Package ‘rdrobust’

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Type        Package
Title       Robust Data-Driven Statistical Inference in Regression-Discontinuity Designs
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Description Regression-discontinuity (RD) designs are quasi-experimental research designs popu-
              lar in social, behavioral and natural sciences. The RD design is usually em-
              ployed to study the (local) causal effect of a treatment, intervention or policy. This package pro-
              vides tools for data-driven graphical and analytical statistical inference in RD
designs: rdrobust() to construct local-polynomial point estimators and robust confidence inter-
vals for average treatment effects at the cutoff in Sharp, Fuzzy and Kink RD settings, rdbwse-
lect() to perform bandwidth selection for the different procedures implemented, and rd-
plot() to conduct exploratory data analysis (RD plots).

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Regression-discontinuity (RD) designs are quasi-experimental research designs popular in social, behavioral and natural sciences. The RD design is usually employed to study the (local) causal effect of a treatment, intervention or policy. This package provides tools for data-driven graphical and analytical statistical inference in RD designs: \texttt{rdrobust} to construct local-polynomial point estimators and robust confidence intervals for average treatment effects at the cutoff in Sharp, Fuzzy and Kink RD settings, \texttt{rdbwselect} to perform bandwidth selection for the different procedures implemented, and \texttt{rdplot} to conduct exploratory data analysis (RD plots).

**Details**

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Function for statistical inference: \texttt{rdrobust}
Function for bandwidth selection: \texttt{rdbwselect}
Function for exploratory data analysis (RD plots): \texttt{rdplot}

**Author(s)**

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\texttt{rdbwselect} implements bandwidth selectors for local polynomial Regression Discontinuity (RD) point estimators and inference procedures developed in Calonico, Cattaneo and Titiunik (2014a),
rdbwselect


Companion commands are: rdrobust for point estimation and inference procedures, and rdplot for data-driven RD plots (see Calonico, Cattaneo and Titiunik (2015a) for details).

A detailed introduction to this command is given in Calonico, Cattaneo and Titiunik (2015b) and Calonico, Cattaneo, Farrell and Titiunik (2019). A companion Stata package is described in Calonico, Cattaneo and Titiunik (2014b).

For more details, and related Stata and R packages useful for analysis of RD designs, visit https://rdpackages.github.io/

Usage

rdbwselect(y, x, c = NULL, fuzzy = NULL, deriv = NULL, p = NULL, q = NULL, covs = NULL, covs_drop = TRUE, kernel = "tri", weights = NULL, bwselect = "mserd", vce = "nn", cluster = NULL, nnmatch = 3, scaleregul = 1, sharpbw = FALSE, all = NULL, subset = NULL, masspoints = "adjust", bwcheck = NULL, bwrestrict = TRUE, stdvars = FALSE)

Arguments

y is the dependent variable.

x is the running variable (a.k.a. score or forcing variable).

c specifies the RD cutoff in x; default is c = 0.

fuzzy specifies the treatment status variable used to implement fuzzy RD estimation (or Fuzzy Kink RD if deriv=1 is also specified). Default is Sharp RD design and hence this option is not used.

deriv specifies the order of the derivative of the regression functions to be estimated. Default is deriv=0 (for Sharp RD, or for Fuzzy RD if fuzzy is also specified). Setting deriv=1 results in estimation of a Kink RD design (up to scale), or Fuzzy Kink RD if fuzzy is also specified.

p specifies the order of the local-polynomial used to construct the point-estimator; default is p = 1 (local linear regression).

q specifies the order of the local-polynomial used to construct the bias-correction; default is q = 2 (local quadratic regression).

covs specifies additional covariates to be used for estimation and inference.

covs_drop if TRUE, it checks for collinear additional covariates and drops them. Default is TRUE.

kernel is the kernel function used to construct the local-polynomial estimator(s). Options are triangular (default option), epanechnikov and uniform.

