Package ‘stable’

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Stable Distribution

Description

These functions provide information about the stable distribution with the location, the dispersion, the skewness and the tail thickness respectively modelled by the parameters \( \text{loc} \), \( \text{disp} \), \( \text{skew} \) and \( \text{tail} \).

Usage

- \( \text{dstable}(x, \text{loc} = 0, \text{disp} = 1/\sqrt{2}, \text{skew} = 0, \text{tail} = 2, \text{npt} = 501, \text{up} = 10, \text{eps} = 1e-06, \text{integration} = "\text{Romberg}") \)
- \( \text{pstable}(q, \text{loc} = 0, \text{disp} = 1/\sqrt{2}, \text{skew} = 0, \text{tail} = 2, \text{eps} = 1e-06) \)
- \( \text{qstable}(p, \text{loc} = 0, \text{disp} = 1/\sqrt{2}, \text{skew} = 0, \text{tail} = 2, \text{eps} = 1e-06) \)
- \( \text{rstable}(n = 1, \text{loc} = 0, \text{disp} = 1/\sqrt{2}, \text{skew} = 0, \text{tail} = 2, \text{eps} = 1e-06) \)
- \( \text{hstable}(x, \text{loc} = 0, \text{disp} = 1/\sqrt{2}, \text{skew} = 0, \text{tail} = 2, \text{eps} = 1e-06) \)

Arguments

- \( x, q \): vector of quantiles.
- \( \text{loc} \): vector of (real) location parameters.
- \( \text{disp} \): vector of (positive) dispersion parameters.
- \( \text{skew} \): vector of skewness parameters (in \([-1,1]\)).
- \( \text{tail} \): vector of parameters (in \([0,2]\)) related to the tail thickness.
- \( \text{npt}, \text{up}, \text{integration} \): As detailed herein – only available when using \( \text{dstable} \).
- \( \text{eps} \): scalar giving the required precision in computation.
- \( p \): vector of probabilities.
- \( n \): number of observations.
Details

dstable, pstable, qstable and hstable compute the density, the distribution, the quantile and the hazard functions of a stable variate. rstable generates random deviates with the prescribed stable distribution.

loc is a location parameter in the same way as the mean in the normal distribution: it can take any real value.

disp is a dispersion parameter in the same way as the standard deviation in the normal distribution: it can take any positive value.

skew is a skewness parameter: it can take any value in \((-1, 1)\). The distribution is right-skewed, symmetric and left-skewed when skew is negative, null or positive respectively.

tail is a tail parameter (often named the characteristic exponent): it can take any value in \((0, 2)\) (with tail=1 and tail=2 yielding the Cauchy and the normal distributions respectively when symmetry holds).

If loc, disp, skew, or tail are not specified they assume the default values of 0, \(1/sqrt(2)\), 0 and 2 respectively. This corresponds to a normal variate with mean= 0 and variance= \(1/2\)disp\(^2\).

The stable characteristic function is given by

\[ greekphi(t) = ilocat - disp[t^{tail}[1 + iskewsign(t)greekomega(t,tail)] \]

where

\[ greekomega(t, tail) = \frac{2}{\pi} LOG(ABS(t)) \]

when tail=1, and

\[ greekomega(t, tail) = tan(\frac{\pi tail}{2}) \]

otherwise.

The characteristic function is inverted using Fourier’s transform to obtain the corresponding stable density. This inversion requires the numerical evaluation of an integral from 0 to \(\infty\). Two algorithms are proposed for this. The default is Romberg’s method (integration=”Romberg”) which is used to evaluate the integral with an error bounded by eps. The alternative method is Simpson’s integration (integration=”Simpson”): it approximates the integral from 0 to \(\infty\) by an integral from 0 to up with npt points subdividing \((0, up)\). These three extra arguments – integration, up and npt – are only available when using dstable. The other functions are all based on Romberg’s algorithm.

Functions

- dstable: density
- pstable: cdf
- qstable: quantiles
- rstable: random deviates
- hstable: hazard

Author(s)

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>)

Jim Lindsey
References


See Also

stablereg to fit generalized nonlinear regression models for the stable distribution parameters.

