Package ‘multcomp’

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Title Simultaneous Inference in General Parametric Models

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Description Simultaneous tests and confidence intervals
for general linear hypotheses in parametric models, including
linear, generalized linear, linear mixed effects, and survival models.
The package includes demos reproducing analyzes presented
in the book ``Multiple Comparisons Using R” (Bretz, Hothorn,

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adevent  Adverse Events Data

Description

Indicators of 28 adverse events in a two-arm clinical trial.

Usage

data(adevent)

Format

A data frame with 160 observations on the following 29 variables.

E1 a factor with levels no event event
E2 a factor with levels no event event
E3 a factor with levels no event event
E4 a factor with levels no event event
E5 a factor with levels no event event
E6 a factor with levels no event event
E7 a factor with levels no event event
The data is provided by Westfall et al. (1999, p. 242) and contains binary indicators of 28 adverse events (E1,..., E28) for two arms (group).

Details

Source

Description

A convenience function for univariate testing via z- and t-tests of estimated model coefficients

Usage

cftest(model, parm, test = univariate(), ...)

Arguments

- `model`: a fitted model.
- `parm`: a vector of parameters to be tested, either a character vector of names or an integer.
- `test`: a function for computing p values, see `summary.glht`.
- `...`: additional arguments passed to `summary.glht`.

Details

The usual z- or t-tests are tested without adjusting for multiplicity.

Value

An object of class `summary.glht`.

See Also

coefftest

Examples

```r
lmod <- lm(dist ~ speed, data = cars)
summary(lmod)
cftest(lmod)
```
cholesterol

Cholesterol Reduction Data Set

Description

Cholesterol reduction for five treatments.

Usage

data("cholesterol")

Format

This data frame contains the following variables

- **trt** treatment groups, a factor at levels 1time, 2times, 4times, drugD and drugE.
- **response** cholesterol reduction.

Details

A clinical study was conducted to assess the effect of three formulations of the same drug on reducing cholesterol. The formulations were 20mg at once (1time), 10mg twice a day (2times), and 5mg four times a day (4times). In addition, two competing drugs were used as control group (drugD and drugE). The purpose of the study was to find which of the formulations, if any, is efficacious and how these formulations compare with the existing drugs.

Source


Examples

```r
### adjusted p-values for all-pairwise comparisons in a one-way layout
### set up ANOVA model
amod <- aov(response ~ trt, data = cholesterol)

### set up multiple comparisons object for all-pair comparisons
cht <- glht(amod, linfct = mcp(trt = "Tukey"))

### cf. Westfall et al. (1999, page 171)
summary(cht, test = univariate())
summary(cht, test = adjusted("Shaffer"))
summary(cht, test = adjusted("Westfall"))

### use only a subset of all pairwise hypotheses
K <- contrMat(table(cholesterol$trt), type="Tukey")
Ksub <- rbind(K[c(1,2,5),],
```
"D - test" = c(-1, -1, -1, 3, 0),
"E - test" = c(-1, -1, -1, 0, 3))

### reproduce results in Westfall et al. (1999, page 172)
### note: the ordering of our estimates here is different
amod <- aov(response ~ trt - 1, data = cholesterol)
summary(glht(amod, linfct = mcp(trt = Ksub[,5:1]),
test = adjusted("Westfall"))

cld

---

Set up a compact letter display of all pair-wise comparisons

### Description

Extract information from glht, summary.glht or confint.glht objects which is required to create and plot compact letter displays of all pair-wise comparisons.

### Usage

```r
## S3 method for class 'summary.glht'
cld(object, level = 0.05, decreasing = FALSE, ...)
## S3 method for class 'glht'
cld(object, level = 0.05, decreasing = FALSE, ...)
## S3 method for class 'confint.glht'
cld(object, decreasing = FALSE, ...)
```

### Arguments

- `object` An object of class glht, summary.glht or confint.glht.
- `level` Significance-level to be used to term a specific pair-wise comparison significant.
- `decreasing` logical. Should the order of the letters be increasing or decreasing?
- `...` additional arguments.

### Details

This function extracts all the information from glht, summary.glht or confint.glht objects that is required to create a compact letter display of all pair-wise comparisons. In case the contrast matrix is not of type "Tukey", an error is issued. In case of confint.glht objects, a pair-wise comparison is termed significant whenever a particular confidence interval contains 0. Otherwise, p-values are compared to the value of "level". Once, this information is extracted, plotting of all pair-wise comparisons can be carried out.
Value

An object of class cld, a list with items:

- **y** Values of the response variable of the original model.
- **yname** Name of the response variable.
- **x** Values of the variable used to compute Tukey contrasts.
- **weights** Weights used in the fitting process.
- **lp** Predictions from the fitted model.
- **covar** A logical indicating whether the fitted model contained covariates.
- **signif** Vector of logicals indicating significant differences with hyphenated names that identify pair-wise comparisons.

References


See Also

- `glht` `plot.cld`

Examples

```r
### multiple comparison procedures
### set up a one-way ANOVA
data(warpbreaks)
amod <- aov(breaks ~ tension, data = warpbreaks)
### specify all pair-wise comparisons among levels of variable "tension"
tuk <- glht(amod, linfct = mcp(tension = "Tukey"))
### extract information
tuk.cld <- cld(tuk)
### use sufficiently large upper margin
old.par <- par(mai=c(1,1,1.25,1), no.readonly = TRUE)
### plot
plot(tuk.cld)
par(old.par)

### now using covariates
data(warpbreaks)
amod2 <- aov(breaks ~ tension + wool, data = warpbreaks)
### specify all pair-wise comparisons among levels of variable "tension"
tuk2 <- glht(amod2, linfct = mcp(tension = "Tukey"))
### extract information
tuk.cld2 <- cld(tuk2)
### use sufficiently large upper margin
old.par <- par(mai=c(1,1,1.25,1), no.readonly = TRUE)
### plot using different colors
plot(tuk.cld2, col=c("black", "red", "blue"))
par(old.par)
```
### set up all pair-wise comparisons for count data
data(Titanic)
mod <- glm(Survived ~ Class, data = as.data.frame(Titanic), weights = Freq, family = binomial())
### specify all pair-wise comparisons among levels of variable "Class"
glht.mod <- glht(mod, mcp(Class = "Tukey"))
### extract information
mod.cld <- cld(glht.mod)
### use sufficiently large upper margin
old.par <- par(mai=c(1,1,1.5,1), no.readonly = TRUE)
### plot
plot(mod.cld)
par(old.par)