weights is the variable used for optional weighting of the estimation procedure. The unit-specific weights multiply the kernel function.
bwselect specifies the bandwidth selection procedure to be used. Options are:
- mserr one common MSE-optimal bandwidth selector for the RD treatment effect estimator.
- msetwo two different MSE-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
- msesum one common MSE-optimal bandwidth selector for the sum of regression estimates (as opposed to difference thereof).
- msecomb1 for min(mserr, msesum).
- msecomb2 for median(msetwo, mserr, msesum), for each side of the cutoff separately.
- cerrd one common CER-optimal bandwidth selector for the RD treatment effect estimator.
- certwo two different CER-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
-cersum one common CER-optimal bandwidth selector for the sum of regression estimates (as opposed to difference thereof).
- cercomb1 for min(cerrd, cersum).
- cercomb2 for median(certwo, cerrd, cersum), for each side of the cutoff separately.

Note: MSE = Mean Square Error; CER = Coverage Error Rate. Default is bwselect=mserr. For details on implementation see Calonico, Cattaneo and Titiunik (2014a), Calonico, Cattaneo and Farrell (2018), and Calonico, Cattaneo, Farrell and Titiunik (2017), and the companion software articles.

vce specifies the procedure used to compute the variance-covariance matrix estimator. Options are:
- nn for heteroskedasticity-robust nearest neighbor variance estimator with nnmatch the (minimum) number of neighbors to be used.
- hc0 for heteroskedasticity-robust plug-in residuals variance estimator without weights.
- hc1 for heteroskedasticity-robust plug-in residuals variance estimator with hc1 weights.
- hc2 for heteroskedasticity-robust plug-in residuals variance estimator with hc2 weights.
- hc3 for heteroskedasticity-robust plug-in residuals variance estimator with hc3 weights.

Default is vce=nn.

cluster indicates the cluster ID variable used for cluster-robust variance estimation with degrees-of-freedom weights. By default it is combined with vce=nn for cluster-robust nearest neighbor variance estimation. Another option is plug-in residuals combined with vce=hc0.

nnmatch to be combined with for vce=nn for heteroskedasticity-robust nearest neighbor variance estimator with nnmatch indicating the minimum number of neighbors to be used. Default is nnmatch=3

scaleregul specifies scaling factor for the regularization term added to the denominator of the bandwidth selectors. Setting scaleregul = 0 removes the regularization term from the bandwidth selectors; default is scaleregul = 1.
**rdbwselect**

- **sharpbw**: option to perform fuzzy RD estimation using a bandwidth selection procedure for the sharp RD model. This option is automatically selected if there is perfect compliance at either side of the threshold.
- **all**: if specified, `rdbwselect` reports all available bandwidth selection procedures.
- **subset**: an optional vector specifying a subset of observations to be used.
- **masspoints**: checks and controls for repeated observations in the running variable. Options are:
  1. **off**: ignores the presence of mass points;
  2. **check**: looks for and reports the number of unique observations at each side of the cutoff.
  3. **adjust**: controls that the preliminary bandwidths used in the calculations contain a minimal number of unique observations. By default it uses 10 observations, but it can be manually adjusted with the option `bwcheck`.
   Default option is `masspoints=adjust`.
- **bwcheck**: if a positive integer is provided, the preliminary bandwidth used in the calculations is enlarged so that at least `bwcheck` unique observations are used.
- **bwrestrict**: if TRUE, computed bandwidths are restricted to lie within the range of `x`; default is `bwrestrict = TRUE`.
- **stdvars**: if TRUE, `x` and `y` are standardized before computing the bandwidths; default is `stdvars = FALSE`.

**Value**

- **N**: vector with sample sizes to the left and to the right of the cutoff.
- **c**: cutoff value.
- **p**: order of the local-polynomial used to construct the point-estimator.
- **q**: order of the local-polynomial used to construct the bias-correction estimator.
- **bws**: matrix containing the estimated bandwidths for each selected procedure.
- **bwselect**: bandwidth selection procedure employed.
- **kernel**: kernel function used to construct the local-polynomial estimator(s).

