Package ‘tfprobability’

February 2, 2022

Title Interface to ‘TensorFlow Probability’

Version 0.15.0

Description Interface to ‘TensorFlow Probability’, a 'Python' library built on ‘TensorFlow’ that makes it easy to combine probabilistic models and deep learning on modern hardware (‘TPU’, ‘GPU’).
‘TensorFlow Probability’ includes a wide selection of probability distributions and bijectors, probabilistic layers, variational inference, Markov chain Monte Carlo, and optimizers such as Nelder-Mead, BFGS, and SGLD.

License Apache License (>= 2.0)

URL https://github.com/rstudio/tfprobability

BugReports https://github.com/rstudio/tfprobability/issues

SystemRequirements TensorFlow Probability
(https://www.tensorflow.org/probability)

Encoding UTF-8

RoxygenNote 7.1.2

Imports tensorflow (>= 2.4.0), reticulate, keras, magrittr

Suggests tfdatasets, testthat (>= 2.1.0), knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation no

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glm_families  GLM families

Description

A list of models that can be used as the model argument in \texttt{glm_fit()}: 

Details

- Bernoulli: \texttt{Bernoulli(probs=mean) where mean = sigmoid(matmul(X, weights))}
- BernoulliNormalCDF: \texttt{Bernoulli(probs=mean) where mean = Normal(0, 1).cdf(matmul(X, weights))}
- GammaExp: \texttt{Gamma(concentration=1, rate=1 / mean) where mean = exp(matmul(X, weights))}
- GammaSoftplus: \texttt{Gamma(concentration=1, rate=1 / mean) where mean = softplus(matmul(X, weights))}
- LogNormal: \texttt{LogNormal(loc=log(mean) - log(2) / 2, scale=sqrt(log(2))) where mean = exp(matmul(X, weights)).}
- LogNormalSoftplus: \texttt{LogNormal(loc=log(mean) - log(2) / 2, scale=sqrt(log(2))) where mean = softplus(matmul(X, weights)).}
- Normal: \texttt{Normal(loc=mean, scale=1) where mean = matmul(X, weights).}
- NormalReciprocal: \texttt{Normal(loc=mean, scale=1) where mean = 1 / matmul(X, weights)}
- Poisson: \texttt{Poisson(rate=mean) where mean = exp(matmul(X, weights)).}
- PoissonSoftplus: \texttt{Poisson(rate=mean) where mean = softplus(matmul(X, weights)).}

Value

list of models that can be used as the model argument in \texttt{glm_fit()}

See Also

Other \texttt{glm_fit}: \texttt{glm_fit.tensorflow.tensor()}, \texttt{glm_fit_one_step.tensorflow.tensor()}
**Description**

Runs multiple Fisher scoring steps

**Usage**

```r
glm_fit(x, ...)
```

**Arguments**

- `x` float-like, matrix-shaped Tensor where each row represents a sample’s features.
- `...` other arguments passed to specific methods.

**Value**

A `glm_fit` object with parameter estimates, number of iterations, etc.

**See Also**

- `glm_fit.tensorflow.tensor()`

---

**Description**

Runs multiple Fisher scoring steps

**Usage**

```r
## S3 method for class 'tensorflow.tensor'
glm_fit(
  x,
  response,
  model,
  model_coefficients_start = NULL,
  predicted_linear_response_start = NULL,
  l2_regularizer = NULL,
  dispersion = NULL,
  offset = NULL,
  convergence_criteria_fn = NULL,
)```
Arguments

- **x** float-like, matrix-shaped Tensor where each row represents a sample’s features.
- **response** vector-shaped Tensor where each element represents a sample’s observed response (to the corresponding row of features). Must have same dtype as x.
- **model** a string naming the model (see glm_families) or a tfp$glm$ExponentialFamily-like instance which implicitly characterizes a negative log-likelihood loss by specifying the distribution’s mean, gradient_mean, and variance.
- **model_coefficients_start** Optional (batch of) vector-shaped Tensor representing the initial model coefficients, one for each column in x. Must have same dtype as model_matrix. Default value: Zeros.
- **predicted_linear_response_start** Optional Tensor with shape, dtype matching response; represents offset shifted initial linear predictions based on model_coefficients_start. Default value: offset if model_coefficients is NULL, and tf$linalg$matvec(x, model_coefficients_start) + offset otherwise.
- **l2_regularizer** Optional scalar Tensor representing L2 regularization penalty. Default: NULL i.e. no regularization.
- **dispersion** Optional (batch of) Tensor representing response dispersion.
- **offset** Optional Tensor representing constant shift applied to predicted_linear_response.
- **convergence_criteria_fn** callable taking: is_converged_previous, iter_, model_coefficients_previous, predicted_linear_response_previous, model_coefficients_next, predicted_linear_response_next, response, model, dispersion and returning a logical Tensor indicating that Fisher scoring has converged.
- **learning_rate** Optional (batch of) scalar Tensor used to dampen iterative progress. Typically only needed if optimization diverges, should be no larger than 1 and typically very close to 1. Default value: NULL (i.e., 1).
- **fast_unsafe_numerics** Optional Python bool indicating if faster, less numerically accurate methods can be employed for computing the weighted least-squares solution. Default value: TRUE (i.e., "fast but possibly diminished accuracy").
- **maximum_iterations** Optional maximum number of iterations of Fisher scoring to run; "and-ed" with result of convergence_criteria_fn. Default value: NULL (i.e., infinity).
- **name** used as name prefix to ops created by this function. Default value: "fit".
- **...** other arguments passed to specific methods.
Runs one Fisher scoring step

Usage

\texttt{glm\_fit\_one\_step(x, \ldots)}

Arguments

- \texttt{x}: float-like, matrix-shaped Tensor where each row represents a sample's features.
- \texttt{\ldots}: other arguments passed to specific methods.

Value

A \texttt{glm\_fit} object with parameter estimates, number of iterations, etc.

See Also

- \texttt{glm\_fit\_one\_step.tensorflow.tensor()}
Usage

```r
## S3 method for class 'tensorflow.tensor'
glm_fit_one_step(
  x,
  response,
  model,
  model_coefficients_start = NULL,
  predicted_linear_response_start = NULL,
  l2_regularizer = NULL,
  dispersion = NULL,
  offset = NULL,
  learning_rate = NULL,
  fast_unsafe_numerics = TRUE,
  name = NULL,
  ...
)
```

Arguments

- **x**: float-like, matrix-shaped Tensor where each row represents a sample’s features.
- **response**: vector-shaped Tensor where each element represents a sample’s observed response (to the corresponding row of features). Must have same dtype as x.
- **model**: a string naming the model (see glm_families) or a tfp$glm$ExponentialFamily-like instance which implicitly characterizes a negative log-likelihood loss by specifying the distribution’s mean, gradient_mean, and variance.
- **model_coefficients_start**: Optional (batch of) vector-shaped Tensor representing the initial model coefficients, one for each column in x. Must have same dtype as model_matrix. Default value: Zeros.
- **predicted_linear_response_start**: Optional Tensor with shape, dtype matching response; represents offset shifted initial linear predictions based on model_coefficients_start. Default value: offset if model_coefficients is NULL, and tf$linalg$matvec(x,model_coefficients_start) + offset otherwise.
- **l2_regularizer**: Optional scalar Tensor representing L2 regularization penalty. Default: NULL i.e. no regularization.
- **dispersion**: Optional (batch of) Tensor representing response dispersion.
- **offset**: Optional Tensor representing constant shift applied to predicted_linear_response.
- **learning_rate**: Optional (batch of) scalar Tensor used to dampen iterative progress. Typically only needed if optimization diverges, should be no larger than 1 and typically very close to 1. Default value: NULL (i.e., 1).
- **fast_unsafe_numerics**: Optional Python bool indicating if faster, less numerically accurate methods can be employed for computing the weighted least-squares solution. Default value: TRUE (i.e., "fast but possibly diminished accuracy").
- **name**: used as name prefix to ops created by this function. Default value: "fit".
- **...**: other arguments passed to specific methods.
initializer_blockwise

Value

A glm_fit object with parameter estimates, and number of required steps.

See Also

Other glm_fit: glm_families, glm_fit.tensorflow.tensor()

initializer_blockwise  Blockwise Initializer

Description

Initializer which concats other initializers

Usage

initializer_blockwise(initializers, sizes, validate_args = FALSE)

Arguments

initializers  list of Keras initializers, eg: keras::initializer_glorot_uniform() or initializer_constant().
sizes  list of integers scalars representing the number of elements associated with each initializer in initializers.
validate_args  bool indicating we should do (possibly expensive) graph-time assertions, if necessary.

@return Initializer which concats other inicializers

install_tfprobability  Installs TensorFlow Probability

Description

Installs TensorFlow Probability

Usage

install_tfprobability(  
method = c("auto", "virtualenv", "conda"),  
conda = "auto",  
version = "default",  
tensorflow = "default",  
extra_packages = NULL,  
...,
  
pip_ignore_installed = TRUE
)

layer_autoregressive

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>method</td>
<td>Installation method. By default, &quot;auto&quot; automatically finds a method that will work in the local environment. Change the default to force a specific installation method. Note that the &quot;virtualenv&quot; method is not available on Windows.</td>
</tr>
<tr>
<td>conda</td>
<td>The path to a conda executable. Use &quot;auto&quot; to allow reticulate to automatically find an appropriate conda binary. See conda_binary() for more details on how reticulate tries to resolve the conda executable.</td>
</tr>
<tr>
<td>version</td>
<td>TensorFlow version to install. Valid values include:</td>
</tr>
<tr>
<td></td>
<td>• &quot;default&quot; installs 2.7</td>
</tr>
<tr>
<td></td>
<td>• &quot;release&quot; installs the latest release version of tensorflow (which may be incompatible with the current version of the R package)</td>
</tr>
<tr>
<td></td>
<td>• A version specification like &quot;2.4&quot; or &quot;2.4.0&quot;. Note that if the patch version is not supplied, the latest patch release is installed (e.g., &quot;2.4&quot; today installs version &quot;2.4.2&quot;)</td>
</tr>
<tr>
<td></td>
<td>• nightly for the latest available nightly build.</td>
</tr>
<tr>
<td></td>
<td>• To any specification, you can append &quot;-cpu&quot; to install the cpu version only of the package (e.g., &quot;2.4-cpu&quot;)</td>
</tr>
<tr>
<td></td>
<td>• The full URL or path to a installer binary or python *.whl file.</td>
</tr>
<tr>
<td>tensorflow</td>
<td>Synonym for version. Maintained for backwards.</td>
</tr>
<tr>
<td>extra_packages</td>
<td>Additional Python packages to install along with TensorFlow.</td>
</tr>
<tr>
<td>pip_ignore_installed</td>
<td>Whether pip should ignore installed python packages and reinstall all already installed python packages. This defaults to TRUE, to ensure that TensorFlow dependencies like NumPy are compatible with the prebuilt TensorFlow binaries.</td>
</tr>
<tr>
<td>...</td>
<td>other arguments passed to reticulate::conda_install() or reticulate::virtualenv_install(), depending on the method used.</td>
</tr>
</tbody>
</table>

**Value**

| Value  | invisible |

---

**Description**

layer_autoregressive takes as input a Tensor of shape [..., event_size] and returns a Tensor of shape [..., event_size, params]. The output satisfies the autoregressive property. That is, the layer is configured with some permutation ord of {0, ..., event_size-1} (i.e., an ordering of the input dimensions), and the output output[batch_idx,1,...] for input dimension i depends only on inputs x[batch_idx,j] where ord(j) < ord(i).
layer_autoregressive

Usage

layer_autoregressive(
  object,
  params,
  event_shape = NULL,
  hidden_units = NULL,
  input_order = "left-to-right",
  hidden_degrees = "equal",
  activation = NULL,
  use_bias = TRUE,
  kernel_initializer = "glorot_uniform",
  validate_args = FALSE,
  ...
)

Arguments

object  What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by \texttt{layer_input()}). The return value depends on \texttt{object}. If \texttt{object} is:
  • missing or \texttt{NULL}, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from \texttt{layer_instance(object)} is returned.

params  integer specifying the number of parameters to output per input.

event_shape  list-like of positive integers (or a single int), specifying the shape of the input to this layer, which is also the event_shape of the distribution parameterized by this layer. Currently only rank-1 shapes are supported. That is, event_shape must be a single integer. If not specified, the event shape is inferred when this layer is first called or built.

hidden_units  list-like of non-negative integers, specifying the number of units in each hidden layer.

input_order  Order of degrees to the input units: 'random', 'left-to-right', 'right-to-left', or an array of an explicit order. For example, 'left-to-right' builds an autoregressive model: \( p(x) = p(x_1) p(x_2 | x_1) \ldots p(x_D | x_{<D}) \). Default: 'left-to-right'.

hidden_degrees  Method for assigning degrees to the hidden units: 'equal', 'random'. If 'equal', hidden units in each layer are allocated equally (up to a remainder term) to each degree. Default: 'equal'.

activation  An activation function. See \texttt{keras::layer_dense}. Default: \texttt{NULL}.

use_bias  Whether or not the dense layers constructed in this layer should have a bias term. See \texttt{keras::layer_dense}. Default: \texttt{TRUE}.

kernel_initializer  Initializer for the kernel weights matrix. Default: 'glorot_uniform'.

validate_args  logical, default \texttt{FALSE}. When \texttt{TRUE}, layer parameters are checked for validity despite possibly degrading runtime performance. When \texttt{FALSE} invalid inputs may silently render incorrect outputs.
Details

The autoregressive property allows us to use output[batch_idx, i] to parameterize conditional distributions: p(x[batch_idx, i] | x[batch_idx, j] for ord(j) < ord(i)) which give us a tractable distribution over input x[batch_idx]:

\[ p(x[batch_idx]) = \prod_i p(x[batch_idx, ord(i)] | x[batch_idx, ord(0:i)]) \]

For example, when params is 2, the output of the layer can parameterize the location and log-scale of an autoregressive Gaussian distribution.

Value

a Keras layer

See Also

Other layers: layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_flipout(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_local_reparameterization(), layer_dense_reparameterization(), layer_dense_variational(), layer_variable()

layer_autoregressive_transform

An autoregressive normalizing flow layer, given a layer_autoregressive.

Description

Following Papamakarios et al. (2017), given an autoregressive model \( p(x) \) with conditional distributions in the location-scale family, we can construct a normalizing flow for \( p(x) \).

Usage

layer_autoregressive_transform(object, made, ...)

Arguments

object

What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from layer_instance(object) is returned.

made

A Made layer, which must output two parameters for each input.

... Additional parameters passed to Keras Layer.
Details

Specifically, suppose made is a [layer_autoregressive()] – a layer implementing a Masked Autoencoder for Distribution Estimation (MADE) – that computes location and log-scale parameters \( \text{made}(x)[i] \) for each input \( x[i] \). Then we can represent the autoregressive model \( p(x) \) as \( x = f(u) \) where \( u \) is drawn from some base distribution and where \( f \) is an invertible and differentiable function (i.e., a Bijector) and \( f^{-1}(x) \) is defined by:

```r
library(tensorflow)
library(zeallot)
f_inverse <- function(x) {
  c(shift, log_scale) <- tf$unstack(made(x), 2, axis = -1L)
  (x - shift) * tf$math$exp(-log_scale)
}
```

Given a layer_autoregressive() made, a layer_autoregressive_transform() transforms an input tfd_* \( p(u) \) to an output tfd_* \( p(x) \) where \( x = f(u) \).

Value

a Keras layer

References

Papamakarios et al. (2017)

See Also

tfb_masked_autoregressive_flow() and layer_autoregressive()

layer_categorical_mixture_of_one_hot_categorical

A OneHotCategorical mixture Keras layer from \( k \times (1 + d) \) params.

Description

\( k \) (i.e., num_components) represents the number of component OneHotCategorical distributions and \( d \) (i.e., event_size) represents the number of categories within each OneHotCategorical distribution.

Usage

```r
layer_categorical_mixture_of_one_hot_categorical(
  object,
  event_size,
  num_components,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  sample_dtype = NULL,
)```
validate_args = FALSE,
...
)

**Arguments**

- **object**
  What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on object. If object is:
  - missing or NULL, the Layer instance is returned.
  - a Sequential model, the model with an additional layer is returned.
  - a Tensor, the output tensor from `layer_instance(object)` is returned.

- **event_size**
  Scalar integer representing the size of single draw from this distribution.

- **num_components**
  Scalar integer representing the number of mixture components. Must be at least 1. (If `num_components`=1, it's more efficient to use the OneHotCategorical layer.)

- **convert_to_tensor_fn**
  A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: `tfd$distributions$Distribution$sample`.

- **sample_dtype**
  Dtype of samples produced by this distribution. Default value: NULL (i.e., previous layer's dtype).

- **validate_args**
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

... Additional arguments passed to args of keras::create_layer.

**Details**

Typical choices for `convert_to_tensor_fn` include:

- `tfp$distributions$Distribution$sample`
- `tfp$distributions$Distribution$mean`
- `tfp$distributions$Distribution$mode`

**Value**

a Keras layer

**See Also**

For an example how to use in a Keras model, see `layer_independent_normal()`.

Other distribution layers: `layer_distribution_lambda()`, `layer_independent_bernoulli()`, `layer_independent_logistic()`, `layer_independent_normal()`, `layer_independent_poisson()`, `layer_kl_divergence_add_loss()`, `layer_kl_divergence_regularizer()`, `layer_mixture_logistic()`, `layer_mixture_normal()`, `layer_mixture_same_family()`, `layer_multivariate_normal_tri_l()`, `layer_one_hot_categorical()`
Description

This layer creates a convolution kernel that is convolved (actually cross-correlated) with the layer input to produce a tensor of outputs. It may also include a bias addition and activation function on the outputs. It assumes the kernel and/or bias are drawn from distributions.

Usage

layer_conv_1d_flipout(
  object,
  filters,
  kernel_size,
  strides = 1,
  padding = "valid",
  data_format = "channels_last",
  dilation_rate = 1,
  activation = NULL,
  activity_regularizer = NULL,
  trainable = TRUE,
  kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
  kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
  kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
  bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  bias_prior_fn = NULL,
  bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  ...
)

Arguments

object
  What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

filters
  Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).

kernel_size
  An integer or list of a single integer, specifying the length of the 1D convolution window.
strides
An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.

padding
One of "valid" or "same" (case-insensitive).

data_format
A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).

dilation_rate
An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.

activation
Activation function. Set it to None to maintain a linear activation.

activity_regularizer
Regularizer function for the output.

trainable
Whether the layer weights will be updated during training.

kernel_posterior_fn
Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().

kernel_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

kernel_prior_fn
Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).

kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

bias_posterior_fn
Function which creates a tfd$Distribution instance representing the surrogate posterior of the bias parameter. Default value: default_mean_field_normal_fn(is_singular = TRUE) (which creates an instance of tfd_deterministic).

bias_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

bias_prior_fn
Function which creates tfd instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

... Additional keyword arguments passed to the keras::layer_dense constructed by this layer.
Details

This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

\[
\text{outputs} = f(\text{inputs}; \text{kernel}, \text{bias}), \text{kernel}, \text{bias} \sim \text{posterior}
\]

where \(f\) denotes the layer's calculation. It uses the Flipout estimator (Wen et al., 2018), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias. Flipout uses roughly twice as many floating point operations as the reparameterization estimator but has the advantage of significantly lower variance.

