Package ‘semTools’

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R topics documented:

auxiliary .................................................. 4
BootMiss-class............................................ 6
bsBootMiss ............................................... 7
calculate.D2 ............................................. 9
chisqSmallN ............................................ 11
clipboard ............................................... 12
combinequark .......................................... 14
compareFit ............................................. 15
dat2way ................................................ 17
dat3way ................................................ 18
datCat .................................................. 19
EFA-class ................................................ 20
efa.ekc .................................................. 21
efaUnrotate ............................................ 23
exLong ................................................... 24
findRMSEApower ....................................... 25
findRMSEApowernested ............................... 26
findRMSEAsamplesize ................................. 27
findRMSEAsamplesizenested .......................... 28
FitDiff-class .......................................... 30
fmi ....................................................... 31
html ..................................................... 33
imposeStart ........................................... 35
indProd ................................................ 37
kd ......................................................... 40
kurtosis ................................................ 41
lavaan.mi-class ...................................... 43
lavTestLRT.mi ......................................... 47
lavTestScore.mi ....................................... 49
lavTestWald.mi ......................................... 52
loadingFromAlpha ..................................... 54
mardiaKurtosis ....................................... 55
mardiaSkew ............................................ 56
maximalRelia .......................................... 57
measEq.syntax .................................................. 59
measEq.syntax-class ....................................... 65
miPowerFit .................................................... 67
modindices.mi ............................................... 70
monteCarloMed .............................................. 73
moreFitIndices .............................................. 75
mvrnnonnorm ............................................... 78
net .......................................................... 79
Net-class ..................................................... 81
nullRMSEA .................................................. 82
orthRotate .................................................. 83
parcelAllocation .......................................... 85
partialInvariance ......................................... 88
PAVranking .................................................. 93
permuteMeasEq ............................................ 97
permuteMeasEq-class .................................... 106
plotProbe ................................................... 109
plotRMSEAdist ............................................ 111
plotRMSEApower .......................................... 113
plotRMSEApowernested .................................. 115
poolMAlloc ................................................ 116
probe2WayMC .............................................. 120
probe2WayRC .............................................. 123
probe3WayMC .............................................. 126
probe3WayRC .............................................. 129
quark ....................................................... 132
reliability .................................................. 135
reliabilityL2 ............................................... 138
residualCovariate ........................................ 139
runMI ....................................................... 140
semTools .................................................... 144
simParcel ................................................... 145
singleParamTest .......................................... 146
skew ......................................................... 147
splitSample ................................................ 149
SSpower ..................................................... 150
tukeySEM .................................................. 153
twostage ..................................................... 154
twostage-class ............................................ 157

Index ......................................................... 160
Implement Saturated Correlates with FIML

Description
Automatically add auxiliary variables to a lavaan model when using full information maximum likelihood (FIML) to handle missing data.

Usage
```r
auxiliary(model, data, aux, fun, ...)
```

```r
dataNauxiliary(model, data, aux, ...)
cfaNauxiliary(model, data, aux, ...)
semNauxiliary(model, data, aux, ...)
growthNauxiliary(model, data, aux, ...)
```

Arguments
- **model**: The analysis model can be specified with 1 of 2 objects:
  1. lavaan `model.syntax` specifying a hypothesized model without mention of auxiliary variables in `aux`
  2. a parameter table, as returned by `parTable`, specifying the target model without auxiliary variables. This option requires these columns (and silently ignores all others): c("lhs","op","rhs","user","group","free","label","plabel","start"
- **data**: data.frame that includes auxiliary variables as well as any observed variables in the model
- **aux**: character. Names of auxiliary variables to add to model
- **fun**: character. Name of a specific lavaan function used to fit model to data (i.e., "lavaan", "cfa", "sem", or "growth"). Only required for auxiliary.
- ... additional arguments to pass to `lavaan`

Details
These functions are wrappers around the corresponding lavaan functions. You can use them the same way you use `lavaan`, but you must pass your full data.frame to the data argument. Because the saturated-correlates approaches (Enders, 2008) treats exogenous variables as random, `fixed.x` must be set to FALSE. Because FIML requires continuous data (although nonnormality corrections can still be requested), no variables in the model nor auxiliary variables specified in `aux` can be declared as ordered.
auxiliary

Value

A fitted lavaan object. Additional information is stored as a list in the \@external slot:

- baseline.model. A fitted lavaan object. Results of fitting an appropriate independence model for the calculation of incremental fit indices (e.g., CFI, TLI) in which the auxiliary variables remain saturated, so only the target variables are constrained to be orthogonal. See Examples for how to send this baseline model to fitMeasures.
- aux. The character vector of auxiliary variable names.
- baseline.syntax. A character vector generated within the auxiliary function, specifying the baseline.model syntax.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

dat1 <- lavaan::HolzingerSwineford1939
set.seed(12345)
dat1$z <- rnorm(nrow(dat1))
dat1$x5 <- ifelse(dat1$z < quantile(dat1$z, .3), NA, dat1$x5)
dat1$x9 <- ifelse(dat1$z > quantile(dat1$z, .8), NA, dat1$x9)

targetModel <- "
  visual  =~ x1 + x2 + x3
  textual =~ x4 + x5 + x6
  speed   =~ x7 + x8 + x9"

## works just like cfa(), but with an extra "aux" argument
fitaux1 <- cfa.auxiliary(targetModel, data = dat1, aux = "z",
                         missing = "fiml", estimator = "mlr")

## with multiple auxiliary variables and multiple groups
fitaux2 <- cfa.auxiliary(targetModel, data = dat1, aux = c("z","ageyr","grade"),
                         group = "school", group.equal = "loadings")

## calculate correct incremental fit indices (e.g., CFI, TLI)
fitMeasures(fitaux2, fit.measures = c("cfi","tli"))
## NOTE: lavaan will use the internally stored baseline model, which
## is the independence model plus saturated auxiliary parameters
lavInspect(fitaux2@external$baseline.model, "free")
BootMiss-class

Class For the Results of Bollen-Stine Bootstrap with Incomplete Data

Description

This class contains the results of Bollen-Stine bootstrap with missing data.

Usage

## S4 method for signature 'BootMiss'
show(object)

## S4 method for signature 'BootMiss'
summary(object)

## S4 method for signature 'BootMiss'
hist(x, ..., alpha = 0.05, nd = 2,
printLegend = TRUE, legendArgs = list(x = "topleft"))

Arguments

- object, x: object of class BootMiss
- ...: Additional arguments to pass to hist
- alpha: alpha level used to draw confidence limits
- nd: number of digits to display
- printLegend: logical. If TRUE (default), a legend will be printed with the histogram
- legendArgs: list of arguments passed to the legend function. The default argument is a list placing the legend at the top-left of the figure.

Value

The hist method returns a list of length == 2, containing the arguments for the call to hist and the arguments to the call for legend, respectively.

Slots

- time: A list containing 2 diffTime objects (transform and fit), indicating the time elapsed for data transformation and for fitting the model to bootstrap data sets, respectively.
- transData: Transformed data
- bootDist: The vector of $\chi^2$ values from bootstrap data sets fitted by the target model
- origChi: The $\chi^2$ value from the original data set
- df: The degree of freedom of the model
- bootP: The p value comparing the original $\chi^2$ with the bootstrap distribution
Objects from the Class

Objects can be created via the \texttt{bsBootMiss} function.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

See Also

\texttt{bsBootMiss}

Examples

\begin{verbatim}
# See the example from the bsBootMiss function
\end{verbatim}

\begin{verbatim}
bsBootMiss
\end{verbatim}

\textbf{Description}

Implement the Bollen and Stine's (1992) Bootstrap when missing observations exist. The implemented method is proposed by Savalei and Yuan (2009). This can be used in two ways. The first and easiest option is to fit the model to incomplete data in \texttt{lavaan} using the FIML estimator, then pass that \texttt{lavaan} object to \texttt{bsBootMiss}.

\textbf{Usage}

\begin{verbatim}
bsBootMiss(x, transformation = 2, nBoot = 500, model, rawdata, Sigma,
Mu, group, ChiSquared, EMcov, writeTransData = FALSE,
transDataOnly = FALSE, writeBootData = FALSE,
bootSamplesOnly = FALSE, writeArgs, seed = NULL,
suppressWarn = TRUE, showProgress = TRUE, ...)
\end{verbatim}

\textbf{Arguments}

\begin{itemize}
  \item \texttt{x} \hspace{1cm} A target \texttt{lavaan} object used in the Bollen-Stine bootstrap
  \item \texttt{transformation} \hspace{1cm} The transformation methods in Savalei and Yuan (2009). There are three methods in the article, but only the first two are currently implemented here. Use \texttt{transformation = 1} when there are few missing data patterns, each of which has a large size, such as in a planned-missing-data design. Use \texttt{transformation = 2} when there are more missing data patterns. The currently unavailable \texttt{transformation = 3} would be used when several missing data patterns have \texttt{n = 1}.
  \item \texttt{nBoot} \hspace{1cm} The number of bootstrap samples.
  \item \texttt{model} \hspace{1cm} Optional. The target model if \texttt{x} is not provided.
\end{itemize}
**rawData**  Optional. The target raw data set if x is not provided.

**Sigma**  Optional. The model-implied covariance matrix if x is not provided.

**Mu**  Optional. The model-implied mean vector if x is not provided.

**group**  Optional character string specifying the name of the grouping variable in rawData if x is not provided.

**ChiSquared**  Optional. The model’s $\chi^2$ test statistic if x is not provided.

**EMcov**  Optional, if x is not provided. The EM (or Two-Stage ML) estimated covariance matrix used to speed up Transformation 2 algorithm.

**writeTransData**  Logical. If TRUE, the transformed data set is written to a text file, transDataOnly is set to TRUE, and the transformed data is returned invisibly.

**transDataOnly**  Logical. If TRUE, the result will provide the transformed data only.

**writeBootData**  Logical. If TRUE, the stacked bootstrap data sets are written to a text file, bootSamplesOnly is set to TRUE, and the list of bootstrap data sets are returned invisibly.

**bootSamplesOnly**  Logical. If TRUE, the result will provide bootstrap data sets only.

**writeArgs**  Optional list. If writeBootData = TRUE or writeBootData = TRUE, user can pass arguments to the write.table function as a list. Some default values are provided: file = "bootstrappedSamples.dat", row.names = FALSE, and na = "-999", but the user can override all of these by providing other values for those arguments in the writeArgs list.

**seed**  The seed number used in randomly drawing bootstrap samples.

**suppressWarn**  Logical. If TRUE, warnings from lavaan function will be suppressed when fitting the model to each bootstrap sample.

**showProgress**  Logical. Indicating whether to display a progress bar while fitting models to bootstrap samples.

...  The additional arguments in the lavaan function. See also lavOptions

**Details**

The second is designed for users of other software packages (e.g., LISREL, EQS, Amos, or Mplus). Users can import their data, $\chi^2$ value, and model-implied moments from another package, and they have the option of saving (or writing to a file) either the transformed data or bootstrapped samples of that data, which can be analyzed in other programs. In order to analyze the bootstrapped samples and return a $p$ value, users of other programs must still specify their model using lavaan syntax.

**Value**

As a default, this function returns a BootMiss object containing the results of the bootstrap samples. Use show, summary, or hist to examine the results. Optionally, the transformed data set is returned if transDataOnly = TRUE. Optionally, the bootstrap data sets are returned if bootSamplesOnly = TRUE.

**Author(s)**

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

Syntax for transformations borrowed from http://www2.psych.ubc.ca/~vsavalei/
References


See Also

*BootMiss*

Examples

```r
## Not run:
dat1 <- HolzingerSwineford1939
dat1$x5 <- ifelse(dat1$x1 <= quantile(dat1$x1, .3), NA, dat1$x5)
dat1$x9 <- ifelse(is.na(dat1$x5), NA, dat1$x9)

targetModel <- "
visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9"

targetFit <- sem(targetModel, dat1, meanstructure = TRUE, std.lv = TRUE,
                 missing = "fiml", group = "school")
summary(targetFit, fit = TRUE, standardized = TRUE)

# The number of bootstrap samples should be much higher.
temp <- bsBootMiss(targetFit, transformation = 1, nBoot = 10, seed = 31415)

temp
summary(temp)
hist(temp)
hist(temp, printLegend = FALSE) # suppress the legend
## user can specify alpha level (default: alpha = 0.05), and the number of
## digits to display (default: nd = 2). Pass other arguments to hist(...),
## or a list of arguments to legend() via "legendArgs"
hist(temp, alpha = .01, nd = 3, xlab = "something else", breaks = 25,
     legendArgs = list("bottomleft", box.lty = 2))

## End(Not run)
```
Description

This is a utility function used to calculate the "D2" statistic for pooling test statistics across multiple imputations. This function is called by several functions used for lavaan.mi objects, such as lavTestLRT.mi, lavTestWald.mi, and lavTestScore.mi. But this function can be used for any general scenario because it only requires a vector of \(\chi^2\) statistics (one from each imputation) and the degrees of freedom for the test statistic. See Li, Meng, Raghunathan, & Rubin (1991) and Enders (2010, chapter 8) for details about how it is calculated.

Usage

calculate.D2(w, DF = 0L, asymptotic = FALSE)

Arguments

- \(w\): numeric vector of Wald \(\chi^2\) statistics. Can also be Wald \(z\) statistics, which will be internally squared to make \(\chi^2\) statistics with one \(df\) (must set \(DF = 0L\)).
- \(DF\): degrees of freedom (\(df\)) of the \(\chi^2\) statistics. If \(DF = 0L\) (default), \(w\) is assumed to contain \(z\) statistics, which will be internally squared.
- \(asymptotic\): logical. If \(FALSE\) (default), the pooled test will be returned as an \(F\)-distributed statistic with numerator (\(df1\)) and denominator (\(df2\)) degrees of freedom. If \(TRUE\), the pooled \(F\) statistic will be multiplied by its \(df1\) on the assumption that its \(df2\) is sufficiently large enough that the statistic will be asymptotically \(\chi^2\) distributed with \(df1\).

Value

A numeric vector containing the test statistic, \(df\), and a \(p\) value.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


See Also

lavTestLRT.mi, lavTestWald.mi, lavTestScore.mi

Examples

```r
## generate a vector of chi-squared values, just for example
DF <- 3 # degrees of freedom
M <- 20 # number of imputations
CHI <- rchisq(M, DF)
```
chisqSmallN

## pool the "results"
calculate.D2(CHI, DF) # by default, an F statistic is returned
calculate.D2(CHI, DF, asymptotic = TRUE) # asymptotically chi-squared

## generate standard-normal values, for an example of Wald z tests
Z <- rnorm(M)
calculate.D2(Z) # default DF = 0 will square Z to make chisq(DF = 1)
## F test is equivalent to a t test with the denominator DF

---

chisqSmallN | \textit{k-factor correction for chi}^2 \textit{test statistic}

### Description

Calculate \textit{k-factor correction for chi}^2 \textit{model-fit test statistic} to adjust for small sample size.

### Usage

\[
\text{chisqSmallN(\texttt{fit0}, \texttt{fit1 = NULL}, ...)}
\]

### Arguments

- **fit0**
  The lavaan model object provided after running the \texttt{cfa}, \texttt{sem}, \texttt{growth}, or \texttt{lavaan} functions.
- **fit1**
  Optional additional \texttt{lavaan} model, in which \texttt{fit0} is nested. If \texttt{fit0} has fewer \textit{df} than \texttt{fit1}, the models will be swapped, still on the assumption that they are nested.
- **...**
  Additional arguments to the \texttt{lavTestLRT} function.

### Details

The \textit{k-factor correction} (Nevitt & Hancock, 2004) is a global fit index which can be computed by:

\[
k_c = 1 - \frac{2 \times P + 4 \times K + 5}{6 \times N}
\]

where \(N\) is the sample size when using normal likelihood, or \(N-1\) when using likelihood = 'wishart'.

### Value

A numeric vector including the unadjusted (naive) chi-squared test statistic, the \textit{k-factor correction}, the corrected test statistic, the \textit{df} for the test, and the \textit{p} value for the test under the null hypothesis that the model fits perfectly (or that the 2 models have equivalent fit).
Author(s)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References

Examples
```
HS.model <- ' 
  visual  =~ x1 + b1*x2 + x3
  textual =~ x4 + b2*x5 + x6
  speed   =~ x7 + b3*x8 + x9
',
fit1 <- cfa(HS.model, data = HolzingerSwineford1939)
## test a single model (implicitly compared to a saturated model)
chisqSmallN(fit1)

## fit a more constrained model
fit0 <- cfa(HS.model, data = HolzingerSwineford1939, orthogonal = TRUE)
## compare 2 models
chisqSmallN(fit1, fit0)
```

Description
Copy or save the result of lavaan or FitDiff objects into a clipboard or a file. From the clipboard, users may paste the result into the Microsoft Excel or spreadsheet application to create a table of the output.

Usage
```
clipboard(object, what = "summary", ...)
saveFile(object, file, what = "summary", tableFormat = FALSE,
          fit.measures = "default", writeArgs = list(), ...)
```

Arguments
```
object The lavaan or FitDiff object
```
clipboard

what

The attributes of the lavaan object to be copied in the clipboard. "summary" is to copy the screen provided from the summary function. "mifit" is to copy the result from the miPowerFit function. Other attributes listed in the inspect method in the lavaan-class could also be used, such as "coef", "se", "fit", "samp", and so on. For the FitDiff object, this argument is not active yet.

... Additional argument listed in the miPowerFit function (for lavaan object only).

file

A file name used for saving the result

tableFormat

If TRUE, save the result in the table format using tabs for separation. Otherwise, save the result as the output screen printed in the R console.

fit.measures

character vector specifying names of fit measures returned by fitMeasures to be copied/saved. Only relevant if object is class FitDiff.

writeArgs

list of additional arguments to be passed to write.table

Value

The resulting output will be saved into a clipboard or a file. If using the clipboard function, users may paste it in the other applications.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

Examples

```r
## Not run:
library(lavaan)
HW.model <- 'visual  =~ x1 + c1*x2 + x3
textual  =~ x4 + c1*x5 + x6
      speed  =~ x7 + x8 + x9'

fit <- cfa(HW.model, data=HolzingerSwineford1939, group="school", meanstructure=TRUE)

# Copy the summary of the lavaan object
clipboard(fit)

# Copy the modification indices and the model fit from the miPowerFit function
clipboard(fit, "mifit")

# Copy the parameter estimates
clipboard(fit, "coef")

# Copy the standard errors
clipboard(fit, "se")

# Copy the sample statistics
clipboard(fit, "samp")
```
## combinequark

**Combine the results from the quark function**

### Description

This function builds upon the `quark` function to provide a final dataset comprised of the original dataset provided to `quark` and enough principal components to be able to account for a certain level of variance in the data.

### Usage

```r
combinequark(quark, percent)
```

### Arguments

- **quark**
  - Provide the `quark` object that was returned. It should be a list of objects. Make sure to include it in its entirety.

- **percent**
  - Provide a percentage of variance that you would like to have explained. That many components (columns) will be extracted and kept with the output dataset. Enter this variable as a number WITHOUT a percentage sign.

### Value

The output of this function is the original dataset used in `quark` combined with enough principal component scores to be able to account for the amount of variance that was requested.
compareFit

Author(s)
Steven R. Chesnut (University of Southern Mississippi <Steven.Chesnut@usm.edu>)

See Also
quark

Examples

set.seed(123321)
dat <- HolzingerSwineford1939[,7:15]
misspat <- matrix(runif(nrow(dat) * 9) < 0.3, nrow(dat))
dat[misspat] <- NA
dat <- cbind(HolzingerSwineford1939[,1:3], dat)
quark.list <- quark(data = dat, id = c(1, 2))
final.data <- combinequark(quark = quark.list, percent = 80)

---

**compareFit**

*Build an object summarizing fit indices across multiple models*

**Description**

This function will create the template to compare fit indices across multiple fitted lavaan objects. The results can be exported to a clipboard or a file later.

**Usage**

```r
compareFit(..., nested = TRUE, argsLRT = list(), indices = TRUE,
baseline.model = NULL)
```

**Arguments**

- `...`
  - fitted lavaan models or list(s) of lavaan objects. *lavaan.mi* objects are also accepted, but all models must belong to the same class.
- `nested`
  - logical indicating whether the models in `...` are nested. See `net` for an empirical test of nesting.
- `argsLRT`
  - list of arguments to pass to `lavTestLRT`, or to `lavTestLRT.mi` when comparing *lavaan.mi* models.
- `indices`
  - logical indicating whether to return fit indices from the `fitMeasures` function.
- `baseline.model`
  - optional fitted *lavaan* model passed to `fitMeasures` to calculate incremental fit indices.
Value

A `FitDiff` object that saves model fit comparisons across multiple models. If the models are not nested, only fit indices for each model are returned. If the models are nested, the differences in fit indices are additionally returned, as well as test statistics comparing each sequential pair of models (ordered by their degrees of freedom).

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

See Also

`FitDiff`, `clipboard`

Examples

```r
HS.model <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9 '

fit1 <- cfa(HS.model, data = HolzingerSwineford1939)

# non-nested model
m2 <- ' f1 = x1 + x2 + x3 + x4 
f2 = x5 + x6 + x7 + x8 + x9 '
fit2 <- cfa(m2, data = HolzingerSwineford1939)
compareFit(fit1, fit2, nested = FALSE)

# nested model comparisons:
out <- measurementInvariance(model = HS.model, data = HolzingerSwineford1939,
                              group = "school", quiet = TRUE)
compareFit(out)

# Not run:
# also applies to lavaan.mi objects (fit model to multiple imputations)
set.seed(12345)
HSMiss <- HolzingerSwineford1939[, paste("x", 1:9, sep = ",")]
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
HSMiss$x9 <- ifelse(is.na(HSMiss$x9), NA, HSMiss$x9)
HSMiss$school <- HolzingerSwineford1939$school
HS.amelia <- amelia(HSMiss, m = 20, noms = "school")
imps <- HS.amelia$imputations

# request robust test statistics
mgfit2 <- cfa.mi(HS.model, data = imps, group = "school", estimator = "mlm")
mgfit1 <- cfa.mi(HS.model, data = imps, group = "school", estimator = "mlm",
                group.equal = "loadings")
mgfit0 <- cfa.mi(HS.model, data = imps, group = "school", estimator = "mlm")
```
dat2way

```r

group.equal = c("loadings", "intercepts")

## request the strictly-positive robust test statistics
compareFit(scalar = mgfit0, metric = mgfit1, config = mgfit2,
          argsLRT = list(asymptotic = TRUE,
                         method = "satorra.bentler.2010")

## End(Not run)
```

dat2way  Simulated Dataset to Demonstrate Two-way Latent Interaction

Description

A simulated data set with 2 independent factors and 1 dependent factor where each factor has three indicators

Usage

dat2way

Format

A `data.frame` with 500 observations of 9 variables.

- `x1` The first indicator of the first independent factor
- `x2` The second indicator of the first independent factor
- `x3` The third indicator of the first independent factor
- `x4` The first indicator of the second independent factor
- `x5` The second indicator of the second independent factor
- `x6` The third indicator of the second independent factor
- `x7` The first indicator of the dependent factor
- `x8` The second indicator of the dependent factor
- `x9` The third indicator of the dependent factor

Source

Data were generated by the `mvrnorm` function in the MASS package.

Examples

```r
head(dat2way)
```
dat3way

Simulated Dataset to Demonstrate Three-way Latent Interaction

Description

A simulated data set with 3 independent factors and 1 dependent factor where each factor has three indicators

Usage
dat3way

Format

A data.frame with 500 observations of 12 variables.

x1 The first indicator of the first independent factor
x2 The second indicator of the first independent factor
x3 The third indicator of the first independent factor
x4 The first indicator of the second independent factor
x5 The second indicator of the second independent factor
x6 The third indicator of the second independent factor
x7 The first indicator of the third independent factor
x8 The second indicator of the third independent factor
x9 The third indicator of the third independent factor
x10 The first indicator of the dependent factor
x11 The second indicator of the dependent factor
x12 The third indicator of the dependent factor

Source

Data were generated by the mvrnorm function in the MASS package.

Examples

head(dat3way)
datCat

Simulated Data set to Demonstrate Categorical Measurement Invariance

Description
A simulated data set with 2 factors with 4 indicators each separated into two groups

Usage
datCat

Format
A data.frame with 200 observations of 9 variables.

- g Sex of respondents
- u1 Indicator 1
- u2 Indicator 2
- u3 Indicator 3
- u4 Indicator 4
- u5 Indicator 5
- u6 Indicator 6
- u7 Indicator 7
- u8 Indicator 8

Source
Data were generated using the lavaan package.

Examples
head(datCat)
Description
This class contains the results of rotated exploratory factor analysis.

Usage

```r
## S4 method for signature 'EFA'
show(object)

## S4 method for signature 'EFA'
summary(object, suppress = 0.1, sort = TRUE)
```

Arguments

- `object`: object of class `EFA`
- `suppress`: any standardized loadings less than the specified value will not be printed to the screen
- `sort`: logical. If TRUE (default), factor loadings will be sorted by their size in the console output

Slots

- `loading`: Rotated standardized factor loading matrix
- `rotate`: Rotation matrix
- `gradRotate`: gradient of the objective function at the rotated loadings
- `convergence`: Convergence status
- `phi`: Factor correlation matrix. Will be an identity matrix if orthogonal rotation is used.
- `se`: Standard errors of the rotated standardized factor loading matrix
- `method`: Method of rotation
- `call`: The command used to generate this object

Objects from the Class

Objects can be created via the `orthRotate` or `oblqRotate` function.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

See Also

`efaUnrotate`; `orthRotate`; `oblqRotate`
Example

unrotated <- efaUnrotate(HolzingerSwineford1939, nf = 3,
    varlist = paste0("x", 1:9), estimator = "mlr")
summary(unrotated, std = TRUE)
lavInspect(unrotated, "std")

# Rotated by Quartimin
rotated <- oblqRotate(unrotated, method = "quartimin")
summary(rotated)

efa.ekc  
| Empirical Kaiser criterion |

Description

Identify the number of factors to extract based on the Empirical Kaiser Criterion (EKC). The analysis can be run on a data.frame or data matrix (data), or on a correlation or covariance matrix (sample.cov) and the sample size (sample.nobs). A data.frame is returned with two columns: the eigenvalues from your data or covariance matrix and the reference eigenvalues. The number of factors suggested by the Empirical Kaiser Criterion (i.e. the sample eigenvalues greater than the reference eigenvalues), and the number of factors suggested by the original Kaiser Criterion (i.e. sample eigenvalues > 1) is printed above the output.

Usage

efa.ekc(data = NULL, sample.cov = NULL, sample.nobs = NULL,
    missing = "default", ordered = NULL, plot = TRUE)

Arguments

data  A data.frame or data matrix containing columns of variables to be factor-analyzed.
sample.cov  A covariance or correlation matrix can be used, instead of data, to estimate the eigenvalues.
sample.nobs  Number of observations (i.e. sample size) if is.null(data) and sample.cov is used.
missing  If "listwise", cases with missing values are removed listwise from the data frame. If "direct" or "ml" or "fiml" and the estimator is maximum likelihood, an EM algorithm is used to estimate the unrestricted covariance matrix (and mean vector). If "pairwise", pairwise deletion is used. If "default", the value is set depending on the estimator and the mimic option (see details in lavCor).
ordered  Character vector. Only used if object is a data.frame. Treat these variables as ordered (ordinal) variables. Importantly, all other variables will be treated as numeric (unless is.ordered == TRUE in data). (see also lavCor)
plot  logical. Whether to print a scree plot comparing the sample eigenvalues with the reference eigenvalues.
Value

A data.frame showing the sample and reference eigenvalues.

The number of factors suggested by the Empirical Kaiser Criterion (i.e. the sample eigenvalues greater than the reference eigenvalues) is returned as an attribute (see Examples).

The number of factors suggested by the original Kaiser Criterion (i.e. sample eigenvalues > 1) is also printed as a header to the data.frame.

