Package ‘rqPen’

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Description Performs penalized quantile regression with LASSO, elastic net, SCAD and MCP penalty functions including group penalties. Provides a function that automatically generates lambdas and evaluates different models with cross validation or BIC, including a large p version of BIC.
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beta_plots

Plots of coefficients by lambda for cv.rq.group.pen and cv.rq.pen

Description

Warning: this function is deprecated and will not be exported in future versions.

Usage

beta_plots(model, voi = NULL, logLambda = TRUE, loi = NULL, ...)

Index

beta_plots
Plots of coefficients by lambda for cv.rq.group.pen and cv.rq.pen
bytau.plot

Arguments

model cv.rq.pen or cv.rq.group.pen object
voi Index of betas to include. Default is all of them.
logLambda Plot of lambdas is on the log scale.
loi Index of lambdas to use, default is all of them.
... Additional arguments to be sent to plot()

Value

Plot of how beta estimates change with lambda.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

## Not run:
set.seed(1)
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModels <- cv.rq.pen(x,y)
b_plot <- beta_plots(lassoModels)
## End(Not run)

bytau.plot

Plot of how coefficients change with tau

Description

Plot of how coefficients change with tau

Usage

bytau.plot(x, ...)

Arguments

x A rq.pen.seq or rq.pen.seq.cv object.
...

Value

Returns the plot of how coefficients change with tau.
bytau.plot.rq.pen.seq  Plot of how coefficients change with tau.

Description
Plot of how coefficients change with tau.

Usage
## S3 method for class 'rq.pen.seq'
bytau.plot(x, a = NULL, lambda = NULL, lambdaIndex = NULL, ...)

Arguments

- **x**: An rq.pen.seq object
- **a**: The tuning parameter a of interest
- **lambda**: The lambda value of interest.
- **lambdaIndex**: The lambda index of interest. Only specify lambdaIndex or lambda, not both.
- **...**: Additional parameters sent to plot()

Value
A plot of coefficient values by tau.

Author(s)
Ben Sherwood, <ben.sherwood@ku.edu>

Examples

```r
code here
```

bytau.plot(x, a = NULL, lambda = NULL, lambdaIndex = NULL, ...)
Description

Produces plots of how coefficient estimates vary by quantile for models selected by using cross validation.

Usage

## S3 method for class 'rq.pen.seq.cv'
bytau.plot(x, septau = TRUE, cvmin = TRUE, useDefaults = TRUE, ...)

Arguments

x An rq.pen.seq.cv object
septau Whether optimal tuning parameters are estimated separately for each quantile.
cvmin Whether the minimum cv error should be used or the one standard error rule.
useDefaults Set to FALSE if you want to use something besides minimum cv or 1se.
... Additional parameters sent to plot()

Value

Returns plots of coefficient estimates varying by quantile.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

```r
set.seed(1)
x <- matrix(runif(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + (1+x[,4])*rnorm(100)
lmcv <- rq.pen.cv(x,y,tau=seq(.1,.9,.1))
bytau.plot(lmcv)
```
Coefficients from a cv.rq.group.pen object

Usage

## S3 method for class 'cv.rq.group.pen'
coef(object, lambda = "min", ...)

Arguments

object A cv.rq.group.pen object.
lambda The lambda value, default is to use the one associated with the minimum cv error.
... Additional parameters.

Value

Vector of coefficients.

Returns Coefficients of a cv.rq.pen object

Description

Warning: this function will be deprecated and not exported in future versions of rqPen, due to the switch from cv.rq.pen() to rq.pen.cv().

Usage

## S3 method for class 'cv.rq.pen'
coef(object, lambda = "min", ...)

Arguments

object cv.rq.pen object
lambda Value of lambda, default is to use the minimum value.
... Additional parameters.

Value

Coefficients for a given lambda, or the lambda associated with the minimum cv value.
## S3 method for class 'rq.pen.seq'
coef(
  object,
  tau = NULL,
  a = NULL,
  lambda = NULL,
  modelsIndex = NULL,
  lambdaIndex = NULL,
  ...
)

### Arguments
- **object**: rq.pen.seq object
- **tau**: Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
- **a**: Tuning parameter of a. Default is NULL, which returns coefficients for all values of a. Should not be specified if modelsIndex is used.
- **lambda**: Tuning parameter of \( \lambda \). Default is NULL, which returns coefficients for all values of \( \lambda \).
- **modelsIndex**: Index of the models for which coefficients should be returned. Does not need to be specified if tau or a are specified.
- **lambdaIndex**: Index of the lambda values for which coefficients should be returned. Does not need to be specified if lambda is specified.
- **...**: Additional parameters.

### Value
A list of a matrix of coefficients for each tau and a combination

### Author(s)
Ben Sherwood, <ben.sherwood@ku.edu>
Examples

```r
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,5,1),tau=c(0.25,.75),lambda=c(.1,.05,.01))
allCoefs <- coef(m1)
targetCoefs <- coef(m1,tau=.25,a=.5,lambda=.1)
idxApproach <- coef(m1,modelsIndex=2)
bothIdxApproach <- coef(m1,modelsIndex=2,lambdaIndex=1)
```

---

**coef.rq.pen.seq.cv**

*Returns coefficients from a rq.pen.seq.cv object.*

### Description

Returns coefficients from a rq.pen.seq.cv object.

### Usage

```r
## S3 method for class 'rq.pen.seq.cv'
coef(object, septau = TRUE, cvmin = TRUE, useDefaults = TRUE, tau = NULL, ...)
```

### Arguments

- **object**: An rq.pen.seq.cv object.
- **septau**: Whether tuning parameter should be optimized separately for each quantile.
- **cvmin**: If TRUE then minimum error is used, if FALSE then one standard error rule is used.
- **useDefaults**: Whether the default results are used. Set to FALSE if you you want to specify specific models and lambda values.
- **tau**: Quantiles of interest.
- **...**: Additional parameters sent to coef.rq.pen.seq()

### Value

Returns coefficients

### Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>
Examples

```r
## Not run:
set.seed(1)
x <- matrix(rnorm(800), nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModels <- rq.pen.cv(x,y,tau=seq(.1,.9,.1))
coefficients(lassoModels, septau=FALSE)
coefficients(lassoModels, cvmin=FALSE)
## End(Not run)
```

Description

This function is deprecated. Recommend using rq.group.pen.cv() instead.