The arguments permit separate specification of the surrogate posterior (\(q(W|x)\)), prior (\(p(W)\)), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the losses property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if \(\text{kl}\) is the sum of losses for each element of the batch, you should pass \(\text{kl} / \text{num_examples_per_epoch}\) to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the kernel_posterior, kernel_prior, bias_posterior and bias_prior properties.

Value

a Keras layer

References


See Also

Other layers: `layer_autoregressive()`, `layer_conv_1d_reparameterization()`, `layer_conv_2d_flipout()`, `layer_conv_2d_reparameterization()`, `layer_conv_3d_flipout()`, `layer_conv_3d_reparameterization()`, `layer_dense_flipout()`, `layer_dense_local_reparameterization()`, `layer_dense_reparameterization()`, `layer_dense_variational()`, `layer_variable()`

---

*layer_conv_1d_reparameterization*

1D convolution layer (e.g. temporal convolution).
Description

This layer creates a convolution kernel that is convolved (actually cross-correlated) with the layer input to produce a tensor of outputs. It may also include a bias addition and activation function on the outputs. It assumes the kernel and/or bias are drawn from distributions.

Usage

```r
layer_conv_1d_reparameterization(
  object,
  filters,
  kernel_size,
  strides = 1,
  padding = "valid",
  data_format = "channels_last",
  dilation_rate = 1,
  activation = NULL,
  activity_regularizer = NULL,
  trainable = TRUE,
  kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
  kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
  kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
  bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  bias_prior_fn = NULL,
  bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  ...
)
```

Arguments

- **object**
  - What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on `object`. If `object` is:
    - missing or NULL, the Layer instance is returned.
    - a Sequential model, the model with an additional layer is returned.
    - a Tensor, the output tensor from `layer_instance(object)` is returned.

- **filters**
  - Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).

- **kernel_size**
  - An integer or list of a single integer, specifying the length of the 1D convolution window.

- **strides**
  - An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.

- **padding**
  - One of "valid" or "same" (case-insensitive).
data_format  A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).

dilation_rate  An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.

activation  Activation function. Set it to None to maintain a linear activation.

activity_regularizer  Regularizer function for the output.

trainable  Whether the layer weights will be updated during training.

kernel_posterior_fn  Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().

kernel_posterior_tensor_fn  Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

kernel_prior_fn  Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).

kernel_divergence_fn  Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

bias_posterior_fn  Function which creates a tfd$Distribution instance representing the surrogate posterior of the bias parameter. Default value: default_mean_field_normal_fn(is_singular = TRUE) (which creates an instance of tfd_deterministic).

bias_posterior_tensor_fn  Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

bias_prior_fn  Function which creates tfd instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn  Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

...  Additional keyword arguments passed to the keras::layer_dense constructed by this layer.
Details

This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

\[
\text{outputs} = f(\text{inputs}; \text{kernel}, \text{bias}), \text{kernel}, \text{bias} \sim \text{posterior}
\]

where \(f\) denotes the layer’s calculation. It uses the reparameterization estimator (Kingma and Welling, 2014), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias.

The arguments permit separate specification of the surrogate posterior \(q(W|x)\), prior \(p(W)\), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the \text{losses} property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if \(k1\) is the sum of losses for each element of the batch, you should pass \(k1 / \text{num_examples_per_epoch}\) to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the \text{kernel_posterior}, \text{kernel_prior}, \text{bias_posterior} and \text{bias_prior} properties.

Value

a Keras layer

References


See Also

Other layers: \text{layer_autoregressive()}, \text{layer_conv_1d_flipout()}, \text{layer_conv_2d_flipout()}, \text{layer_conv_2d_reparameterization()}, \text{layer_conv_3d_flipout()}, \text{layer_conv_3d_reparameterization()}, \text{layer_dense_flipout()}, \text{layer_dense_local_reparameterization()}, \text{layer_dense_reparameterization()}, \text{layer_dense_variational()}, \text{layer_variable}()

\text{layer_conv_2d_flipout} 2D convolution layer (e.g. spatial convolution over images) with Flipout

Description

This layer creates a convolution kernel that is convolved (actually cross-correlated) with the layer input to produce a tensor of outputs. It may also include a bias addition and activation function on the outputs. It assumes the kernel and/or bias are drawn from distributions.
Usage

layer_conv_2d_flipout(
  object,
  filters,
  kernel_size,
  strides = 1,
  padding = "valid",
  data_format = "channels_last",
  dilation_rate = 1,
  activation = NULL,
  activity_regularizer = NULL,
  trainable = TRUE,
  kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
  kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
  kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
  bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  bias_prior_fn = NULL,
  bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  ...
)

Arguments

  object  What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
    • missing or NULL, the Layer instance is returned.
    • a Sequential model, the model with an additional layer is returned.
    • a Tensor, the output tensor from layer_instance(object) is returned.
  filters  Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).
  kernel_size  An integer or list of a single integer, specifying the length of the 1D convolution window.
  strides  An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.
  padding  One of "valid" or "same" (case-insensitive).
  data_format  A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).
  dilation_rate  An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.
activation Activation function. Set it to None to maintain a linear activation.
activity_regularizer Regularizer function for the output.
trainable Whether the layer weights will be updated during training.
kernel_posterior_fn Function which creates \texttt{tfd$Distribution} instance representing the surrogate posterior of the kernel parameter. Default value: \texttt{default\_mean\_field\_normal\_fn()}.  
kernel_posterior_tensor_fn Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: \texttt{function(d) d \%\% tfd\_sample()}.  
kernel_prior_fn Function which creates \texttt{tfd$Distribution} instance. See \texttt{default\_mean\_field\_normal\_fn} docstring for required parameter signature. Default value: \texttt{tfd\_normal(loc = 0, scale = 1)}.  
kernel_divergence_fn Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a \texttt{Tensor}.

bias_posterior_fn Function which creates a \texttt{tfd$Distribution} instance representing the surrogate posterior of the bias parameter. Default value: \texttt{default\_mean\_field\_normal\_fn(is\_singular = TRUE)} (which creates an instance of \texttt{tfd\_deterministic}).  
bias_posterior_tensor_fn Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: \texttt{function(d) d \%\% tfd\_sample()}.  
bias_prior_fn Function which creates \texttt{tfd} instance. See \texttt{default\_mean\_field\_normal\_fn} docstring for required parameter signature. Default value: \texttt{NULL} (no prior, no variational inference)  
bias_divergence_fn Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a \texttt{Tensor}.

... Additional keyword arguments passed to the \texttt{keras::layer\_dense} constructed by this layer.

**Details**

This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors.

$$outputs = f(inputs; kernel, bias), kernel, bias \sim \text{posterior}$$
where $f$ denotes the layer's calculation. It uses the Flipout estimator (Wen et al., 2018), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias. Flipout uses roughly twice as many floating point operations as the reparameterization estimator but has the advantage of significantly lower variance.

The arguments permit separate specification of the surrogate posterior ($q(W|x)$), prior ($p(W)$), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the `losses` property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if $\text{kl}$ is the sum of losses for each element of the batch, you should pass $\text{kl} / \text{num examples per epoch}$ to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the `kernel_posterior`, `kernel_prior`, `bias_posterior` and `bias_prior` properties.

Value

a Keras layer

References


See Also

Other layers: `layer_autoregressive()`, `layer_conv_1d_flipout()`, `layer_conv_1d_reparameterization()`, `layer_conv_2d_reparameterization()`, `layer_conv_3d_flipout()`, `layer_conv_3d_reparameterization()`, `layer_dense_flipout()`, `layer_dense_local_reparameterization()`, `layer_dense_reparameterization()`, `layer_dense_variational()`, `layer_variable()`
layer_conv_2d_reparameterization

strides = 1,
padding = "valid",
data_format = "channels_last",
dilation_rate = 1,
activation = NULL,
activity_regularizer = NULL,
trainable = TRUE,
kernelposterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
kernelposterior_tensor_fn = function(d) d %>% tfd_sample(),
kernelprior_fn = tfp$layers$util$default_multivariate_normal_fn,
kerneldivergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
bias_posterior.tensor_fn = function(d) d %>% tfd_sample(),
bias_prior_fn = NULL,
bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

filters Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).

kernel_size An integer or list of a single integer, specifying the length of the 1D convolution window.

strides An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.

padding One of "valid" or "same" (case-insensitive).

data_format A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).

dilation_rate An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.

activation Activation function. Set it to None to maintain a linear activation.

activity_regularizer Regularizer function for the output.

trainable Whether the layer weights will be updated during training.
layer_conv_2d_reparameterization

kernel_posterior_fn
Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().

kernel_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

kernel_prior_fn
Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).

kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

bias_posterior_fn
Function which creates a tfd$Distribution instance representing the surrogate posterior of the bias parameter. Default value: default_mean_field_normal_fn(is_singular = TRUE) (which creates an instance of tfd_deterministic).

bias_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

bias_prior_fn
Function which creates tfd instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

...
Additional keyword arguments passed to the keras::layer_dense constructed by this layer.

Details
This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

outputs = f(inputs; kernel, bias), kernel, bias ~ posterior

where f denotes the layer's calculation. It uses the reparameterization estimator (Kingma and Welling, 2014), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias.

The arguments permit separate specification of the surrogate posterior (q(W|x)), prior (p(W)), and divergence for both the kernel and bias distributions.
Upon being built, this layer adds losses (accessible via the `losses` property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if `kl` is the sum of losses for each element of the batch, you should pass `kl / num_examples_per_epoch` to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the `kernel_posterior`, `kernel_prior`, `bias_posterior` and `bias_prior` properties.

**Value**

a Keras layer

**References**


**See Also**

Other layers: `layer_autoregressive()`, `layer_conv_1d_flipout()`, `layer_conv_1d_reparameterization()`, `layer_conv_2d_flipout()`, `layer_conv_3d_flipout()`, `layer_conv_3d_reparameterization()`, `layer_dense_flipout()`, `layer_dense_local_reparameterization()`, `layer_dense_reparameterization()`, `layer_dense_variational()`, `layer_variable()`

---

**layer_conv_3d_flipout** 3D convolution layer (e.g. spatial convolution over volumes) with Flipout

**Description**

This layer creates a convolution kernel that is convolved (actually cross-correlated) with the layer input to produce a tensor of outputs. It may also include a bias addition and activation function on the outputs. It assumes the kernel and/or bias are drawn from distributions.

**Usage**

```python
def layer_conv_3d_flipout(
    object,
    filters,
    kernel_size,
    strides = 1,
    padding = "valid",
    data_format = "channels_last",
    dilation_rate = 1,
    activation = NULL,
    activity_regularizer = NULL,
    trainable = TRUE,
    kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
)```
kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
bias_prior_fn = NULL,
bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
...

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from layer_instance(object) is returned.

filters Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).

kernel_size An integer or list of a single integer, specifying the length of the 1D convolution window.

strides An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.

padding One of "valid" or "same" (case-insensitive).

data_format A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).

dilation_rate An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.

activation Activation function. Set it to None to maintain a linear activation.
activity_regularizer Regularizer function for the output.
 trainable Whether the layer weights will be updated during training.
kernel_posterior_fn Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().
kernel_posterior_tensor_fn Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().
kernel_prior_fn
Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).

kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

bias_posterior_fn
Function which creates a tfd$Distribution instance representing the surrogate posterior of the bias parameter. Default value: default_mean_field_normal_fn(is_singular = TRUE) (which creates an instance of tfd_deterministic).

bias_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

bias_prior_fn
Function which creates tfd instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

... Additional keyword arguments passed to the keras::layer_dense constructed by this layer.

Details
This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

outputs = f(inputs; kernel, bias), kernel, bias ~ posterior

where f denotes the layer's calculation. It uses the Flipout estimator (Wen et al., 2018), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias. Flipout uses roughly twice as many floating point operations as the reparameterization estimator but has the advantage of significantly lower variance.

The arguments permit separate specification of the surrogate posterior (q(W|x)), prior (p(W)), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the losses property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if kl is the sum of losses for each element of the batch, you should pass kl
/ num_examples_per_epoch to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the kernel_posterior, kernel_prior, bias_posterior and bias_prior properties.

Value

a Keras layer

References


See Also

Other layers: layer_autoregressive(), layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_local_reparameterization(), layer_dense_reparameterization(), layer_dense_variational(), layer_variable()
kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
bias_prior_fn = NULL,
bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
...)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

filters Integer, the dimensionality of the output space (i.e. the number of filters in the convolution).

kernel_size An integer or list of a single integer, specifying the length of the 1D convolution window.

strides An integer or list of a single integer, specifying the stride length of the convolution. Specifying any stride value != 1 is incompatible with specifying any dilation_rate value != 1.

padding One of "valid" or "same" (case-insensitive).

data_format A string, one of channels_last (default) or channels_first. The ordering of the dimensions in the inputs. channels_last corresponds to inputs with shape (batch, length, channels) while channels_first corresponds to inputs with shape (batch, channels, length).

dilation_rate An integer or tuple/list of a single integer, specifying the dilation rate to use for dilated convolution. Currently, specifying any dilation_rate value != 1 is incompatible with specifying any strides value != 1.

activation Activation function. Set it to None to maintain a linear activation.

activity_regularizer Regularizer function for the output.

trainable Whether the layer weights will be updated during training.

kernel_posterior_fn Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().

kernel_posterior_tensor_fn Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

kernel_prior_fn Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).
kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

bias_posterior_fn
Function which creates a tfd$Distribution instance representing the surrogate posterior of the bias parameter. Default value: default_mean_field_normal_fn(is_singular = TRUE) (which creates an instance of tfd_deterministic).

bias_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

bias_prior_fn
Function which creates tfd instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.

... Additional keyword arguments passed to the keras::layer_dense constructed by this layer.

Details
This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

outputs = f(inputs; kernel, bias), kernel, bias ~ posterior

where f denotes the layer's calculation. It uses the reparameterization estimator (Kingma and Welling, 2014), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias.

The arguments permit separate specification of the surrogate posterior (q(W|x)), prior (p(W)), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the losses property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if kl is the sum of losses for each element of the batch, you should pass kl / num_examples_per_epoch to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the kernel_posterior, kernel_prior, bias_posterior and bias_prior properties.

Value
a Keras layer
layer_dense_flipout

Densely-connected layer class with Flipout estimator.

Description

This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

Usage