Author(s)

Ylenio Longo (University of Nottingham; <yleniolongo@gmail.com>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
## Simulate data with 3 factors
model <- 'f1 = .3*x1 + .5*x2 + .4*x3
f2 = .3*x4 + .5*x5 + .4*x6
f3 = .3*x7 + .5*x8 + .4*x9',
dat <- simulateData(model, seed = 123)
## save summary statistics
myCovMat <- cov(dat)
myCorMat <- cor(dat)
N <- nrow(dat)

## Run the EKC function
(out <- efa.ekc(dat))

## To extract the recommended number of factors using the EKC:
attr(out, "nfactors")

## If you do not have raw data, you can use summary statistics
(x1 <- efa.ekc(sample.cov = myCovMat, sample.nobs = N, plot = FALSE))
(x2 <- efa.ekc(sample.cov = myCorMat, sample.nobs = N, plot = FALSE))
```
efaUnrotate

Analyze Unrotated Exploratory Factor Analysis Model

Description

This function will analyze unrotated exploratory factor analysis model. The unrotated solution can be rotated by the orthRotate and oblqRotate functions.

Usage

efaUnrotate(data, nf, varList = NULL, start = TRUE, aux = NULL, ...)

Arguments

data A target data.frame
nf The desired number of factors
varList Target observed variables. If not specified, all variables in data will be used.
start Use starting values in the analysis from the factanal function. If FALSE, the starting values from the lavaan package will be used. TRUE is ignored with a warning if the aux argument is used.
aux The list of auxiliary variables. These variables will be included in the model by the saturated-correlates approach to account for missing information.
... Other arguments in the cfa function in the lavaan package, such as ordered, se, or estimator

Details

This function will generate a lavaan script for unrotated exploratory factor analysis model such that (1) all factor loadings are estimated, (2) factor variances are fixed to 1, (3) factor covariances are fixed to 0, and (4) the dot products of any pairs of columns in the factor loading matrix are fixed to zero (Johnson & Wichern, 2002). The reason for creating this function in addition to the factanal function is that users can enjoy some advanced features from the lavaan package such as scaled $\chi^2$, diagonal weighted least squares for ordinal indicators, or full-information maximum likelihood (FIML).

Value

A lavaan output of unrotated exploratory factor analysis solution.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
Examples

```r
unrotated <- efaUnrotate(HolzingerSwineford1939, nf = 3,
varList=paste0("x", 1:9), estimator = "mlr")
summary(unrotated, std = TRUE)
inspect(unrotated, "std")

dat <- data.frame(HolzingerSwineford1939,
  z = rnorm(nrow(HolzingerSwineford1939), 0, 1))
unrotated2 <- efaUnrotate(dat, nf = 2, varList = paste0("x", 1:9), aux = "z")
```

---

**exLong**  
*Simulated Data set to Demonstrate Longitudinal Measurement Invariance*

**Description**

A simulated data set with 1 factors with 3 indicators in three timepoints

**Usage**

`exLong`

**Format**

A `data.frame` with 200 observations of 10 variables.

- **sex**  Sex of respondents  
- **y1t1**  Indicator 1 in Time 1  
- **y2t1**  Indicator 2 in Time 1  
- **y3t1**  Indicator 3 in Time 1  
- **y1t2**  Indicator 1 in Time 2  
- **y2t2**  Indicator 2 in Time 2  
- **y3t2**  Indicator 3 in Time 2  
- **y1t3**  Indicator 1 in Time 3  
- **y2t3**  Indicator 2 in Time 3  
- **y3t3**  Indicator 3 in Time 3  

**Source**

Data were generated using the `simsem` package.

**Examples**

```r
head(exLong)
```
findRMSEApower

Find the statistical power based on population RMSEA

Description

Find the proportion of the samples from the sampling distribution of RMSEA in the alternative hypothesis rejected by the cutoff derived from the sampling distribution of RMSEA in the null hypothesis. This function can be applied for both test of close fit and test of not-close fit (MacCallum, Browne, & Sugawara, 1996)

Usage

```r
findRMSEApower(rmsea0, rmseaA, df, n, alpha = 0.05, group = 1)
```

Arguments

- `rmsea0`: Null RMSEA
- `rmseaA`: Alternative RMSEA
- `df`: Model degrees of freedom
- `n`: Sample size of a dataset
- `alpha`: Alpha level used in power calculations
- `group`: The number of group that is used to calculate RMSEA.

Details

This function find the proportion of sampling distribution derived from the alternative RMSEA that is in the critical region derived from the sampling distribution of the null RMSEA. If `rmseaA` is greater than `rmsea0`, the test of close fit is used and the critical region is in the right hand side of the null sampling distribution. On the other hand, if `rmseaA` is less than `rmsea0`, the test of not-close fit is used and the critical region is in the left hand side of the null sampling distribution (MacCallum, Browne, & Sugawara, 1996).

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References

findRMSEApowernested

See Also
- `plotRMSEApower` to plot the statistical power based on population RMSEA given the sample size
- `plotRMSEAdist` to visualize the RMSEA distributions
- `findRMSEAsamplesize` to find the minimum sample size for a given statistical power based on population RMSEA

Examples

```r
t# Find power given a sample size in nested model comparison

findRMSEApowernested(rmsea0A = NULL, rmsea0B = NULL, rmsea1A, rmsea1B = NULL, dfA, dfB, n, alpha = 0.05, group = 1)
```
findRMSEAsamplesize

References


See Also

- `plotRMSEApowernested` to plot the statistical power for nested model comparison based on population RMSEA given the sample size
- `findRMSEAsamplesizenested` to find the minimum sample size for a given statistical power in nested model comparison based on population RMSEA

Examples

```r
findRMSEApowernested(rmsea0 = 0.06, rmsea0B = 0.05, rmsea1A = 0.08,
rmsea1B = 0.05, dfA = 22, dfB = 20, n = 200,
alpha = 0.05, group = 1)
```

```r
findRMSEAsamplesize Find the minimum sample size for a given statistical power based on population RMSEA
```

Description

Find the minimum sample size for a specified statistical power based on population RMSEA. This function can be applied for both test of close fit and test of not-close fit (MacCallum, Browne, & Suguwara, 1996)

Usage

```r
findRMSEAsamplesize(rmsea0, rmseaA, df, power = 0.8, alpha = 0.05,
group = 1)
```

Arguments

- `rmsea0` Null RMSEA
- `rmseaA` Alternative RMSEA
- `df` Model degrees of freedom
- `power` Desired statistical power to reject misspecified model (test of close fit) or retain good model (test of not-close fit)
- `alpha` Alpha level used in power calculations
- `group` The number of group that is used to calculate RMSEA.
Details

This function finds the minimum sample size for a specified power based on an iterative routine. The sample size keeps increasing until the calculated power from `findRMSEApower` function is just over the specified power. If group is greater than 1, the resulting sample size is the sample size per group.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also

- `plotRMSEApower` to plot the statistical power based on population RMSEA given the sample size
- `plotRMSEAdist` to visualize the RMSEA distributions
- `findRMSEApower` to find the statistical power based on population RMSEA given a sample size

Examples

```r
findRMSEAsamplesize(rmsea0 = .05, rmseaA = .08, df = 20, power = 0.80)
```

```
findRMSEAsamplesizenested

Find sample size given a power in nested model comparison
```

Description

Find the sample size that the power in rejecting the samples from the alternative pair of RMSEA is just over the specified power.

Usage

```r
findRMSEAsamplesizenested(rmsea0A = NULL, rmsea0B = NULL, rmsea1A, rmsea1B = NULL, dfA, dfB, power = 0.8, alpha = 0.05, group = 1)
```
Arguments

- `rmsea0A`: The $H_0$ baseline RMSEA
- `rmsea0B`: The $H_0$ alternative RMSEA (trivial misfit)
- `rmsea1A`: The $H_1$ baseline RMSEA
- `rmsea1B`: The $H_1$ alternative RMSEA (target misfit to be rejected)
- `dfA`: degree of freedom of the more-restricted model.
- `dfB`: degree of freedom of the less-restricted model.
- `power`: The desired statistical power.
- `alpha`: The alpha level.
- `group`: The number of group in calculating RMSEA.

Author(s)

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Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also

- `plotRMSEApowernested` to plot the statistical power for nested model comparison based on population RMSEA given the sample size
- `findRMSEApowernested` to find the power for a given sample size in nested model comparison based on population RMSEA

Examples

```r
findRMSEAsamplesizenested(rmsea0A = 0, rmsea0B = 0, rmsea1A = 0.06, rmsea1B = 0.05, dfA = 22, dfB = 20, power = 0.80, alpha = .05, group = 1)
```
FitDiff-class  

Class For Representing A Template of Model Fit Comparisons

Description

This class contains model fit measures and model fit comparisons among multiple models.

Usage

```r
## S4 method for signature 'FitDiff'
show(object)

## S4 method for signature 'FitDiff'
summary(object, fit.measures = "default", nd = 3)
```

Arguments

- `object` object of class `FitDiff`
- `fit.measures` character vector naming fit indices the user can request from `fitMeasures`. If "default", the fit measures will be `c("chisq", "df", "pvalue", "cfi", "tli", "rmsea", "srmr")`. If "all", all available fit measures will be returned.
- `nd` number of digits printed

Slots

- `name` character. The name of each model
- `model.class` character. One class to which each model belongs
- `nested` data.frame. Model fit comparisons between adjacently nested models that are ordered by their degrees of freedom (`df`)
- `fit` data.frame. Fit measures of all models specified in the `name` slot, ordered by their `df`

Objects from the Class

Objects can be created via the `compareFit` function.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

See Also

`compareFit`; `clipboard`
fmi

Examples

```r
HS.model <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9'

out <- measurementInvariance(model = HS.model, data = HolzingerSwinford1939,
                                group = "school", quiet = TRUE)
modelDiff <- compareFit(out)
summary(modelDiff)
summary(modelDiff, fit.measures = "all")
summary(modelDiff, fit.measures = c("aic", "bic"))

# Not run:
# Save results to a file
saveFile(modelDiff, file = "modelDiff.txt")

# Copy to a clipboard
clipboard(modelDiff)

# End(Not run)
```

fmi  

Fraction of Missing Information.

Description

This function estimates the Fraction of Missing Information (FMI) for summary statistics of each variable, using either an incomplete data set or a list of imputed data sets.

Usage

```r
fmi(data, method = "saturated", group = NULL, ords = NULL,
     varnames = NULL, exclude = NULL, fewImps = FALSE)
```

Arguments

data  

Either a single data.frame with incomplete observations, or a list of imputed data sets.

method  

character. If "saturated" or "sat" (default), the model used to estimate FMI is a freely estimated covariance matrix and mean vector for numeric variables, and/or polychoric correlations and thresholds for ordered categorical variables, for each group (if applicable). If "null", only means and variances are estimated for numeric variables, and/or thresholds for ordered categorical variables (i.e., covariances and/or polychoric correlations are constrained to zero). See Details for more information.
group character. The optional name of a grouping variable, to request FMI in each group.

ords character. Optional vector of names of ordered-categorical variables, which are not already stored as class ordered in data.

varnames character. Optional vector of variable names, to calculate FMI for a subset of variables in data. By default, all numeric and ordered variables will be included, unless data is a single incomplete data frame, in which case only numeric variables can be used with FIML estimation. Other variable types will be removed.

exclude character. Optional vector of variable names to exclude from the analysis.

fewImps logical. If TRUE, use the estimate of FMI that applies a correction to the estimated between-imputation variance. Recommended when there are few imputations; makes little difference when there are many imputations. Ignored when data is not a list of imputed data sets.

Details

The function estimates a saturated model with lavaan for a single incomplete data set using FIML, or with lavaan.mi for a list of imputed data sets. If method = "saturated", FMI will be estimated for all summary statistics, which could take a lot of time with big data sets. If method = "null", FMI will only be estimated for univariate statistics (e.g., means, variances, thresholds). The saturated model gives more reliable estimates, so it could also help to request a subset of variables from a large data set.

Value

fmi returns a list with at least 2 of the following:

- Covariances A list of symmetric matrices: (1) the estimated/pooled covariance matrix, or a list of group-specific matrices (if applicable) and (2) a matrix of FMI, or a list of group-specific matrices (if applicable). Only available if method = "saturated".
- Variances The estimated/pooled variance for each numeric variable. Only available if method = "null" (otherwise, it is on the diagonal of Covariances).
- Means The estimated/pooled mean for each numeric variable.
- Thresholds The estimated/pooled threshold(s) for each ordered-categorical variable.
- message A message indicating caution when the null model is used.

Author(s)

Mauricio Garnier Villarreal (University of Kansas; <mauricio.garniervillarreal@marquette.edu>)
Terrence Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


**Examples**

```r
HSMiss <- HolzingerSwineford1939[, c(paste("x", 1:9, sep = ""),
                       "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)
## calculate FMI (using FIML, provide partially observed data set)
(out1 <- fmi(HSMiss, exclude = "school"))
(out2 <- fmi(HSMiss, exclude = "school", method = "null"))
(out3 <- fmi(HSMiss, varnames = c("x5","x6","x7","x8","x9")))
(out4 <- fmi(HSMiss, group = "school"))
## Not run:
## ordered-categorical data
data(datCat)
lapply(datCat, class)
## impose missing values
set.seed(123)
for (i in 1:8) datCat[sample(1:nrow(datCat), size = .1*nrow(datCat)), i] <- NA
## impute data m = 3 times
library(Amelia)
set.seed(456)
impout <- amelia(datCat, m = 3, noms = "g", ords = paste0("u", 1:8), p2s = FALSE)
imps <- impout$imputations
## calculate FMI, using list of imputed data sets
fmi(imps, group = "g")
## End(Not run)
```

**Description**

This function assesses discriminant validity through the heterotrait-monotrait ratio (HTMT) of the correlations (Henseler, Ringle, & Sarstedt, 2015). Specifically, it assesses the average correlation among indicators across constructs (i.e. heterotrait-heteromethod correlations), relative to the average correlation among indicators within the same construct (i.e. monotrait-heteromethod correlations). The resulting HTMT values are interpreted as estimates of inter-construct correlations. Absolute values of the correlations are recommended to calculate the HTMT matrix. Correlations are estimated using the `lavCor` function in the lavaan package.
Usage

htmt(model, data = NULL, sample.cov = NULL, missing = "listwise",
      ordered = NULL, absolute = TRUE)

Arguments

model lavaan model.syntax of a confirmatory factor analysis model where at least two factors are required for indicators measuring the same construct.
data A data.frame or data matrix
sample.cov A covariance or correlation matrix can be used, instead of data, to estimate the HTMT values.
missing If "listwise", cases with missing values are removed listwise from the data frame. If "direct" or "ml" or "fiml" and the estimator is maximum likelihood, an EM algorithm is used to estimate the unrestricted covariance matrix (and mean vector). If "pairwise", pairwise deletion is used. If "default", the value is set depending on the estimator and the mimic option (see details in lavCor).
ordered Character vector. Only used if object is a data.frame. Treat these variables as ordered (ordinal) variables. Importantly, all other variables will be treated as numeric (unless is.ordered == TRUE in data). (see also lavCor)
absolute logical. Whether HTMT values should be estimated based on absolute correlations (recommended and default is TRUE)

Value

A matrix showing HTMT values (i.e., discriminant validity) between each pair of factors

Author(s)

Ylenio Longo (University of Nottingham; <yleniolongo@gmail.com>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
HS.model <- 'visual =~ x1 + x2 + x3
textual =~ x4 + x5 + x6
speed =~ x7 + x8 + x9'
dat <- HolzingerSwineford1939[, paste0("x", 1:9)]
htmt(HS.model, dat)
```
**imposeStart**  
Specify starting values from a lavaan output

**Description**
This function will save the parameter estimates of a lavaan output and impose those parameter estimates as starting values for another analysis model. The free parameters with the same names or the same labels across two models will be imposed the new starting values. This function may help to increase the chance of convergence in a complex model (e.g., multitrait-multimethod model or complex longitudinal invariance model).

**Usage**
imposeStart(out, expr, silent = TRUE)

**Arguments**
- **out**: The lavaan output that users wish to use the parameter estimates as staring values for an analysis model
- **expr**: The original code that users use to run a lavaan model
- **silent**: Logical to print the parameter table with new starting values

**Value**
A fitted lavaan model

**Author(s)**
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

**Examples**

```r
## The following example show that the longitudinal weak invariance model  
## using effect coding was not convergent with three time points but convergent  
## with two time points. Thus, the parameter estimates from the model with  
## two time points are used as starting values of the three time points.  
## The model with new starting values is convergent properly.

weak2time <- '
# Loadings
flt1 <- LOAD1*y1t1 + LOAD2*y2t1 + LOAD3*y3t1
  flt2 <- LOAD1*y1t2 + LOAD2*y2t2 + LOAD3*y3t2

# Factor Variances
flt1 ~~ flt1
flt2 ~~ flt2
```
# Factor Covariances
f1t1 -- f1t2

# Error Variances
y1t1 -- y1t1
y2t1 -- y2t1
y3t1 -- y3t1
y1t2 -- y1t2
y2t2 -- y2t2
y3t2 -- y3t2

# Error Covariances
y1t1 -- y1t2
y2t1 -- y2t2
y3t1 -- y3t2

# Factor Means
f1t1 ~ NA*1
f1t2 ~ NA*1

# Measurement Intercepts
y1t1 ~ INT1*1
y2t1 ~ INT2*1
y3t1 ~ INT3*1
y1t2 ~ INT4*1
y2t2 ~ INT5*1
y3t2 ~ INT6*1

# Constraints for Effect-coding Identification
LOAD1 == 3 - LOAD2 - LOAD3
INT1 == 0 - INT2 - INT3
INT4 == 0 - INT5 - INT6

modelWeakTime <- lavaan(weak2time, data = exLong)
weak3time <- '

# Loadings
f1t1 <- LOAD1*y1t1 + LOAD2*y2t1 + LOAD3*y3t1
f1t2 <- LOAD1*y1t2 + LOAD2*y2t2 + LOAD3*y3t2
f1t3 <- LOAD1*y1t3 + LOAD2*y2t3 + LOAD3*y3t3

# Factor Variances
f1t1 -- f1t1
f1t2 -- f1t2
f1t3 -- f1t3

# Factor Covariances
f1t1 -- f1t2 + f1t3
f1t2 -- f1t3

# Error Variances
y1t1 -- y1t1
y2t1 -- y2t1
```r
y3t1 ~~ y3t1
y1t2 ~~ y1t2
y2t2 ~~ y2t2
y3t2 ~~ y3t2
y1t3 ~~ y1t3
y2t3 ~~ y2t3
y3t3 ~~ y3t3

# Error Covariances
y1t1 ~~ y1t2
y2t1 ~~ y2t2
y3t1 ~~ y3t2
y1t1 ~~ y1t3
y2t1 ~~ y2t3
y3t1 ~~ y3t3
y1t2 ~~ y1t3
y2t2 ~~ y2t3
y3t2 ~~ y3t3

# Factor Means
f1t1 ~ NAx1
f1t2 ~ NAx1
f1t3 ~ NAx1

# Measurement Intercepts
y1t1 ~ INT1x1
y2t1 ~ INT2x1
y3t1 ~ INT3x1
y1t2 ~ INT4x1
y2t2 ~ INT5x1
y3t2 ~ INT6x1
y1t3 ~ INT7x1
y2t3 ~ INT8x1
y3t3 ~ INT9x1

# Constraints for Effect-coding Identification
LOAD1 == 3 - LOAD2 - LOAD3
INT1 == 0 - INT2 - INT3
INT4 == 0 - INT5 - INT6
INT7 == 0 - INT8 - INT9

### The following command does not provide convergent result
# model3time <- lavaan(weak3time, data = exLong)

### Use starting values from the model with two time points
model3time <- imposeStart(model2time, lavaan(weak3time, data = exLong))
summary(model3time)
```
indProd

Make products of indicators using no centering, mean centering, double-mean centering, or residual centering

Description

The indProd function will make products of indicators using no centering, mean centering, double-mean centering, or residual centering. The orthogonalize function is the shortcut of the indProd function to make the residual-centered indicators products.

Usage

```r
indProd(data, var1, var2, var3 = NULL, match = TRUE, meanC = TRUE, residualC = FALSE, doubleMC = TRUE, namesProd = NULL)

orthogonalize(data, var1, var2, var3 = NULL, match = TRUE, namesProd = NULL)
```

Arguments

data The desired data to be transformed.
var1 Names or indices of the variables loaded on the first factor
var2 Names or indices of the variables loaded on the second factor
var3 Names or indices of the variables loaded on the third factor (for three-way interaction)
match Specify TRUE to use match-paired approach (Marsh, Wen, & Hau, 2004). If FALSE, the resulting products are all possible products.
meanC Specify TRUE for mean centering the main effect indicator before making the products
residualC Specify TRUE for residual centering the products by the main effect indicators (Little, Bovaird, & Widaman, 2006).
doubleMC Specify TRUE for centering the resulting products (Lin et. al., 2010)
namesProd The names of resulting products

Value

The original data attached with the products.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>) Alexander Schoemann (East Carolina University; <schoemanna@ecu.edu>)
References


See Also

- `probe2WayMC` For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering.
- `probe3WayMC` For probing the three-way latent interaction when the results are obtained from mean-centering, or double-mean centering.
- `probe2WayRC` For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- `probe3WayRC` For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- `plotProbe` Plot the simple intercepts and slopes of the latent interaction.

Examples

```r
## Mean centering / two-way interaction / match-paired
dat <- indProd(attitude[, -1], var1 = 1:3, var2 = 4:6)

## Residual centering / two-way interaction / match-paired
dat2 <- indProd(attitude[, -1], var1 = 1:3, var2 = 4:6, match = FALSE,
                   meanC = FALSE, residualC = TRUE, doubleMC = FALSE)

## Double-mean centering / two-way interaction / match-paired
dat3 <- indProd(attitude[, -1], var1 = 1:3, var2 = 4:6, match = FALSE,
                   meanC = TRUE, residualC = FALSE, doubleMC = TRUE)

## Mean centering / three-way interaction / match-paired
dat4 <- indProd(attitude[, -1], var1 = 1:2, var2 = 3:4, var3 = 5:6)

## Residual centering / three-way interaction / match-paired
dat5 <- orthogonalize(attitude[, -1], var1 = 1:2, var2 = 3:4, var3 = 5:6,
                       match = FALSE)

## Double-mean centering / three-way interaction / match-paired
dat6 <- indProd(attitude[, -1], var1 = 1:2, var2 = 3:4, var3 = 5:6,
                match = FALSE, meanC = TRUE, residualC = TRUE,
                doubleMC = TRUE)
```
kd  

Generate data via the Kaiser-Dickman (1962) algorithm.

Description

Given a covariance matrix and sample size, generate raw data that correspond to the covariance matrix. Data can be generated to match the covariance matrix exactly, or to be a sample from the population covariance matrix.

Usage

kd(covmat, n, type = c("exact", "sample"))

Arguments

covmat a symmetric, positive definite covariance matrix
n the sample size for the data that will be generated

type type of data generation. exact generates data that exactly correspond to covmat. sample treats covmat as a population covariance matrix, generating a sample of size n.

Details

By default, R’s cov() function divides by n-1. The data generated by this algorithm result in a covariance matrix that matches covmat, but you must divide by n instead of n-1.

Value

kd returns a data matrix of dimension n by nrow(covmat).

Author(s)

Ed Merkle (University of Missouri; <merkle@missouri.edu>)

References


Examples

#### First Example

## Get data
dat <- HolzingerSwineford1939[, 7:15]
hs.n <- nrow(dat)
# Covariance matrix divided by n
hs cov <- ((hs.n - 1)/hs.n) * cov(dat)

# Generate new, raw data corresponding to hscov
newdat <- kd(hscov, hs.n)

# Difference between new covariance matrix and hscov is minimal
newcov <- (hs.n - 1)/hs.n * cov(newdat)
summary(as.numeric(hscov - newcov))

# Generate sample data, treating hscov as population matrix
newdat2 <- kd(hscov, hs.n, type = "sample")

### Another example

# Define a covariance matrix
covmat <- matrix(0, 3, 3)
diag(covmat) <- 1.5
covmat[2:3,1] <- c(1.3, 1.7)
covmat[3,2] <- 2.1
covmat <- covmat + t(covmat)

# Generate data of size 300 that have this covariance matrix
rawdat <- kd(covmat, 300)

# Covariances are exact if we compute sample covariance matrix by
# dividing by n (vs by n - 1)
summary(as.numeric((299/300)*cov(rawdat) - covmat))

# Generate data of size 300 where covmat is the population covariance matrix
rawdat2 <- kd(covmat, 300)

---

**kurtosis**

*Finding excessive kurtosis*

**Description**

Finding excessive kurtosis ($g_2$) of an object

**Usage**

```r
kurtosis(object, population = FALSE)
```

**Arguments**

- **object**
  A vector used to find a excessive kurtosis

- **population**
  TRUE to compute the parameter formula. FALSE to compute the sample statistic formula.
Details

The excessive kurtosis computed is \( g_2 \). The parameter excessive kurtosis \( \gamma_2 \) formula is

\[
\gamma_2 = \frac{\mu_4}{\mu_2^2} - 3,
\]

where \( \mu_i \) denotes the \( i \) order central moment.

The excessive kurtosis formula for sample statistic \( g_2 \) is

\[
g_2 = \frac{k_4}{k_2^2},
\]

where \( k_i \) are the \( i \) order \( k \)-statistic.

The standard error of the excessive kurtosis is

\[
\text{Var}(\hat{g}_2) = \frac{24}{N}
\]

where \( N \) is the sample size.

Value

A value of an excessive kurtosis with a test statistic if the population is specified as FALSE.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also

• skew Find the univariate skewness of a variable
• mardiaSkew Find the Mardia’s multivariate skewness of a set of variables
• mardiaKurtosis Find the Mardia’s multivariate kurtosis of a set of variables

Examples

kurtosis(1:5)
Description

This class extends the `lavaanList` class, created by fitting a lavaan model to a list of data sets. In this case, the list of data sets are multiple imputations of missing data.

Usage

```r
## S4 method for signature 'lavaan.mi'
show(object)

## S4 method for signature 'lavaan.mi'
summary(object, se = TRUE, ci = FALSE,
         level = 0.95, standardized = FALSE, rsquare = FALSE, fmi = FALSE,
         header = TRUE, scale.W = TRUE, asymptotic = FALSE,
         add.attributes = TRUE)

## S4 method for signature 'lavaan.mi'
nobs(object, total = TRUE)

## S4 method for signature 'lavaan.mi'
coef(object, type = "free", labels = TRUE)

## S4 method for signature 'lavaan.mi'
vcov(object, type = c("pooled", "between",
               "within", "ariv"), scale.W = TRUE)

## S4 method for signature 'lavaan.mi'
anova(object, ...)

## S4 method for signature 'lavaan.mi'
fitMeasures(object, fit.measures = "all",
             baseline.model = NULL)

## S4 method for signature 'lavaan.mi'
fitmeasures(object, fit.measures = "all",
             baseline.model = NULL)

## S4 method for signature 'lavaan.mi'
fitted(object)

## S4 method for signature 'lavaan.mi'
fitted.values(object)
```
Arguments

object
An object of class lavaan.mi

se, ci, level, standardized, rsquare, header, add.attributes
See parameterestimates.

fmi
logical indicating whether to include the Fraction Missing Information (FMI) for parameter estimates in the summary output (see Value section).

scale.W
logical. If TRUE (default), the vcov method will calculate the pooled covariance matrix by scaling the within-imputation component by the ARIV (see Enders, 2010, p. 235, for definition and formula). Otherwise, the pooled matrix is calculated as the weighted sum of the within-imputation and between-imputation components (see Enders, 2010, ch. 8, for details). This in turn affects how the summary method calculates its pooled standard errors, as well as the Wald test (lavTestWald.mi).

asymptotic
logical. If FALSE (typically a default, but see Value section for details using various methods), pooled tests (of fit or pooled estimates) will be F or t statistics with associated degrees of freedom (df). If TRUE, the (denominator) df are assumed to be sufficiently large for a t statistic to follow a normal distribution, so it is printed as a z statistic; likewise, F times its numerator df is printed, assumed to follow a χ² distribution.

total
logical (default: TRUE) indicating whether the nobs method should return the total sample size or (if FALSE) a vector of group sample sizes.

type
The meaning of this argument varies depending on which method it it used for. Find detailed descriptions in the Value section under coef, vcov, and residuals.

labels
logical indicating whether the coef output should include parameter labels. Default is TRUE.

... Additional arguments passed to lavTestLRT.mi, or subsequently to lavTestLRT.

fit.measures, baseline.model
See fitModel.

Value

coeff
signature(object = "lavaan.mi", type = "free", labels = TRUE):
See lavaan. Returns the pooled point estimates (i.e., averaged across imputed data sets; see Rubin, 1987).

vcov
signature(object = "lavaan.mi", scale.W = TRUE, type = c("pooled","between","within"),
By default, returns the pooled covariance matrix of parameter estimates (type = "pooled"),
the within-imputations covariance matrix (type = "within"), the between-imputations covariance matrix (type = "between"), or the average relative increase in variance (type = "ariv") due to missing data.
fitted.values signature(object = "lavaan.mi") : Returns model-implied moments, evaluated at the pooled point estimates.

fitted signature(object = "lavaan.mi") : alias for fitted.values

residuals signature(object = "lavaan.mi", type = c("raw","cor")): See lavaan. By default (type = "raw"), returns the difference between the model-implied moments from fitted.values and the pooled observed moments (i.e., averaged across imputed data sets). Standardized residuals are also available, using Bollen's (type = "cor" or "cor.bollen") or Bentler's (type = "cor.bentler") formulas.

resid signature(object = "lavaan.mi", type = c("raw","cor")): alias for residuals

nobs signature(object = "lavaan.mi", total = TRUE): either the total (default) sample size or a vector of group sample sizes (total = FALSE).

anova signature(object = "lavaan.mi", ...): Returns a test of model fit for a single model (object) or test(s) of the difference(s) in fit between nested models passed via .... See lavTestLRT.mi and compareFit for details.

fitMeasures signature(object = "lavaan.mi", fit.measures = "all", baseline.model = NULL): See lavaan's fitMeasures for details. Pass additional arguments to lavTestLRT.mi via ....

fitmeasures alias for fitMeasures.

show signature(object = "lavaan.mi") : returns a message about convergence rates and estimation problems (if applicable) across imputed data sets.

summary signature(object = "lavaan.mi", se = TRUE, ci = FALSE, level = .95, standardized = FALSE): See parameterEstimates for details. By default, summary returns pooled point and SE estimates, along with t test statistics and their associated df and p values. If ci = TRUE, confidence intervals are returned with the specified confidence level (default 95% CI). If asymptotic = TRUE, z instead of t tests are returned. standardized solution(s) can also be requested by name ("std.lv" or "std.all") or both are returned with TRUE. R-squared for endogenous variables can be requested, as well as the Fraction Missing Information (FMI) for parameter estimates. By default, the output will appear like lavaan's summary output, but if add.attributes = FALSE, the returned data.frame will resemble the parameterEstimates output. The scale.W argument is passed to vcov (see description above).

Slots

coeffList list of estimated coefficients in matrix format (one per imputation) as output by lavInspect(fit, "est")

GLIST pooled list of coefficients in GLIST format

miList list of modification indices output by modindices

seed integer seed set before running imputations

lavListCall call to lavaanList used to fit the model to the list of imputed data sets in @DataList, stored as a list of arguments

imputeCall call to imputation function (if used), stored as a list of arguments
convergence list of logical vectors indicating whether, for each imputed data set, (1) the model converged on a solution, (2) SEs could be calculated, (3) the (residual) covariance matrix of latent variables ($\Psi$) is non-positive-definite, and (4) the residual covariance matrix of observed variables ($\Theta$) is non-positive-definite.

lavaanList_slots All remaining slots are from lavaanList, but runMI only populates a subset of the list slots, two of them with custom information:

DataList The list of imputed data sets
SampleStatsList List of output from lavInspect(fit, "sampstat") applied to each fitted model
ParTableList See lavaanList
vcovList See lavaanList
testList See lavaanList

Objects from the Class

See the runMI function for details. Wrapper functions include lavaan.mi, cfa.mi, sem.mi, and growth.mi.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
## See ?runMI help page
```
Likelihood ratio test (LRT) for lavaan models fitted to multiple imputed data sets. Statistics for comparing nested models can be calculated by pooling the likelihood ratios across imputed data sets, as described by Meng & Rubin (1992), or by pooling the LRT statistics from each imputation, as described by Li, Meng, Raghunathan, & Rubin (1991).

Usage

lavTestLRT.mi(object, h1 = NULL, test = c("D3", "D2"), asymptotic = FALSE, pool.robust = FALSE, ...)

Arguments

object, h1 An object of class lavaan.mi. object should be nested within (more constrained than) h1.

test character indicating which pooling method to use. "D3", "mr", or "meng.rubin" (default) requests the method described by Meng & Rubin (1992). "D2", "LMRR", or "Li.et.al" requests the complete-data LRT statistic should be calculated using each imputed data set, which will then be pooled across imputations, as described in Li, Meng, Raghunathan, & Rubin (1991). Find additional details in Enders (2010, chapter 8).

asymptotic logical. If FALSE (default), the pooled test will be returned as an F-distributed statistic with numerator (df1) and denominator (df2) degrees of freedom. If TRUE, the pooled F statistic will be multiplied by its df1 on the assumption that its df2 is sufficiently large enough that the statistic will be asymptotically $\chi^2$ distributed with df1.

pool.robust logical. Ignored unless test = "D2" and a robust test was requested. If pool.robust = TRUE, the robust test statistic is pooled, whereas pool.robust = FALSE will pool the naive test statistic (or difference statistic) and apply the average scale/shift parameter to it (unavailable for mean- and variance-adjusted difference statistics, so pool.robust will be set TRUE).

Details

The Meng & Rubin (1992) method, also referred to as the "D3" statistic, is only applicable when using a likelihood-based estimator. Otherwise (e.g., DWLS for categorical outcomes), users are notified that test was set to "D2".

test = "Mplus" implies "D3" and asymptotic = TRUE (see Asparouhov & Muthen, 2010).

Note that unlike lavTestLRT, lavTestLRT can only be used to compare a single pair of models, not a longer list of models. To compare several nested models fitted to multiple imputations, see examples on the compareFit help page.
Value

A vector containing the LRT statistic (either an $F$ or $\chi^2$ statistic, depending on the asymptotic argument), the degrees of freedom (numerator and denominator, if asymptotic = FALSE), and a $p$ value. Robust statistics will also include the average (across imputations) scaling factor and (if relevant) shift parameter(s), unless pool.robust = TRUE.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


See Also

lavTestLRT, compareFit

Examples

```r
## Not run:
## impose missing data for example
HSMiss <- HolzingerSwineford1939[, c(paste("x", 1:9, sep = ""),
    "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

## impute missing data
library(Amelia)
set.seed(12345)
HS.amelia <- amelia(HSMiss, m = 20, naoms = "school", p2s = FALSE)
imps <- HS.amelia$imputations

## specify CFA model from lavaan's ?cfa help page
HS.model <- ' visual =~ x1 + b1*x2 + x3
textual =~ x4 + b2*x5 + x6
    speed =~ x7 + b3*x8 + x9
',

fit1 <- cfa.mi(HS.model, data = imps, estimator = "mlm")
fit0 <- cfa.mi(HS.model, data = imps, estimator = "mlm", orthogonal = TRUE)
```
## lavTestScore.mi

Score Test for Multiple Imputations

### Description

Score test (or "Lagrange multiplier" test) for lavaan models fitted to multiple imputed data sets. Statistics for releasing one or more fixed or constrained parameters in model can be calculated by pooling the gradient and information matrices pooled across imputed data sets using Rubin's (1987) rules, or by pooling the score test statistics across imputed data sets (Li, Meng, Raghunathan, & Rubin, 1991).

### Usage