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**References**


**See Also**

*rdrobust, rdplot*

**Examples**

```r
x<_spinner(1000,-1,1)
y<_spinner(5+3*x+2*(x>=0)+rnorm(1000))
rdbwselect(y,x)
```

---

**Description**

*rdbwselect_2014* is a deprecated command implementing three bandwidth selectors for local polynomial Regression Discontinuity (RD) point estimators and inference procedures, as described in Calonico, Cattaneo and Titiunik (2014).

This command is no longer supported or updated, and it is made available only for backward compatibility purposes. Please use *rdbwselect* instead.

The latest version of the rdrobust package includes the following commands: *rdrobust* for point estimation and inference procedures. *rdbwselect* for data-driven bandwidth selection. *rdplot* for data-driven RD plots.

For more details, and related Stata and R packages useful for analysis of RD designs, visit [https://rdpackages.github.io/](https://rdpackages.github.io/)
Usage

```r
rdbwselect_2014(y, x, subset = NULL, c = 0, p = 1, q = 2, deriv = 0,
    rho = NULL, kernel = "tri", bwselect = "CCT", scaleregul = 1,
    delta = 0.5, cvgrid_min = NULL, cvgrid_max = NULL,
    cvgrid_length = NULL, cvplot = FALSE, vce = "nn", matches = 3,
    all = FALSE, precalc = TRUE )
```

Arguments

- **y**: is the dependent variable.
- **x**: is the running variable (a.k.a. score or forcing variable).
- **subset**: an optional vector specifying a subset of observations to be used.
- **c**: specifies the RD cutoff in x; default is $c = 0$.
- **p**: specifies the order of the local-polynomial used to construct the point-estimator; default is $p = 1$ (local linear regression).
- **q**: specifies the order of the local-polynomial used to construct the bias-correction; default is $q = 2$ (local quadratic regression).
- **deriv**: specifies the order of the derivative of the regression function to be estimated; default is $deriv = 0$ (Sharp RD, or Fuzzy RD if `fuzzy` is also specified). Setting it equal to 1 results in estimation of a Kink RD design (or Fuzzy Kink RD if `fuzzy` is also specified).
- **rho**: if specified, sets the pilot bandwidth $b$ equal to $h/rho$, where $h$ is computed using the method and options chosen below.
- **kernel**: is the kernel function used to construct the local-polynomial estimator(s). Options are: triangular (default option), epanechnikov and uniform.
- **bwselect**: selects the bandwidth selection procedure to be used. By default it computes both $h$ and $b$, unless `rho` is specified, in which case it only computes $h$ and sets $b = h/rho$. Options are: CCT for bandwidth selector proposed by Calonico, Cattaneo and Titiunik (2014) (default option).
- **scaleregul**: specifies scaling factor for the regularization terms of CCT and IK bandwidth selectors. Setting `scaleregul = 0` removes the regularization term from the bandwidth selectors; default is $scaleregul = 1$.
- **delta**: sets the quantile that defines the sample used in the cross-validation procedure. This option is used only if bwselect(CV) is specified; default is $delta = 0.5$, that is, the median of the control and treated samples.
- **cvgrid_min**: sets the minimum value of the bandwidth grid used in the cross-validation procedure. This option is used only if bwselect = "CV" is specified.
- **cvgrid_max**: sets the maximum value of the bandwidth grid used in the cross-validation procedure. This option is used only if bwselect = "CV" is specified.
cvgrid_length sets the bin length of the (evenly-spaced) bandwidth grid used in the cross-validation procedure. This option is used only if bwselect = "CV" is specified.

cvplot generates a graph of the CV objective function. This option is used only if bwselect = "CV" is specified.

vce specifies the procedure used to compute the variance-covariance matrix estimator. This option is used only if CCT or IK bankdwith procedures are employed. Options are:

nn for nearest-neighbor matches residuals using matches number of matches. This is the default option (with matches = 3, see below).

resid for estimated plug-in residuals using h bandwidth.

matches specifies the number of matches in the nearest-neighbor based variance-covariance matrix estimator. This options is used only when nearest-neighbor matches residuals are employed; default is matches = 3.

all if specified, rdbwselect_2014 reports three different procedures:

CCT for bandwidth selector proposed by Calonico, Cattaneo and Titiunik (2014).

