred.
- **loglik**: the log-likelihood of the fitted model.
- **nobs**: the number of nonredundant response categories.
- **fitted**: the fitted response frequencies.
- **goodness.of.fit**: the goodness of fit statistic including the likelihood ratio fitted vs. saturated model (G2), the degrees of freedom, and the p-value of the corresponding chi-square distribution.
- **ntrees**: the number of trees in a joint multinomial model.
- **n**: the total number of observations per tree.
- **y**: the vector of response frequencies.
- **pcat**: the predicted probabilities for each response category.
- **treeid**: a vector that identifies each tree.
- **a, b, c**: structural constants passed to `mptEM`.
- **spec**: the MPT model specification returned by `mptspec`.
- **method**: the optimization method used.
- **optim**: the return value of the optimization function.

References


See Also

`mptEM`, `mptspec`, `simulate.mpt`, `plot.mpt`, `residuals.mpt`, `logLik.mpt`, `vcov.mpt`, `optim`.

Examples

```r
## Storage-retrieval model for pair clustering (Riefer & Batchelder, 1988)
data(retroact)
spec <- mptspec(
c*r,
(1 - c)*u^2,
2*(1 - c)*u*(1 - u),
c*(1 - r) + (1 - c)*(1 - u)^2,
```

---
mptEM

EM Algorithm for Multinomial Processing Tree Models

Description

Applies the EM algorithm to fit a multinomial processing tree model.

Usage

mptEM(theta, data, a, b, c, maxit = 1000, tolerance = 1e-8, stepsize = 1, verbose = FALSE)

Arguments

theta a vector of starting values for the parameter estimates.
data a vector of absolute response frequencies.
a a three-dimensional array representing the model structure.
b a three-dimensional array representing the model structure.
c a matrix of structural constants.
maxit the maximum number of iterations.
tolerance the convergence criterion; the iterations converge when logLik - logLik.old < tolerance.
stepsize the step size defaulting to 1; slightly larger values may speed up convergence, but may also give errors; use with care.
verbose logical indicating if output should be produced for each iteration.
Details

Usually, `mptEM` is automatically called by `mpt`.

A prerequisite for the application of the EM algorithm is that the probabilities of the i-th branch leading to the j-th category take the form

\[ p_{ij}(\Theta) = c_{ij} \prod_{s=1}^{S} \vartheta_s^{a_{ij,s}} (1 - \vartheta_s)^{b_{ij,s}}, \]

where \( \Theta = (\vartheta_s) \) is the parameter vector, \( a_{ij,s} \) and \( b_{ij,s} \) count the occurrences of \( \vartheta_s \) and \( 1 - \vartheta_s \) in a branch, respectively, and \( c_{kj} \) is a nonnegative real number. The branch probabilities sum up to the total probability of a given category, \( p_j = p_{1j} + \ldots + p_{Ij} \). This is the structural restriction of the class of MPT models that can be represented by binary trees. Other model types have to be suitably reparameterized for the algorithm to apply.

See Hu and Batchelder (1994) and Hu (1999) for details on the algorithm.

Value

- `theta`: the vector of parameter estimates.
- `loglik`: the log-likelihood at termination of the algorithm.
- `pcat`: a vector of predicted probabilities for each response category.
- `pbranch`: a vector of predicted branch probabilities.
- `iter`: the number of iterations of the algorithm.

References


See Also

`mpt`.

Examples

```r
## Fit storage-retrieval model to data in Riefer et al. (2002)
mpt(mptspec("SR2"), c(243, 64, 58, 55), method = "EM")
```
Specify a Multinomial Processing Tree (MPT) Model

Description

Returns the specification of an MPT model object for fitting with mpt.

Usage

mptspec(..., .restr = NULL)

## S3 method for class 'mptspec'
update(object, .restr = NULL, ...)

Arguments

... (named) expressions or a character string specifying the model. See Details.
.restr a named list of parameter restrictions. See Details.
object an object of class mptspec.

Details

... is used to symbolically specify the MPT model equations by suitable expressions, for example, they could look like this

\[ r + (1 - r) \times b, (1 - r) \times (1 - b), b, 1 - b \]

where each expression represents the probability of a response in the corresponding category (link probabilities are multiplied, branch probabilities are added). Thus, there usually are as many expressions as response categories.