```r
lavTestScore.mi(object, add = NULL, release = NULL, test = c("D2", "Rubin"), scale.W = FALSE, asymptotic = !is.null(add), univariate = TRUE, cumulative = FALSE, epc = FALSE, verbose = FALSE, warn = TRUE, information = "expected")
```

### Arguments

- **object**: An object of class `lavaan.mi`.
- **add**: Either a character string (typically between single quotes) or a parameter table containing additional (currently fixed-to-zero) parameters for which the score test must be computed.
- **release**: Vector of integers. The indices of the equality constraints that should be released. The indices correspond to the order of the equality constraints as they appear in the parameter table.
- **test**: Character indicating which pooling method to use. "Rubin" indicates Rubin's (1987) rules will be applied to the gradient and information, and those pooled values will be used to calculate modification indices in the usual manner. "D2" (default), "LMRR", or "Li.et.al" indicate that modification indices calculated from each imputed data set will be pooled across imputations, as described in Li, Meng, Raghunathan, & Rubin (1991) and Enders (2010).
scaleNw logical. If FALSE (default), the pooled information matrix is calculated as the weighted sum of the within-imputation and between-imputation components. Otherwise, the pooled information is calculated by scaling the within-imputation component by the average relative increase in variance (ARIV; see Enders, 2010, p. 235). Not recommended, and ignored (irrelevant) if test = "D2".

asymptotic logical. If FALSE (default when using add to test adding fixed parameters to the model), the pooled test will be returned as an $F$-distributed variable with numerator (df1) and denominator (df2) degrees of freedom. If TRUE, the pooled $F$ statistic will be multiplied by its df1 on the assumption that its df2 is sufficiently large enough that the statistic will be asymptotically $\chi^2$ distributed with df1. When using the release argument, asymptotic will be set to TRUE because (A)RIV can only be calculated for added parameters.

univariate logical. If TRUE, compute the univariate score statistics, one for each constraint.

cumulative logical. If TRUE, order the univariate score statistics from large to small, and compute a series of multivariate score statistics, each time including an additional constraint in the test.

epc logical. If TRUE, and we are releasing existing constraints, compute the expected parameter changes for the existing (free) parameters (and any specified with add), if all constraints were released. For EPCs associated with a particular (1-df) constraint, only specify one parameter in add or one constraint in release.

verbose logical. Not used for now.

warn logical. If TRUE, print warnings if they occur.

information character indicating the type of information matrix to use (check lavInspect for available options). "expected" information is the default, which provides better control of Type I errors.

Value

A list containing at least one data.frame:

- $test$: The total score test, with columns for the score test statistic ($xR$), the degrees of freedom (df), and a $p$ value under the $\chi^2$ distribution ($pNvalue$).
- $uni$: Optional (if univariate=TRUE). Each 1-df score test, equivalent to modification indices.
- $cumulative$: Optional (if cumulative=TRUE). Cumulative score tests.
- $epc$: Optional (if epc=TRUE). Parameter estimates, expected parameter changes, and expected parameter values if all the tested constraints were freed.

See lavTestScore for details.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

Adapted from lavaan source code, written by Yves Rosseel (Ghent University; <Yves.Rosseel@UGent.be>)

test = "Rubin" method proposed by Maxwell Mansolf (University of California, Los Angeles; <mamansolf@gmail.com>)
References


See Also

lavTestScore

Examples

```r
## Not run:
## impose missing data for example
HSMiss <- HolzingerSwineford1939[, c(paste("x", 1:9, sep = ""),
                                  "ageyr", "ageemo", "school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$ageemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

## impute missing data
library(Amelia)
set.seed(12345)
HS.amelia <- amelia(HSMiss, m = 20, nom = "school", p2s = FALSE)
imps <- HS.amelia$imputations

## specify CFA model from lavaan's ?cfa help page
HS.model <- 
  speed ~ c(L1, L1)*x7 + c(L1, L1)*x8 + c(L1, L1)*x9

out <- cfa.mi(HS.model, data = imps, group = "school", std.lv = TRUE)

## Mode 1: Score test for releasing equality constraints

## default test: Li et al.'s (1991) "D2" method
lavTestScore.mi(out, cumulative = TRUE)

## Rubin's rules
lavTestScore.mi(out, test = "Rubin")

## Mode 2: Score test for adding currently fixed-to-zero parameters
lavTestScore.mi(out, add = 'x7 ~ x8 + x9')

## End(Not run)
```
Description

Wald test for testing a linear hypothesis about the parameters of lavaan models fitted to multiple imputed data sets. Statistics for constraining one or more free parameters in a model can be calculated from the pooled point estimates and asymptotic covariance matrix of model parameters using Rubin’s (1987) rules, or by pooling the Wald test statistics across imputed data sets (Li, Meng, Raghunathan, & Rubin, 1991).

Usage

lavTestWald.mi(object, constraints = NULL, test = c("D1", "D2"), asymptotic = FALSE, scale.W = FALSE, verbose = FALSE, warn = TRUE)

Arguments

- **object**: An object of class `lavaan.mi`.
- **constraints**: A character string (typically between single quotes) containing one or more equality constraints. See examples for more details.
- **test**: character indicating which pooling method to use. "D1" or "Rubin" (default) indicates Rubin’s (1987) rules will be applied to the point estimates and the asymptotic covariance matrix of model parameters, and those pooled values will be used to calculate the Wald test in the usual manner. "D2", "LMRR", or "Li.et.al" indicate that the complete-data Wald test statistic should be calculated using each imputed data set, which will then be pooled across imputations, as described in Li, Meng, Raghunathan, & Rubin (1991) and Enders (2010, chapter 8).
- **asymptotic**: logical. If FALSE (default), the pooled test will be returned as an F-distributed statistic with numerator (df1) and denominator (df2) degrees of freedom. If TRUE, the pooled F statistic will be multiplied by its df1 on the assumption that its df2 is sufficiently large enough that the statistic will be asymptotically χ² distributed with df1.
- **scale.W**: logical. If FALSE (default), the pooled asymptotic covariance matrix of model parameters is calculated as the weighted sum of the within-imputation and between-imputation components. Otherwise, the pooled asymptotic covariance matrix of model parameters is calculated by scaling the within-imputation component by the average relative increase in variance (ARIV; see Enders, 2010, p. 235). Not recommended, and ignored (irrelevant) if test = "D2".
- **verbose**: logical. If TRUE, print the restriction matrix and the estimated restricted values.
- **warn**: logical. If TRUE, print warnings if they occur.
Details

The constraints are specified using the "==" operator. Both the left-hand side and the right-hand side of the equality can contain a linear combination of model parameters, or a constant (like zero). The model parameters must be specified by their user-specified labels from the link[lavaan]{model.syntax}. Names of defined parameters (using the ":=" operator) can be included too.

Value

A vector containing the Wald test statistic (either an $F$ or $\chi^2$ statistic, depending on the asymptotic argument), the degrees of freedom (numerator and denominator, if asymptotic = FALSE), and a $p$ value.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
Adapted from lavaan source code, written by Yves Rosseel (Ghent University; <Yves.Rosseel@UGent.be>)

References


See Also

lavTestWald

Examples

```r
## Not run:
## impose missing data for example
HSMiss <- HolzingerSwineford1939[, c(paste("x", 1:9, sep = ""),
                                  "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <- quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

## impute missing data
library(Amelia)
set.seed(12345)
HS.amelia <- amelia(HSMiss, m = 20, names = "school", p2s = FALSE)
imps <- HS.amelia$imputations

## specify CFA model from lavaan's ?cfa help page
HS.model <- '    visual = x1 + b1*x2 + x3
    textual = x4 + b2*x5 + x6'
```
speed <- x7 + b3*x8 + x9

fit <- cfa.mi(HS.model, data = imps)

## Testing whether a single parameter equals zero yields the 'chi-square'
## version of the Wald z statistic from the summary() output, or the
## 'F' version of the t statistic from the summary() output, depending
## whether asymptotic = TRUE or FALSE
lavTestWald.mi(fit, constraints = "b1 == 0")  # default D1 statistic
lavTestWald.mi(fit, constraints = "b1 == 0", test = "D2")  # D2 statistic

## The real advantage is simultaneously testing several equality
## constraints, or testing more complex constraints:
con <- '2*b1 == b3
      b2 - b3 == 0
',
lavTestWald.mi(fit, constraints = con)  # default F statistic
lavTestWald.mi(fit, constraints = con, asymptotic = TRUE)  # chi-squared

## End(Not run)

loadingFromAlpha

Find standardized factor loading from coefficient alpha

Description
Find standardized factor loading from coefficient alpha assuming that all items have equal loadings.

Usage
loadingFromAlpha(alpha, ni)

Arguments
alpha A desired coefficient alpha value.
ni A desired number of items.

Value
result The standardized factor loadings that make desired coefficient alpha with specified number of items.

Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)
Examples

loadingFromAlpha(0.8, 4)

mardiaKurtosis  Finding Mardia's multivariate kurtosis

Description
Finding Mardia's multivariate kurtosis of multiple variables

Usage
mardiaKurtosis(dat, use = "everything")

Arguments
dat           The target matrix or data frame with multiple variables
use           Missing data handling method from the cov function.

Details
The Mardia's multivariate kurtosis formula (Mardia, 1970) is

\[
b_{2,d} = \frac{1}{n} \sum_{i=1}^{n} \left( (X_i - \bar{X})^\prime S^{-1} (X_i - \bar{X}) \right)^2,
\]

where \( d \) is the number of variables, \( X \) is the target dataset with multiple variables, \( n \) is the sample size, \( S \) is the sample covariance matrix of the target dataset, and \( \bar{X} \) is the mean vectors of the target dataset binded in \( n \) rows. When the population multivariate kurtosis is normal, the \( b_{2,d} \) is asymptotically distributed as normal distribution with the mean of \( d(d + 2) \) and variance of \( 8d(d + 2)/n \).

Value
A value of a Mardia's multivariate kurtosis with a test statistic

Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References
See Also

- `skew` Find the univariate skewness of a variable
- `kurtosis` Find the univariate excessive kurtosis of a variable
- `mardiaSkew` Find the Mardia’s multivariate skewness of a set of variables

Examples

```r
library(lavaan)
mardiaKurtosis(HolzingerSwineford1939[, paste0("x", 1:9)])
```

Description

Finding Mardia’s multivariate skewness of multiple variables

Usage

```r
mardiaSkew(dat, use = "everything")
```

Arguments

- `dat` The target matrix or data frame with multiple variables
- `use` Missing data handling method from the `cov` function.

Details

The Mardia's multivariate skewness formula (Mardia, 1970) is

\[
b_{1,d} = \frac{1}{n^2} \sum_{i=1}^{n} \sum_{j=1}^{n} \left( (X_i - \bar{X})' S^{-1} (X_j - \bar{X}) \right)^3,
\]

where \(d\) is the number of variables, \(X\) is the target dataset with multiple variables, \(n\) is the sample size, \(S\) is the sample covariance matrix of the target dataset, and \(\bar{X}\) is the mean vectors of the target dataset banded in \(n\) rows. When the population multivariate skewness is normal, the \(\frac{6}{\delta} b_{1,d}\) is asymptotically distributed as \(\chi^2\) distribution with \(d(d + 1)(d + 2)/6\) degrees of freedom.

Value

A value of a Mardia’s multivariate skewness with a test statistic

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
maximalRelia

References

See Also
- `skew` Find the univariate skewness of a variable
- `kurtosis` Find the univariate excessive kurtosis of a variable
- `mardiaKurtosis` Find the Mardia’s multivariate kurtosis of a set of variables

Examples

```r
library(lavaan)
mardiaSkew(HolzingerSwineford1939[, paste0("x", 1:9)])
```

```
maximalRelia

Calculate maximal reliability

Description
Calculate maximal reliability of a scale

Usage
maximalRelia(object)

Arguments

object The lavaan model object provided after running the cfa, sem, growth, or lavaan functions.

Details
Given that a composite score \( W \) is a weighted sum of item scores:

\[
W = w'x,
\]

where \( x \) is a \( k \times 1 \) vector of the scores of each item, \( w \) is a \( k \times 1 \) weight vector of each item, and \( k \) represents the number of items. Then, maximal reliability is obtained by finding \( w \) such that reliability attains its maximum (Li, 1997; Raykov, 2012). Note that the reliability can be obtained by

\[
\rho = \frac{w'S_xw}{w'S_xw}
\]
where $S_T$ is the covariance matrix explained by true scores and $S_X$ is the observed covariance matrix. Numerical method is used to find $w$ in this function.

For continuous items, $S_T$ can be calculated by

$$S_T = \Lambda \Psi \Lambda',$$

where $\Lambda$ is the factor loading matrix and $\Psi$ is the covariance matrix among factors. $S_X$ is directly obtained by covariance among items.

For categorical items, Green and Yang’s (2009) method is used for calculating $S_T$ and $S_X$. The element $i$ and $j$ of $S_T$ can be calculated by

$$[S_T]_{ij} = \sum_{c_i=1}^{C_i-1} \sum_{c_j=1}^{C_j-1} \Phi_2(\tau_{x_i}, \tau_{x_j}, \Lambda \Psi \Lambda'[ij]) - \sum_{c_i=1}^{C_i-1} \Phi_1(\tau_{x_i}) \sum_{c_j=1}^{C_j-1} \Phi_1(\tau_{x_j}),$$

where $C_i$ and $C_j$ represents the number of thresholds in Items $i$ and $j$, $\tau_{x_i}$ represents the threshold $c_i$ of Item $i$, $\tau_{x_j}$ represents the threshold $c_j$ of Item $j$, $\Phi_1(\tau_{x_i})$ is the cumulative probability of $\tau_{x_i}$ given a univariate standard normal cumulative distribution and $\Phi_2(\tau_{x_i}, \tau_{x_j}, \rho)$ is the joint cumulative probability of $\tau_{x_i}$ and $\tau_{x_j}$ given a bivariate standard normal cumulative distribution with a correlation of $\rho$.

Each element of $S_X$ can be calculated by

$$[S_X]_{ij} = \sum_{c_i=1}^{C_i-1} \sum_{c_j=1}^{C_j-1} \Phi_2(\tau_{x_i}, \tau_{x_j}, \rho_{ij}^*) - \sum_{c_i=1}^{C_i-1} \Phi_1(\tau_{x_i}) \sum_{c_j=1}^{C_j-1} \Phi_1(\tau_{x_j}),$$

where $\rho_{ij}^*$ is a polychoric correlation between Items $i$ and $j$.

Value

Maximal reliability values of each group. The maximal-reliability weights are also provided. Users may extracted the weighted by the attr function (see example below).

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also

reliability for reliability of an unweighted composite score
Examples

total <- 'f <- x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x9'
fit <- cfa(total, data = HolzingerSwineford1939)
maximalRelia(fit)

# Extract the weight
mr <- maximalRelia(fit)
attr(mr, "weight")

Description

Automatically generates lavaan model syntax to specify a confirmatory factor analysis (CFA) model with equality constraints imposed on user-specified measurement (or structural) parameters. Optionally returns the fitted model (if data are provided) representing some chosen level of measurement equivalence/invariance across groups and/or repeated measures.

Usage

measeqNsyntax(configuralNmodel, ..., ID.fac = "std.1v",
ID.cat = "Wu.Estabrook.2016", ID.thr = c(1L, 2L), group = NULL,
group.equal = ",", group.partial = ",", longFacNames = list(),
longIndNames = list(), long.equal = ",", long.partial = ",",
auto = "all", warn = TRUE, debug = FALSE, return.fit = FALSE)

Arguments

configuralNmodel
A model with no measurement-invariance constraints (i.e., representing only configural invariance), unless required for model identification. configuralNmodel can be either:

- lavaan model.syntax or a parameter table (as returned by parTable) specifying the configurual model. Using this option, the user can also provide either raw data or summary statistics via sample.cov and (optionally) sample.mean. In order to include thresholds in the syntax, raw data must be provided. See lavaan.
- a fitted lavaan model (e.g., as returned by cfa) estimating the configurual model

... Additional arguments (e.g., data, ordered, or parameterization) passed to the lavaan function. See also lavOptions.

ID.fac character. The method for identifying common-factor variances and (if meanstructure = TRUE) means. Three methods are available, which go by different names in the literature:
• Standardize the common factor (mean = 0, \(SD = 1\)) by specifying any of:
  - "std.lv",
  - "unit.variance",
  - "UY",
  - "fixed.factor",
  - "fixed-factor"

• Choose a reference indicator by specifying any of:
  - "auto.fix.first",
  - "unit.loading",
  - "UL",
  - "marker",
  - "ref",
  - "ref.indicator",
  - "reference.indicator",
  - "reference-indicator",
  - "marker.variable",
  - "marker-variable"

• Apply effects-code constraints to loadings and intercepts by specifying any of:
  - "FX",
  - "EC",
  - "effects",
  - "effects.coding",
  - "effects-coding",
  - "effects.code",
  - "effects-code"

See Little et al. (2006) for details on all three methods.

**ID.cat** character. The method for identifying (residual) variances and intercepts of latent item-responses underlying any ordered indicators. Four methods are available:

• To follow Wu & Estabrook's (2016) guidelines (default), specify any of:
  - "Wu.Estabrook.2016",
  - "Wu.2016",
  - "Wu.Estabrook",
  - "Wu",
  - "Wu2016".

• To use the default settings of Mplus and lavaan, specify any of:
  - "default",
  - "Mplus",
  - "Muthen". Details provided in Millsap & Tein (2004).

• To use the constraints recommended by Millsap & Tein (2004; see also Liu et al., 2017) specify any of:
  - "millsap",
  - "millsap.2004",
  - "millsap.tein.2004"

• To use the default settings of LISREL, specify "LISREL" or "Joreskog". Details provided in Millsap & Tein (2004).

See Details and References for more information.

**ID.thr** integer. Only relevant when **ID.cat** = "Millsap.Tein.2004". Used to indicate which thresholds should be constrained for identification. The first integer indicates the threshold used for all indicators, the second integer indicates the additional threshold constrained for a reference indicator (ignored if binary).

**group** optional character indicating the name of a grouping variable. See cfa.

**group.equal** optional character vector indicating type(s) of parameter to equate across groups. Ignored if is.null(group). See lavOptions.

**group.partial** optional character vector or a parameter table indicating exceptions to **group.equal** (see lavOptions). Any variables not appearing in the configural.model will be ignored, and any parameter constraints needed for identification (e.g., two thresholds per indicator when **ID.cat** = "Millsap") will be removed.

**longFacNames** optional named list of character vectors, each indicating multiple factors in the model that are actually the same construct measured repeatedly. See Details and Examples.

**longIndNames** optional named list of character vectors, each indicating multiple indicators in the model that are actually the same indicator measured repeatedly. See Details and Examples.

**long.equal** optional character vector indicating type(s) of parameter to equate across repeated measures. Ignored if no factors are indicated as repeatedly measured in longFacNames.

**long.partial** optional character vector or a parameter table indicating exceptions to **long.equal**. Any longitudinal variable names not appearing in names(longFacNames) or names(longIndNames) will be ignored, and any parameter constraints needed for identification will be removed.
auto

Used to automatically included autocorrelated measurement errors among repeatedly measured indicators in \texttt{longIndNames}. Specify a single integer to set the maximum order (e.g., \texttt{auto = 1L} indicates that an indicator’s unique factors should only be correlated between adjacently measured occasions). \texttt{auto = TRUE} or “all” will specify residual covariances among all possible lags per repeatedly measured indicator in \texttt{longIndNames}.

\texttt{warn}, \texttt{debug}

\texttt{logical}. Passed to \texttt{lavaan} and \texttt{lavParseModelString}. See \texttt{lavOptions}.

\texttt{return.fit}

\texttt{logical} indicating whether the generated syntax should be fitted to the provided data (or summary statistics, if provided via \texttt{sample.cov}). If \texttt{configural.model} is a fitted lavaan model, the generated syntax will be fitted using the update method (see \texttt{lavaan}), and \ldots will be passed to \texttt{lavaan}. If neither data nor a fitted lavaan model were provided, this must be \texttt{FALSE}. If \texttt{TRUE}, the generated \texttt{measEq.syntax} object will be included in the \texttt{lavaan} object's \texttt{@external} slot, accessible by \texttt{fit@external$measEq.syntax}.

Details

This function is a pedagogical and analytical tool to generate model syntax representing some level of measurement equivalence/invariance across any combination of multiple groups and/or repeated measures. Support is provided for confirmatory factor analysis (CFA) models with simple or complex structure (i.e., cross-loadings and correlated residuals are allowed). For any complexities that exceed the limits of automation, this function is intended to still be useful by providing a means to generate syntax that users can easily edit to accommodate their unique situations.

Limited support is provided for bifactor models and higher-order constructs. Because bifactor models have cross-loadings by definition, the option \texttt{ID.fac = "effects.code"} is unavailable. \texttt{ID.fac = "UV"} is recommended for bifactor models, but \texttt{ID.fac = "UL"} is available on the condition that each factor has a unique first indicator in \texttt{configural.model}. In order to maintain generality, higher-order factors may include a mix of manifest and latent indicators, but they must therefore require \texttt{ID.fac = "UL"} to avoid complications with differentiating lower-order vs. higher-order (or mixed-level) factors. The keyword “loadings” in group.equal or long.equal constrains factor loadings of all manifest indicators (including loadings on higher-order factors that also have latent indicators), whereas the keyword “regressions” constrains factor loadings of latent indicators. Users can edit the model syntax manually to adjust constraints as necessary, or clever use of the \texttt{group.partial} or \texttt{long.partial} arguments could make it possible for users to still automated their model syntax. The keyword “intercepts” constrains the intercepts of all manifest indicators, and the keyword “means” constrains intercepts and means of all latent common factors, regardless of whether they are latent indicators of higher-order factors. To test equivalence of lower-order and higher-order intercepts/means in separate steps, the user can either manually edit their generated syntax or conscientiously exploit the \texttt{group.partial} or \texttt{long.partial} arguments as necessary.

\texttt{ID.fac:} If the \texttt{configural.model} fixes any (e.g., the first) factor loadings, the generated syntax object will retain those fixed values. This allows the user to retain additional constraints that might be necessary (e.g., if there are only 1 or 2 indicators). Some methods must be used in conjunction with other settings:

- \texttt{ID.cat = "Millsap"} requires \texttt{ID.fac = "UL"} and parameterization = "theta".
- \texttt{ID.cat = "LISREL"} requires parameterization = "theta".
• ID.fac = "effects.code" is unavailable when there are any cross-loadings.

ID.cat: Wu & Estabrook (2016) recommended constraining thresholds to equality first, and doing so should allow releasing any identification constraints no longer needed. For each ordered indicator, constraining one threshold to equality will allow the item’s intercepts to be estimated in all but the first group or repeated measure. Constraining a second threshold (if applicable) will allow the item’s (residual) variance to be estimated in all but the first group or repeated measure. For binary data, there is no independent test of threshold, intercept, or residual-variance equality. Equivalence of thresholds must also be assumed for three-category indicators. These guidelines provide the least restrictive assumptions and tests, and are therefore the default.

The default setting in Mplus is similar to Wu & Estabrook (2016), except that intercepts are always constrained to zero (so they are assumed to be invariant without testing them). Millsap & Tein (2004) recommended parameterization = "theta" and identified an item’s residual variance in all but the first group (or occasion; Liu et al., 2017) by constraining its intercept to zero and one of its thresholds to equality. A second threshold for the reference indicator (so ID.fac = "UL") is used to identify the common-factor means in all but the first group/occasion. The LISREL software fixes the first threshold to zero and (if applicable) the second threshold to 1, and assumes any remaining thresholds to be equal across groups/repeated measures; thus, the intercepts are always identified, and residual variances (parameterization = "theta") are identified except for binary data, when they are all fixed to one.

Repeated Measures: If each repeatedly measured factor is measured by the same indicators (specified in the configural.model) on each occasion, without any cross-loadings, the user can let longIndNames be automatically generated. Generic names for the repeatedly measured indicators are created using the name of the repeatedly measured factors (i.e., names(longFacNames)) and the number of indicators. So the repeatedly measured first indicator ("ind") of a longitudinal construct called "factor" would be generated as "_.factor_ind.1".

The same types of parameter can be specified for long.equal as for group.equal (see lavOptions for a list), except for "residual.covariances" or "lv.covariances". Instead, users can constrain autocovariances using keywords "resid.autocov" or "lv.autocov". Note that group.equal = "lv.covariances" or group.equal = "residual.covariances" will constrain any autocovariances across groups, along with any other covariances the user specified in the configural.model. Note also that autocovariances cannot be specified as exceptions in long.partial, so anything more complex than the auto argument automatically provides should instead be manually specified in the configural.model.

When users set orthogonal=TRUE in the configural.model (e.g., in bifactor models of repeatedly measured constructs), autocovariances of each repeatedly measured factor will still be freely estimated in the generated syntax.

Missing Data: If users wish to utilize the auxiliary function to automatically include auxiliary variables in conjunction with missing = "FIML", they should first generate the hypothesized-model syntax, then submit that syntax as the model to auxiliary(). If users utilized runMI to fit their configural.model to multiply imputed data, that model can also be passed to the configural.model argument, and if return.fit = TRUE, the generated model will be fitted to the multiple imputations.

Value

By default, an object of class measEq.syntax. If return.fit = TRUE, a fitted lavaan model, with the measEq.syntax object stored in the @external slot, accessible by fit@external$measEq.syntax.
measEq.syntax

Author(s)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References

See Also
compareFit

Examples
mod.cat <- 'FU1 =~ u1 + u2 + u3 + u4
FU2 =~ u5 + u6 + u7 + u8'
## the 2 factors are actually the same factor (FU) measured twice
longFacNames <- list(FU = c("FU1","FU2"))

## configural model: no constraints across groups or repeated measures
syntax.config <- measEq.syntax(configural.model = mod.cat, data = datCat,
    ordered = paste0("u", 1:8),
    parameterization = "theta",
    ID.fac = "std.lv", ID.cat = "Wu.Estabrook.2016",
    group = "g", longFacNames = longFacNames)

## print lavaan syntax to the console
cat(as.character(syntax.config))
## print a summary of model features
summary(syntax.config)

## threshold invariance
syntax.thresh <- measEq.syntax(configural.model = mod.cat, data = datCat,
    ordered = paste0("u", 1:8),
    parameterization = "theta",
    ID.fac = "std.lv", ID.cat = "Wu.Estabrook.2016",
    group = "g", group.equal = "thresholds",
    longFacNames = longFacNames,
    long.equal = "thresholds")

## notice that constraining 4 thresholds allows intercepts and residual
## variances to be freely estimated in all but the first group & occasion
cat(as.character(syntax.thresh))
## print a summary of model features
summary(syntax.thresh)

## Fit a model to the data either in a subsequent step:
mod.config <- as.character(syntax.config)
fit.config <- cfa(mod.config, data = datCat, group = "g",
    ordered = paste0("u", 1:8), parameterization = "theta")
## or in a single step:
fit.thresh <- measEq.syntax(configural.model = mod.cat, data = datCat,
    ordered = paste0("u", 1:8),
    parameterization = "theta",
    ID.fac = "std.lv", ID.cat = "Wu.Estabrook.2016",
    group = "g", group.equal = "thresholds",
    longFacNames = longFacNames, long.equal = "thresholds", return.fit = TRUE)

## compare their fit to test threshold invariance
anova(fit.config, fit.thresh)

## Not run:

## compare several invariance models
test.seq <- c("thresholds","loadings","intercepts","means","residuals")
meq.list <- list()
for (i in 0:length(test.seq)) {
    if (i == 0L) {
        meq.label <- "configural"
        group.equal <- ""
        long.equal <- ""
    } else {
        meq.label <- test.seq[i]
        group.equal <- test.seq[1:i]
        long.equal <- test.seq[1:i]
    }
    meq.list[[meq.label]] <- measEq.syntax(configural.model = mod.cat,
        data = datCat,
        ordered = paste0("u", 1:8),
        parameterization = "theta",
        ID.fac = "std.lv",
        ID.cat = "Wu.Estabrook.2016",
        group = "g",
        group.equal = group.equal,
        longFacNames = longFacNames, long.equal = long.equal,
        return.fit = TRUE)
}
compareFit(meq.list)

## End(Not run)
**measEq.syntax-class**  
*Class for Representing a Measurement-Equivalence Model*

**Description**

This class of object stores information used to automatically generate lavaan model syntax to represent user-specified levels of measurement equivalence/invariance across groups and/or repeated measures. See `measEq.syntax` for details.

**Usage**

```r
## S4 method for signature 'measEq.syntax'
as.character(x, package = "lavaan")

## S4 method for signature 'measEq.syntax'
show(object)

## S4 method for signature 'measEq.syntax'
summary(object, verbose = TRUE)

## S4 method for signature 'measEq.syntax'
update(object, ..., evaluate = TRUE)
```

**Arguments**

- `x, object`: an object of class `measEq.syntax`
- `package`: character indicating the package for which the syntax should be generated. Currently, only "lavaan".
- `verbose`: logical indicating whether to print a summary to the screen (default). If `FALSE`, only a pattern matrix is returned.
- `...`: Additional arguments to the call, or arguments with changed values.
- `evaluate`: If `TRUE`, evaluate the new call; otherwise, return the new call.

**Value**

- `summary`: signature(object = "measEq.syntax", verbose = TRUE): A character matrix indicating the pattern of numeric, ordered, or latent indicators loading on common factors. By default (verbose = TRUE), summary also prints descriptive details about the model, including the numbers of indicators and factors, and which parameters are constrained to equality.
- `show`: signature(object = "measEq.syntax"): Prints a message about how to use the object for model fitting. Invisibly returns the object.
- `update`: signature(object = "measEq.syntax"), ..., evaluate = TRUE: Creates a new object with updated arguments.
as.character measeqNsyntax object to model syntax that can be copy/pasted into a syntax file to be edited before analysis, or simply passed to lavaan to fit the model to data.

Slots

package character indicating the software package used to represent the model. Currently, only "lavaan" is available, which uses the LISREL representation (see lavOptions). In the future, "OpenMx" may become available, using RAM representation.

model.type character. Currently, only "cfa" is available. Future versions may allow for MIMIC / RFA models, where invariance can be tested across levels of exogenous variables explicitly included as predictors of indicators, controlling for their effects on (or correlation with) the common factors.

call The function call as returned by match.call(), with some arguments updated if necessary for logical consistency.

meanstructure logical indicating whether a mean structure is included in the model.

numeric character vector naming numeric manifest indicators.

ordered character vector naming ordered indicators.

parameterization character. See lavOptions.

specify list of parameter matrices, similar in form to the output of lavInspect(fit, "free"). These matrices are logical, indicating whether each parameter should be specified in the model syntax.

values list of parameter matrices, similar in form to the output of lavInspect(fit, "free"). These matrices are numeric, indicating whether each parameter should be freely estimated (indicated by NA) or fixed to a particular value.

labels list of parameter matrices, similar in form to the output of lavInspect(fit, "free"). These matrices contain character labels used to constrain parameters to equality.

constraints character vector containing additional equality constraints used to identify the model when ID.fac = "fx".

ngroups integer indicating the number of groups.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

Examples

## See ?measEq.syntax help page
Description

The model fit evaluation approach using modification indices and expected parameter changes.

Usage

miPowerFit(lavaanObj, stdLoad = 0.4, cor = 0.1, stdBeta = 0.1, 
intcept = 0.2, stdDelta = NULL, delta = NULL, cilevel = 0.9)

Arguments

- lavaanObj: The lavaan model object used to evaluate model fit
- stdLoad: The amount of standardized factor loading that one would like to be detected (rejected). The default value is 0.4, which is suggested by Saris and colleagues (2009, p. 571).
- cor: The amount of factor or error correlations that one would like to be detected (rejected). The default value is 0.1, which is suggested by Saris and colleagues (2009, p. 571).
- stdBeta: The amount of standardized regression coefficients that one would like to be detected (rejected). The default value is 0.1, which is suggested by Saris and colleagues (2009, p. 571).
- intercept: The amount of standardized intercept (similar to Cohen’s $d$ that one would like to be detected (rejected). The default value is 0.2, which is equivalent to a low effect size proposed by Cohen (1988, 1992).
- stdDelta: The vector of the standardized parameters that one would like to be detected (rejected). If this argument is specified, the value here will overwrite the other arguments above. The order of the vector must be the same as the row order from modification indices from the lavaan object. If a single value is specified, the value will be applied to all parameters.
- delta: The vector of the unstandardized parameters that one would like to be detected (rejected). If this argument is specified, the value here will overwrite the other arguments above. The order of the vector must be the same as the row order from modification indices from the lavaan object. If a single value is specified, the value will be applied to all parameters.
- cilevel: The confidence level of the confidence interval of expected parameter changes. The confidence intervals are used in the equivalence testing.