```r
layer_dense_flipout(
  object,
  units,
  activation = NULL,
  activity_regularizer = NULL,
  trainable = TRUE,
  kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
  kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
  kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
  bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  bias_prior_fn = NULL,
  bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  seed = NULL,
  ...
)
```

Arguments

- `object` What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on `object`. If `object` is:
  - missing or NULL, the Layer instance is returned.
  - a Sequential model, the model with an additional layer is returned.

References


See Also

Other layers: `layer_autoregressive()`, `layer_conv_1d_flipout()`, `layer_conv_1d_reparameterization()`, `layer_conv_2d_flipout()`, `layer_conv_2d_reparameterization()`, `layer_conv_3d_flipout()`, `layer_dense_flipout()`, `layer_dense_local_reparameterization()`, `layer_dense_reparameterization()`, `layer_dense_variational()`, `layer_variable()`
- a Tensor, the output tensor from layer_instance(object) is returned.

units
integer dimensionality of the output space

activation
Activation function. Set it to None to maintain a linear activation.

activity_regularizer
Regularizer function for the output.

trainable
Whether the layer weights will be updated during training.

kernel_posterior_fn
Function which creates \texttt{tfd$Distribution} instance representing the surrogate posterior of the kernel parameter. Default value: \texttt{default_mean_field_normal_fn()}.

kernel_posterior_tensor_fn
Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: \texttt{function(d) d \%>\% tfd_sample()}.

kernel_prior_fn
Function which creates \texttt{tfd$Distribution} instance. See \texttt{default_mean_field_normal_fn} docstring for required parameter signature. Default value: \texttt{tfd_normal(loc = 0, scale = 1)}.

kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a Tensor.

bias_posterior_fn
Function which creates a \texttt{tfd$Distribution} instance representing the surrogate posterior of the bias parameter. Default value: \texttt{default_mean_field_normal_fn(is_singular = TRUE)} (which creates an instance of \texttt{tfd_deterministic}).

bias_posterior_tensor_fn
Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: \texttt{function(d) d \%>\% tfd_sample()}.

bias_prior_fn
Function which creates \texttt{tfd} instance. See \texttt{default_mean_field_normal_fn} docstring for required parameter signature. Default value: \texttt{NULL} (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a Tensor.

seed
scalar integer which initializes the random number generator. Default value: \texttt{NULL} (i.e., use global seed).

... Additional keyword arguments passed to the \texttt{keras::layer_dense} constructed by this layer.

Details
By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,
It uses the Flipout estimator (Wen et al., 2018), which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias. Flipout uses roughly twice as many floating point operations as the reparameterization estimator but has the advantage of significantly lower variance.

The arguments permit separate specification of the surrogate posterior ($q(W|x)$), prior ($p(W)$), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the `losses` property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if $k_1$ is the sum of losses for each element of the batch, you should pass $k_1 / \text{num\_examples\_per\_epoch}$ to your optimizer).

**Value**

A Keras layer

**References**


**See Also**

Other layers: `layer_autoregressive()`, `layer_conv_1d_flipout()`, `layer_conv_1d_reparameterization()`, `layer_conv_2d_flipout()`, `layer_conv_2d_reparameterization()`, `layer_conv_3d_flipout()`, `layer_conv_3d_reparameterization()`, `layer_dense_local_reparameterization()`, `layer_dense_reparameterization()`, `layer_dense_variational()`, `layer_variable()`
layer_dense_local_reparameterization

Usage

layer_dense_local_reparameterization(
    object,
    units,
    activation = NULL,
    activity_regularizer = NULL,
    trainable = TRUE,
    kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
    kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
    kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
    kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
    bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
    bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
    bias_prior_fn = NULL,
    bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
    ...
)

Arguments

object
What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from layer_instance(object) is returned.

units
integer dimensionality of the output space

activation
Activation function. Set it to None to maintain a linear activation.

activity_regularizer
Regularizer function for the output.

trainable
Whether the layer weights will be updated during training.

kernel_posterior_fn
Function which creates tfd$Distribution instance representing the surrogate posterior of the kernel parameter. Default value: default_mean_field_normal_fn().

kernel_posterior_tensor_fn
Function which takes a tfd$Distribution instance and returns a representative value. Default value: function(d) d %>% tfd_sample().

kernel_prior_fn
Function which creates tfd$Distribution instance. See default_mean_field_normal_fn docstring for required parameter signature. Default value: tfd_normal(loc = 0, scale = 1).

kernel_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are tfd$Distribution-like instances and the sample is a Tensor.
layer_dense_local_reparameterization

bias_posterior_fn
Function which creates a \texttt{tfd\$Distribution} instance representing the surrogate posterior of the bias parameter. Default value: \texttt{default_mean_field_normal_fn(is_singular = TRUE)} (which creates an instance of \texttt{tfd_deterministic}).

bias_posterior_tensor_fn
Function which takes a \texttt{tfd\$Distribution} instance and returns a representative value. Default value: \texttt{function(d) d \%\% tfd_sample()}.

bias_prior_fn
Function which creates \texttt{tfd} instance. See \texttt{default_mean_field_normal_fn} docstring for required parameter signature. Default value: \texttt{NULL} (no prior, no variational inference)

bias_divergence_fn
Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd\$Distribution}-like instances and the sample is a Tensor.

Details

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,

\[
\text{kernel, bias} \sim \text{posterior}
\]
\[
\text{outputs} = \text{activation(matmul(inputs, kernel) + bias)}
\]

It uses the local reparameterization estimator (Kingma et al., 2015), which performs a Monte Carlo approximation of the distribution on the hidden units induced by the kernel and bias. The default \texttt{kernel_posterior_fn} is a normal distribution which factorizes across all elements of the weight matrix and bias vector. Unlike that paper’s multiplicative parameterization, this distribution has trainable location and scale parameters which is known as an additive noise parameterization (Molchanov et al., 2017).

The arguments permit separate specification of the surrogate posterior (q(\(W|X\))), prior (p(\(W\))), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the \texttt{losses} property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if \(k1\) is the sum of losses for each element of the batch, you should pass \(k1 / \text{num\_examples\_per\_epoch}\) to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the \texttt{kernel\_posterior}, \texttt{kernel\_prior}, \texttt{bias\_posterior} and \texttt{bias\_prior} properties.

Value

a Keras layer
layer_dense_reparameterization

Densely-connected layer class with reparameterization estimator.

Description

This layer implements the Bayesian variational inference analogue to a dense layer by assuming the kernel and/or the bias are drawn from distributions.

Usage

layer_dense_reparameterization(
  object,
  units,
  activation = NULL,
  activity_regularizer = NULL,
  trainable = TRUE,
  kernel_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(),
  kernel_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  kernel_prior_fn = tfp$layers$util$default_multivariate_normal_fn,
  kernel_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  bias_posterior_fn = tfp$layers$util$default_mean_field_normal_fn(is_singular = TRUE),
  bias_posterior_tensor_fn = function(d) d %>% tfd_sample(),
  bias_prior_fn = NULL,
  bias_divergence_fn = function(q, p, ignore) tfd_kl_divergence(q, p),
  ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

References


See Also

Other layers: layer_autoregressive(), layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_flipout(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_reparameterization(), layer_dense_variational(), layer_variable()
layer_dense_reparameterization

- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from layer_instance(object) is returned.

units integer dimensionality of the output space
activation Activation function. Set it to None to maintain a linear activation.
activity_regularizer Regularizer function for the output.
trainable Whether the layer weights will be updated during training.
kernel_posterior_fn Function which creates \texttt{tfd$Distribution} instance representing the surrogate posterior of the kernel parameter. Default value: \texttt{default\_mean\_field\_normal\_fn()}. 
kernel_posterior_tensor_fn Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: function(d) d \texttt{tfd\_sample}().
kernel_prior_fn Function which creates \texttt{tfd$Distribution} instance. See \texttt{default\_mean\_field\_normal\_fn} docstring for required parameter signature. Default value: \texttt{tfd\_normal(loc = 0, scale = 1)}. 
kernel_divergence_fn Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a Tensor.

bias_posterior_fn Function which creates \texttt{tfd$Distribution} instance representing the surrogate posterior of the bias parameter. Default value: \texttt{default\_mean\_field\_normal\_fn(is\_singular = TRUE)} (which creates an instance of \texttt{tfd\_deterministic}).
bias_posterior_tensor_fn Function which takes a \texttt{tfd$Distribution} instance and returns a representative value. Default value: function(d) d \texttt{tfd\_sample}().
bias_prior_fn Function which creates \texttt{tfd} instance. See \texttt{default\_mean\_field\_normal\_fn} docstring for required parameter signature. Default value: NULL (no prior, no variational inference)

bias_divergence_fn Function which takes the surrogate posterior distribution, prior distribution and random variate sample(s) from the surrogate posterior and computes or approximates the KL divergence. The distributions are \texttt{tfd$Distribution}-like instances and the sample is a Tensor.

... Additional keyword arguments passed to the \texttt{keras::layer\_dense} constructed by this layer.

Details

By default, the layer implements a stochastic forward pass via sampling from the kernel and bias posteriors,
layer_dense_variational

kernel, bias ~ posterior
outputs = activation(matmul(inputs, kernel) + bias)

It uses the reparameterization estimator (Kingma and Welling, 2014) which performs a Monte Carlo approximation of the distribution integrating over the kernel and bias.

The arguments permit separate specification of the surrogate posterior ($q(W|x)$), prior ($p(W)$), and divergence for both the kernel and bias distributions.

Upon being built, this layer adds losses (accessible via the losses property) representing the divergences of kernel and/or bias surrogate posteriors and their respective priors. When doing minibatch stochastic optimization, make sure to scale this loss such that it is applied just once per epoch (e.g. if $k_l$ is the sum of losses for each element of the batch, you should pass $k_l / \text{num\_examples\_per\_epoch}$ to your optimizer). You can access the kernel and/or bias posterior and prior distributions after the layer is built via the kernel_posterior, kernel_prior, bias_posterior and bias_prior properties.

Value

- a Keras layer

References


See Also

Other layers: layer_autoregressive(), layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_flipout(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_local_reparameterization(), layer_dense_variational(), layer_variable()
layer_dense_variational

Usage

layer_dense_variational(
  object,
  units,
  make_posterior_fn,
  make_prior_fn,
  kl_weight = NULL,
  kl_use_exact = FALSE,
  activation = NULL,
  use_bias = TRUE,
  ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

units Positive integer, dimensionality of the output space.

make_posterior_fn function taking tf$size(kernel), tf$size(bias), dtype and returns another callable which takes an input and produces a tfd$Distribution instance.

make_prior_fn function taking tf$size(kernel), tf$size(bias), dtype and returns another callable which takes an input and produces a tfd$Distribution instance.

kl_weight Amount by which to scale the KL divergence loss between prior and posterior.

kl_use_exact Logical indicating that the analytical KL divergence should be used rather than a Monte Carlo approximation.

activation An activation function. See keras::layer_dense. Default: NULL.

use_bias Whether or not the dense layers constructed in this layer should have a bias term. See keras::layer_dense. Default: TRUE.

... Additional keyword arguments passed to the keras::layer_dense constructed by this layer.

Value

a Keras layer

See Also

Other layers: layer_autoregressive(), layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_flipout(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_local_reparameterization(), layer_dense_reparameterization(), layer_variable()
**Description**

Keras layer enabling plumbing TFP distributions through Keras models

**Usage**

```r
layer_distribution_lambda(
  object,
  make_distribution_fn,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  ...
)
```

**Arguments**

- **object**: What to compose the new `Layer` instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on `object`. If `object` is:
  - missing or NULL, the `Layer` instance is returned.
  - a Sequential model, the model with an additional layer is returned.
  - a Tensor, the output tensor from `layer_instance(object)` is returned.

- **make_distribution_fn**: A callable that takes previous layer outputs and returns a `tfd$distributions$Distribution` instance.

- **convert_to_tensor_fn**: A callable that takes a `tfd$Distribution` instance and returns a `tf$Tensor-like` object. Default value: `tfd$distributions$Distribution$sample`.

- **...**: Additional arguments passed to args of `keras::create_layer`.

**Value**

a Keras layer

**See Also**

For an example how to use in a Keras model, see `layer_independent_normal()`.

Other distribution layers: `layer_categorical_mixture_of_one_hot_categorical()`, `layer_independent_bernoulli()`, `layer_independent_logistic()`, `layer_independent_normal()`, `layer_independent_poisson()`, `layer_kl_divergence_add_loss()`, `layer_kl_divergence_regularizer()`, `layer_mixture_logistic()`, `layer_mixture_normal()`, `layer_mixture_same_family()`, `layer_multivariate_normal_tri_l()`, `layer_one_hot_categorical()`
layer_independent_bernoulli

An Independent-Bernoulli Keras layer from prod(event_shape) params

Description

An Independent-Bernoulli Keras layer from prod(event_shape) params

Usage

layer_independent_bernoulli(
    object,
    event_shape,
    convert_to_tensor_fn = tfp$distributions$Distribution$sample,
    sample_dtype = NULL,
    validate_args = FALSE,
    ...
)

Arguments

object
What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

• missing or NULL, the Layer instance is returned.
• a Sequential model, the model with an additional layer is returned.
• a Tensor, the output tensor from layer_instance(object) is returned.

event_shape
Scalar integer representing the size of single draw from this distribution.

convert_to_tensor_fn
A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.

sample_dtype
dtype of samples produced by this distribution. Default value: NULL (i.e., previous layer’s dtype).

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param ...

Additional arguments passed to args of keras::create_layer.

...

Additional arguments passed to args of keras::create_layer.

Value

a Keras layer
layer_independent_logistic

See Also

For an example how to use in a Keras model, see layer_independent_normal().

Other distribution_layers: layer_categorical_mixture_of_one_hot_categorical(), layer_distribution_lambda(), layer_independent_logistic(), layer_independent_normal(), layer_independent_poisson(), layer_kl_divergence_add_loss(), layer_kl_divergence_regularizer(), layer_mixture_logistic(), layer_mixture_normal(), layer_mixture_same_family(), layer_multivariate_normal_tril(), layer_one_hot_categorical()

layer_independent_logistic

An independent Logistic Keras layer.

Description

An independent Logistic Keras layer.

Usage

layer_independent_logistic(
  object,
  event_shape,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  validate_args = FALSE,
  ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

event_shape Scalar integer representing the size of single draw from this distribution.

convert_to_tensor_fn A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param ...

Additional arguments passed to args of keras::create_layer.

... Additional arguments passed to args of keras::create_layer.
layer_independent_normal

Value

A Keras layer.

See Also

For an example how to use in a Keras model, see layer_independent_normal().

Other distribution_layers: layer_categorical_mixture_of_one_hot_categorical(), layer_distribution_lambda(), layer_independent_bernoulli(), layer_independent_normal(), layer_independent_poisson(), layer_kl_divergence_add_loss(), layer_kl_divergence_regularizer(), layer_mixuture_logistic(), layer_mixture_normal(), layer_mixture_same_family(), layer_multivariate_normal_tri_l(), layer_one_hot_categorical()

layer_independent_normal

An independent Normal Keras layer.

Description

An independent Normal Keras layer.

Usage

layer_independent_normal(
  object,
  event_shape,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  validate_args = FALSE,
  ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.

event_shape Scalar integer representing the size of single draw from this distribution.

convert_to_tensor_fn A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param ...

... Additional arguments passed to args of keras::create_layer.

... Additional arguments passed to args of keras::create_layer.
**Value**

A Keras layer

**See Also**

Other distribution layers: `layer_categorical_mixture_of_one_hot_categorical()`, `layer_distribution_lambda()`, `layer_independent_bernoulli()`, `layer_independent_logistic()`, `layer_independent_poisson()`, `layer_kl_divergence_add_loss()`, `layer_kl_divergence_regularizer()`, `layer_mixture_logistic()`, `layer_mixture_normal()`, `layer_mixture_same_family()`, `layer_multivariate_normal_tri_l()`, `layer_one_hot_categorical()`

**Examples**

```r
library(keras)
input_shape <- c(28, 28, 1)
encoded_shape <- 2
n <- 2
model <- keras_model_sequential(
  list(
    layer_input(shape = input_shape),
    layer_flatten(),
    layer_dense(units = n),
    layer_dense(units = params_size_independent_normal(encoded_shape)),
    layer_independent_normal(event_shape = encoded_shape)
  )
)
```

---

**layer_independent_poisson**

*An independent Poisson Keras layer.*

**Description**

An independent Poisson Keras layer.

**Usage**

```r
layer_independent_poisson(
  object,
  event_shape,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  validate_args = FALSE,
  ...
)
```
Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from `layer_instance(object)` is returned.

event_shape Scalar integer representing the size of single draw from this distribution.

customize_to_tensor_fn A callable that takes a `tfd$Distribution` instance and returns a `tf$Tensor-like` object. Default value: `tfd$Distributions$Distribution$sample`.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param ... Additional arguments passed to args of `keras::create_layer`.

Value

a Keras layer

See Also

For an example how to use in a Keras model, see `layer_independent_normal()`.

Other distribution_layers: `layer_categorical_mixture_of_one_hot_categorical()`, `layer_distribution_lambda()`, `layer_independent_bernoulli()`, `layer_independent_logistic()`, `layer_independent_normal()`, `layer_kl_divergence_add_loss()`, `layer_kl_divergence_regularizer()`, `layer_mixture_logistic()`, `layer_mixture_normal()`, `layer_mixture_same_family()`, `layer_multivariate_normal_tri_l()`, `layer_one_hot_categorical()`

---

**layer_kl_divergence_add_loss**

Pass-through layer that adds a KL divergence penalty to the model loss

---

Description

Pass-through layer that adds a KL divergence penalty to the model loss
layer_kl_divergence_add_loss

Usage

layer_kl_divergence_add_loss(
  object,
  distribution_b,
  use_exact_kl = FALSE,
  test_points_reduce_axis = NULL,
  test_points_fn = tf$convert_to_tensor,
  weight = NULL,
  ...
)

Arguments

object         What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
                • missing or NULL, the Layer instance is returned.
                • a Sequential model, the model with an additional layer is returned.
                • a Tensor, the output tensor from layer_instance(object) is returned.
distribution_b Distribution instance corresponding to b as in KL[a,b]. The previous layer's output is presumed to be a Distribution instance and is a.
use_exact_kl   Logical indicating if KL divergence should be calculated exactly via tfp$distributions$kl_divergence or via Monte Carlo approximation. Default value: FALSE.
test_points_reduce_axis Integer vector or scalar representing dimensions over which to reduce_mean while calculating the Monte Carlo approximation of the KL divergence. As is with all tf$reduce_* ops, NULL means reduce over all dimensions; () means reduce over none of them. Default value: () (i.e., no reduction).
test_points_fn  A callable taking a tfp$distributions$Distribution instance and returning a tensor used for random test points to approximate the KL divergence. Default value: tf$convert_to_tensor.
weight         Multiplier applied to the calculated KL divergence for each Keras batch member. Default value: NULL (i.e., do not weight each batch member).
...             Additional arguments passed to args of keras::create_layer.

Value

a Keras layer

See Also

For an example how to use in a Keras model, see layer_independent_normal().
Other distribution_layers: layer_categorical_mixture_of_one_hot_categorical(), layer_distribution_lambda(), layer_independent_bernoulli(), layer_independent_logistic(), layer_independent_normal(), layer_independent_poisson(), layer_kl_divergence_regularizer(), layer_mixture_logistic(), layer_mixture_normal(), layer_mixture_same_family(), layer_multivariate_normal_tri_l(), layer_one_hot_categorical()
layer_kl_divergence_regularizer

Regularizer that adds a KL divergence penalty to the model loss

Description

When using Monte Carlo approximation (e.g., use_exact = FALSE), it is presumed that the input distribution’s concretization (i.e., tf$convert_to_tensor(distribution)) corresponds to a random sample. To override this behavior, set test_points_fn.

Usage

layer_kl_divergence_regularizer(
  object,
  distribution_b,
  use_exact_kl = FALSE,
  test_points_reduce_axis = NULL,
  test_points_fn = tf$convert_to_tensor,
  weight = NULL,
  ...
)

Arguments

- **object**: What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  - missing or NULL, the Layer instance is returned.
  - a Sequential model, the model with an additional layer is returned.
  - a Tensor, the output tensor from layer_instance(object) is returned.

- **distribution_b**: Distribution instance corresponding to b as in KL[a,b]. The previous layer’s output is presumed to be a Distribution instance and is a.

- **use_exact_kl**: Logical indicating if KL divergence should be calculated exactly via tfp$distributions$kl_divergence or via Monte Carlo approximation. Default value: FALSE.

- **test_points_reduce_axis**: Integer vector or scalar representing dimensions over which to reduce_mean while calculating the Monte Carlo approximation of the KL divergence. As is with all tf$reduce_* ops, NULL means reduce over all dimensions; () means reduce over none of them. Default value: () (i.e., no reduction).

- **test_points_fn**: A callable taking a tfp$distributions$Distribution instance and returning a tensor used for random test points to approximate the KL divergence. Default value: tf$convert_to_tensor.

- **weight**: Multiplier applied to the calculated KL divergence for each Keras batch member. Default value: NULL (i.e., do not weight each batch member).

- **...**: Additional arguments passed to args of keras::create_layer.
**layer_mixture_logistic**

A mixture distribution Keras layer, with independent logistic components.

### Description

A mixture distribution Keras layer, with independent logistic components.

### Usage

```r
layer_mixture_logistic(
  object,  # What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  num_components,  # Number of component distributions in the mixture distribution.
  event_shape = list(),  # integer vector Tensor representing the shape of single draw from this distribution.
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,  # A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.
  validate_args = FALSE,
  ...  # Other arguments.
)
```

### Arguments

- **object**
  - What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
    - missing or NULL, the Layer instance is returned.
    - a Sequential model, the model with an additional layer is returned.
    - a Tensor, the output tensor from layer_instance(object) is returned.

- **num_components**
  - Number of component distributions in the mixture distribution.

- **event_shape**
  - integer vector Tensor representing the shape of single draw from this distribution.

- **convert_to_tensor_fn**
  - A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.
layer_mixture_normal

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param Additional arguments passed to args of keras::create_layer.

... Additional arguments passed to args of keras::create_layer.

Value

a Keras layer

See Also

For an example how to use in a Keras model, see layer_independent_normal().

Other distribution_layers: layer_categorical_mixture_of_one_hot_categorical(), layer_distribution_lambda(), layer_independent_bernoulli(), layer_independent_logistic(), layer_independent_normal(), layer_independent_poisson(), layer_kl_divergence_add_loss(), layer_kl_divergence_regularizer(), layer_mixture_normal(), layer_mixture_same_family(), layer_multivariate_normal_tri_l(), layer_one_hot_categorical()

layer_mixture_normal A mixture distribution Keras layer, with independent normal components.

Description

A mixture distribution Keras layer, with independent normal components.

Usage

layer_mixture_normal(
  object,
  num_components,
  event_shape = list(),
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  validate_args = FALSE,
  ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:
  • missing or NULL, the Layer instance is returned.
  • a Sequential model, the model with an additional layer is returned.
  • a Tensor, the output tensor from layer_instance(object) is returned.
**layer_mixture_same_family**

A mixture (same-family) Keras layer.

**Description**

A mixture (same-family) Keras layer.

**Usage**