Examples

```r
par(mfrow=c(2,2))
x <- seq(-5,5,by=0.1)

# Influence of loc (location)
plot(x,dstable(x,loc=-2,disp=1/sqrt(2),skew=-0.8,tail=1.5),
     type="l",ylab="",main="Varying LOCALtion")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=-0.8,tail=1.5))
lines(x,dstable(x,loc=2,disp=1/sqrt(2),skew=-0.8,tail=1.5))

# Influence of disp (dispersion)
plot(x,dstable(x,loc=0,disp=0.5,skew=0,tail=1.5),
     type="l",ylab="",main="Varying DISPersion")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=0.9,skew=0,tail=1.5))

# Influence of skew (skewness)
plot(x,dstable(x,loc=0,disp=1/sqrt(2),skew=-0.8,tail=1.5),
     type="l",ylab="",main="Varying SKEWness")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0.8,tail=1.5))

# Influence of tail (tail)
plot(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=0.8),
     type="l",ylab="",main="Varying TAIL thickness")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=2))

stabledist::dstable(x=1, 1, 0)
```

---

Links

**Description**

Link and inverse functions for use in stablereg
Parameter_Conversion

Usage

loc_g(x)
loc_h(x)
disp_g(x)
disp_h(x)
skew_g(x)
skew_h(x)
tail_g(x)
tail_h(x)

Arguments

x the function argument

Description

sd2s has stabledist parameter inputs and returns stable parameters. s2sd has stable parameter inputs and returns stabledist parameters.

Usage

sd2s(alpha, beta, gamma, delta, pm = 1)
s2sd(tail, skew, disp, loc, pm = 1)

Arguments

alpha the stabledist 'alpha'
beta the stabledist 'beta'
gamma the stabledist 'gamma'
delta the stabledist 'delta'

pm default 1; currently only value supported. the stabledist parameterization 'pm'
tail the stable 'tail' analogous to 'alpha'
skew the stable 'skew' analogous to 'beta'
disp the stable 'disp' analogous to 'gamma'
loc the stable 'loc' analogous to 'delta'
Details

This is a generic function: methods can be defined for it directly or via the `Summary` group generic. For this to work properly, the arguments ... should be unnamed, and dispatch is on the first argument.

Value

What you need. See examples.

Examples

```r
q <- -1
# nolan pm=1 parameters:
a <- 1.3
b <- -0.4
c <- 2
d <- 0.75
s <- sd2s(alpha=a, beta=b, gamma=c, delta=d)
stabledist::pstable(q, alpha=a, beta=b, gamma=c, delta=d, pm=1)
sd <- s2sd(tail = s$tail, skew=s$skew, disp = s$disp, loc = s$loc)
stabledist::pstable(q, alpha=sd$alpha, beta=sd$beta, gamma=sd$gamma, delta=sd$delta, pm=1)
```

Description

`pm0_to_pm1` has stabledist parameter inputs for pm=0 and returns pm=1 equivalent parameterization. `pm1_to_pm0` has stabledist parameter inputs for pm=1 and returns pm=0 equivalent parameterization.

Usage

```r
pm0_to_pm1(a0, b0, c0, d0)

pm1_to_pm0(a1, b1, c1, d1)
```

Arguments

- `a0`: the stabledist 'alpha' for pm=0 in 'stabledist'
- `b0`: the stabledist 'beta' for pm=0 in 'stabledist'
- `c0`: the stabledist 'gamma' for pm=0 in 'stabledist'
- `d0`: the stabledist 'delta' for pm=0 in 'stabledist'
- `a1`: the stabledist 'alpha' for pm=1 in 'stabledist'
The mode of a stable distribution is given by

$$\hat{\alpha} = \frac{\alpha}{\beta + \Delta}, \quad \hat{\beta} = \frac{\beta}{\Delta}, \quad \hat{\gamma} = \frac{\gamma}{\Delta}, \quad \hat{\delta} = \frac{\delta}{\Delta}$$

where

- \( \alpha \) is the location parameter,
- \( \beta \) is the dispersion parameter,
- \( \gamma \) is the skewness parameter,
- \( \delta \) is the tail thickness parameter,
- \( \Delta = \frac{\alpha^2}{\beta^2} + \gamma^2 \) is the coefficient of tail thickness.

