

Package ‘qLearn’

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Type Package

Title Estimation and inference for Q-learning

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Description Functions to implement Q-learning for estimating optimal dynamic treatment regimes from two stage sequentially randomized trials, and to perform inference via m-out-of-n bootstrap for parameters indexing the optimal regime.

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chooseMDoubleBootstrap	<i>Choose the bootstrap sample size for stage 1 inference</i>
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Description

Choose the resample size for stage 1 bootstrap using double bootstrap. The form of m is: $m = n \frac{1+Xi(1-p\hat{H}at)}{1+Xi}$, where the tuning parameter Xi is chosen via double bootstrap and $p\hat{H}at$ is the estimated non-regularity level computed by `getModel`. Example could be found under [qLearn](#).

Usage

```
chooseMDoubleBootstrap(s2Formula,s1Formula,
  completeData,s2Treat,interact,s2Indicator,alpha=0.05,
  boot1Num=500,boot2Num=500,...)
```

Arguments

s2Formula	stage 2 regression formula
s1Formula	Stage 1 regression formula
completeData	data frame containing all the variables
s2Treat	character string: name of the stage 2 treatment variable
interact	character vector: names of variables that interact with s2Treat
s2Indicator	character string: names of the stage 2 treatment indicator variable
alpha	level of significance
boot1Num	numbers of bootstrap sampling for first order bootstrap
boot2Num	numbers of bootstrap sampling for second order bootstrap
...	other arguments of the <code>lm</code> function

Value

m	resample size for stage 1 bootstrap
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References

Chakraborty, B., and Laber, E.B. (2012). Inference for Optimal Dynamic Treatment Regimes using an Adaptive m-out-of-n Bootstrap Scheme. *Submitted*.

See Also

[qLearn](#)

Examples

```
set.seed(100)
# Simple Simulation on 1000 subjects
sim<-matrix(0,nrow=1000,ncol=7)
colnames(sim)<-c("H1","A1","Y1","H2","A2","Y2","IS2")
sim<-as.data.frame(sim)

# Randomly generate stage 1 covariates and stage 1 and 2 treatments
sim[,c("H1","A1","A2")<-2*rbinom(1000*3,1,0.5)-1

# Generate stage 2 covariates based on H1 and T1
expit<-exp(0.5*sim$H1+0.5*sim$A1)/(1+exp(0.5*sim$H1+0.5*sim$A1))
sim$H2<-2*rbinom(1000,1,expit)-1

# Assume stage 1 outcome Y1 is 0
# Generate stage 2 outcome Y2
sim$Y2<-0.5*sim$A2+0.5*sim$A2*sim$A1-0.5*sim$A1+rnorm(1000)

# Randomly assign 500 subjects to S2
sim[sample(1000,500),"IS2"]<-1
sim[sim$IS2==0,c("A2","Y2")<-NA

# Define models for both stages
s2Formula<-Y2~H1*A1+A1*A2+A2:H2
s1Formula<-Y1~H1*A1

# Use boot1Num=boot2Num=20 in the example to save computational time
# In real case should use greater number
m<-chooseMDoubleBootstrap(s2Formula,s1Formula,sim,s2Treat="A2",
  interact=c("A1","H2"),s2Indicator="IS2",boot1Num=20,boot2Num=20)
```

getModel

Compute the regression coefficients for both stages

Description

getModel computes the regression coefficients for both stages. For stage 1 regression, pseudo-outcomes are constructed based on stage 2 coefficients. Additionally it outputs the standard outputs of the `lm` function; however, the inference for stage 1 parameters based on these outputs is invalid due to non-regularity. Example could be found under [qLearn](#).

Usage

```
getModel(s2Formula,s1Formula,completeData,
  s2Treat,interact,s2Indicator,...)
```

Arguments

s2Formula	stage 2 regression formula
s1Formula	Stage 1 regression formula
completeData	data frame containing all the variables
s2Treat	character string: name of the stage 2 treatment variable
interact	character vector: names of variables that interact with s2_treat
s2Indicator	character string: names of the stage 2 treatment indicator variable
...	other arguments of the lm function

Value

A list containing:

s2Model	stage2 regression model
s1Model	stage1 regression model
pHat	estimated non-regularity level

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References

Chakraborty, B., and Laber, E.B. (2012). Inference for Optimal Dynamic Treatment Regimes using an Adaptive m-out-of-n Bootstrap Scheme. *Submitted*.

See Also

[qLearn](#)

Examples

```
set.seed(100)
# Simple Simulation on 1000 subjects
sim<-matrix(0,nrow=1000,ncol=7)
colnames(sim)<-c("H1","A1","Y1","H2","A2","Y2","IS2")
sim<-as.data.frame(sim)

# Randomly generate stage 1 covariates and stage 1 and 2 treatments
sim[,c("H1","A1","A2")]<-2*rbinom(1000*3,1,0.5)-1

# Generate stage 2 covariates based on H1 and T1
expit<-exp(0.5*sim$H1+0.5*sim$A1)/(1+exp(0.5*sim$H1+0.5*sim$A1))
sim$H2<-2*rbinom(1000,1,expit)-1

# Assume stage 1 outcome Y1 is 0
# Generate stage 2 outcome Y2
```

```

sim$Y2<-0.5*sim$A2+0.5*sim$A2*sim$A1-0.5*sim$A1+rnorm(1000)

# Randomly assign 500 subjects to S2
sim[sample(1000,500),"IS2"]<-1
sim[sim$IS2==0,c("A2","Y2")]<-NA

# Define models for both stages
s2Formula<-Y2~H1*A1+A1*A2+A2:H2
s1Formula<-Y1~H1*A1

## Fit model for both stages
getModel(s2Formula,s1Formula,sim,s2Treat="A2",interact=c("A1","H2"),
s2Indicator="IS2")

