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Title L1-Penalized Multinomial Regression with Statistical Inference
Version 0.1.0
Description We aim for fitting a multinomial regression model with Lasso penalty and doing statistical inference (calculating confidence intervals of coefficients and p-values for individual variables). It implements 1) the coordinate descent algorithm to fit an l1-penalized multinomial regression model (parameterized with a reference level); 2) the debiasing approach to obtain the inference results, which is described in Tian et al. (2023) <arXiv:2302.02310>.
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cv.pemultinom

Fit a multinomial regression model with Lasso penalty.

Description

Fit a multinomial regression model with Lasso penalty. This function implements the l1-penalized multinomial regression model (parameterized with a reference level). A cross-validation procedure is applied to choose the tuning parameter. See Tian et al. (2023) for details.

Usage

```r
cv.pemultinom(
  x, 
  y, 
  ref = NULL, 
  nfolds = 5, 
  nlambda = 100, 
  max_iter = 200, 
  tol = 0.001, 
  ncores = 1, 
  standardized = TRUE, 
  weights = NULL
)
```

Arguments

- `x` the design/predictor matrix, each row of which is an observation vector.
- `y` the response variable. Can be of one type from factor/integer/character.
- `ref` the reference level. Default = NULL, which sets the reference level to the last category (sorted by alphabetical order).
- `nfolds` the number of cross-validation folds to use. Default = 5.
- `nlambda` the number of penalty parameter candidates. Default = 100.
- `max_iter` the maximum iteration rounds in each iteration of the coordinate descent algorithm. Default = 200.
- `tol` convergence threshold (tolerance level) for coordinate descent. Default = 1e-3.
- `ncores` the number of cores to use for parallel computing. Default = 1.
- `standardized` logical flag for x variable standardization, prior to fitting the model sequence. Default = TRUE. Note that the fitting results will be translated to the original scale before output.
- `weights` observation weights. Should be a vector of non-negative numbers of length n (the number of observations). Default = NULL, which sets equal weights for all observations.
Value

A list with the following components.

- **beta.list**: the estimates of coefficients. It is a list of which the k-th component is the contrast coefficient between class k and the reference class corresponding to different lambda values. The j-th column of each list component corresponds to the j-th lambda value.

- **beta.1se**: the coefficient estimate corresponding to lambda.1se. It is a matrix, and the k-th column is the contrast coefficient between class k and the reference class.

- **beta.min**: the coefficient estimate corresponding to lambda.min. It is a matrix, and the k-th column is the contrast coefficient between class k and the reference class.

- **lambda.1se**: the largest value of lambda such that error is within 1 standard error of the minimum. See Chapter 2.3 of Hastie et al. (2015) for more details.

- **lambda.min**: the value of lambda that gives minimum cvm.

- **cvm**: the weights in objective function.

- **cvsd**: the estimated marginal probability for each class.

- **lambda**: lambda values considered in the cross-validation process.

References


See Also

debiased_lasso, predict_pemultinom.

Examples

```r
# generate data from Model 1 in Tian et al. (2023) with n = 50 and p = 50
set.seed(0, kind = "L'Ecuyer-CMRG")
n <- 50
p <- 50
K <- 3
Sigma <- outer(1:p, 1:p, function(x,y) {
  0.9^(abs(x-y))
})
R <- chol(Sigma)
s <- 3
beta_coef <- matrix(0, nrow = p+1, ncol = K-1)
beta_coef[1+1:s, 1] <- c(1.5, 1.5, 1.5)
beta_coef[1+1:s+s, 2] <- c(1.5, 1.5, 1.5)
x <- matrix(rnorm(n*p), ncol = p) %*% R
```
debiased_lasso

Doing statistical inference on l1-penalized multinomial regression via debiased Lasso (or desparisified Lasso).

debiased_lasso

Description

Doing statistical inference on l1-penalized multinomial regression via debiased Lasso (or desparisified Lasso). This function implements the algorithm described in Tian et al. (2023), which is an extension of the original debiased Lasso (Van de Geer et al. (2014); Zhang and Zhang (2014)) to the multinomial case.

Usage

debiased_lasso(
  x,
  y,
  ref = NULL,
)
debiased_lasso

beta,  
nfolds = 5,  
ncores = 1,  
nlambda = 50,  
max_iter = 200,  
tol = 0.001,  
lambda.choice = "lambda.min",  
alpha = 0.05  
)

Arguments

x  
the design/predictor matrix, each row of which is an observation vector.
y  
the response variable. Can be of one type from factor/integer/character.
ref  
the reference level. Default = NULL, which sets the same reference level as used in obtaining beta. Even when the user inputs ref manually, it should be always the same reference level as used in obtaining beta.
beta  
the beta estimate from l1-penalized multinomial regression. Should be in the same format as beta.min or beta.1se in output of function cv.pemultinom. The user is recommended to directly pass beta.min or beta.1se from the output of function cv.pemultinom to parameter beta.
folds  
the number of cross-validation folds to use. Cross-validation is used to determine the best tuning parameter lambda in the nodewise regression, i.e., Algorithm 2 in Tian et al. (2023). Default = 5.
ncores  
the number of cores to use for parallel computing. Default = 1.
nlambda  
the number of penalty parameter candidates in the cross-validation procedure. Cross-validation is used to determine the best tuning parameter lambda in the nodewise regression, i.e., Algorithm 2 in Tian et al. (2023). Default = 100.
max_iter  
the maximum iteration rounds in each iteration of the coordinate descent algorithm. Default = 200.
tol  
convergence threshold (tolerance level) for coordinate descent. Default = 1e-3.
lambda.choice  
observation weights. Should be a vector of non-negative numbers of length n (the number of observations). Default = NULL, which sets equal weights for all observations.
alpha  
significance level used in the output confidence interval. Has to be a number between 0 and 1. Default = 0.05.