Details

In the lavaan object, one can inspect the modification indices and expected parameter changes. Those values can be used to evaluate model fit by two methods.
First, Saris, Satorra, and van der Veld (2009, pp. 570-573) used the power to detect modification indices and expected parameter changes to evaluate model fit. First, one should evaluate whether the modification index of each parameter is significant. Second, one should evaluate whether the power to detect a target expected parameter change is high enough. If the modification index is not significant and the power is high, there is no misspecification. If the modification index is significant and the power is low, the fixed parameter is misspecified. If the modification index is significant and the power is high, the expected parameter change is investigated. If the expected parameter change is large (greater than the the target expected parameter change), the parameter is misspecified. If the expected parameter change is low (lower than the target expected parameter change), the parameter is not misspecified. If the modification index is not significant and the power is low, the decision is inconclusive.

Second, the confidence intervals of the expected parameter changes are formed. These confidence intervals are compared with the range of trivial misspecification, which could be (-delta, delta) or (0, delta) for nonnegative parameters. If the confidence intervals are outside of the range of trivial misspecification, the fixed parameters are severely misspecified. If the confidence intervals are inside the range of trivial misspecification, the fixed parameters are trivially misspecified. If confidence intervals are overlapped the range of trivial misspecification, the decision is inconclusive.

Value

A data frame with these variables:

1. lhs: The left-hand side variable, with respect to the operator in in the lavaan model syntax
2. op: The lavaan syntax operator: "~~" represents covariance, "=~" represents factor loading, "~" represents regression, and "~1" represents intercept.
3. rhs: The right-hand side variable
4. group: The level of the group variable for the parameter in question
5. mi: The modification index of the fixed parameter
6. epc: The expected parameter change if the parameter is freely estimated
7. target.epc: The target expected parameter change that represents the minimum size of misspecification that one would like to be detected by the test with a high power
8. std.epc: The standardized expected parameter change if the parameter is freely estimated
9. std.target.epc: The standardized target expected parameter change
10. significant.mi: Represents whether the modification index value is significant
11. high.power: Represents whether the power is enough to detect the target expected parameter change
12. decision.pow: The decision whether the parameter is misspecified or not based on Saris et al’s method: "M" represents the parameter is misspecified, "NM" represents the parameter is not misspecified, "EPC:M" represents the parameter is misspecified decided by checking the expected parameter change value, "EPC:NM" represents the parameter is not misspecified decided by checking the expected parameter change value, and "I" represents the decision is inconclusive.
13. se.epc: The standard errors of the expected parameter changes.
14. lower.epc: The lower bound of the confidence interval of expected parameter changes.
15. upper.epc: The upper bound of the confidence interval of expected parameter changes.
16. lower.std.epc: The lower bound of the confidence interval of standardized expected parameter changes.
17. upper.std.epc: The upper bound of the confidence interval of standardized expected parameter changes.
18. decision.ci: The decision whether the parameter is misspecified or not based on the confidence interval method: "M" represents the parameter is misspecified, "NM" represents the parameter is not misspecified, and "I" represents the decision is inconclusive.

The row numbers matches with the results obtained from the `inspec(object, "mi")` function.

**Author(s)**

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**References**


**See Also**

`moreFitIndices` For the additional fit indices information

**Examples**

```r
library(lavaan)

HS.model <- \\
visual =~ x1 + x2 + x3
    textual =~ x4 + x5 + x6
    speed =~ x7 + x8 + x9

fit <- cfa(HS.model, data = HolzingerSwineford1939, 
           group = "sex", meanstructure = TRUE)
miPowerFit(fit)

model <- \\
# latent variable definitions
    ind60 =~ x1 + x2 + x3
    dem60 =~ y1 + a*y2 + b*y3 + c*y4
    dem65 =~ y5 + a*y6 + b*y7 + c*y8

# regressions
    dem60 ~ ind60
    dem65 ~ ind60 + dem60
```

# residual correlations
y1 ~~ y5
y2 ~~ y4 + y6
y3 ~~ y7
y4 ~~ y8
y6 ~~ y8

fit2 <- sem(model, data = PoliticalDemocracy, meanstructure = TRUE)
miPowerFit(fit2, stdLoad = 0.3, cor = 0.2, stdBeta = 0.2, intcept = 0.5)

---
modindices.mi  Modification Indices for Multiple Imputations

Description

Modification indices (1-df Lagrange multiplier tests) from a latent variable model fitted to multiple imputed data sets. Statistics for releasing one or more fixed or constrained parameters in model can be calculated by pooling the gradient and information matrices across imputed data sets using Rubin’s (1987) rules, or by pooling the test statistics across imputed data sets (Li, Meng, Raghunathan, & Rubin, 1991).

Usage

modindices.mi(object, type = c("D2", "Rubin"), standardized = TRUE,
               cov.std = TRUE, information = "expected", power = FALSE,
               delta = 0.1, alpha = 0.05, high.power = 0.75, sort. = FALSE,
               minimum.value = 0, maximum.number = nrow(LIST), na.remove = TRUE,
               op = NULL)

modificationIndices.mi(object, type = c("D2", "Rubin"),
                        standardized = TRUE, cov.std = TRUE, information = "expected",
                        power = FALSE, delta = 0.1, alpha = 0.05, high.power = 0.75,
                        sort. = FALSE, minimum.value = 0, maximum.number = nrow(LIST),
                        na.remove = TRUE, op = NULL)

Arguments

object  An object of class lavaan.mi
type   character indicating which pooling method to use. type = "D2" (default) indicates that modification indices that were calculated within each imputed data set will be pooled across imputations, as described in Li, Meng, Raghunathan, & Rubin (1991) and Enders (2010). "Rubin" indicates Rubin’s (1987) rules will be applied to the gradient and information, and those pooled values will be used to calculate modification indices in the usual manner.
modindices.mi

standardized logical. If TRUE, two extra columns (\$sepc.lv and \$sepc.all) will contain standardized values for the EPCs. In the first column (\$sepc.lv), standardization is based on the variances of the (continuous) latent variables. In the second column (\$sepc.all), standardization is based on both the variances of both (continuous) observed and latent variables. (Residual) covariances are standardized using (residual) variances.

cov.std logical. TRUE if type == "D2". If TRUE (default), the (residual) observed covariances are scaled by the square-root of the diagonal elements of the \( \Theta \) matrix, and the (residual) latent covariances are scaled by the square-root of the diagonal elements of the \( \Psi \) matrix. If FALSE, the (residual) observed covariances are scaled by the square-root of the diagonal elements of the model-implied covariance matrix of observed variables (\( \Sigma \)), and the (residual) latent covariances are scaled by the square-root of the diagonal elements of the model-implied covariance matrix of the latent variables.

information character indicating the type of information matrix to use (check lavInspect for available options). "expected" information is the default, which provides better control of Type I errors.

power logical. If TRUE, the (post-hoc) power is computed for each modification index, using the values of delta and alpha.

delta The value of the effect size, as used in the post-hoc power computation, currently using the unstandardized metric of the \$epc column.

alpha The significance level used for deciding if the modification index is statistically significant or not.

high.power If the computed power is higher than this cutoff value, the power is considered 'high'. If not, the power is considered 'low'. This affects the values in the $decision column in the output.

sort logical. If TRUE, sort the output using the values of the modification index values. Higher values appear first.

minimum.value numeric. Filter output and only show rows with a modification index value equal or higher than this minimum value.

maximum.number integer. Filter output and only show the first maximum number rows. Most useful when combined with the sort option.

na.remove logical. If TRUE (default), filter output by removing all rows with NA values for the modification indices.

op character string. Filter the output by selecting only those rows with operator op.

Value

A data.frame containing modification indices and (S)EPCs.

Note

When type = "D2", each (S)EPC will be pooled by taking its average across imputations. When type = "Rubin", EPCs will be calculated in the standard way using the pooled gradient and information, and SEPCs will be calculated by standardizing the EPCs using model-implied (residual) variances.
Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
Adapted from lavaan source code, written by Yves Rosseel (Ghent University; <Yves.Rrosseel@UGent.be>)
type = "Rubin" method proposed by Maxwell Mansolf (University of California, Los Angeles; <mamansolf@gmail.com>)

References


Examples

## Not run:
## impose missing data for example
HSMiss <- HolzingerSwineford1939[ , c(paste("x", 1:9, sep = ""),
   "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

## impute missing data
library(Amelia)
set.seed(12345)
HS.amelia <- amelia(HSMiss, m = 20, nom = "school", p2s = FALSE)
imps <- HS.amelia$imputations

## specify CFA model from lavaan's ?cfa help page
HS.model <- ' visual =~ x1 + x2 + x3
textual =~ x4 + x5 + x6
   speed =~ x7 + x8 + x9
',

out <- cfa.mi(HS.model, data = imps)

modindices.mi(out) # default: Li et al.'s (1991) "D2" method
modindices.mi(out, type = "Rubin") # Rubin's rules

## End(Not run)
Description

This function takes an expression for an indirect effect, the parameters and standard errors associated with the expression and returns a confidence interval based on a Monte Carlo test of mediation (MacKinnon, Lockwood, & Williams, 2004).

Usage

monteCarloMed(expression, ..., ACM = NULL, object = NULL, rep = 20000, CI = 95, plot = FALSE, outputValues = FALSE)

Arguments

expression A character scalar representing the computation of an indirect effect. Different parameters in the expression should have different alphanumeric values. Expressions can use either addition (+) or multiplication (*) operators.

... Parameter estimates for all parameters named in expression. The order of parameters should follow from expression (the first parameter named in expression should be the first parameter listed in ...). Alternatively ... can be a vector of parameter estimates.

ACM A matrix representing the asymptotic covariance matrix of the parameters described in expression. This matrix should be a symmetric matrix with dimensions equal to the number of parameters names in expression. Information on finding the ACOV is popular SEM software is described below.)

object A lavaan model object fitted after running the running the cfa, sem, growth, or lavaan functions. The model must have parameters labelled with the same labels used in expression. When using this option do not specify values for ...or ACM

rep The number of replications to compute. Many thousand are recommended.

CI Width of the confidence interval computed.

plot Should the function output a plot of simulated values of the indirect effect?

outputValues Should the function output all simulated values of the indirect effect?

Details

This function implements the Monte Carlo test of mediation first described in MacKinnon, Lockwood, & Williams (2004) and extends it to complex cases where the indirect effect is more than a function of two parameters. The function takes an expression for the indirect effect, randomly simulated values of the indirect effect based on the values of the parameters (and the associated standard errors) comprising the indirect effect, and outputs a confidence interval of the indirect effect based on the simulated values. For further information on the Monte Carlo test of mediation see MacKinnon, Lockwood, & Williams (2004) and Preacher & Selig (2012).

The asymptotic covariance matrix can be easily found in many popular SEM software applications.
- LISREL: Including the EC option on the OU line will print the ACM to a separate file. The file contains the lower triangular elements of the ACM in free format and scientific notation.
- Mplus: Include the command TECH3; in the OUTPUT section. The ACM will be printed in the output.
- lavaan: Use the command vcov on the fitted lavaan object to print the ACM to the screen.

Value

A list with two elements. The first element is the point estimate for the indirect effect. The second element is a matrix with values for the upper and lower limits of the confidence interval generated from the Monte Carlo test of mediation. If `outputValues = TRUE`, output will be a list with a list with the point estimate and values for the upper and lower limits of the confidence interval as the first element and a vector of simulated values of the indirect effect as the second element.

Author(s)

Corbin Quick (University of Michigan; <corbinq@umich.edu>)
Alexander M. Schoemann (East Carolina University; <schoemann@ecu.edu>)
James P. Selig (University of New Mexico; <selig@unm.edu>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
## Simple two path mediation
## Write expression of indirect effect
med <- 'a*b'
## Parameter values from analyses
aparam <- 1
bparam <- 2
## Asymptotic covariance matrix from analyses
AC <- matrix(c(.01,.0002,
               .0002,.02), nrow=2, byrow=TRUE)
## Compute CI, include a plot
```
`moreFitIndices`  

Calculate more fit indices that are not already provided in lavaan.

**Description**

Calculate more fit indices that are not already provided in lavaan.

**Usage**

`moreFitIndices(object, fit.measures = "all", nPrior = 1)`

**Arguments**

- **object**
  - The lavaan model object provided after running the `cfa`, `sem`, `growth`, or `lavaan` functions.

- **fit.measures**
  - Additional fit measures to be calculated. All additional fit measures are calculated by default.

- **nPrior**
  - The sample size on which prior is based. This argument is used to compute BIC*.
Details

Gamma Hat (gammaHat; West, Taylor, & Wu, 2012) is a global fit index which can be computed (assuming equal number of indicators across groups) by

\[
gammaHat = \frac{p}{p + 2 \times \frac{\chi^2_k - df_k}{N}}
\]

where \( p \) is the number of variables in the model, \( \chi^2_k \) is the \( \chi^2 \) test statistic value of the target model, \( df_k \) is the degree of freedom when fitting the target model, and \( N \) is the sample size (or sample size minus the number of groups if \( \text{mimic} \) is set to "EQS").

Adjusted Gamma Hat (adjGammaHat; West, Taylor, & Wu, 2012) is a global fit index which can be computed by

\[
adjGammaHat = \left(1 - \frac{K \times p \times (p + 1)}{2 \times df_k}\right) \times \left(1 - \gammaHat\right),
\]

where \( K \) is the number of groups (please refer to Dudgeon, 2004 for the multiple-group adjustment for \( \text{agfi}^* \)).

Corrected Akaike Information Criterion (aic.smallN; Burnham & Anderson, 2003) is a corrected version of AIC for small sample size, often abbreviated AICc:

\[
aic.smallN = AIC + \frac{2k(k+1)}{N - k - 1},
\]

where \( AIC \) is the original AIC: \(-2 \times LL + 2k\) (where \( k \) is the number of estimated parameters in the target model). Note that AICc is a small-sample correction derived for univariate regression models, so it is probably not appropriate for comparing SEMs.

Corrected Bayesian Information Criterion (bic.priorN; Kuha, 2004) is similar to BIC but explicitly specifying the sample size on which the prior is based (\( N_{prior} \)).

\[
bic.priorN = f + k \log (1 + N/N_{prior}),
\]

Stochastic information criterion (SIC; Preacher, 2006) is similar to AIC or BIC. This index will account for model complexity in the model’s function form, in addition to the number of free parameters. This index will be provided only when the \( \chi^2 \) value is not scaled. The SIC can be computed by

\[
sic = \frac{1}{2} \left( f - \log \det I(\hat{\theta}) \right),
\]

where \( I(\hat{\theta}) \) is the information matrix of the parameters.

Hannan-Quinn Information Criterion (hqc; Hannan & Quinn, 1979) is used for model selection similar to AIC or BIC.

\[
hqc = f + 2k \log (\log N),
\]

Note that if Satorra–Bentler or Yuan–Bentler’s method is used, the fit indices using the scaled \( \chi^2 \) values are also provided.

See \texttt{nullRMSEA} for the further details of the computation of RMSEA of the null model.
Value

1. gammaHat: Gamma Hat
2. adjGammaHat: Adjusted Gamma Hat
3. baseline.rmsea: RMSEA of the Baseline (Null) Model
4. aic.smallN: Corrected (for small sample size) Akaike Information Criterion
5. bic.priorN: Bayesian Information Criterion with specified prior sample size
6. sic: Stochastic Information Criterion
7. hqc: Hannan-Quinn Information Criterion
8. gammaHatNscaled: Gamma Hat using scaled $\chi^2$
9. adjGammaHatNscaled: Adjusted Gamma Hat using scaled $\chi^2$
10. baseline.rmseaNscaled: RMSEA of the Baseline (Null) Model using scaled $\chi^2$

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
Aaron Boulton (University of North Carolina, Chapel Hill; <aboulton@email.unc.edu>)
Ruben Arslan (Humboldt-University of Berlin, <rubenarslan@gmail.com>)
Yves Rosseel (Ghent University; <Yves.Rosseel@UGent.be>)

References


See Also

- miPowerFit For the modification indices and their power approach for model fit evaluation
- nullRMSEA For RMSEA of the null model
**Examples**

```r
HS.model <- ' visual  = x1 + x2 + x3
textual  = x4 + x5 + x6
speed    = x7 + x8 + x9 '

fit <- cfa(HS.model, data = HolzingerSwineford1939)
moreFitIndices(fit)

fit2 <- cfa(HS.model, data = HolzingerSwineford1939, estimator = "mlr")
moreFitIndices(fit2)
```

---

**mvrnonnorm**

*Generate Non-normal Data using Vale and Maurelli (1983) method*

**Description**

Generate Non-normal Data using Vale and Maurelli (1983) method. The function is designed to be as similar as the popular `mvrnorm` function in the `MASS` package. The codes are copied from `mvrnorm` function in the `MASS` package for argument checking and `lavaan` package for data generation using Vale and Maurelli (1983) method.

**Usage**

```r
mvrnonnorm(n, mu, Sigma, skewness = NULL, kurtosis = NULL,
           empirical = FALSE)
```

**Arguments**

- `n` Sample size
- `mu` A mean vector. If elements are named, those will be used as variable names in the returned data matrix.
- `Sigma` A positive-definite symmetric matrix specifying the covariance matrix of the variables. If rows or columns are named (and `mu` is unnamed), those will be used as variable names in the returned data matrix.
- `skewness` A vector of skewness of the variables
- `kurtosis` A vector of excessive kurtosis of the variables
- `empirical` If TRUE, `mu` and `Sigma` specify the empirical rather than population mean and covariance matrix

**Value**

A data matrix
Author(s)

The original function is the simulateData function written by Yves Rosseel in the lavaan package. The function is adjusted for a convenient usage by Sunthud Pornprasertmanit (<psunthud@gmail.com>). Terrence D. Jorgensen added the feature to retain variable names from mu or Sigma.

References


Examples

```r
set.seed(123)
mvrnonnorm(20, c(1, 2), matrix(c(10, 2, 2, 5), 2, 2), skewness = c(5, 2), kurtosis = c(3, 3))
```

```
set.seed(123)
mvrnonnorm(20, c(a = 1, b = 2), matrix(c(10, 2, 2, 5), 2, 2), skewness = c(5, 2), kurtosis = c(3, 3))
```

net

**Nesting and Equivalence Testing**

Description

This test examines whether models are nested or equivalent based on Bentler and Satorra’s (2010) procedure.

Usage

```
net(..., crit = 1e-04)
```

Arguments

- `...`: The lavaan objects used for test of nesting and equivalence
- `crit`: The upper-bound criterion for testing the equivalence of models. Models are considered nested (or equivalent) if the difference between their $\chi^2$ fit statistics is less than this criterion.

Details

The concept of nesting/ equivalence should be the same regardless of estimation method. However, the particular method of testing nesting/ equivalence (as described in Bentler & Satorra, 2010) employed by the net function analyzes summary statistics (model-implied means and covariance matrices, not raw data). In the case of robust methods like MLR, the raw data is only utilized for the robust adjustment to SE and chi-sq, and the net function only checks the unadjusted chi-sq for
the purposes of testing nesting/equivalence. This method does not apply to models that estimate thresholds for categorical data, so an error message will be issued if such a model is provided.

Value

The `Net` object representing the outputs for nesting and equivalent testing, including a logical matrix of test results and a vector of degrees of freedom for each model.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
## Not run:
m1 <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9

m2 <- ' f1 = x1 + x2 + x3 + x4
f2 = x5 + x6 + x7 + x8 + x9

m3 <- ' visual = x1 + x2 + x3
textual = eq*x4 + eq*x5 + eq*x6
speed = x7 + x8 + x9

fit1 <- cfa(m1, data = HolzingerSwineford1939)
fit1a <- cfa(m1, data = HolzingerSwineford1939, std.lv = TRUE) # Equivalent to fit1
fit2 <- cfa(m2, data = HolzingerSwineford1939) # Not equivalent to or nested in fit1
fit3 <- cfa(m3, data = HolzingerSwineford1939) # Nested in fit1 and fit1a

tests <- net(fit1, fit1a, fit2, fit3)
tests
summary(tests)

## End(Not run)
```
Description

This class contains the results of nesting and equivalence testing among multiple models.

Usage

```r
## S4 method for signature 'Net'
show(object)

## S4 method for signature 'Net'
summary(object)
```

Arguments

- `object`: An object of class `Net`.

Value

- `show`: `signature(object = "Net")`: prints the logical matrix of test results.
- `summary`: `signature(object = "Net")`: prints a narrative description of results. The original object is invisibly returned.

Slots

- `test`: Logical matrix indicating nesting/equivalence among models.
- `df`: The degrees of freedom of tested models.

Objects from the Class

Objects can be created via the `net` function.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

See Also

`net`

Examples

```r
# See the example in the net function.
```
nullRMSEA

Calculate the RMSEA of the null model

Description

Calculate the RMSEA of the null (baseline) model

Usage

nullRMSEA(object, scaled = FALSE, silent = FALSE)

Arguments

object: The lavaan model object provided after running the cfa, sem, growth, or lavaan functions.

scaled: If TRUE, the scaled (or robust, if available) RMSEA is returned. Ignored if a robust test statistic was not requested.

silent: If TRUE, do not print anything on the screen.

Details

RMSEA of the null model is calculated similar to the formula provided in the lavaan package. The standard formula of RMSEA is

$$RMSEA = \sqrt{\frac{\chi^2}{N \times df}} - \frac{1}{N} \times \sqrt{G}$$

where $\chi^2$ is the chi-square test statistic value of the target model, $N$ is the total sample size, $df$ is the degree of freedom of the hypothesized model, $G$ is the number of groups. Kenny proposed in his website that

"A reasonable rule of thumb is to examine the RMSEA for the null model and make sure that is no smaller than 0.158. An RMSEA for the model of 0.05 and a TLI of .90, implies that the RMSEA of the null model is 0.158. If the RMSEA for the null model is less than 0.158, an incremental measure of fit may not be that informative."

See also http://davidakenny.net/cm/fit.htm

Value

A value of RMSEA of the null model (a numeric vector) returned invisibly.

Author(s)

Ruben Arslan (Humboldt-University of Berlin, <rubenarslan@gmail.com>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
**References**


**See Also**

- `miPowerFit` For the modification indices and their power approach for model fit evaluation
- `moreFitIndices` For other fit indices

**Examples**

```r
HS.model <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9 '

fit <- cfa(HS.model, data = HolzingerSwineford1939)
nullRMSEA(fit)
```

**orthRotate**

Implement orthogonal or oblique rotation

**Description**

These functions will implement orthogonal or oblique rotation on standardized factor loadings from a lavaan output.

**Usage**

```r
orthRotate(object, method = "varimax", ...)
oblqRotate(object, method = "quartimin", ...)
funRotate(object, fun, ...)
```

**Arguments**

- `object` A lavaan output
- `method` The method of rotations, such as "varimax", "quartimax", "geomin", "oblimin", or any gradient projection algorithms listed in the GPA function in the GPArotation package.
- `...` Additional arguments for the GPForth function (for orthRotate), the GPFoblq function (for oblqRotate), or the function that users provide in the fun argument.
fun The name of the function that users wish to rotate the standardized solution. The functions must take the first argument as the standardized loading matrix and return the GPArotation object. Check this page for available functions: rotations.

Details
These functions will rotate the unrotated standardized factor loadings by orthogonal rotation using the GPforth function or oblique rotation using the GPFoblq function the GPArotation package. The resulting rotation matrix will be used to calculate standard errors of the rotated standardized factor loading by delta method by numerically computing the Jacobian matrix by the lav_func_jacobian_simple function.

Value
An linkS4class{EFA} object that saves the rotated EFA solution

Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

Examples

```r
## Not run:

unrotated <- efaUnrotate(HolzingerSwineford1939, nf = 3,
                         varList = paste0("x", 1:9), estimator = "mlr")

# Orthogonal varimax
out.varimax <- orthRotate(unrotated, method = "varimax")
summary(out.varimax, sort = FALSE, suppress = 0.3)

# Orthogonal Quartzimin
orthRotate(unrotated, method = "quartimin")

# Oblique Quartzimin
oblqRotate(unrotated, method = "quartimin")

# Geomin
oblqRotate(unrotated, method = "geomin")

# Target rotation
library(GPArotation)
target <- matrix(0, 9, 3)
target[1:3, 1] <- NA
target[4:6, 2] <- NA
target[7:9, 3] <- NA
colnames(target) <- c("factor1", "factor2", "factor3")
## This function works with GPArotation version 2012.3-1
funRotate(unrotated, fun = "targetQ", Target = target)
```
Description

This function generates a given number of randomly generated item-to-parcel allocations, fits a model to each allocation, and provides averaged results over all allocations.

Usage

```
parcelAllocation(model, data, parcel.names, item.syntax, nAlloc = 100,
fun = "sem", alpha = 0.05, fit.measures = c("chisq", "df", "cfi",
"tli", "rmsea", "srmr"), ..., show.progress = FALSE, do.fit = TRUE)
```

Arguments

- `model` lavaan model syntax specifying the model fit to (at least some) parceled data. Note that there can be a mixture of items and parcels (even within the same factor), in case certain items should never be parceled. Can be a character string or parameter table. Also see `lavaanify` for more details.
- `data` A `data.frame` containing all observed variables appearing in the model, as well as those in the `item.syntax` used to create parcels. If the data have missing values, multiple imputation before parceling is recommended: submit a stacked data set (with a variable for the imputation number, so they can be separated later) and set `do.fit = FALSE` to return the list of `data.frame`s (one per allocation), each of which is a stacked, imputed data set with parcels.
- `parcel.names` character vector containing names of all parcels appearing as indicators in model.
- `item.syntax` lavaan model syntax specifying the model that would be fit to all of the unparceled items, including items that should be randomly allocated to parcels appearing in model.
- `nAlloc` The number of random items-to-parcels allocations to generate.
- `fun` character string indicating the name of the `lavaan` function used to fit model to data. Can only take the values "lavaan", "sem", "cfa", or "growth".
- `alpha` Alpha level used as criterion for significance.
- `fit.measures` character vector containing names of fit measures to request from each fitted `lavaan` model. See the output of `fitMeasures` for a list of available measures.
- `...` Additional arguments to be passed to `lavaanList`.
- `show.progress` If TRUE, show a `txtProgressBar` indicating how fast the model-fitting iterates over allocations.
- `do.fit` If TRUE (default), the model is fitted to each parceled data set, and the summary of results is returned (see the Value section below). If FALSE, the items are randomly parceled, but the model is not fit; instead, the list of `data.frame`s is returned (so assign it to an object).
Details

This function implements the random item-to-parcel allocation procedure described in Sterba (2011) and Sterba and MacCallum (2010). The function takes a single data set with item-level data, randomly assigns items to parcels, fits a structural equation model to the parceled data (using lavaan), and repeats this process for a user-specified number of random allocations. Results from all fitted models are summarized in the output. For further details on the benefits of the random allocation of items to parcels, see Sterba (2011) and Sterba and MacCallum (2010).

Value

**Estimates**

A data frame containing results related to parameter estimates with columns corresponding to parameter names, average parameter estimates across allocations, the standard deviation of parameter estimates across allocations, the minimum parameter estimate across allocations, the maximum parameter estimate across allocations, the range of parameter estimates across allocations, and the proportions of allocations in which the parameter estimate is significant.

**SE**

A data frame containing results related to standard errors with columns corresponding to parameter names, average standard errors across allocations, the standard deviation of standard errors across allocations, the minimum standard error across allocations, the maximum standard error across allocations, and the range of standard errors across allocations.

**Fit**

A data frame containing results related to model fit with columns corresponding to fit index names, the average of each index across allocations, the standard deviation of each fit index across allocations, the minimum of each fit index across allocations, the maximum of each fit index across allocations, and the range of each fit index across allocations.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <tjorgensen34@gmail.com>)

References


See Also

`PAVranking`, `poolMAlloc`

Examples

```r
## Fit 2-factor CFA to simulated data. Each factor has 9 indicators.
## Specify the item-level model (if NO parcels were created)
```

# Below, we reduce the size of this same model by applying different parceling schemes

## 3-indicator parcels

```r
mod.parcels <- 
  f1 <- par1 + par2 + par3
  f2 <- par4 + par5 + par6
```

*names of parcels*

```r
(parcel.names <- paste0("par", 1:6))
```

## Not run:

```r
parcelAllocation(mod.parcels, data = simParcel, parcel.names, item.syntax, 
  nAlloc = 20, std.lv = TRUE, parallel = "snow", iseed = 12345)
```

## End(Not run)

## multigroup example

```r
simParcel$group <- 0:1 # arbitrary groups for example
mod.mg <- 
  f1 <- par1 + c(L2, L2) + par2 + par3
  f2 <- par4 + par5 + par6
```

*names of parcels*

```r
(parcel.names <- paste0("par", 1:6))
```

```r
set.seed(12345)
p parcelAllocation(mod.mg, data = simParcel, parcel.names, item.syntax, 
  std.lv = TRUE, group = "group", group.equal = "loadings", 
  nAlloc = 20, show.progress = TRUE)
```

## parcels for first factor, items for second factor

```r
mod.items <- 
  f1 <- par1 + par2 + par3
  f2 <- f2item2 + f2item7 + f2item8
```

*names of parcels*

```r
(parcel.names <- paste0("par", 1:3))
```

```r
set.seed(12345)
p parcelAllocation(mod.items, data = simParcel, parcel.names, item.syntax, 
  nAlloc = 20, std.lv = TRUE)
```

## mixture of 1- and 3-indicator parcels for second factor

```r
```
mod.mix <-`
  f1 <- par1 + par2 + par3
  f2 <- f2item2 + f2item7 + f2item8 + par4 + par5 + par6`

# names of parcels
(parcel.names <- paste0("par", 1:6))

set.seed(12345)
parcelAllocation(mod.mix, data = simParcel, parcel.names, item.syntax, nAlloc = 20, std.lv = TRUE)

---

partialInvariance  Partial Measurement Invariance Testing Across Groups

Description

This test will provide partial invariance testing by (a) freeing a parameter one-by-one from nested model and compare with the original nested model or (b) fixing (or constraining) a parameter one-by-one from the parent model and compare with the original parent model. This function only works with congeneric models. The `partialInvariance` is used for continuous variable. The `partialInvarianceCat` is used for categorical variables.

Usage

```r
partialInvariance(fit, type = "metric", free = NULL, fix = NULL, refgroup = 1, poolvar = TRUE, p.adjust = "none", fbound = 2, return.fit = FALSE, method = "satorra.bentler.2001")
```

```r
partialInvarianceCat(fit, type = "metric", free = NULL, fix = NULL, refgroup = 1, poolvar = TRUE, p.adjust = "none", return.fit = FALSE, method = "satorra.bentler.2001")
```

Arguments

- **fit**: A list of models for invariance testing. Each model should be assigned by appropriate names (see details). The result from `measurementInvariance` or `measurementInvarianceCat` could be used in this argument directly.
- **type**: The types of invariance testing: "metric", "scalar", "strict", or "means"
- **free**: A vector of variable names that are free across groups in advance. If partial mean invariance is tested, this argument represents a vector of factor names that are free across groups.
- **fix**: A vector of variable names that are constrained to be equal across groups in advance. If partial mean invariance is tested, this argument represents a vector of factor names that are fixed across groups.
- **refgroup**: The reference group used to make the effect size comparison with the other groups.
If TRUE, the variances are pooled across group for standardization. Otherwise, the variances of the reference group are used for standardization.

The method used to adjust p values. See \texttt{p.adjust} for the options for adjusting p values. The default is to not use any corrections.

The z-scores of factor that is used to calculate the effect size of the loading difference proposed by Millsap and Olivera-Aguilar (2012).