Usage

```r
cv.rq.group.pen(x,
y,groups, tau = 0.5, lambda = NULL, penalty = "SCAD", intercept = TRUE, criteria = "CV", cvFunc = "check", nfolds = 10, foldid = NULL, nlambda = 100, eps = 1e-04, init.lambda = 1, alg = "huber", penGroups = NULL, ...)
```

Arguments

- `x` Matrix of predictors.
- `y` Vector of responses.
- `groups` Vector of groups.
- `tau` Quantile being modeled.
lambda Vector of lambdas. Default is for lambdas to be automatically generated.
penalty Type of penalty: "LASSO", "SCAD" or "MCP".
intercept Whether model should include an intercept. Constant does not need to be included in "x".
criteria How models will be evaluated. Either cross-validation "CV", BIC "BIC" or large P BIC "PBIC".
cvFunc If cross-validation is used how errors are evaluated. Check function "check", "SqErr" (Squared Error) or "AE" (Absolute Value).
nfolds K for K-folds cross-validation.
foldid Group id for cross-validation. Function will randomly generate groups if not specified.
nlambda Number of lambdas for which models are fit.
eps Multiple of lambda max for Smallest lambda used.
init.lambda Initial lambda used to find the maximum lambda. Not needed if lambda values are set.
alg Algorithm used for fit. "QICD" or "LP".
penGroups Specify which groups will be penalized. Default is to penalize all groups.
... Additional arguments to be sent to rq.group.fit or groupQICDMultLambda.

Value

Returns the following:

- beta Matrix of coefficients for different values of lambda
- residuals Matrix of residuals for different values of lambda.
- rho Vector of rho, unpenalized portion of the objective function, for different values of lambda.
- cv Data frame with "lambda" and second column is the evaluation based on the criteria selected.
- lambda.min Lambda which provides the smallest statistic for the selected criteria.
- penalty Penalty selected.
- intercept Whether intercept was included in model.
- groups Group structure for penalty function.

References

Examples

```r
## Not run:
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
cv_model <- cv.rq.group.pen(x,y,groups=c(rep(1,4),rep(2,4)),criteria="BIC")
## End(Not run)
```

cv.rq.pen

Cross Validated quantile regression

Description

Warning: this function is deprecated and will not be exported in future rqPen releases. Produces penalized quantile regression models for a range of lambdas and penalty of choice. If lambda is unselected than an iterative algorithm is used to find a maximum lambda such that the penalty is large enough to produce an intercept only model. Then range of lambdas goes from the maximum lambda found to "eps" on the log scale. For non-convex penalties local linear approximation approach used by Wang, Wu and Li to extend LLA as proposed by Zou and Li (2008) to the quantile regression setting.

Usage

```r
cv.rq.pen(
x,
y,
tau = 0.5,
lambda = NULL,
weights = NULL,
penalty = "LASSO",
intercept = TRUE,
criteria = "CV",
cvFunc = "check",
nfolds = 10,
foldid = NULL,
nlambda = 100,
eps = 1e-04,
init.lambda = 1,
penVars = NULL,
alg = ifelse(ncol(x) < 50, "LP", "QICD"),
internal = FALSE,
...)
```
Arguments

x  Matrix of predictors.
y  Numeric vector of response values.
tau  Conditional quantile being modelled.
lambda  Vector of lambdas. Default is for lambdas to be automatically generated.
weights  Weights for the objective function.
penalty  Type of penalty: "LASSO", "SCAD" or "MCP".
intercept  Whether model should include an intercept. Constant does not need to be included in "x".
criteria  How models will be evaluated. Either cross-validation "CV", BIC "BIC" or large P BIC "PBIC".
cvFunc  If cross-validation is used how errors are evaluated. Check function "check", "SqErr" (Squared Error) or "AE" (Absolute Value).
nfolds  K for K-folds cross-validation.
foldid  Group id for cross-validation. Function will randomly generate groups if not specified.
nlambda  Number of lambdas for which models are fit.
eps  Smallest lambda used.
init.lambda  Initial lambda used to find the maximum lambda. Not needed if lambda values are set.
penVars  Variables that should be penalized. With default value of NULL all variables are penalized.
alg  Algorithm that will be used, either linear programming (LP) or coordinate descent (QICD) algorithm from Peng and Wang (2015).
internal  If this is an internal call to this function.
...  Additional arguments to be sent to rq.lasso.fit or rq.nc.fit.

Value

Returns the following:

- modelsList of penalized models fit. Number of models will match number of lambdas and correspond to cv$lambda.
- cvData frame with "lambda" and second column is the evaluation based on the criteria selected.
- lambda.minLambda which provides the smallest statistic for the selected criteria.
- penaltyPenalty selected.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>
cv.plots

Examples

```r
## Not run:
x <- matrix(rnorm(800), nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
cv_model <- cv.rq.pen(x, y)
## End(Not run)
```

Description

Plots of cross validation results as a function of lambda.

Usage

```r
cv_plots(model, logLambda = TRUE, loi = NULL, ...)
```

Arguments

- `model`: A cv.rq.pen() object.
- `logLambda`: Whether lambda values should be logged or not.
- `loi`: Lambda indexes of interest, if null all lambda values will be used.
- `...`: Additional parameters sent to plot function.

Value

returns a cross validation plot

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>
plot.cv.rq.group.pen  
Cross validation plot for cv.rq.group.pen object

Description
Cross validation plot for cv.rq.group.pen object

Usage
## S3 method for class 'cv.rq.group.pen'
plot(x, ...)

Arguments

- **x**  
  A cv.rq.group.pen object
- **...**  
  Additional parameters for plot function.

Value
A cross validation plot.

plot.rq.pen.seq  
Plot of coefficients of rq.pen.seq object as a function of lambda

Description
Plot of coefficients of rq.pen.seq object as a function of lambda

Usage
## S3 method for class 'rq.pen.seq'
plot(
  x,
  vars = NULL,
  logLambda = TRUE,
  tau = NULL,
  a = NULL,
  lambda = NULL,
  modelsIndex = NULL,
  lambdaIndex = NULL,
  main = NULL,
  ...  
)

)
Arguments

- **x**: rq.pen.seq object
- **vars**: Variables of interest
- **logLambda**: Whether lambda should be reported on the log scale
- **tau**: Quantiles of interest
- **a**: Tuning parameter a values of interest.
- **lambda**: Values of lambda of interest.
- **modelsIndex**: Specific models of interest.
- **lambdaIndex**: Specific lambda values of interest.
- **main**: Title of the plots. Can be a vector of multiple titles if multiple plots are created.
- **...**: Additional arguments sent to plot

Value

Returns plot(s) of coefficients as they change with lambda.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

```r
set.seed(1)
x <- matrix(rnorm(100*8,sd=10),ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(100,3)
m1 <- rq.pen(x,y,tau=c(.1,.5,.7),penalty="SCAD",a=c(3,4))
plot(m1,a=3,tau=.7)
plot(m1)
mlist <- list()
for(i in 1:6){
  mlist[[i]] <- paste("Plot",i)
}
plot(m1,main=mlist)
```

Description

Provides plots of cross-validation results by lambda. If septau is set to TRUE then plots the cross-validation results for each quantile. If septau is set to FALSE then provides one plot for cross-validation results across all quantiles.
Usage

## S3 method for class 'rq.pen.seq.cv'
plot(x, septau = TRUE, tau = NULL, logLambda = FALSE, main = NULL, ...)

Arguments

x The rq.pen.seq.cv object
septau If set to true then optimal tuning parameters are selected separately for each quantile and there will be a different plot for each quantile.
tau Quantiles of interest.
logLambda Whether log(lambda) is used for the x-axis
main Title to the plot
... Additional parameters sent to the plot function.