```

qLearn

Based on the input contrast vectors, compute point estimates and construct confidence intervals using bootstrap for both stages

Description

Suppose the goal is to find the point estimates and CIs for stage 1 and stage 2 contrasts $C_1^T \theta_1$ and $C_2^T \theta_2$. Given C_1 , C_2 , regular n-out-of-n bootstrap will be used in stage 2 and different bootstrap scheme can be used in stage 1 analysis by assigning different value to s1Method. "Fixed Xi" will fix the Xi value as fixedXi and calculate the corresponding m; "Double Bootstrap" will calculate m using double bootstrap method; and the default "Regular" will skip choosing m and go with a regular bootstrap. Also m can be specified in s1M if not using "Fixed Xi" or "Double Bootstrap"

Usage

```

qLearn(s2Formula,s1Formula,completeData,
s2Treat,interact,s2Indicator,s2Contrast,s1Contrast,
alpha=0.05,bootNum=1000,s1Method="Regular",fixedXi,
doubleBoot1Num=500,doubleBoot2Num=500,s1M,...)

```

Arguments

s2Formula	stage 2 regression formula
s1Formula	Stage 1 regression formula
completeData	data frame containing all the variables
s2Treat	character string: name of the stage 2 treatment variable
interact	character vector: names of variables that interact with s2Treat
s2Indicator	character string: names of the stage 2 treatment indicator variable
s2Contrast	contrast for the stage 2 coefficients
s1Contrast	contrast for the stage 1 coefficients
alpha	level of significance

<code>bootNum</code>	numbers of bootstrap sampling in constructing CIs
<code>s1Method</code>	character string: method to choose stage 1 bootstrap sample size, <code>m</code> ; "Double Bootstrap" will calculate <code>m</code> using double bootstrap method; "Fixed Xi" will fix the <code>Xi</code> value and calculate the corresponding <code>m</code> ; "Regular" will use a regular <code>n</code> -out-of- <code>n</code> bootstrap for stage 1.
<code>fixedXi</code>	fixed <code>xi</code> value if <code>s1Method</code> ="Fixed Xi"
<code>doubleBoot1Num</code>	numbers of bootstrap sampling for first order bootstrap if <code>s1Method</code> ="Double Bootstrap"
<code>doubleBoot2Num</code>	numbers of bootstrap sampling for second order bootstrap if <code>s1Method</code> ="Double Bootstrap"
<code>s1M</code>	specify <code>m</code> if necessary
<code>...</code>	other arguments of the <code>lm</code> function

Value

A list containing:

<code>s1Coefficients</code>	stage 1 regression coefficients
<code>s2Coefficients</code>	stage 2 regression coefficients
<code>s1Inference</code>	stage 1 coefficients confidence interval based on stage1 contrast
<code>s2Inference</code>	stage 2 coefficients confidence interval based on stage2 contrast
<code>s1Size</code>	stage 1 bootstrap sample size

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References

Chakraborty, B., and Laber, E.B. (2012). Inference for Optimal Dynamic Treatment Regimes using an Adaptive `m`-out-of-`n` Bootstrap Scheme. *Submitted*.

See Also

[getModel chooseMDoubleBootstrap](#)

Examples

```
set.seed(100)
# Simple Simulation on 1000 subjects
sim<-matrix(0,nrow=1000,ncol=7)
colnames(sim)<-c("H1","A1","Y1","H2","A2","Y2","IS2")
sim<-as.data.frame(sim)
```

```
# Randomly generate stage 1 covariates and stage 1 and 2 treatments
sim[,c("H1", "A1", "A2")]<-2*rbinom(1000*3,1,0.5)-1

# Generate stage 2 covariates based on H1 and T1
expit<-exp(0.5*sim$H1+0.5*sim$A1)/(1+exp(0.5*sim$H1+0.5*sim$A1))
sim$H2<-2*rbinom(1000,1,expit)-1

# Assume stage 1 outcome Y1 is 0
# Generate stage 2 outcome Y2
sim$Y2<-0.5*sim$A2+0.5*sim$A2*sim$A1-0.5*sim$A1+rnorm(1000)

# Randomly assign 500 subjects to S2
sim[sample(1000,500),"IS2"]<-1
sim[sim$IS2==0,c("A2", "Y2")]<-NA

# Define models for both stages
s2Formula<-Y2~H1*A1+A1*A2+A2:H2
s1Formula<-Y1~H1*A1

## Fixed Xi as 0.05
qLearn(s2Formula,s1Formula,sim,s2Treat="A2",interact=c("A1", "H2"),
s2Indicator="IS2",s1Method="Fixed Xi",fixedXi=0.05,bootNum=100)
```

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