IK for bandwidth selector proposed by Imbens and Kalyanaraman (2012).

CV for cross-validation method proposed by Ludwig and Miller (2007).

precalc internal option.

Value

bws matrix containing the estimated bandwidths for each selected procedure.

bwselect bandwidth selection procedure employed.

kernel kernel function used to construct the local-polynomial estimator(s).

order of the local-polynomial used to construct the point-estimator.

q order of the local-polynomial used to construct the bias-correction estimator.

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References


See Also

rdrobust, rdplot
Examples

```r
x<-runif(1000,-1,1)
y<-5+3*x+2*(x>=0)+rnorm(1000)
rdbwselect_2014(y,x)
```

---

**Description**

`rdplot` implements several data-driven Regression Discontinuity (RD) plots, using either evenly-spaced or quantile-spaced partitioning. Two type of RD plots are constructed: (i) RD plots with binned sample means tracing out the underlying regression function, and (ii) RD plots with binned sample means mimicking the underlying variability of the data. For technical and methodological details see Calonico, Cattaneo and Titiunik (2015a).

Companion commands are: `rdrobust` for point estimation and inference procedures, and `rdbwselect` for data-driven bandwidth selection.

A detailed introduction to this command is given in Calonico, Cattaneo and Titiunik (2015b) and Calonico, Cattaneo, Farrell and Titiunik (2017). A companion Stata package is described in Calonico, Cattaneo and Titiunik (2014).

For more details, and related Stata and R packages useful for analysis of RD designs, visit [https://rdpackages.github.io/](https://rdpackages.github.io/)

**Usage**

```r
rdplot(y, x, c = 0, p = 4, nbins = NULL, binselect = "esmv", scale = NULL, kernel = "uni", weights = NULL, h = NULL, covs = NULL, covs_eval = 0, covs_drop = TRUE, support = NULL, subset = NULL, hide = FALSE, ci = NULL, shade = FALSE, title = NULL, x.label = NULL, y.label = NULL, x.lim = NULL, y.lim = NULL, col.dots = NULL, col.lines = NULL)
```

**Arguments**

- `y` is the dependent variable.
- `x` is the running variable (a.k.a. score or forcing variable).
- `c` specifies the RD cutoff in `x`; default is `c = 0`.
- `p` specifies the order of the global-polynomial used to approximate the population conditional mean functions for control and treated units; default is `p = 4`.
- `nbins` specifies the number of bins used to the left of the cutoff, denoted $J_-$, and to the right of the cutoff, denoted $J_+$, respectively. If not specified, $J_+$ and $J_-$ are estimated using the method and options chosen below.
binselect specifies the procedure to select the number of bins. This option is available only if $J_-$ and $J_+$ are not set manually. Options are:

- esnv: mimicking variance evenly-spaced method using spacings estimators. This is the default option.
- qs: IMSE-optimal quantile-spaced method using spacings estimators.
- qsmv: mimicking variance quantile-spaced method using spacings estimators.

scale specifies a multiplicative factor to be used with the optimal numbers of bins selected. Specifically, the number of bins used for the treatment and control groups will be $\text{scale} \times \hat{J}_+$ and $\text{scale} \times \hat{J}_-$, where $\hat{J}$ denotes the estimated optimal numbers of bins originally computed for each group; default is $\text{scale} = 1$.

kernel specifies the kernel function used to construct the local-polynomial estimator(s). Options are: triangular, epanechnikov, and uniform. Default is kernel=uniform (i.e., equal/no weighting to all observations on the support of the kernel).

weights is the variable used for optional weighting of the estimation procedure. The unit-specific weights multiply the kernel function.

h specifies the bandwidth used to construct the (global) polynomial fits given the kernel choice kernel. If not specified, the bandwidths are chosen to span the full support of the data. If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.