Value

Plots of the cross validation results by lambda.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

set.seed(1)
x <- matrix(rnorm(100*8,sd=1),ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(100,3)
m1 <- rq.pen.cv(x,y,tau=c(.1,.3,.7))
plot(m1)
plot(m1,septau=FALSE)

---

 predict.cv.rq.pen Prediction for a cv.rq.pen object

Description

This function is deprecated and will not be exported in future versions.

Usage

## S3 method for class 'cv.rq.pen'
predict(object, newx, lambda = "lambda.min", ...)
Arguments

- **object**: A cv.rq.pen object.
- **newx**: Matrix of new data to make predictions with.
- **lambda**: Lambda value used, default is the value associated with the minimum cross validation result.
- **...**: Additional parameters that are currently ignored

Value

A vector of predictions.

Description

Predictions from a qic.select object

Usage

```r
## S3 method for class 'qic.select'
predict(object, newdata, ...)
```

Arguments

- **object**: qic.select object
- **newdata**: Data matrix to make predictions from.
- **...**: optional arguments

Value

A matrix of predicted values.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

```r
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,tau=c(.25,.75))
q1 <- qic.select(m1)
newx <- matrix(runif(80),ncol=8)
preds <- predict(q1,newx)
```
predict.rq.pen  

**Prediction for a rq.pen object**

---

**Description**

This function is deprecated and will not be exported in future versions.

**Usage**

```r
## S3 method for class 'rq.pen'
predict(object, newx, ...)  
```

**Arguments**

- `object`: An rq.pen object.
- `newx`: Matrix of new data to make predictions with.
- `...`: Additional parameters that are currently ignored

**Value**

A vector of predictions.

---

predict.rq.pen.seq  

**Predictions from rq.pen.seq object**

---

**Description**

Predictions from rq.pen.seq object

**Usage**

```r
## S3 method for class 'rq.pen.seq'
predict(
  object,
  newx,
  tau = NULL,
  a = NULL,
  lambda = NULL,
  modelsIndex = NULL,
  lambdaIndex = NULL,
  ...
)
```
**predict.rq.pen.seq.cv**

**Arguments**

- `object`  
  rq.pen.seq object
- `newx`  
  Matrix of predictors
- `tau`  
  Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
- `a`  
  Tuning parameter of a. Default is NULL, which returns coefficients for all values of a. Should not be specified if modelsIndex is used.
- `lambda`  
  Tuning parameter of \( \lambda \). Default is NULL, which returns coefficients for all values of \( \lambda \).
- `modelsIndex`  
  Index of the models for which coefficients should be returned. Does not need to be specified if tau or a are specified.
- `lambdaIndex`  
  Index of the lambda values for which coefficients should be returned. Does not need to be specified if lambda is specified.
- `...`  
  Additional parameters passed to coef.rq.pen.seq()

**Value**

A matrix of predictions for each tau and a combination

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```r
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75),lambda=c(.1,.05,.01))
newx <- matrix(runif(80),ncol=8)
allCoefs <- predict(m1,newx)
targetCoefs <- predict(m1,newx,tau=.25,a=.5,lambda=.1)
idxApproach <- predict(m1,newx,modelsIndex=2)
bothIdxApproach <- predict(m1,newx,modelsIndex=2,lambdaIndex=1)
```

**Description**

Predictions from rq.pen.seq.cv object
Usage

## S3 method for class 'rq.pen.seq.cv'
predict(
  object,
  newx,
  tau = NULL,
  septau = TRUE,
  cvmin = TRUE,
  useDefaults = TRUE,
  ...
)

Arguments

- **object**: rq.pen.seq.cv object
- **newx**: Matrix of predictors
- **tau**: Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
- **septau**: Whether tuning parameter should be optimized separately for each quantile.
- **cvmin**: If TRUE then minimum error is used, if FALSE then one standard error rule is used.
- **useDefaults**: Whether the default results are used. Set to FALSE if you want to specify specific models and lambda values.
- **...**: Additional parameters sent to coef.rq.pen.seq.cv().

Value

A matrix of predictions for each tau and a combination

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

Examples

```r
x <- matrix(runif(1600), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+5*x[,3])*rnorm(200)
m1 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75),lambda=c(.1,.05,.01))
newx <- matrix(runif(80),ncol=8)
cvpreds <- predict(m1,newx)
```
print.cv.rq.pen

Prints a cv.rq.pen object.

Description

Warning: this function is deprecated and will not be exported in future releases.

Usage

## S3 method for class 'cv.rq.pen'
print(x, ...)

Arguments

x A cv.rq.pen object

... Additional arguments

Details

Warning this function is deprecated and will not be exported in future releases.

Value

Prints cross validation or information criterion values by lambda.
Prints coefficients and cross validation results.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

print.qic.select

Print a qic.select object

Description

Print a qic.select object

Usage

## S3 method for class 'qic.select'
print(x, ...)

...
Arguments

x qic.select object

... optional arguments

Value

Prints the coefficients of the qic.select object

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

---

Description

Warning this function is deprecated and will not be exported in future releases.

Usage

```r
## S3 method for class 'rq.pen'
print(x, ...)
```

```r
## S3 method for class 'rq.pen'
print(x, ...)
```

Arguments

x A rq.pen object

... Additional arguments

Value

Prints the coefficients of the object.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>
print.rq.pen.seq  

Print a rq.pen.seq object

Description
Print a rq.pen.seq object

Usage
## S3 method for class 'rq.pen.seq'
print(x, ...)

Arguments
x rq.pen.seq object
...
optional arguments

Value
If only one model, prints a data.frame of the number of nonzero coefficients and lambda. Otherwise
prints information about the quantiles being modeled and choices for a.

Author(s)
Ben Sherwood, <ben.sherwood@ku.edu>

print.rq.pen.seq.cv  

Print a rq.pen.seq.cv object

Description
Prints a rq.pen.seq.cv object

Usage
## S3 method for class 'rq.pen.seq.cv'
print(x, ...)

Arguments
x A rq.pen.seq.cv object.
...
Additional arguments.

Value
Print of btr and gtr from a rq.pen.seq.cv object. If only one quantile is modeled then only btr is returned.
Calculate information criterion for penalized quantile regression models

Usage

qic(model, n, method = c("BIC", "AIC", "PBIC"))

Arguments

- **model**: model from a rq.pen.seq() object
- **n**: Sample size
- **method**: Choice of BIC, AIC or PBIC, a large p BIC.

Value

Let \( \hat{\beta} \) be the coefficient vectors for the estimated model. Function returns the value

\[
\log\left( \sum_{i=1}^{n} \rho_{\tau}(y_i - \mathbf{x}_i^\top \hat{\beta}) \right) + d \cdot b/(2n),
\]

where \( d \) is the number of nonzero coefficients and \( b \) depends on the method used. For AIC \( b = 2 \), for BIC \( b = \log(n) \) and for PBIC \( d = \log(n) \cdot \log(p) \) where \( p \) is the dimension of \( \hat{\beta} \). Returns this value for each coefficient vector in the model, so one for every value of \( \lambda \).

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

References


Examples

