

# Package ‘popkin’

January 27, 2022

**Title** Estimate Kinship and FST under Arbitrary Population Structure

**Version** 1.3.17

**Description** Provides functions to estimate the kinship matrix of individuals from a large set of biallelic SNPs, and extract inbreeding coefficients and the generalized FST (Wright's fixation index). Method described in Ochoa and Storey (2021) <[doi:10.1371/journal.pgen.1009241](https://doi.org/10.1371/journal.pgen.1009241)>.

**Depends** R (>= 3.5.0)

**Imports** Rcpp (>= 0.12.10), RColorBrewer, graphics, grDevices, ape

**LinkingTo** Rcpp, RcppEigen

**Suggests** BEDMatrix, testthat, knitr, rmarkdown, lfa, bnpsd

**License** GPL-3

**Encoding** UTF-8

**RoxygenNote** 7.1.2

**VignetteBuilder** knitr

**URL** <https://github.com/StoreyLab/popkin/>

**BugReports** <https://github.com/StoreyLab/popkin/issues>

**NeedsCompilation** yes

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**Repository** CRAN

**Date/Publication** 2022-01-27 10:00:02 UTC

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popkin-package	<i>A package for estimating kinship and FST under arbitrary population structure</i>
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## Description

The heart of this package is the `popkin()` function, which estimates the kinship matrix of all individual pairs from their genotype matrix. Inbreeding coefficients, the generalized FST, and the individual-level pairwise FST matrix are extracted from the kinship matrix using `inbr()`, `fst()`, and `pwfst()`, respectively. `fst()` accepts weights for individuals to balance subpopulations obtained with `weights_subpops()`. Kinship matrices can be renormalized (to change the most recent common ancestor population or MRCA) using `rescale_popkin()`. Coancestry matrices can be estimated from allele frequency matrices using `popkin_af()`. Lastly, kinship, coancestry, and pairwise FST matrices can be visualized using `plot_popkin()` (with the help of `inbr_diag()` for kinship matrices only).

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## See Also

Useful links:

- <https://github.com/StoreyLab/popkin/>
- Report bugs at <https://github.com/StoreyLab/popkin/issues>

**Examples**

```

# estimate and visualize kinship and FST from a genotype matrix

# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow = 3, byrow = TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals
subpops2 <- 1:3 # alternate labels treat every individual as a different subpop

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix from the genotypes "X"!
# all downstream analysis require "kinship", none use "X" after this
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels

# plot the kinship matrix, marking the subpopulations
# note inbr_diag replaces the diagonal of kinship with inbreeding coefficients
plot_popkin( inbr_diag(kinship), labs = subpops )

# extract inbreeding coefficients from kinship
inbreeding <- inbr(kinship)

# estimate FST
weights <- weights_subpops(subpops) # weigh individuals so subpopulations are balanced
Fst <- fst(kinship, weights) # use kinship matrix and weights to calculate fst
Fst <- fst(inbreeding, weights) # estimate more directly from inbreeding vector (same result)

# estimate and visualize the pairwise FST matrix
pairwise_fst <- pwfst(kinship) # estimated matrix
leg_title <- expression(paste('Pairwise ', F[ST])) # fancy legend label
# NOTE no need for inbr_diag() here!
plot_popkin(pairwise_fst, labs = subpops, leg_title = leg_title)

# rescale the kinship matrix using different subpopulations (implicitly changes the MRCA)
kinship2 <- rescale_popkin(kinship, subpops2)

# toy allele frequency data
P <- matrix( runif( 9 ), nrow = 3 )

# estimate coancestry from allele frequency matrix
# (useful from P matrices from admixture models)
coancestry <- popkin_af( P )

```

---

avg\_kinship\_subpops     *Calculate a kinship matrix between subpopulations by averaging individual data*

---

**Description**

This function calculates a kinship matrix between subpopulations, whose values are the average kinship values between all individual pairs where one individual is in the first subpopulation and the other individual is in the second subpopulation. To estimate coancestry instead of kinship, which is recommended to get more interpretable diagonal values, the input kinship matrix should be transformed using `inbr_diag()`.

**Usage**

```
avg_kinship_subpops(kinship, subpops, subpop_order = unique(subpops))
```

**Arguments**

kinship	A symmetric n-by-n kinship matrix.
subpops	The length-n vector of subpopulation assignments for each individual.
subpop_order	The optional order of subpopulations in the output matrix. subpop_order must contain every unique subpopulation in subpops. Any additional subpopulations in subpop_order (missing in subpops) are ignored. By default, subpopulations are in the order of first appearance in subpops.

**Value**

The symmetric K-by-K kinship matrix between subpopulations, where K is the number of unique subpopulations in subpops, ordered as in subpop\_order.

**Examples**

```
# a toy kinship matrix with 5 individuals belonging to 2 subpopulations
kinship <- matrix(
  c(
    0.7, 0.4, 0.4, 0.1, 0.0,
    0.4, 0.7, 0.4, 0.2, 0.1,
    0.4, 0.4, 0.7, 0.2, 0.0,
    0.1, 0.2, 0.2, 0.6, 0.1,
    0.0, 0.1, 0.0, 0.1, 0.6
  ),
  nrow = 5,
  ncol = 5
)
subpops <- c(1, 1, 1, 2, 2)

# calculate mean kinship between (and within) subpopulations
# a 2x2 matrix
avg_kinship_subpops( kinship, subpops )

# calculate coancestry estimate instead (difference is diagonal)
avg_kinship_subpops( inbr_diag( kinship ), subpops )
```

---

fst	<i>Calculate FST from a population-level kinship matrix or vector of inbreeding coefficients</i>
-----	--

---

## Description

This function simply returns the weighted mean inbreeding coefficient. If weights are NULL (default), the regular mean is calculated. If a kinship matrix is provided, then the inbreeding coefficients are extracted from its diagonal using `inbr()` (requires the diagonal to contain self-kinship values as `popkin()` returns, and not inbreeding coefficients as `inbr_diag()` returns). If there is local inbreeding and it can be estimated (from known pedigrees, for example), it can be subtracted from the total inbreeding coefficients, resulting in a vector of structural inbreeding that correctly averages into FST.

## Usage

```
fst(x, weights = NULL, x_local = NULL)
```

## Arguments

<code>x</code>	The vector of inbreeding coefficients, or the kinship matrix if <code>x</code> is a matrix.
<code>weights</code>	Weights for individuals (optional, defaults to uniform weights)
<code>x_local</code>	An optional vector of inbreeding coefficients, or a local kinship matrix if <code>x_local</code> is a matrix.

## Details

The returned weighted mean inbreeding coefficient equals the generalized FST if all individuals are "locally outbred" (i.e. if the self-relatedness of every individual stems entirely from the population structure rather than due partly to having unusually closely related parents, such as first or second cousins). Note most individuals in population-scale human data are locally outbred. If there are locally-inbred individuals, but their local inbreeding cannot be estimated, then the returned value will overestimate FST. Good estimates of local inbreeding can be passed (parameter `x_local`), in which case the code will subtract their effect and FST will be more accurate.