---

cml

**Chronic Myelogenous Leukemia survival data.**

**Description**

Survival in a randomised trial comparing three treatments for Chronic Myelogeneous Leukemia (simulated data).

**Usage**

data("cml")

**Format**

A data frame with 507 observations on the following 7 variables.

center  a factor with 54 levels indicating the study center.
treatment a factor with levels trt1, trt2, trt3 indicating the treatment group.
sex   sex (0 = female, 1 = male)
age age in years
riskgroup risk group (0 = low, 1 = medium, 2 = high)
status censoring status (FALSE = censored, TRUE = dead)
time survival or censoring time in days.

**Details**

The data are simulated according to structure of the data by the German CML Study Group used in Hehlmann (1994).

**Source**

Examples

```r
if (require("coxme")) {
  data("cml")
  ### one-sided simultaneous confidence intervals for many-to-one
  ### comparisons of treatment effects concerning time of survival
  ### modeled by a frailty Cox model with adjustment for further
  ### covariates and center-specific random effect.
  cml_coxme <- coxme(Surv(time, status) ~ treatment + sex + age + riskgroup + (1|center),
                     data = cml)
  glht_coxme <- glht(model = cml_coxme, linfct = mcp(treatment = "Dunnett"),
                     alternative = "greater")
  ci_coxme <- confint(glht_coxme)
  exp(ci_coxme$confinf)[1:2,]
}
```

---

**contrMat**

<table>
<thead>
<tr>
<th><strong>Contrast Matrices</strong></th>
</tr>
</thead>
</table>

### Description

Computes contrast matrices for several multiple comparison procedures.

### Usage

```r
ccontrMat(n, type = c("Dunnett", "Tukey", "Sequen", "AVE",
                        "Changepoint", "Williams", "Marcus",
                        "McDermott", "UmbrellaWilliams", "GrandMean"),
            base = 1)
```

### Arguments

- **n**: a (possibly named) vector of sample sizes for each group.
- **type**: type of contrast.
- **base**: an integer specifying which group is considered the baseline group for Dunnett contrasts.

### Details

Computes the requested matrix of contrasts for comparisons of mean levels.

### Value

The matrix of contrasts with appropriate row names is returned.
References


Examples

```r
n <- c(10, 20, 30, 40)
names(n) <- paste("group", 1:4, sep="")
contrMat(n) # Dunnett is default
contrMat(n, base = 2) # use second level as baseline
contrMat(n, type = "Tukey")
contrMat(n, type = "Sequen")
contrMat(n, type = "AVE")
contrMat(n, type = "Changepoint")
contrMat(n, type = "Williams")
contrMat(n, type = "Marcus")
contrMat(n, type = "McDermott")
### Umbrella-protected Williams contrasts, i.e. a sequence of
### Williams-type contrasts with groups of higher order
### stepwise omitted
contrMat(n, type = "UmbrellaWilliams")
### comparison of each group with grand mean of all groups
contrMat(n, type = "GrandMean")
```

detergent

**Detergent Durability Data Set**

Description

Detergent durability in an incomplete two-way design.

Usage

```r
data("detergent")
```

Format

This data frame contains the following variables

- **detergent** detergent, a factor at levels A, B, C, D, and E.
- **block** block, a factor at levels B_1, ..., B_10.
- **plates** response variable: number of plates washed before the foam disappears.
Details

Plates were washed with five detergent varieties, in ten blocks. A complete design would have 50 combinations, here only three detergent varieties in each block were applied in a balanced incomplete block design. Note that there are six observations taken at each detergent level.

Source


Examples

```r
### set up two-way ANOVA without interactions
amod <- aov(plates ~ block + detergent, data = detergent)

### set up all-pair comparisons
dht <- glht(amod, linfct = mcp(detergent = "Tukey"))

### see Westfall et al. (1999, p. 190)
confint(dht)

### see Westfall et al. (1999, p. 192)
summary(dht, test = univariate())
## Not run:
summary(dht, test = adjusted("Shaffer"))
summary(dht, test = adjusted("Westfall"))
## End(Not run)
```

---

### fattyacid

**Fatty Acid Content of Bacillus simplex.**

Description

Fatty acid content of different putative ecotypes of Bacillus simplex.

Usage

data("fattyacid")

Format

A data frame with 93 observations on the following 2 variables.

**PE** a factor with levels PE3, PE4, PE5, PE6, PE7, PE9 indicating the putative ecotype (PE).

**FA** a numeric vector indicating the content of fatty acid (FA).
Details

The data give the fatty acid content for different putative ecotypes of Bacillus simplex. Variances of the values of fatty acid are heterogeneous among the putative ecotypes.