Return the submodels fitted by this function

The method used to calculate likelihood ratio test. See \texttt{lavTestLRT} for available options

There are four types of partial invariance testing:

- **Partial weak invariance.** The model named 'fit.configural' from the list of models is compared with the model named 'fit.loadings'. Each loading will be freed or fixed from the metric and configural invariance models respectively. The modified models are compared with the original model. Note that the objects in the list of models must have the names of "fit.configural" and "fit.loadings". Users may use "metric", "weak", "loading", or "loadings" in the type argument. Note that, for testing invariance on marker variables, other variables will be assigned as marker variables automatically.

- **Partial strong invariance.** The model named 'fit.loadings' from the list of models is compared with the model named either 'fit.intercepts' or 'fit.thresholds'. Each intercept will be freed or fixed from the scalar and metric invariance models respectively. The modified models are compared with the original model. Note that the objects in the list of models must have the names of "fit.loadings" and either "fit.intercepts" or "fit.thresholds". Users may use "scalar", "strong", "intercept", "intercepts", "threshold", or "thresholds" in the type argument. Note that, for testing invariance on marker variables, other variables will be assigned as marker variables automatically. Note that if all variables are dichotomous, scalar invariance testing is not available.

- **Partial strict invariance.** The model named either 'fit.intercepts' or 'fit.thresholds' (or 'fit.loadings') from the list of models is compared with the model named 'fit.residuals'. Each residual variance will be freed or fixed from the strict and scalar (or metric) invariance models respectively. The modified models are compared with the original model. Note that the objects in the list of models must have the names of "fit.residuals" and either "fit.intercepts", "fit.thresholds", or "fit.loadings". Users may use "strict", "residual", "residuals", "error", or "errors" in the type argument.

- **Partial mean invariance.** The model named either 'fit.intercepts' or 'fit.thresholds' (or 'fit.residuals' or 'fit.loadings') from the list of models is compared with the model named 'fit.means'. Each factor mean will be freed or fixed from the means and scalar (or strict or metric) invariance models respectively. The modified models are compared with the original model. Note that the objects in the list of models must have the names of "fit.means" and either "fit.residuals", "fit.intercepts", "fit.thresholds", or "fit.loadings". Users may use "means" or "mean" in the type argument.

Two types of comparisons are used in this function:
1. **free**: The nested model is used as a template. Then, one parameter indicating the differences between two models is free. The new model is compared with the nested model. This process is repeated for all differences between two models. The likelihood-ratio test and the difference in CFI are provided.

2. **fix**: The parent model is used as a template. Then, one parameter indicating the differences between two models is fixed or constrained to be equal to other parameters. The new model is then compared with the parent model. This process is repeated for all differences between two models. The likelihood-ratio test and the difference in CFI are provided.

3. **wald**: This method is similar to the **fix** method. However, instead of building a new model and compare them with likelihood-ratio test, multivariate wald test is used to compare equality between parameter estimates. See `lavTestWald` for further details. Note that if any rows of the contrast cannot be summed to 0, the Wald test is not provided, such as comparing two means where one of the means is fixed as 0. This test statistic is not as accurate as likelihood-ratio test provided in **fix**. I provide it here in case that likelihood-ratio test fails to converge.

Note that this function does not adjust for the inflated Type I error rate from multiple tests. The degree of freedom of all tests would be the number of groups minus 1.

The details of standardized estimates and the effect size used for each parameters are provided in the vignettes by running `vignette("partialInvariance")`.

**Value**

A list of results are provided. The list will consists of at least two elements:

1. **estimates**: The results of parameter estimates including pooled estimates (`poolest`), the estimates for each group, standardized estimates for each group (`std`), the difference in standardized values, and the effect size statistic (\(q\) for factor loading difference and \(h\) for error variance difference). See the details of this effect size statistic by running `vignette("partialInvariance")`. In the `partialInvariance` function, the additional effect statistics proposed by Millsap and Olivera-Aguilar (2012) are provided. For factor loading, the additional outputs are the observed mean difference (`diff_mean`), the mean difference if factor scores are low (`low_fscore`), and the mean difference if factor scores are high (`high_fscore`). The low factor score is calculated by (a) finding the factor scores that its \(z\) score equals \(-\text{bound}\) (the default is \(-2\)) from all groups and (b) picking the minimum value among the factor scores. The high factor score is calculated by (a) finding the factor scores that its \(z\) score equals \(\text{bound}\) (default = 2) from all groups and (b) picking the maximum value among the factor scores. For measurement intercepts, the additional outputs are the observed means difference (`diff_mean`) and the proportion of the differences in the intercepts over the observed means differences (`propdiff`). For error variances, the additional outputs are the proportion of the difference in error variances over the difference in observed variances (`propdiff`).

2. **results**: Statistical tests as well as the change in CFI are provided. \(\chi^2\) and \(p\) value are provided for all methods.

3. **models**: The submodels used in the **free** and **fix** methods, as well as the nested and parent models. The nested and parent models will be changed from the original models if **free** or **fit** arguments are specified.

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References


See Also

measurementInvariance for measurement invariance for continuous variables; measurementInvarianceCat for measurement invariance for categorical variables; lavTestWald for multivariate Wald test

Examples

```r
## Conduct weak invariance testing manually by using fixed-factor
## method of scale identification

library(lavaan)

conf <- "
f1 <- NA*x1 + x2 + x3
f2 <- NA*x4 + x5 + x6
f1 ~~ c(1, 1)*f1
f2 ~~ c(1, 1)*f2
"

weak <- "
f1 <- NA*x1 + x2 + x3
f2 <- NA*x4 + x5 + x6
f1 ~~ c(1, NA)*f1
f2 ~~ c(1, NA)*f2
"

configural <- cfa(conf, data = HolzingerSwineford1939, std.lv = TRUE, group="school")
weak <- cfa(weak, data = HolzingerSwineford1939, group="school", group.equal="loadings")
models <- list(fit.configural = configural, fit.loadings = weak)
partialInvariance(models, "metric")

## Not run:
partialInvariance(models, "metric", free = "x5") # "x5" is free across groups in advance
partialInvariance(models, "metric", fix = "x4") # "x4" is fixed across groups in advance

## Use the result from the measurementInvariance function
HW.model <- ' visual =- x1 + x2 + x3
textual =- x4 + x5 + x6
speed =- x7 + x8 + x9 '

models2 <- measurementInvariance(model = HW.model, data=HolzingerSwineford1939,
                                 group="school")
partialInvariance(models2, "scalar")

## Conduct weak invariance testing manually by using fixed-factor
## method of scale identification for dichotomous variables
```
```r
f <- rnorm(1000, 0, 1)
u1 <- 0.9*r + rnorm(1000, 1, sqrt(0.19))
u2 <- 0.8*r + rnorm(1000, 1, sqrt(0.36))
u3 <- 0.6*r + rnorm(1000, 1, sqrt(0.64))
u4 <- 0.7*r + rnorm(1000, 1, sqrt(0.57))
u1 <- as.numeric(cut(u1, breaks = c(-Inf, 0, Inf)))
u2 <- as.numeric(cut(u2, breaks = c(-Inf, 0.5, Inf)))
u3 <- as.numeric(cut(u3, breaks = c(-Inf, 0, Inf)))
u4 <- as.numeric(cut(u4, breaks = c(-Inf, -0.5, Inf)))
g <- rep(c(1, 2), 500)
dat2 <- data.frame(u1, u2, u3, u4, g)

configural2 <- "
f1 = NA*u1 + u2 + u3 + u4
u1 | c(t11, t11)*t1
u2 | c(t21, t21)*t1
u3 | c(t31, t31)*t1
u4 | c(t41, t41)*t1
f1 -- c(1, 1)*f1
f1 ~ c(0, NA)*1
u1 -- c(1, 1)*u1
u2 -- c(1, NA)*u2
u3 -- c(1, NA)*u3
u4 -- c(1, NA)*u4
"

outConfigural2 <- cfa(configural2, data = dat2, group = "g",
 parameterization = "theta", estimator = "wlsmv",
 ordered = c("u1", "u2", "u3", "u4"))

weak2 <- "
f1 = NA*u1 + c(f11, f11)*u1 + c(f21, f21)*u2 + c(f31, f31)*u3 + c(f41, f41)*u4
u1 | c(t11, t11)*t1
u2 | c(t21, t21)*t1
u3 | c(t31, t31)*t1
u4 | c(t41, t41)*t1
f1 -- c(1, NA)*f1
f1 ~ c(0, NA)*1
u1 -- c(1, 1)*u1
u2 -- c(1, NA)*u2
u3 -- c(1, NA)*u3
u4 -- c(1, NA)*u4
"

outWeak2 <- cfa(weak2, data = dat2, group = "g", parameterization = "theta",
 estimator = "wlsmv", ordered = c("u1", "u2", "u3", "u4"))

modelsCat <- list(fit.configural = outConfigural2, fit.loadings = outWeak2)

partialInvarianceCat(modelsCat, type = "metric")
partialInvarianceCat(modelsCat, type = "metric", free = "u2")
partialInvarianceCat(modelsCat, type = "metric", fix = "u3")
```
## Description

This function quantifies and assesses the consequences of parcel-allocation variability for model ranking of structural equation models (SEMs) that differ in their structural specification but share the same parcel-level measurement specification (see Sterba & Rights, 2016). This function is a modified version of `parcelAllocation` which can be used with only one SEM in isolation. The `pavranking` function repeatedly generates a specified number of random item-to-parcel allocations, and then fits two models to each allocation. Output includes summary information about the distribution of model selection results (including plots) and the distribution of results for each model individually, across allocations within-sample. Note that this function can be used when selecting among more than two competing structural models as well (see instructions below involving `seed`).

## Usage

```r
pavranking(nPerPar, facPlc, nAlloc = 100, parceloutput = NULL, syntaxA, syntaxB, dataset, names = NULL, leaveout = 0, seed = NA, ...)
```

## Arguments

- **nPerPar**: A list in which each element is a vector, corresponding to each factor, indicating sizes of parcels. If variables are left out of parceling, they should not be accounted for here (i.e., there should not be parcels of size 1).
- **facPlc**: A list of vectors, each corresponding to a factor, specifying the item indicators of that factor (whether included in parceling or not). Either variable names or column numbers. Variables not listed will not be modeled or included in output datasets.
- **nAlloc**: The number of random allocations of items to parcels to generate.
- **parceloutput**: folder where parceled data sets will be outputted (note for Windows users: file path must specified using forward slashes).
syntaxA lavaan syntax for Model A. Note that, for likelihood ratio test (LRT) results to be interpreted, Model A should be nested within Model B (though the function will still provide results when Models A and B are nonnested).

tsyntaxB lavaan syntax for Model B. Note that, for likelihood ratio test (LRT) results to be appropriate, Model A should be nested within Model B (though the function will still provide results when Models A and B are nonnested).

dataset Item-level dataset

names (Optional) A character vector containing the names of parceled variables.

leaveout (Optional) A vector of variables to be left out of randomized parceling. Either variable names or column numbers are allowed.

seed (Optional) Random seed used for parceling items. When the same random seed is specified and the program is re-run, the same allocations will be generated. The seed argument can be used to assess parcel-allocation variability in model ranking when considering more than two models. For each pair of models under comparison, the program should be rerun using the same random seed. Doing so ensures that multiple model comparisons will employ the same set of parcel datasets.

... Additional arguments to be passed to lavaan. See also lavOptions

Details

This is a modified version of parcelAllocation which was, in turn, based on the SAS macro ParcelAlloc (Sterba & MacCallum, 2010). The PAVranking function produces results discussed in Sterba and Rights (2016) relevant to the assessment of parcel-allocation variability in model selection and model ranking. Specifically, the PAVranking function first uses a modified version of parcelAllocation to generate a given number (nalloc) of item-to-parcel allocations. Then, PAVranking provides the following new developments: specifying more than one SEM and producing results for Model A and Model B separately that summarize parcel allocation variability in estimates, standard errors, and fit indices. PAVranking also newly produces results summarizing parcel allocation variability in model selection index values and model ranking between Models A and B. Additionally, PAVranking newly allows for nonconverged solutions and outputs the proportion of allocations that converged as well as the proportion of proper solutions (results are summarized for converged and proper allocations only).

For further details on the benefits of the random allocation of items to parcels, see Sterba (2011) and Sterba and MacCallum (2010).

Note: This function requires the lavaan package. Missing data code needs to be NA. If function returns "Error in plot.new() : figure margins too large," user may need to increase size of the plot window and rerun.

Value

Estimates_A, Estimates_B

A table containing results related to parameter estimates (in table Estimates_A for Model A and in table Estimates_B for Model B) with columns corresponding to parameter name, average parameter estimate across allocations, standard deviation of parameter estimate across allocations, the maximum parameter estimate across allocations, the minimum parameter estimate across allocations, the
range of parameter estimates across allocations, and the percent of allocations in which the parameter estimate is significant.

**SE_A, SE_B**  
A table containing results related to standard errors (in table SE_A for Model A and in table SE_B for Model B) with columns corresponding to parameter name, average standard error across allocations, the standard deviation of standard errors across allocations, the maximum standard error across allocations, the minimum standard error across allocations, and the range of standard errors across allocations.

**Fit_A, Fit_B**  
A table containing results related to model fit (in table Fit_A for Model A and in table Fit_B for Model B) with columns corresponding to fit index name, the average of the fit index across allocations, the standard deviation of the fit index across allocations, the maximum of the fit index across allocations, the minimum of the fit index across allocations, the range of the fit index across allocations, and the percent of allocations where the chi-square test of absolute fit was significant.

**LRT Summary, Model A vs. Model B**  
A table with columns corresponding to: average likelihood ratio test (LRT) statistic for comparing Model A vs. Model B (null hypothesis is no difference in fit between Models A and B in the population), degrees of freedom (i.e. difference in the number of free parameters between Models A and B), as well as the standard deviation, maximum, and minimum of LRT statistics across allocations, and the percent of allocations where the LRT was significant (indicating preference for the more complex Model B).

**Fit index differences**  
A table containing percentage of allocations where Model A is preferred over Model B according to BIC, AIC, RMSEA, CFI, TLI and SRMR and where Model B is preferred over Model A according to the same indices. Also includes the average amount by which the given model is preferred (calculated only using allocations where it was preferred).

**Fit index difference histograms**  
Histograms are automatically outputted showing the distribution of the differences (Model A - Model B) for each fit index and for the p-value of the likelihood ratio difference test.

**Percent of Allocations with | BIC Diff | > 10**  
A table containing the percentage of allocations with (BIC for Model A) - (BIC for Model B) < -10, indicating "very strong evidence" to prefer Model A over Model B and the percentage of allocations with (BIC for Model A) - (BIC for Model B) > 10, indicating "very strong evidence" to prefer Model B over Model A (Raftery, 1995).
Converged and proper

A table containing the proportion of allocations that converged for Model A, Model B, and both models, and the proportion of allocations with converged and proper solutions for Model A, Model B, and both models.

Author(s)

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The author would also like to credit Corbin Quick and Alexander Schoemann for providing the original parcelAllocation function on which this function is based.

References


See Also

*parcelAllocation, poolMAloc*

Examples

```r
## Not run:
## lavaan syntax for Model A: a 2 Uncorrelated
## factor CFA model to be fit to parceled data

parmodelA <-'
f1 ~ NA+p1f1 + p2f1 + p3f1
f2 ~ NA+p1f2 + p2f2 + p3f2
p1f1 ~ 1
p2f1 ~ 1
p3f1 ~ 1
p1f2 ~ 1
p2f2 ~ 1
p3f2 ~ 1
p1f1 ~~ p1f1
p2f1 ~~ p2f1
p3f1 ~~ p3f1
p1f2 ~~ p1f2
p2f2 ~~ p2f2
p3f2 ~~ p3f2
```
permuteMeasEq

\[
\begin{align*}
  f_1 & \sim 1 \cdot f_1 \\
  f_2 & \sim 1 \cdot f_2 \\
  f_1 & \sim 0 \cdot f_2
\end{align*}
\]

## lavaan syntax for Model B: a 2 Correlated
## factor CFA model to be fit to parceled data

```r
parmodelB <- ' 
  f1 =~ NA * p1f1 + p2f1 + p3f1 
  f2 =~ NA * p1f2 + p2f2 + p3f2 
  p1f1 ~ 1 
  p2f1 ~ 1 
  p3f1 ~ 1 
  p1f2 ~ 1 
  p2f2 ~ 1 
  p3f2 ~ 1 
  p1f1 ~ p1f1 
  p2f1 ~ p2f1 
  p3f1 ~ p3f1 
  p1f2 ~ p1f2 
  p2f2 ~ p2f2 
  p3f2 ~ p3f2 
  f1 ~ 1 \cdot f1 
  f2 ~ 1 \cdot f2 
  f1 ~ f2
',
```

## specify items for each factor

```r
f1name <- colnames(simParcel)[1:9] 
f2name <- colnames(simParcel)[10:18]
```

## run function

```r
PAVranking(nPerPar = list(c(3,3,3), c(3,3,3)), facPlc = list(f1name,f2name), 
  nAlloc = 100, parceloutput = 0, leaveout = 0, 
  syntaxA = parmodelA, syntaxB = parmodelB, dataset = simParcel, 
  names = list("p1f1","p2f1","p3f1","p1f2","p2f2","p3f2"))
```

## End(Not run)

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permuteMeasEq  

**Permutation Randomization Tests of Measurement Equivalence and Differential Item Functioning (DIF)**

---

**Description**

The function `permuteMeasEq` provides tests of hypotheses involving measurement equivalence, in one of two frameworks: multigroup CFA or MIMIC models.
Usage

permuteMeasEq(nPermute, modelType = c("mgcfa", "mimic"), con,
uncon = NULL, null = NULL, param = NULL, freeParam = NULL,
covariates = NULL, moreAFIs = NULL, maxSparse = 10,
maxNonconv = 10, showProgress = TRUE, warn = -1, datafun, extra,
parallelType = c("none", "multicore", "snow"), ncpus = NULL,
c1 = NULL, iseed = 12345)

Arguments

nPermute An integer indicating the number of random permutations used to form empirical distributions under the null hypothesis.

modelType A character string indicating type of model employed: multiple-group CFA ("mgcfa") or MIMIC ("mimic").

con The constrained lavaan object, in which the parameters specified in param are constrained to equality across all groups when modelType = "mgcfa", or which regression paths are fixed to zero when modelType = "mimic". In the case of testing configural invariance when modelType = "mgcfa", con is the configural model (implicitly, the unconstrained model is the saturated model, so use the defaults uncon = NULL and param = NULL). When modelType = "mimic", con is the MIMIC model in which the covariate predicts the latent construct(s) but no indicators (unless they have already been identified as DIF items).

uncon Optional. The unconstrained lavaan object, in which the parameters specified in param are freely estimated in all groups. When modelType = "mgcfa", only in the case of testing configural invariance should uncon = NULL. When modelType = "mimic", any non-NULL uncon is silently set to NULL.

null Optional. A lavaan object, in which an alternative null model is fit (besides the default independence model specified by lavaan) for the calculation of incremental fit indices. See Widamin & Thompson (2003) for details. If NULL, lavaan’s default independence model is used.

param An optional character vector or list of character vectors indicating which parameters the user would test for DIF following a rejection of the omnibus null hypothesis tested using (more)AFIs. Note that param does not guarantee certain parameters are constrained in con; that is for the user to specify when fitting the model. If users have any "anchor items" that they would never intend to free across groups (or levels of a covariate), these should be excluded from param; exceptions to a type of parameter can be specified in freeParam. When modelType = "mgcfa", param indicates which parameters of interest are constrained across groups in con and are unconstrained in uncon. Parameter names must match those returned by names(coef(con)), but omitting any group-specific suffixes (e.g., "f1~1" rather than "f1~1.g2") or user-specified labels (that is, the parameter names must follow the rules of lavaan’s model.syntax). Alternatively (or additionally), to test all constraints of a certain type (or multiple types) of parameter in con, param may take any combination of the following values: "loadings", "intercepts", "thresholds", "residuals", "residual.covariances", "means", "lv.variances", and/or "lv.covariances". When modelType = "mimic", param must be a vector of
individual parameters or a list of character strings to be passed one-at-a-time to `lavTestscore(object = con, add = param[i])`, indicating which (sets of) regression paths fixed to zero in con that the user would consider freeing (i.e., exclude anchor items). If modelType = "mimic" and param is a list of character strings, the multivariate test statistic will be saved for each list element instead of 1-df modification indices for each individual parameter, and names(param) will name the rows of the MLE obs slot (see `permuteMeasEq`). Set param = NULL (default) to avoid collecting modification indices for any follow-up tests.

`freeParam` An optional character vector, silently ignored when modelType = "mimic". If param includes a type of parameter (e.g., "loadings"), freeParam indicates exceptions (i.e., anchor items) that the user would not intend to free across groups and should therefore be ignored when calculating p values adjusted for the number of follow-up tests. Parameter types that are already unconstrained across groups in the fitted con model (i.e., a partial invariance model) will automatically be ignored, so they do not need to be specified in freeParam. Parameter names must match those returned by `names(coef(con))`, but omitting any group-specific suffixes (e.g., "f1~1" rather than "f1~1.g2") or user-specified labels (that is, the parameter names must follow the rules of lavaan modelNsyntax).

`covariates` An optional character vector, only applicable when modelType = "mimic". The observed data are partitioned into columns indicated by covariates, and the rows are permuted simultaneously for the entire set before being merged with the remaining data. Thus, the covariance structure is preserved among the covariates, which is necessary when (e.g.) multiple dummy codes are used to represent a discrete covariate or when covariates interact. If covariates = NULL when modelType = "mimic", the value of covariates is inferred by searching param for predictors (i.e., variables appearing after the "~" operator).

`AFIs` A character vector indicating which alternative fit indices (or chi-squared itself) are to be used to test the multiparameter omnibus null hypothesis that the constraints specified in con hold in the population. Any fit measures returned by `fitmeasures` may be specified (including constants like "df", which would be nonsensical). If both AFIs and moreAFIs are NULL, only "chisq" will be returned.

`moreAFIs` Optional. A character vector indicating which (if any) alternative fit indices returned by `morefitindices` are to be used to test the multiparameter omnibus null hypothesis that the constraints specified in con hold in the population.

`maxSparse` Only applicable when modelType = "mgcfa" and at least one indicator is ordered. An integer indicating the maximum number of consecutive times that randomly permuted group assignment can yield a sample in which at least one category (of an ordered indicator) is unobserved in at least one group, such that the same set of parameters cannot be estimated in each group. If such a sample occurs, group assignment is randomly permuted again, repeatedly until a sample is obtained with all categories observed in all groups. If maxSparse is exceeded, NA will be returned for that iteration of the permutation distribution.

`maxNonconv` An integer indicating the maximum number of consecutive times that a random permutation can yield a sample for which the model does not converge on a solution. If such a sample occurs, permutation is attempted repeatedly until
a sample is obtained for which the model does converge. If maxNonconv is exceeded, NA will be returned for that iteration of the permutation distribution, and a warning will be printed when using show or summary.

**showProgress** Logical. Indicating whether to display a progress bar while permuting. Silently set to FALSE when using parallel options.

**warn** Sets the handling of warning messages when fitting model(s) to permuted data sets. See options.

**datafun** An optional function that can be applied to the data (extracted from con) after each permutation, but before fitting the model(s) to each permutation. The datafun function must have an argument named data that accepts a data.frame, and it must return a data.frame containing the same column names. The column order may differ, the values of those columns may differ (so be careful!), and any additional columns will be ignored when fitting the model, but an error will result if any column names required by the model syntax do not appear in the transformed data set. Although available for any modelType, datafun may be useful when using the MIMIC method to test for nonuniform DIF (metric/weak invariance) by using product indicators for a latent factor representing the interaction between a factor and one of the covariates, in which case the product indicators would need to be recalculated after each permutation of the covariates. To access other R objects used within `permuteMeasEq`, the arguments to datafun may also contain any subset of the following: "con", "uncon", "null", "param", "freeParam", "covariates", "AFIs", "moreAFIs", "maxSparse", "maxNonconv", and/or "iseed". The values for those arguments will be the same as the values supplied to `permuteMeasEq`.

**extra** An optional function that can be applied to any (or all) of the fitted lavaan objects (con, uncon, and/or null). This function will also be applied after fitting the model(s) to each permuted data set. To access the R objects used within `permuteMeasEq`, the arguments to extra must be any subset of the following: "con", "uncon", "null", "param", "freeParam", "covariates", "AFIs", "moreAFIs", "maxSparse", "maxNonconv", and/or "iseed". The values for those arguments will be the same as the values supplied to `permuteMeasEq`. The extra function must return a named numeric vector or a named list of scalars (i.e., a list of numeric vectors of length \( \leq 1 \)). Any unnamed elements (e.g., "" or NULL) of the returned object will result in an error.

**parallelType** The type of parallel operation to be used (if any). The default is "none". Forking is not possible on Windows, so if " multicore" is requested on a Windows machine, the request will be changed to "snow" with a message.

**ncpus** Integer: number of processes to be used in parallel operation. If NULL (the default) and parallelType c(" multicore", "snow"), the default is one less than the maximum number of processors detected by detectCores. This default is also silently set if the user specifies more than the number of processors detected.

**cl** An optional parallel or snow cluster for use when parallelType = "snow". If NULL, a "PSOCK" cluster on the local machine is created for the duration of the `permuteMeasEq` call. If a valid makeCluster object is supplied, parallelType is silently set to "snow", and ncpus is silently set to length(cl).

**iseed** Integer: Only used to set the states of the RNG when using parallel options, in which case RNGkind is set to "L'Ecuier-CMRG" with a message. See clusterSetRNGStream
and Section 6 of vignette("parallel", "parallel") for more details. If user supplies an invalid value, iseed is silently set to the default (12345). To set the state of the RNG when not using parallel options, call set.seed before calling permuteMeasEq.

Details

The function permuteMeasEq provides tests of hypotheses involving measurement equivalence, in one of two frameworks:

1. For multiple-group CFA models, provide a pair of nested lavaan objects, the less constrained of which (uncon) freely estimates a set of measurement parameters (e.g., factor loadings, intercepts, or thresholds; specified in param) in all groups, and the more constrained of which (con) constrains those measurement parameters to equality across groups. Group assignment is repeatedly permuted and the models are fit to each permutation, in order to produce an empirical distribution under the null hypothesis of no group differences, both for (a) changes in user-specified fit measures (see AFIs and moreAFIs) and for (b) the maximum modification index among the user-specified equality constraints. Configural invariance can also be tested by providing that fitted lavaan object to con and leaving uncon = NULL, in which case param must be NULL as well.

2. In MIMIC models, one or a set of continuous and/or discrete covariates can be permuted, and a constrained model is fit to each permutation in order to provide a distribution of any fit measures (namely, the maximum modification index among fixed parameters in param) under the null hypothesis of measurement equivalence across levels of those covariates.

In either framework, modification indices for equality constraints or fixed parameters specified in param are calculated from the constrained model (con) using the function lavTestScore.

For multiple-group CFA models, the multiparameter omnibus null hypothesis of measurement equivalence/invariance is that there are no group differences in any measurement parameters (of a particular type). This can be tested using the anova method on nested lavaan objects, as seen in the output of measurementInvariance, or by inspecting the change in alternative fit indices (AFIs) such as the CFI. The permutation randomization method employed by permuteMeasEq generates an empirical distribution of any AFIs under the null hypothesis, so the user is not restricted to using fixed cutoffs proposed by Cheung & Rensvold (2002), Chen (2007), or Meade, Johnson, & Braddy (2008).

If the multiparameter omnibus null hypothesis is rejected, partial invariance can still be established by freeing invalid equality constraints, as long as equality constraints are valid for at least two indicators per factor. Modification indices can be calculated from the constrained model (con), but multiple testing leads to inflation of Type I error rates. The permutation randomization method employed by permuteMeasEq creates a distribution of the maximum modification index if the null hypothesis is true, which allows the user to control the familywise Type I error rate in a manner similar to Tukey's q (studentized range) distribution for the Honestly Significant Difference (HSD) post hoc test.

For MIMIC models, DIF can be tested by comparing modification indices of regression paths to the permutation distribution of the maximum modification index, which controls the familywise Type I error rate. The MIMIC approach could also be applied with multiple-group models, but the grouping variable would not be permuted; rather, the covariates would be permuted separately within each group to preserve between-group differences. So whether parameters are constrained
or unconstrained across groups, the MIMIC approach is only for testing null hypotheses about the
effects of covariates on indicators, controlling for common factors.

In either framework, lavaan's `.label` argument is used to preserve the order of groups seen
in con when permuting the data.