Joint (or product) multinomial models consist of more than a single processing tree. To identify the trees in such a model, expressions may have optional names. Canonically, these names are of the form \( x.y \), where \( x \) is the tree identifier (\text{treeid}) and \( y \) specifies the response category within a tree.

Alternatively, ... may be a character string identifying one out of a list of prevalent MPT models. Currently implemented are the following models (other models have to be specified by explicit expressions as described above):

2HT: the two-high-threshold model (Snodgrass & Corwin, 1988; see also Broeder & Schuetz, 2009).
PairAsso: the paired-associate learning model (Riefer & Batchelder, 1988).
prospec: the event-based prospective memory model (Smith & Bayen, 2004).
rmodel: the r-model of recognition heuristic use (Hilbig, Erdfelder, & Pohl, 2010).
SR, SR2: the storage-retrieval model for pair clustering (Batchelder & Riefer, 1986). SR2 is the model without singleton items.
WST: the inference-guessing model with relaxed assumptions (Klauer, Stahl, & Erdfelder, 2007) for the Wason selection task.

If one of these models is selected, . . . may include an optional .replicates argument that specifies the number of replicates of the model equations, for example, when the same model is applied repeatedly in several experimental conditions. Accordingly, parameter names are augmented by numbers to make them unique.

Parameter restrictions included in .restr may be of the form \( b = r \) or \( b = 0.5 \) etc. Depending on the fitting algorithm employed in mpt (BFGS, but not EM), mathematical functions are permissible, for example, \( b = \sqrt{r} \).

The update method is used to add parameter restrictions to an existing mptspec object.

**Value**

An object of class mptspec that serves as input to mpt which fits the model to data. It consists of the following components:

- **par2prob**: a function that takes a vector of parameter values and computes the response probabilities.
- **par2deriv**: a function that takes a vector of parameter values and computes first and second derivatives of the model equations.
- **prob**: a list containing expressions of the model equations.
- **deriv**: a list containing expressions of the first and second derivatives of the model equations.
- **par**: a named vector of parameter values.
- **restr**: a list containing expressions of parameter restrictions.
- **treeid**: a vector that identifies each tree.

**References**


See Also

mpt.

Examples

```r
## Specify storage-retrieval model for pairs
spec1 <- mptspec(
  c*r,
  (1 - c)*u^2,
  2*(1 - c)*u*(1 - u),
  c*(1 - r) + (1 - c)*(1 - u)^2
)

## Specify storage-retrieval model with parameter restrictions
spec2 <- mptspec(
  c*r,
  (1 - c)*u^2,
  2*(1 - c)*u*(1 - u),
  c*(1 - r) + (1 - c)*(1 - u)^2,
  .restr = list(c = r/2, u = 0.3)
)

## Optional names identifying trees in joint MPT model
spec3 <- mptspec(
  "1.1" = r + (1 - r)*b,
  "1.2" = (1 - r)*(1 - b),
  "2.1" = b,
  "2.2" = 1 - b
)

## Fit one-high-threshold model to data in Broeder and Schuetz (2009)
m <- mpt(spec <- mptspec("1HT"), c(55, 35, 45, 765))

## Working with the mptspec object
spec$par2prob(c(0.5, 0.1)) # response probabilities
spec$par2deriv(coef(m))$deriv # Jacobian matrix at ML estimate

## See data(package = "mpt") for application examples.
```
plot.mpt

Diagnostic Plot for MPT Models

Description

Plots MPT residuals against fitted values.

Usage

## S3 method for class 'mpt'
plot(x, showNames = TRUE,
     xlab = "Predicted response probabilities", ylab = "Deviance residuals",
     ...) 

## S3 method for class 'mpt'
residuals(object, type = c("deviance", "pearson"), ...) 

Arguments

x, object an object of class mpt, typically the result of a call to mpt.
showNames logical. Should the names of the residuals be plotted? Defaults to TRUE.
xlab, ylab graphical parameters passed to plot.
type the type of residuals which should be returned; the alternatives are: "deviance" (default) and "pearson".
... further arguments passed to or from other methods.