## Value

FST

## Examples

```
# Get FST from a genotype matrix

# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow = 3, byrow = TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals
```

```

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix "kinship" from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels
weights <- weights_subpops(subpops) # can weigh individuals so subpopulations are balanced
Fst <- fst(kinship, weights) # use kinship matrix and weights to calculate fst

Fst <- fst(kinship) # no (or NULL) weights implies uniform weights

inbr <- inbr(kinship) # if you extracted inbr for some other analysis...
Fst <- fst(inbr, weights) # ...use this inbreeding vector as input too!

```

---

inbr

---

*Extract inbreeding coefficients from a kinship matrix*


---

### Description

The kinship matrix contains transformed inbreeding coefficients along the diagonal. This function extracts the vector of inbreeding values from the input kinship matrix, by transforming the diagonal using the formula  $2 * x - 1$ .

### Usage

```
inbr(kinship)
```

### Arguments

kinship            The n-by-n kinship matrix.

### Value

The length-n vector of inbreeding coefficient for each individual.

### See Also

[inbr\\_diag\(\)](#) to replace kinship diagonal with inbreeding values (better for plots)

### Examples

```

#####
# illustrate the main transformation on a 2x2 kinship matrix:
# same inbreeding values for both individuals
inbr <- 0.2
# corresponding self kinship (diagonal values) for both individuals
kinship_self <- (1 + inbr)/2
# actual kinship matrix (zero kinship between individuals)

```

```

kinship <- matrix(c(kinship_self, 0, 0, kinship_self), nrow=2)
# expected output of inbr (extracts inbreeding coefficients)
inbr_exp <- c(inbr, inbr)
# actual output from this function
inbr_obs <- inbr(kinship)
# verify that they match (up to machine precision)
stopifnot( all( abs(inbr_obs - inbr_exp) < .Machine$double.eps ) )

#####
# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels

# extract inbreeding coefficients from Kinship
inbr <- inbr(kinship)

```

---

inbr\_diag

*Replace kinship diagonal with inbreeding coefficients*


---

### Description

The usual kinship matrix contains self-kinship values along their diagonal given by  $\text{diag}(\text{kinship}) = (1 + \text{inbr}) / 2$ , where  $\text{inbr}$  is the vector of inbreeding coefficient. This function returns a modified kinship matrix with diagonal values replaced with  $\text{inbr}$  (off-diagonal values stay the same). The resulting matrix is better for visualization, but is often not appropriate for modeling (e.g. in mixed-effects models for association or heritability estimation).

### Usage

```
inbr_diag(kinship)
```

### Arguments

kinship	A kinship matrix with self-kinship values along the diagonal. Can pass multiple kinship matrices contained in a list. If NULL, it is returned as-is.
---------	--

### Value

The modified kinship matrix, with inbreeding coefficients along the diagonal, preserving column and row names. If the input was a list of kinship matrices, the output is the corresponding list of transformed matrices. NULL inputs are preserved without causing errors.

**See Also**

The inverse function is given by `bnpsd::coanc_to_kinship()`.

`inbr()` to extract the vector of inbreeding values from a kinship matrix.

**Examples**

```
#####
# illustrate the main transformation on a 2x2 kinship matrix:
# same inbreeding values for both individuals
inbr <- 0.2
# corresponding self kinship (diagonal values) for both individuals
kinship_self <- (1 + inbr)/2
# kinship between the two individuals
kinship_between <- 0.1
# actual kinship matrix
kinship <- matrix(c(kinship_self, kinship_between, kinship_between, kinship_self), nrow=2)
# expected output of inbr_diag (replaces self kinship with inbreeding)
kinship_inbr_diag_exp <- matrix(c(inbr, kinship_between, kinship_between, inbr), nrow=2)
# actual output from this function
kinship_inbr_diag_obs <- inbr_diag(kinship)
# verify that they match (up to machine precision)
stopifnot( all( abs(kinship_inbr_diag_obs - kinship_inbr_diag_exp) < .Machine$double.eps ) )

# for a list of matrices, returns list of transformed matrices:
inbr_diag( list(kinship, kinship) )

# a list with NULL values also works
inbr_diag( list(kinship, NULL, kinship) )

#####
# Construct toy data (to more closely resemble real data analysis)
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels

# lastly, replace diagonal of kinship matrix with inbreeding coefficients
kinship_inbr_diag <- inbr_diag(kinship)
```

**Description**

This function computes a particular weighted mean kinship that arises in the context of kinship and FST estimators and in the definition of the effective sample size. This function allows for weights to be zero or even negative, but they are internally normalized to sum to one.

**Usage**

```
mean_kinship(kinship, weights = NULL)
```

**Arguments**

kinship	The kinship matrix
weights	Weights for individuals (optional). If NULL (default), uniform weights are used.

**Value**

The weighted mean kinship matrix, equivalent to `drop( weights %*% kinship %*% weights )` after normalizing weights to sum to one.

**Examples**

```
# construct a dummy kinship matrix
kinship <- matrix(c(0.5, 0, 0, 0.6), nrow=2)

# this is the ordinary mean
mean_kinship(kinship)

# weighted mean with twice as much weight on the second individual
# (weights are internally normalized to sum to one)
weights <- c(1, 2)
mean_kinship(kinship, weights)
```

---

n\_eff

*Calculates the effective sample size of the data*


---

**Description**

The effective sample size `n_eff` is the equivalent number of independent haplotypes that gives the same variance as that observed under the given population. The variance in question is for the weighted sample mean ancestral allele frequency estimator. It follows that `n_eff` equals the inverse of the weighted mean kinship. If `max = TRUE`, a calculation is performed that implicitly uses optimal weights which maximize `n_eff`, which equals the sum of the elements of the inverse kinship matrix. However, if `nonneg = TRUE` and if the above solution has negative weights (common), optimal non-negative weights are found instead (there are three algorithms available, see `algo`). If `max = FALSE`, then the input weights are used in this calculation, and if weights are NULL, uniform weights are used.