```r
layer_mixture_same_family(
  object,
  num_components,
  component_layer,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  validate_args = FALSE,
  ...
)
```
Arguments

**object**
What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on object. If object is:
- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from `layer_instance(object)` is returned.

**num_components**
Number of component distributions in the mixture distribution.

**component_layer**
Function that, given a tensor of shape `batch_shape + [num_components, component_params_size]`, returns a `tfd.Distribution`-like instance that implements the component distribution (with batch shape `batch_shape + [num_components]`) — e.g., a TFP distribution layer.

**convert_to_tensor_fn**
A callable that takes a `tfd$Distribution` instance and returns a `tf$Tensor`-like object. Default value: `tfd$distributions$Distribution$sample`.

**validate_args**
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE. @param ...
Additional arguments passed to args of `keras::create_layer`.

Value

a Keras layer

See Also

For an example how to use in a Keras model, see `layer_independent_normal()`. Other distribution layers: `layer_categorical_mixture_of_one_hot_categorical()`, `layer_distribution_lambda()`, `layer_independent_bernoulli()`, `layer_independent_logistic()`, `layer_independent_normal()`, `layer_independent_poisson()`, `layer_kl_divergence_add_loss()`, `layer_kl_divergence_regularizer()`, `layer_mixture_logistic()`, `layer_mixture_normal()`, `layer_multivariate_normal_tri_l()`, `layer_one_hot_categorical()`
layer_one_hot_categorical

Usage

layer_multivariate_normal_tri_l(
    object,
    event_size,
    convert_to_tensor_fn = tfp$distributions$Distribution$sample,
    validate_args = FALSE,
    ...
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

- missing or NULL, the Layer instance is returned.
- a Sequential model, the model with an additional layer is returned.
- a Tensor, the output tensor from layer_instance(object) is returned.

event_size Integer vector tensor representing the shape of single draw from this distribution.

convert_to_tensor_fn A callable that takes a tfd$Distribution instance and returns a tf$Tensor-like object. Default value: tfd$distributions$Distribution$sample.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

... Additional arguments passed to args of keras::create_layer.

Value

a Keras layer

See Also

For an example how to use in a Keras model, see layer_independent_normal().

Other distribution_layers: layer_categorical_mixture_of_one_hot_categorical(), layer_distribution_lambda(), layer_independent_bernoulli(), layer_independent_logistic(), layer_independent_normal(), layer_independent_poisson(), layer_kl_divergence_add_loss(), layer_kl_divergence_regularizer(), layer_mixture_logistic(), layer_mixture_normal(), layer_mixture_same_family(), layer_one_hot_categorical.
**Description**

Typical choices for `convert_to_tensor_fn` include:

- `tfp$distributions$Distribution$sample`
- `tfp$distributions$Distribution$mean`
- `tfp$distributions$Distribution$mode`
- `tfp$distributions$OneHotCategorical$logits`

**Usage**

```r
layer_one_hot_categorical(
  object,
  event_size,
  convert_to_tensor_fn = tfp$distributions$Distribution$sample,
  sample_dtype = NULL,
  validate_args = FALSE,
  ...
)
```

**Arguments**

- **object** What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by `layer_input()`). The return value depends on `object`. If `object` is:
  - missing or NULL, the Layer instance is returned.
  - a Sequential model, the model with an additional layer is returned.
  - a Tensor, the output tensor from `layer_instance(object)` is returned.

- **event_size** Scalar integer representing the size of single draw from this distribution.

- **convert_to_tensor_fn** A callable that takes a `tfd$Distribution` instance and returns a `tf$Tensor-like` object. Default value: `tfd$distributions$Distribution$sample`.

- **sample_dtype** dtype of samples produced by this distribution. Default value: NULL (i.e., previous layer's dtype).

- **validate_args** Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **...** Additional arguments passed to `args` of `keras::create_layer`.

**Value**

a Keras layer
**See Also**

For an example how to use in a Keras model, see \texttt{layer_independent_normal()}. Other distribution layers: \texttt{layer_categorical_mixture_of_one_hot_categorical()}, \texttt{layer_distribution_lambda()}, \texttt{layer_independent_bernoulli()}, \texttt{layer_independent_logistic()}, \texttt{layer_independent_normal()}, \texttt{layer_independent_poisson()}, \texttt{layer_kl_divergence_add_loss()}, \texttt{layer_kl_divergence_regularizer()}, \texttt{layer_mixture_logistic()}, \texttt{layer_mixture_normal()}, \texttt{layer_mixture_same_family()}, \texttt{layer_multivariate_normal()}

---

**layer\_variable**

**Variable Layer**

**Description**

Simply returns a (trainable) variable, regardless of input. This layer implements the mathematical function $f(x) = c$ where $c$ is a constant, i.e., unchanged for all $x$. Like other Keras layers, the constant is trainable. This layer can also be interpreted as the special case of \texttt{layer\_dense()} when the kernel is forced to be the zero matrix (\texttt{tf$\$zeros}).

**Usage**

```r
layer\_variable(
  object,
  shape,
  dtype = NULL,
  activation = NULL,
  initializer = "zeros",
  regularizer = NULL,
  constraint = NULL,
  ...
)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>object</td>
<td>What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by \texttt{layer_input()}). The return value depends on object. If object is:</td>
</tr>
<tr>
<td></td>
<td>- missing or NULL, the Layer instance is returned.</td>
</tr>
<tr>
<td></td>
<td>- a Sequential model, the model with an additional layer is returned.</td>
</tr>
<tr>
<td></td>
<td>- a Tensor, the output tensor from \texttt{layer_instance(object)} is returned.</td>
</tr>
<tr>
<td>shape</td>
<td>integer or integer vector specifying the shape of the output of this layer.</td>
</tr>
<tr>
<td>dtype</td>
<td>TensorFlow dtype of the variable created by this layer.</td>
</tr>
<tr>
<td>activation</td>
<td>An activation function. See \texttt{keras::layer_dense}. Default: NULL.</td>
</tr>
<tr>
<td>initializer</td>
<td>Initializer for the constant vector.</td>
</tr>
<tr>
<td>regularizer</td>
<td>Regularizer function applied to the constant vector.</td>
</tr>
<tr>
<td>constraint</td>
<td>Constraint function applied to the constant vector.</td>
</tr>
<tr>
<td>...</td>
<td>Additional keyword arguments passed to the \texttt{keras::layer_dense} constructed by this layer.</td>
</tr>
</tbody>
</table>
layer_variational_gaussian_process

Value

A Keras layer

See Also

Other layers: layer_autoregressive(), layer_conv_1d_flipout(), layer_conv_1d_reparameterization(), layer_conv_2d_flipout(), layer_conv_2d_reparameterization(), layer_conv_3d_flipout(), layer_conv_3d_reparameterization(), layer_dense_flipout(), layer_dense_local_reparameterization(), layer_dense_reparameterization(), layer_dense_variational()

layer_variational_gaussian_process

A Variational Gaussian Process Layer.

Description

Create a Variational Gaussian Process distribution whose index_points are the inputs to the layer. Parameterized by number of inducing points and a kernel_provider, which should be a tf.keras.Layer with an @property that late-binds variable parameters to a tfp.positive_semidefinite_kernel.PositiveSemidefiniteKernel instance (this requirement has to do with the way that variables must be created in a keras model). The mean_fn is an optional argument which, if omitted, will be automatically configured to be a constant function with trainable variable output.

Usage

layer_variational_gaussian_process(
    object,
    num_inducing_points,
    kernel_provider,
    event_shape = 1,
    inducing_index_points_initializer = NULL,
    unconstrained_observation_noise_variance_initializer = NULL,
    mean_fn = NULL,
    jitter = 1e-06,
    name = NULL
)

Arguments

object What to compose the new Layer instance with. Typically a Sequential model or a Tensor (e.g., as returned by layer_input()). The return value depends on object. If object is:

• missing or NULL, the Layer instance is returned.
• a Sequential model, the model with an additional layer is returned.
• a Tensor, the output tensor from layer_instance(object) is returned.
num_inducing_points

number of inducing points in the Variational Gaussian Process distribution.

kernel_provider

a Layer instance equipped with an @property, which yields a PositiveSemidefiniteKernel instance. The latter is used to parametrize the constructed Variational Gaussian Process distribution returned by calling the layer.

event_shape

the shape of the output of the layer. This translates to a batch of underlying Variational Gaussian Process distributions. For example, event_shape = 3 means we are modelling a batch of 3 distributions over functions. We can think of this as a distribution over 3-dimensional vector-valued functions.

inducing_index_points_initializer

a tf.keras.initializer.Initializer used to initialize the trainable inducing_index_points variables. Training VGP’s is pretty sensitive to choice of initial inducing index point locations. A reasonable heuristic is to scatter them near the data, not too close to each other.

unconstrained_observation_noise_variance_initializer

a tf.keras.initializer.Initializer used to initialize the unconstrained observation noise variable. The observation noise variance is computed from this variable via the tf.nn.softplus function.

mean_fn

a callable that maps layer inputs to mean function values. Passed to the mean_fn parameter of Variational Gaussian Process distribution. If omitted, defaults to a constant function with trainable variable value.

jitter

a small term added to the diagonal of various kernel matrices for numerical stability.

name

name to give to this layer and the scope of ops and variables it contains.

Value

a Keras layer

---

mcmc_dual_averaging_step_size_adaptation

Adapts the inner kernel's step_size based on log_accept_prob.

---

Description

The dual averaging policy uses a noisy step size for exploration, while averaging over tuning steps to provide a smoothed estimate of an optimal value. It is based on section 3.2 of Hoffman and Gelman (2013), which modifies the stochastic convex optimization scheme of Nesterov (2009). The modified algorithm applies extra weight to recent iterations while keeping the convergence guarantees of Robbins-Monro, and takes care not to make the step size too small too quickly when maintaining a constant trajectory length, to avoid expensive early iterations. A good target acceptance probability depends on the inner kernel. If this kernel is HamiltonianMonteCarlo, then 0.6-0.9 is a good range to aim for. For RandomWalkMetropolis this should be closer to 0.25. See the individual kernels' docstrings for guidance.
Usage

mcmc_dual_averaging_step_size_adaptation(
    inner_kernel,
    num_adaptation_steps,
    target_accept_prob = 0.75,
    exploration_shrinkage = 0.05,
    step_count_smoothing = 10,
    decay_rate = 0.75,
    step_size_setter_fn = NULL,
    step_size_getter_fn = NULL,
    log_accept_prob_getter_fn = NULL,
    validate_args = FALSE,
    name = NULL
)

Arguments

inner_kernel  TransitionKernel-like object.
num_adaptation_steps
    Scalar integer Tensor number of initial steps to during which to adjust the step
    size. This may be greater, less than, or equal to the number of burnin steps.
target_accept_prob
    A floating point Tensor representing desired acceptance probability. Must be a
    positive number less than 1. This can either be a scalar, or have shape [num_chains].
    Default value: 0.75 (the center of asymptotically optimal rate for HMC).
exploration_shrinkage
    Floating point scalar Tensor. How strongly the exploration rate is biased to-
    wards the shrinkage target.
step_count_smoothing
    Int32 scalar Tensor. Number of "pseudo-steps" added to the number of steps
    taken to prevents noisy exploration during the early samples.
decay_rate
    Floating point scalar Tensor. How much to favor recent iterations over earlier
    ones. A value of 1 gives equal weight to all history.
step_size_setter_fn
    A function with the signature (kernel_results, new_step_size) -> new_kernel_results
    where kernel_results are the results of the inner_kernel, new_step_size is a Tensor or a
    nested collection of Tensors with the same structure as returned by the step_size_getter_fn,
    and new_kernel_results are a copy of kernel_results with the step size(s) set.
step_size_getter_fn
    A callable with the signature (kernel_results) -> step_size where kernel_results
    are the results of the inner_kernel, and step_size is a floating point Tensor or a
    nested collection of such Tensors.
log_accept_prob_getter_fn
    A callable with the signature (kernel_results) -> log_accept_prob where
    kernel_results are the results of the inner_kernel, and log_accept_prob is
    a floating point Tensor. log_accept_prob can either be a scalar, or have shape
[num_chains]. If it’s the latter, step_size should also have the same leading dimension.

validate_args logical. When TRUE kernel parameters are checked for validity. When FALSE invalid inputs may silently render incorrect outputs.

name name prefixed to Ops created by this function. Default value: NULL (i.e., ‘dual_averaging_step_size_adaptation’).

Details

In general, adaptation prevents the chain from reaching a stationary distribution, so obtaining consistent samples requires num_adaptation_steps be set to a value somewhat smaller than the number of burnin steps. However, it may sometimes be helpful to set num_adaptation_steps to a larger value during development in order to inspect the behavior of the chain during adaptation. The step size is assumed to broadcast with the chain state, potentially having leading dimensions corresponding to multiple chains. When there are fewer of those leading dimensions than there are chain dimensions, the corresponding dimensions in the log_accept_prob are averaged (in the direct space, rather than the log space) before being used to adjust the step size. This means that this kernel can do both cross-chain adaptation, or per-chain step size adaptation, depending on the shape of the step size. For example, if your problem has a state with shape [S], your chain state has shape [C0, C1, S] (meaning that there are C0 * C1 total chains) and log_accept_prob has shape [C0, C1] (one acceptance probability per chain), then depending on the shape of the step size, the following will happen:

• Step size has shape [], [S] or [1], the log_accept_prob will be averaged across its C0 and C1 dimensions. This means that you will learn a shared step size based on the mean acceptance probability across all chains. This can be useful if you don’t have a lot of steps to adapt and want to average away the noise.

• Step size has shape [C1, 1] or [C1, S], the log_accept_prob will be averaged across its C0 dimension. This means that you will learn a shared step size based on the mean acceptance probability across chains that share the coordinate across the C1 dimension. This can be useful when the C1 dimension indexes different distributions, while C0 indexes replicas of a single distribution, all sampled in parallel.

• Step size has shape [C0, C1, 1] or [C0, C1, S], then no averaging will happen. This means that each chain will learn its own step size. This can be useful when all chains are sampling from different distributions. Even when all chains are for the same distribution, this can help during the initial warmup period.

• Step size has shape [C0, 1, 1] or [C0, 1, S], the log_accept_prob will be averaged across its C1 dimension. This means that you will learn a shared step size based on the mean acceptance probability across chains that share the coordinate across the C0 dimension. This can be useful when the C0 dimension indexes different distributions, while C1 indexes replicas of a single distribution, all sampled in parallel.

Value

a Monte Carlo sampling kernel
mcmc_effective_sample_size

References


See Also

For an example how to use see mcmc_no_u_turn_sampler().

Other mcmc_kernels: mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()
filter_beyond_lag

Tensor or list of Tensor objects. Must be int-like and scalar valued. The auto-
correlation sequence is truncated to this length. Setting to NULL means we do
not filter based on number of lags.

name

name to prepend to created ops.

Details

More precisely, given a stationary sequence of possibly correlated random variables $X_1, X_2, \ldots, X_N$, each identically distributed ESS is the number such that $\text{Variance}\left(\frac{N^{-1} \times \sum X_i}{\text{ESS}}\right) = ESS^{-1} \times \text{Variance}\left( X_1 \right)$.

If the sequence is uncorrelated, $ESS = N$. In general, one should expect $ESS \leq N$, with more highly correlated sequences having smaller $ESS$.

Value

Tensor or list of Tensor objects. The effective sample size of each component of states. Shape will be states$\text{shape}[1:]$.

See Also

Other mcmc_functions: mcmc_potential_scale_reduction(), mcmc_sample_annealed_importance_chain(), mcmc_sample_chain(), mcmc_sample_halton_sequence()
Arguments

**target_log_prob_fn**
Function which takes an argument like `current_state` (if it's a list `current_state` will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.

**step_size**
Tensor or list of Tensors representing the step size for the leapfrog integrator. Must broadcast with the shape of `current_state`. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. When possible, it's often helpful to match per-variable step sizes to the standard deviations of the target distribution in each variable.

**num_leapfrog_steps**
Integer number of steps to run the leapfrog integrator for. Total progress per HMC step is roughly proportional to `step_size * num_leapfrog_steps`.

**state_gradients_are_stopped**
Logical indicating that the proposed new state be run through `tf$stop_gradient`. This is particularly useful when combining optimization over samples from the HMC chain. Default value: FALSE (i.e., do not apply `stop_gradient`).

**step_size_update_fn**
Function taking current `step_size` (typically a `tf$Variable`) and `kernel_results` (typically `collections$namedtuple`) and returns updated `step_size` (Tensors). Default value: NULL (i.e., do not update `step_size` automatically).

**seed**
integer to seed the random number generator.

**store_parameters_in_results**
If TRUE, then `step_size` and `num_leapfrog_steps` are written to and read from eponymous fields in the kernel results objects returned from `one_step` and `bootstrap_results`. This allows wrapper kernels to adjust those parameters on the fly. This is incompatible with `step_size_update_fn`, which must be set to NULL.

**name**
string prefixed to Ops created by this function. Default value: NULL (i.e., 'hmc_kernel').

Details

The `one_step` function can update multiple chains in parallel. It assumes that all leftmost dimensions of `current_state` index independent chain states (and are therefore updated independently). The output of `target_log_prob_fn(current_state)` should sum log-probabilities across all event dimensions. Slices along the rightmost dimensions may have different target distributions; for example, `current_state[0, :]` could have a different target distribution from `current_state[1, :]`. These semantics are governed by `target_log_prob_fn(current_state)`. (The number of independent chains is `tf$size(target_log_prob_fn(current_state))`.)

Value

a Monte Carlo sampling kernel

References

mcmc_metropolis_adjusted_langevin_algorithm


**See Also**

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()

---

mcmc_metropolis_adjusted_langevin_algorithm

*Runs one step of Metropolis-adjusted Langevin algorithm.*

**Description**

Metropolis-adjusted Langevin algorithm (MALA) is a Markov chain Monte Carlo (MCMC) algorithm that takes a step of a discretised Langevin diffusion as a proposal. This class implements one step of MALA using Euler-Maruyama method for a given current_state and diagonal preconditioning volatility matrix.

**Usage**

```python
mcmc_metropolis_adjusted_langevin_algorithm(
  target_log_prob_fn,
  step_size,
  volatility_fn = NULL,
  seed = NULL,
  parallel_iterations = 10,
  name = NULL
)
```

**Arguments**

- `target_log_prob_fn`  
  Function which takes an argument like current_state (if it’s a list current_state will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.

- `step_size`  
  Tensor or list of Tensors representing the step size for the leapfrog integrator. Must broadcast with the shape of current_state. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. When possible, it’s often helpful to match per-variable step sizes to the standard deviations of the target distribution in each variable.