```r
set.seed(1)
x <- matrix(rnorm(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x, y, tau=c(.25,.75))
# returns the IC values for tau=.25
qic(m1$models[[1]], m1$n)
# returns the IC values for tau=.75
qic(m1$models[[2]], m1$n)
```
qic.select

Select tuning parameters using IC

Description
Select tuning parameters using IC

Usage
qic.select(obj, ...)

Arguments
obj    A rq.pen.seq or rq.pen.seq.cv object.
...    Additional arguments see qic.select.rq.pen.seq() or qic.select.rq.pen.seq.cv() for
        more information.

Value
Returns the plot of how coefficients change with tau.

Author(s)
Ben Sherwood, <ben.sherwood@ku.edu>

qic.select.rq.pen.seq

Select tuning parameters using IC

Description
Selects tuning parameter $\lambda$ and $a$ according to information criterion of choice. For a given $\hat{\beta}$ the information criterion is calculated as

$$\log(\sum_{i=1}^{n} \rho_r(y_i - x_i^T \hat{\beta})) + d \ast b/(2n),$$

where $d$ is the number of nonzero coefficients and $b$ depends on the method used. For AIC $b = 2$, for BIC $b = \log(n)$ and for PBIC $d = \log(n) \ast \log(p)$ where $p$ is the dimension of $\beta$. If septau set to FALSE then calculations are made across the quantiles. Let $\hat{\beta}_q$ be the coefficient vector for the $q$th quantile of $Q$ quantiles. In addition let $d_q$ and $b_q$ be $d$ and $b$ values from the $q$th quantile model. Note, for all of these we are assuming eqn and $a$ are the same. Then the summary across all quantiles is

$$\sum_{q=1}^{Q} w_q [\log(\sum_{i=1}^{n} \rho_r(y_i - x_i^T \hat{\beta}_q)) + d_q \ast b_q/(2n)],$$

where $w_q$ is the weight assigned for the $q$th quantile model.
qic.select.rq.pen.seq

Usage

```r
## S3 method for class 'rq.pen.seq'
qic.select(
  obj,
  method = c("BIC", "AIC", "PBIC"),
  septau = TRUE,
  weights = NULL,
  ...)
```

Arguments

- `obj` A rq.pen.seq or rq.pen.seq.cv object.
- `method` Choice of BIC, AIC or PBIC, a large p BIC.
- `septau` If optimal values of $\lambda$ and $a$ can vary with $\tau$. Default is TRUE.
- `weights` Weights for each quantile. Useful if you set septau to FALSE but want different weights for the different quantiles. If not specified default is to have $w_q = 1$ for all quantiles.
- `...` Additional arguments.

Value

- `coefficients` Coefficients of the selected models.
- `ic` Information criterion values for all considered models.
- `models` Model info for the selected models related to the original object `obj`.
- `gic` Information criterion summarized across all quantiles. Only returned if septau set to FALSE

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

References


Examples

```r
set.seed(1)
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75))
qic.select(m1)
```
Select tuning parameters using IC

Description

Selects tuning parameter $\lambda$ and $a$ according to information criterion of choice. For a given $\hat{\beta}$ the information criterion is calculated as

$$\log \left( \sum_{i=1}^{n} \rho_{\tau}(y_i - x_i^T \hat{\beta}) \right) + d * b / (2n),$$

where $d$ is the number of nonzero coefficients and $b$ depends on the method used. For AIC $b = 2$, for BIC $b = \log(n)$ and for PBIC $d = \log(n) * \log(p)$ where $p$ is the dimension of $\hat{\beta}$. If septau set to FALSE then calculations are made across the quantiles. Let $\hat{\beta}_q$ be the coefficient vector for the $q$th quantile of $Q$ quantiles. In addition let $d_q$ and $b_q$ be $d$ and $b$ values from the $q$th quantile model. Note, for all of these we are assuming eqn and $a$ are the same. Then the summary across all quantiles is

$$\sum_{q=1}^{Q} w_q \left[ \log \left( \sum_{i=1}^{n} \rho_{\tau}(y_i - x_i^T \hat{\beta}_q) \right) + d_q * b_q / (2n) \right],$$

where $w_q$ is the weight assigned for the $q$th quantile model.

Usage

```r
# S3 method for class 'rq.pen.seq.cv'
qic.select(
  obj,
  method = c("BIC", "AIC", "PBIC"),
  septau = TRUE,
  weights = NULL,
  ...
)
```

Arguments

- **obj** A rq.pen.seq.cv object.
- **method** Choice of BIC, AIC or PBIC, a large p BIC.
- **septau** If optimal values of $\lambda$ and $a$ can vary with $\tau$. Default is TRUE.
- **weights** Weights for each quantile. Useful if you set septau to FALSE but want different weights for the different quantiles. If not specified default is to have $w_q = 1$ for all quantiles.
- **...** Additional arguments.
Value

- coefficients: Coefficients of the selected models.
- ic: Information criterion values for all considered models.
- models: Info model info for the selected models related to the original object obj.
- gic: Information criterion summarized across all quantiles. Only returned if septau set to FALSE

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

References


Examples

```r
set.seed(1)
x <- matrix(runif(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75))
qic.select(m1)
```

QICD

*Implements QICD algorithm*

Description

Implements QICD algorithm

Usage

```r
QICD(
  y,
  x,
  tau = 0.5,
  lambda,
  intercept = TRUE,
  penalty = "SCAD",
  initial_beta = NULL,
  maxin = 100,
  maxout = 20,
  eps = 1e-05,
  coef.cutoff = 1e-08,
  a = 3.7,
)```
QICD.nonpen

scalex = TRUE,
...
)

Arguments

ty response variable, length n vector
x input nxp matrix, of dimension nobs x nvars; each row is an observation vector.
tau the quantile value
lambda the tuning parameter (numeric value > 0)
intercept a logical value, should intercept be fitted (default=TRUE) (intercept should be included when using splines)
penalty The name of the penalty function ("SCAD", "MCP", "LASSO")
initial_beta Vector containing initial values for intercept (if included) and x coefficients. Should be in the form (intercept, coefficients) intercept should be left out if intercept=FALSE.
maxin maximum number of iterations for inside coordinate descent, default value is 100
maxout maximum number of iterations for outside MM step, default value is 20
eps The convergence threshold for coordinate descent and majorization minimization step
coeff.cutoff Threshold for determining nonzero coefficients
a Scale parameter, the default value is 3.7 (>2 for SCAD, >1 for MCP, not used in LASSO)
scalex Whether predictors are centered and scaled
...
additional parameters