Value

A list of data frames, each of which contains the inference results for each class (v.s. the reference class). In the data frame, each row represents a variable. The columns include:

beta  
the debiased point estimate of the coefficient
p_value  
p value of each variable
CI_lower  
lower endpoint of the confidence interval for each coefficient
CI_upper  
upper endpoint of the confidence interval for each coefficient
std_dev  
the estimated standard deviation of each component of beta estimate
References


See Also
cv.pemultinom, predict_pemultinom.

Examples

# generate data from Model 1 in Tian et al. (2023) with n = 100 and p = 50
set.seed(0, kind = "L'Ecuyer-CMRG")
n <- 50
p <- 50
K <- 3
Sigma <- outer(1:p, 1:p, function(x,y) { 0.9^abs(x-y) })
R <- chol(Sigma)
s <- 3
beta_coef <- matrix(0, nrow = p+1, ncol = K-1)
beta_coef[1+1:s, 1] <- c(1.5, 1.5, 1.5)
beta_coef[1+1:s+s, 2] <- c(1.5, 1.5, 1.5)
x <- matrix(rnorm(n*p), ncol = p) %*% R
y <- sapply(1:n, function(j){
  prob_i <- c(sapply(1:(K-1), function(k){
    exp(sum(x[j, ]*beta_coef[-1, k]))
  })), 1)
  prob_i <- prob_i/sum(prob_i)
  sample(1:K, size = 1, replace = TRUE, prob = prob_i)
})

# fit the l1-penalized multinomial regression model
fit <- cv.pemultinom(x, y, ncores = 2)
beta <- fit$beta.min

# run the debiasing approach
fit_debiased <- debiased_lasso(x, y, beta = beta, ncores = 2)
predict_pemultinom

Make predictions on new predictors based on fitted 11-penalized multinomial regression model.

Description

Make predictions on new predictors based on fitted 11-penalized multinomial regression model, by using the fitted beta.

Usage

predict_pemultinom(beta, ref, xnew, type = c("class", "prob"))

Arguments

beta
  the beta estimate from 11-penalized multinomial regression. Should be in the same format as beta.min or beta.1se in output of function cv.pemultinom. The user is recommended to directly pass beta.min or beta.1se from the output of function cv.pemultinom to parameter beta.
ref
  the reference level, which should be the same reference level as used in obtaining beta. An input is required.
xnew
  new observations to predict labels for. Should be a matrix or a data frame, where each row and column represents an observation and predictor, respectively.
type
  the type of prediction output. Can be 'class' or 'prob'. Default = 'class'.
    • class: the predicted class/label.
    • prob: the predicted probability for each class.

Value

When type = 'class', return a vector. When type = 'prob', return a matrix where each row and column represent an observation and a probability of that class, respectively. Default = 'class'.

References


See Also

cv.pemultinom, debiased_lasso.
Examples

# generate training data from Model 1 in Tian et al. (2023) with n = 50 and p = 50
set.seed(1, kind = "L'Ecuyer-CMRG")
n <- 50
p <- 50
K <- 3

Sigma <- outer(1:p, 1:p, function(x,y) {
  0.9^(abs(x-y))
})
R <- chol(Sigma)
s <- 3
beta_coef <- matrix(0, nrow = p+1, ncol = K-1)
beta_coef[1+1:s, 1] <- c(1.5, 1.5, 1.5)
beta_coef[1+1:s+s, 2] <- c(1.5, 1.5, 1.5)

x <- matrix(rnorm(n*p), ncol = p) %*% R
y <- sapply(1:n, function(j){
  prob_i <- c(sapply(1:(K-1), function(k){
    exp(sum(x[j, ]*beta_coef[-1, k])))
  })), 1)
  prob_i <- prob_i/sum(prob_i)
sample(1:K, size = 1, replace = TRUE, prob = prob_i)
})

# fit the l1-penalized multinomial regression model
fit <- cv.pemultinom(x, y, ncores = 2)

# generate test data from the same model
x.test <- matrix(rnorm(n*p), ncol = p) %*% R
y.test <- sapply(1:n, function(j){
  prob_i <- c(sapply(1:(K-1), function(k){
    exp(sum(x.test[j, ]*beta_coef[-1, k])))
  })), 1)
  prob_i <- prob_i/sum(prob_i)
sample(1:K, size = 1, replace = TRUE, prob = prob_i)
})

# predict labels of test data and calculate the misclassification error rate (using beta.min)
ypred.min <- predict_pemultinom(fit$beta.min, ref = 3, xnew = x.test, type = "class")
mean(ypred.min != y.test)

# predict labels of test data and calculate the misclassification error rate (using beta.1se)
ypred.1se <- predict_pemultinom(fit$beta.1se, ref = 3, xnew = x.test, type = "class")
mean(ypred.1se != y.test)

# predict posterior probabilities of test data
ypred.prob <- predict_pemultinom(fit$beta.min, ref = 3, xnew = x.test, type = "prob")
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