- `volatility_fn`  
  function which takes an argument like current_state (or *current_state if it’s a list) and returns volatility value at current_state. Should return a Tensor or list of Tensors that must broadcast with the shape of current_state. Defaults to the identity function.
mcmc_metropolis_hastings

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>seed</td>
<td>integer to seed the random number generator.</td>
</tr>
<tr>
<td>parallel_iterations</td>
<td>the number of coordinates for which the gradients of the volatility matrix volatility_fn can be computed in parallel.</td>
</tr>
<tr>
<td>name</td>
<td>String prefixed to Ops created by this function. Default value: NULL (i.e., 'mala_kernel').</td>
</tr>
</tbody>
</table>

Details

Mathematical details and derivations can be found in Roberts and Rosenthal (1998) and Xifara et al. (2013).

The one_step function can update multiple chains in parallel. It assumes that all leftmost dimensions of current_state index independent chain states (and are therefore updated independently). The output of target_log_prob_fn(current_state) should reduce log-probabilities across all event dimensions. Slices along the rightmost dimensions may have different target distributions; for example, current_state[0, :] could have a different target distribution from current_state[1, :]. These semantics are governed by target_log_prob_fn(current_state). (The number of independent chains is tf.size(target_log_prob_fn(current_state)).)

References


See Also

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()

---

**mcmc_metropolis_hastings**

Runs one step of the Metropolis-Hastings algorithm.

**Description**

The Metropolis-Hastings algorithm is a Markov chain Monte Carlo (MCMC) technique which uses a proposal distribution to eventually sample from a target distribution.

**Usage**

mcmc_metropolis_hastings(inner_kernel, seed = NULL, name = NULL)
**Arguments**

- **inner_kernel** TransitionKernel-like object which has collections$namedtuple kernel_results and which contains a target_log_prob member and optionally a log_acceptance_correction member.
- **seed** integer to seed the random number generator.
- **name** string prefixed to Ops created by this function. Default value: NULL (i.e., "mh_kernel").

**Details**

Note: inner_kernel$one_step must return kernel_results as a collections$namedtuple which must:

- have a target_log_prob field,
- optionally have a log_acceptance_correction field, and,
- have only fields which are Tensor-valued.

The Metropolis-Hastings log acceptance-probability is computed as:

\[
\text{log_accept_ratio} = (\text{current_kernel_results}.\text{target_log_prob} - \text{previous_kernel_results}.\text{target_log_prob} + \text{current_kernel_results}.\text{log_acceptance_correction})
\]

If current_kernel_results$log_acceptance_correction does not exist, it is presumed 0 (i.e., that the proposal distribution is symmetric). The most common use-case for log_acceptance_correction is in the Metropolis-Hastings algorithm, i.e.,

\[
\text{accept_prob}(x' | x) = \frac{p(x')}{p(x)} \left( \frac{g(x|x')}{g(x'|x)} \right)
\]

where,
- \(p\) represents the target distribution,
- \(g\) represents the proposal (conditional) distribution,
- \(x'\) is the proposed state, and,
- \(x\) is current state

The log of the parenthetical term is the log_acceptance_correction. The log_acceptance_correction may not necessarily correspond to the ratio of proposal distributions, e.g, log_acceptance_correction has a different interpretation in Hamiltonian Monte Carlo.

**Value**

a Monte Carlo sampling kernel

**See Also**

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()
mcmc_no_u_turn_sampler

*Runs one step of the No U-Turn Sampler*

**Description**

The No U-Turn Sampler (NUTS) is an adaptive variant of the Hamiltonian Monte Carlo (HMC) method for MCMC. NUTS adapts the distance traveled in response to the curvature of the target density. Conceptually, one proposal consists of reversibly evolving a trajectory through the sample space, continuing until that trajectory turns back on itself (hence the name, 'No U-Turn'). This class implements one random NUTS step from a given `current_state`. Mathematical details and derivations can be found in Hoffman & Gelman (2011).

**Usage**

```r
mcmc_no_u_turn_sampler(
  target_log_prob_fn,
  step_size,
  max_tree_depth = 10,
  max_energy_diff = 1000,
  unrolled_leapfrog_steps = 1,
  seed = NULL,
  name = NULL
)
```

**Arguments**

- `target_log_prob_fn` function which takes an argument like `current_state` and returns its (possibly unnormalized) log-density under the target distribution.
- `step_size` Tensor or list of Tensors representing the step size for the leapfrog integrator. Must broadcast with the shape of `current_state`. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. When possible, it's often helpful to match per-variable step sizes to the standard deviations of the target distribution in each variable.
- `max_tree_depth` Maximum depth of the tree implicitly built by NUTS. The maximum number of leapfrog steps is bounded by \(2^{ \text{max\_tree\_depth}}\) i.e. the number of nodes in a binary tree \(\text{max\_tree\_depth}\) nodes deep. The default setting of 10 takes up to 1024 leapfrog steps.
- `max_energy_diff` Scaler threshold of energy differences at each leapfrog, divergence samples are defined as leapfrog steps that exceed this threshold. Default to 1000.
- `unrolled_leapfrog_steps` The number of leapfrogs to unroll per tree expansion step. Applies a direct linear multiplier to the maximum trajectory length implied by `max_tree_depth`. Defaults to 1.
seed  integer to seed the random number generator.
name   name prefixed to Ops created by this function. Default value: NULL (i.e., 'nuts_kernel').

Details

The one_step function can update multiple chains in parallel. It assumes that a prefix of leftmost
dimensions of current_state index independent chain states (and are therefore updated inde-
pendently). The output of target_log_prob_fn(current_state) should sum log-probabilities
across all event dimensions. Slices along the rightmost dimensions may have different target
distributions; for example, current_state[0][0,...] could have a different target distribution from
current_state[0][1,...]. These semantics are governed by target_log_prob_fn(*current_state).
(The number of independent chains is tf$size(target_log_prob_fn(current_state)).)

Value

a Monte Carlo sampling kernel

References

- Matthew D. Hoffman, Andrew Gelman. The No-U-Turn Sampler: Adaptively Setting Path
  Lengths in Hamiltonian Monte Carlo. 2011.

See Also

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(),
mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_random_walk_metropolis(),
mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(),
mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(),
mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()

Examples

predictors <- tf$cast(c(201,244, 47,287,203,58,210,202,198,158,165,201,157,
                        131,166,160,186,125,218,146),tf$float32)
obs <- tf$cast(c(592,401,583,402,495,173,479,504,510,416,393,442,317,311,400,
                 337,423,334,533,344),tf$float32)
y_sigma <- tf$cast(c(61,25,38,15,21,15,27,14,30,16,14,25,52,16,34,31,42,26,
                    16,22),tf$float32)

# Robust linear regression model
robust_lm <- tfd_joint_distribution_sequential(
  list(
    tfd_normal(loc = 0, scale = 1, name = "b0"),
    tfd_normal(loc = 0, scale = 1, name = "b1"),
    tfd_half_normal(5, name = "df"),
    function(df, b1, b0)
      tfd_independent(
        tfd_student_t(
          # Likelihood
tf$expand_dims(df, axis = -1L),
```r
loc = tf\$expand_dims(b0, axis = -1L) +
    tf\$expand_dims(b1, axis = -1L) * predictors[tf\$newaxis, ],
scale = y_sigma,
name = "st"
), name = "ind"), validate_args = TRUE)

log_prob <- function(b0, b1, df) {robust_lm \%\%
    tfd_log_prob(list(b0, b1, df, obs))}
step_size0 <- Map(function(x) tf\$cast(x, tf\$float32), c(1, .2, .5))
number_of_steps <- 10
burnin <- 5
nchain <- 50

run_chain <- function() {
  # random initialization of the starting position of each chain
  samples <- robust_lm \%\% tfd_sample(nchain)
  b0 <- samples[[1]]
  b1 <- samples[[2]]
  df <- samples[[3]]

  # bijector to map constrained parameters to real
  unconstraining_bijectors <- list(
    tfb_identity(), tfb_identity(), tfb_exp())

  trace_fn <- function(x, pkr) {
    list(pkr$inner_results$inner_results$step_size,
         pkr$inner_results$inner_results$log_accept_ratio)
  }

  nuts <- mcmc_no_u_turn_sampler(
    target_log_prob_fn = log_prob,
    step_size = step_size0
  ) \%\%
  mcmc_transformed_transition_kernel(bijector = unconstraining_bijectors) \%\%
  mcmc_dual_averaging_step_size_adaptation(
    num_adaptation_steps = burnin,
    step_size_setter_fn = function(pkr, new_step_size)
      pkr$\_replace(
        inner_results = pkr$inner_results$\_replace(step_size = new_step_size),
        step_size_getter_fn = function(pkr) pkr$inner_results$step_size,
        log_accept_prob_getter_fn = function(pkr) pkr$inner_results$log_accept_ratio
      )
  ) \%\%
  mcmc_sample_chain(
    num_results = number_of_steps,
    num_burnin_steps = burnin,
    current_state = list(b0, b1, df),
    trace_fn = trace_fn
  )

  run_chain <- tensorflow::tf_function(run_chain)
  res <- run_chain()
```
Gelman and Rubin (1992)’s potential scale reduction for chain convergence.

**Description**

Given \( N > 1 \) states from each of \( C > 1 \) independent chains, the potential scale reduction factor, commonly referred to as R-hat, measures convergence of the chains (to the same target) by testing for equality of means.

**Usage**

```r
mcmc_potential_scale_reduction(
  chains_states,
  independent_chain_ndims = 1,
  name = NULL
)
```

**Arguments**

- `chains_states` Tensor or list of Tensors representing the state(s) of a Markov Chain at each result step. The \( i \)th state is assumed to have shape \([N_i, C_1, C_2, \ldots, C_D] + A\). Dimension 0 indexes the \( N_i > 1 \) result steps of the Markov Chain. Dimensions 1 through \( D \) index the \( C_1 \times \ldots \times C_D \) independent chains to be tested for convergence to the same target. The remaining dimensions, \( A \), can have any shape (even empty).
- `independent_chain_ndims` Integer type Tensor with value \( \geq 1 \) giving the number of dimensions, from \( \text{dim} = 1 \) to \( \text{dim} = D \), holding independent chain results to be tested for convergence.
- `name` name to prepend to created tf. Default: `potential_scale_reduction`.

**Details**

Specifically, R-hat measures the degree to which variance (of the means) between chains exceeds what one would expect if the chains were identically distributed. See Gelman and Rubin (1992), Brooks and Gelman (1998).

Some guidelines:

- The initial state of the chains should be drawn from a distribution overdispersed with respect to the target.
- If all chains converge to the target, then as \( N \to \infty \), R-hat \( \to 1 \). Before that, R-hat > 1 (except in pathological cases, e.g. if the chain paths were identical).
• The above holds for any number of chains \( C > 1 \). Increasing \( C \) improves effectiveness of the diagnostic.

• Sometimes, R-hat < 1.2 is used to indicate approximate convergence, but of course this is problem dependent. See Brooks and Gelman (1998).

• R-hat only measures non-convergence of the mean. If higher moments, or other statistics are desired, a different diagnostic should be used. See Brooks and Gelman (1998).

To see why R-hat is reasonable, let \( X \) be a random variable drawn uniformly from the combined states (combined over all chains). Then, in the limit \( N, C \to \infty \), with \( E, \text{Var} \) denoting expectation and variance, \( \text{R-hat} = \frac{E[\text{Var}[X | \text{chain}]] + \text{Var}[E[X | \text{chain}]]}{E[\text{Var}[X | \text{chain}]]} \). Using the law of total variance, the numerator is the variance of the combined states, and the denominator is the total variance minus the variance of the the individual chain means. If the chains are all drawing from the same distribution, they will have the same mean, and thus the ratio should be one.

Value

Tensor or list of Tensors representing the R-hat statistic for the state(s). Same dtype as state, and shape equal to state$shape[1 + independent\_chain\_ndims:]$.

References


See Also

Other mcmc_functions: mcmc_effective_sample_size(), mcmc_sample_annealed_importance_chain(), mcmc_sample_chain(), mcmc_sample_halton_sequence()
Usage

\[
\text{mcmc_random_walk_metropolis(}
\text{target_log_prob_fn,}
\text{new_state_fn = NULL,}
\text{seed = NULL,}
\text{name = NULL)}
\]

Arguments

target_log_prob_fn

Function which takes an argument like \text{current_state} ((if it's a list \text{current_state}
will be unpacked) and returns its (possibly unnormalized) log-density under the
target distribution.

new_state_fn

Function which takes a list of state parts and a seed; returns a same-type list
of Tensors, each being a perturbation of the input state parts. The perturbation
distribution is assumed to be a symmetric distribution centered at the input state
part. Default value: NULL which is mapped to \text{tfp$random_walk_normal_fn()}.

seed

integer to seed the random number generator.

name

String name prefixed to Ops created by this function. Default value: NULL (i.e.,
'rwm_kernel').

Details

The current class implements RWM for normal and uniform proposals. Alternatively, the user can
supply any custom proposal generating function. The function \text{one_step} can update multiple chains
in parallel. It assumes that all leftmost dimensions of \text{current_state} index independent chain
states (and are therefore updated independently). The output of \text{target_log_prob_fn(current_state)}
should sum log-probabilities across all event dimensions. Slices along the rightmost dimensions
may have different target distributions; for example, \text{current_state}[0, :] could have a different target
distribution from \text{current_state}[1, :]. These semantics are governed by \text{target_log_prob_fn(current_state)}.
(The number of independent chains is \text{tf$size(target_log_prob_fn(current_state))}.)

Value

a Monte Carlo sampling kernel

See Also

Other \text{mcmc_kernels}: \text{mcmc_dual_averaging_step_size_adaptation()}, \text{mcmc_hamiltonian_monte_carlo()},
\text{mcmc_metropolis_adjusted_langevin_algorithm()}, \text{mcmc_metropolis_hastings()}, \text{mcmc_no_u_turn_sampler()},
\text{mcmc_replica_exchange_mc()}, \text{mcmc_simple_step_size_adaptation()}, \text{mcmc_slice_sampler()},
\text{mcmc_transformed_transition_kernel()}, \text{mcmc_uncalibrated_hamiltonian_monte_carlo()},
\text{mcmc_uncalibrated_langevin()}, \text{mcmc_uncalibrated_random_walk()}. 
mcmc_replica_exchange_mc

Runs one step of the Replica Exchange Monte Carlo

Description

Replica Exchange Monte Carlo is a Markov chain Monte Carlo (MCMC) algorithm that is also known as Parallel Tempering. This algorithm performs multiple sampling with different temperatures in parallel, and exchanges those samplings according to the Metropolis-Hastings criterion. The \( K \) replicas are parameterized in terms of inverse temperature’s, \((\beta[0], \beta[1], \ldots, \beta[K-1])\). If the target distribution has probability density \( p(x) \), the \( k \)th replica has density \( p(x)^{\beta_k} \).

Usage

```r
mcmc_replica_exchange_mc(
  target_log_prob_fn,
  inverse_temperatures,
  make_kernel_fn,
  swap_proposal_fn = tfp$mcmc$replica_exchange_mc$default_swap_proposal_fn(1),
  state_includes_replicas = FALSE,
  seed = NULL,
  name = NULL
)
```

Arguments

- `target_log_prob_fn`: Function which takes an argument like `current_state` (if it’s a list `current_state` will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.
- `inverse_temperatures`: 1D Tensor of inverse temperatures to perform samplings with each replica. Must have statically known shape. `inverse_temperatures[0]` produces the states returned by samplers, and is typically == 1.
- `make_kernel_fn`: Function which takes `target_log_prob_fn` and `seed` args and returns a TransitionKernel instance.
- `swap_proposal_fn`: function which take a number of replicas, and return combinations of replicas for exchange.
- `state_includes_replicas`: Boolean indicating whether the leftmost dimension of each state sample should index replicas. If TRUE, the leftmost dimension of the `current_state` kwarg to `tfp.mcmc.sample_chain` will be interpreted as indexing replicas.
- `seed`: integer to seed the random number generator.
- `name`: string prefixed to Ops created by this function. Default value: NULL (i.e., "remc_kernel").
mcmc_sample_annealed_importance_chain

Details

Typically beta[0] = 1.0, and 1.0 > beta[1] > beta[2] > ... > 0.0.

- beta[0] == 1 ==> First replicas samples from the target density, \( p \).
- beta[k] < 1, for k = 1, ..., K-1 ==> Other replicas sample from "flattened" versions of \( p \) (peak is less high, valley less low). These distributions are somewhat closer to a uniform on the support of \( p \). Samples from adjacent replicas \( i, i + 1 \) are used as proposals for each other in a Metropolis step. This allows the lower beta samples, which explore less dense areas of \( p \), to occasionally be used to help the beta == 1 chain explore new regions of the support. Samples from replica 0 are returned, and the others are discarded.

Value

- list of next_state (Tensor or Python list of Tensors representing the state(s) of the Markov chain(s) at each result step. Has same shape as and current_state.) and
- kernel_results (collections$namedtuple of internal calculations used to 'advance the chain).

See Also

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()

mcmc_sample_annealed_importance_chain

Runs annealed importance sampling (AIS) to estimate normalizing constants.

Description

This function uses an MCMC transition operator (e.g., Hamiltonian Monte Carlo) to sample from a series of distributions that slowly interpolates between an initial "proposal" distribution: \( \exp(\text{proposal\_log\_prob\_fn}(x) - \text{proposal\_log\_normalizer}) \) and the target distribution: \( \exp(\text{target\_log\_prob\_fn}(x) - \text{target\_log\_normalizer}) \), accumulating importance weights along the way. The product of these importance weights gives an unbiased estimate of the ratio of the normalizing constants of the initial distribution and the target distribution: \( \mathbb{E}[\exp(\text{ais\_weights})] = \exp(\text{target\_log\_normalizer} - \text{proposal\_log\_normalizer}) \).

Usage

mcmc_sample_annealed_importance_chain(
    num_steps,
    proposal_log_prob_fn,
    target_log_prob_fn,
    current_state,
    make_kernel_fn,
parallel_iterations = 10,
name = NULL
)

Arguments

num_steps
Integer number of Markov chain updates to run. More iterations means more expense, but smoother annealing between q and p, which in turn means exponentially lower variance for the normalizing constant estimator.

proposal_log_prob_fn
function that returns the log density of the initial distribution.

target_log_prob_fn
function which takes an argument like current_state and returns its (possibly unnormalized) log-density under the target distribution.

current_state
Tensor or list of Tensors representing the current state(s) of the Markov chain(s). The first r dimensions index independent chains, r = tf$rank(target_log_prob_fn(current_state)).

make_kernel_fn
function which returns a TransitionKernel-like object. Must take one argument representing the TransitionKernel's target_log_prob_fn. The target_log_prob_fn argument represents the TransitionKernel's target log distribution. Note: sample_annealed_importance_chain creates a new target_log_prob_fn which is an interpolation between the supplied target_log_prob_fn and proposal_log_prob_fn; it is this interpolated function which is used as an argument to make_kernel_fn.

parallel_iterations
The number of iterations allowed to run in parallel. It must be a positive integer. See tf$while_loop for more details.

name
string prefixed to Ops created by this function. Default value: NULL (i.e., "sample_annealed_importance_chain").