**Usage**

```
n_eff(
  kinship,
  max = TRUE,
  weights = NULL,
  nonneg = TRUE,
  algo = c("gradient", "newton", "heuristic"),
  tol = 1e-10
)
```

**Arguments**

kinship	An n-by-n kinship matrix.
max	If TRUE, returns the maximum n_eff value among those computed using all possible vectors of weights that sum to one (and which are additionally non-negative if nonneg = TRUE). If FALSE, n_eff is computed using the specific weight vector provided.
weights	Weights for individuals (optional). If NULL, uniform weights are used. This parameter is ignored if max = TRUE.
nonneg	If TRUE (default) and max = TRUE, non-negative weights that maximize n_eff are found. See algo. This has no effect if max = FALSE.
algo	Algorithm for finding optimal non-negative weights (applicable only if nonneg = TRUE and max = TRUE and the weights found by matrix inversion are non-negative). May be abbreviated. If "gradient" (default), an optimized gradient descent algorithm is used (fastest; recommended). If "newton", the exact multivariate newton's Method is used (slowest since (n+1)-by-(n+1) Hessian matrix needs to be inverted at every iteration; use if possible to confirm that "gradient" gives the best answer). If "heuristic", if the optimal solution by the inverse matrix method contains negative weights, the most negative weight in an iteration is forced to be zero in all subsequent iterations and the rest of the weights are solved for using the inverse matrix method, repeating until all resulting weights are non-negative (also slow, since inversion of large matrices is required; least likely to find optimal solution).
tol	Tolerance parameter for "gradient" and "newton" algorithms. The algorithms converge when the norm of the step vector is smaller than this tolerance value.

**Details**

The maximum n\_eff possible is  $2 * n$ , where  $n$  is the number of individuals; this value is attained only when all haplotypes are independent (a completely unstructured population in Hardy-Weinberg equilibrium). The minimum n\_eff possible is 1, which is attained in an extremely structured population with FST of 1, where every individual has exactly the same haplotype at every locus (no heterozygotes). Moreover, for  $K$  extremely-differentiated subpopulations (FST = 1 per subpopulation) n\_eff =  $K$ . In this way, n\_eff is smaller than the ideal value of  $2 * n$  depending on the amount of kinship (covariance) in the data.

Occasionally, depending on the quality of the input kinship matrix, the estimated n\_eff may be outside the theoretical  $[1, 2*n]$  range, in which case the return value is set to the closest boundary

value. The quality of the results depends on the success of matrix inversion (which for numerical reasons may incorrectly contain negative eigenvalues, for example) or of the gradient optimization.

### Value

A list containing `n_eff` and `weights` (optimal weights if `max = TRUE`, input weights otherwise).

### Examples

```
# Get n_eff from a genotype matrix

# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix "kinship" from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels
weights <- weights_subpops(subpops) # can weigh individuals so subpopulations are balanced

# use kinship matrix to calculate n_eff
# default mode returns maximum n_eff possible across all non-negative weights that sum to one
# also returns the weights that were optimal
obj <- n_eff(kinship)
n_eff_max <- obj$n_eff
w_max <- obj$weights

# version that uses weights provided
obj <- n_eff(kinship, max = FALSE, weights = weights)
n_eff_w <- obj$n_eff
w <- obj$weights # returns input weights renormalized for good measure

# no (or NULL) weights implies uniform weights
obj <- n_eff(kinship, max = FALSE)
n_eff_u <- obj$n_eff
w <- obj$weights # uniform weights
```

---

plot\_admix

*Make a structure/admixture plot*

---

### Description

This function facilitates structure plots with options that resemble those of `plot_popkin()` in name and results. The biggest difference is this function plots single panels (technically 2 panels including the legend, unless it is omitted), whereas `plot_popkin()` can plot multiple kinship matrices with a shared legend.

**Usage**

```

plot_admix(
  Q,
  col = RColorBrewer::brewer.pal(max(ncol(Q), 3), "Paired"),
  mar_pad = 0.2,
  panel_letters = NA,
  panel_letters_cex = 1.5,
  panel_letters_adj = -0.1,
  axis_lab_cex = 1,
  xlab = "Individuals",
  xlab_line = 1,
  xlab_cex = axis_lab_cex,
  ylab = "Ancestry",
  ylab_line = 2,
  ylab_side = 2,
  ylab_cex = axis_lab_cex,
  leg_title = "Ancestries",
  leg_title_cex = axis_lab_cex,
  leg_cex = 1,
  leg_mar = 3,
  leg_width = 0.2,
  leg_omit = FALSE,
  layout_add = !leg_omit,
  names = FALSE,
  names_cex = 1,
  names_line = NA,
  names_las = 2,
  labs = NULL,
  labs_cex = 1,
  labs_las = 0,
  labs_line = 0,
  labs_sep = TRUE,
  labs_lwd = 1,
  labs_col = "black",
  labs_ticks = FALSE,
  labs_text = TRUE,
  labs_even = FALSE,
  ...
)

```

**Arguments**

Q	The admixture proportions matrix, with $n$ individuals along rows and $K$ ancestries along columns. Rows should sum to 1, but this is not enforced. There must be at least 2 ancestries. The ancestry labels used by the legend must be the column names, which are unlabeled if the column names are missing.
col	A vector of at least $K$ colors for the ancestries (extra colors are ignored). By default uses the "Paired" palette of RColorBrewer, which has at most 12 colors,

so please provide colors if  $K > 12$ . Since the minimum number of colors for "Paired" is 3, when  $K = 2$  we ask for 3 colors, then remove the middle color internally.

mar_pad	Margin padding used for legend panel only (margins for first/main panel are not altered by this function).
panel_letters	Panel letter to include in first/main panel (default NA is no letter). Despite name (matches <code>plot_popkin()</code> ), must be scalar.
panel_letters_cex	Scaling factor of panel letter (default 1.5).
panel_letters_adj	X-axis adjustment for panel letter (default -0.1). Negative values place the letter into the left margin area. Might need adjustment depending on the size of the left margin.
AXIS LABEL OPTIONS	
axis_lab_cex	Scaling factor for x-axis, y-axis, and legend title labels (which can also be set individually, see below).
xlab	X-axis label (default "Individuals"). Set to NA to omit.
xlab_line	The value of line for xlab passed to <code>graphics::mtext()</code> .
xlab_cex	Scaling factor for x-axis label.
ylab	Y-axis label (default "Ancestry"). Set to NA to omit.
ylab_line	The value of line for ylab passed to <code>graphics::mtext()</code> .
ylab_side	The value of side for ylab passed to <code>graphics::mtext()</code> (2 is y-axis, 1 is x-axis, can also place on top (3) or right (4)).
ylab_cex	Scaling factor for y-axis label.
LEGEND (COLOR KEY) OPTIONS	
leg_title	The name of the categorical ancestry variable (default "Ancestries").
leg_title_cex	Scaling factor for legend title label.
leg_cex	Scaling factor for ancestry labels.
leg_mar	Margin values for the kinship legend panel only. A length-4 vector (in <code>c(bottom, left, top, right)</code> format that <code>graphics::par()</code> 'mar' expects) specifies the full margins, to which <code>mar_pad</code> is added. Otherwise, the margins used in the last panel are preserved with the exception that the left margin is set to <code>mar_pad</code> , and if <code>leg_mar</code> is length-1, it is added to <code>mar_pad</code> to specify the right margin.
leg_width	The width of the legend panel, relative to the width of the main panel. This value is passed to <code>graphics::layout()</code> (ignored if <code>layout_add = FALSE</code> ).
leg_omit	If TRUE, no legend (second panel) is produced (default FALSE is to include legend).
layout_add	If TRUE (default) then <code>graphics::layout()</code> is called internally to create two panels: the main panel and the color key legend. The original layout is reset when plotting is complete and if <code>layout_add = TRUE</code> . If a non-standard layout or additional panels (beyond those provided by this function) are desired, set to FALSE and call <code>graphics::layout()</code> yourself beforehand.

