Package ‘rofanova’

October 14, 2022

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Description Implements the robust functional analysis of variance (RoFANOVA), described in Centofanti et al. (2021) <arXiv:2112.10643>. It allows testing mean differences among groups of functional data by being robust against the presence of outliers.
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**Description**

Implements the robust functional analysis of variance (RoFANOVA), described in Centofanti et al. (2021) <arXiv:2112.10643>. It allows testing mean differences among groups of functional data by being robust against the presence of outliers.

**Details**

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**References**


**See Also**

rofanova funmad fusem

**Examples**

```r
library(rofanova)
data_out<-simulate_data(scenario="one-way")
```
funmad

label_1=data_out$label_1
X_fdata<-data_out$X_fdata
B=10
cores=1
per_list_median<-rofanova(X_fdata,label_1,B = B,family="median",cores=cores)
pvalue_median_vec<-per_list_median$pval_vec
per_list_huber<-rofanova(X_fdata,label_1,B = B,family="huber",cores=cores)
pvalue_huber_vec<-per_list_huber$pval_vec
per_list_bisquare<-rofanova(X_fdata,label_1,B = B,family="bisquare",cores=cores)
pvalue_bisquare_vec<-per_list_bisquare$pval_vec
per_list_hampel<-rofanova(X_fdata,label_1,B = B,family="hampel",cores=cores)
pvalue_hampel_vec<-per_list_hampel$pval_vec
per_list_optimal<-rofanova(X_fdata,label_1,B = B,family="optimal",cores=cores)
pvalue_optimal<-per_list_optimal$pval

---

funmad

The functional normalized median absolute deviation estimators

Description
Compute the functional normalized median absolute deviation (FuNMAD) estimator as described in Centofanti et al. (2021).

Usage
funmad(X, ...)

Arguments

X Either an object of class fdata for monodimensional functional data or an object of class fdata2d for bi-dimensional functional data.

... Additional argument to be passed to fusem.

Value
The FuNMAD estimator.

References

See Also
rofanova, fusem
Examples

library(rofanova)
data_out<-simulate_data(scenario="one-way")
X_fdata<-data_out$X_fdata
per_list_median<-funmad(X_fdata)

fusem

The scale equivariant functional M-estimator

Description

Compute the scale equivariant functional M-estimator as described in Centofanti et al. (2021).

Usage

fusem(
  X, 
  family = "bisquare", 
  eff = 0.95, 
  maxit = 50, 
  tol = 1e-04, 
  mu0_g = NULL, 
  sig0_g = NULL
)

Arguments

X Either an object of class fdata for monodimensional functional data or an object of class fdata2d for bi-dimensional functional data.

family The family of loss function for the calculation of the equivariant functional M-estimator. The values allowed are "bisquare" for the bisquare or Tukey’s biweight family of loss functions; "huber" for the the Huber’s family of loss functions; "optimal" for the optimal family of loss functions; "hampel" for the the Hampel’s family of loss functions; "median" for the median loss function. A non-robust functional estimator of the mean based on the standard least squares loss function is used with the value "mean". Default is "bisquare".

eff Asymptotic efficiency of the equivariant functional M-estimator. When family is either "mean" or "median", eff is ignored.

maxit The maximum number of iterations allowed in the re-weighted least-squares algorithm to compute the equivariant functional M-estimator.

tol The tolerance for the stopping condition of the re-weighted least-squares algorithm to compute the equivariant functional M-estimator. The algorithm stops when the relative variation of the weighted norm sum between two consecutive iterations is less than tol.
mu0_g

Initial estimate used in re-weighted least-squares algorithm to compute the equivariant functional M-estimator. If NULL the standard non-robust functional mean is used. Default is NULL.

sig0_g

Estimate of the standard error of \( X \). If NULL, the functional mean is used. Default is NULL.

Value

A list containing the following arguments:

- mu: The scale equivariant functional M-estimator.
- mu0_g: mu0_g.
- sig0_g: sig0_g.