Source


Examples

```r
if (require("sandwich")) {
  data("fattyacid")
  ### all-pairwise comparisons of the means of fatty acid content
  ### FA between different putative ecotypes PE accounting for
  ### heteroscedasticity by using a heteroscedastic consistent
  ### covariance estimation
  amod <- aov(FA ~ PE, data = fattyacid)
  amod_glht <- glht(amod, mcp(PE = "Tukey"), vcov = vcovHC)
  summary(amod_glht)

  ### simultaneous confidence intervals for the differences of
  ### means of fatty acid content between the putative ecotypes
  confint(amod_glht)
}
```

---

**glht**

*General Linear Hypotheses*

**Description**

General linear hypotheses and multiple comparisons for parametric models, including generalized linear models, linear mixed effects models, and survival models.

**Usage**

```r
## S3 method for class 'matrix'
glht(model, linfct,
       alternative = c("two.sided", "less", "greater"),
       rhs = 0, ...)
## S3 method for class 'character'
glht(model, linfct, ...)
## S3 method for class 'expression'
glht(model, linfct, ...)
## S3 method for class 'mcp'
glht(model, linfct, ...)
```
## glht

### S3 method for class 'mlf'

```r
glht(model, linfct, ...)
mcp(..., interaction_average = FALSE, covariate_average = FALSE)
```

### Arguments

- `model` a fitted model, for example an object returned by `lm`, `glm`, or `aov` etc. It is assumed that `coef` and `vcov` methods are available for `model`. For multiple comparisons of means, methods `model.matrix`, `model.frame` and `terms` are expected to be available for `model` as well.
- `linfct` a specification of the linear hypotheses to be tested. Linear functions can be specified by either the matrix of coefficients or by symbolic descriptions of one or more linear hypotheses. Multiple comparisons in AN(C)OVA models are specified by objects returned from function `mcp`.
- `alternative` a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less". You can specify just the initial letter.
- `rhs` an optional numeric vector specifying the right hand side of the hypothesis.
- `interaction_average` logical indicating if comparisons are averaging over interaction terms. Experimental!
- `covariate_average` logical indicating if comparisons are averaging over additional covariates. Experimental!
- `...` additional arguments to function `modelparm` in all `glht` methods. For function `mcp`, multiple comparisons are defined by matrices or symbolic descriptions specifying contrasts of factor levels where the arguments correspond to factor names.

### Details

A general linear hypothesis refers to null hypotheses of the form $H_0 : K\theta = m$ for some parametric model `model` with parameter estimates `coef(model)`.

The null hypothesis is specified by a linear function $K\theta$, the direction of the alternative and the right hand side $m$. Here, `alternative` equal to "two.sided" refers to a null hypothesis $H_0 : K\theta = m$, whereas "less" corresponds to $H_0 : K\theta \geq m$ and "greater" refers to $H_0 : K\theta \leq m$. The right hand side vector $m$ can be defined via the `rhs` argument.

The generic method `glht` dispatches on its second argument (linfct). There are three ways, and thus methods, to specify linear functions to be tested:

1) The matrix of coefficients $K$ can be specified directly via the `linfct` argument. In this case, the number of columns of this matrix needs to correspond to the number of parameters estimated by `model`. It is assumed that appropriate `coef` and `vcov` methods are available for `model` (`modelparm` deals with some exceptions).

2) A symbolic description, either a character or expression vector passed to `glht` via its `linfct` argument, can be used to define the null hypothesis. A symbolic description must be interpretable as a valid R expression consisting of both the left and right hand side of a linear hypothesis. Only the names of `coef(model)` must be used as variable names. The alternative is given by the direction...
under the null hypothesis (= or == refer to "two.sided", <= means "greater" and >= indicates "less"). Numeric vectors of length one are valid values for the right hand side.

3) Multiple comparisons of means are defined by objects of class mcp as returned by the mcp function. For each factor, which is included in model as independent variable, a contrast matrix or a symbolic description of the contrasts can be specified as arguments to mcp. A symbolic description may be a character or expression where the factor levels are only used as variables names. In addition, the type argument to the contrast generating function contrMat may serve as a symbolic description of contrasts as well.

4) The lsm function in package lsmeans offers a symbolic interface for the definition of least-squares means for factor combinations which is very helpful when more complex contrasts are of special interest.

The mcp function must be used with care when defining parameters of interest in two-way ANOVA or ANCOVA models. Here, the definition of treatment differences (such as Tukey’s all-pair comparisons or Dunnett’s comparison with a control) might be problem specific. Because it is impossible to determine the parameters of interest automatically in this case, mcp in multcomp version 1.0-0 and higher generates comparisons for the main effects only, ignoring covariates and interactions (older versions automatically averaged over interaction terms). A warning is given. We refer to Hsu (1996), Chapter 7, and Searle (1971), Chapter 7.3, for further discussions and examples on this issue.

glht extracts the number of degrees of freedom for models of class lm (via modelparm) and the exact multivariate t distribution is evaluated. For all other models, results rely on the normal approximation. Alternatively, the degrees of freedom to be used for the evaluation of multivariate t distributions can be given by the additional df argument to modelparm specified via . . .

glht methods return a specification of the null hypothesis \( H_0 : K\theta = m \). The value of the linear function \( K\theta \) can be extracted using the coef method and the corresponding covariance matrix is available from the vcov method. Various simultaneous and univariate tests and confidence intervals are available from summary.glht and confint.glht methods, respectively.

A more detailed description of the underlying methodology is available from Hothorn et al. (2008) and Bretz et al. (2010).