Value

The `permuteMeasEq` object representing the results of testing measurement equivalence (the mul-
tiparameter omnibus test) and DIF (modification indices), as well as diagnostics and any extra
output.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References

Papers about permutation tests of measurement equivalence:

tion methods for testing measurement equivalence and detecting differential item functioning in

measurement invariance testing with ordered-categorical indicators. *Structural Equation Modeling.*
doi:10.1080/10705511.2017.1421467

Jorgensen, T. D. (2017). Applying permutation tests and multivariate modification indices to config-

Additional reading:


Cheung, G. W., & Rensvold, R. B. (2002). Evaluating goodness-of-fit indexes for testing measure-
ment invariance. *Structural Equation Modeling, 9*(2), 233–255. doi:10.1207/S15328007SEM0902_5

doi:10.1037/0021-9010.93.3.568

Widamin, K. F., & Thompson, J. S. (2003). On specifying the null model for incremental fit in-
dices in structural equation modeling. *Psychological Methods, 8*(1), 16–37. doi:10.1037/1082-
989X.8.1.16

See Also

`TukeyHSD, lavTestScore, measurementInvariance, measurementInvarianceCat`
Examples

```r
## Not run:

# Example: Multiple-Group CFA

# Create 3-group data in lavaan example(cfa) data
HS <- lavaan::HolzingerSwinford1939
HS$ageGroup <- ifelse(HS$ageyr < 13, "preteen",
                      ifelse(HS$ageyr > 13, "teen", "thirteen"))

# Specify and fit an appropriate null model for incremental fit indices
mod.null <- c(paste0("x", 1:9, " ~ c(T", 1:9, ", T", 1:9, ", T", 1:9, ", T")*1"),
              paste0("x", 1:9, " ~ c(L", 1:9, ", L", 1:9, ", L", 1:9, ", L")*x", 1:9))
fit.null <- cfa(mod.null, data = HS, group = "ageGroup")

# Fit target model with varying levels of measurement equivalence
mod.config <-
  visual  <- x1 + x2 + x3
  textual <- x4 + x5 + x6
  speed   <- x7 + x8 + x9

miout <- measurementInvariance(mod.config, data = HS, std.lv = TRUE,
                                group = "ageGroup")

(fit.config <- miout["fit.configural"])
(fit.metric <- miout["fit.loadings"])
(fit.scalar <- miout["fit.intercepts"])

# Permutation Method

# Fit indices of interest for multiparameter omnibus test
myAFIs <- c("chisq","cfi","rmsea","mfi","aic")
moreAFIs <- c("gammaHat","adjGammaHat")

# Use only 20 permutations for a demo. In practice,
# use > 1000 to reduce sampling variability of estimated p values

# Test configural invariance
set.seed(12345)
out.config <- permuteMeasEq(nPermute = 20, con = fit.config)
out.config

# Test metric equivalence
set.seed(12345) # Same permutations
out.metric <- permuteMeasEq(nPermute = 20, uncon = fit.config, con = fit.metric,
                            param = "loadings", AFIs = myAFIs,
                            moreAFIs = moreAFIs, null = fit.null)
summary(out.metric, nd = 4)
```
# test scalar equivalence
set.seed(12345) # same permutations
out.scalar <- permuteMeasEq(nPermute = 20, uncon = fit.metric, con = fit.scalar,
                         param = "intercepts", AFIis = myAFIs,
                         moreAFIs = moreAFIs, null = fit.null)

summary(out.scalar)

## Not much to see without significant DIF.
## Try using an absurdly high alpha level for illustration.
outsum <- summary(out.scalar, alpha = .50)

## notice that the returned object is the table of DIF tests
outsum

## visualize permutation distribution
hist(out.config, AFI = "chisq")
hist(out.metric, AFI = "chisq", nd = 2, alpha = .01,
     legendArgs = list(x = "topright"))
hist(out.scalar, AFI = "cfi", printLegend = FALSE)

# Extra Output

## function to calculate expected change of Group-2 and -3 latent means if
## each intercept constraint were released
extra <- function(con) {
  output <- list()
  output["x1.vis2"] <- lavTestScore(con, release = 19:20, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x1.vis3"] <- lavTestScore(con, release = 19:20, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x2.vis2"] <- lavTestScore(con, release = 21:22, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x2.vis3"] <- lavTestScore(con, release = 21:22, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x3.vis2"] <- lavTestScore(con, release = 23:24, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x3.vis3"] <- lavTestScore(con, release = 23:24, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x4.txt2"] <- lavTestScore(con, release = 25:26, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x4.txt3"] <- lavTestScore(con, release = 25:26, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x5.txt2"] <- lavTestScore(con, release = 27:28, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x5.txt3"] <- lavTestScore(con, release = 27:28, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x6.txt2"] <- lavTestScore(con, release = 29:30, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x6.txt3"] <- lavTestScore(con, release = 29:30, univariate = FALSE,
                                    epc = TRUE, warn = FALSE)
  output["x7.spd2"] <- lavTestScore(con, release = 31:32, univariate = FALSE,
permuteMeasEq

```r
epc = TRUE, warn = FALSE)$epc$epc[72]
output["x7.spd3"] <- lavTestScore(con, release = 31:32, univariate = FALSE,
epc = TRUE, warn = FALSE)$epc$epc[108]
output["x8.spd2"] <- lavTestScore(con, release = 33:34, univariate = FALSE,
epc = TRUE, warn = FALSE)$epc$epc[72]
output["x8.spd3"] <- lavTestScore(con, release = 33:34, univariate = FALSE,
epc = TRUE, warn = FALSE)$epc$epc[108]
output["x9.spd2"] <- lavTestScore(con, release = 35:36, univariate = FALSE,
epc = TRUE, warn = FALSE)$epc$epc[72]
output["x9.spd3"] <-lavTestScore(con, release = 35:36, univariate = FALSE,
epc = TRUE, warn = FALSE)$epc$epc[108]
output
}
```

## observed EPC
eextra$fit.scalar)

## permutation results, including extra output
set.seed(12345) # same permutations
out.scalar <- permuteMeasEq(nPermute = 20, uncon = fit.metric, con = fit.scalar,
param = "intercepts", AFIs = myAFIs,
moreAFIs = moreAFIs, null = fit.null, extra = extra)

## summarize extra output
summary(out.scalar, extra = TRUE)

```
##########
# MIMIC ##
##########

## Specify Restricted Factor Analysis (RFA) model, equivalent to MIMIC, but
## the factor covaries with the covariate instead of being regressed on it.
## The covariate defines a single-indicator construct, and the
## double-mean-centered products of the indicators define a latent
## interaction between the factor and the covariate.
mod.mimic <-
visual = x1 + x2 + x3
age = ageyr
age.by.vis = x1.ageyr + x2.ageyr + x3.ageyr

x1 -- x1.ageyr
x2 -- x2.ageyr
x3 -- x3.ageyr

HS.orth <- indProd(var1 = paste0("x", 1:3), var2 = "ageyr", match = FALSE,
data = HS[, c("ageyr", paste0("x", 1:3))])
fit.mimic <- cfa(mod.mimic, data = HS.orth, meanstructure = TRUE)
summary(fit.mimic, stand = TRUE)

## Whereas MIMIC models specify direct effects of the covariate on an indicator,
## DIF can be tested in RFA models by specifying free loadings of an indicator
## on the covariate's construct (uniform DIF, scalar invariance) and the
permuteMeasEq-class

Class for the Results of Permutation Randomization Tests of Measurement Equivalence and DIF

Description

This class contains the results of tests of Measurement Equivalence and Differential Item Functioning (DIF).

Usage

## S4 method for signature 'permuteMeasEq'
show(object)

## S4 method for signature 'permuteMeasEq'
summary(object, alpha = 0.05, nd = 3,
          extra = FALSE)

## S4 method for signature 'permuteMeasEq'
hist(x, ..., AFI, alpha = 0.05, nd = 3,
      printLegend = TRUE, legendArgs = list(x = "topleft"))

### Interaction construct (nonuniform DIF, metric invariance).
param <- as.list(paste0("age + age.by.vis =~ x", 1:3))
names(param) <- paste0("x", 1:3)
# param <- as.list(paste0("x", 1:3, " ~ age + age.by.vis")) # equivalent

## test both parameters simultaneously for each indicator
do.call(rbind, lapply(param, function(x) lavTestScore(fit.mimic, add = x)$test))
## or test each parameter individually
lavTestScore(fit.mimic, add = as.character(param))

########################### Permutation Method

## function to recalculate interaction terms after permuting the covariate
datafun <- function(data) {
  d <- data[, !names(data) %in% paste0("x", 1:3, ".ageyr")]
  indProd(var1 = paste0("x", 1:3), var2 = "ageyr", match = FALSE, data = d)
}

set.seed(12345)
perm.mimic <- permuteMeasEq(nPermute = 20, modelType = "mimic",
                           con = fit.mimic, param = param,
                           covariates = "ageyr", datafun = datafun)

summary(perm.mimic)

## End(Not run)
Arguments

object, x  object of class permuteMeasEq
alpha  alpha level used to draw confidence limits in hist and flag significant statistics in summary output
nd  number of digits to display
extra  logical indicating whether the summary output should return permutation-based p values for each statistic returned by the extra function. If FALSE (default), summary will return permutation-based p values for each modification index.

...  Additional arguments to pass to hist

AFI  character indicating the fit measure whose permutation distribution should be plotted
printLegend  logical. If TRUE (default), a legend will be printed with the histogram
legendArgs  list of arguments passed to the legend function. The default argument is a list placing the legend at the top-left of the figure.

Value

- The show method prints a summary of the multiparameter omnibus test results, using the user-specified AFIs. The parametric (Δ)χ² test is also displayed.
- The summary method prints the same information from the show method, but when extra = FALSE (the default) it also provides a table summarizing any requested follow-up tests of DIF using modification indices in slot MI.obs. The user can also specify an alpha level for flagging modification indices as significant, as well as nd (the number of digits displayed). For each modification index, the p value is displayed using a central χ² distribution with the df shown in that column. Additionally, a p value is displayed using the permutation distribution of the maximum index, which controls the familywise Type I error rate in a manner similar to Tukey’s studentized range test. If any indices are flagged as significant using the tukeyNpNvalue, then a message is displayed for each flagged index. The invisibly returned data.frame is the displayed table of modification indices, unless permuteMeasEq was called with param = NULL, in which case the invisibly returned object is object. If extra = TRUE, the permutation-based p values for each statistic returned by the extra function are displayed and returned in a data.frame instead of the modification indices requested in the param argument.
- The hist method returns a list of length R, containing the arguments for the call to hist and the arguments to the call for legend, respectively. This list may facilitate creating a customized histogram of AFI.dist, MI.dist, or extra.dist.

Slots

PT  A data.frame returned by a call to parTable on the constrained model
modelType  A character indicating the specified modelType in the call to permuteMeasEq
ANOVA  A numeric vector indicating the results of the observed (Δ)χ² test, based on the central χ² distribution
AFI.obs  A vector of observed (changes in) user-selected fit measures
AFI.dist  The permutation distribution(s) of user-selected fit measures. A data.frame with n.Permutations rows and one column for each AFI.obs.
AFI.pval  A vector of p values (one for each element in slot AFI.obs) calculated using slot AFI.dist, indicating the probability of observing a change at least as extreme as AFI.obs if the null hypothesis were true.

MI.obs  A data.frame of observed Lagrange Multipliers (modification indices) associated with the equality constraints or fixed parameters specified in the param argument. This is a subset of the output returned by a call to lavTestScore on the constrained model.

MI.dist  The permutation distribution of the maximum modification index (among those seen in slot MI.obs$X2) at each permutation of group assignment or of covariates.

extra.obs  If permuteMeasEq was called with an extra function, the output when applied to the original data is concatenated into this vector.

extra.dist  A data.frame, each column of which contains the permutation distribution of the corresponding statistic in slot extra.obs.

n.Permutations  An integer indicating the number of permutations requested by the user.

n.Converged  An integer indicating the number of permutation iterations which yielded a converged solution.

n.nonConverged  An integer vector of length n.Permutations indicating how many times group assignment was randomly permuted (at each iteration) before converging on a solution.

n.Sparse  Only relevant with ordered indicators when modelType == "mcgfa". An integer vector of length n.Permutations indicating how many times group assignment was randomly permuted (at each iteration) before obtaining a sample with all categories observed in all groups.

oldSeed  An integer vector storing the value of .Random.seed before running permuteMeasEq. Only relevant when using a parallel/multicore option and the original RNGkind() != "L'Ecuyer-CMRG". This enables users to restore their previous .Random.seed state, if desired, by running: .Random.seed[-1] <- permuteMeasEq(oldSeed).

**Objects from the Class**

Objects can be created via the permuteMeasEq function.

**Author(s)**

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**See Also**

permuteMeasEq

**Examples**

```r
# See the example from the permuteMeasEq function
```
**plotProbe**

*Plot the graphs for probing latent interaction*

**Description**

This function will plot the line graphs representing the simple effect of the independent variable given the values of the moderator.

**Usage**

```
plotProbe(object, xlim, xlab = "Independent Variable",
ylab = "Dependent Variable", legend = TRUE, legendArgs = list(),
...)
```

**Arguments**

- `object` The result of probing latent interaction obtained from `probe2WayMC`, `probe2WayRC`, `probe3WayMC`, or `probe3WayRC` function.
- `xlim` The vector of two numbers: the minimum and maximum values of the independent variable
- `xlab` The label of the x-axis
- `ylab` The label of the y-axis
- `legend` logical. If `TRUE` (default), a legend is printed.
- `legendArgs` list of arguments passed to `legend` function if `legend=TRUE`.
- `...` Any addition argument for the `plot` function

**Value**

None. This function will plot the simple main effect only.

**Author(s)**

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

**See Also**

- `indProd` For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.
- `probe2WayMC` For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- `probe3WayMC` For probing the three-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- `probe2WayRC` For probing the two-way latent interaction when the results are obtained from residual-centering approach.
• **probe3WayRC** For probing the two-way latent interaction when the results are obtained from residual-centering approach.

**Examples**

```r
library(lavaan)

dat2wayMC <- indProd(dat2way, 1:3, 4:6)

model1 <- "
f1 <- x1 + x2 + x3
f2 <- x4 + x5 + x6
f12 <- x1.x4 + x2.x5 + x3.x6
f3 <- x7 + x8 + x9
f3 ~ f1 + f2 + f12
f12 ~~ 0*f1
f12 ~~ 0*f2
x1 ~ 0*x1
x4 ~ 0*x1
x1.x4 ~ 0*x1
x7 ~ 0*x1
f1 ~ NA*x1
f2 ~ NA*x1
f12 ~ NA*x1
f3 ~ NA*x1"

fitMC2way <- sem(model1, data = dat2wayMC, std.lv = FALSE, meanstructure = TRUE)
result2wayMC <- probeWayMC(fitMC2way, c("f1", "f2", "f12"),
                          "f3", c(-1, 0, 1))
plotProbe(result2wayMC, xlim = c(-2, 2))

dat3wayMC <- indProd(dat3way, 1:3, 4:6, 7:9)

model3 <- "
f1 <- x1 + x2 + x3
f2 <- x4 + x5 + x6
f3 <- x7 + x8 + x9
f12 <- x1.x4 + x2.x5 + x3.x6
f13 <- x1.x7 + x2.x8 + x3.x9
f23 <- x4.x7 + x5.x8 + x6.x9
f123 <- x1.x4.x7 + x2.x5.x8 + x3.x6.x9
f4 <- x10 + x11 + x12
f4 ~ f1 + f2 + f3 + f12 + f13 + f23 + f123
f1 ~~ 0*f12
f1 ~~ 0*f13
f1 ~~ 0*f123
f2 ~~ 0*f12
f2 ~~ 0*f23
f2 ~~ 0*f123"
```
```r
f3 ~ 0*f13
f3 ~ 0*f23
f3 ~ 0*f123
f12 ~ 0*f123
f13 ~ 0*f123
f23 ~ 0*f123
x1 ~ 0*x1
x4 ~ 0*x1
x7 ~ 0*x1
x10 ~ 0*x1
x1.x4 ~ 0*x1
x1.x7 ~ 0*x1
x4.x7 ~ 0*x1
x1.x4.x7 ~ 0*x1
f1 ~ NA*x1
f2 ~ NA*x1
f3 ~ NA*x1
f12 ~ NA*x1
f13 ~ NA*x1
f23 ~ NA*x1
f123 ~ NA*x1
f4 ~ NA*x1
```

```r
fitMC3way <- sem(model3, data = dat3wayMC, std.lv = FALSE, meanstructure = TRUE)
result3wayMC <- probe3WayMC(fitMC3way, c("f1", "f2", "f3", "f12", "f13", "f23", "f123"), "f4", c("f1", "f2"), c(-1, 0, 1), c(-1, 0, 1))
plotProbe(result3wayMC, xlim = c(-2, 2))
```

---

### plotRMSEAdist

**Plot the sampling distributions of RMSEA**

**Description**

Plots the sampling distributions of RMSEA based on the noncentral chi-square distributions

**Usage**

```r
plotRMSEAdist(rmse, n, df, ptile = NULL, caption = NULL, rmseascale = TRUE, group = 1)
```

**Arguments**

- `rmsea` The vector of RMSEA values to be plotted
- `n` Sample size of a dataset
- `df` Model degrees of freedom
The percentile rank of the distribution of the first RMSEA that users wish to plot a vertical line in the resulting graph

caption
The name vector of each element of rmsea

rmseaScale
If TRUE, the RMSEA scale is used in the x-axis. If FALSE, the chi-square scale is used in the x-axis.

group
The number of group that is used to calculate RMSEA.

Details
This function creates overlapping plots of the sampling distribution of RMSEA based on noncentral \( \chi^2 \) distribution (MacCallum, Browne, & Sugawara, 1996). First, the noncentrality parameter (\( \lambda \)) is calculated from RMSEA (Steiger, 1998; Dudgeon, 2004) by

\[
\lambda = (N - 1) \frac{d \varepsilon^2}{K},
\]

where \( N \) is sample size, \( d \) is the model degree of freedom, \( K \) is the number of group, and \( \varepsilon \) is the population RMSEA. Next, the noncentral \( \chi^2 \) distribution with a specified \( df \) and noncentrality parameter is plotted. Thus, the x-axis represents the sample \( \chi^2 \) value. The sample \( \chi^2 \) value can be transformed to the sample RMSEA scale (\( \hat{\varepsilon} \)) by

\[
\hat{\varepsilon} = \sqrt{K} \sqrt{\frac{\chi^2 - d}{(N - 1)d}},
\]

where \( \chi^2 \) is the \( \chi^2 \) value obtained from the noncentral \( \chi^2 \) distribution.

Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also
- *plotRMSEApower* to plot the statistical power based on population RMSEA given the sample size
- *findRMSEApower* to find the statistical power based on population RMSEA given a sample size
- *findRMSEAsamplesize* to find the minimum sample size for a given statistical power based on population RMSEA
**plotRMSEApower**

**Examples**

```r
plotRMSEAdist(c(.05, .08), n = 200, df = 20, ptile = .95, rmseaScale = TRUE)
plotRMSEAdist(c(.05, .01), n = 200, df = 20, ptile = .95, rmseaScale = FALSE)
```

---

**plotRMSEApower**  
*Plot power curves for RMSEA*

**Description**

Plots power of RMSEA over a range of sample sizes

**Usage**

```r
plotRMSEApower(rmseA0, rmseaA, df, nlow, nhigh, steps = 1, 
alpha = 0.05, group = 1, ...)
```

**Arguments**

- `rmsea0`: Null RMSEA  
- `rmseaA`: Alternative RMSEA  
- `df`: Model degrees of freedom  
- `nlow`: Lower sample size  
- `nhigh`: Upper sample size  
- `steps`: Increase in sample size for each iteration. Smaller values of steps will lead to more precise plots. However, smaller step sizes means a longer run time.  
- `alpha`: Alpha level used in power calculations  
- `group`: The number of group that is used to calculate RMSEA.  
- `...`: The additional arguments for the plot function.

**Details**

This function creates plot of power for RMSEA against a range of sample sizes. The plot places sample size on the horizontal axis and power on the vertical axis. The user should indicate the lower and upper values for sample size and the sample size between each estimate ("step size") We strongly urge the user to read the sources below (see References) before proceeding. A web version of this function is available at: [http://quantpsy.org/rmseaplot.htm](http://quantpsy.org/rmseaplot.htm).

**Value**

Plot of power for RMSEA against a range of sample sizes
plotRMSEApower

Author(s)

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Donna L. Coffman (Pennsylvania State University; <dlc30@psu.edu>)

References


See Also

- `plotRMSEAdist` to visualize the RMSEA distributions
- `findRMSEApower` to find the statistical power based on population RMSEA given a sample size
- `findRMSEAsamplesize` to find the minimum sample size for a given statistical power based on population RMSEA

Examples

```r
plotRMSEApower(rmsea0 = .025, rmseaA = .075, df = 23, nlow = 100, nhigh = 500, steps = 10)
```
**plotRMSEApowernested**  
*Plot power of nested model RMSEA*

**Description**
Plot power of nested model RMSEA over a range of possible sample sizes.

**Usage**
```
plotRMSEApowernested(rmsea0A = NULL, rmsea0B = NULL, rmsea1A, rmsea1B = NULL, dfA, dfB, nlow, nhigh, steps = 1, alpha = 0.05, group = 1, ...)
```

**Arguments**
- `rmsea0A` The $H_0$ baseline RMSEA
- `rmsea0B` The $H_0$ alternative RMSEA (trivial misfit)
- `rmsea1A` The $H_1$ baseline RMSEA
- `rmsea1B` The $H_1$ alternative RMSEA (target misfit to be rejected)
- `dfA` degree of freedom of the more-restricted model
- `dfB` degree of freedom of the less-restricted model
- `nlow` Lower bound of sample size
- `nhigh` Upper bound of sample size
- `steps` Step size
- `alpha` The alpha level
- `group` The number of group in calculating RMSEA
- `...` The additional arguments for the plot function.

**Author(s)**
- Bell Clinton
- Pavel Panko (Texas Tech University; <pavel.panko@ttu.edu>)
- Sunthud Pornprasertmanit (<psunthud@gmail.com>)

**References**
poolMAloc

Pooled estimates and standard errors across M parcel-allocations:
Combining sampling variability and parcel-allocation variability.

Description

This function employs an iterative algorithm to pick the number of random item-to-parcel allocations needed to meet user-defined stability criteria for a fitted structural equation model (SEM) (see "Details" below for more information). Pooled parameter and standard error estimates from this SEM can be outputted at this final selected number of allocations. Additionally, new indices (see Sterba & Rights, 2016) are outputted for assessing the relative contributions of parcel-allocation variability vs. sampling variability in each estimate. At each iteration, this function generates a given number of random item-to-parcel allocations using a modified version of the parcelAllocation function (Quick & Schoemann, 2012), fits a SEM to each allocation, pools results across allocations from that iteration, and then assesses whether stopping criteria are met. If stopping criteria are not met, the algorithm increments the number of allocations used (generating all new allocations).

Usage

poolMAloc(nPerPar, facPlc, nAllocStart, nAllocAdd = 0, parceloutput = NULL, syntax, dataset, stopProp, stopValue, selectParam = NULL, indices = "default", double = FALSE, checkConv = FALSE, names = "default", leaveout = 0, useTotalAlloc = FALSE, ...)

Arguments

nPerPar A list in which each element is a vector, corresponding to each factor, indicating sizes of parcels. If variables are left out of parceling, they should not be accounted for here (i.e., there should not be parcels of size "1").
facPlc A list of vectors, each corresponding to a factor, specifying the item indicators of that factor (whether included in parceling or not). Either variable names or column numbers. Variables not listed will not be modeled or included in output datasets.

nAllocStart The number of random allocations of items to parcels to generate in the first iteration of the algorithm.

nAllocAdd The number of allocations to add with each iteration of the algorithm. Note that if only one iteration is desired, nAllocAdd can be set to 0 and results will be output for nAllocStart allocations only.

parceloutput Optional character. Path (folder/directory) where M (the final selected number of allocations) parceled data sets will be outputted from the iteration where the algorithm met stopping criteria. Note for Windows users: file path must be specified using forward slashes (/), not backslashes (\). See path.expand for details. If NULL (default), nothing is saved to disk.

syntax lavaan syntax that defines the model.

dataset Item-level dataset

stopProp Value used in defining stopping criteria of the algorithm (\(\delta_a\) in Sterba & Rights, 2016). This is the minimum proportion of change (in any pooled parameter or pooled standard error estimate listed in selectParam) that is allowable from one iteration of the algorithm to the next. That is, change in pooled estimates and pooled standard errors from one iteration to the next must all be less than (stopProp) x (value from former iteration). Note that stopValue can override this criterion (see below). Also note that values less than .01 are unlikely to lead to more substantively meaningful precision. Also note that if only stopValue is a desired criterion, stopProp can be set to 0.

stopValue Value used in defining stopping criteria of the algorithm (\(\delta_b\) in Sterba & Rights, 2016). stopValue is a minimum allowable amount of absolute change (in any pooled parameter or pooled standard error estimate listed in selectParam) from one iteration of the algorithm to the next. For a given pooled estimate or pooled standard error, stopValue is only invoked as a stopping criteria when the minimum change required by stopProp is less than stopValue. Note that values less than .01 are unlikely to lead to more substantively meaningful precision. Also note that if only stopProp is a desired criterion, stopValue can be set to 0.

selectParam (Optional) A list of the pooled parameters to be used in defining stopping criteria (i.e., stopProp and stopValue). These parameters should appear in the order they are listed in the lavaan syntax. By default, all pooled parameters are used. Note that selectParam should only contain freely-estimated parameters. In one example from Sterba & Rights (2016) selectParam included all free parameters except item intercepts and in another example selectParam included only structural parameters.

indices Optional character vector indicating the names of available fitMeasures to be included in the output. The first and second elements should be a chi-squared test statistic and its associated degrees of freedom, both of which will be added if missing. If "default", the indices will be c("chisq", "df", "cfi", "tli", "rmsea", "srmr"). If a robust test statistic is requested (see lavOptions), c("chisq","df") will
be replaced by c("chisq.scaled","df.scaled"). For the output to include both the naive and robust test statistics, indices should include both, but put the scaled test statistics first, as in indices = c("chisq.scaled", "df.scaled", "chisq", "df")

double (Optional) If set to TRUE, requires stopping criteria (stopProp and stopValue) to be met for all parameters (in selectParam) for two consecutive iterations of the algorithm. By default, this is set to FALSE, meaning stopping criteria need only be met at one iteration of the algorithm.

checkConv (Optional) If set to TRUE, function will output pooled estimates and standard errors from 10 iterations post-convergence.

names (Optional) A character vector containing the names of parceled variables.

leaveout (Optional) A vector of variables to be left out of randomized parceling. Either variable names or column numbers are allowed.

useTotalAlloc (Optional) If set to TRUE, function will output a separate set of results that uses all allocations created by the algorithm, rather than M allocations (see "Allocations needed for stability" below). This distinction is further discussed in Sterba and Rights (2016).

... Additional arguments to be passed to lavaan. See also lavOptions

Details

This is a modified version of parcelAllocation. It implements a new algorithm for choosing the number of allocations (M), (described in Sterba & Rights (2016)), newly pools parameter estimate and standard error results across these M allocations, and produces indices for assessing the relative contributions of parcel-allocation variability vs. sampling variability in each estimate. This function randomly generates a given number (nAllocStart) of item-to-parcel allocations, fits a SEM to each allocation, and then increments the number of allocations used (by nAllocAdd) until the pooled parameter estimates and pooled standard errors fulfill stopping criteria (stopProp and stopValue, defined above). Results from the model that was fit to the M allocations are outputted.

Additionally, this function newly outputs the proportion of allocations with solutions that converged (using a maximum likelihood estimator) as well as the proportion of allocations with solutions that were converged and proper. The converged and proper solutions among the final M allocations are used in computing pooled results. The original parcelAllocation function could not be employed if any allocations yielded nonconverged solutions.

For further details on the benefits of the random allocation of items to parcels, see Sterba (2011) and Sterba & MacCallum (2010).

Additionally, after each iteration of the algorithm, information useful in monitoring the algorithm is outputted. The number of allocations used at that iteration, the proportion of pooled parameter estimates meeting stopping criteria at the previous iteration, the proportion of pooled standard errors meeting stopping criteria at the previous iteration, and the runtime of that iteration are outputted. When stopping criteria are satisfied, the full set of results are outputted.

Value

Estimates A table containing pooled results across M allocations at the iteration where stopping criteria were met. Columns correspond to individual parameter name, pooled estimate, pooled standard error, p-value for a z-test of the parameter,
z-based 95% confidence interval, 

$p$-value for a $t$-test of the parameter (using degrees of freedom described in Sterba & Rights, 2016), and $t$-based 95% confidence interval for the parameter.

**Fit**

A table containing results related to model fit from the $M$ allocations at the iteration where stopping criteria were met. Columns correspond to fit index names, the average of each index across allocations, the standard deviation of each fit index across allocations, the maximum of each fit index across allocations, the minimum of each fit index across allocations, the range of each fit index across allocations, and the percent of the $M$ allocations where the chi-square test of absolute fit was significant.

**Proportion of converged and proper allocations**

A table containing the proportion of the final $M$ allocations that converged (using a maximum likelihood estimator) and the proportion of allocations that converged to proper solutions. Note that pooled estimates, pooled standard errors, and other results are computed using only the converged, proper allocations.

**Allocations needed for stability ($M$)**

The number of allocations ($M$) at which the algorithm’s stopping criteria (defined above) were met.

**Indices used to quantify uncertainty in estimates due to sample vs. allocation variability**

A table containing individual parameter names, an estimate of the proportion of total variance of a pooled parameter estimate that is attributable to parcel-allocation variability (PPAV), and an estimate of the ratio of the between-allocation variance of a pooled parameter estimate to the within-allocation variance (RPAV). See Sterba & Rights (2016) for more detail.

**Total runtime (minutes)**

The total runtime of the function, in minutes. Note that the total runtime will be greater when the specified model encounters convergence problems for some allocations, as is the case with the simParcel dataset used below.

**Author(s)**

Jason D. Rights (Vanderbilt University; <jason.d.rights@vanderbilt.edu>)

The author would also like to credit Corbin Quick and Alexander Schoemann for providing the original parcelAllocation function on which this function is based.

**References**


See Also

parcelAllocation, PAVranking

Examples

```r
## Not run:
## lavaan syntax: A 2 Correlated
## factor CFA model to be fit to parceled data

parmodel <- ' f1 =~ NA*p1f1 + p2f1 + p3f1
  f2 =~ NA*p1f2 + p2f2 + p3f2
  p1f1 ~ 1
  p2f1 ~ 1
  p3f1 ~ 1
  p1f2 ~ 1
  p2f2 ~ 1
  p3f2 ~ 1
  p1f1 ~~ p1f1
  p2f1 ~~ p2f1
  p3f1 ~~ p3f1
  p1f2 ~~ p1f2
  p2f2 ~~ p2f2
  p3f2 ~~ p3f2
  f1 ~~ 1*f1
  f2 ~~ 1*f2
  f1 ~~ f2

## specify items for each factor
f1name <- colnames(simParcel)[1:9]
f2name <- colnames(simParcel)[10:18]

## run function
poolMalloc(nPerPar = list(c(3,3,3), c(3,3,3)),
  facPlc = list(f1name, f2name), nAllocStart = 10, AllocAdd = 10,
  syntax = parmodel, dataset = simParcel, stopProp = .03,
  stopValue = .03, selectParam = c(1:6, 13:18, 21),
  names = list("p1f1","p2f1","p3f1","p1f2","p2f2","p3f2"),
  double = FALSE, useTotalAlloc = FALSE)

## End(Not run)
```

```r
probe2WayMC

Probing two-way interaction on the no-centered or mean-centered latent interaction
```
Description

Probing interaction for simple intercept and simple slope for the no-centered or mean-centered latent two-way interaction

Usage

probe2WayMC(fit, nameX, nameY, modVar, valProbe)

Arguments

- **fit**: The lavaan model object used to evaluate model fit
- **nameX**: The vector of the factor names used as the predictors. The first-order factor will be listed first. The last name must be the name representing the interaction term.
- **nameY**: The name of factor that is used as the dependent variable.
- **modVar**: The name of factor that is used as a moderator. The effect of the other independent factor on each moderator variable value will be probed.
- **valProbe**: The values of the moderator that will be used to probe the effect of the other independent factor.

Details

Before using this function, researchers need to make the products of the indicators between the first-order factors using mean centering (Marsh, Wen, & Hau, 2004). Note that the double-mean centering may not be appropriate for probing interaction if researchers are interested in simple intercepts. The mean or double-mean centering can be done by the `indProd` function. The indicator products can be made for all possible combination or matched-pair approach (Marsh et al., 2004). Next, the hypothesized model with the regression with latent interaction will be used to fit all original indicators and the product terms. See the example for how to fit the product term below. Once the lavaan result is obtained, this function will be used to probe the interaction.

Let that the latent interaction model regressing the dependent variable ($Y$) on the independent variable ($X$) and the moderator ($Z$) be

$$Y = b_0 + b_1X + b_2Z + b_3XZ + r,$$

where $b_0$ is the estimated intercept or the expected value of $Y$ when both $X$ and $Z$ are 0, $b_1$ is the effect of $X$ when $Z$ is 0, $b_2$ is the effect of $Z$ when $X$ is 0, $b_3$ is the interaction effect between $X$ and $Z$, and $r$ is the residual term.

For probing two-way interaction, the simple intercept of the independent variable at each value of the moderator (Aiken & West, 1991; Cohen, Cohen, West, & Aiken, 2003; Preacher, Curran, & Bauer, 2006) can be obtained by

$$b_{0,X=0,Z} = b_0 + b_2Z.$$

The simple slope of the independent variable at each value of the moderator can be obtained by

$$b_{X|Z} = b_1 + b_3Z.$$

The variance of the simple intercept formula is

$$Var\left(b_{0,X=0,Z}\right) = Var\left(b_0\right) + 2ZCov\left(b_0,b_2\right) + Z^2Var\left(b_2\right)$$
where \( \text{Var} \) denotes the variance of a parameter estimate and \( \text{Cov} \) denotes the covariance of two parameter estimates.

The variance of the simple slope formula is

\[
\text{Var} (b_{X|Z}) = \text{Var} (b_1) + 2Z\text{Cov} (b_1, b_3) + Z^2\text{Var} (b_3)
\]

Wald statistic is used for test statistic.

### Value

A list with two elements:

1. **SimpleIntercept**: The intercepts given each value of the moderator. This element will be shown only if the factor intercept is estimated (e.g., not fixed as 0).
2. **SimpleSlope**: The slopes given each value of the moderator.

In each element, the first column represents the values of the moderators specified in the `valProbe` argument. The second column is the simple intercept or simple slope. The third column is the \( SE \) of the simple intercept or simple slope. The fourth column is the Wald (\( z \)) statistic. The fifth column is the \( p \) value testing whether the simple intercepts or slopes are different from 0.

### Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

### References


### See Also

- **indProd** For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.
- **probe3WayMC** For probing the three-way latent interaction when the results are obtained from mean-centering, or double-mean centering.
- **probe2WayMC** For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering.
- **probe2WayRC** For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- **probe3WayRC** For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- **plotProbe** Plot the simple intercepts and slopes of the latent interaction.
**Examples**