covs specifies additional covariates to be used in the polynomial regression.

covs_eval sets the evaluation points for the additional covariates, when included in the estimation. Options are: covs_eval = 0 (default) and covs_eval = "mean"

covs_drop if TRUE, it checks for collinear additional covariates and drops them. Default is TRUE.

support specifies an optional extended support of the running variable to be used in the construction of the bins; default is the sample range.

subset an optional vector specifying a subset of observations to be used.

hide logical. If TRUE, it omits the RD plot; default is hide = FALSE.

ci optional graphical option to display confidence intervals of selected level for each bin.

shade optional graphical option to replace confidence intervals with shaded areas.

title optional title for the RD plot.

x.label optional label for the x-axis of the RD plot.

y.label optional label for the y-axis of the RD plot.
rdplot

x.lim  optional setting for the range of the x-axis in the RD plot.
y.lim  optional setting for the range of the y-axis in the RD plot.
col.dots  optional setting for the color of the dots in the RD plot.
col.lines  optional setting for the color of the lines in the RD plot.

Value

binselect  method used to compute the optimal number of bins.
N  sample sizes used to the left and right of the cutoff.
Nh  effective sample sizes used to the left and right of the cutoff.
c  cutoff value.
p  order of the global polynomial used.
h  bandwidth used to the left and right of the cutoff.
kernel  kernel used.
J  selected number of bins to the left and right of the cutoff.
J_IMSE  IMSE optimal number of bins to the left and right of the cutoff.
J_MV  Mimicking variance number of bins to the left and right of the cutoff.
coef  matrix containing the coefficients of the $p^{th}$ order global polynomial estimated both sides of the cutoff.
scale  selected scale value.
rscale  implicit scale value.
bin_avg  average bin length.
bin_med  median bin length.
vars_bins  data frame containing the variables used to construct the bins: bin id, cutoff values, mean of x and y within each bin, cutoff points and confidence interval bounds.
vars_poly  data frame containing the variables used to construct the global polynomial plot.
rdplot  a standard ggplot object that can be used for further customization.

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References


See Also

rdbwselect, rdrobust

Examples

```r
x<-runif(1000,-1,1)
y<-5+3*x+2*(x>=0)+rnorm(1000)
rdbplot(y,x)
```

---

rdrobust

*Local-Polynomial RD Estimation with Robust Confidence Intervals*

Description

`rdrobust` implements local polynomial Regression Discontinuity (RD) point estimators with robust bias-corrected confidence intervals and inference procedures developed in Calonico, Cattaneo and Titiunik (2014a), Calonico, Cattaneo and Farrell (2018), Calonico, Cattaneo, Farrell and Titiunik (2019), and Calonico, Cattaneo and Farrell (2020). It also computes alternative estimation and inference procedures available in the literature.

Companion commands are: `rdbwselect` for data-driven bandwidth selection, and `rdplot` for data-driven RD plots (see Calonico, Cattaneo and Titiunik (2015a) for details).

A detailed introduction to this command is given in Calonico, Cattaneo and Titiunik (2015b), and Calonico, Cattaneo, Farrell and Titiunik (2017). A companion *Stata* package is described in Calonico, Cattaneo and Titiunik (2014b).

For more details, and related *Stata* and *R* packages useful for analysis of RD designs, visit [https://rdpackages.github.io/](https://rdpackages.github.io/)
rdrobust(y, x, c = NULL, fuzzy = NULL, deriv = NULL, p = NULL, q = NULL, h = NULL, b = NULL, rho = NULL, covs = NULL, covs_drop = TRUE, kernel = "tri", weights = NULL, bwselect = "msrd", vce = "nn", cluster = NULL, nmmatch = 3, level = 95, scalepar = 1, scaleregul = 1, sharpbw = FALSE, all = NULL, subset = NULL, masspoints = "adjust", bwcheck = NULL, bwrestrict = TRUE, stdvars = FALSE)

Arguments

y is the dependent variable.

x is the running variable (a.k.a. score or forcing variable).

c specifies the RD cutoff in x; default is c = 0.