QICD.nonpen Implements QICD algorithm with some variables not being penalized

Description

Implements QICD algorithm with some variables not being penalized

Usage

QICD.nonpen( y, x, z, tau = 0.5, lambda, intercept = TRUE, penalty = "SCAD",...
initial_beta = NULL,
maxin = 100,
maxout = 20,
eps = 1e-05,
coef.cutoff = 1e-08,
a = 3.7,
method = "br",
scalex = TRUE,
...
}

Arguments

y                   response variable, length n vector
x                   input n x p matrix, of dimension nobs x nvars; each row is an observation vector.
z                   nxq matrix of bases; the coefficients for these columns will be unpenalized
 tau                the quantile value
lambda              the tuning parameter (numeric value > 0)
intercept           a logical value, should intercept be fitted (default=TRUE) (intercept should be included when using splines)
penalty              The name of the penalty function ("SCAD", "MCP", "LASSO")
initial_beta        Vector containing initial values for intercept (if included) and x coefficients. Should be in the form (intercept, coefficients) intercept should be left out if intercept=FALSE. The intercept should be included to be consistent with other methods, but intercept and z coefficients will be initialized to by a rq() fit of residuals from initial beta against the unpenalized predictors, z.
maxin               maximum number of iterations for inside coordinate descent, default value is 100
maxout              maximum number of iterations for outside MM step, default value is 20
eps                 The convergence threshold for coordinate descent and majorization minimization step
coef.cutoff         Threshold for determining nonzero coefficients
a                   Scale parameter, the default value is 3.7 (>2 for SCAD, >1 for MCP, not used in LASSO)
method              quantile regression initialization method, can be "br" or "fn".
scalex              Whether predictors are centered and scaled
...                  additional parameters
rq.group.fit

Estimates a quantile regression model with a group penalized objective function.

Description

Warning: function is deprecated and will not be exported in future R packages. Recommend using rq.group.pen() instead. Similar to cv.rq.pen function, but uses group penalty. Group penalties use the L1 norm instead of L2 for computational convenience. As a result of this the group lasso penalty is the same as the typical lasso penalty and thus you should only use a SCAD or MCP penalty. Only the SCAD and MCP penalties incorporate the group structure into the penalty. The group lasso penalty is implemented because it is needed for the SCAD and MCP algorithm. We use a group penalty extension of the QICD algorithm presented by Peng and Wang (2015).

Usage

rq.group.fit(
  x,
  y,
  groups,
  tau = 0.5,
  lambda,
  intercept = TRUE,
  penalty = "SCAD",
  alg = "QICD",
  a = 3.7,
  penGroups = NULL,
  ...
)

Arguments

- **x** Matrix of predictors.
- **y** Vector of responses.
- **groups** Vector of group assignments.
- **tau** Single quantile to be modeled.
- **lambda** Single value or separate value for each group.
- **intercept** Whether intercept should be included in the model or not.
- **penalty** Type of penalty used: SCAD, MCP or LASSO.
- **alg** Type of algorithm used: QICD or LP.
- **a** Additional tuning parameter for SCAD and MCP.
- **penGroups** Vector of TRUE and FALSE entries for each group determining if they should be penalized. Default is TRUE for all groups.
- **...** Additional arguments sent to rq.group.lin.prog()
Value

Returns the following:

• coefficients Coefficients of the model.
• residuals Residuals from the fitted model.
• rho Unpenalized portion of the objective function.
• tau Quantile being modeled.
• n Sample size.
• intercept Whether intercept was included in model.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu> and Adam Maidman

References


rq.group.pen

Fits quantile regression models using a group penalized objective function.

Description

Let the predictors be divided into G groups with G corresponding vectors of coefficients, $\beta_1, \ldots, \beta_G$. Let $\rho_\tau(a) = a[\tau - I(a < 0)]$. Fits quantile regression models for Q quantiles by minimizing the penalized objective function of

$$
\sum_{q=1}^{Q} \frac{1}{n} \sum_{i=1}^{n} \rho_{\tau}(y_i - x_i^\top \beta_q^*) + \sum_{q=1}^{Q} \sum_{g=1}^{G} P(||\beta_q^*||_{k}, w_q * v_j * \lambda, a).
$$

Where $w_q$ and $v_j$ are designated by penalty.factor and tau.penalty.factor respectively. The value of $k$ is chosen by norm. Value of $P()$ depends on the penalty. Briefly, but see references or vignette for more details,

• Group LASSO (gLASSO) $P(||\beta||_{k}, \lambda, a) = \lambda||\beta||_{k}$
• Group SCAD $P(||\beta||_{k}, \lambda, a) = \text{SCAD}||\beta||_{k}, \lambda, a)$
• Group MCP $P(||\beta||_{k}, \lambda, a) = \text{MCP}||\beta||_{k}, \lambda, a)$
• Group Adaptive LASSO $P(||\beta||_{k}, \lambda, a) = \frac{\lambda||\beta||_{k}}{||\beta||_{k}}$
Note if \( k = 1 \) and the group lasso penalty is used then this is identical to the regular lasso and thus function will stop and suggest that you use rq.pen() instead. For Adaptive LASSO the values of \( \beta_0 \) come from a Ridge solution with the same value of \( \lambda \). If the Huber algorithm is used than \( \rho_\tau(y_i - x_i^T \beta) \) is replaced by a Huber-type approximation. Specifically, it is replaced by \( h_\tau^\gamma(y_i - x_i^T \beta)/2 \) where

\[
h_\tau^\gamma(a) = a^2/(2\gamma)I(|a| \leq \gamma) + (|a| - \gamma/2)I(|a| > \gamma) + (2\tau - 1)a.
\]

Where if \( \tau = .5 \), we get the usual Huber loss function.

Usage

```r
rq.group.pen(
  x,
  y,
  tau = 0.5,
  groups = 1:ncol(x),
  penalty = c("gLASSO", "gAdLASSO", "gSCAD", "gMCP"),
  lambda = NULL,
  nlambda = 100,
  eps = ifelse(nrow(x) < ncol(x), 0.05, 0.01),
  alg = c("huber", "br", "qicd"),
  a = NULL,
  norm = 2,
  group.pen.factor = rep(1, length(unique(groups))),
  tau.penalty.factor = rep(1, length(tau)),
  scalex = TRUE,
  coef.cutoff = 1e-08,
  max.iter = 10000,
  converge.eps = 1e-07,
  gamma = IQR(y)/10,
  lambda.discard = TRUE,
  ...
)
```

Arguments

- **x**: Matrix of predictors.
- **y**: Vector of responses.
- **tau**: Vector of quantiles.
- **groups**: Vector of group assignments for predictors.
- **penalty**: Penalty used, choices are group lasso ("gLASSO"), group adaptive lasso ("gAdLASSO"), group SCAD ("gSCAD") and group MCP ("gMCP")
- **lambda**: Vector of lambda tuning parameters. Will be automatically generated if it is not set.
- **nlambda**: The number of lambda tuning parameters.
- **eps**: The value to be multiplied by the largest lambda value to determine the smallest lambda value.
alg
Algorithm used. Choices are Huber approximation ("huber"), linear programming ("lp") or quantile iterative coordinate descent ("qicd").

a
The additional tuning parameter for adaptive lasso, SCAD and MCP.

norm
Whether a L1 or L2 norm is used for the grouped coefficients.

group.pen.factor
Penalty factor for each group.

tau.penalty.factor
Penalty factor for each quantile.

cscale
Whether X should be centered and scaled so that the columns have mean zero and standard deviation of one. If set to TRUE, the coefficients will be returned to the original scale of the data.

coef.cutoff
Coefficient cutoff where any value below this number is set to zero. Useful for the lp algorithm, which are prone to finding almost, but not quite, sparse solutions.

max.iter
The maximum number of iterations for the algorithm.

converge.eps
The convergence criteria for the algorithms.

gamma
The tuning parameter for the Huber loss.

lambda.discard
Whether lambdas should be discarded if for small values of lambda there is very little change in the solutions.

