Package ‘sparseHessianFD’

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Description Estimates Hessian of a scalar-valued function, and returns it
in a sparse Matrix format. The sparsity pattern must be known in advance. The
algorithm is especially efficient for hierarchical models with a large number of

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Estimate sparse Hessians using finite differences of gradients.

Description

Estimate sparse Hessians using finite differences of gradients.

Details

The Hessian is returned as a sparse Matrix (dgCMatrix-class). The user supplies the objective function, the gradient, and the row and column indices of the non-zero elements of the lower triangle of the Hessian (i.e., the sparsity structure must be known in advance).

In a typical case, you should only need to use the sparseHessianFD initializer, and the fn, gr and hessian methods of the sparseHessian class, and the Matrix.to.Coord utility function.

References


**binary**

**Binary choice example**

**Description**

Functions for binary choice example in the vignette.

**Usage**

```r
binary.f(P, data, priors, order.row = FALSE)
binary.grad(P, data, priors, order.row = FALSE)
binary.hess(P, data, priors, order.row = FALSE)
```

**Arguments**

- **P**: Numeric vector of length \((N + 1)k\). First \(Nk\) elements are heterogeneous coefficients. The remaining \(k\) elements are population parameters.
- **data**: Named list of data matrices \(Y\) and \(X\), and choice count integer \(T\)
- **priors**: Named list of matrices \(\text{inv.Omega}\) and \(\text{inv.Sigma}\)
- **order.row**: Determines order of heterogeneous coefficients in parameter vector. If TRUE, heterogeneous coefficients are ordered by unit. If FALSE, they are ordered by covariate.

**Details**

These functions are used by the heterogeneous binary choice example in the vignette. There are \(N\) heterogeneous units, each making \(T\) binary choices. The choice probabilities depend on \(k\) covariates.

**Value**

Log posterior density, gradient and Hessian. The Hessian is a \(\text{dgCMatrix}\) object.

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**binary-data**

*Sample simulated data for binary choice example in vignette*

**Description**

Sample datasets for vignette
Details

The package provides four sample datasets for the hierarchical binary choice model described in the vignette. These datasets are:

- **binary**  \( N = 50, k = 3 \)
- **binary_small**  \( N = 20, k = 2 \)
- **binary_large**  \( N = 800, k = 3 \)
- **binary_super**  \( N = 1200, k = 3 \)

\( N \) is the number of heterogeneous units. \( k \) is the number of covariates.

The datasets were generated using the code in data-raw/binary_sim.R.

coloring

### Description

Triangular partitioning of variables

coloring(L)

Usage

coloring(L)

Arguments

- \( L \) sparsity pattern of the Hessian as a lower triangular pattern matrix

Details

For internal use. Exported in order for replication files for JSS article to run.

Value

Integer vector of length nvars with color assignments for each variable.
Coord.to.Pointers

Convert a matrix defined by row and column indices to one defined by a row- or column-oriented compression scheme.

Description

Returns indices and pointers that define a sparse Hessian in compressed format. Inputs are the row and column indices.

Usage

Coord.to.Pointers(
  rows,
  cols,
  dims,
  triangle = TRUE,
  lower = TRUE,
  symmetric = FALSE,
  order = c("column", "row", "triplet"),
  index1 = TRUE
)

Arguments

- **rows, cols**: row and column indices of non-zero elements
- **dims**: 2-element vector for number of rows and columns.
- **triangle**: Is input intended to be a triangular (TRUE) or full (FALSE) matrix. See details for how this argument is interpreted for different values of order.
- **lower**: If triangular is true, this argument identifies the input matrix as lower- or upper-triangular. This argument is ignored if triangle is FALSE.
- **symmetric**: If TRUE, and matrix is triangular, then the matrix will be treated as symmetric, with only the triangular elements provided. If matrix is neither triangular nor symmetric, then symmetric=TRUE will probably trigger an error.
- **order**: Determines the indexing/compression scheme for the output matrix. Use "triplet" to get row and column indices. Defaults to the same class as M.
- **index1**: TRUE if using 1-based indexing. FALSE for 0-based indexing.

Details

- **triangle** and **order** have the following interpretation:
  
  **triangle=TRUE**  Input rows and cols represent lower or upper triangle of a matrix. If order="symmetric", then the output list will be for a full, symmetric matrix. Otherwise, the output list will be for only the lower or upper triangle. Any elements outside of the specified triangle will trigger an error.
**deprecated**

**triangle**=FALSE  Input rows and cols represent a full matrix. If that matrix is not symmetric, then order="symmetric" will trigger an error. If symmetric=FALSE and order='triplet', the output list should contain the same row and column indices as the input list.

**Value**

A list. See Matrix.to.Pointers (no values are included in return list).

**See Also**

Matrix.to.Pointers

---

**Description**

These functions were in earlier versions, but will no longer be maintained, and are not even guaranteed to work now.

Build sparse matrix from data in CSC (column compressed) format.

Converts row and column indices to a pattern Matrix object of Matrix class

This function is deprecated. Use sparseHessianFD instead.