Details

The deviance residuals are plotted against the predicted response probabilities. If showNames is true, plotting symbols are the names of the residuals.

Value

For residuals, a named vector of residuals having as many elements as response categories.

See Also

mpt.residuals.glm.

Examples

## Compare two constrained MPT models
data(proact)

spec <- mptspec(
    p1*q1*r1,
    p1*q1*(1 - r1),
    )
Recall Frequencies for DaPolito’s Experiment on Proactive Inhibition

Description

In DaPolito’s experiment (Greeno, James, DaPolito, & Polson, 1978), 60 subjects were presented with lists of stimulus-response associates to be learned, followed by a test in which only the stimuli were presented and the responses had to be recalled. Stimuli consisted of three-letter syllables, responses of the numbers from 1 to 30, so list items looked like, say, ESI-12, JOK-3, MAL-8, etc. Part of the items had two responses (A-B, A-C), the control items had only a single correct response. If the recall of C responses is poorer than that of control items, then proactive inhibition has occurred, that is interference with the recall by information that has been learned earlier.

Riefer and Batchelder (1988) analyzed only the A-B and A-C items. They investigated how repeated A-B presentation affects the B and C recall, respectively. The responses were classified into four categories and pooled across subjects.

Usage

data(proact)

Format

A data frame consisting of five variables:

test first or second test.
abpres  the number of A-B presentations.
resp  a factor giving the response category; BC both B and C responses are correctly recalled, Bc only B is recalled, bC only C is recalled, bc neither response is recalled.
freq  the aggregate recall frequencies per condition.
treed  an identifier for the single trees of the joint multinomial model.

Source

See Also
mpt.

Examples

```r
data(proact)

## Testing effects of repeated A-B presentations
spec <- mptspec(
  p1*q1*r1,
  p1*q1*(1 - r1),
  p1*(1 - q1)*r1,
  (1 - p1) + p1*(1 - q1)*(1 - r1),

  p2*q2*r2,
  p2*q2*(1 - r2),
  p2*(1 - q2)*r2,
  (1 - p2) + p2*(1 - q2)*(1 - r2),

  p3*q3*r3,
  p3*q3*(1 - r3),
  p3*(1 - q3)*r3,
  (1 - p3) + p3*(1 - q3)*(1 - r3),

  p4*q4*r4,
  p4*q4*(1 - r4),
  p4*(1 - q4)*r4,
  (1 - p4) + p4*(1 - q4)*(1 - r4),

  p5*q5*r5,
  p5*q5*(1 - r5),
  p5*(1 - q5)*r5,
  (1 - p5) + p5*(1 - q5)*(1 - r5),

  p6*q6*r6,
  p6*q6*(1 - r6),
  p6*(1 - q6)*r6,
)```
\[(1 - p6) + p6 \times (1 - q6) \times (1 - r6)\]

\[m1 \leftarrow \text{mpt(spec, proact)}\]
\[m2 \leftarrow \text{mpt(update(spec, .restr=list(q2=q1, q3=q1, q5=q4, q6=q4)), proact)}\]
\[m3 \leftarrow \text{mpt(update(spec, .restr=list(r2=r1, r3=r1, r5=r4, r6=r4)), proact)}\]

anova(m2, m1) # q increases with number of A-B presentations
anova(m3, m1) # r remains constant

---

**prospecMemory**

**Prospective Memory and Task Importance**

**Description**

Smith and Bayen (2004) tested the performance of 64 participants in an event-based prospective memory task that was embedded in a color-matching task. On each trial, participants were presented with four colored rectangles followed by a colored word. Their task was to press a key to indicate whether the color of the word matched one of the rectangles. Interspersed among these nontarget words were six target words for which subjects had to remember to press a special key (prospective memory response) regardless of the color. Participants received two different instruction types either stressing the importance of the color-matching (CMI) or of the prospective-memory task (PMI).

In a replication study, the performance of 72 German-speaking participants was tested; this study was designed to be similar to Experiment 1 in Smith and Bayen (2004).

**Usage**

data(prospecMemory)

**Format**

**PMSmithBayen** A data frame consisting of five variables:

- **instruction** instruction type, either color-matching importance (cmi) or prospective memory importance (pmi).
- **item** a factor specifying one of four item types: either a target word that did or did not match the color of the rectangles, or a nontarget word that did or did not match.
- **resp** a factor giving the response categories: match, nonmatch, or the prospective memory response (prospec).
- **freq** the aggregate response frequencies per condition.
- **treeid** an identifier for the single trees of the joint multinomial model.

**PMreplication** A data frame containing 72 observations on five variables:

- **gender** factor. Participant gender.
- **age** Participant age.
- **instr** factor. Instruction type.
Average response time difference (in milliseconds) between color-matching and prospective-memory task.

A matrix of aggregate response frequencies per participant. The column names indicate each of twelve response categories: match, nonmatch, prospective memory response for targets in matching (tmm, tnn, tmp) or in nonmatching condition (tnm, tnn, tnp), and again for nontargets (nmm, nnn, npm vs. nmm, nnn, nnp).

**Source**


For the replication study, data were collected at the Department of Psychology, University of Tuebingen, between December 2018 and January 2019.

**See Also**

mpt.

**Examples**