fuzzy specifies the treatment status variable used to implement fuzzy RD estimation (or Fuzzy Kink RD if deriv=1 is also specified). Default is Sharp RD design and hence this option is not used.

deriv specifies the order of the derivative of the regression functions to be estimated. Default is deriv=0 (for Sharp RD, or for Fuzzy RD if fuzzy is also specified). Setting deriv=1 results in estimation of a Kink RD design (up to scale), or Fuzzy Kink RD if fuzzy is also specified.

p specifies the order of the local-polynomial used to construct the point-estimator; default is p = 1 (local linear regression).

q specifies the order of the local-polynomial used to construct the bias-correction; default is q = 2 (local quadratic regression).

h specifies the main bandwidth used to construct the RD point estimator. If not specified, bandwidth h is computed by the companion command rdbwselect. If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.

b specifies the bias bandwidth used to construct the bias-correction estimator. If not specified, bandwidth b is computed by the companion command rdbwselect. If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.

rho specifies the value of rho, so that the bias bandwidth b equals h/rho. Default is rho = 1 if h is specified but b is not.

covs specifies additional covariates to be used for estimation and inference.

covs_drop if TRUE, it checks for collinear additional covariates and drops them. Default is TRUE.

kernel is the kernel function used to construct the local-polynomial estimator(s). Options are triangular (default option), epanechnikov and uniform.

weights is the variable used for optional weighting of the estimation procedure. The unit-specific weights multiply the kernel function.
**bwselect** specifies the bandwidth selection procedure to be used. By default it computes both $h$ and $b$, unless $\rho$ is specified, in which case it only computes $h$ and sets $b = h/\rho$. Options are:

- **mserd** one common MSE-optimal bandwidth selector for the RD treatment effect estimator.
- **msetwo** two different MSE-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
- **mssum** one common MSE-optimal bandwidth selector for the sum of regression estimates (as opposed to difference thereof).
- **msecomb1** for $\min(mserd,mssum)$.
- **msecomb2** for median($msetwo,mserd,mssum$), for each side of the cutoff separately.

- **cerrd** one common CER-optimal bandwidth selector for the RD treatment effect estimator.
- **certwo** two different CER-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
- **cersum** one common CER-optimal bandwidth selector for the sum of regression estimates (as opposed to difference thereof).
- **cercomb1** for $\min(cerrd,cersum)$.
- **cercomb2** for median($certwo,cerrd,cersum$), for each side of the cutoff separately.

Note: MSE = Mean Square Error; CER = Coverage Error Rate. Default is **bwselect=mserd**. For details on implementation see Calonico, Cattaneo and Titiunik (2014a), Calonico, Cattaneo and Farrell (2018), and Calonico, Cattaneo, Farrell and Titiunik (2019), and the companion software articles.

**vce** specifies the procedure used to compute the variance-covariance matrix estimator. Options are:

- **nn** for heteroskedasticity-robust nearest neighbor variance estimator with nnmatch the (minimum) number of neighbors to be used.
- **hc0** for heteroskedasticity-robust plug-in residuals variance estimator without weights.
- **hc1** for heteroskedasticity-robust plug-in residuals variance estimator with hc1 weights.
- **hc2** for heteroskedasticity-robust plug-in residuals variance estimator with hc2 weights.
- **hc3** for heteroskedasticity-robust plug-in residuals variance estimator with hc3 weights.

Default is **vce=nn**.

**cluster** indicates the cluster ID variable used for cluster-robust variance estimation with degrees-of-freedom weights. By default it is combined with vce=nn for cluster-robust nearest neighbor variance estimation. Another option is plug-in residuals combined with vce=hc0.