Details
Note: When running in graph mode, proposal_log_prob_fn and target_log_prob_fn are called exactly three times (although this may be reduced to two times in the future).

Value
list of next_state (Tensor or Python list of Tensors representing the state(s) of the Markov chain(s) at the final iteration. Has same shape as input current_state), ais_weights (Tensor with the estimated weight(s). Has shape matching target_log_prob_fn(current_state)), and kernel_results (collections.namedtuple of internal calculations used to advance the chain).

See Also
For an example how to use see mcmc_sample_chain().

Other mcmc_functions: mcmc_effective_sample_size(), mcmc_potential_scale_reduction(), mcmc_sample_chain(), mcmc_sample_halton_sequence()
mcmc_sample_chain

Implements Markov chain Monte Carlo via repeated TransitionKernel steps.

Description

This function samples from an Markov chain at current_state and whose stationary distribution is governed by the supplied TransitionKernel instance (kernel).

Usage

```r
mcmc_sample_chain(
  kernel = NULL,
  num_results,
  current_state,
  previous_kernel_results = NULL,
  num_burnin_steps = 0,
  num_steps_between_results = 0,
  trace_fn = NULL,
  return_final_kernel_results = FALSE,
  parallel_iterations = 10,
  seed = NULL,
  name = NULL
)
```

Arguments

- **kernel**: An instance of `tfp$mcmc$TransitionKernel` which implements one step of the Markov chain.
- **num_results**: Integer number of Markov chain draws.
- **current_state**: Tensor or list of Tensors representing the current state(s) of the Markov chain(s).
- **previous_kernel_results**: A Tensor or a nested collection of Tensors representing internal calculations made within the previous call to this function (or as returned by `bootstrap_results`).
- **num_burnin_steps**: Integer number of chain steps to take before starting to collect results. Default value: 0 (i.e., no burn-in).
- **num_steps_between_results**: Integer number of chain steps between collecting a result. Only one out of every `num_steps_between_samples + 1` steps is included in the returned results. The number of returned chain states is still equal to `num_results`. Default value: 0 (i.e., no thinning).
- **trace_fn**: A function that takes in the current chain state and the previous kernel results and return a Tensor or a nested collection of Tensors that is then traced along with the chain state.
return_final_kernel_results
    If TRUE, then the final kernel results are returned alongside the chain state and
    the trace specified by the trace_fn.

parallel_iterations
    The number of iterations allowed to run in parallel. It must be a positive integer.
    See tf$while_loop for more details.

seed
    Optional, a seed for reproducible sampling.

name
    string prefixed to Ops created by this function. Default value: NULL, (i.e.,
    "mcmc_sample_chain").

Details

This function can sample from multiple chains, in parallel. (Whether or not there are multiple
chains is dictated by the kernel.)

The current_state can be represented as a single Tensor or a list of Tensors which collectively represent the current state. Since MCMC states are correlated, it is sometimes desirable to produce additional intermediate states, and then discard them, ending up with a set of states with decreased autocorrelation. See Owen (2017). Such “thinning” is made possible by setting num_steps_between_results > 0. The chain then takes num_steps_between_results extra steps between the steps that make it into the results. The extra steps are never materialized (in calls to sess$run), and thus do not increase memory requirements.

Warning: when setting a seed in the kernel, ensure that sample_chain’s parallel_iterations=1, otherwise results will not be reproducible. In addition to returning the chain state, this function supports tracing of auxiliary variables used by the kernel. The traced values are selected by specifying trace_fn. By default, all kernel results are traced but in the future the default will be changed to no results being traced, so plan accordingly. See below for some examples of this feature.

Value

list of:

- checkpointable_states_and_trace: if return_final_kernel_results is TRUE. The return value is an instance of CheckpointableStatesAndTrace.
- all_states: if return_final_kernel_results is FALSE and trace_fn is NULL. The return value is a Tensor or Python list of Tensors representing the state(s) of the Markov chain(s) at each result step. Has same shape as input current_state but with a prepended num_results-size dimension.
- states_and_trace: if return_final_kernel_results is FALSE and trace_fn is not NULL. The return value is an instance of StatesAndTrace.

References


See Also

Other mcmc_functions: mcmc_effective_sample_size(), mcmc_potential_scale_reduction(), mcmc_sample_annealed_importance_chain(), mcmc_sample_halton_sequence()
mcmc_sample_halton_sequence

Examples

dims <- 10
true_stddev <- sqrt(seq(1, 3, length.out = dims))
likelihood <- tfd_multivariate_normal_diag(scale_diag = true_stddev)

kernel <- mcmc_hamiltonian_monte_carlo(
  target_log_prob_fn = likelihood$log_prob,
  step_size = 0.5,
  num_leapfrog_steps = 2
)

states <- kernel %>% mcmc_sample_chain(
  num_results = 1000,
  num_burnin_steps = 500,
  current_state = rep(0, dims),
  trace_fn = NULL
)

sample_mean <- tf$reduce_mean(states, axis = 0L)
sample_stddev <- tf$sqrt(
  tf$reduce_mean(tf$math$squared_difference(states, sample_mean), axis = 0L))

mcmc_sample_halton_sequence

Returns a sample from the dim dimensional Halton sequence.

Description

Warning: The sequence elements take values only between 0 and 1. Care must be taken to appropriately transform the domain of a function if it differs from the unit cube before evaluating integrals using Halton samples. It is also important to remember that quasi-random numbers without randomization are not a replacement for pseudo-random numbers in every context. Quasi random numbers are completely deterministic and typically have significant negative autocorrelation unless randomization is used.

Usage

mcmc_sample_halton_sequence(
  dim,
  num_results = NULL,
  sequence_indices = NULL,
  dtype = tf$float32,
  randomized = TRUE,
  seed = NULL,
  name = NULL
)
Arguments

**dim**
Positive integer representing each sample’s *event_size*. Must not be greater than 1000.

**num_results** (Optional) Positive scalar *Tensor* of dtype int32. The number of samples to generate. Either this parameter or `sequence_indices` must be specified but not both. If this parameter is `None`, then the behaviour is determined by the `sequence_indices`. Default value: `NULL`.

**sequence_indices** (Optional) *Tensor* of dtype int32 and rank 1. The elements of the sequence to compute specified by their position in the sequence. The entries index into the Halton sequence starting with 0 and hence, must be whole numbers. For example, `sequence_indices=[0, 5, 6]` will produce the first, sixth and seventh elements of the sequence. If this parameter is `None`, then the `num_results` parameter must be specified which gives the number of desired samples starting from the first sample. Default value: `NULL`.

**dtype** (Optional) The dtype of the sample. One of: `float16`, `float32` or `float64`. Default value: `tf$float32`.

**randomized** (Optional) bool indicating whether to produce a randomized Halton sequence. If `TRUE`, applies the randomization described in Owen (2017). Default value: `TRUE`.

**seed** (Optional) integer to seed the random number generator. Only used if `randomized` is `TRUE`. If not supplied and `randomized` is `TRUE`, no seed is set. Default value: `NULL`.

**name** (Optional) string describing ops managed by this function. If not supplied the name of this function is used. Default value: "sample_halton_sequence".

Details

Computes the members of the low discrepancy Halton sequence in dimension `dim`. The `dim`-dimensional sequence takes values in the unit hypercube in `dim` dimensions. Currently, only dimensions up to 1000 are supported. The prime base for the `k`-th axes is the `k`-th prime starting from 2. For example, if `dim = 3`, then the bases will be `[2, 3, 5]` respectively and the first element of the non-randomized sequence will be: `[0.5, 0.333, 0.2]`. For a more complete description of the Halton sequences see [here](#). For low discrepancy sequences and their applications see [here](#).

If `randomized` is true, this function produces a scrambled version of the Halton sequence introduced by Owen (2017). For the advantages of randomization of low discrepancy sequences see [here](#).

The number of samples produced is controlled by the `num_results` and `sequence_indices` parameters. The user must supply either `num_results` or `sequence_indices` but not both. The former is the number of samples to produce starting from the first element. If `sequence_indices` is given instead, the specified elements of the sequence are generated. For example, `sequence_indices=tf$range(10)` is equivalent to specifying `n=10`.

Value

`halton_elements` Elements of the Halton sequence. *Tensor* of supplied dtype and shape `[num_results, dim]` if `num_results` was specified or shape `[s, dim]` where `s` is the size of `sequence_indices` if `sequence_indices` were specified.
mcmc_simple_step_size_adaptation

References


See Also

For an example how to use see mcmc_sample_chain().

Other mcmc_functions: mcmc_effective_sample_size(), mcmc_potential_scale_reduction(), mcmc_sample_annealed_importance_chain(), mcmc_sample_chain()

mcmc_simple_step_size_adaptation

Adapts the inner kernel's step size based on log_accept_prob.

Description

The simple policy multiplicatively increases or decreases the step size of the inner kernel based on the value of log_accept_prob. It is based on equation 19 of Andrieu and Thoms (2008). Given enough steps and small enough adaptation rate the median of the distribution of the acceptance probability will converge to the target_accept_prob. A good target acceptance probability depends on the inner kernel. If this kernel is HamiltonianMonteCarlo, then 0.6-0.9 is a good range to aim for. For RandomWalkMetropolis this should be closer to 0.25. See the individual kernels' docstrings for guidance.

Usage

mcmc_simple_step_size_adaptation(
  inner_kernel,
  num_adaptation_steps,
  target_accept_prob = 0.75,
  adaptation_rate = 0.01,
  step_size_setter_fn = NULL,
  step_size_getter_fn = NULL,
  log_accept_prob_getter_fn = NULL,
  validate_args = FALSE,
  name = NULL
)

Arguments

inner_kernel TransitionKernel-like object.
num_adaptation_steps Scalar integer Tensor number of initial steps to during which to adjust the step size. This may be greater, less than, or equal to the number of burnin steps.
target_accept_prob A floating point Tensor representing desired acceptance probability. Must be a positive number less than 1. This can either be a scalar, or have shape list(num_chains). Default value: 0.75 (the center of asymptotically optimal rate for HMC).
adaptation_rate

Tensor representing amount to scale the current step_size.

step_size_setter_fn

A function with the signature (kernel_results, new_step_size) -> new_kernel_results
where kernel_results are the results of the inner_kernel, new_step_size is a Tensor or a nested collection of Tensors with the same structure as returned by the step_size_getter_fn, and new_kernel_results are a copy of kernel_results with the step size(s) set.

step_size_getter_fn

A function with the signature (kernel_results) -> step_size where kernel_results are the results of the inner_kernel, and step_size is a floating point Tensor or a nested collection of such Tensors.

log_accept_prob_getter_fn

A function with the signature (kernel_results) -> log_accept_prob where kernel_results are the results of the inner_kernel, and log_accept_prob is a floating point Tensor. log_accept_prob can either be a scalar, or have shape list(num_chains). If it’s the latter, step_size should also have the same leading dimension.

validate_args Logical. When True kernel parameters are checked for validity. When False invalid inputs may silently render incorrect outputs.

name string prefixed to Ops created by this class. Default: "simple_step_size_adaptation".

Details

In general, adaptation prevents the chain from reaching a stationary distribution, so obtaining consistent samples requires num_adaptation_steps be set to a value somewhat smaller than the number of burnin steps. However, it may sometimes be helpful to set num_adaptation_steps to a larger value during development in order to inspect the behavior of the chain during adaptation.

The step size is assumed to broadcast with the chain state, potentially having leading dimensions corresponding to multiple chains. When there are fewer of those leading dimensions than there are chain dimensions, the corresponding dimensions in the log_accept_prob are averaged (in the direct space, rather than the log space) before being used to adjust the step size. This means that this kernel can do both cross-chain adaptation, or per-chain step size adaptation, depending on the shape of the step size.

For example, if your problem has a state with shape [S], your chain state has shape [C0, C1, Y] (meaning that there are C0 * C1 total chains) and log_accept_prob has shape [C0, C1] (one acceptance probability per chain), then depending on the shape of the step size, the following will happen:

- Step size has shape [], [S] or [1], the log_accept_prob will be averaged across its C0 and C1 dimensions. This means that you will learn a shared step size based on the mean acceptance probability across all chains. This can be useful if you don’t have a lot of steps to adapt and want to average away the noise.
- Step size has shape [C1, 1] or [C1, S], the log_accept_prob will be averaged across its C0 dimension. This means that you will learn a shared step size based on the mean acceptance probability across chains that share the coordinate across the C1 dimension. This can be useful when the C1 dimension indexes different distributions, while C0 indexes replicas of a single distribution, all sampled in parallel.
mcmc_simple_step_size_adaptation

- Step size has shape [C0, C1, 1] or [C0, C1, S], then no averaging will happen. This means that each chain will learn its own step size. This can be useful when all chains are sampling from different distributions. Even when all chains are for the same distribution, this can help during the initial warmup period.
- Step size has shape [C0, 1, 1] or [C0, 1, S], the log_accept_prob will be averaged across its C1 dimension. This means that you will learn a shared step size based on the mean acceptance probability across chains that share the coordinate across the C0 dimension. This can be useful when the C0 dimension indexes different distributions, while C1 indexes replicas of a single distribution, all sampled in parallel.

Value

A Monte Carlo sampling kernel

References


See Also

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_slice_sampler(), mcmc_transformed_transformation(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk().

Examples

```r
target_log_prob_fn <- tf$distribution(normal(loc = 0, scale = 1))$log_prob
num_burnin_steps <- 500
num_results <- 500
num_chains <- 64L
step_size <- tf$fill(list(num_chains), 0.1)

kernel <- mcmc_hamiltonian_monte_carlo(
  target_log_prob_fn = target_log_prob_fn,
  num_leapfrog_steps = 2,
  step_size = step_size
)

res <- kernel %>% mcmc_sample_chain(
  num_results = num_results,
  num_burnin_steps = num_burnin_steps,
  current_state = rep(0, num_chains),
  trace_fn = function(x, pkr) {
      list (}
```
mcmc_slice_sampler

Runs one step of the slice sampler using a hit and run approach

Description
Slice Sampling is a Markov Chain Monte Carlo (MCMC) algorithm based, as stated by Neal (2003), on the observation that "...one can sample from a distribution by sampling uniformly from the region under the plot of its density function. A Markov chain that converges to this uniform distribution can be constructed by alternately uniform sampling in the vertical direction with uniform sampling from the horizontal slice defined by the current vertical position, or more generally, with some update that leaves the uniform distribution over this slice invariant". Mathematical details and derivations can be found in Neal (2003). The one dimensional slice sampler is extended to n-dimensions through use of a hit-and-run approach: choose a random direction in n-dimensional space and take a step, as determined by the one-dimensional slice sampling algorithm, along that direction (Belisle et al. 1993).

Usage
mcmc_slice_sampler(
  target_log_prob_fn,
  step_size,
  max_doublings,
  seed = NULL,
  name = NULL
)

Arguments

  target_log_prob_fn
  Function which takes an argument like current_state (if it's a list current_state will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.

  step_size
  Tensor or list of Tensors representing the step size for the leapfrog integrator. Must broadcast with the shape of current_state. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. When possible, it's often helpful to match per-variable step sizes to the standard deviations of the target distribution in each variable.
Applies a bijector to the MCMC’s state space

The transformed transition kernel enables fitting a bijector which serves to decorrelate the Markov chain Monte Carlo (MCMC) event dimensions thus making the chain mix faster. This is particularly useful when the geometry of the target distribution is unfavorable. In such cases it may take many evaluations of the target_log_prob_fn for the chain to mix between faraway states.
mcmc_transformed_transition_kernel

Usage

mcmc_transformed_transition_kernel(inner_kernel, bijector, name = NULL)

Arguments

inner_kernel TransitionKernel-like object which has a target_log_prob_fn argument.
bijector bijector or list of bijectors. These bijectors use forward to map the inner_kernel state space to the state expected by inner_kernel$target_log_prob_fn.
name string prefixed to Ops created by this function. Default value: NULL (i.e., "transformed_kernel").

Details

The idea of training an affine function to decorrelate chain event dims was presented in Parno and Marzouk (2014). Used in conjunction with the Hamiltonian Monte Carlo transition kernel, the Parno and Marzouk (2014) idea is an instance of Riemannian manifold HMC (Girolami and Calderhead, 2011).

The transformed transition kernel enables arbitrary bijective transformations of arbitrary transition kernels, e.g., one could use bijectors tfb_affine, tfb_real_nvp, etc. with transition kernels mcmc_hamiltonian_monte_carlo, mcmc_random_walk_metropolis, etc.

Value

a Monte Carlo sampling kernel

References


See Also

Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_langevin(), mcmc_uncalibrated_random_walk()
Runs one step of Uncalibrated Hamiltonian Monte Carlo

Description

Warning: this kernel will not result in a chain which converges to the target_log_prob. To get a convergent MCMC, use mcmc_hamiltonian_monte_carlo(...) or mcmc_metropolis_hastings(mcmc_uncalibrated_hamiltonian_monte_carlo(...)).

For more details on UncalibratedHamiltonianMonteCarlo, see HamiltonianMonteCarlo.

Usage

mcmc_uncalibrated_hamiltonian_monte_carlo(
    target_log_prob_fn,
    step_size,
    num_leapfrog_steps,
    state_gradients_are_stopped = FALSE,
    seed = NULL,
    store_parameters_in_results = FALSE,
    name = NULL
)

Arguments

target_log_prob_fn
Function which takes an argument like current_state (if it's a list current_state will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.

step_size
Tensor or list of Tensors representing the step size for the leapfrog integrator. Must broadcast with the shape of current_state. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. When possible, it's often helpful to match per-variable step sizes to the standard deviations of the target distribution in each variable.

num_leapfrog_steps
Integer number of steps to run the leapfrog integrator for. Total progress per HMC step is roughly proportional to step_size * num_leapfrog_steps.

state_gradients_are_stopped
logical indicating that the proposed new state be run through tf$stop_gradient. This is particularly useful when combining optimization over samples from the HMC chain. Default value: FALSE (i.e., do not apply stop_gradient).

seed
integer to seed the random number generator.

store_parameters_in_results
If TRUE, then step_size and num_leapfrog_steps are written to and read from eponymous fields in the kernel results objects returned from one_step and bootstrap_results. This allows wrapper kernels to adjust those parameters on the fly. This is incompatible with step_size_update_fn, which must be set to NULL.
mcmc_uncalibrated_langevin

name: string prefixed to Ops created by this function. Default value: NULL (i.e., 'hmc_kernel').

Value:
a Monte Carlo sampling kernel

See Also:
Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(),
mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(),
mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(),
mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_langevin(),
mcmc_uncalibrated_random_walk()

mcmc_uncalibrated_langevin

Runs one step of Uncalibrated Langevin discretized diffusion.