**Value**

What you need. See examples.

**Examples**

```r
q <- -1
# nolan pm=1 parameters:
a1 <- 1.3
b1 <- -0.4
c1 <- 2
d1 <- 0.75
# Convert to nolan pm=0 parameters:
pm0 <- pm1_to_pm0(a1,b1,c1,d1)
a0 <- pm0$a0
b0 <- pm0$b0
c0 <- pm0$c0
d0 <- pm0$d0
# check:
stabledist::pstable(q, alpha=a1, beta=b1, gamma=c1, delta=d1, pm=1)
#> [1] 0.1965513
# only change delta=d0 for pm=0
nstabledist::pstable(q, alpha=a1, beta=b1, gamma=c1, delta=d0, pm=0)
#> [1] 0.1965513
rstabledist::dstable(q, alpha=a1, beta=b1, gamma=c1, delta=d1, pm=1)
#> [1] 0.0527133
# only change delta=d0 for pm=0
rstabledist::dstable(q, alpha=a1, beta=b1, gamma=c1, delta=d0, pm=0)
#> [1] 0.0572133
```

**stable.mode**

*Mode of a Stable Distribution*

This function gives a reliable approximation to the mode of a stable distribution with location, dispersion, skewness and tail thickness specified by the parameters `loc`, `disp`, `skew` and `tail`. `tail` must be in (1,2).

**Usage**

```
stable.mode(loc, disp, skew, tail)
```
Arguments

loc vector of (real) location parameters.
disp vector of (positive) dispersion parameters.
skew vector of skewness parameters (in [-1,1]).
tail vector of parameters (in [1,2]) related to the tail thickness.

Details

loc is a location parameter in the same way as the mean in the normal distribution: it can take any real value.
disp is a dispersion parameter in the same way as the standard deviation in the normal distribution: it can take any positive value.
skew is a skewness parameter: it can take any value in (-1,1). The distribution is right-skewed, symmetric and left-skewed when skew is negative, null or positive respectively.
tail is a tail parameter (often named the characteristic exponent): it can take any value in (0,2) (with tail=1 and tail=2 yielding the Cauchy and the normal distributions respectively when symmetry holds).

The simplest empirical formula found to give a satisfactory approximation to the mode for values of tail in (1,2) is

\[ \text{loc} + \text{disp} \times a \times \text{skew} \times \exp(-b \times \text{abs}(\text{skew})) \]

with

\[ a = 1.7665114 + 1.8417675 \times \text{tail} - 2.2954390 \times \text{tail}^2 + 0.4666749 \times \text{tail}^3 \]

and

\[ b = -0.003142967 + 632.4715 \times \text{tail} \times \exp(-7.106035 \times \text{tail}) \]

Value

A list of size 3 giving the mode, a and b.

Author(s)

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>) and Jim Lindsey.

References


See Also

stable for more details on the stable distribution.
stablereg to fit generalized linear models for the stable distribution parameters.
Examples

```r
x <- seq(-5, 5, by = 0.1)
plot(x, dstable(x, loc = 0, disp = 1, skew = -1, tail = 1.5), type = "l", ylab = "f(x)")
xhat <- stable.mode(loc = 0, disp = 1, skew = -1, tail = 1.5)
fxhat <- dstable(xhat, loc = 0, disp = 1, skew = -1, tail = 1.5)
lines(c(xhat, xhat), c(0, fxhat), lty = "dotted")
```

---

stablereg

### Stable Generalized Regression Models

**Description**

stablereg fits user specified generalized linear and nonlinear regression models based on the stable distribution to (uncensored, right and/or left censored) data. This allows the location, the dispersion, the skewness and the tails of the fitted stable distribution to vary with explanatory variables.