Value

An object of class glht, more specifically a list with elements

- model a fitted model, used in the call to glht
- linfct the matrix of linear functions
- rhs the vector of right hand side values m
- coef the values of the linear functions
- vcov the covariance matrix of the values of the linear functions
- df optionally, the degrees of freedom when the exact t distribution is used for inference
- alternative a character string specifying the alternative hypothesis
- type optionally, a character string giving the name of the specific procedure

with print, summary, confint, coef and vcov methods being available. When called with linfct being an mcp object, an additional element focus is available storing the names of the factors under test.
References


Examples

```r
### multiple linear model, swiss data
lmod <- lm(Fertility ~ ., data = swiss)

### test of H_0: all regression coefficients are zero
### (ignore intercept)
### define coefficients of linear function directly
K <- diag(length(coef(lmod)))[-1,]
rownames(K) <- names(coef(lmod))[-1]
K

### set up general linear hypothesis
glht(lmod, linfct = K)

### alternatively, use a symbolic description
### instead of a matrix
### describe differences symbolically
### alternatively, define contrast matrix directly
contr <- rbind("M - L" = c(-1, 1, 0),
               "H - L" = c(-1, 0, 1),
               "H - M" = c(1, -2, 1))
```

```r
### multiple comparison procedures
### set up a one-way ANOVA
amod <- aov(breaks ~ tension, data = warpbreaks)

### set up all-pair comparisons for factor 'tension'
### using a symbolic description ('type' argument
### to 'contrMat()')
glht(amod, linfct = mcp(tension = "Tukey"))

### alternatively, describe differences symbolically
### alternatively, define contrast matrix directly
glht(amod, linfct = mcp(tension = c("M - L = 0",
                                 "H - L = 0",
                                 "H - M = 0")))
```
glht-methods

Methods for General Linear Hypotheses

Description
Simultaneous tests and confidence intervals for general linear hypotheses.

Usage

## S3 method for class 'glht'
summary(object, test = adjusted(), ...)
## S3 method for class 'glht'
confint(object, parm, level = 0.95, calpha = adjusted_calpha(), ...)

## S3 method for class 'glht'
coef(object, rhs = FALSE, ...)

## S3 method for class 'glht'
vcov(object, ...)

## S3 method for class 'confint.glht'
plot(x, xlim, xlab, ylim, ...)

## S3 method for class 'glht'
plot(x, ...)

univariate()

adjusted(type = c("single-step", "Shaffer", "Westfall", "free", p.adjust.methods), ...)

Ftest()

ChiSqtest()
adjusted_calpha(...)

univariate_calpha(...)

### Arguments

- **object**: an object of class `glht`.
- **test**: a function for computing p values.
- **parm**: additional parameters, currently ignored.
- **level**: the confidence level required.
- **calpha**: either a function computing the critical value or the critical value itself.
- **rhs**: logical, indicating whether the linear function \( K\hat{\theta} \) or the right hand side \( m \) (rhs = TRUE) of the linear hypothesis should be returned.
- **type**: the multiplicity adjustment (adjusted) to be applied. See below and `p.adjust`.
- **x**: an object of class `glht` or `confint.glht`.
- **xlim**: the x limits \((x1, x2)\) of the plot.
- **ylim**: the y limits of the plot.
- **xlab**: a label for the x axis.
- **...**: additional arguments, such as maxpts, abseps or releps to `pmvnorm` in adjusted or `qmvnorm` in `confint`. Note that additional arguments specified to `summary`, `confint`, `coef` and `vcov` methods are currently ignored.

### Details

The methods for general linear hypotheses as described by objects returned by `glht` can be used to actually test the global null hypothesis, each of the partial hypotheses and for simultaneous confidence intervals for the linear function \( K\hat{\theta} \).

The `coef` and `vcov` methods compute the linear function \( K\hat{\theta} \) and its covariance, respectively.

The `test` argument to `summary` takes a function specifying the type of test to be applied. Classical ChiSq (Wald test) or F statistics for testing the global hypothesis \( H_0 \) are implemented in functions
Chisqtest and Ftest. Several approaches to multiplicity adjusted p values for each of the linear hypotheses are implemented in function adjusted. The type argument to adjusted specifies the method to be applied: "single-step" implements adjusted p values based on the joint normal or t distribution of the linear function, and "Shaffer" and "Westfall" implement logically constraint multiplicity adjustments (Shaffer, 1986; Westfall, 1997). "free" implements multiple testing procedures under free combinations (Westfall et al, 1999). In addition, all adjustment methods implemented in p.adjust are available as well.

Simultaneous confidence intervals for linear functions can be computed using method confint. Univariate confidence intervals can be computed by specifying calpha = univariate_calpha() to confint. The critical value can directly be specified as a scalar to calpha as well. Note that plot(a) for some object a of class glht is equivalent to plot(confint(a)).

All simultaneous inference procedures implemented here control the family-wise error rate (FWER). Multivariate normal and t distributions, the latter one only for models of class lm, are evaluated using the procedures implemented in package mvtnorm. Note that the default procedure is stochastic. Reproducible p-values and confidence intervals require appropriate settings of seeds.
A more detailed description of the underlying methodology is available from Hothorn et al. (2008) and Bretz et al. (2010).

Value

summary computes (adjusted) p values for general linear hypotheses, confint computes (adjusted) confidence intervals. coef returns estimates of the linear function \( K\theta \) and vcov its covariance.

References

Frank Bretz, Torsten Hothorn and Peter Westfall (2010), Multiple Comparisons Using R, CRC Press, Boca Raton.