... Additional parameters

Value
An rq.pen.seq object.

- modelsA list of each model fit for each tau and a combination.
- nSample size.
- pNumber of predictors.
- algAlgorithm used.
- tauQuantiles modeled.
- penaltyPenalty used.
- aTuning parameters a used.
- lambdaLambda values used for all models. If a model has fewer coefficients than lambda, say k. Then it used the first k values of lambda. Setting lambda.discard to TRUE will guarantee all values use the same lambdas, but may increase computational time noticeably and for little gain.
- modelsInfoInformation about the quantile and a value for each model.
- callOriginal call.

Each model in the models list has the following values.

- coefficientsCoefficients for each value of lambda.
- rhoThe unpenalized objective function for each value of lambda.
rq.group.pen.cv

- PenRho: The penalized objective function for each value of lambda.
- nzero: The number of nonzero coefficients for each value of lambda.
- tau: Quantile of the model.
- a: Value of a for the penalized loss function.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>, Shaobo Li <shaobo.li@ku.edu> and Adam Maidman

References


Examples

```r
## Not run:
set.seed(1)
x <- matrix(rnorm(200*8,sd=1),ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(200,3)
g <- c(1,1,1,2,2,2,3,3)
tvals <- c(.25,.75)
r1 <- rq.group.pen(x,y,groups=g)
r5 <- rq.group.pen(x,y,groups=g,tau=tvals)
#Linear programming approach with group SCAD penalty and L1-norm
m2 <- rq.group.pen(x,y,groups=g,alg="br",penalty="gSCAD",norm=1,a=seq(3,4))
# No penalty for the first group
m3 <- rq.group.pen(x,y,groups=g,group.pen.factor=c(0,rep(1,2)))
# Smaller penalty for the median
m4 <- rq.group.pen(x,y,groups=g,tau=c(.25,.5,.75),tau.penalty.factor=c(1,.25,1))
## End(Not run)
```

rq.group.pen.cv

Performs cross validation for a group penalty. #'

Description

Performs cross validation for a group penalty. #'

Usage

```r
rq.group.pen.cv(
  x,
  y,
  tau = 0.5,
  groups = 1:ncol(x),
  lambda = NULL,
)```

```
a = NULL,  
cvFunc = NULL,  
nfolds = 10,  
foldid = NULL,  
groupError = TRUE,  
cvSummary = mean,  
tauWeights = rep(1, length(tau)),  
printProgress = FALSE,  
...

Arguments

x  Matrix of predictors.
y  Vector of responses.
tau  Vector of quantiles.

groups  Vector of group assignments for the predictors.

lambda  Vector of lambda values, if set to NULL they will be generated automatically.
a  Vector of the other tuning parameter values.
cvFunc  Function used for cross-validation error, default is quantile loss.
nfolds  Number of folds used for cross validation.
foldid  Fold assignments, if not set this will be randomly created.
groupError  If errors are to be reported as a group or as the average for each fold.
cvSummary  
tauWeights  Weights for the tau penalty.
printProgress  If set to TRUE will print which fold the process is working on.
...
...  Additional parameters that will be sent to rq.group.pen().

Value

• cverrMatrix of cvSummary function, default is average, cross-validation error for each model, tau and a combination, and lambda.
• cvseMatrix of the standard error of cverr for each model, tau and a combination, and lambda.
• fitThe rq.pen.seq object fit to the full data.
• btrA data.table of the values of a and lambda that are best as determined by the minimum cross validation error and the one standard error rule, which fixes a. In btr the values of lambda and a are selected separately for each quantile.
• gtrA data.table for the combination of a and lambda that minimize the cross validation error across all tau.
• gcveGroup, across all quantiles, cross-validation error results for each value of a and lambda.
• callOriginal call to the function.
rq.lasso.fit

Estimates a quantile regression model with a lasso penalized quantile loss function.

Description

Fits a quantile regression model with the LASSO penalty. Uses the augmented data approach similar to the proposal in Sherwood and Wang (2016).

Usage

rq.lasso.fit(
  x,
  y,
  tau = 0.5,
  lambda = NULL,
  weights = NULL,
  intercept = TRUE,
  coef.cutoff = 1e-08,
  method = "br",
  penVars = NULL,
  scalex = TRUE,
  lambda.discard = TRUE,
  ...
)
Arguments

- **x**: Matrix of predictors.
- **y**: Vector of responses.
- **tau**: Quantile of interest.
- **lambda**: Tuning parameter.
- **weights**: Weights for the objective function.
- **intercept**: Whether model should include an intercept. Constant does not need to be included in "x".
- **coef.cutoff**: Coefficients below this value will be set to zero.
- **method**: Use method "br" or "fn" as outlined in quantreg package. We have found "br" to be more stable for penalized regression problems.
- **penVars**: Variables that should be penalized. With default value of NULL all variables are penalized.
- **scalex**: If set to true the predictors will be scaled to have mean zero and standard deviation of one before fitting the model. The output returned will be on the original scale of the data.
- **lambda.discard**: If TRUE lambda sequence will stop early if for small values of lambda the estimates do not change much.
- **...**: Additional items to be sent to rq. Note this will have to be done carefully as rq is run on the augmented data to account for penalization and could provide strange results if this is not taken into account.

Value

Returns the following:

- coefficients: Coefficients from the penalized model.
- PenRho: Penalized objective function value.
- residuals: Residuals from the model.
- rho: Objective function evaluation without the penalty.
- tau: Conditional quantile being modeled.
- n: Sample size.

References

Examples

```r
x <- matrix(rnorm(800), nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModel <- rq.lasso.fit(x, y, lambda=.1)
```

---

**Description**

Warning: this function is deprecated and will not be exported in future releases. Produces penalized quantile regression models for a range of lambdas and penalty of choice. If lambda is unselected than an iterative algorithm is used to find a maximum lambda such that the penalty is large enough to produce an intercept only model. Then range of lambdas goes from the maximum lambda found to "eps" on the log scale. Local linear approximation approach used by Wang, Wu and Li to extend LLA as proposed by Zou and Li (2008) to the quantile regression setting.