```r
## Prospective memory model: identifiability
qr(mptspec("prospec", .restr = list(M1=M, M2=M))$par2deriv(runif(6))$deriv)$rank
qr(mptspec("prospec", .restr = list(M1=M, M2=M, g=.1, c=.5))$par2deriv(runif(4))$deriv)$rank

## Prospective memory model: goodness of fit
data(prospecMemory)
cmi <- PMSmithBayen[PMSmithBayen$instruction == "cmi", ]
m2 <- mpt(mptspec("prospec", .restr = list(M1=M, M2=M, g=.1, c=.5)), cmi)
m1 <- mpt(update(m2$spec, .restr = list(C2=C1)), cmi)
anova(m1, m2)

pmi <- PMSmithBayen[PMSmithBayen$instruction == "pmi", ]
anova(mpt(m1$spec, pmi), mpt(m2$spec, pmi))

## Testing P_cmi = P_pmi and M_cmi = M_pmi

## Smith and Bayen
m2 <- mpt(mptspec("prospec", .replicates = 2, .restr = list(M11=M1, M21=M1, g1=.1, c1=.5, M12=M2, M22=M2, g2=.1, c2=.5)), data = PMSmithBayen)
m1 <- mpt(update(m2$spec, .restr = list(P2=P1)), PMSmithBayen)
m0 <- mpt(update(m2$spec, .restr = list(M2=M1)), PMSmithBayen)
anova(m1, m2)
anova(m0, m2)

## Replication
pm.agg <- aggregate(y ~ instr, PMreplication, sum)
```
y <- as.vector(t(pm.agg[2:1, -1]))

m3 <- mpt(m2$spec, y)
m1 <- mpt(update(m3$spec, .restr = list(P2=P1)), y)
m0 <- mpt(update(m3$spec, .restr = list(M2=M1)), y)
anova(m1, m3)
anova(m0, m3)

par(mfrow = 1:2)
dotchart(coef(m2)[c("C12", "C22", "P2", "M2")], xlim=0:1, xlab="",
  labels=c("C1", "C2", "P", "M"), main="Smith and Bayen (2004, Exp. 1)")
points(coef(m2)[c("C11", "C21", "P1", "M1")], 1:4, pch=16)
legend("bottomleft", c("CMI", "PMI"), pch=c(1, 16), title="Instruction",
  title.adj=1, bty="n")

dotchart(coef(m3)[c("C12", "C22", "P2", "M2")], xlim=0:1, xlab="",
  labels=c("C1", "C2", "P", "M"), main="Replication study")
points(coef(m3)[c("C11", "C21", "P1", "M1")], 1:4, pch=16)

mtext("Parameter estimate (prospective memory model)", side=1,
  line=-2, outer=TRUE)

---

**recogROC**

**Recognition Receiver Operating Characteristics**

**Description**

Broeder and Schuetz (2009) tested the shape of recognition receiver operating characteristics. 75 participants studied 60 words. In a recognition test, 60 words – old and new items mixed – were presented, and participants had to classify them as old or new. The percentage of old items varied in order to manipulate the response bias.

**Usage**

data(recogROC)

**Format**

A data frame consisting of five variables:

- **p.target** percentage of target (old) items.
- **item** factor. Target (old) or distractor (new) item.
- **resp** a factor giving the response category, old or new.
- **freq** the aggregate response frequencies per condition.
- **treeid** an identifier for the single trees of the joint multinomial model.

**Source**

See Also

mpt.

Examples