Examples

```r
### set up a two-way ANOVA
amod <- aov(breaks ~ wool + tension, data = warpbreaks)

### set up all-pair comparisons for factor `tension`
wht <- glht(amod, linfct = mcp(tension = “Tukey”))

### 95% simultaneous confidence intervals
plot(print(confint(wht)))
```
### the same (for balanced designs only)
TukeyHSD(amod, "tension")

### corresponding adjusted p values
summary(wht)

### all means for levels of 'tension'
amod <- aov(breaks ~ tension, data = warpbreaks)
glht(amod, linfct = matrix(c(1, 0, 0,
                              1, 1, 0,
                              1, 0, 1), byrow = TRUE, ncol = 3))

### confidence bands for a simple linear model, 'cars' data
plot(cars, xlab = "Speed (mph)", ylab = "Stopping distance (ft)",
     las = 1)

### fit linear model and add regression line to plot
lmod <- lm(dist ~ speed, data = cars)
abline(lmod)

### a grid of speeds
speeds <- seq(from = min(cars$speed), to = max(cars$speed),
              length = 10)

### linear hypotheses: 10 selected points on the regression line != 0
K <- cbind(1, speeds)

### set up linear hypotheses
cht <- glht(lmod, linfct = K)

### confidence intervals, i.e., confidence bands, and add them plot
cci <- confint(cht)
lines(speeds, cci$confint[,"lwr",] , col = "blue")
lines(speeds, cci$confint[,"upr",] , col = "blue")

### simultaneous p values for parameters in a Cox model
if (require("survival") && require("MASS")) {
  data("leuk", package = "MASS")
  leuk.cox <- coxph(Surv(time) ~ ag + log(wbc), data = leuk)

  ### set up linear hypotheses
  lht <- glht(leuk.cox, linfct = diag(length(coef(leuk.cox))))

  ### adjusted p values
  print(summary(lht))
}

---

**litter**

---

**Litter Weights Data Set**
Description

Dose response of litter weights in rats.

Usage

data("litter")

Format

This data frame contains the following variables

- **dose**: dosages at four levels: 0, 5, 50, 500.
- **gesttime**: gestation time as covariate.
- **number**: number of animals in litter as covariate.
- **weight**: response variable: average post-birth weights in the entire litter.

Details

Pregnant mice were divided into four groups and the compound in four different doses was administered during pregnancy. Their litters were evaluated for birth weights.

Source


Examples

```R
### fit ANCOVA model to data
amod <- aov(weight ~ dose + gesttime + number, data = litter)

### define matrix of linear hypotheses for 'dose'
doselev <- as.integer(levels(litter$dose))
K <- rbind(contrMat(table(litter$dose), "Tukey"),
           otrend = c(-1.5, -0.5, 0.5, 1.5),
           atrend = doselev - mean(doselev),
           ltrend = log(1:4) - mean(log(1:4)))

### set up multiple comparison object
Kht <- glht(amod, linfct = mcp(dose = K), alternative = "less")

### cf. Westfall (1997, Table 2)
summary(Kht, test = univariate())
summary(Kht, test = adjusted("bonferroni"))
summary(Kht, test = adjusted("Shaffer"))
summary(Kht, test = adjusted("Westfall"))
summary(Kht, test = adjusted("single-step"))
```
Calculation of correlation between test statistics from multiple marginal models using the score decomposition

Usage

\texttt{mmm(...)}

\texttt{mlf(...)}

Arguments

\texttt{...} A names argument list containing fitted models (\texttt{mmm}) or definitions of linear functions (\texttt{mlf}). If only one linear function is defined for \texttt{mlf}, it will be applied to all models in \texttt{mmm} by \texttt{glht.mlf}.

Details

Estimated correlations of the estimated parameters of interest from the multiple marginal models are obtained using a stacked version of the i.i.d. decomposition of parameter estimates by means of score components (first derivatives of the log likelihood). The method is less conservative than the Bonferroni correction. The details are provided by Pipper, Ritz and Bisgaard (2012).

The implementation assumes that the model were fitted to the same data, i.e., the rows of the matrices returned by \texttt{estfun} belong to the same observations for each model.

The reference distribution is always multivariate normal, if you want to use the multivariate t, please specify the corresponding degrees of freedom as an additional \texttt{df} argument to \texttt{glht}.

Observations with missing values contribute zero to the score function. Models have to be fitted using \texttt{na.exclude} as \texttt{na.action} argument.

Value

An object of class \texttt{mmm} or \texttt{mlf}, basically a named list of the arguments with a special method for \texttt{glht} being available for the latter. \texttt{vcov}, \texttt{estfun}, and \texttt{bread} methods are available for objects of class \texttt{mmm}.

Author(s)

Code for the computation of the joint covariance and sandwich matrices was contributed by Christian Ritz and Christian B. Pipper.

References

Examples

```r
### replicate analysis of Hasler & Hothorn (2011),
### A Dunnett-Type Procedure for Multiple Endpoints,
### The International Journal of Biostatistics: Vol. 7: Iss. 1, Article 3.
### DOI: 10.2202/1557-4679.1258

### see ?coagulation
if (require("SimComp")) {
  data("coagulation", package = "SimComp")

  ### level "S" is the standard, "H" and "B" are novel procedures
  coagulation$Group <- relevel(coagulation$Group, ref = "S")

  ### fit marginal models
  (m1 <- lm(Thromb.count ~ Group, data = coagulation))
  (m2 <- lm(ADP ~ Group, data = coagulation))
  (m3 <- lm(TRAP ~ Group, data = coagulation))

  ### set-up Dunnett comparisons for H - S and B - S
  ### for all three models
  g <- glht(mmm(Thromb = m1, ADP = m2, TRAP = m3),
            mlf(mcp(Group = "Dunnett")), alternative = "greater")

  ### joint correlation
  cov2cor(vcov(g))

  ### simultaneous p-values adjusted by taking the correlation
  ### between the score contributions into account
  summary(g)

  ### simultaneous confidence intervals
  confint(g)

  ### compare with
  ## Not run:
  library("SimComp")
  SimCiDiff(data = coagulation, grp = "Group",
            resp = c("Thromb.count","ADP","TRAP"),
            type = "Dunnett", alternative = "greater",
            covar.equal = TRUE)

  ## End(Not run)

  ### use sandwich variance matrix
  library("sandwich")
  g <- glht(mmm(Thromb = m1, ADP = m2, TRAP = m3),
            mlf(mcp(Group = "Dunnett")),
            alternative = "greater", vcov = sandwich)

  summary(g)
  confint(g)
}
```
### attitude towards science data

data("mn6.9", package = "TH.data")