**Usage**

```r
stablereg(y = NULL, loc = 0, disp = 1, skew = 0, tail = 1.5,
          oloc = TRUE, odisp = TRUE, oskew = TRUE, otail = TRUE,
          noopt = FALSE, iloc = NULL, idisp = NULL, iskew = NULL,
          itail = NULL, loc_h = NULL, disp_h = NULL, skew_h = NULL,
          tail_h = NULL, weights = 1, exact = FALSE, delta = 1,
          envir = parent.frame(), integration = "Romberg", eps = 1e-06,
          up = 10, npoint = 501, hessian = TRUE, llik.output = FALSE,
          print.level = 0, ndigit = 10, steptol = 1e-05, gradtol = 1e-05,
          fscale = 1, typsize = abs(p), stepmax = sqrt(p0 * %%% p0),
          iterlim = 100)
```

**Arguments**

- `y`: The response vector or a repeated data object. If the repeated data object contains more than one response variable, give that object in `envir` and give the name of the response variable to be used here.
  - For censored data, two columns with the second being the censoring indicator (1: uncensored, 0: right censored, -1: left censored.)

- `loc`, `loc_h`, `oloc`, `iloc`:
  - Describe the regression model fitted for the location parameter of the stable distribution, perhaps after transformation by the link function `loc_g` (set to the identity by default. The inverse link function is denoted by `loc_h`. Note that these functions cannot contain unknown parameters).
  - Two specifications are possible:
    1. `loc` is a linear or nonlinear language expression beginning with `~` or an R function, describing the regression function for the location parameter (after transformation by `loc_g`, the link function).
iloc is a vector of initial conditions for the parameters in the regression for this parameter.

oloc is a boolean indicating if an optimization of the likelihood has to be carried out on these parameters. If oloc is set to TRUE, a default zero value is considered for the starting values iloc. But if no optimization is desired on the location parameters, i.e. when the likelihood has to be evaluated or optimized at a fixed location, then iloc has to be explicitly specified.

(2) loc is a numeric expression (i.e. a scalar or a vector of the same size as the data vector y, or y[1,] when censoring is considered).

If oloc is set to TRUE, i.e. when an optimization of the likelihood has to be carried out on the location parameter, then the location parameter (after transformation by the link function loc_g) is set to an unknown parameter with initial value equal to iloc[1] or loc[1] when iloc is not specified.

But when oloc is set to FALSE, i.e. when the likelihood has to be evaluated or optimized at a fixed location, then the transformed location is assumed to be equal to loc when it is of the same length as the data vector y (or y[1] when censoring is considered), and to loc[1] otherwise.

Specification (1) is especially useful in ANOVA-like situations where the location is assumed to change with the levels of some factor variable.

disp, disp_h, odisp, idisp
describe the regression model for the dispersion parameter of the fitted stable distribution, after transformation by the link function disp_g (set to the log function by default). The inverse link function is denoted by disp_h. Again these functions cannot contain unknown parameters. The same rules as above apply when specifying the generalized regression model for the dispersion parameter.

skew, skew_h, oskew, iskew
describe the regression model for the skewness parameter of the fitted stable distribution, after transformation by the link function skew_g (set to \log((1 + .)/(1 - .)) by default). The inverse link function is denoted by skew_h. Again these functions cannot contain unknown parameters. The same rules as above apply when specifying the generalized regression model for the skewness parameter.

tail, tail_h, otail, itail
describe the regression model considered for the tail parameter of the fitted stable distribution, after transformation by the link function tail_g (set to \log((. - 1)/(2 - .)) by default. The inverse link function is denoted by tail_h. Again these functions cannot contain unknown parameters). The same rules as above apply when specifying the generalized regression model for the tail parameter.

noopt
When set to TRUE, it forces oloc, odisp, oskew and otail to FALSE, whatever the user choice for these last three arguments. It is especially useful when looking for appropriate initial values for the regression model parameters, before undertaking the optimization of the likelihood.

weights
Weight vector.

exact
If TRUE, fits the exact likelihood function for continuous data by integration over intervals of observation, i.e. interval censoring.

delta
Scalar or vector giving the unit of measurement for each response value, set to unity by default. For example, if a response is measured to two decimals,
If the response is transformed, this must be multiplied by the Jacobian. For example, with a log transformation, \( \delta = 1/y \). (The \( \delta \) values for the censored response are ignored.) The transformation cannot contain unknown parameters.