Description:
The class generates a Langevin proposal using _euler_method function and also computes helper
UncalibratedLangevinKernelResults for the next iteration. Warning: this kernel will not result
in a chain which converges to the target_log_prob. To get a convergent MCMC, use MetropolisAdjustedLangevinAlgorithm(...) or
MetropolisHastings(UncalibratedLangevin(...)).

Usage:
mcmc_uncalibrated_langevin(
  target_log_prob_fn,
  step_size,
  volatility_fn = NULL,
  parallel_iterations = 10,
  compute_acceptance = TRUE,
  seed = NULL,
  name = NULL
)

Arguments:
target_log_prob_fn
Function which takes an argument like current_state (if it's a list current_state
will be unpacked) and returns its (possibly unnormalized) log-density under the
target distribution.

step_size
Tensor or list of Tensors representing the step size for the leapfrog integrator.
Must broadcast with the shape of current_state. Larger step sizes lead to
faster progress, but too-large step sizes make rejection exponentially more likely.
When possible, it's often helpful to match per-variable step sizes to the standard
deviations of the target distribution in each variable.
volatility_fn  function which takes an argument like current_state (or *current_state if it's a list) and returns volatility value at current_state. Should return a Tensor or list of Tensors that must broadcast with the shape of current_state. Defaults to the identity function.

parallel_iterations  the number of coordinates for which the gradients of the volatility matrix volatility_fn can be computed in parallel.

compute_acceptance  logical indicating whether to compute the Metropolis log-acceptance ratio used to construct MetropolisAdjustedLangevinAlgorithm kernel.

seed  integer to seed the random number generator. Default value: NULL (i.e., 'mala_kernel').

name  String prefixed to Ops created by this function. Default value: NULL (i.e., 'mala_kernel').

Value  list of next_state (Tensor or Python list of Tensors representing the state(s) of the Markov chain(s) at each result step. Has same shape as and current_state.) and kernel_results (collections$namedtuple of internal calculations used to 'advance the chain).

See Also  Other mcmc_kernels: mcmc_dual_averaging_step_size_adaptation(), mcmc_hamiltonian_monte_carlo(), mcmc_metropolis_adjusted_langevin_algorithm(), mcmc_metropolis_hastings(), mcmc_no_u_turn_sampler(), mcmc_random_walk_metropolis(), mcmc_replica_exchange_mc(), mcmc_simple_step_size_adaptation(), mcmc_slice_sampler(), mcmc_transformed_transition_kernel(), mcmc_uncalibrated_hamiltonian_monte_carlo(), mcmc_uncalibrated_random_walk()

---

mcmc_uncalibrated_random_walk

Generate proposal for the Random Walk Metropolis algorithm.

Description

Warning: this kernel will not result in a chain which converges to the target_log_prob. To get a convergent MCMC, use mcmc_random_walk_metropolis(...) or mcmc_metropolis_hastings(mcmc_uncalibrated_random_walk(...))

Usage

mcmc_uncalibrated_random_walk(
    target_log_prob_fn,
    new_state_fn = NULL,
    seed = NULL,
    name = NULL
)
Arguments

**target_log_prob_fn**

Function which takes an argument like `current_state` (if it's a list `current_state` will be unpacked) and returns its (possibly unnormalized) log-density under the target distribution.

**new_state_fn**

Function which takes a list of state parts and a seed; returns a same-type list of Tensors, each being a perturbation of the input state parts. The perturbation distribution is assumed to be a symmetric distribution centered at the input state part. Default value: NULL which is mapped to `tfp$mcmc$random_walk_normal_fn()`.

**seed**

integer to seed the random number generator.

**name**

String name prefixed to Ops created by this function. Default value: NULL (i.e., 'rwm_kernel').

Value

a Monte Carlo sampling kernel

See Also

Other mcmc_kernels: `mcmc_dual_averaging_step_size_adaptation()`, `mcmc_hamiltonian_monte_carlo()`, `mcmc_metropolis_adjusted_langevin_algorithm()`, `mcmc_metropolis_hastings()`, `mcmc_no_u_turn_sampler()`, `mcmc_random_walk_metropolis()`, `mcmc_replica_exchange_mc()`, `mcmc_simple_step_size_adaptation()`, `mcmc_slice_sampler()`, `mcmc_transformed_transition_kernel()`, `mcmc_uncalibrated_hamiltonian_monte_carlo()`, `mcmc_uncalibrated_langevin()`

---

**params_size_categorical_mixture_of_one_hot_categorical**

number of params needed to create a CategoricalMixtureOfOneHotCategorical distribution

Description

number of params needed to create a CategoricalMixtureOfOneHotCategorical distribution

Usage

```python
params_size_categorical_mixture_of_one_hot_categorical(
    event_size,
    num_components
)
```

Arguments

**event_size**

event size of this distribution

**num_components**

number of components in the mixture
**params_size_independent_bernoulli**

**Value**

A scalar

**Description**

Number of params needed to create an IndependentBernoulli distribution

**Usage**

`params_size_independent_bernoulli(event_size)`

**Arguments**

- `event_size` event size of this distribution

**Value**

A scalar

---

**params_size_independent_logistic**

Number of params needed to create an IndependentLogistic distribution

**Description**

Number of params needed to create an IndependentLogistic distribution

**Usage**

`params_size_independent_logistic(event_size)`

**Arguments**

- `event_size` event size of this distribution

**Value**

A scalar
**params_size_independent_normal**

_number of params needed to create an IndependentNormal distribution_

**Description**

number of params needed to create an IndependentNormal distribution

**Usage**

`params_size_independent_normal(event_size)`

**Arguments**

- `event_size` event size of this distribution

**Value**

a scalar

---

**params_size_independent_poisson**

_number of params needed to create an IndependentPoisson distribution_

**Description**

number of params needed to create an IndependentPoisson distribution

**Usage**

`params_size_independent_poisson(event_size)`

**Arguments**

- `event_size` event size of this distribution

**Value**

a scalar
**params_size_mixture_logistic**

_number of params needed to create a MixtureLogistic distribution_

**Description**

number of params needed to create a MixtureLogistic distribution

**Usage**

`params_size_mixture_logistic(num_components, event_shape)`

**Arguments**

- `num_components`  Number of component distributions in the mixture distribution.
- `event_shape`  Number of parameters needed to create a single component distribution.

**Value**

a scalar

---

**params_size_mixture_normal**

_number of params needed to create a MixtureNormal distribution_

**Description**

number of params needed to create a MixtureNormal distribution

**Usage**

`params_size_mixture_normal(num_components, event_shape)`

**Arguments**

- `num_components`  Number of component distributions in the mixture distribution.
- `event_shape`  Number of parameters needed to create a single component distribution.

**Value**

a scalar
**params_size_mixture_same_family**

number of params needed to create a MixtureSameFamily distribution

**Description**

number of params needed to create a MixtureSameFamily distribution

**Usage**

`params_size_mixture_same_family(num_components, component_params_size)`

**Arguments**

- `num_components` Number of component distributions in the mixture distribution.
- `component_params_size` Number of parameters needed to create a single component distribution.

**Value**

a scalar

---

**params_size_multivariate_normal_tri_l**

number of params needed to create a MultivariateNormalTriL distribution

**Description**

number of params needed to create a MultivariateNormalTriL distribution

**Usage**

`params_size_multivariate_normal_tri_l(event_size)`

**Arguments**

- `event_size` event size of this distribution

**Value**

a scalar
**params_size_one_hot_categorical**

number of params needed to create a OneHotCategorical distribution

**Description**

number of params needed to create a OneHotCategorical distribution

**Usage**

```r
code
```

**Arguments**

- `event_size` event size of this distribution

**Value**

a scalar

---

**sts_additive_state_space_model**

A state space model representing a sum of component state space models.

**Description**

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$. The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see `tfd_linear_gaussian_state_space_model` for details.

**Usage**

```r
code
```
Arguments

component_ssms list containing one or more tfd_linear_gaussian_state_space_model instances. The components will in general implement different time-series models, with possibly different latent_size, but they must have the same dtype, event shape (num_timesteps and observation_size), and their batch shapes must broadcast to a compatible batch shape.#

custom_offset scalar float tensor, or batch of scalars, specifying a constant value added to the sum of outputs from the component models. This allows the components to model the shifted series observed_time_series -constant_offset. Default value: 0.#

observation_noise_scale Optional scalar float tensor indicating the standard deviation of the observation noise. May contain additional batch dimensions, which must broadcast with the batch shape of elements in component_ssms. If observation_noise_scale is specified for the sts_additive_state_space_model, the observation noise scales of component models are ignored. If NULL, the observation noise scale is derived by summing the noise variances of the component models, i.e., observation_noise_scale = sqrt(sum([ssm.observation_noise_scale**2 for ssm in component_ssms])).

initial_state_prior instance of tfd_multivariate_normal representing the prior distribution on latent states. Must have event shape [1] (as tfd_linear_gaussian_state_space_model requires a rank-1 event shape).

initial_step Optional scalar integer tensor specifying the starting timestep. Default value: 0.

validate_args logical. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.

allow_nan_stats logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.

name string prefixed to ops created by this class. Default value: "AdditiveStateSpaceModel".

Details

The sts_additive_state_space_model represents a sum of component state space models. Each of the N components describes a random process generating a distribution on observed time series x1[t], x2[t], ..., xN[t]. The additive model represents the sum of these processes, y[t] = x1[t] + x2[t] + ... + xN[t] + eps[t], where eps[t] ~ N(0, observation_noise_scale) is an observation noise term.

Mathematical Details
The additive model concatenates the latent states of its component models. The generative process runs each component’s dynamics in its own subspace of latent space, and then observes the sum of the observation models from the components.

Formally, the transition model is linear Gaussian:

\[ p(z_{t+1} | z_t) \sim \text{Normal}(\text{loc} = \text{transition_matrix}.\text{matmul}(z_t), \text{cov} = \text{transition_cov}) \]

where each \( z_t \) is a latent state vector concatenating the component state vectors, \( z[t] = [z1[t], z2[t], ..., zN[t]] \), so it has size \( \text{latent_size} = \sum(\{c.latin\text{}_s\text{ize} \text{ for c in components}\}) \).

The transition matrix is the block-diagonal composition of transition matrices from the component processes:

\[
\text{transition_matrix} = \\
\begin{bmatrix}
    [c_0.\text{transition_matrix}, 0., ..., 0.], \\
    [0., c_1.\text{transition_matrix}, ..., 0.], \\
    [... ... ... ], \\
    [0., 0., ..., c_N.\text{transition_matrix}]
\end{bmatrix}
\]

and the noise covariance is similarly the block-diagonal composition of component noise covariances:

\[
\text{transition_cov} = \\
\begin{bmatrix}
    [c_0.\text{transition_cov}, 0., ..., 0.], \\
    [0., c_1.\text{transition_cov}, ..., 0.], \\
    [... ... ... ], \\
    [0., 0., ..., c_N.\text{transition_cov}]
\end{bmatrix}
\]

The observation model is also linear Gaussian,

\[ p(y_t | z_t) \sim \text{Normal}(\text{loc} = \text{observation_matrix}.\text{matmul}(z_t), \text{stddev} = \text{observation_noise_scale}) \]

This implementation assumes scalar observations, so \( \text{observation_matrix} \) has shape \([1, \text{latent\_size}]\).

The additive observation matrix simply concatenates the observation matrices from each component:

\[
\text{observation_matrix} = \text{concat}([c_0.\text{obs\_matrix}, c_1.\text{obs\_matrix}, ..., c_N.\text{obs\_matrix}], \text{axis}=-1)
\]

The effect is that each component observation matrix acts on the dimensions of latent state corresponding to that component, and the overall expected observation is the sum of the expected observations from each component.

If \( \text{observation_noise_scale} \) is not explicitly specified, it is also computed by summing the noise variances of the component processes:

\[ \text{observation_noise_scale} = \sqrt{\sum([c.\text{observation_noise_scale}^2 \text{ for c in components}])} \]

Value

an instance of \texttt{LinearGaussianStateSpaceModel}. 
See Also

Other sts: \texttt{sts_autoregressive\_state\_space\_model()}, \texttt{sts_autoregressive()}, \texttt{sts\_constrained\_seasonal\_state\_space\_model()}, \texttt{sts\_dynamic\_linear\_regression\_state\_space\_model()}, \texttt{sts\_dynamic\_linear\_regression()}, \texttt{sts\_linear\_regression()}, \texttt{sts\_local\_level\_state\_space\_model()}, \texttt{sts\_local\_level()}, \texttt{sts\_local\_linear\_trend()}, \texttt{sts\_local\_linear\_trend\_state\_space\_model()}, \texttt{sts\_seasonal\_state\_space\_model()}, \texttt{sts\_seasonal()}, \texttt{sts\_semi\_local\_linear\_trend()}, \texttt{sts\_semi\_local\_linear\_trend\_state\_space\_model()}, \texttt{sts\_smooth\_seasonal\_state\_space\_model()}, \texttt{sts\_smooth\_seasonal()}, \texttt{sts\_sparse\_linear\_regression()}, \texttt{sts\_sum()}

\begin{center}
\begin{tabular}{ll}
\texttt{sts\_autoregressive} & \textit{Formal representation of an autoregressive model.} \\
\end{tabular}
\end{center}

Description

An autoregressive (AR) model posits a latent level whose value at each step is a noisy linear combination of previous steps:

\[
\text{level}[t+1] = (\text{sum}(\text{coefficients} \times \text{levels}[t:t-\text{order}:1]) + \text{Normal}(0.0, \text{level\_scale}))
\]

Usage

\begin{verbatim}
sts_autoregressive(
    observed_time_series = NULL,
    order,
    coefficients_prior = NULL,
    level_scale_prior = NULL,
    initial_state_prior = NULL,
    coefficient_constraining_bijector = NULL,
    name = NULL
)
\end{verbatim}

Arguments

\begin{itemize}
\item \texttt{observed\_time\_series} optional float tensor of shape \texttt{batch\_shape + [T, 1]} (omitting the trailing unit dimension is also supported when \texttt{T > 1}), specifying an observed time series. Any priors not explicitly set will be given default values according to the scale of the observed time series (or batch of time series). May optionally be an instance of \texttt{sts\_masked\_time\_series}, which includes a mask tensor to specify timesteps with missing observations. Default value: \texttt{NULL}.
\item \texttt{order} scalar positive integer specifying the number of past timesteps to regress on.
\item \texttt{coefficients\_prior} optional Distribution instance specifying a prior on the coefficients parameter. If \texttt{NULL}, a default standard normal (\texttt{tfd\_multivariate\_normal\_diag(scale\_diag = tf\$ones(list(order)))}) prior is used. Default value: \texttt{NULL}.
\end{itemize}
level_scale_prior
optional Distribution instance specifying a prior on the level_scale parameter. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

initial_state_prior
optional Distribution instance specifying a prior on the initial state, corresponding to the values of the process at a set of size order of imagined timesteps before the initial step. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

coefficient_constraining_bijector
optional Bijector instance representing a constraining mapping for the autoregressive coefficients. For example, tfb_tanh() constrains the coefficients to lie in (-1, 1), while tfb_softplus() constrains them to be positive, and tfb_identity() implies no constraint. If NULL, the default behavior constrains the coefficients to lie in (-1, 1) using a tanh bijector. Default value: NULL.

name
the name of this model component. Default value: 'Autoregressive'.

Details
The latent state is levels[t:t-order:-1]. We observe a noisy realization of the current level: f[t] = level[t] + Normal(0.,observation_noise_scale) at each timestep.

If coefficients=[1.], the AR process is a simple random walk, equivalent to a LocalLevel model. However, a random walk’s variance increases with time, while many AR processes (in particular, any first-order process with abs(coefficient) < 1) are stationary, i.e., they maintain a constant variance over time. This makes AR processes useful models of uncertainty.

Value
an instance of StructuralTimeSeries.

See Also
For usage examples see sts_fit_with_hmc(), sts_forecast(), sts_decompose_by_component().

Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state_space_model(), sts_dynamic_linear_regression(), sts_linear_regression(), sts_local_level_state_space_model(), sts_local_level(), sts_local_linear_trend_state_space_model(), sts_local_linear_trend(), sts_seasonal_state_space_model(), sts_seasonal(), sts_semi_local_linear_trend_state_space_model(), sts_semi_local_linear_trend(), sts_smooth_seasonal_state_space_model(), sts_smooth_seasonal(), sts_sparse_linear_regression(), sts_sum()
Description

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$. The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see `tfd_linear_gaussian_state_space_model` for details.

Usage

```r
sts_autoregressive_state_space_model(
  num_timesteps,
  coefficients,
  level_scale,
  initial_state_prior,
  observation_noise_scale = 0,
  initial_step = 0,
  validate_args = FALSE,
  name = NULL
)
```

Arguments

- `num_timesteps`: Scalar integer tensor number of timesteps to model with this distribution.
- `level_scale`: Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the transition noise at each step.
- `initial_state_prior`: Instance of `tfd_multivariate_normal` representing the prior distribution on latent states. Must have event shape `list(order)`.
- `observation_noise_scale`: Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise. Default value: 0.
- `initial_step`: Optional scalar int tensor specifying the starting timestep. Default value: 0.
- `validate_args`: Logical. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.
name  

name prefixed to ops created by this class. Default value: "AutoregressiveStateSpaceModel".

Details

In an autoregressive process, the expected level at each timestep is a linear function of previous levels, with added Gaussian noise:

\[
\text{level}[t+1] = (\text{sum}(\text{coefficients} * \text{levels}[t:t:\text{order}-1]) + \text{Normal}(0., \text{level.scale}))
\]

The process is characterized by a vector coefficients whose size determines the order of the process (how many previous values it looks at), and by level_scale, the standard deviation of the noise added at each step. This is formulated as a state space model by letting the latent state encode the most recent values; see 'Mathematical Details' below.

The parameters level_scale and observation_noise_scale are each (a batch of) scalars, and coefficients is a (batch) vector of size \text{list(order)}. The batch shape of this Distribution is the broadcast batch shape of these parameters and of the \text{initial_state_prior}.

Mathematical Details

The autoregressive model implements a \text{tfd_linear_gaussian_state_space_model} with \text{latent_size} = \text{order} and \text{observation_size} = 1. The latent state vector encodes the recent history of the process, with the current value in the topmost dimension. At each timestep, the transition sums the previous values to produce the new expected value, shifts all other values down by a dimension, and adds noise to the current value. This is formally encoded by the transition model:

\[
\text{transition_matrix} = \begin{bmatrix}
\text{coeffs[0]}, & \text{coeffs[1]}, & \ldots, & \text{coeffs[order]} \\
1., & 0., & \ldots, & 0. \\
0., & 1., & \ldots, & 0. \\
\vdots \\
0., & 0., & \ldots, & 1., & 0.
\end{bmatrix}
\]

\[
\text{transition_noise} \sim \text{N(loc=0., scale=diag([level_scale, 0., 0., \ldots, 0.]))}
\]

The observation model simply extracts the current (topmost) value, and optionally adds independent noise at each step:

\[
\text{observation_matrix} = \begin{bmatrix}
1., & 0., & \ldots, & 0.
\end{bmatrix}
\]

\[
\text{observation_noise} \sim \text{N(loc=0, scale=observation_noise_scale)}
\]

Models with \text{observation_noise_scale} = 0 are AR processes in the formal sense. Setting \text{observation_noise_scale} to a nonzero value corresponds to a latent AR process observed under an iid noise model.