### one model for each item

mn6.9.y1 <- glm(y1 ~ group, family = binomial(),
    na.action = na.omit, data = mn6.9)
mn6.9.y2 <- glm(y2 ~ group, family = binomial(),
    na.action = na.omit, data = mn6.9)
mn6.9.y3 <- glm(y3 ~ group, family = binomial(),
    na.action = na.omit, data = mn6.9)
mn6.9.y4 <- glm(y4 ~ group, family = binomial(),
    na.action = na.omit, data = mn6.9)

### test all parameters simultaneously

summary(glht(mmm(mn6.9.y1, mn6.9.y2, mn6.9.y3, mn6.9.y4),
    mlf(diag(2))))

### group differences

summary(glht(mmm(mn6.9.y1, mn6.9.y2, mn6.9.y3, mn6.9.y4),
    mlf("group2 = 0")))

### alternative analysis of Klingenberg & Satopaa (2013),
### Simultaneous Confidence Intervals for Comparing Margins of
### Multivariate Binary Data, CSDA, 64, 87-98
### http://dx.doi.org/10.1016/j.csda.2013.02.016
### see supplementary material for data description

### NOTE: this is not the real data but only a subsample

influenza <- influenza[rep(1:nrow(influenza), influenza$Freq), 1:5]

### Fitting marginal logistic regression models

(head_logreg <- glm(HEADACHE ~ group, data = influenza,
    family = binomial()))

(mala_logreg <- glm(MALAISE ~ group, data = influenza,
    family = binomial()))

(pyre_logreg <- glm(PYREXIA ~ group, data = influenza,
family = binomial())

(arth_logreg <- glm(ARTHRALGIA ~ group, data = influenza,
family = binomial()))

### Simultaneous inference for log-odds
xy.sim <- glht(mmm(head = head_logreg,
     mala = mala_logreg,
     pyre = pyre_logreg,
     arth = arth_logreg),
     mlf("grouptrt = 0"))
summary(xy.sim)
confint(xy.sim)

### Artificial examples
### Combining linear regression and logistic regression
set.seed(29)
y1 <- rnorm(100)
y2 <- factor(y1 + rnorm(100, sd = .1) > 0)
x1 <- gl(4, 25)
x2 <- runif(100, 0, 10)
m1 <- lm(y1 ~ x1 + x2)
m2 <- glm(y2 ~ x1 + x2, family = binomial())
### Note that the same explanatory variables are considered in both models
### but the resulting parameter estimates are on 2 different scales
### (original and log-odds scales)

### Simultaneous inference for the same parameter in the 2 model fits
summary(glht(mmm(m1 = m1, m2 = m2), mlf("x12 = 0")))

### Simultaneous inference for different parameters in the 2 model fits
summary(glht(mmm(m1 = m1, m2 = m2),
      mlf(m1 = "x12 = 0", m2 = "x13 = 0")))

### Simultaneous inference for different and identical parameters in the 2
### model fits
summary(glht(mmm(m1 = m1, m2 = m2),
      mlf(m1 = c("x12 = 0", "x13 = 0"), m2 = "x13 = 0")))

### Examples for binomial data
### Two independent outcomes
y1.1 <- rbinom(100, 1, 0.45)
y1.2 <- rbinom(100, 1, 0.55)
group <- factor(rep(c("A", "B"), 50))
m1 <- glm(y1.1 ~ group, family = binomial)
m2 <- glm(y1.2 ~ group, family = binomial)

summary(glht(mmm(m1 = m1, m2 = m2),
      mlf("groupB = 0")))

### Two perfectly correlated outcomes
y2.1 <- rbinom(100, 1, 0.45)
\[
y_{2.2} \leftarrow y_{2.1} \\
group \leftarrow \text{factor(rep(c("A", "B"), 50))}
\]

\[
m_1 \leftarrow \text{glm}(y_{2.1} \sim \text{group}, \text{family = binomial}) \\
m_2 \leftarrow \text{glm}(y_{2.2} \sim \text{group}, \text{family = binomial})
\]

\[
\text{summary(glht(mmm(m1 = m1, m2 = m2),} \\
\text{mlf("groupB = 0")))}
\]

### use sandwich covariance matrix

\[
\text{summary(glht(mmm(m1 = m1, m2 = m2),} \\
\text{mlf("groupB = 0"), vcov = sandwich))}
\]

drop parameter function for model parameters

**Description**

Extract model parameters and their covariance matrix as well as degrees of freedom (if available) from a fitted model.

**Usage**

\[
\text{modelparm(model, coef., vcov., df, ...)}
\]

**Arguments**

- **model**: a fitted model, for example an object returned by `lm`, `glm`, `aov`, `survreg`, or `lmer` etc.
- **coef.**: an accessor function for the model parameters. Alternatively, the vector of coefficients.
- **vcov.**: an accessor function for the covariance matrix of the model parameters. Alternatively, the covariance matrix directly.
- **df**: an optional specification of the degrees of freedom to be used in subsequent computations.
- **...**: additional arguments, currently ignored.

**Details**

One can’t expect `coef` and `vcov` methods for arbitrary models to return a vector of $p$ fixed effects model parameters (coef) and corresponding $p \times p$ covariance matrix (vcov).

The `coef` and `vcov` arguments can be used to define modified `coef` or `vcov` methods for a specific model. Methods for `lmer` and `survreg` objects are available (internally).