**Usage**

```r
rq.nc.fit(
  x, 
  y, 
  tau = 0.5, 
  lambda = NULL, 
  weights = NULL, 
  intercept = TRUE, 
  penalty = "SCAD", 
  a = 3.7, 
  iterations = 1, 
  converge_criteria = 1e-06, 
  alg = ifelse(p < 50, "LP", "QICD"), 
  penVars = NULL, 
  internal = FALSE, 
  ...
)
```

**Arguments**

- `x` Matrix of predictors.
- `y` Vector of response values.
- `tau` Conditional quantile being modelled.
- `lambda` Vector of lambdas. Default is for lambdas to be automatically generated.
- `weights` Weights for the objective function.
- `intercept` Whether model should include an intercept. Constant does not need to be included in "x".
penalty Type of penalty: "LASSO", "SCAD" or "MCP".

a Additional tuning parameter for SCAD and MCP

iterations Number of iterations to be done for iterative LLA algorithm.

converge_criteria Difference in betas from iteration process that would satisfy convergence.

alg Defaults for small p to linear programming (LP), see Wang, Wu and Li (2012) for details. Otherwise a coordinate descent algorithm is used (QICD), see Peng and Wang (2015) for details. Both methods rely on the One-step sparse estimates algorithm.

penVars Variables that should be penalized. With default value of NULL all variables are penalized.

internal Whether call to this function has been made internally or not.

... Additional items to be sent to rq.lasso.fit.

Value

Returns the following:

- coefficients Coefficients from the penalized model.
- PenRho Penalized objective function value.
- residuals Residuals from the model.
- rho Objective function evaluation without the penalty.
- coefficients Coefficients from the penalized model.
- tau Conditional quantile being modeled.
- n Sample size.
- penalty Penalty used, SCAD or MCP.
- penaltyPenalty selected.

Author(s)

Ben Sherwood, <ben.sherwood@ku.edu> and Adam Maidman.

References

Examples

```r
x <- matrix(rnorm(800), nrow = 100)
y <- 1 + x[, 1] - 3 * x[, 5] + rnorm(100)
scadModel <- rq.nc.fit(x, y, lambda = 1)
```

---

**rq.pen**

Fit a quantile regression model using a penalized quantile loss function.

---

**Description**

Let $q$ index the $Q$ quantiles of interest. Let $\rho_\tau(a) = a[\tau - I(a < 0)]$. Fits quantile regression models by minimizing the penalized objective function of

$$
\frac{1}{n} \sum_{q=1}^{Q} \sum_{i=1}^{n} \rho_\tau(y_i - x_i^T \beta_q) + \sum_{q=1}^{Q} \sum_{p=1}^{P} P(q, q, w, v, \lambda, a).
$$

Where $w_q$ and $v_j$ are designated by penalty.factor and tau.penalty.factor respectively. Value of $P()$ depends on the penalty. See references or vignette for more details,

- **LASSO:** $P(\beta, \lambda, a) = \lambda |\beta|$  
- **SCAD:** $P(\beta, \lambda, a) = SCAD(\beta, \lambda, a)$  
- **MCP:** $P(\beta, \lambda, a) = MCP(\beta, \lambda, a)$  
- **Ridge:** $P(\beta, \lambda, a) = \lambda \beta^2$  
- **Elastic Net:** $P(\beta, \lambda, a) = a \lambda |\beta| + (1 - a) \lambda * \beta^2$  
- **Adaptive LASSO:** $P(\beta, \lambda, a) = \frac{\lambda |\beta|}{|\beta_0|}$

For Adaptive LASSO the values of $\beta_0$ come from a Ridge solution with the same value of $\lambda$. Three different algorithms are implemented

- **huber:** Uses a Huber approximation of the quantile loss function. See Yi and Huang 2017 for more details.
- **br:** Solution is found by re-formulating the problem so it can be solved with the rq() function from quantreg with the br algorithm.
- **QICD:** A coordinate descent algorithm for SCAD and MCP penalties, see Peng and Wang (2015) for details.

The huber algorithm offers substantial speed advantages without much, if any, loss in performance. However, it should be noted that it solves an approximation of the quantile loss function.
Usage

\[
\text{rq.pen}( \\
\text{x,} \\
\text{y,} \\
\text{tau = 0.5,} \\
\text{lambda = NULL,} \\
\text{penalty = c("LASSO", "Ridge", "ENet", "aLASSO", "SCAD", "MCP"),} \\
\text{a = NULL,} \\
\text{nlambda = 100,} \\
\text{eps = ifelse(nrow(x) < ncol(x), 0.05, 0.01),} \\
\text{penalty.factor = rep(1, ncol(x)),} \\
\text{alg = c("huber", "br", "QICD", "fn"),} \\
\text{scalex = TRUE,} \\
\text{tau.penalty.factor = rep(1, length(tau)),} \\
\text{coef.cutoff = 1e-08,} \\
\text{max.iter = 10000,} \\
\text{converge.eps = 1e-07,} \\
\text{lambda.discard = TRUE,} \\
\text{...} \\
\)

Arguments

- **x**: matrix of predictors
- **y**: vector of responses
- **tau**: vector of quantiles
- **lambda**: vector of lambda, if not set will be generated automatically
- **penalty**: choice of penalty
- **a**: Additional tuning parameter, not used for lasso or ridge penalties. However, will be set to the elastic net values of 1 and 0 respectively. Defaults are ENet(0), aLASSO(1), SCAD(3.7) and MCP(3).
- **nlambda**: number of lambda, ignored if lambda is set
- **eps**: If not pre-specified the lambda vector will be from lambda_max to lambda_max times eps
- **penalty.factor**: penalty factor for the predictors
- **alg**: Algorithm used.
- **scalex**: Whether x should be scaled before fitting the model. Coefficients are returned on the original scale.
- **tau.penalty.factor**: A penalty factor for each quantile.
- **coef.cutoff**: Some of the linear programs will provide very small, but not sparse solutions. Estimates below this number will be set to zero. This is ignored if a non-linear programming algorithm is used.
- **max.iter**: Maximum number of iterations of non-linear programming algorithms.
Convergence threshold for non-linear programming algorithms.

Algorithm may stop for small values of lambda if the coefficient estimates are not changing drastically. One example of this is it is possible for the LLA weights of the non-convex functions to all become zero and smaller values of lambda are extremely likely to produce the same zero weights.

Extra parameters.

Value

An `rq.pen.seq` object.

- `models`: A list of each model fit for each tau and a combination.
- `n`: Sample size.
- `p`: Number of predictors.
- `alg`: Algorithm used. Options are "huber", "qicd" or any method implemented in `rq()`, such as "br".
- `tau`: Quantiles modeled.
- `a`: Tuning parameters a used.
- `modelsInfo`: Information about the quantile and a value for each model.
- `lambda`: Lambda values used for all models. If a model has fewer coefficients than lambda, say k. Then it used the first k values of lambda. Setting lambda.discard to TRUE will guarantee all values use the same lambdas, but may increase computational time noticeably and for little gain.
- `penalty`: Penalty used.
- `call`: Original call.