INDIVIDUAL LABEL OPTIONS

names	If TRUE, the row (individual) names are plotted in the structure barplot.
names_cex	Scaling factor for the individual names.
names_line	Line where individual names are placed.
names_las	Orientation of labels relative to axis. Default (2) makes labels perpendicular to axis.
SUBPOPULATION LABEL OPTIONS	
labs	Subpopulation labels for individuals in the admixture matrix. Use a matrix of labels to show groupings at more than one level (for a hierarchy or otherwise).
labs_cex	A vector of label scaling factors for each level of labs.
labs_las	A vector of label orientations (in format that <code>graphics::mtext()</code> expects) for each level of labs.
labs_line	A vector of lines where labels are placed (in format that <code>graphics::mtext()</code> expects) for each level of labs.
labs_sep	A vector of logicals that specify whether lines separating the subpopulations are drawn for each level of labs.
labs_lwd	A vector of line widths for the lines that divide subpopulations (if <code>labs_sep = TRUE</code> ) for each level of labs.
labs_col	A vector of colors for the lines that divide subpopulations (if <code>labs_sep = TRUE</code> ) for each level of labs.
labs_ticks	A vector of logicals that specify whether ticks separating the subpopulations are drawn for each level of labs.
labs_text	A vector of logicals that specify whether the subpopulation labels are shown for each level of labs. Useful for including separating lines or ticks without text.
labs_even	A vector of logicals that specify whether the subpopulations labels are drawn with equal spacing for each level of labs. When TRUE, lines mapping the equally-spaced labels to the unequally-spaced subsections of the heatmap are also drawn.
...	Additional options passed to <code>graphics::barplot()</code> .

### Examples

```
# create random proportions for two ancestries
Q <- runif( 10 )
Q <- cbind( Q, 1 - Q )
# add ancestry names
colnames( Q ) <- c('A1', 'A2')

# plot this data!
plot_admix( Q )

# See vignette for more elaborate examples!
```

---

plot_phylo	<i>Plot a phylo tree object</i>
------------	---------------------------------

---

### Description

This is a wrapper around `ape::plot.phylo()` that makes several adjustments so plots agree more with accompanying kinship matrices. In particular, tree is reversed on the y-axis to match matrix orientation, y-axis spacing is more padded for small trees, and an x-axis scale is always added.

### Usage

```
plot_phylo(tree, xlab = "Coancestry", xmax = NULL, leg_n = 5, ...)
```

### Arguments

tree	A phylo object to plot.
xlab	The x-axis label (default "Coancestry").
xmax	X-axis maximum limit.
leg_n	The desired number of ticks in the x-axis (input to <code>pretty()</code> , see that for more details).
...	Additional parameters passed to <code>ape::plot.phylo()</code> . However, these parameters cannot be passed: <code>x.lim</code> (controlled via <code>xmax</code> ), <code>y.lim</code> (a better default for small trees is passed and cannot be changed) and <code>font</code> (takes the value of <code>par('font')</code> instead of <code>ape</code> 's default of 3 (italic)).

### See Also

`plot_popkin()` can create multipanel figures including kinship matrices and trees (calling the present function in the process).

### Examples

```
# create a small random tree
library(ape)
tree <- rtree( 3 )

# plot it!
plot_phylo( tree )
```

---

`plot_popkin`*Visualize one or more kinship matrices and other related objects*

---

**Description**

This function plots one or more kinship matrices, trees (class phylo objects, see ape package), and arbitrary functions, and a shared legend for the kinship color key. Many options allow for fine control of individual or subpopulation labeling.

**Usage**

```
plot_popkin(  
  kinship,  
  titles = NULL,  
  col = NULL,  
  col_n = 100,  
  mar = NULL,  
  mar_pad = 0.2,  
  oma = 1.5,  
  diag_line = FALSE,  
  panel_letters = toupper(letters),  
  panel_letters_cex = 1.5,  
  panel_letters_adj = -0.1,  
  ylab = "Individuals",  
  ylab_adj = NA,  
  ylab_line = 0,  
  ylab_side = 2,  
  layout_add = TRUE,  
  layout_rows = 1,  
  leg_per_panel = FALSE,  
  leg_title = "Kinship",  
  leg_cex = 1,  
  leg_n = 5,  
  leg_mar = 3,  
  leg_width = 0.3,  
  leg_column = NA,  
  names = FALSE,  
  names_cex = 1,  
  names_line = NA,  
  names_las = 2,  
  labs = NULL,  
  labs_cex = 1,  
  labs_las = 0,  
  labs_line = 0,  
  labs_sep = TRUE,  
  labs_lwd = 1,  
  labs_col = "black",
```

```

    labs_ticks = FALSE,
    labs_text = TRUE,
    labs_even = FALSE,
    null_panel_data = FALSE,
    weights = NULL,
    raster = is.null(weights),
    sym = FALSE,
    ...
)

```

## Arguments

kinship	A numeric kinship matrix, a phylo or function object, or a list of any such objects (at least one kinship matrix is expected). This list may contain NULL elements (makes blank panels with titles; good for placeholders or non-existent data) phylo objects are plotted with <code>plot_phylo()</code> , which is a wrapper around <code>ape::plot.phylo()</code> that makes some adjustments so resulting plots are more consistent with accompanying kinship matrices. function elements are executed without arguments, and are expected to produce single arbitrary plot panels.
titles	Titles to add to each matrix panel (default is no titles). Applied to kinship and phylo panels only.
col	Colors for kinship heatmap (default is a red-white-blue palette symmetric about zero constructed using <code>RColorBrewer</code> ).
col_n	The number of colors to use in the heatmap (applies if <code>col = NULL</code> ).
mar	Margins shared by all panels (if a vector) or for each panel (if a list of such vectors). If the vector has length 1, <code>mar</code> corresponds to the shared lower and left margins, while the top and right margins are set to zero. If this length is 2, <code>mar[1]</code> is the same as above, while <code>mar[2]</code> is the top margin. If this length is 4, then <code>mar</code> is a fully-specified margin vector in the standard format <code>c(bottom, left, top, right)</code> that <code>graphics::par()</code> 'mar' expects. Vectors of invalid lengths produce a warning. Note the padding <code>mar_pad</code> below is added to every margin if set. If <code>NULL</code> , the original margin values are used without change, and are reset for every panel that has a <code>NULL</code> value. The original margins are also reset after plotting is complete. Applied to panels of all types (kinship, phylo, and function).
mar_pad	Margin padding added to all panels ( <code>mar</code> above and <code>leg_mar</code> below). Default 0.2. Must be a scalar or a vector of length 4 to match <code>graphics::par()</code> 'mar'. Applied to panels of all types (kinship, phylo, and function).
oma	Outer margin vector. If length 1, the value of <code>oma</code> is applied to the left outer margin only (so <code>ylab</code> below displays correctly) and zero outer margins elsewhere. If length 4, all outer margins are expected in standard format <code>graphics::par()</code> 'mar' expects (see <code>mar</code> above). <code>mar_pad</code> above is never added to outer margins. If <code>NULL</code> , no outer margins are set (previous settings are preserved). Vectors of invalid lengths produce a warning.
diag_line	If <code>TRUE</code> adds a line along the kinship diagonal (default no line). May also be a