For objects inheriting from class `lm` the degrees of freedom are determined from `model` and the corresponding multivariate t distribution is used by all methods to `glht` objects. By default, the asymptotic multivariate normal distribution is used in all other cases unless `df` is specified by the user.
Value

An object of class `modelparm` with elements

- `coef` model parameters
- `vcov` covariance matrix of model parameters
- `df` degrees of freedom

---

**mtept**  
*Multiple Endpoints Data*

---

Description

Measurements on four endpoints in a two-arm clinical trial.

Usage

`data(mtept)`

Format

A data frame with 111 observations on the following 5 variables.

- `treatment` a factor with levels `Drug` `Placebo`
- `E1` endpoint 1
- `E2` endpoint 2
- `E3` endpoint 3
- `E4` endpoint 4

Details

The data (from Westfall et al., 1999) contain measurements of patients in treatment (`Drug`) and control (`Placebo`) groups, with four outcome variables.

Source

Description

Directly specify estimated model parameters and their covariance matrix.

Usage

```r
cparm(coef, vcov, df = 0)
```

Arguments

- `coef`: estimated coefficients.
- `vcov`: estimated covariance matrix of the coefficients.
- `df`: an optional specification of the degrees of freedom to be used in subsequent computations.

Details

When only estimated model parameters and the corresponding covariance matrix is available for simultaneous inference using `glht` (for example, when only the results but not the original data are available or, even worse, when the model has been fitted outside R), function `p parm` sets up an object `glht` is able to compute on (mainly by offering `coef` and `vcov` methods).

Note that the linear function in `glht` can't be specified via `mcp` since the model terms are missing.

Value

An object of class `parm` with elements

- `coef`: model parameters
- `vcov`: covariance matrix of model parameters
- `df`: degrees of freedom

Examples

```r
## example from
## Bretz, Hothorn, and Westfall (2002).

beta <- c(V1 = 14.8, V2 = 12.6667, V3 = 7.3333, V4 = 13.1333)
Sigma <- 6.7099 * (diag(1 / c(20, 3, 3, 15)))
confint(glht(model = parm(beta, Sigma, 37),
            linfct = c("V2 - V1 >= 0",
                       "V3 - V1 >= 0",
                       "V4 - V1 >= 0")),
           level = 0.9)
```
plot.cld  

Plot a cld object

Description

Plot information of glht, summary.glht or confint.glht objects stored as cld objects together with a compact letter display of all pair-wise comparisons.

Usage

## S3 method for class 'cld'
plot(x, type = c("response", "lp"), ...)

Arguments

x  
An object of class cld.

type  
Should the response or the linear predictor (lp) be plotted. If there are any covariates, the lp is automatically used. To use the response variable, set type="response" and covar=FALSE of the cld object.

...  
Other optional print parameters which are passed to the plotting functions.

Details

This function plots the information stored in glht, summary.glht or confint.glht objects. Prior to plotting, these objects have to be converted to cld objects (see cld for details). All types of plots include a compact letter display (cld) of all pair-wise comparisons. Equal letters indicate no significant differences. Two levels are significantly different, in case they do not have any letters in common. If the fitted model contains any covariates, a boxplot of the linear predictor is generated with the cld within the upper margin. Otherwise, three different types of plots are used depending on the class of variable y of the cld object. In case of class(y) == "numeric", a boxplot is generated using the response variable, classified according to the levels of the variable used for the Tukey contrast matrix. Is class(y) == "factor", a mosaic plot is generated, and the cld is printed above. In case of class(y) == "Surv", a plot of fitted survival functions is generated where the cld is plotted within the legend. The compact letter display is computed using the algorithm of Piepho (2004). Note: The user has to provide a sufficiently large upper margin which can be used to depict the compact letter display (see examples).

References


See Also

glht cld cld.summary.glht cld.confint.glht cld.glht boxplot mosaicplot plot.survfit
### multiple comparison procedures
### set up a one-way ANOVA
data(warpbreaks)
amod <- aov(breaks ~ tension, data = warpbreaks)
### specify all pair-wise comparisons among levels of variable "tension"
tuk <- glht(amod, linfct = mcp(tension = "Tukey"))
### extract information
tuk.cld <- cld(tuk)
### use sufficiently large upper margin
old.par <- par(mai=c(1,1,1.25,1), no.readonly=TRUE)
### plot
plot(tuk.cld)
par(old.par)

### now using covariates
amod2 <- aov(breaks ~ tension + wool, data = warpbreaks)
tuk2 <- glht(amod2, linfct = mcp(tension = "Tukey"))
tuk.cld2 <- cld(tuk2)
old.par <- par(mai=c(1,1,1.25,1), no.readonly=TRUE)
### use different colors for boxes
plot(tuk.cld2, col=c("green", "red", "blue"))
par(old.par)

### get confidence intervals
ci.glht <- confint(tuk)
### plot them
plot(ci.glht)
old.par <- par(mai=c(1,1,1.25,1), no.readonly=TRUE)
### use 'confint.glht' object to plot all pair-wise comparisons
plot(cld(ci.glht), col=c("white", "blue", "green"))
par(old.par)

### set up all pair-wise comparisons for count data
data(Titanic)
mod <- glm(Survived ~ Class, data = as.data.frame(Titanic),
weights = Freq, family = binomial())
### specify all pair-wise comparisons among levels of variable "Class"
ghlmod <- glht(mod, mcp(Class = "Tukey"))
### extract information
mod.cld <- cld(ghlmod)
### use sufficiently large upper margin
old.par <- par(mai=c(1,1,1.5,1), no.readonly=TRUE)
### plot
plot(mod.cld)
par(old.par)

### set up all pair-wise comparisons of a Cox-model
if (require("survival") && require("MASS")) {
    ### construct 4 classes of age
    Melanoma$Cage <- factor(sapply(Melanoma$age, function(x){
    ...}})
if ( x <= 25 ) return(1)
if ( x > 25 & x <= 50 ) return(2)
if ( x > 50 & x <= 75 ) return(3)
if ( x > 75 & x <= 100 ) return(4)
)