References


See Also

rofanova funmad

Examples

```r
library(rofanova)
data_out<-simulate_data(scenario="one-way")
X_fdata<-data_out$X_fdata
per_list_median<-fusem(X_fdata)
```

Description

Robust Functional Analysis of Variance (RoFANOVA) allows identifying the presence of significant differences, in terms of functional mean, among groups of a functional data by being robust against the presence of outliers (Centofanti et al., 2021).

Usage

```r
rofanova(
  X,
  label_1,
  label_2 = NULL,
  B = 100,
  cores = 1,
)```
family = "bisquare",
    eff = 0.95,
    mu0_g = NULL,
    scale = NULL,
    maxit = 50,
    tol = 1e-04
)
Arguments

X Either an object of class fdata for monodimensional functional data or an object of class fdata2d for bi-dimensional functional data.

label_1 A vector of containing group label corresponding to the first main effect.

label_2 A vector of containing group label corresponding to the second main effect. If it is NULL, the one-way RoFANOVA is performed. Otherwise, the two-way RoFANOVA with interaction is employed. Default is NULL.

B The number of permutations used to approximate the p-value in the permutation test. Default is 1000.

cores If cores>1, then parallel computing is used, with cores cores. Default is 1.

family The family of loss function for the calculation of the equivariant functional M-estimator. The values allowed are "bisquare" for the bisquare or Tukey’s bi-weight family of loss functions; "huber" for the the Huber’s family of loss functions; "optimal" for the optimal family of loss functions; "hampel" for the the Hampel’s family of loss functions; "median" for the median loss function. A non-robust functional estimator of the mean based on the standard least squares loss function is used with the value "mean". Default is "bisquare".

eff Asymptotic efficiency of the equivariant functional M-estimator. When family is either "mean" or "median", eff is ignored.

mu0_g Initial estimate used in re-weighted least-squares algorithm to compute the equivariant functional M-estimator. If NULL the standard non-robust functional mean is used. Default is NULL.

scale Estimate of the standard error of X. If NULL, the functional normalized median absolute deviation estimator is used. Default is NULL.

maxit The maximum number of iterations allowed in the re-weighted least-squares algorithm to compute the equivariant functional M-estimator.

tol The tolerance for the stopping condition of the re-weighted least-squares algorithm to compute the equivariant functional M-estimator. The algorithm stops when the relative variation of the weighted norm sum between two consecutive iterations is less than tol.

Value

pval_vec Vector of p-value corresponding to the test of significance of the whole model, the main effects and the interaction. For one-way RoFANOVA, it is the p-value corresponding to the test of the main effect.

Tr_obs The observed value of the test statistic.
mod A list containing the following arguments:

- **Tr**: The observed value of the test statistic.
- **global_mean**: The robust estimate of functional grand mean.
- **group_mean_1**: The robust estimate of the first functional main effect.
- **group_mean_2**: The robust estimate of the second functional main effect. For one-way RoFANOVA, it is NULL.
- **group_mean_ij**: The robust estimate of the group functional mean. For one-way, it RoFANOVA is NULL.
- **scale**: The robust estimate of functional standard deviation.
- **scale_1**: The robust estimate of functional standard deviation corresponding to the first functional main effect.
- **scale_2**: The robust estimate of functional standard deviation corresponding to the second functional main effect. For one-way RoFANOVA, it is NULL.
- **scale_re**: The robust estimate of the functional standard deviation of the error distribution. For one-way RoFANOVA, it is NULL.
- **X**: The variable X.
- **label_1**: The vector of containing group label corresponding to the first main effect.
- **label_2**: The vector of containing group label corresponding to the second main effect. For one-way RoFANOVA, it is NULL.
- **family**: The family of loss function for the calculation of the equivariant functional M-estimator.

References


See Also

fusem funmad

Examples

library(rofanova)
data_out<-simulate_data(scenario="one-way")
label_1=data_out$label_1
X_fdata<-data_out$X_fdata
B=10
cores=1
per_list_median<-rofanova(X_fdata,label_1,B = B,family="median",cores=cores)
pvalue_median_vec<-per_list_median$pval_vec
per_list_huber<-rofanova(X_fdata,label_1,B = B,family="huber",cores=cores)
pvalue_huber_vec<-per_list_huber$pval_vec
per_list_bisquare<-rofanova(X_fdata,label_1,B = B,family="bisquare",cores=cores)
### simulate_data

Simulate data for Robust Functional ANOVA

**Description**

Generate synthetic data as in the simulation study of Centofanti et al. (2021) with the addition of the case of bi-variate functional data. All the details are in Centofanti et al. (2021).

**Usage**