	vector of logicals to set per panel (lengths must agree). Has no effect on non-kinship panels.
panel_letters	Vector of strings for labeling panels (default A-Z). No labels are added if NULL, or when there is only one panel except if its set to a single letter in that case (this behavior is useful if goal is to have multiple external panels but popkin only creates one of these panels). Applied to panels of all types (kinship, phylo, and function).
panel_letters_cex	Scaling factor of panel letters (default 1.5).
panel_letters_adj	X-axis adjustment for panel letters (default -0.1). Negative values place the letter into the left margin area. Might need adjustment depending on the size of the left margin.
ylab	The y-axis label (default "Individuals"). If <code>length(ylab) == 1</code> , the label is placed in the outer margin (shared across panels); otherwise <code>length(ylab)</code> must equal the number of panels and each label is placed in the inner margin of the respective panel. Applied to panels of all types (kinship, phylo, and function).
ylab_adj	The value of <code>adj</code> for <code>ylab</code> passed to <code>graphics::mtext()</code> . If <code>length(ylab) == 1</code> , only the first value is used, otherwise <code>length(ylab_adj)</code> must equal the number of panels.
ylab_line	The value of <code>line</code> for <code>ylab</code> passed to <code>graphics::mtext()</code> . If <code>length(ylab) == 1</code> , only the first value is used, otherwise <code>length(ylab_line)</code> must equal the number of panels.
ylab_side	The value of <code>side</code> for <code>ylab</code> passed to <code>graphics::mtext()</code> (2 is y-axis, 1 is x-axis, can also place on top (3) or right (4)). If <code>length(ylab) == 1</code> , only the first value is used, otherwise <code>length(ylab_side)</code> must equal the number of panels.
	LAYOUT OPTIONS
layout_add	If TRUE (default) then <code>graphics::layout()</code> is called internally with appropriate values for the required number of panels for each matrix, the desired number of rows (see <code>layout_rows</code> below) plus the color key legend. The original layout is reset when plotting is complete and if <code>layout_add = TRUE</code> . If a non-standard layout or additional panels (beyond those provided by <code>plot_popkin</code> ) are desired, set to FALSE and call <code>graphics::layout()</code> yourself beforehand.
layout_rows	Number of rows in layout, used only if <code>layout_add = TRUE</code> .
	LEGEND (COLOR KEY) OPTIONS
leg_per_panel	If TRUE, every kinship matrix get its own legend/color key (best for matrices with very different scales), and each phylo tree has its own x-axis range. If FALSE (default), a single legend/color key is shared by all kinship matrix panels, and also every tree has the same x-axis range (different from the kinship range).
leg_title	The name of the variable that the kinship heatmap colors measure (default "Kinship"), or a vector of such values if they vary per panel.
leg_cex	Scaling factor for <code>leg_title</code> (default 1), or a vector of such values if they vary per panel.

leg_n	The desired number of ticks in the kinship legend y-axis, and phylo x-axis (input to <code>pretty()</code> , see that for more details), or a vector of such values if they vary per panel.
leg_mar	Margin values for the kinship legend panel only, or a list of such values if they vary per panel. A length-4 vector (in <code>c( bottom, left, top, right )</code> format that <code>graphics::par()</code> 'mar' expects) specifies the full margins, to which <code>mar_pad</code> is added. Otherwise, the margins used in the last panel are preserved with the exception that the left margin is set to <code>mar_pad</code> , and if <code>leg_mar</code> is length-1, it is added to <code>mar_pad</code> to specify the right margin.
leg_width	The width of the legend panel, relative to the width of a single main panel. This value is passed to <code>graphics::layout()</code> (ignored if <code>layout_add = FALSE</code> ).
leg_column	The column number in which to place the kinship legend (default NA is for last column). Ignored if <code>leg_per_panel = TRUE</code> .
	INDIVIDUAL LABEL OPTIONS
names	If TRUE, the column and row names are plotted in the kinship heatmap, or a vector of such values if they vary per panel. (names has no effect on phylo panels, whose tip labels are always plotted, or other panel types.)
names_cex	Scaling factor for the column and row names of a kinship matrix, or the tip labels of a phylo object, or a vector of such values if they vary per panel.
names_line	Line where kinship column and row names are placed, or a vector of such values if they vary per panel. Has no effect on non-kinship panels.
names_las	Orientation of labels relative to axis. Default (2) makes labels perpendicular to axis. Has no effect on non-kinship panels.
	SUBPOPULATION LABEL OPTIONS
labs	Subpopulation labels for individuals in kinship matrices. Use a matrix of labels to show groupings at more than one level (for a hierarchy or otherwise). If input is a vector or a matrix, the same subpopulation labels are shown for every kinship matrix; the input must be a list of such vectors or matrices if the labels vary per panel. Has no effect on non-kinship panels.
labs_cex	A vector of label scaling factors for each level of labs, or a list of such vectors if labels vary per panel.
labs_las	A vector of label orientations (in format that <code>graphics::mtext()</code> expects) for each level of labs, or a list of such vectors if labels vary per panel.
labs_line	A vector of lines where labels are placed (in format that <code>graphics::mtext()</code> expects) for each level of labs, or a list of such vectors if labels vary per panel.
labs_sep	A vector of logicals that specify whether lines separating the subpopulations are drawn for each level of labs, or a list of such vectors if labels vary per panel.
labs_lwd	A vector of line widths for the lines that divide subpopulations (if <code>labs_sep = TRUE</code> ) for each level of labs, or a list of such vectors if labels vary per panel.
labs_col	A vector of colors for the lines that divide subpopulations (if <code>labs_sep = TRUE</code> ) for each level of labs, or a list of such vectors if labels vary per panel.
labs_ticks	A vector of logicals that specify whether ticks separating the subpopulations are drawn for each level of labs, or a list of such vectors if labels vary per panel.