Each model in the models list has the following values.

- `coefficients`: Coefficients for each value of lambda.
- `rho`: The unpenalized objective function for each value of lambda.
- `PenRho`: The penalized objective function for each value of lambda.
- `nzero`: The number of nonzero coefficients for each value of lambda.
- `tau`: Quantile of the model.
- `a`: Value of a for the penalized loss function.

If the Huber algorithm is used than $\rho_\tau(y_i - x_i^T \beta)$ is replaced by a Huber-type approximation. Specifically, it is replaced by $h_\tau^\gamma(y_i - x_i^T \beta)/2$ where

$$h_\tau^\gamma(a) = \frac{a^2}{(2\gamma)I(|a| \leq \gamma) + (|a| - \gamma/2)I(|a| > \gamma) + (2\tau - 1)a}.$$ 

Where if $\tau = .5$, we get the usual Huber loss function. The Huber implementation calls the package `hqreg` which implements the methods of Yi and Huang (2017) for Huber loss with elastic net penalties. For non-elastic net penalties the LLA algorithm of Zou and Li (2008) is used to approximate those loss functions with a lasso penalty with different weights for each predictor.
Author(s)
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References

Examples
n <- 200
p <- 8
x <- matrix(runif(n*p),ncol=p)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
r1 <- rq.pen(x,y) #Lasso fit for median
# Lasso for multiple quantiles
r2 <- rq.pen(x,y,tau=c(.25,.5,.75))
# Elastic net fit for multiple quantiles, which must use Huber algorithm
r3 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),alg="huber")
# First variable is not penalized
r4 <- rq.pen(x,y,penalty.factor=c(0,rep(1,7))
tvals <- c(.1,.2,.3,.4,.5)
#Similar to penalty proposed by Belloni and Chernouzhkov.
#To be exact you would divide the tau.penalty.factor by n.
r5 <- rq.pen(x,y,tau=tvals, tau.penalty.factor=sqrt(tvals*(1-tvals))

rq.pen.cv

Does k-folds cross validation for rq.pen. If multiple values of a are specified then does a grid based search for best value of \( \lambda \) and a.

Description
Does k-folds cross validation for rq.pen. If multiple values of a are specified then does a grid based search for best value of \( \lambda \) and a.

Usage
rq.pen.cv(
x,
y,
tau = 0.5,
lambda = NULL,
penalty = c("LASSO", "Ridge", "ENet", "aLASSO", "SCAD", "MCP"),
a = NULL,
cvFunc = NULL,
nfolds = 10,
foldid = NULL,
nlambda = 100,
groupError = TRUE,
cvSummary = mean,
tauWeights = rep(1, length(tau)),
printProgress = FALSE,
...  
)

Arguments

x Matrix of predictors.
y Vector of responses.
tau Quantiles to be modeled.
lambda Values of λ. Default will automatically select the λ values.
penalty Choice of penalty between LASSO, Ridge, Elastic Net (ENet), Adaptive Lasso (aLASSO), SCAD and MCP.
a Tuning parameter of a. LASSO and Ridge has no second tuning parameter, but for notation is set to 1 or 0 respectively, the values for elastic net. Defaults are Ridge ()
cvFunc Loss function for cross-validation. Defaults to quantile loss, but user can specify their own function.
nfolds Number of folds.
foldid Ids for folds. If set will override nfolds.
nlambda Number of lambda, ignored if lambda is set.
groupError If set to false then reported error is the sum of all errors, not the sum of error for each fold.
cvSummary Function to summarize the errors across the folds, default is mean. User can specify another function, such as median.
tauWeights Weights for the different tau models.
printProgress If set to TRUE prints which partition is being worked on.
... Additional arguments passed to rq.pen()

Details

Two cross validation results are returned. One that considers the best combination of a and lambda for each quantile. The second considers the best combination of the tuning parameters for all quantiles. Let \( y_{b,i} \) and \( x_{b,i} \) index the observations in fold b. Let \( \hat{\beta}_{r,a,\lambda}^{b} \) be the estimator for a given
quantile and tuning parameters that did not use the bth fold. Let \( n_b \) be the number of observations in fold \( b \). Then the cross validation error for fold \( b \) is

\[
CV(b, \tau) = \frac{1}{n_b} \sum_{i=1}^{n_b} \rho_{\tau}(y_{b,i} - x_{b,i}^\top \hat{\beta}_{b,\tau,a,\lambda}).
\]

Note that \( \rho_{\tau}() \) can be replaced by a different function by setting the cvFunc parameter. The function returns two different cross-validation summaries. The first is btr, by tau results. It provides the values of lambda and a that minimize the average, or whatever function is used for cvSummary, of \( CV(b) \). In addition it provides the sparsest solution that is within one standard error of the minimum results.

The other approach is the group tau results, gtr. Consider the case of estimating \( Q \) quantiles of \( \tau_1, \ldots, \tau_Q \). It returns the values of lambda and a that minimizes the average, or again whatever function is used for cvSummary, of

\[
\sum_{q=1}^{Q} CV(b, \tau_q).
\]

If only one quantile is modeled then the gtr results can be ignored as they provide the same minimum solution as btr.

Value

- cverr: Matrix of cvSummary function, default is average, cross-validation error for each model, tau and a combination, and lambda.
- cvse: Matrix of the standard error of cverr foreach model, tau and a combination, and lambda.
- fit: The rq.pen.seq object fit to the full data.
- btr: A data.table of the values of a and lambda that are best as determined by the minimum cross validation error and the one standard error rule, which fixes a. In btr the values of lambda and a are selected seperately for each quantile.
- gtr: A data.table for the combination of a and lambda that minimize the cross validation error across all tau.
- gcve: Group, across all quantiles, cross-validation error results for each value of a and lambda.
- call: Original call to the function.

Author(s)

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Examples

```r
## Not run:
x <- matrix(runif(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
r1 <- rq.pen.cv(x,y) #lasso fit for median
# Elastic net fit for multiple values of a and tau
r2 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.5,.75))
#same as above but more weight given to median when calculating group cross validation error.
r3 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.5,.75),tauWeights=c(.25,.5,.25))
```
rqPen

Description

The package estimates a quantile regression model using LASSO, Adaptive LASSO, SCAD, MCP, elastic net, and their group counterparts, with the exception of elastic net for which there is no group penalty implementation.

rqPen functions

The most important functions are rq.pen(), rq.group.pen(), rq.pen.cv() and rq.group.pen.cv(). These functions fit quantile regression models with individual or group penalties. The cv functions automate the cross-validation process for selection of tuning parameters.

```r
# uses median cross-validation error instead of mean.
r4 <- rq.pen.cv(x,y,cvSummary=median)
#Cross-validation with no penalty on the first variable.
r5 <- rq.pen.cv(x,y,penalty.factor=c(1,rep(0,7)))
## End(Not run)
```
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