```r
## Data from Broeder and Schuetz (2009, Table 1, Exp. 1)
data(recogROC)

## Fit the two-high-threshold model with restrictions
m <- mpt(mptspec("2HT", .replicates=5,
  .restr=list(r1=r, r2=r, r3=r, r4=r, r5=r,
    d1=d, d2=d, d3=d, d4=d, d5=d)), recogROC)

summary(m) # Table 2

## Hit rate and false alarm rate
i.hit <- with(recogROC, item == "target" & resp == "old")
i.fa <- with(recogROC, item == "distractor" & resp == "old")

hrfa <- data.frame(
  obshr = (recogROC$freq/m$n)[i.hit],
  obsfa = (recogROC$freq/m$n)[i.fa],
  predhr = m$pcat[i.hit],
  predfa = m$pcat[i.fa]
)

## Plot ROC, Figure 5
plot(obshr ~ obsfa, hrfa, xlim=0:1, ylim=0:1, pch=16,
  main="Broeder and Schuetz (2009)",
  ylab="Hit rate", xlab="False alarm rate")
abline(0, 1)
lines(predhr ~ predfa, hrfa, lty=2)
```

---

**retroact**

*Recall Frequencies in Retroactive Inhibition*

**Description**

Riefer and Batchelder (1988) presented each of 75 participants with either one, two, three, four, or five successive lists of words (15 subjects per group). These words were shown in random order on a computer screen, one word at a time, at a rate of 5 s per word. Each list contained 25 words, consisting of 10 categories (with 2 associate words per category) and five singletons. Subjects were given 1.5 min to recall in writing the 25 words from each individual list. After all of the lists had been presented, a final free-recall test was given in which subjects attempted to recall the words from all of the previous lists. Subjects were given up to 5 min for this final written recall.

The focus here is on the recall of the first-list words during the final recall task. The responses were classified into six categories and pooled across subjects.
Usage

data(retroact)

Format

A data frame consisting of four variables:

- **lists**: the number of interpolated lists.
- **treeid**: an identifier for the single trees of the joint multinomial model.
- **resp**: a factor giving the response category; E1 pair is recalled adjacent, E2 pair is recalled non-adjacent, E3 one word in a pair is recalled, E4 neither word in a pair is recalled, F1 recall of a singleton, F2 non-recall of a singleton.
- **freq**: the aggregate recall frequencies per condition.

Source


See Also

- **mpt**.

Examples

data(retroact)