labs_text	A vector of logicals that specify whether the subpopulation labels are shown for each level of labs, or a list of such vectors if labels vary per panel. Useful for including separating lines or ticks without text.
labs_even	A vector of logicals that specify whether the subpopulations labels are drawn with equal spacing for each level of labs, or a list of such vectors if labels vary per panel. When TRUE, lines mapping the equally-spaced labels to the unequally-spaced subsections of the heatmap are also drawn.
null_panel_data	If FALSE (default), panels with NULL kinship matrices must not have titles or other parameters set, and no panel letters are used in these cases. If TRUE, panels with NULL kinship matrices must have titles and other parameters set. In the latter case, these NULL panels also get panel letters. The difference is important when checking that lengths of non-singleton parameters agree.
weights	A vector with weights for every individual, or a list of such vectors if they vary per panel. The width of every individual in the kinship matrix becomes proportional to their weight. Individuals with zero or negative weights are omitted. Has no effect on non-kinship panels.
raster	A logical equivalent to useRaster option in the image function used internally, or a vector of such logicals if the choice varies per panel. If weights are non-NULL in a given panel, raster = FALSE is forced (this is necessary to plot images where columns and rows have variable width). If weights are NULL, the default is raster = TRUE, but in this case the user may override (for example, so panels are visually coherent when some use weights while others do not, as there are small differences in rendering implementation for each value of raster). Note that a multipanel figure with a list of weights sets raster = FALSE to all panels by default, even if the weights were only applied to a subset of panels. Has no effect on non-kinship panels.
sym	If FALSE (default), plots non-symmetric (but square) kinship matrices without issues. If TRUE, stops if any input kinship matrices (excluding phylo or function objects) are not symmetric.
	AXIS LABEL OPTIONS
...	Additional options passed to <code>graphics::image()</code> . These are shared across kinship panels. Have no effect on non-kinship panels.

### Details

plot\_popkin plots the input kinship matrices as-is. For best results, a standard kinship matrix (such as the output of popkin()) should have its diagonal rescaled to contain inbreeding coefficients using inbr\_diag() before plot\_popkin is used.

This function permits the labeling of individuals (from row and column names when names = TRUE) and of subpopulations (passed through labs). The difference is that the labels passed through labs are assumed to be shared by many individuals, and lines (or other optional visual aids) are added to demarcate these subgroups.

### Examples

```
# Construct toy data
```

```

X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow = 3, byrow = TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels

# simple plot of the kinship matrix, marking the subpopulations only
# note inbr_diag replaces the diagonal of kinship with inbreeding coefficients
# (see vignette for more elaborate examples)
plot_popkin( inbr_diag(kinship), labs = subpops )

```

---

popkin	<i>Estimate kinship from a genotype matrix and subpopulation assignments</i>
--------	--

---

## Description

Given the biallelic genotypes of  $n$  individuals, this function returns the  $n$ -by- $n$  kinship matrix such that the kinship estimate between the most distant subpopulations is zero on average (this sets the ancestral population to the most recent common ancestor population).

## Usage

```

popkin(
  X,
  subpops = NULL,
  n = NA,
  loci_on_cols = FALSE,
  mem_factor = 0.7,
  mem_lim = NA,
  want_M = FALSE,
  m_chunk_max = 1000
)

```

## Arguments

<code>X</code>	Genotype matrix, BEDMatrix object, or a function $X(m)$ that returns the genotypes of all individuals at $m$ successive locus blocks each time it is called, and NULL when no loci are left. If a regular matrix, $X$ must have values only in $c(0, 1, 2, NA)$ , encoded to count the number of reference alleles at the locus, or NA for missing data.
<code>subpops</code>	The length- $n$ vector of subpopulation assignments for each individual. If NULL, every individual is effectively treated as a different population.

n	Number of individuals (required only when X is a function, ignored otherwise). If n is missing but subpops is not, n is taken to be the length of subpops.
loci_on_cols	If TRUE, X has loci on columns and individuals on rows; if FALSE (default), loci are on rows and individuals on columns. Has no effect if X is a function. If X is a BEDMatrix object, loci_on_cols is ignored (set automatically to TRUE internally).
mem_factor	Proportion of available memory to use loading and processing genotypes. Ignored if mem_lim is not NA.
mem_lim	Memory limit in GB, used to break up genotype data into chunks for very large datasets. Note memory usage is somewhat underestimated and is not controlled strictly. Default in Linux and Windows is mem_factor times the free system memory, otherwise it is 1GB (OSX and other systems).
want_M	If TRUE, includes the matrix M of non-missing pair counts in the return value, which are sample sizes that can be useful in modeling the variance of estimates. Default FALSE is to return the kinship matrix only.
m_chunk_max	Sets the maximum number of loci to process at the time. Actual number of loci loaded may be lower if memory is limiting.

### Details

The subpopulation assignments are only used to estimate the baseline kinship (the zero value). If the user wants to re-estimate the kinship matrix using different subpopulation labels, it suffices to rescale it using [rescale\\_popkin\(\)](#) (as opposed to starting from the genotypes again, which gives the same answer but more slowly).

### Value

If want\_M = FALSE, returns the estimated n-by-n kinship matrix only. If X has names for the individuals, they will be copied to the rows and columns of this kinship matrix. If want\_M = TRUE, a named list is returned, containing:

- kinship: the estimated n-by-n kinship matrix
- M: the n-by-n matrix of non-missing pair counts (see want\_M option).

### See Also

[popkin\\_af\(\)](#) for coancestry estimation from allele frequency matrices.

### Examples

```
# Construct toy data
X <- matrix(
  c(0, 1, 2,
    1, 0, 1,
    1, 0, 2),
  nrow = 3,
  byrow = TRUE
) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals
```

```
# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

kinship <- popkin(X, subpops) # calculate kinship from genotypes and subpopulation labels
```

---

popkin\_A

---

*Compute popkin's A and M matrices from genotypes*


---

### Description

This function returns lower-level, intermediate calculations for the main popkin function. These are not intended for most users, but rather for researchers studying the estimator.

### Usage

```
popkin_A(
  X,
  n = NA,
  loci_on_cols = FALSE,
  mem_factor = 0.7,
  mem_lim = NA,
  m_chunk_max = 1000
)
```

### Arguments

X	Genotype matrix, BEDMatrix object, or a function $X(m)$ that returns the genotypes of all individuals at $m$ successive locus blocks each time it is called, and NULL when no loci are left. If a regular matrix, X must have values only in $c(0, 1, 2, NA)$ , encoded to count the number of reference alleles at the locus, or NA for missing data.
n	Number of individuals (required only when X is a function, ignored otherwise). If n is missing but subpops is not, n is taken to be the length of subpops.
loci_on_cols	If TRUE, X has loci on columns and individuals on rows; if FALSE (default), loci are on rows and individuals on columns. Has no effect if X is a function. If X is a BEDMatrix object, loci_on_cols is ignored (set automatically to TRUE internally).
mem_factor	Proportion of available memory to use loading and processing genotypes. Ignored if mem_lim is not NA.
mem_lim	Memory limit in GB, used to break up genotype data into chunks for very large datasets. Note memory usage is somewhat underestimated and is not controlled strictly. Default in Linux and Windows is mem_factor times the free system memory, otherwise it is 1GB (OSX and other systems).