**Usage**

Sym.CSC.to.Matrix(H, nvars)

Coord.to.Sym.Pattern.Matrix(H, nvars)

Coord.to.Pattern.Matrix(
  rows,
  cols,
  dims,
  compressed = TRUE,
  symmetric = FALSE,
  index1 = TRUE
)

new.sparse.hessian.obj(
  x,
  fn,
  gr,
  hs,
  fd.method = 0L,
  eps = sqrt(.Machine$double.eps),
  ...
)
sparseHessianFD.new(
    x,
    fn,
    gr,
    rows,
    cols,
    direct = NULL,
    eps = sqrt(.Machine$double.eps),
    ...
)

Arguments

H     a list containing Hessian data. See details.
nvars the number of rows (and columns) in the matrix.
rows, cols row and column indices of non-zero elements
dims   2-element vector for number of rows and columns in matrix
compressed If TRUE, returns a matrix is compressed column (default=TRUE)
symmetric If TRUE, matrix will be symmetric, and only the lower triangular elements need
to be provided (default=FALSE)
index1 TRUE if input row and col use 1-based indexing, and FALSE for 0-based index-
ing.
x     variable vector for initialization
fn    R function that returns function value
gr    R function that returns the gradient of the function
hs    list of two vectors: row and column indices of non-zero elements of lower trian-
gle of Hessian. See details.
fd.method If TRUE, use direct method for computatation. Otherwise, use indirect/substitution
          method. See references.
eps   The perturbation amount for finite differencing of the gradient to compute the
       Hessian. Defaults to sqrt(.Machine$double.eps).
...   Other parameters to be passed to fn and gr.
direct If TRUE, use direct method for computatation. Otherwise, use indirect/substitution
        method. See references.

Details

Use Matrix::sparseMatrix instead of Sym.CSC.to.Matrix.
This function is useful to prototype a sparsity pattern. No assumptions are made about symmetry.
hs is a list of two elements:
**iRow**  Integer vector of row indices of non-zero elements in lower triangle of Hessian.

**jCol**  Integer vector of column indices of non-zero elements in lower triangle of Hessian.

This function is deprecated. Use `sparseHessianFD` instead.

**Value**

An object of Matrix class.

A sparse pattern matrix

An object of class `sparseHessianFD`

---

**get_colors**  *Vertex coloring of a sparse undirected graph*

**Description**

Generate proper vertex coloring of a sparse undirected graph.

**Usage**

```
get_colors(pntr, idx, nvars)
```

**Arguments**

- **pntr, idx**  row pointers and column indices of the adjacency matrix, in compressed column-oriented format. Must use zero-based indexing.
- **nvars**  Number of vertices.

**Details**

For internal use. You should not have to call this function directly.

**Value**

An integer vector of length `nvars`, where each element represents the color of the corresponding vertex. Indices are zero-based.
Matrix.to.Coord

Row and column indices from sparse matrix.

Description

Utility function to extract row and column indices of the non-zero elements of a sparse matrix.

Usage

Matrix.to.Coord(M, index1 = TRUE)

Arguments

M
A matrix that is a subclass of sparseMatrix, as defined in the Matrix package.

index1
TRUE if the index of the first element should be 1, and FALSE if 0.

Details

A wrapper to Matrix.to.Pointers for order='triplet' and values=FALSE, for extracting the row and column indices of a sparsity pattern from a matrix that has that same pattern.

Value

A list with two named elements.

rows Integer vector containing row indices of non-zero elements

cols Integer vector containing column indices of non-zero elements

Examples

M1 <- as(kronecker(diag(3), matrix(TRUE,2,2)),"sparseMatrix")
C <- Matrix.to.Coord(M1)
M2 <- Matrix::sparseMatrix(i=C$rows, j=C$cols)
all.equal(M1,M2)

Matrix.to.Pointers

Extract row and column indices, pointers and values from a sparse matrix.

Description

Returns a list of row indices, column indices, pointers, and/or values of a sparse Hessian.
Matrix.to.Pointers

Usage

Matrix.to.Pointers(
  M,
  as.symmetric = Matrix::isSymmetric(M),
  values = !is(M, "nMatrix"),
  order = NULL,
  index1 = TRUE
)

Arguments

M A sparse Matrix, as defined in the Matrix package.

as.symmetric Defaults to isSymmetric(M). If M is symmetric, and as.symmetric is FALSE, then index/pointer elements in the output list will be labeled according to order. If M is not symmetric, and as.symmetric is TRUE, then an error will be triggered.

values If TRUE, values are returned in list as 'x'. Defaults to TRUE for numeric and logical matrices, and FALSE for pattern matrices. If M is a pattern matrix, values=TRUE will trigger a warning.

order Determines the indexing/compression scheme for the output matrix. Use 'triplet' to get row and column indices. Defaults to the same class as M.

index1 TRUE (default) if return indices and pointers should use 1-based indexing. FALSE for 0-based indexing.

Details

This function is included primarily for debugging purposes. It is used internally, but would not ordinarily be called by an end user.