```r
## Fitting individual storage-retrieval models per condition
spec <- mptspec(
  c*r,
  (1 - c)*u^2,
  2*(1 - c)*u*(1 - u),
  c*(1 - r) + (1 - c)*(1 - u)^2,
  u,
  1 - u
)
pars <- sapply(0:4,
  function(x) coef(mpt(spec, retroact[retroact$lists == x, ])))
## Figure 3 in Riefer & Batchelder (1988)
plot(pars["c", ] ~ I(0:4), pch=16, type="b", ylim=c(.3, 1),
  xlab="Number of interpolated lists, j",
  ylab="Parameter estimate (Storage-retrieval model)",
  main="Riefer and Batchelder (1988)"
)points(pars["r", ] ~ I(0:4), type="b", lty=2)
text(3, .89, expression("Storage of clusters," ~ hat(c)[j]))
text(3, .46, expression("Retrieval of clusters," ~ hat(r)[j]))
## Testing effects of interpolated lists
spec <- mptspec(
```

\begin{verbatim}
c0*r0,
(1 - c0)*u0^2,
2*(1 - c0)*u0*(1 - u0),
c0*(1 - r0) + (1 - c0)*(1 - u0)^2,
u0,
1 - u0,

c1*r1,
(1 - c1)*u1^2,
2*(1 - c1)*u1*(1 - u1),
c1*(1 - r1) + (1 - c1)*(1 - u1)^2,
u1,
1 - u1,

c2*r2,
(1 - c2)*u2^2,
2*(1 - c2)*u2*(1 - u2),
c2*(1 - r2) + (1 - c2)*(1 - u2)^2,
u2,
1 - u2,

c3*r3,
(1 - c3)*u3^2,
2*(1 - c3)*u3*(1 - u3),
c3*(1 - r3) + (1 - c3)*(1 - u3)^2,
u3,
1 - u3,

c4*r4,
(1 - c4)*u4^2,
2*(1 - c4)*u4*(1 - u4),
c4*(1 - r4) + (1 - c4)*(1 - u4)^2,
u4,
1 - u4
)
m1 <- mpt(spec, retroact)
m2 <- mpt(update(spec, .restr=list(r0=r, r1=r, r2=r, r3=r, r4=r)),
retroact)
m3 <- mpt(update(spec, .restr=list(c0=c, c1=c, c2=c, c3=c, c4=c)),
retroact)

anova(m2, m1)  # r decreases the more lists have been interpolated
anova(m3, m1)  # c remains constant
\end{verbatim}

**Description**

In the Wason selection task, a participant is presented with four cards, each one having a letter side and a number side, e.g., A B 3 4. The task is to select the card(s) that have to be turned around
in order to test the rule "If there is an A on the letter side then there is a 3 on the number side." Klauer, Stahl, and Erdfelder (2007) report a series of experiments to test their WST model using the aggregate frequencies of the 16 possible response patterns.

Usage
data(selectiontask)

Format
A data frame consisting of four variables:

- **group** factor. The control group (CG) received standard instructions, the experimental group (EG) got additional helpful hints.
- **pattern** character. Response pattern indicating which card(s) were selected (1) or not selected (0).
- **exp1, exp2** the aggregate response frequencies for Experiment 1 and 2, respectively.

Note
In the original analyses, a constant of one was added to all frequencies.

Source

See Also
mpt.

Examples
data(selectiontask)

```r
## Inference-guessing model with relaxed assumptions
s <- mptspec("WST", .replicates = 2)
m1 <- mpt(s, data = selectiontask$exp1, method = "EM")

## Inference-guessing model
m2 <- mpt(update(s, .restr = list(sf1=s1, sb1=s1, sfb1=s1, 
                   sf2=s2, sb2=s2, sfb2=s2)),
            data = m1$y, method = "EM")

## Effect of hint on i parameter (Exp. 1)
m3 <- mpt(update(m2$spec, .restr = list(i2=i1)),
          data = m1$y,
          method = "EM")