**envir**

Environment in which model formulae are to be interpreted or a data object of class, `repeated`, `tccov`, or `tvcov`; the name of the response variable should be given in `y`. If `y` has class `repeated`, it is used as the environment.

**integration, eps, up, npoint**

Integration indicates which algorithm must be used to evaluate the stable density when the likelihood is computed with `exact` set to `FALSE`. See the man page on `stable` for extra information.

**hessian**

Arguments controlling the optimization procedure `nlm`.

**llik.output**

is `TRUE` when the likelihood has to be displayed at each iteration of the optimization.

**print.level**

Arguments controlling the optimization procedure `nlm`.

**ndigit**

Arguments controlling the optimization procedure `nlm`.

**steptol**

Arguments controlling the optimization procedure `nlm`.

**gradtol**

Arguments controlling the optimization procedure `nlm`.

**fscale**

Arguments controlling the optimization procedure `nlm`.

**typsize**

Arguments controlling the optimization procedure `nlm`.

**stepmax**

Arguments controlling the optimization procedure `nlm`.

**iterlim**

Arguments controlling the optimization procedure `nlm`.

**Value**

A list of class `stable` is returned. The printed output includes the -log-likelihood, the corresponding AIC, the maximum likelihood estimates, standard errors, and correlations. It also include all the relevant information calculated, including error codes.

**Warning**

Because of the numerical integrations involved, convergence can be very sensitive to the initial parameter values supplied and to the settings of the arguments controlling `nlm`. If `nlm` feeds extreme parameter values in the tails of the distribution to the likelihood function, the integration may hang for a long time.

**Author(s)**

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>) and Jim Lindsey.

**References**

See Also

`lm`, `glm`, `stable` and `stableNmode`.

Examples

```r
## Share return over a 50 day period (see reference above)
# shares

# returns
ret <- (y[2:50]-y[1:49])/y[1:49]

# hist(ret, breaks=seq(-0.035,0.045,0.01))

day <- seq(0,0.48,by=0.01) # time measured in days/100
x <- seq(1,length(ret)-1)

# Classic stationary normal model tail=2
print(z1 <- stablereg(y = ret, delta = 1/y[1:49],
loc = -1, disp = -1, skew = -1, tail = tail_g(1.9999999),
iloc = 0, idisp = -3, iskew = 0, oskew = FALSE, otail = FALSE))

# Normal model (tail=2) with dispersion=disp_h(b0+b1*day)
print(z2 <- stablereg(y = ret, delta = 1/y[1:49], loc = -day,
disp = -1, skew = -1, tail = tail_g(1.9999999), idisp = c(0.003,0),
iskew = c(-4,5), oskew = FALSE, otail = FALSE))

# Stable model with loc(ation)=loc_h(b0+b1*day)
print(z3 <- stablereg(y = ret, delta = 1/y[1:49],
loc = -day, disp = -1, skew = -1, tail = -1,
iloc = c(0.001,-0.004), idisp = -4.8, iskew = 0, itail = 0.6))

# Stable model with disp(ersion)=disp_h(b0+b1*day)
print(z4 <- stablereg(y = ret, delta = 1/y[1:49],
loc = -1, disp = -day, skew = -1, tail = -1,
iloc = 0.003, idisp = c(-4.8,0), iskew = -0.03, itail = 1.6))

# Stable model with skew(ness)=skew_h(b0+b1*day)
# Evaluation at fixed parameter values (because noopt is set to TRUE)
print(z5 <- stablereg(y = ret, delta = 1/y[1:49],
loc = -1, disp = -1, skew = -day, tail = -1,
iloc = 5.557e-04, idisp = -4.957, iskew = c(2.811,-2.158),
itail = 1.57, noopt=TRUE))

# Stable model with tail=tail_h(b0+b1*day)
print(z6 <- stablereg(y = ret, delta = 1/y[1:49], loc = ret ~ 1,
disp = -1, skew = -1, tail = -day, iloc = 0.002,
idisp = -4.8, iskew = -2, itail = c(2.4,-4), hessian=FALSE))
```
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