`m_chunk_max` Sets the maximum number of loci to process at the time. Actual number of loci loaded may be lower if memory is limiting.

### Value

A named list containing:

- A: n-by-n matrix, for individuals  $j$  and  $k$ , of average  $(x_{ij} - 1) * (x_{ik} - 1) - 1$  values across all loci  $i$  in  $X$
- M: n-by-n matrix of sample sizes (number of loci with non-missing individual  $j$  and  $k$  pairs, used to normalize A)

### See Also

The main `popkin()` function (a wrapper of this `popkin_A` function and `popkin_A_min_subpops()` to estimate the minimum A value).

### Examples

```
# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow = 3, byrow = TRUE) # genotype matrix

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
# library(BEDMatrix)
# X <- BEDMatrix(file) # load genotype matrix object

obj <- popkin_A(X) # calculate A and M from genotypes
A <- obj$A
M <- obj$M
```

---

popkin\_af

*Estimate coancestry from an allele frequency matrix and subpopulation assignments*

---

### Description

Given the individual-specific allele frequencies of  $n$  individuals, this function returns the  $n$ -by- $n$  coancestry matrix. This function is the analog of `popkin()` for allele frequencies rather than genotypes, and as a consequence estimates coancestry instead of kinship. These coancestry estimates are unbiased if the true allele frequencies are provided, but may be less accurate when the allele frequencies themselves are estimated. This function is intended for cases where allele frequencies, but not individual genotypes, are available; otherwise it is best to use the individual genotypes and `popkin()`. An application of interest is the allele frequency matrices from admixture models, in which case the columns correspond to subpopulations rather than individuals, and `subpops = NULL` is an acceptable choice.

**Usage**

```
popkin_af(
  P,
  subpops = NULL,
  loci_on_cols = FALSE,
  mem_factor = 0.7,
  mem_lim = NA,
  want_M = FALSE,
  m_chunk_max = 1000
)
```

**Arguments**

P	m-by-n matrix of individual-specific allele frequencies, which should have values between [0, 1] (range is not strictly required) or NA for missing data.
subpops	The length-n vector of subpopulation assignments for each individual. If NULL, every individual is effectively treated as a different population.
loci_on_cols	If TRUE, P has loci on columns and individuals on rows; if FALSE (default), loci are on rows and individuals on columns.
mem_factor	Proportion of available memory to use loading and processing loci. Ignored if mem_lim is not NA.
mem_lim	Memory limit in GB, used to break up P into chunks for very large datasets. Note memory usage is somewhat underestimated and is not controlled strictly. Default in Linux and Windows is mem_factor times the free system memory, otherwise it is 1GB (OSX and other systems).
want_M	If TRUE, includes the matrix M of non-missing pair counts in the return value, which are sample sizes that can be useful in modeling the variance of estimates. Default FALSE is to return the coancestry matrix only.
m_chunk_max	Sets the maximum number of loci to process at the time. Actual number of loci loaded may be lower if memory is limiting.

**Value**

If want\_M = FALSE, returns the estimated n-by-n coancestry matrix only. If P has names for the individuals, they will be copied to the rows and columns of this coancestry matrix. If want\_M = TRUE, a named list is returned, containing:

- coancestry: the estimated n-by-n coancestry matrix
- M: the n-by-n matrix of non-missing pair counts (see want\_M option).

**See Also**

[popkin\(\)](#) for kinship estimation from genotype matrices.

**Examples**

```
# a matrix of random uniform allele frequencies
# (unstructured, unlike real data)
P <- matrix( runif( 9 ), nrow = 3 )

coancestry <- popkin_af( P )
```

---

popkin\_A\_min\_subpops    *Estimate the minimum expected value of a matrix A using subpopulations*

---

**Description**

This function averages the values of a square matrix A between every subpopulation pair and returns the minimum of these averages. If no subpopulation partition is provided, the function returns the minimum value of A excluding the diagonal, to agree when the code treats each individual as a subpopulation. The return value can be used to adjust an A matrix to yield the kinship matrix.

**Usage**

```
popkin_A_min_subpops(A, subpops = NULL)
```

**Arguments**

A	A symmetric n-by-n matrix with values between every individual pair, including self comparisons.
subpops	A length-n vector of subpopulation assignments for each individual. If missing, every individual is treated as a different subpopulation.

**Value**

The minimum of the average between-subpopulation A values, which estimates the minimum expected value of A

**See Also**

[popkin\\_A\(\)](#) to generate the A matrix usually inputted into this function (popkin\_A\_min\_subpops). [popkin\(\)](#) is the wrapper function around both of these.

[avg\\_kinship\\_subpops\(\)](#) for the full matrix of mean kinship values between subpopulations.

**Examples**

```

# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# calculate A from genotypes
A <- popkin_A(X)$A

# the recommended form using appropriate subpopulation labels
A_min_est <- popkin_A_min_subpops( A, subpops )

# this recovers the popkin estimate
kinship <- 1 - A / A_min_est
stopifnot( kinship == popkin( X, subpops ) )

# a simple default for exploratory analysis, equals min( A ) for correctly-calculated A
A_min_est <- popkin_A_min_subpops( A )
stopifnot( A_min_est == min( A ) )

```

pwfst

*Estimate the individual-level pairwise FST matrix***Description**

This function constructs the individual-level pairwise FST matrix implied by the input kinship matrix. If the input is the true kinship matrix, the return value corresponds to the true pairwise FST matrix. On the other hand, if the input is the estimated kinship returned by `popkin()`, the same code results in the return value being the pairwise FST estimates described in our paper. In all cases the diagonal of the pairwise FST matrix is zero by definition.

**Usage**

```
pwfst(kinship)
```

**Arguments**

kinship            The n-by-n kinship matrix

**Value**

The n-by-n pairwise FST matrix

**Examples**

```

# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# estimate the kinship matrix from the genotypes "X"!
kinship <- popkin(X, subpops) # calculate kinship from X and optional subpop labels

# lastly, compute pairwise FST matrix from the kinship matrix
pwF <- pwfst(kinship)

```

---

rescale\_popkin

*Rescale kinship matrix to set a given kinship value to zero.*


---

**Description**

If you already have a population kinship matrix, and you desire to estimate the kinship matrix in a subset of the individuals, you could do it the slow way (reestimating starting from the genotypes of the subset of individuals) or you can do it the fast way: first subset the kinship matrix to only contain the individuals of interest, then use this function to rescale this kinship matrix so that the minimum kinship is zero. This rescaling is required when subsetting results in a more recent Most Recent Common Ancestor (MRCA) population compared to the original dataset (for example, if the original data had individuals from across the world but the subset only contains individuals from a single continent).