```r
simulate_data(
  scenario = "one-way",  
  mean = "M1",  
  con = "C0",  
  p = 0.1,  
  M = 1,  
  n_i = 25,  
  k_1 = 3,  
  k_2 = 3,  
  alpha = 0,  
  beta = 0,  
  sd = 0.01,  
  grid = seq(0, 1, length.out = 30),  
  err = "s"
)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
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<tr>
<td>scenario</td>
<td>A character strings indicating the scenario considered. It could be &quot;one-way&quot;, &quot;two-way&quot;, &quot;one-way surface&quot; and &quot;two-way surface&quot;.</td>
</tr>
<tr>
<td>mean</td>
<td>A character strings indicating the type of mean function in one-way ANOVA. It could be &quot;M1&quot;, &quot;M2&quot;, and &quot;M3&quot;.</td>
</tr>
<tr>
<td>con</td>
<td>A character strings indicating the type of contamination function. It could be &quot;C0&quot;, for no contamination, &quot;C1&quot;, &quot;C2&quot;, &quot;C3&quot;, &quot;C4&quot;, &quot;C5&quot;, and &quot;C6&quot;.</td>
</tr>
<tr>
<td>p</td>
<td>The parameter related to the bernoulli variable in the contamination function.</td>
</tr>
<tr>
<td>M</td>
<td>The contamination size constant.</td>
</tr>
<tr>
<td>n_i</td>
<td>The number of observation for each group.</td>
</tr>
<tr>
<td>k_1</td>
<td>The number of level for the first main effect.</td>
</tr>
<tr>
<td>k_2</td>
<td>The number of level for the second main effect. For One-way ANOVA, it is ignored.</td>
</tr>
</tbody>
</table>
alpha  The parameter a in the Two-way ANOVA scenarios. For One-way ANOVA, it is ignored.

beta  The parameter b in the Two-way ANOVA scenarios. For One-way ANOVA, it is ignored.

sd  The sigma parameter in the covariance of the error function.

grid  The grid over which the functional data are observed.

err  The direction of the dependence in the error function for the case of bi-variate functional data. It could be either "s", for dependence along the first dimension or "t" for dependence along the second dimension.

Value

A list containing the following arguments:

• X_fdata: The generated functional data.
• label_1: The vector of containing group label corresponding to the first main effect.
• label_2: The vector of containing group label corresponding to the second main effect. For one-way ANOVA, it is NULL.

References


See Also

rofanova fusem funmad

Examples

```r
library(rofanova)
data_out<-simulate_data(scenario="one-way")
label_1=data_out$label_1
X_fdata<-data_out$X_fdata
B=10
cores=1
per_list_median<-rofanova(X_fdata,label_1,B = B,family="median",cores=cores)
pvalue_median_vec<-per_list_median$pval_vec
per_list_huber<-rofanova(X_fdata,label_1,B = B,family="huber",cores=cores)
pvalue_huber_vec<-per_list_huber$pval_vec
per_list_bisquare<-rofanova(X_fdata,label_1,B = B,family="bisquare",cores=cores)
pvalue_bisquare_vec<-per_list_bisquare$pval_vec
per_list_hampel<-rofanova(X_fdata,label_1,B = B,family="hampel",cores=cores)
pvalue_hampel_vec<-per_list_hampel$pval_vec
per_list_optimal<-rofanova(X_fdata,label_1,B = B,family="optimal",cores=cores)
pvalue_optimal<-per_list_optimal$pval
```
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