```r
library(lavaan)

dat2wayMC <- indProd(dat2way, 1:3, 4:6)

model1 <- "
f1 =~ x1 + x2 + x3
f2 =~ x4 + x5 + x6
f12 =~ x1.x4 + x2.x5 + x3.x6
f3 =~ x7 + x8 + x9
f3 ~ f1 + f2 + f12
f12 =~0*f1
f12 =~ 0*f2
x1 ~ 0*1
x4 ~ 0*1
x1.x4 ~ 0*1
x7 ~ 0*1
f1 ~ NA*1
f2 ~ NA*1
f12 ~ NA*1
f3 ~ NA*1
"

fitMC2way <- sem(model1, data = dat2wayMC, std.lv = FALSE,
meanstructure = TRUE)

summary(fitMC2way)

result2wayMC <- probe2WayMC(fitMC2way, c("f1", "f2", "f12"),
    "f3", "f2", c(-1, 0, 1))

result2wayMC
```

---

**probe2WayRC**  
*Probing two-way interaction on the residual-centered latent interaction*

**Description**

Probing interaction for simple intercept and simple slope for the residual-centered latent two-way interaction (Pornprasertmanit, Schoemann, Geldhof, & Little, submitted)

**Usage**

```r
probe2WayRC(fit, nameX, nameY, modVar, valProbe)
```
Arguments

fit The lavaan model object used to evaluate model fit
nameX The vector of the factor names used as the predictors. The first-order factor will be listed first. The last name must be the name representing the interaction term.
nameY The name of factor that is used as the dependent variable.
modVar The name of factor that is used as a moderator. The effect of the other independent factor on each moderator variable value will be probed.
valProbe The values of the moderator that will be used to probe the effect of the other independent factor.

Details

Before using this function, researchers need to make the products of the indicators between the first-order factors and residualize the products by the original indicators (Lance, 1988; Little, Bovaird, & Widaman, 2006). The process can be automated by the indProd function. Note that the indicator products can be made for all possible combination or matched-pair approach (Marsh et al., 2004). Next, the hypothesized model with the regression with latent interaction will be used to fit all original indicators and the product terms. To use this function the model must be fit with a mean structure. See the example for how to fit the product term below. Once the lavaan result is obtained, this function will be used to probe the interaction.

The probing process on residual-centered latent interaction is based on transforming the residual-centered result into the no-centered result. See Pornprasertmanit, Schoemann, Geldhof, and Little (submitted) for further details. Note that this approach based on a strong assumption that the first-order latent variables are normally distributed. The probing process is applied after the no-centered result (parameter estimates and their covariance matrix among parameter estimates) has been computed. See the probe2WayMC for further details.

Value

A list with two elements:

1. SimpleIntercept: The intercepts given each value of the moderator. This element will be shown only if the factor intercept is estimated (e.g., not fixed as 0).
2. SimpleSlope: The slopes given each value of the moderator.

In each element, the first column represents the values of the moderators specified in the valProbe argument. The second column is the simple intercept or simple slope. The third column is the standard error of the simple intercept or simple slope. The fourth column is the Wald (z) statistic. The fifth column is the p value testing whether the simple intercepts or slopes are different from 0.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
References


See Also

- **indProd** For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.
- **probe2WayMC** For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- **probe3WayMC** For probing the three-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- **probe3WayRC** For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- **plotProbe** Plot the simple intercepts and slopes of the latent interaction.

Examples

```r
library(lavaan)

dat2wayRC <- orthogonalize(dat2way, 1:3, 4:6)

model1 <- "
f1 <- x1 + x2 + x3
f2 <- x4 + x5 + x6
f12 <- x1.x4 + x2.x5 + x3.x6
f3 <- x7 + x8 + x9
f3 ~ f1 + f2 + f12
f12 ~~ 0*f1
f12 ~~ 0*f2
x1 ~ 0*x1
x4 ~ 0*x1
x1.x4 ~ 0*x1
x7 ~ 0*x1
f1 ~ NA*x1
f2 ~ NA*x1
f12 ~ NA*x1
```
\[ f_{3} \sim \text{NAx1} \]

```r
fitRC2way <- sem(model1, data = dat2wayRC, std.lv = FALSE, meanstructure = TRUE)
summary(fitRC2way)
result2wayRC <- probe2WayRC(fitRC2way, c("f1", "f2", "f12"), "f3", "f2", c(-1, 0, 1))
result2wayRC
```

## probe3WayMC

### Probing two-way interaction on the no-centered or mean-centered latent interaction

#### Description
Probing interaction for simple intercept and simple slope for the no-centered or mean-centered latent two-way interaction

#### Usage

```r
probe3WayMC(fit, nameX, nameY, modVar, valProbe1, valProbe2)
```

#### Arguments

- **fit**: The lavaan model object used to evaluate model fit
- **nameX**: The vector of the factor names used as the predictors. The three first-order factors will be listed first. Then the second-order factors will be listed. The last element of the name will represent the three-way interaction. Note that the fourth element must be the interaction between the first and the second variables. The fifth element must be the interaction between the first and the third variables. The sixth element must be the interaction between the second and the third variables.
- **nameY**: The name of factor that is used as the dependent variable.
- **modVar**: The name of two factors that are used as the moderators. The effect of the independent factor on each combination of the moderator variable values will be probed.
- **valProbe1**: The values of the first moderator that will be used to probe the effect of the independent factor.
- **valProbe2**: The values of the second moderator that will be used to probe the effect of the independent factor.
Details

Before using this function, researchers need to make the products of the indicators between the first-order factors using mean centering (Marsh, Wen, & Hau, 2004). Note that the double-mean centering may not be appropriate for probing interaction if researchers are interested in simple intercepts. The mean or double-mean centering can be done by the indProd function. The indicator products can be made for all possible combination or matched-pair approach (Marsh et al., 2004). Next, the hypothesized model with the regression with latent interaction will be used to fit all original indicators and the product terms. See the example for how to fit the product term below. Once the lavaan result is obtained, this function will be used to probe the interaction.

Let that the latent interaction model regressing the dependent variable (Y) on the independent variable (X) and two moderators (Z and W) be

\[ Y = b_0 + b_1 X + b_2 Z + b_3 W + b_4 XZ + b_5 XW + b_6 ZW + b_7 XZW + r, \]

where \( b_0 \) is the estimated intercept or the expected value of \( Y \) when \( X, Z, \) and \( W \) are 0, \( b_1 \) is the effect of \( X \) when \( Z \) and \( W \) are 0, \( b_2 \) is the effect of \( Z \) when \( X \) and \( W \) is 0, \( b_3 \) is the effect of \( W \) when \( X \) and \( Z \) are 0, \( b_4 \) is the interaction effect between \( X \) and \( Z \) when \( W \) is 0, \( b_5 \) is the interaction effect between \( X \) and \( W \) when \( Z \) is 0, \( b_6 \) is the interaction effect between \( Z \) and \( W \) when \( X \) is 0, \( b_7 \) is the three-way interaction effect between \( X, Z, \) and \( W, \) and \( r \) is the residual term.

For probing three-way interaction, the simple intercept of the independent variable at the specific values of the moderators (Aiken & West, 1991) can be obtained by

\[ b_{0 | X=0,Z,W} = b_0 + b_2 Z + b_3 W + b_6 ZW. \]

The simple slope of the independent variable at the specific values of the moderators can be obtained by

\[ b_{X | Z,W} = b_1 + b_3 Z + b_4 W + b_7 ZW. \]

The variance of the simple intercept formula is

\[ \text{Var} (b_{0 | X=0,Z,W}) = \text{Var} (b_0) + Z^2 \text{Var} (b_2) + W^2 \text{Var} (b_3) + Z^2 W^2 \text{Var} (b_6) + 2Z \text{Cov} (b_0,b_2) + 2W \text{Cov} (b_0,b_3) + 2ZW \text{Cov} (b_0,b_6) + ZCov (b_2,b_3) + WCov (b_2,b_6) + ZW Cov (b_3,b_6) + ZW Cov (b_2,b_3) + WZ Cov (b_2,b_3) + ZW Cov (b_2,b_6) + ZW Cov (b_3,b_6) + Z^2 W^2 Cov (b_6,b_6) \]

where \( \text{Var} \) denotes the variance of a parameter estimate and \( \text{Cov} \) denotes the covariance of two parameter estimates.

The variance of the simple slope formula is

\[ \text{Var} (b_{X | Z,W}) = \text{Var} (b_1) + Z^2 \text{Var} (b_4) + W^2 \text{Var} (b_5) + Z^2 W^2 \text{Var} (b_7) + 2Z \text{Cov} (b_1,b_4) + 2W \text{Cov} (b_1,b_5) + 2ZW \text{Cov} (b_1,b_7) + 2ZCov (b_4,b_5) + WCov (b_4,b_7) + ZW Cov (b_4,b_7) + ZW Cov (b_4,b_5) + WZ Cov (b_4,b_5) + ZW Cov (b_4,b_7) + ZW Cov (b_5,b_7) + ZW Cov (b_4,b_5) + ZW Cov (b_4,b_7) + ZW Cov (b_5,b_7) + Z^2 W^2 Cov (b_7,b_7) \]

Wald statistic is used for test statistic.

Value

A list with two elements:

1. SimpleIntercept: The intercepts given each value of the moderator. This element will be shown only if the factor intercept is estimated (e.g., not fixed as 0).
2. SimpleSlope: The slopes given each value of the moderator.

In each element, the first column represents values of the first moderator specified in the valProbe1 argument. The second column represents values of the second moderator specified in the valProbe2 argument. The third column is the simple intercept or simple slope. The fourth column is the standard error of the simple intercept or simple slope. The fifth column is the Wald (z) statistic. The sixth column is the p value testing whether the simple intercepts or slopes are different from 0.
Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References

See Also
- `indProd` For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.
- `probe2WayMC` For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- `probe2WayRC` For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- `probe3WayRC` For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- `plotProbe` Plot the simple intercepts and slopes of the latent interaction.

Examples

```r
library(lavaan)

dat3wayMC <- indProd(dat3way, 1:3, 4:6, 7:9)

model3 <- "
f1 =~ x1 + x2 + x3
f2 =~ x4 + x5 + x6
f3 =~ x7 + x8 + x9
f12 =~ x1.x4 + x2.x5 + x3.x6
f13 =~ x1.x7 + x2.x8 + x3.x9
f23 =~ x4.x7 + x5.x8 + x6.x9
f123 =~ x1.x4.x7 + x2.x5.x8 + x3.x6.x9
f4 =~ x10 + x11 + x12
f4 ~ f1 + f2 + f3 + f12 + f13 + f23 + f123
f1 ~~ 0*f12
f1 ~~ 0*f13
f1 ~~ 0*f123
f2 ~~ 0*f12
f2 ~~ 0*f23
f2 ~~ 0*f123
f3 ~~ 0*f13
f3 ~~ 0*f23
f3 ~~ 0*f123
```
Description

Probing interaction for simple intercept and simple slope for the residual-centered latent three-way interaction (Pornprasertmanit, Schoemann, Geldhof, & Little, submitted)

Usage

probeswayrc(fit, nameX, nameY, modVar, valProbe1, valProbe2)

Arguments

fit The lavaan model object used to evaluate model fit
nameX The vector of the factor names used as the predictors. The three first-order factors will be listed first. Then the second-order factors will be listed. The
last element of the name will represent the three-way interaction. Note that the fourth element must be the interaction between the first and the second variables. The fifth element must be the interaction between the first and the third variables. The sixth element must be the interaction between the second and the third variables.

**nameY**  The name of factor that is used as the dependent variable.

**modVar**  The name of two factors that are used as the moderators. The effect of the independent factor on each combination of the moderator variable values will be probed.

**valProbe1**  The values of the first moderator that will be used to probe the effect of the independent factor.

**valProbe2**  The values of the second moderator that will be used to probe the effect of the independent factor.

**Details**

Before using this function, researchers need to make the products of the indicators between the first-order factors and residualize the products by the original indicators (Lance, 1988; Little, Bovaird, & Widaman, 2006). The process can be automated by the `indProd` function. Note that the indicator products can be made for all possible combination or matched-pair approach (Marsh et al., 2004). Next, the hypothesized model with the regression with latent interaction will be used to fit all original indicators and the product terms (Geldhof, Pornprasertmanit, Schoemann, & Little, in press). To use this function the model must be fit with a mean structure. See the example for how to fit the product term below. Once the lavaan result is obtained, this function will be used to probe the interaction.

The probing process on residual-centered latent interaction is based on transforming the residual-centered result into the no-centered result. See Pornprasertmanit, Schoemann, Geldhof, and Little (submitted) for further details. Note that this approach based on a strong assumption that the first-order latent variables are normally distributed. The probing process is applied after the no-centered result (parameter estimates and their covariance matrix among parameter estimates) has been computed See the `probe3WayMC` for further details.

**Value**

A list with two elements:

1. **SimpleIntercept**: The intercepts given each value of the moderator. This element will be shown only if the factor intercept is estimated (e.g., not fixed as 0).

2. **SimpleSlope**: The slopes given each value of the moderator.

In each element, the first column represents values of the first moderator specified in the `valProbe1` argument. The second column represents values of the second moderator specified in the `valProbe2` argument. The third column is the simple intercept or simple slope. The fourth column is the `SE` of the simple intercept or simple slope. The fifth column is the `Wald (z)` statistic. The sixth column is the `p` value testing whether the simple intercepts or slopes are different from 0.

**Author(s)**

Sunthud Pornprasertmanit (<psunthud@gmail.com>)
References


See Also

- **indProd** For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.
- **probe2WayMC** For probing the two-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- **probe3WayMC** For probing the three-way latent interaction when the results are obtained from mean-centering, or double-mean centering
- **probe2WayRC** For probing the two-way latent interaction when the results are obtained from residual-centering approach.
- **plotProbe** Plot the simple intercepts and slopes of the latent interaction.

Examples

```r
library(lavaan)

dat3wayRC <- orthogonalize(dat3way, 1:3, 4:6, 7:9)

code <- "
  f1 <- x1 + x2 + x3
  f2 <- x4 + x5 + x6
  f3 <- x7 + x8 + x9
  f12 <- x1.x4 + x2.x5 + x3.x6
  f13 <- x1.x7 + x2.x8 + x3.x9
  f23 <- x4.x7 + x5.x8 + x6.x9
  f123 <- x1.x4.x7 + x2.x5.x8 + x3.x6.x9
  f4 <- x10 + x11 + x12
  f4 ~ f1 + f2 + f3 + f12 + f13 + f23 + f123
  f1 ~ 0*f12
  f1 ~ 0*f13
"
The quark function provides researchers with the ability to calculate and include component scores calculated by taking into account the variance in the original dataset and all of the interaction and polynomial effects of the data in the dataset.

Usage

quark(data, id, order = 1, silent = FALSE, ...)
**Arguments**

- **data** The data frame is a required component for quark. In order for quark to process a data frame, it must not contain any factors or text-based variables. All variables must be in numeric format. Identifiers and dates can be left in the data; however, they will need to be identified under the `id` argument.

- **id** Identifiers and dates within the dataset will need to be acknowledged as quark cannot process these. By acknowledging the identifiers and dates as a vector of column numbers or variable names, quark will remove them from the data temporarily to complete its main processes. Among many potential issues of not acknowledging identifiers and dates are issues involved with imputation, product and polynomial effects, and principal component analysis.

- **order** Order is an optional argument provided by quark that can be used when the imputation procedures in mice fail. Under some circumstances, mice cannot calculate missing values due to issues with extreme missingness. Should an error present itself stating a failure due to not having any columns selected, set the argument `order = 2` in order to reorder the imputation method procedure. Otherwise, use the default `order = 1`.

- **silent** If `FALSE`, the details of the quark process are printed.

- **...** additional arguments to pass to `mice`.

**Details**

The quark function calculates these component scores by first filling in the data via means of multiple imputation methods and then expanding the dataset by aggregating the non-overlapping interaction effects between variables by calculating the mean of the interactions and polynomial effects. The multiple imputation methods include one of iterative sampling and group mean substitution and multiple imputation using a polytomous regression algorithm (`mice`). During the expansion process, the dataset is expanded to three times its normal size (in width). The first third of the dataset contains all of the original data post imputation, the second third contains the means of the polynomial effects (squares and cubes), and the final third contains the means of the non-overlapping interaction effects. A full principal component analysis is conducted and the individual components are retained. The subsequent `combinequark` function provides researchers the control in determining how many components to extract and retain. The function returns the dataset as submitted (with missing values) and the component scores as requested for a more accurate multiple imputation in subsequent steps.

**Value**

The output value from using the quark function is a list. It will return a list with 7 components.

- **id columns** Is a vector of the identifier columns entered when running quark.
- **id variables** Is a subset of the dataset that contains the identifiers as acknowledged when running quark.
- **used data** Is a matrix / dataframe of the data provided by user as the basis for quark to process.
- **imputed data** Is a matrix / dataframe of the data after the multiple method imputation process.
Big Matrix  
Is the expanded product and polynomial matrix.

Principal Components
Is the entire dataframe of principal components for the dataset. This dataset will have the same number of rows of the big matrix, but will have 1 less column (as is the case with principal component analyses).

Percent Variance Explained
Is a vector of the percent variance explained with each column of principal components.

Author(s)
Steven R. Chesnut (University of Southern Mississippi; <Steven.Chesnut@usm.edu>)
Danny Squire (Texas Tech University)
Terrence D. Jorgensen (University of Amsterdam)

The PCA code is copied and modified from the FactoMineR package.

References

See Also
combinequark

Examples

set.seed(123321)

dat <- HolzingerSwineford1939[,7:15]
misspat <- matrix(runif(nrow(dat) * 9) < 0.3, nrow(dat))
dat[misspat] <- NA
dat <- cbind(HolzingerSwineford1939[,1:3], dat)
## Not run:
quark.list <- quark(data = dat, id = c(1, 2))

final.data <- combinequark(quark = quark.list, percent = 80)

## Example to rerun quark after imputation failure:
quark.list <- quark(data = dat, id = c(1, 2), order = 2)

## End(Not run)
Calculate reliability values of factors

Description

Calculate reliability values of factors by coefficient omega

Usage

reliability(object)

Arguments

object The lavaan model object provided after running the cfa, sem, growth, or lavaan functions.

Details

The coefficient alpha (Cronbach, 1951) can be calculated by

$$\alpha = \frac{k}{k-1} \left[ 1 - \frac{\sum_{i=1}^{k} \sigma_{ii}}{\sum_{i=1}^{k} \sigma_{ii} + 2 \sum_{i<j} \sigma_{ij}} \right],$$

where \(k\) is the number of items in a factor, \(\sigma_{ii}\) is the item \(i\) observed variances, \(\sigma_{ij}\) is the observed covariance of items \(i\) and \(j\).

The coefficient omega (Bollen, 1980; see also Raykov, 2001) can be calculated by

$$\omega_1 = \frac{\left( \sum_{i=1}^{k} \lambda_i \right)^2 Var(\psi)}{\left( \sum_{i=1}^{k} \lambda_i \right)^2 Var(\psi) + \sum_{i=1}^{k} \theta_{ii} + 2 \sum_{i<j} \theta_{ij}},$$

where \(\lambda_i\) is the factor loading of item \(i\), \(\psi\) is the factor variance, \(\theta_{ii}\) is the variance of measurement errors of item \(i\), and \(\theta_{ij}\) is the covariance of measurement errors from item \(i\) and \(j\).

The second coefficient omega (Bentler, 1972, 2009) can be calculated by

$$\omega_2 = \frac{\left( \sum_{i=1}^{k} \lambda_i \right)^2 Var(\psi)}{1' \hat{\Sigma} 1},$$

where \(\hat{\Sigma}\) is the model-implied covariance matrix, and \(1\) is the \(k\)-dimensional vector of 1. The first and the second coefficients omega will have the same value when the model has simple structure, but different values when there are (for example) cross-loadings or method factors. The first coefficient omega can be viewed as the reliability controlling for the other factors (like \(\eta^2_{partial}\) in ANOVA). The second coefficient omega can be viewed as the unconditional reliability (like \(\eta^2\) in ANOVA).
The third coefficient omega (McDonald, 1999), which is sometimes referred to hierarchical omega, can be calculated by

\[
\omega_3 = \frac{\left(\sum_{i=1}^{k} \lambda_i\right)^2 \text{Var} (\psi)}{1'\Sigma 1},
\]

where \(\Sigma\) is the observed covariance matrix. If the model fits the data well, the third coefficient omega will be similar to the \(\omega_2\). Note that if there is a directional effect in the model, all coefficients omega will use the total factor variances, which is calculated by \(\text{lavInspect}(\text{object, "cov.1v"})\).

In conclusion, \(\omega_1, \omega_2, \text{and } \omega_3\) are different in the denominator. The denominator of the first formula assumes that a model is congeneric factor model where measurement errors are not correlated. The second formula accounts for correlated measurement errors. However, these two formulas assume that the model-implied covariance matrix explains item relationships perfectly. The residuals are subject to sampling error. The third formula uses observed covariance matrix instead of model-implied covariance matrix to calculate the observed total variance. This formula is the most conservative method in calculating coefficient omega.

The average variance extracted (AVE) can be calculated by

\[
\text{AVE} = \frac{1'\text{diag}(\Lambda \Psi \Lambda')} {1'\text{diag}(\hat{\Sigma}) 1},
\]

Note that this formula is modified from Fornell & Larcker (1981) in the case that factor variances are not 1. The proposed formula from Fornell & Larcker (1981) assumes that the factor variances are 1. Note that AVE will not be provided for factors consisting of items with dual loadings. AVE is the property of items but not the property of factors.

Regarding categorical indicators, coefficient alpha and AVE are calculated based on polychoric correlations. The coefficient alpha from this function may be not the same as the standard alpha calculation for categorical items. Researchers may check the \text{alpha} function in the \text{psych} package for the standard coefficient alpha calculation.

Item thresholds are not accounted for. Coefficient omega for categorical items, however, is calculated by accounting for both item covariances and item thresholds using Green and Yang’s (2009, formula 21) approach. Three types of coefficient omega indicate different methods to calculate item total variances. The original formula from Green and Yang is equivalent to \(\omega_3\) in this function. Green and Yang did not propose a method for calculating reliability with a mixture of categorical and continuous indicators, and we are currently unaware of an appropriate method. Therefore, when \text{reliability} detects both categorical and continuous indicators in the model, an error is returned. If the categorical indicators load on a different factor(s) than continuous indicators, then reliability can be calculated separately for those scales by fitting separate models and submitting each to the \text{reliability} function.

Value

Reliability values (coefficient alpha, coefficients omega, average variance extracted) of each factor in each group.
Author(s)

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Yves Rosseel (Ghent University; <Yves.Rosseel@UGent.be>)

References


See Also

`reliabilityL2` for reliability value of a desired second-order factor, `maximalRelia` for the maximal reliability of weighted composite

Examples

```r
library(lavaan)

HS.model <- ' visual =~ x1 + x2 + x3
textual =~ x4 + x5 + x6
speed =~ x7 + x8 + x9 '

fit <- cfa(HS.model, data = HolzingerSwineford1939)
reliability(fit)
```
Calculate the reliability values of a second-order factor

Description

Calculate the reliability values (coefficient omega) of a second-order factor

Usage

reliabilityL2(object, secondFactor)

Arguments

object

The lavaan model object provided after running the cfa, sem, growth, or lavaan functions that has a second-order factor

secondFactor

The name of the second-order factor

Details

The first formula of the coefficient omega (in the reliability) will be mainly used in the calculation. The model-implied covariance matrix of a second-order factor model can be separated into three sources: the second-order factor, the uniqueness of the first-order factor, and the measurement error of indicators:

\[ \hat{\Sigma} = \Lambda B \Phi_2 B' \Lambda' + \Lambda \Psi_u \Lambda' + \Theta, \]

where \( \hat{\Sigma} \) is the model-implied covariance matrix, \( \Lambda \) is the first-order factor loading, \( B \) is the second-order factor loading, \( \Phi_2 \) is the covariance matrix of the second-order factors, \( \Psi_u \) is the covariance matrix of the unique scores from first-order factors, and \( \Theta \) is the covariance matrix of the measurement errors from indicators. Thus, the proportion of the second-order factor explaining the total score, or the coefficient omega at Level 1, can be calculated:

\[ \omega_{L1} = \frac{1' \Lambda B \Phi_2 B' \Lambda' 1}{1' \Lambda B \Phi_2 B' \Lambda' 1 + 1' \Lambda \Psi_u \Lambda' 1 + 1' \Theta 1}, \]

where \( 1 \) is the \( k \)-dimensional vector of 1 and \( k \) is the number of observed variables. When model-implied covariance matrix among first-order factors (\( \Phi_1 \)) can be calculated:

\[ \Phi_1 = B \Phi_2 B' + \Psi_u, \]

Thus, the proportion of the second-order factor explaining the variance at first-order factor level, or the coefficient omega at Level 2, can be calculated:

\[ \omega_{L2} = \frac{1_F' B \Phi_2 B' 1_F}{1_F' B \Phi_2 B' 1_F + 1_F' \Psi_u 1_F}, \]

where \( 1_F \) is the \( F \)-dimensional vector of 1 and \( F \) is the number of first-order factors.
The partial coefficient omega at Level 1, or the proportion of observed variance explained by the second-order factor after partialling the uniqueness from the first-order factor, can be calculated:

$$\omega_{L1} = \frac{1'\Lambda B \Phi B'\Lambda 1}{1'\Lambda B \Phi B'\Lambda 1 + 1'\Theta 1'}$$

Note that if the second-order factor has a direct factor loading on some observed variables, the observed variables will be counted as first-order factors.

Value

Reliability values at Levels 1 and 2 of the second-order factor, as well as the partial reliability value at Level 1

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

See Also

reliability for the reliability of the first-order factors.

Examples

library(lavaan)

HS.model3 <-'visual =~ x1 + x2 + x3
textual =~ x4 + x5 + x6
speed =~ x7 + x8 + x9
higher =~ visual + textual + speed'

fit6 <- cfa(HS.model3, data = HolzingerSwineford1939)
reliability(fit6) # Should provide a warning for the endogenous variables
reliabilityL2(fit6, "higher")

residualCovariate Target indicators by covariates

Description

This function will regress target variables on the covariate and replace the target variables by the residual of the regression analysis. This procedure is useful to control the covariate from the analysis model (Geldhof, Pornprasertmanit, Schoemann, & Little, 2013).

Usage

residualCovariate(data, targetVar, covVar)
Arguments

data The desired data to be transformed.
targetVar Variable names or the position of indicators that users wish to be residual centered (as dependent variables)
covVar Covariate names or the position of the covariates using for residual centering (as independent variables) onto target variables

Value

The data that the target variables replaced by the residuals

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References


See Also

indProd For creating the indicator products with no centering, mean centering, double-mean centering, or residual centering.

Examples

dat <- residualCovariate(attitude, 2:7, 1)

---

runMI  Fit a lavaan Model to Multiple Imputed Data Sets

Description

This function fits a lavaan model to a list of imputed data sets, and can also implement multiple imputation for a single data frame with missing observations, using either the Amelia package or the mice package.
runMI

Usage

runMI(model, data, fun = "lavaan", ..., m, miArgs = list(), miPackage = "Amelia", seed = 12345)

lavaan.mi(model, data, ..., m, miArgs = list(), miPackage = "Amelia", seed = 12345)

cfa.mi(model, data, ..., m, miArgs = list(), miPackage = "Amelia", seed = 12345)

sem.mi(model, data, ..., m, miArgs = list(), miPackage = "Amelia", seed = 12345)

growth.mi(model, data, ..., m, miArgs = list(), miPackage = "Amelia", seed = 12345)

Arguments

model The analysis model can be specified using lavaan model syntax or a parameter table (as returned by parTable).

data A data.frame with missing observations, or a list of imputed data sets (if data are imputed already). If runMI has already been called, then imputed data sets are stored in the @DataList slot, so data can also be a lavaan.mi object from which the same imputed data will be used for additional analyses.

fun character. Name of a specific lavaan function used to fit model to data (i.e., "lavaan", "cfa", "sem", or "growth"). Only required for runMI.

... additional arguments to pass to lavaan or lavaanList. See also lavOptions. Note that lavaanList provides parallel computing options, as well as a FUN argument so the user can extract custom output after the model is fitted to each imputed data set (see Examples). TIP: If a custom FUN is used and parallel = "snow" is requested, the user-supplied function should explicitly call library or use :: for any functions not part of the base distribution.

m integer. Request the number of imputations. Ignored if data is already a list of imputed data sets or a lavaan.mi object.

miArgs Addition arguments for the multiple-imputation function (miPackage). The arguments should be put in a list (see example below). Ignored if data is already a list of imputed data sets or a lavaan.mi object.

miPackage Package to be used for imputation. Currently these functions only support "Amelia" or "mice" for imputation. Ignored if data is already a list of imputed data sets or a lavaan.mi object.

seed integer. Random number seed to be set before imputing the data. Ignored if data is already a list of imputed data sets or a lavaan.mi object.

Value

A lavaan.mi object
Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References


Examples

```r
# Not run:
# impose missing data for example
HSMiss <- HolzingerSwineford1939[, c(paste("x", 1:9, sep = ","),
                               "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

# specify CFA model from lavaan's ?cfa help page
HS.model <- 'visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9',

# impute data within runMI...
out1 <- cfa.mi(HS.model, data = HSMiss, m = 20, seed = 12345,
               miArgs = list(noms = "school"))

# ... or impute missing data first
library(Amelia)
set.seed(12345)
HS.amelia <- amelia(HSMiss, m = 20, noms = "school", p2s = FALSE)
imps <- HS.amelia$imputations
out2 <- cfa.mi(HS.model, data = imps)

# same results (using the same seed results in the same imputations)
cbind(impute.within = coef(out1), impute.first = coef(out2))

summary(out1)
summary(out1, ci = FALSE, fmi = TRUE, add.attributes = FALSE)
summary(out1, ci = FALSE, stand = TRUE, rsq = TRUE)

# model fit. D3 includes information criteria
anova(out1)
# equivalently:
lavTestLRT.mi(out1)
# request D2
anova(out1, test = "D2")
# request fit indices
fitMeasures(out1)
```
## fit multigroup model without invariance constraints

```r
mgfit.config <- cfa.mi(HS.model, data = imps, estimator = "mlm", group = "school")
## add invariance constraints, and use previous fit as "data"
mgfit.metric <- cfa.mi(HS.model, data = mgfit1, estimator = "mlm", group = "school", group.equal = "loadings")
mgfit.scalar <- cfa.mi(HS.model, data = mgfit1, estimator = "mlm", group = "school", group.equal = c("loadings","intercepts"))
```

## compare fit of 2 models to test metric invariance

```r
## (scaled likelihood ratio test)
lavTestLRT.mi(mgfit.metric, h1 = mgfit.config)
## To compare multiple models, you must use anova()
anova(mgfit.config, mgfit.metric, mgfit.scalar)
## or compareFit(), which also includes fit indices for comparison
## (optional: name the models)
compareFit(config = mgfit.config, metric = mgfit.metric, scalar = mgfit.scalar,
argsLRT = list(test = "D2", method = "satorra.bentler.2010"))
```

## correlation residuals to investigate local misfit

```r
resid(mgfit.scalar, type = "cor.bentler")
## modification indices for fixed parameters, to investigate local misfit
modindices.mi(mgfit.scalar)
## or lavTestScore.mi for modification indices about equality constraints
lavTestScore.mi(mgfit.scalar)
```

## Wald test of whether latent means are == (fix 3 means to zero in group 2)

```r
eq.means <- c(.
  .p70. == 0
  .p71. == 0
  .p72. == 0
)
lavTestWald.mi(mgfit.scalar, constraints = eq.means)
```

## ordered-categorical data

```r
data(datCat)
lapply(datCat, class)
## impose missing values
set.seed(123)
for (i in 1:8) datCat[sample(1:nrow(datCat), size = .1*nrow(datCat)), i] <- NA

catout <- cfa.mi("' f = u1 + u2 + u3 + u4 ', data = datCat,
m = 3, seed = 456,
miArgs = list(ords = paste0("u", 1:8), noms = "g"),
FUN = function(fit) {
  list(wrmr = lavaan::fitMeasures(fit, "wrmr"),
    zeroCells = lavaan::lavInspect(fit, "zero.cell.tables"))
})
summary(catout)
```
semTools: Useful Tools for Structural Equation Modeling

Description

The semTools package provides many miscellaneous functions that are useful for statistical analysis involving SEM in R. Many functions extend the functionality of the lavaan package. Some sets of functions in semTools correspond to the same theme. We call such a collection of functions a suite. Our suites include:

- Model Fit Evaluation: moreFitIndices, nullRMSEA, singleParamTest, miPowerFit, and chisqSmallN
- Measurement Invariance: measEq.syntax, partialInvariance, partialInvarianceCat, and permuteMeasEq
- Power Analysis: SSmper, findRMSEApower, plotRMSEApower, plotRMSEAdist, findRMSEAsamplesize, findRMSEApowernested, plotRMSEApowernested, and findRMSEAsamplesizennested
- Missing Data Analysis: auxiliary, runMI, twostage, fmi, bsBootMiss, quark, and combinequark
- Exploratory Factor Analysis (EFA): efa.ekc, efaUnrotate, orthRotate, oblqRotate, and funRotate
- Reliability Estimation: reliability, reliabilityL2, and maximalRelia
- Parcelling: parcelAllocation, PAVranking, and poolMAlloc
- Non-Normality: skew, kurtosis, mardiaSkew, mardiaKurtosis, and mvronnorm

All users of R (or SEM) are invited to submit functions or ideas for functions by contacting the maintainer, Terrence Jorgensen (<tjorgensen314@gmail.com>). Contributors are encouraged to use Roxygen comments to document their contributed code, which is consistent with the rest of semTools. Read the vignette from the roxygen2 package for details: vignette("rd", package = "roxygen2")
simParcel

Simulated Data set to Demonstrate Random Allocations of Parcels

Description
A simulated data set with 2 factors with 9 indicators for each factor

Usage

simParcel

Format
A data.frame with 800 observations of 18 variables.

f1item1 Item 1 loading on factor 1
f1item2 Item 2 loading on factor 1
f1item3 Item 3 loading on factor 1
f1item4 Item 4 loading on factor 1
f1item5 Item 5 loading on factor 1
f1item6 Item 6 loading on factor 1
f1item7 Item 7 loading on factor 1
f1item8 Item 8 loading on factor 1
f1item9 Item 9 loading on factor 1
f2item1 Item 1 loading on factor 2
f2item2 Item 2 loading on factor 2
f2item3 Item 3 loading on factor 2
f2item4 Item 4 loading on factor 2
f2item5 Item 5 loading on factor 2
f2item6 Item 6 loading on factor 2
f2item7 Item 7 loading on factor 2
f2item8 Item 8 loading on factor 2
f2item9 Item 9 loading on factor 2

Source
Data were generated using the simsem package.