### fit Cox-model
cm <- coxph(Surv(time, status == 1) ~ Cage, data = Melanoma)
### specify all pair-wise comparisons among levels of "Cage"
cm.glht <- glht(cm, mcp(Cage = "Tukey"))
# extract information & plot
old.par <- par(no.readonly=TRUE)
### use mono font family
if (dev.interactive())
  old.par <- par(family = "mono")
plot(cld(cm.glht), col=c("black", "red", "blue", "green"))
par(old.par)

if (require("nlme") && require("lme4")) {
data("ergoStool", package = "nlme")

stool.lmer <- lmer(effort ~ Type + (1 | Subject),
  data = ergoStool)
glme41 <- glht(stool.lmer, mcp(Type = "Tukey"))
old.par <- par(mai=c(1,1,1.5,1), no.readonly=TRUE)
plot(cld(glme41))
par(old.par)
}

---

<table>
<thead>
<tr>
<th>recovery</th>
<th>Recovery Time Data Set</th>
</tr>
</thead>
</table>

**Description**

Recovery time after surgery.

**Usage**

data("recovery")

**Format**

This data frame contains the following variables

- **blanket**  blanket type, a factor at four levels: b0, b1, b2, and b3.
- **minutes**  response variable: recovery time after a surgical procedure.
Details

A company developed specialized heating blankets designed to help the body heat following a surgical procedure. Four types of blankets were tried on surgical patients with the aim of comparing the recovery time of patients. One of the blanket was a standard blanket that had been in use already in various hospitals.

Source


Examples

```r
### set up one-way ANOVA
amod <- aov(minutes ~ blanket, data = recovery)

### set up multiple comparisons: one-sided Dunnett contrasts
rht <- glht(amod, linfct = mcp(blanket = "Dunnett"),
            alternative = "less")

### cf. Westfall et al. (1999, p. 80)
confint(rht, level = 0.9)

### the same
rht <- glht(amod, linfct = mcp(blanket = c("b1 - b0 >= 0",
                                     "b2 - b0 >= 0",
                                     "b3 - b0 >= 0")))

confint(rht, level = 0.9)
```

---

**sbp**  
*Systolic Blood Pressure Data*

**Description**

Systolic blood pressure, age and gender of 69 people.

**Usage**

data("sbp")

**Format**

A data frame with 69 observations on the following 3 variables.

- gender: a factor with levels male female
- sbp: systolic blood pressure in mmHg
- age: age in years
Frankonian Tree Damage Data

Description

Damages on young trees caused by deer browsing.

Usage

data("trees513")

Format

A data frame with 2700 observations on the following 4 variables.

damage  a factor with levels yes and no indicating whether or not the trees has been damaged by
game animals, mostly roe deer.

species  a factor with levels spruce, fir, pine, softwood (other), beech, oak, ash/maple/elm/lime,
and hardwood (other).

lattice  a factor with levels 1, ..., 53, essentially a number indicating the position of the sampled
area.

plot    a factor with levels x_1, ..., x_5 where x is the lattice. plot is nested within lattice and is
a replication for each lattice point.

Details

In most parts of Germany, the natural or artificial regeneration of forests is difficult due to a high
browsing intensity. Young trees suffer from browsing damage, mostly by roe and red deer. In order
to estimate the browsing intensity for several tree species, the Bavarian State Ministry of Agriculture
and Forestry conducts a survey every three years. Based on the estimated percentage of damaged
trees, suggestions for the implementation or modification of deer management plans are made.
The survey takes place in all 756 game management districts (‘Hegegemeinschaften’) in Bavaria.
The data given here are from the game management district number 513 ‘Unterer Aischgrund’
(located in Frankonia between Erlangen and Höchstadt) in 2006. The data of 2700 trees include
the species and a binary variable indicating whether or not the tree suffers from damage caused by
deer browsing.

Source

Bayerisches Staatsministerium fuer Landwirtschaft und Forsten (2006), Forstliche Gutachten zur

Torsten Hothorn, Frank Bretz and Peter Westfall (2008), Simultaneous Inference in General Para-
= "multcomp").
Examples

summary(trees513)

---

### Industrial Waste Data Set

**Description**

Industrial waste output in a manufacturing plant.

**Usage**

```r
data("waste")
```

**Format**

This data frame contains the following variables

- **temp** temperature, a factor at three levels: low, medium, high.
- **envir** environment, a factor at five levels: env1 ... env5.
- **waste** response variable: waste output in a manufacturing plant.

**Details**

The data are from an experiment designed to study the effect of temperature (temp) and environment (envir) on waste output in a manufacturing plant. Two replicate measurements were taken at each temperature / environment combination.

**Source**


**Examples**

```r
### set up two-way ANOVA with interactions
amod <- aov(waste ~ temp * envir, data=waste)

### comparisons of main effects only
K <- glht(amod, linfct = mcp(temp = "Tukey"))$linfct
K

### comparisons of means (by averaging interaction effects)
low <- grep("low:envi", colnames(K))
```
```
med <- grep("medium:envi", colnames(K))
K[3, low] <- 1 / (length(low) + 1)
K[2, med] <- 1 / (length(low) + 1)
K[3, med] <- 1 / (length(low) + 1)
K[3, low] <- -1 / (length(low) + 1)
K
confint(glht(amod, K))

### same as TukeyHSD
TukeyHSD(amod, "temp")

### set up linear hypotheses for all-pairs of both factors
wht <- glht(amod, linfct = mcp(temp = "Tukey", envir = "Tukey"))

### cf. Westfall et al. (1999, page 181)
summary(wht, test = adjusted("Shaffer"))
```
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