

# Package ‘quad’

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**Type** Package

**Title** Exact permutation moments of quadratic form statistics

**Version** 1.0

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**Imports** PearsonDS

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**Description** This package gives you the exact first four permutation moments for the most commonly used quadratic form statistics, which need not be positive definite. The extension of this work to quadratic forms greatly expands the utility of density approximations for these problems, including for high-dimensional applications, where the statistics must be extreme in order to exceed stringent testing thresholds. Approximate p-values are obtained by matching the exact moments to the Pearson family of distributions using the PearsonDS package.

**License** GPL (>= 2)

**LazyLoad** yes

**NeedsCompilation** no

**Repository** CRAN

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quad-package

*This package gives the exact the first four moments of any quadratic form and its corresponding p-values.*

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### Description

The Mantel and Knox space-time clustering statistics are popular tools to establish transmissibility of a disease and detect outbreaks. The most commonly used null distributional approximations may provide poor fits, and researchers often resort to direct sampling from the permutation distribution. However, the exact first four moments for these statistics are available, and Pearson distributional approximations are often effective. Thus, our first goals are to clarify the literature and make these tools more widely available. In addition, by rewriting terms in the statistics, we obtain the exact first four permutation moments for the most commonly used quadratic form statistics, which need not be positive definite. The extension of this work to quadratic forms greatly expands the utility of density approximations for these problems, including for high-dimensional applications, where the statistics must be extreme in order to exceed stringent testing thresholds.

### Details

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License: GPL (>= 2)

### Author(s)

Yi-Hui Zhou

Maintainer: Yi-Hui Zhou <yihui\_zhou@ncsu.edu>

### References

YH Zhou, G Mayhew, Z Sun, X Xu, F Zou, FA Wright, 2013 *Space-time clustering and the permutation moments of quadratic forms*, Stat 2(1), 292-302

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lincombfun

*linear combination function*

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### Description

This is a prestep function for *momentfun*

**Usage**

```
lincombfun(S,mycoef)
```

**Arguments**

S                    S is a list of sums output from the sum function  
mycoef              global coefficients for the linear combination function

**References**

YH Zhou, G Mayhew, Z Sun, X Xu, F Zou, FA Wright, 2013 *Space-time clustering and the permutation moments of quadratic forms*, Stat 2(1), 292-302

**See Also**

[coef](#), [sumfun](#), [momentfun](#).

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momentfun	<i>Generate the first four exact permutation moments of quadratic form statistics.</i>
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**Description**

For symmetric  $C$  and  $D$  (with zero diagonals), we implement the Siemiatycki moment computation.

**Usage**

```
momentfun(Px, Py, n, mycoef)
```

**Arguments**

Px                    list of linear combinations  
Py                    list of linear combinations  
n                     sample size  $n$  has to be at least 8.  
mycoef                global coefficients we need for the function.

**Value**

first                 first permutation moment of quadratic form  
second                second permutation moment  
third                 third permutation moment  
fourth                fourth permutation moment

**References**

YH Zhou, G Mayhew, Z Sun, X Xu, F Zou, FA Wright, 2013 *Space-time clustering and the permutation moments of quadratic forms*, Stat 2(1), 292-302

**See Also**

[quadp](#), [lincombfun](#).

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mycoef

*Global variables for several main functions.*

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**Description**

We need the global variables to generate the linear combination function.

**Usage**

data(mycoef)

**Details**

It gives all the global variables

**References**

YH Zhou, G Mayhew, Z Sun, X Xu, F Zou, FA Wright, 2013 *Space-time clustering and the permutation moments of quadratic forms*, Stat 2(1), 292-302

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quadp

*This function provides you the pvalue based on the Pearson Family distribution.*

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**Description**

Main function of this package. It returns the pvalue of the quadratic form statistics.

**Usage**

quadp(y, A, mycoef)

**Arguments**

y                    y is the vector in quadratic form  $y^T A y$   
 A                    A is the symmetric matrix  
 mycoef            global variables

**Details**

This is the main function in the package. It returns the test statistics of the quadratic form and its corresponding p value using Pearson family for the fitting.

**Value**

stat            test statistics value  
p                pvalue based on the Pearson family fitting using the exact four moments

**Author(s)**

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**See Also**

[lincombfun](#), [sumfun](#)

**Examples**

```
##### m is the dimension of the A matrix, n is the length of y        ##
##### no row/column of A can be all constant, as this is degenerate and creates problems.
library(PearsonDS)

m=15
n=20
set.seed(1)
x=matrix(rnorm(m*n),m,n) # just an example
y=rnorm(n)
A=t(x-rowMeans(x))
data(mycoef)
##### The code below assumes that y and A have been presepecified or otherwise preloaded
#result=quadp(y,A,mycoef)
#print(result)
```

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sumfun

*Get Sum*

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**Description**

This is a prestep function for *momentfun*

**Usage**

```
sumfun(W)
```

**Arguments**

W                mid step for generating linear combination function

**References**

YH Zhou, G Mayhew, Z Sun, X Xu, F Zou, FA Wright, 2013 *Space-time clustering and the permutation moments of quadratic forms*, Stat 2(1), 292-302

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