Examples

head(simParcel)
Description

In comparing two nested models, $\Delta \chi^2$ test may indicate that two models are different. However, like other omnibus tests, researchers do not know which fixed parameters or constraints make these two models different. This function will help researchers identify the significant parameter.

Usage

```
singleParamTest(model1, model2, return.fit = FALSE,
                 method = "satorra.bentler.2001")
```

Arguments

- `model1`: Model 1.
- `model2`: Model 2. Note that two models must be nested models. Further, the order of parameters in their parameter tables are the same. That is, nested models with different scale identifications may not be able to test by this function.
- `return.fit`: Return the submodels fitted by this function
- `method`: The method used to calculate likelihood ratio test. See `lavTestLRT` for available options

Details

This function first identify the differences between these two models. The model with more free parameters is referred to as parent model and the model with less free parameters is referred to as nested model. Three tests are implemented here:

1. free: The nested model is used as a template. Then, one parameter indicating the differences between two models is free. The new model is compared with the nested model. This process is repeated for all differences between two models.
2. fix: The parent model is used as a template. Then, one parameter indicating the differences between two models is fixed or constrained to be equal to other parameters. The new model is then compared with the parent model. This process is repeated for all differences between two models.
3. mi: No longer available because the test of modification indices is not consistent. For example, if two parameters are equality constrained, the modification index from the first parameter is not equal to the second parameter.

Note that this function does not adjust for the inflated Type I error rate from multiple tests.
Value

If \( \text{return.fit} = \text{FALSE} \), the result tables are provided. \( \chi^2 \) and \( p \) value are provided for all methods. Note that the \( \chi^2 \) is all based on 1 df. Expected parameter changes and their standardized forms are also provided.

If \( \text{return.fit} = \text{TRUE} \), a list with two elements are provided. The first element is the tabular result. The second element is the submodels used in the free and fix methods.

Author(s)

Sunthud Pornprasertmanit (<psunthud@gmail.com>)

Examples

library(lavaan)

# Nested model comparison by hand
HS.model1 <- ' visual =~ x1 + x2 + x3
             textual =~ x4 + x5 + x6'
HS.model2 <- ' visual =~ a*x1 + a*x2 + a*x3
             textual =~ b*x4 + b*x5 + b*x6'

m1 <- cfa(HS.model1, data = HolzingerSwineford1939, std.lv = TRUE,
           estimator = "MLR")
m2 <- cfa(HS.model2, data = HolzingerSwineford1939, std.lv = TRUE,
           estimator = "MLR")
anova(m1, m2)
singleParamTest(m1, m2)

## Nested model comparison from the measurementInvariance function
HW.model <- ' visual =~ x1 + x2 + x3
             textual =~ x4 + x5 + x6
             speed =~ x7 + x8 + x9'

models <- measurementInvariance(model = HW.model, data = HolzingerSwineford1939,
                                  group = "school")
singleParamTest(models[[1]], models[[2]])

## Note that the comparison between weak (Model 2) and scalar invariance
## (Model 3) cannot be done by this function # because the weak invariance
## model fixes factor means as 0 in Group 2 but the strong invariance model
## frees the factor means in Group 2. Users may try to compare
## strong (Model 3) and means invariance models by this function.

---

Finding skewness
Description
Finding skewness \( g_1 \) of an object

Usage
\[
\text{skew(object, population = FALSE)}
\]

Arguments
- object: A vector used to find a skewness
- population: TRUE to compute the parameter formula. FALSE to compute the sample statistic formula.

Details
The skewness computed is \( g_1 \). The parameter skewness \( \gamma_2 \) formula is
\[
\gamma_2 = \frac{\mu_3}{\mu_2^{3/2}},
\]
where \( \mu_i \) denotes the \( i \) order central moment.
The excessive kurtosis formula for sample statistic \( g_2 \) is
\[
g_2 = \frac{k_3}{k_2},
\]
where \( k_i \) are the \( i \) order \( k \)-statistic.
The standard error of the skewness is
\[
\text{Var}(\hat{g}_2) = \frac{6}{N}
\]
where \( N \) is the sample size.

Value
A value of a skewness with a test statistic if the population is specified as FALSE

Author(s)
Sunthud Pornprasertmanit (<psunthud@gmail.com>)

References
splitSample

See Also

- kurtosis Find the univariate excessive kurtosis of a variable
- mardiaSkew Find Mardia’s multivariate skewness of a set of variables
- mardiaKurtosis Find the Mardia’s multivariate kurtosis of a set of variables

Examples

skew(1:5)

splitSample Randomly Split a Data Set into Halves

Description

This function randomly splits a data set into two halves, and saves the resulting data sets to the same folder as the original.

Usage

splitSample(dataset, path = "default", div = 2, type = "default", name = "splitSample")

Arguments

dataset The original data set to be divided. Can be a file path to a *.csv or *.dat file (headers will automatically be detected) or an R object (matrix or dataframe). (Windows users: file path must be specified using FORWARD SLASHES (/) ONLY.)

path File path to folder for output data sets. NOT REQUIRED if dataset is a filename. Specify ONLY if dataset is an R object, or desired output folder is not that of original data set. If path is specified as "object", output data sets will be returned as a list, and not saved to hard drive.

div Number of output data sets. NOT REQUIRED if default, 2 halves.

type Output file format ("dat" or "csv"). NOT REQUIRED unless desired output formatting differs from that of input, or dataset is an R object and csv formatting is desired.

name Output file name. NOT REQUIRED unless desired output name differs from that of input, or input dataset is an R object. (If input is an R object and name is not specified, name will be "splitSample".)
Details

This function randomly orders the rows of a data set, divides the data set into two halves, and saves
the halves to the same folder as the original data set, preserving the original formatting. Data set
type (*.csv or *.dat) and formatting (headers) are automatically detected, and output data sets will
preserve input type and formatting unless specified otherwise. Input can be in the form of a file path
(*.dat or *.csv), or an R object (matrix or dataframe). If input is an R object and path is default,
output data sets will be returned as a list object.

Value

If path = "object", list of output data sets. Otherwise, output will saved to hard drive in the
same format as input.

Author(s)

Corbin Quick (University of Michigan; <corbinq@umich.edu>)

Examples

#### Input is .dat file

```r
#splitSample("C:/Users/Default/Desktop/MYDATA.dat")
```  
#### Output saved to "C:/Users/Default/Desktop/" in .dat format

```r
#### Names are "MYDATA_s1.dat" and "MYDATA_s2.dat"
```  
#### Input is R object

```r
## Split CO2 dataset from the datasets package
library(datasets)
splitMyData <- splitSample(CO2, path = "object")
summary(splitMyData[[1]])
summary(splitMyData[[2]])
```  
#### Output object splitMyData becomes list of output data sets

#### Input is .dat file in "C:/" folder

```r
#splitSample("C:/testdata.dat", path = "C:/Users/Default/Desktop/", type = "csv")
```  
#### Output saved to "C:/Users/Default/Desktop/" in *.csv format

```r
#### Names are "testdata_s1.csv" and "testdata_s2.csv"
```  
#### Input is R object

```r
#splitSample(mydata, path = "C:/Users/Default/Desktop/", name = "splitdata"
```  
#### Output saved to "C:/Users/Default/Desktop/" in *.dat format

```r
#### Names are "splitdata_s1.dat" and "splitdata_s2.dat"
```
SSpower

Description


Usage

SSpower(powerModel, n, nparam, popModel, mu, Sigma, fun = "cfa",
alpha = 0.05, ...)

Arguments

- **powerModel** lavaan model syntax for the model to be analyzed. This syntax should constrain at least one nonzero parameter to 0 (or another number).
- **n** integer. Sample size used in power calculation, or a vector of sample sizes if analyzing a multigroup model. If \( \text{length}(n) < \text{length}(	ext{Sigma}) \) when Sigma is a list, \( n \) will be recycled.
- **nparam** integer. Number of invalid constraints in powerModel.
- **popModel** lavaan model syntax specifying the data-generating model. This syntax should specify values for all nonzero parameters in the model. If \( \text{length}(n) > 1 \), the same population values will be used for each group. Different population values per group can only be specified by utilizing Sigma (and mu).
- **mu** numeric or list. For a single-group model, a vector of population means. For a multigroup model, a list of vectors (one per group). If mu and popModel are missing, mean structure will be excluded from the analysis.
- **Sigma** matrix or list. For a single-group model, a population covariance matrix. For a multigroup model, a list of matrices (one per group). If missing, popModel will be used to generate a model-implied Sigma.
- **fun** character. Name of lavaan function used to fit powerModel (i.e., "cfa", "sem", "growth", or "lavaan").
- **alpha** Type I error rate used to set a criterion for rejecting H0.
- **...** additional arguments to pass to lavaan.

Details

Specify all non-zero parameters in a population model, either by using lavaan syntax (popModel) or by submitting a population covariance matrix (Sigma) and optional mean vector (mu) implied by the population model. Then specify an analysis model that constrains at least one nonzero parameter to an incorrect value. Note the number in the nparam argument.

Author(s)

Alexander M. Schoemann (East Carolina University; <schoemanna@ecu.edu>)
Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

References

Examples

```r
## Specify population values. Note every parameter has a fixed value.
modelP <- '
  f1 = .7*V1 + .7*V2 + .7*V3 + .7*V4
  f2 = .7*V5 + .7*V6 + .7*V7 + .7*V8
  f1 = .3*f2
  f1 = 1*f1
  f2 = 1*f2
  V1 = .51*V1
  V2 = .51*V2
  V3 = .51*V3
  V4 = .51*V4
  V5 = .51*V5
  V6 = .51*V6
  V7 = .51*V7
  V8 = .51*V8
',

## Specify analysis model. Note parameter of interest f1--f2 is fixed to 0.
modelA <- '
  f1 = V1 + V2 + V3 + V4
  f2 = V5 + V6 + V7 + V8
  f1 = 0*f2
',

## Calculate power
SSpower(powerModel = modelA, popModel = modelP, n = 150, nparam = 1,
  std.lv = TRUE)

## Get power for a range of sample sizes
Ns <- seq(100, 500, 40)
Power <- rep(NA, length(Ns))
for(i in 1:length(Ns)) {
  Power[i] <- SSpower(powerModel = modelA, popModel = modelP,
    n = Ns[i], nparam = 1, std.lv = TRUE)
}
plot(x = Ns, y = Power, type = "l", xlab = "Sample Size")

## Specify second population to calculate power for multigroup model
popMoments1 <- fitted(cfa(modelP))
modelP2 <- '
  f1 = .7*V1 + .7*V2 + .7*V3 + .7*V4
  f2 = .7*V5 + .7*V6 + .7*V7 + .7*V8
  f1 = .5*f2    ## higher correlation in Group 2
  f1 = 1*f1
  f2 = 1*f2
  V1 = .51*V1
  V2 = .51*V2
  V3 = .51*V3
  V4 = .51*V4
  V5 = .51*V5
  V6 = .51*V6
```
Tukey's WSD post-hoc test of means for unequal variance and sample size

Description

This function computes Tukey’s WSD post hoc test of means when variances and sample sizes are not equal across groups. It can be used as a post hoc test when comparing latent means in multiple group SEM.

Usage

tukeySEM(m1, m2, var1, var2, n1, n2, ng)

Arguments

- `m1`: Mean of group 1.
- `m2`: Mean of group 2.
- `var1`: Variance of group 1.
- `var2`: Variance of group 2.
- `n1`: Sample size of group 1.
- `n2`: Sample size of group 2.
- `ng`: Total number of groups to be compared (i.e., the number of groups compared in the omnibus test).

Details

After conducting an omnibus test of means across three of more groups, researchers often wish to know which sets of means differ at a particular Type I error rate. Tukey’s WSD test holds the error rate stable across multiple comparisons of means. This function implements an adaptation of Tukey’s WSD test from Maxwell & Delaney (2004), that allows variances and sample sizes to differ across groups.
Value

A vector with three elements:

1. \(q\): The \(q\) statistic
2. \(df\): The degrees of freedom for the \(q\) statistic
3. \(p\): A \(p\) value based on the \(q\) statistic, \(df\), and the total number of groups to be compared

Author(s)

Alexander M. Schoemann (East Carolina University; <schoemanna@ecu.edu>)

References


Examples

```r
## For a case where three groups have been compared:
## Group 1: mean = 3.91, var = 0.46, n = 246
## Group 2: mean = 3.96, var = 0.62, n = 465
## Group 3: mean = 2.94, var = 1.07, n = 64

## compare group 1 and group 2
tukeySEM(3.91, 3.96, 0.46, 0.62, 246, 425, 3)

## compare group 1 and group 3
tukeySEM(3.91, 2.94, 0.46, 1.07, 246, 64, 3)

## compare group 2 and group 3
tukeySEM(3.96, 2.94, 0.62, 1.07, 465, 64, 3)
```

twostage

Fit a lavaan model using 2-Stage Maximum Likelihood (TSML) estimation for missing data.

Description

This function automates 2-Stage Maximum Likelihood (TSML) estimation, optionally with auxiliary variables. Step 1 involves fitting a saturated model to the partially observed data set (to variables in the hypothesized model as well as auxiliary variables related to missingness). Step 2 involves fitting the hypothesized model to the model-implied means and covariance matrix (also called the "EM" means and covariance matrix) as if they were complete data. Step 3 involves correcting the Step-2 standard errors (SEs) and chi-squared statistic to account for additional uncertainty due to missing data (using information from Step 1; see References section for sources with formulas).
Usage
twostage(..., aux, fun, baseline.model = NULL)
lavaan.2stage(..., aux = NULL, baseline.model = NULL)
cfa.2stage(..., aux = NULL, baseline.model = NULL)
sem.2stage(..., aux = NULL, baseline.model = NULL)
growth.2stage(..., aux = NULL, baseline.model = NULL)

Arguments

... Arguments passed to the lavaan function specified in the fun argument. See also lavOptions. At a minimum, the user must supply the first two named arguments to lavaan (i.e., model and data).

aux An optional character vector naming auxiliary variable(s) in data

fun The character string naming the lavaan function used to fit the Step-2 hypothesized model ("cfa", "sem", "growth", or "lavaan").

baseline.model An optional character string, specifying the lavaan model.syntax for a user-specified baseline model. Interested users can use the fitted baseline model to calculate incremental fit indices (e.g., CFI and TLI) using the corrected chi-squared values (see the anova method in twostage). If NULL, the default "independence model" (i.e., freely estimated means and variances, but all covariances constrained to zero) will be specified internally.

Details

All variables (including auxiliary variables) are treated as endogenous variables in the Step-1 saturated model (fixed.x = FALSE), so data are assumed continuous, although not necessarily multivariate normal (dummy-coded auxiliary variables may be included in Step 1, but categorical endogenous variables in the Step-2 hypothesized model are not allowed). To avoid assuming multivariate normality, request se = "robust.huber.white". CAUTION: In addition to setting fixed.x = FALSE and conditional.x = FALSE in lavaan, this function will automatically set meanstructure = TRUE, estimator = "ML", missing = "fiml", and test = "standard". lavaan's se option can only be set to "standard" to assume multivariate normality or to "robust.huber.white" to relax that assumption.

Value

The twostage object contains 3 fitted lavaan models (saturated, target/hypothesized, and baseline) as well as the names of auxiliary variables. None of the individual models provide the correct model results (except the point estimates in the target model are unbiased). Use the methods in twostage to extract corrected SEs and test statistics.

Author(s)

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)
References


See Also

twostage

Examples

```r
## impose missing data for example
HSMiss <- HolzingerSwineford1939[ , c(paste("x", 1:9, sep = ""),
                      "ageyr","agemo","school")]
set.seed(12345)
HSMiss$x5 <- ifelse(HSMiss$x5 <= quantile(HSMiss$x5, .3), NA, HSMiss$x5)
age <- HSMiss$ageyr + HSMiss$agemo/12
HSMiss$x9 <- ifelse(age <= quantile(age, .3), NA, HSMiss$x9)

## specify CFA model from lavaan's ?cfa help page
HS.model <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + x8 + x9

## use ageyr and agemo as auxiliary variables
out <- cfa.2stage(model = HS.model, data = HSMiss, aux = c("ageyr","agemo"))

## two versions of a corrected chi-squared test results are shown
out
## see Savalei & Bentler (2009) and Savalei & Falk (2014) for details

## the summary additionally provides the parameter estimates with corrected
## standard errors, test statistics, and confidence intervals, along with
## any other options that can be passed to parameterEstimates()
summary(out, standardized = TRUE)

## use parameter labels to fit a more constrained model
modc <- ' visual = x1 + x2 + x3
textual = x4 + x5 + x6
speed = x7 + a*x8 + a*x9

outc <- cfa.2stage(model = modc, data = HSMiss, aux = c("ageyr","agemo"))
```
## Description

This class contains the results of 2-Stage Maximum Likelihood (TSML) estimation for missing data. The summary, anova, vcov methods return corrected SEs and test statistics. Other methods are simply wrappers around the corresponding `lavaan` methods.

## Usage

```r
## S4 method for signature 'twostage'
show(object)

## S4 method for signature 'twostage'
summary(object, ...)

## S4 method for signature 'twostage'
anova(object, h1 = NULL, baseline = FALSE)

## S4 method for signature 'twostage'
nobs(object, type = c("ntotal", "ngroups", "n.per.group", "norig", "patterns", "coverage"))

## S4 method for signature 'twostage'
coef(object, type = c("free", "user"))

## S4 method for signature 'twostage'
vcov(object, baseline = FALSE)

## S4 method for signature 'twostage'
fitted.values(object, model = c("target", "saturated", "baseline"), type = "moments", labels = TRUE)

## S4 method for signature 'twostage'
fitted(object, model = c("target", "saturated", "baseline"), type = "moments", labels = TRUE)

## S4 method for signature 'twostage'
residuals(object, type = c("raw", "cor", "pearson"))
```
"normalized", "standardized")

## S4 method for signature 'twostage'
resid(object, type = c("raw", "cor", "normalized", "standardized"))

**Arguments**

- **object**: An object of class `twostage`.
- **...**: arguments passed to `parameterEstimates`.
- **h1**: An object of class `twostage` in which `object` is nested, so that their difference in fit can be tested using `anova` (see **Value** section for details).
- **baseline**: logical indicating whether to return results for the baseline model, rather than the default target (hypothesized) model.
- **type**: The meaning of this argument varies depending on which method it it used for. Find detailed descriptions in the **Value** section under `coef`, `nobs`, and `residuals`.
- **model**: character naming the slot for which to return the model-implied sample moments (see fitted.values description.)
- **labels**: logical indicating whether the model-implied sample moments should have (row/column) labels.

**Value**

- **show**: signature(object = "twostage"): The show function is used to display the results of the anova method, as well as the header of the (uncorrected) target model results.
- **summary**: signature(object = "twostage", ...): The summary function prints the same information from the show method, but also provides (and returns) the output of `parameterEstimates(object@target, ...)` with corrected SEs, test statistics, and confidence intervals. Additional arguments can be passed to `parameterEstimates`, including `fmi = TRUE` to provide an estimate of the fraction of missing information.
- **anova**: signature(object = "twostage", h1 = NULL, baseline = FALSE): The anova function returns the residual-based $\chi^2$ test statistic result, as well as the scaled $\chi^2$ test statistic result, for the model in the target slot, or for the model in the baseline slot if `baseline = TRUE`. The user can also provide a single additional `twostage` object to the `h1` argument, in which case anova returns residual-based and scaled ($\Delta$)$\chi^2$ test results, under the assumption that the models are nested. The models will be automatically sorted according their degrees of freedom.
- **nobs**: signature(object = "twostage", type = c("ntotal", "ngroups", "n.per.group", "norig", "patterns", "coverage"): The nobs function will return the total sample sized used in the analysis by default. Also available are the number of groups or the sample size per group, the original sample size (if any rows were deleted because all variables were missing), the missing data patterns, and the matrix of coverage (diagonal is the
proportion of sample observed on each variable, and off-diagonal is the proportion observed for both of each pair of variables).

c\text{coef} \quad \text{signature(object} = \text{"twostage"}, \text{type} = \text{c("free", "user")}): \text{This is simply a wrapper around the corresponding lavaan method, providing point estimates from the target slot.}

c\text{vcov} \quad \text{signature(object} = \text{"twostage"}, \text{baseline} = \text{FALSE}): \text{Returns the asymptotic covariance matrix of the estimated parameters (corrected for additional uncertainty due to missing data) for the model in the target slot, or for the model in the baseline slot if baseline} = \text{TRUE.}

\text{fitted.values, fitted} \\
\quad \text{signature(object} = \text{"twostage"}, \text{model} = \text{c("target", "saturated", "baseline")}): \text{This is simply a wrapper around the corresponding lavaan method, providing model-implied sample moments from the slot specified in the model argument.}

\text{residuals, resid} \\
\quad \text{signature(object} = \text{"twostage"}, \text{type} = \text{c("raw", "cor", "normalized", "standardized")}): \text{This is simply a wrapper around the corresponding lavaan method, providing residuals of the specified type from the target slot.}

\text{Slots}

- \text{saturated} \quad \text{A fitted lavaan object containing the saturated model results}
- \text{target} \quad \text{A fitted lavaan object containing the target/hypothesized model results}
- \text{baseline} \quad \text{A fitted lavaan object containing the baseline/null model results}
- \text{auxNames} \quad \text{A character string (potentially of length} = \text{0) of any auxiliary variable names, if used}

\text{Objects from the Class}

\text{Objects can be created via the twostage function.}

\text{Author(s)}

Terrence D. Jorgensen (University of Amsterdam; <TJorgensen314@gmail.com>)

\text{See Also}

- \text{twostage}

\text{Examples}

\# See the example from the twostage function
Index

*Topic datasets

dat2way, 17
dat3way, 18
datCat, 19
exLong, 24
simParcell, 145
::, 141

anova, lavaan.mi-method
(lavaan.mi-class), 43
anova, twostage-method(twostage-class), 157
as.character, measEq.syntax-method
(measEq syntax-class), 65
auxiliary, 4, 62, 144

BootMiss, 8, 9
BootMiss-class, 6
bsBootMiss, 7, 7, 144

calculate.D2, 9
cfa, 23, 59, 60
cfa.2stage (twostage), 154
cfa.auxiliary (auxiliary), 4
cfa.mi, 46
cfa.mi (runMI), 140
chisqSmallN, 11, 144
clipboard, 12, 16, 30
clusterSetRNGStream, 100
coeff, lavaan.mi-method
(lavaan mi-class), 43
coeff, twostage-method (twostage-class), 157
combinequark, 14, 133, 134, 144
cmpareFit, 15, 30, 45, 47, 48, 63
cov, 55, 56

dat2way, 17
dat3way, 18
datCat, 19
detectCores, 100
EFA-class, 20
efa.ec, 21, 144
efaUnrotate, 20, 23, 144
exLong, 24

factanal, 23
findRMSEApower, 25, 28, 112, 114, 144
findRMSEApowerNested, 26, 29, 116, 144
findRMSEAsamplesize, 26, 27, 112, 114, 144
findRMSEAsamplesizenested, 27, 28, 116, 144
FitDiff, 12, 13, 16
FitDiff-class, 30
fitMeasures, 5, 13, 15, 30, 44, 45, 85, 99, 117
fitMeasures, lavaan.mi-method
(lavaan mi-class), 43
fitmeasures, lavaan.mi-method
(lavaan mi-class), 43
fitted, lavaan.mi-method
(lavaan mi-class), 43
fitted, twostage-method
(twostage-class), 157
fitted.values, lavaan.mi-method
(lavaan mi-class), 43
fitted.values, twostage-method
(twostage-class), 157
fmi, 31, 144
funRotate, 144
funRotate (orthRotate), 83

GPA, 83
gPFlexible, 83, 84
gPForth, 83, 84
growth.2stage (twostage), 154
growth.auxiliary (auxiliary), 4
growth.mi, 46
growth.mi (runMI), 140

hist, 6, 107

160
INDEX

hist, BootMiss-method (BootMiss-class), 6
hist, permutMeasEq-method (permutMeasEq-class), 106
htm, 33
imposeStart, 35
indProd, 37, 109, 121, 122, 124, 125, 127, 128, 130, 131, 140, 144
kd, 40
kurtosis, 41, 56, 57, 144, 149
lav_func_jacobian_simple, 84
lavaan, 4, 5, 8, 11, 15, 32, 44, 45, 59, 61, 62, 66, 83, 86, 94, 102, 118, 141, 151, 155, 157, 159
lavaan-class, 13
lavaan.2stage (twostage), 154
lavaan.auxiliary (auxiliary), 4
lavaan.mi, 10, 15, 32, 46, 47, 49, 52, 70, 141
lavaan.mi (runMI), 140
lavaan.mi-class, 43
lavaanify, 85
lavaanList, 43, 45, 46, 85, 141
lavCor, 21, 34
lavInspect, 45, 46, 50, 66, 71, 136
lavOptions, 8, 59–62, 66, 94, 117, 118, 141, 155
lavParseModelString, 61
lavTestLRT, 11, 15, 44, 47, 48, 89, 146
lavTestLRT.mi, 10, 15, 44, 45, 47
lavTestScore, 50, 51, 99, 101, 102, 108
lavTestScore.mi, 10, 49
lavTestWald, 53, 90, 91
lavTestWald.mi, 10, 44, 52
legend, 6, 107, 109
loadingFromAlpha, 54
makeCluster, 100
mardiaKurtosis, 42, 55, 57, 144, 149
mardiaSkew, 42, 56, 56, 144, 149
maximalRelia, 57, 137, 144
measEq.syntax, 59, 62, 65, 144
measEq.syntax-class, 65
measurementInvariance, 88, 91, 101, 102
measurementInvarianceCat, 88, 91, 102
mice, 133
miPowerFit, 13, 67, 77, 83, 144
model.syntax, 4, 34, 59, 68, 98, 99, 141, 151, 155
modificationIndices.mi (modindices.mi), 70
modificationindices.mi (modindices.mi), 70
modindices, 45
modindices.mi, 70
monteCarloMed, 73
moreFitIndices, 69, 75, 83, 99, 144
mvnnonnorm, 78, 144
mvnorm, 17, 18
Net, 80
net, 15, 79, 81
Net-class, 81
nobs, lavaan.mi-method (lavaan.mi-class), 43
nobs, twostage-method (twostage-class), 157
nullRMSEA, 76, 77, 82, 144
oblqRotate, 20, 23, 144
oblqRotate (orthRotate), 83
options, 100
orthogonalize, 144
orthogonalize (indProd), 38
orthRotate, 20, 23, 83, 144
p.adjust, 89
parameterEstimates, 44, 45, 158
parcelAllocation, 85, 93, 94, 96, 116, 118, 120, 144
parTable, 4, 59, 107, 141
partialInvariance, 88, 144
partialInvarianceCat, 144
partialInvarianceCat (partialInvariance), 88
path.expand, 117
PAVranking, 86, 93, 120, 144
permuteMeasEq, 97, 99, 102, 107, 108, 144
permuteMeasEq-class, 106
plot, 109
plotProbe, 39, 109, 122, 125, 128, 131, 144
plotRMSEAdist, 26, 28, 111, 114, 144
plotRMSEApower, 26, 28, 112, 113, 144
plotRMSEApowernested, 27, 29, 115, 144
poolMAloc, 86, 96, 116, 144
probe2WayMC, 39, 109, 120, 124, 125, 128, 131, 144
probe2WayRC, 39, 109, 122, 123, 128, 131, 144
probeswayMC, 39, 109, 122, 125, 126, 130, 131, 144
probeswayRC, 39, 109, 110, 122, 125, 128, 129, 144
quark, 14, 15, 132, 144
reliability, 58, 135, 138, 139, 144
reliabilityL2, 137, 138, 144
resid, lavaan.mi-method
(lavaan.mi-class), 43
resid, twostage-method (twostage-class), 157
residualCovariate, 139
residuals, lavaan.mi-method
(lavaan.mi-class), 43
residuals, twostage-method (twostage-class), 157
RNGkind, 100
rotations, 84
runMI, 46, 62, 140, 144
saveFile (clipboard), 12
sem.2stage (twostage), 154
sem.auxiliary (auxiliary), 4
sem.mi, 46
sem.mi (runMI), 140
semTools, 144
semTools-package (semTools), 144
set.seed, 101
show, BootMiss-method (BootMiss-class), 6
show, EFA-method (EFA-class), 20
show, FitDiff-method (FitDiff-class), 30
show, lavaan.mi-method
(lavaan.mi-class), 43
show, measEq.syntax-method
(measEq.syntax-class), 65
show, Net-method (Net-class), 81
show, permuteMeasEq-method
(permuteMeasEq-class), 106
show, twostage-method (twostage-class), 157
simParcel, 119, 145
simulateData, 79
singleParamTest, 144, 146
skew, 42, 56, 57, 144, 147
splitSample, 149
SSpower, 144, 150
summary, BootMiss-method
(BootMiss-class), 6
summary, EFA-method (EFA-class), 20
summary, FitDiff-method (FitDiff-class), 30
summary, lavaan.mi-method
(lavaan.mi-class), 43
summary, measEq.syntax-method
(measEq.syntax-class), 65
summary, Net-method (Net-class), 81
summary, permuteMeasEq-method
(permuteMeasEq-class), 106
summary, twostage-method (twostage-class), 157
TukeyHSD, 102
tukeySEM, 153
twostage, 144, 154, 155, 156, 159
twostage-class, 157
txtProgressBar, 85
update, measEq.syntax-method
(measEq.syntax-class), 65
vcov, lavaan.mi-method
(lavaan.mi-class), 43
vcov, twostage-method (twostage-class), 157
write.table, 8, 13