**nnmatch** to be combined with for vce=nn for heteroskedasticity-robust nearest neighbor variance estimator with nnmatch indicating the minimum number of neighbors to be used. Default is **nnmatch=3**.
level sets the confidence level for confidence intervals; default is $level = 95$.

scalepar specifies scaling factor for RD parameter of interest. This option is useful when the population parameter of interest involves a known multiplicative factor (e.g., sharp kink RD). Default is $scalepar = 1$ (no scaling).

scaleregul specifies scaling factor for the regularization term added to the denominator of the bandwidth selectors. Setting $scaleregul = 0$ removes the regularization term from the bandwidth selectors; default is $scaleregul = 1$.

sharpbw option to perform fuzzy RD estimation using a bandwidth selection procedure for the sharp RD model. This option is automatically selected if there is perfect compliance at either side of the cutoff.

all if specified, \texttt{rdrobust} reports three different procedures:
(i) conventional RD estimates with conventional standard errors.
(ii) bias-corrected estimates with conventional standard errors.
(iii) bias-corrected estimates with robust standard errors.

subset an optional vector specifying a subset of observations to be used.

masspoints checks and controls for repeated observations in the running variable. Options are:
(i) \texttt{off}: ignores the presence of mass points;
(ii) \texttt{check}: looks for and reports the number of unique observations at each side of the cutoff.
(iii) \texttt{adjust}: controls that the preliminary bandwidths used in the calculations contain a minimal number of unique observations. By default it uses 10 observations, but it can be manually adjusted with the option \texttt{bwcheck}).
Default option is \texttt{masspoints=adjust}.

bwcheck if a positive integer is provided, the preliminary bandwidth used in the calculations is enlarged so that at least \texttt{bwcheck} unique observations are used.

bwrestrict if \texttt{TRUE}, computed bandwidths are restricted to lie within the range of \texttt{x}; default is \texttt{bwrestrict = TRUE}.

stdvars if \texttt{TRUE}, \texttt{x} and \texttt{y} are standardized before computing the bandwidths; default is \texttt{stdvars = FALSE}.

\textbf{Value}

\begin{itemize}
  \item \texttt{N} vector with the sample sizes used to the left and to the right of the cutoff.
  \item \texttt{N_h} vector with the effective sample sizes used to the left and to the right of the cutoff.
  \item \texttt{c} cutoff value.
  \item \texttt{p} order of the polynomial used for estimation of the regression function.
  \item \texttt{q} order of the polynomial used for estimation of the bias of the regression function.
  \item \texttt{bws} matrix containing the bandwidths used.
  \item \texttt{tau_cl} conventional local-polynomial estimate to the left and to the right of the cutoff.
  \item \texttt{tau_bc} bias-corrected local-polynomial estimate to the left and to the right of the cutoff.
\end{itemize}
coef  vector containing conventional and bias-corrected local-polynomial RD estimates.
se  vector containing conventional and robust standard errors of the local-polynomial RD estimates.
bias  estimated bias for the local-polynomial RD estimator below and above the cutoff.
beta_p_l  conventional p-order local-polynomial estimates to the left of the cutoff.
beta_p_r  conventional p-order local-polynomial estimates to the right of the cutoff.
V_cl_l  conventional variance-covariance matrix estimated below the cutoff.
V_cl_r  conventional variance-covariance matrix estimated above the cutoff.
V_rb_l  robust variance-covariance matrix estimated below the cutoff.
V_rb_r  robust variance-covariance matrix estimated above the cutoff.
pv  vector containing the p-values associated with conventional, bias-corrected and robust local-polynomial RD estimates.
ci  matrix containing the confidence intervals associated with conventional, bias-corrected and robust local-polynomial RD estimates.

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See Also

`rdbwselect`, `rdplot`

Examples

```r
x<-runif(1000,-1,1)
y<-5+3*x+2*(x>=0)+rnorm(1000)
rdrobust(y,x)
```

**rdrobust_RDsenate**

**RD Senate Data**

Description

Extract of the dataset constructed by Cattaneo, Frandsen, and Titiunik (2015), which include measures of incumbency advantage in the U.S. Senate for the period 1914-2010.

Usage

```r
data(rdrobust_RDsenate)
```

Format

A data frame with 1390 observations on the following 2 variables.

- `margin` a numeric vector.
- `vote` a numeric vector.

Source


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