Value

A list with the following elements. If order==`row`,

- jCol Integer vector containing column indices of non-zero elements
- ipntr Integer vector containing pointers to elements of jCol at which the next row begins.

If order==`column`

- iRow Integer vector containing row indices of non-zero elements
- jpntr Integer vector containing pointers to elements of iRow at which the next column begins.

If order==`triplet`

- rows Row indices of non-zero elements
- cols Column indices of non-zero elements

If as.symmetric is TRUE, then the row/column orientation does not matter.

- idx Integer vector containing indices of non-zero elements
sparseHessiadFD

`pntr` Integer vector containing pointers to elements of idx at which the next row or column begins.

If values=TRUE, the return list includes x, the values of the non-zero elements. The ‘class’ element is the name of the sparse matrix class to which the output corresponds (identifies numeric type, pattern, and indexing/compression scheme).

See Also

Matrix.to.Coord

---

**Description**

A reference class for computing sparse Hessians

**Details**

The sparseHessiadFD function calls the initializer for the sparseHessiadFD class, and returns a sparseHessiadFD object.

`sparseHessiadFD(x, fn, gr, rows, cols, delta, index1, complex, ...)`

The function, gradient and sparsity pattern are declared as part of the initialization.

Once initialized, the $hessian method will evaluate the Hessian at x.

`obj <- sparseHessian(x, fn, gr, rows, cols, ...)`

`obj$hessian(x)`

For convenience, the class provides wrapper methods to the fn and gr functions that were specified in the initializer.

`obj$fn(P) ## wrapper to objective function`
`obj$gr(P) ## wrapper to gradient`
`obj$fngr(P) ## list of obj function and gradient`
`obj$fngrhs(P) ## list of obj function, gradient and Hessian`

**Arguments to initializer:**

- `x` an vector at which the function, gradient and Hessian are initialized and tested.
- `fn, gr` R functions that return the function value and gradient, evaluated at x.
- `rows, cols` Numeric vectors with row and column indices of the non-zero elements in the lower triangle (including diagonal) of the Hessian.
- `delta` The perturbation amount for finite difference (or complex step) of the gradient to compute the Hessian. Defaults to 1e-07.
- `index1` TRUE if rows and cols use 1-based (R format) indexing (FALSE for 0-based (C format) indexing.)
complex TRUE if Hessian will be computed using the complex step method, and FALSE (default) if using finite differences. If TRUE, both fn and gr must accept complex arguments and return complex values.

... other arguments to be passed to fn and gr.

Other methods are described below. Do not access any of the fields directly. The internal structure is subject to change in future versions.

Fields

fn1 A closure for calling fn(x, ...).
gr1 A closure for calling gr(x, ...).
iRow, jCol Numeric vectors with row and column indices of the non-zero elements in the lower triangle (including diagonal) of the Hessian.
delta The perturbation amount for finite differencing of the gradient to compute the Hessian. Defaults to 1e-07.
index1 TRUE if rows and cols use 1-based (R format) indexing (FALSE for 0-based (C format) indexing.
complex TRUE if Hessian will be computed using the complex step method, and FALSE (default) if using finite differences.
D raw finite differences (internal use only)
nvars Number of variables (length of x)
nnz Number of non-zero elements in the lower triangle of the Hessian.
ready TRUE if object has been initialized, and Hessian has been partitioned.
idx, pntr Column indices and row pointers for non-zero elements in lower triangle of the permuted Hessian. Row-oriented compressed storage.
colors A vector representation of the partitioning of the columns. There are nvars elements, one for each column of the permuted Hessian. The value corresponds to the "color" for that column.
perm, invperm Permutation vector and its inverse

Methods

fn(x) Return function value, evaluated at x: fn(x, ...)
fngr(x) Return list of function value and gradient, evaluated at x
fngrhs(x) Return list of function value, gradient, and Hessian, evaluated at x
get_invperm() Return integer vector of inverse of permutation used for computing Hessian
get_nnz() Return number of non-zero elements in lower triangle of Hessian
get_nvars() Return dimension (number of rows or columns) of Hessian
get_pattern() Return pattern matrix of lower triangle of Hessian
get_perm() Return integer vector of permutation used for computing Hessian
get_perm_pattern() Return pattern matrix of lower triangle of *permuted* Hessian
Estimate sparse Hessian

Estimate Hessian using triangular subsitution algorithm

Usage

```r
subst(Y, colors, jCol, ipntr, delta, nvars, nnz)
```
Arguments

- **Y**: Matrix of finite differences of gradients.
- **colors**: Vector of length nvars that identifies color of each variable.
- **jCol, ipntr**: Column indices and row pointers for non-zero elements of lower triangle of Hessian (row-oriented compressed format).
- **delta**: Perturbation factor used to compute finite differences of gradients.
- **nvars**: Dimension of Hessian (number of variables).
- **nnz**: Number of non-zero elements in the lower triangle of the Hessian.

Details

For internal use. You should not have to call this function directly.

Value

A sparse Hessian of class dgCMatrix.
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