**Usage**

```
rescale_popkin(kinship, subpops = NULL, min_kinship = NA)
```

**Arguments**

kinship	An n-by-n kinship matrix.
subpops	The length-n vector of subpopulation assignments for each individual.
min_kinship	A scalar kinship value to define the new zero kinship.

**Details**

This function rescales the input kinship matrix so that the value `min_kinship` in the original kinship matrix becomes zero, using the formula  $\text{kinship}_{\text{rescaled}} = (\text{kinship} - \text{min\_kinship}) / (1 - \text{min\_kinship})$ . This is equivalent to changing the ancestral population of the data. If subpopulation labels `subpops` are provided (recommended), they are used to estimate `min_kinship`

using the function `popkin_A_min_subpops()`, which is the recommended way to set the MRCA population correctly. If both `subpops` and `min_kinship` are provided, only `min_kinship` is used. If both `subpops` and `min_kinship` are omitted, the function sets `min_kinship = min(kinship)`.

### Value

The rescaled n-by-n kinship matrix, with the desired level of relatedness set to zero.

### Examples

```
# Construct toy data
X <- matrix(c(0,1,2,1,0,1,1,0,2), nrow=3, byrow=TRUE) # genotype matrix
subpops <- c(1,1,2) # subpopulation assignments for individuals
subpops2 <- 1:3 # alternate labels treat every individual as a different subpop

# NOTE: for BED-formatted input, use BEDMatrix!
# "file" is path to BED file (excluding .bed extension)
## library(BEDMatrix)
## X <- BEDMatrix(file) # load genotype matrix object

# suppose we first estimate kinship without subpopulations, which will be more biased
kinship <- popkin(X) # calculate kinship from genotypes, WITHOUT subpops
# then we visualize this matrix, figure out a reasonable subpopulation partition

# now we can adjust the kinship matrix!
kinship2 <- rescale_popkin(kinship, subpops)
# prev is faster but otherwise equivalent to re-estimating kinship from scratch with subpops:
# kinship2 <- popkin(X, subpops)

# can also manually set the level of relatedness min_kinship we want to be zero:
min_kinship <- min(kinship) # a naive choice for example
kinship2 <- rescale_popkin(kinship, min_kinship = min_kinship)

# lastly, omitting both subpops and min_kinship sets the minimum value in kinship to zero
kinship3 <- rescale_popkin(kinship2)
# equivalent to both of:
# kinship3 <- popkin(X)
# kinship3 <- rescale_popkin(kinship2, min_kinship = min(kinship))
```

---

validate\_kinship

*Validate a kinship matrix*

---

### Description

Tests that the input is a valid kinship matrix (a numeric, square, and optionally symmetric R matrix). Intended for matrices to plot and for other uses, including biased estimates, so there is flexibility as to what constitutes a valid kinship matrix. Throws errors if the input is not as above. Can instead return TRUE/FALSE if `logical = TRUE`.

**Usage**

```
validate_kinship(kinship, sym = TRUE, name = "kinship", logical = FALSE)
```

**Arguments**

kinship	The kinship matrix to validate.
sym	If TRUE (default), the matrix is required to be symmetric. Otherwise this particular test is skipped.
name	Default "kinship". Change to desired variable name for more informative error messages (i.e. "A" when used to validate the A matrix inside popkin_A_min_subpops).
logical	If FALSE (default), function stops with an error message if the input is not a kinship matrix. If TRUE, function instead returns TRUE if the input passed all tests (appears to be a valid kinship matrix) or FALSE otherwise.

**Details**

True kinship matrices have values strictly between 0 and 1, and diagonal values strictly between 0.5 and 1. However, estimated matrices may contain values slightly out of range. For greater flexibility, this function does not check for out-of-range values.

**Value**

If `logical = FALSE` (default), nothing. If `logical = TRUE`, returns TRUE if the input is a valid kinship matrix, FALSE otherwise.

**Examples**

```
# this is a valid (positive) example
kinship <- matrix(c(0.5, 0, 0, 0.6), nrow=2)
# this will run without errors or warnings
validate_kinship(kinship)

# negative examples

# dies if input is missing
try( validate_kinship() )

# and if input is not a matrix
try( validate_kinship( 1:5 ) )

# and for non-numeric matrices
char_mat <- matrix(c('a', 'b', 'c', 'd'), nrow=2)
try( validate_kinship( char_mat ) )

# and non-square matrices
non_kinship <- matrix(1:2, nrow=2)
try( validate_kinship( non_kinship ) )

# and non-symmetric matrices
non_kinship <- matrix(1:4, nrow=2)
```

```

try( validate_kinship( non_kinship ) )
# but example passes if we drop symmetry requirement this way
validate_kinship( non_kinship, sym = FALSE )

# instead of stopping, can get a logical value
# this returns FALSE
validate_kinship( non_kinship, logical = TRUE )

```

---

weights\_subpops

*Get weights for individuals that balance subpopulations*


---

### Description

This function returns positive weights that sum to one for individuals using subpopulation labels, such that every subpopulation receives equal weight. In particular, if there are  $K$  subpopulations, then the sum of weights for every individuals of a given subpopulation will equal  $1 / K$ . The weight of every individual is thus inversely proportional to the number of individuals in its subpopulation. If the optional sub-subpopulation labels are also provided, then each sub-subpopulation within a given subpopulation is also weighted equally.

### Usage

```
weights_subpops(subpops, subsubpops = NULL)
```

### Arguments

subpops	The length- $n$ vector of subpopulation assignments for each individual.
subsubpops	The optional length- $n$ vector of sub-subpopulation assignments for each individual. Each sub-subpopulation must belong to a single subpopulation (a nested hierarchy) or an error is produced.

### Value

The length- $n$  vector of weights for each individual.

### Examples

```

# if every individual has a different subpopulation, weights are uniform:
subpops <- 1:10
weights <- weights_subpops( subpops )
stopifnot( all( weights == rep.int( 1/10, 10 ) ) )

# subpopulations can be strings too
subpops <- c('a', 'b', 'c')
weights <- weights_subpops( subpops )
stopifnot( all( weights == rep.int( 1/3, 3 ) ) )

# if there are two subpopulations

```

```
# and the first has twice as many individuals as the second
# then the individuals in this first subpopulation weight half as much
# as the ones in the second subpopulation
subpops <- c(1, 1, 2)
weights <- weights_subpops( subpops )
stopifnot( all( weights == c( 1/4, 1/4, 1/2 ) ) )

# 2-level hierarchy example
subpops <- c(1, 1, 1, 2, 2)
subsubpops <- c('a', 'b', 'b', 'c', 'd')
weights <- weights_subpops( subpops, subsubpops )
stopifnot( all( weights == c( 1/4, 1/8, 1/8, 1/4, 1/4 ) ) )
```

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