## Independence model
m4 <- mpt(update(m2$spec,
               .restr = list(a1=0, c1=0, x1=0, d1=0, s1=0, i1=0,
               "}
```
simulate.mpt

Simulate Responses from MPT Models

Description

Simulates responses from the distribution corresponding to a fitted mpt model object.

Usage

## S3 method for class 'mpt'
simulate(object, nsim, seed, pool = TRUE, ...)

Arguments

- **object**: an object of class mpt, typically the result of a call to mpt.
- **nsim**, **seed**: currently not used.
- **pool**: logical, if TRUE (default), pooled responses (summed across respondents) are returned.
- **...**: further arguments passed to or from other methods. None are used in this method.
Details

Responses are simulated by (repeatedly) applying \texttt{rmultinom} with sizes taken from the original sample and probabilities computed from the model object.

Value

A named vector of (pooled) responses. Names identify the tree from which responses were simulated.

See Also

\texttt{mpt} \texttt{.rmultinom}.

Examples

data(retroact)

m <- mpt(mptspec(
  c*r,
  (1 - c)*u^2,
  2*(1 - c)*u*(1 - u),
  c*(1 - r) + (1 - c)*(1 - u)^2,
  u,
  1 - u
), retroact[retroact$lists == 1, ])

simulate(m)

## Parametric bootstrap of goodness-of-fit test
LR.stat <- replicate(200, deviance(mpt(m$spec, simulate(m))))

hist(LR.stat, col="lightgray", border="white", freq=FALSE, breaks=20,
  main="Parametric bootstrap")
curve(dchisq(x, df=1), add=TRUE)
abline(v=deviance(m), lty=2)

valence

\textit{World Valence and Source Memory for Vertical Position}

Description

Sixty-four participants studied words with positive, negative, or neutral valence displayed at the top or bottom part of a computer screen. Later, these words were presented intermixed with new words, and participants had to classify them as "top," "bottom," or "new." It was of interest if memory is improved in congruent trials, in which word valence and vertical position match (positive-top, negative-bottom), as opposed to incongruent trials.
Usage
data(valence)

Format
A data frame consisting of five components:

id  factor. Participant ID.
gender  factor. Participant gender.
age  Participant age.
condition  factor. In congruent trials, positive words were presented at the top, negative words at the bottom, and vice versa for incongruent trials.
y  a matrix of aggregate response frequencies per participant and condition. The column names indicate each of nine response categories, for example, top.bottom means that words were presented at the top, but participant responded "bottom."

Source
Data were collected at the Department of Psychology, University of Tuebingen, in 2010.

See Also
mpt.

Examples
data(valence)

## Fit source-monitoring model to subsets of data
spec <- mptspec("SourceMon", .restr=list(d1=d, d2=d))
names(spec$prob) <- colnames(valence$y)

mpt(spec, valence[valence$condition == "congruent" & valence$gender == "female", "y"])
mpt(spec, valence[valence$condition == "incongruent" & valence$gender == "female", "y"])

## Test the congruency effect
val.agg <- aggregate(y ~ gender + condition, valence, sum)
y <- as.vector(t(val.agg[, -(1:2)]))

spec <- mptspec("SourceMon", .replicates=4,
  .restr=list(d11=d1, d21=d1, d12=d2, d22=d2,
  d13=d3, d23=d3, d14=d4, d24=d4))
m1 <- mpt(spec, y)
m2 <- mpt(update(spec, .restr=list(d1=d.f, d3=d.f, d2=d.m, d4=d.m)), y)
anova(m2, m1)  # better discrimination in congruent trials

## Plot parameter estimates
mat <- matrix(coef(m1), 5)
rownames(mat) <- c("D1", "d", "g", "b", "D2")
mat <- mat[c("D1", "D2", "d", "b", "g")]
matplot(mat, type="b", axes=FALSE, ylab="MPT model parameter estimate",
main="Word valence and source monitoring", ylim=0:1, pch=1:4)
axis(1, 1:5, rownames(mat)); axis(2)
legend("bottomleft", c("female, congruent", "male, congruent",
"female, incongruent", "male, incongruent"), pch=1:4, bty="n")

vcov.mpt

Covariance and Information Matrix for MPT Models

Description

Returns the covariance matrix or the Fisher information matrix of a fitted mpt model object.

Usage

## S3 method for class 'mpt'
vcov(object, logit = FALSE, what = c("vcov", "fisher"), ...)

Arguments

object

an object of class mpt, typically the result of a call to mpt.

logit

logical. Switch between logit and probability scale.

what

character. If vcov (default), the covariance matrix is returned; if fisher, the Fisher information matrix is returned.

...

further arguments passed to or from other methods. None are used in this method.

Details

If logit is false, the covariance matrix is based on the observed Fisher information matrix of the ML estimator on the probability scale. This is equivalent to the equations for the covariance matrix given in Hu and Batchelder (1994) and Hu (1999), although the implementation here is different.

If logit is true, the covariance matrix and the estimated information matrix (Elandt-Johnson, 1971) of the ML estimator on the logit scale are obtained by the multivariate delta method (Bishop, Fienberg, and Holland, 1975; Grizzle, Starmer, and Koch, 1969).

Value

A (named) square matrix.
References


See Also

- mpt.

Examples

```r
data(retroact)
m <- mpt(mptspec("SR"), retroact[retroact$lists == 1, ])

vcov(m) # covariance matrix (probability scale)
vcov(m, logit = TRUE) # covariance matrix (logit scale)
vcov(m, what = "fisher") # Fisher information
```
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