Value

an instance of \text{LinearGaussianStateSpaceModel}. 
sts_build_factored_surrogate_posterior

Build a variational posterior that factors over model parameters.

Description

The surrogate posterior consists of independent Normal distributions for each parameter with trainable loc and scale, transformed using the parameter’s bijector to the appropriate support space for that parameter.

Usage

```r
sts_build_factored_surrogate_posterior(
    model,
    batch_shape = list(),
    seed = NULL,
    name = NULL
)
```

Arguments

- **model**: An instance of `StructuralTimeSeries` representing a time-series model. This represents a joint distribution over time-series and their parameters with batch shape `[b1, ..., bN].`'
- **batch_shape**: Batch shape (list, or integer) of initial states to optimize in parallel. Default value: `list()`. (i.e., just run a single optimization).
- **seed**: integer to seed the random number generator.
- **name**: string prefixed to ops created by this function. Default value: `NULL` (i.e., `build_factored_surrogate_posterior`).

Value

`variational_posterior tfd_joint_distribution_named` defining a trainable surrogate posterior over model parameters. Samples from this distribution are named lists with character parameter names as keys.
sts_build_factored_variational_loss

Build a loss function for variational inference in STS models.

Description

Variational inference searches for the distribution within some family of approximate posteriors that
minimizes a divergence between the approximate posterior $q(z)$ and true posterior $p(z|\text{observed_time_series})$.
By converting inference to optimization, it’s generally much faster than sampling-based inference
algorithms such as HMC. The tradeoff is that the approximating family rarely contains the true
posterior, so it may miss important aspects of posterior structure (in particular, dependence between
variables) and should not be blindly trusted. Results may vary; it’s generally wise to compare to
HMC to evaluate whether inference quality is sufficient for your task at hand.

Usage

```r
sts_build_factored_variational_loss(
  observed_time_series,
  model,
  init_batch_shape = list(),
  seed = NULL,
  name = NULL
)
```

Arguments

- **observed_time_series**
  float tensor of shape concat([sample_shape, model.batch_shape, [num_timesteps, 1]])
  where sample_shape corresponds to i.i.d. observations, and the trailing [1] di-
  mension may (optionally) be omitted if num_timesteps > 1. May optionally
  be an instance of `sts_masked_time_series`, which includes a mask tensor to
  specify timesteps with missing observations.

- **model**
  An instance of ` StructuralTimeSeries` representing a time-series model. This
  represents a joint distribution over time-series and their parameters with batch
  shape [b1, ..., bN].

- **init_batch_shape**
  Batch shape (list) of initial states to optimize in parallel. Default value: list().
  (i.e., just run a single optimization).

- **seed**
  integer to seed the random number generator.

- **name**
  name prefixed to ops created by this function. Default value: NULL (i.e., 'build_factored_variational_loss')

See Also

Other sts-functions: `sts_build_factored_variational_loss()`,
`sts_decompose_by_component()`, `sts_decompose_forecast_by_component()`,
`sts_fit_with_hmc()`, `sts_forecast()`, `sts_one_step_predictive()`,
`sts_sample_uniform_initial_state()`
Details

This method constructs a loss function for variational inference using the Kullback-Liebler divergence $KL[q(z) || p(z|\text{observed}_\text{time}_\text{series})]$, with an approximating family given by independent Normal distributions transformed to the appropriate parameter space for each parameter. Minimizing this loss (the negative ELBO) maximizes a lower bound on the log model evidence $-\log p(\text{observed}_\text{time}_\text{series})$. This is equivalent to the ‘mean-field’ method implemented in Kucukelbir et al. (2017) and is a standard approach. The resulting posterior approximations are unimodal; they will tend to underestimate posterior uncertainty when the true posterior contains multiple modes (the $KL[q||p]$ divergence encourages choosing a single mode) or dependence between variables.

Value

This function returns a list of:

- **variational_loss**: float Tensor of shape tf$concat([init\_batch\_shape, model$batch\_shape]) encoding a stochastic estimate of an upper bound on the negative model evidence $-\log p(y)$. Minimizing this loss performs variational inference; the gap between the variational bound and the true (generally unknown) model evidence corresponds to the divergence $KL[q||p]$ between the approximate and true posterior.

- **variational_distributions**: a named list giving the approximate posterior for each model parameter. The keys are character parameter names in order, corresponding to [param.name for param in model$parameters]. The values are tf$distribution$ instances with batch shape tf$concat([init\_batch\_shape, model$batch\_shape]); these will typically be of the form tf$distribution$TransformedDistribution(tfd.Normal(...),bijector=param.bijector).

References


See Also

Other sts-functions: `sts_build_factored_surrogate_posterior()`, `sts_decompose_by_component()`, `sts_decompose_forecast_by_component()`, `sts_fit_with_hmc()`, `sts_forecast()`, `sts_one_step_predictive()`, `sts_sample_uniform_initial_state()`

Description

Seasonal state space model with effects constrained to sum to zero.
**Usage**

```r
sts_constrained_seasonal_state_space_model(
  num_timesteps,
  num_seasons,
  drift_scale,
  initial_state_prior,
  observation_noise_scale = 1e-04,
  num_steps_per_season = 1,
  initial_step = 0,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = NULL
)
```

**Arguments**

- `num_timesteps` Scalar integer tensor number of timesteps to model with this distribution.
- `num_seasons` Scalar integer number of seasons.
- `drift_scale` Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the change in effect between consecutive occurrences of a given season. This is assumed to be the same for all seasons.
- `initial_state_prior` instance of `tfd_multivariate_normal` representing the prior distribution on latent states; must have event shape `[num_seasons]`.
- `observation_noise_scale` Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise.
- `num_steps_per_season` integer number of steps in each season. This may be either a scalar (shape []), in which case all seasons have the same length, or an array of shape `[num_seasons]`, in which seasons have different length, but remain constant around different cycles, or an array of shape `[num_cycles, num_seasons]`, in which `num_steps_per_season` for each season also varies in different cycle (e.g., a 4 years cycle with leap day). Default value: 1.
- `initial_step` Optional scalar integer tensor specifying the starting timestep. Default value: 0.
- `validate_args` logical. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.
- `allow_nan_stats` logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.
- `name` string prefixed to ops created by this class. Default value: "SeasonalStateSpaceModel".
Value

an instance of LinearGaussianStateSpaceModel.

See Also

sts_seasonal_state_space_model().

Mathematical details

The constrained model implements a reparameterization of the naive SeasonalStateSpaceModel. Instead of directly representing the seasonal effects in the latent space, the latent space of the constrained model represents the difference between each effect and the mean effect. The following discussion assumes familiarity with the mathematical details of SeasonalStateSpaceModel.

Reparameterization and constraints: let the seasonal effects at a given timestep be $E = [e_1, ..., e_N]$. The difference between each effect $e_i$ and the mean effect is $z_i = e_i - \frac{\sum_i(e_i)}{N}$. By itself, this transformation is not invertible because recovering the absolute effects requires that we know the mean as well. To fix this, we’ll define $z_N = \frac{\sum_i(e_i)}{N}$ as the mean effect. It’s easy to see that this is invertible: given the mean effect and the differences of the first $N-1$ effects from the mean, it’s easy to solve for all $N$ effects. Formally, we’ve defined the invertible linear reparameterization $Z = R E$, where

$$R = [1 - 1/N, -1/N, ..., -1/N]
-1/N, 1 - 1/N, ..., -1/N,
\vdots
1/N, 1/N, ..., 1/N]$$

represents the change of basis from ‘effect coordinates’ $E$ to ‘residual coordinates’ $Z$. The $Z$s form the latent space of the ConstrainedSeasonalStateSpaceModel. To constrain the mean effect $z_N$ to zero, we fix the prior to zero, $p(z_N) \sim N(0, 0)$, and after the transition at each timestep we project $z_N$ back to zero. Note that this projection is linear: to set the $N$th dimension to zero, we simply multiply by the identity matrix with a missing element in the bottom right, i.e., $Z_{\text{constrained}} = P Z$, where $P = \text{eye}(N) - \text{scatter}((N-1, N-1), 1)$.

Model: concretely, suppose a naive seasonal effect model has initial state prior $N(m, S)$, transition matrix $F$ and noise covariance $Q$, and observation matrix $H$. Then the corresponding constrained seasonal effect model has initial state prior $N(P R m, P R S R' P')$, transition matrix $P R F R^{-1}$ and noise covariance $F R Q R' F'$, and observation matrix $H R^{-1}$, where the change-of-basis matrix $R$ and constraint projection matrix $P$ are as defined above. This follows directly from applying the reparameterization $Z = R E$, and then enforcing the zero-sum constraint on the prior and transition noise covariances. In practice, because the sum of effects $z_N$ is constrained to be zero, it will never contribute a term to any linear operation on the latent space, so we can drop that dimension from the model entirely. ConstrainedSeasonalStateSpaceModel does this, so that it implements the $N-1$ dimension latent space $z_1, ..., z_{N-1}$. Note that since we constrained the mean effect to be zero, the latent $z_i$’s now recover their interpretation as the actual effects, $z_i = e_i$ for $i = 1, ..., N - 1$, even though they were originally defined as residuals. The $N$th effect is represented only implicitly, as the nonzero mean of the first $N - 1$ effects. Although the computational representation is not symmetric across all $N$ effects, we derived the ConstrainedSeasonalStateSpaceModel by starting with a symmetric representation and imposing only a symmetric constraint (the zero-sum constraint), so the probability model remains symmetric over all $N$ seasonal effects.
**Description**

This method decomposes a time series according to the posterior representation of a structural time series model. In particular, it:

- Computes the posterior marginal mean and covariances over the additive model’s latent space.
- Decomposes the latent posterior into the marginal blocks for each model component.
- Maps the per-component latent posteriors back through each component’s observation model, to generate the time series modeled by that component.

**Usage**

```python
sts_decompose_by_component(observed_time_series, model, parameter_samples)
```

**Arguments**

- **observed_time_series**
  float tensor of shape `concat([sample_shape, model.batch_shape, [num_timesteps, 1]])` where `sample_shape` corresponds to i.i.d. observations, and the trailing `[1]` dimension may (optionally) be omitted if `num_timesteps > 1`. May optionally be an instance of `sts_masked_time_series`, which includes a mask tensor to specify timesteps with missing observations.

- **model**
  An instance of `sts_sum` representing a structural time series model.

- **parameter_samples**
  list of tensors representing posterior samples of model parameters, with shapes `list(tf$concat(list(list(num_posterior_draws), param<1>$prior$batch_shape, param<1>$prior$event_shape), list(list(num_posterior_draws), param<2>$prior$batch_shape, param<2>$prior$event_shape), ... ) )` for all model parameters. This may optionally also be a named list mapping parameter names to tensor values.

**Value**

- **component_dists** A named list mapping component StructuralTimeSeries instances (elements of `model$components`) to Distribution instances representing the posterior marginal distributions on the process modeled by each component. Each distribution has batch shape matching that of `posterior_means/posterior_covs`, and event shape of `list(num_timesteps)`.
sts_decompose_forecast_by_component

Decompose a forecast distribution into contributions from each component.

Description

Decompose a forecast distribution into contributions from each component.

Usage

sts_decompose_forecast_by_component(model, forecast_dist, parameter_samples)

Arguments

- **model**: An instance of `sts_sum` representing a structural time series model.
- **forecast_dist**: A `Distribution` instance returned by `sts_forecast()`. (Specifically, must be an `tfd.MixtureSameFamily` over a `tfd_linear_gaussian_state_space_model` parameterized by posterior samples).

Examples

```r
observed_time_series <- array(rnorm(2 * 1 * 12), dim = c(2, 1, 12))
day_of_week <- observed_time_series %>% sts_seasonal(num_seasons = 7, name = "seasonal")
local_linear_trend <- observed_time_series %>% sts_local_linear_trend(name = "local_linear")
model <- observed_time_series %>%
  sts_sum(components = list(day_of_week, local_linear_trend))
states_and_results <- observed_time_series %>%
  sts_fit_with_hmc(model, num_results = 10, num_warmup_steps = 5, num_variational_steps = 15)
samples <- states_and_results[[1]]

component_dists <- observed_time_series %>%
  sts_decompose_by_component(model = model, parameter_samples = samples)
```
parameter_samples
  list of tensors representing posterior samples of model parameters, with
  shapes list(tf$concat(list(list(num_posterior_draws), param<1>$prior$batch_shape, param<1>$prior$event_shape), list(list(num_posterior_draws), param<2>$prior$batch_shape, param<2>$prior$event_shape), ... )
  for all model parameters. This may optionally also be a named list mapping pa-
  rameter names to tensor values.

Value
  component_dists A named list mapping component StructuralTimeSeries instances (elements of
  model$components) to Distribution instances representing the marginal forecast for each com-
  ponent. Each distribution has batch shape matching forecast_dist (specifically, the event shape
  is [num_steps_forecast]).

See Also
  Other sts-functions: sts_build_factored_surrogate_posterior(), sts_build_factored_variational_loss(),
  sts_decompose_by_component(), sts_fit_with_hmc(), sts_forecast(), sts_one_step_predictive(),
  sts_sample_uniform_initial_state()

sts_dynamic_linear_regression
  
  Formal representation of a dynamic linear regression model.

Description
  The dynamic linear regression model is a special case of a linear Gaussian SSM and a generalization
  of typical (static) linear regression. The model represents regression weights with a latent state
  which evolves via a Gaussian random walk:

Usage
  
  sts_dynamic_linear_regression(
    observed_time_series = NULL,
    design_matrix,
    drift_scale_prior = NULL,
    initial_weights_prior = NULL,
    name = NULL
  )

Arguments
  observed_time_series
    optional float tensor of shape batch_shape + [T, 1] (omitting the trailing unit
    dimension is also supported when T > 1), specifying an observed time series.
    Any priors not explicitly set will be given default values according to the scale
    of the observed time series (or batch of time series). May optionally be an in-
    stance of sts_masked_time_series, which includes a mask tensor to specify
    timesteps with missing observations. Default value: NULL.
**Description**

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$. The special case where both the transition and observation models are Gaussians with mean...
specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see \texttt{tfd_linear_gaussian_state_space_model} for details.

\textbf{Usage}

\begin{verbatim}
sts_dynamic_linear_regression_state_space_model(
    num_timesteps,
    design_matrix,
    drift_scale,
    initial_state_prior,
    observation_noise_scale = 0,
    initial_step = 0,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = NULL
)
\end{verbatim}

\textbf{Arguments}

- \texttt{num_timesteps} \texttt{Scalar integer tensor, number of timesteps to model with this distribution.}
- \texttt{design_matrix} \texttt{float tensor of shape \texttt{tf$concat(list(batch\_shape, list(num\_timesteps, num\_features)))}. This may also optionally be an instance of \texttt{tf$linalg$LinearOperator}.}
- \texttt{drift_scale} \texttt{Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the latent state transitions.}
- \texttt{initial_state_prior} \texttt{instance of \texttt{tfd_multivariate_normal} representing the prior distribution on latent states. Must have event shape \texttt{list(num\_features)}.}
- \texttt{observation_noise_scale} \texttt{Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise. Default value: 0.}
- \texttt{initial_step} \texttt{scalar integer tensor specifying the starting timestep. Default value: 0.}
- \texttt{validate_args} \texttt{logical. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.}
- \texttt{allow_nan_stats} \texttt{logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.}
- \texttt{name} \texttt{name prefixed to ops created by this class. Default value: 'DynamicLinearRegressionStateSpaceModel'.}

\textbf{Details}

The dynamic linear regression model is a special case of a linear Gaussian SSM and a generalization of typical (static) linear regression. The model represents regression weights with a latent state which evolves via a Gaussian random walk: \texttt{weights[t] \sim Normal(weights[t-1], drift_scale)}
The latent state (the weights) has dimension num_features, while the parameters drift_scale and observation_noise_scale are each (a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these parameters, the initial_state_prior, and the design_matrix. num_features is determined from the last dimension of design_matrix (equivalent to the number of columns in the design matrix in linear regression).

Mathematical Details
The dynamic linear regression model implements a tfd_linear_gaussian_state_space_model with latent_size = num_features and observation_size = 1 following the transition model:

\[
  \text{transition_matrix} = \text{eye}(\text{num_features}) \\
  \text{transition_noise} \sim \text{Normal}(0, \text{diag}([\text{drift_scale}]))
\]

which implements the evolution of weights described above. The observation model is:

\[
  \text{observation_matrix}[t] = \text{design_matrix}[t] \\
  \text{observation_noise} \sim \text{Normal}(0, \text{observation_noise_scale})
\]

Value
an instance of LinearGaussianStateSpaceModel.

See Also
Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model().
sts_autoregressive(). sts_constrained_seasonal_state_space_model(). sts_dynamic_linear_regression().
sts_linear_regression(). sts_local_level_state_space_model(). sts_local_level(). sts_local_linear_trend().
sts_local_linear_trend(). sts_seasonal_state_space_model(). sts_seasonal(). sts_semi_local_linear_trend().
sts_semi_local_linear_trend(). sts_smooth_seasonal_state_space_model(). sts_smooth_seasonal().
sts_sparse_linear_regression(). sts_sum()

---

**sts_fit_with_hmc**

*Draw posterior samples using Hamiltonian Monte Carlo (HMC)*

Description
Markov chain Monte Carlo (MCMC) methods are considered the gold standard of Bayesian inference; under suitable conditions and in the limit of infinitely many draws they generate samples from the true posterior distribution. HMC (Neal, 2011) uses gradients of the model’s log-density function to propose samples, allowing it to exploit posterior geometry. However, it is computationally more expensive than variational inference and relatively sensitive to tuning.
Usage

```r
calls_fit_with_hmc(
  observed_time_series,
  model,
  num_results = 100,
  num_warmup_steps = 50,
  num_leapfrog_steps = 15,
  initial_state = NULL,
  initial_step_size = NULL,
  chain_batch_shape = list(),
  num_variational_steps = 150,
  variational_optimizer = NULL,
  variational_sample_size = 5,
  seed = NULL,
  name = NULL
)
```

Arguments

- **observed_time_series**: float tensor of shape `concat([sample_shape, model.batch_shape, [num_timesteps, 1]])` where `sample_shape` corresponds to i.i.d. observations, and the trailing [1] dimension may (optionally) be omitted if `num_timesteps > 1`. May optionally be an instance of `sts_masked_time_series`, which includes a mask tensor to specify timesteps with missing observations.

- **model**: An instance of `StructuralTimeSeries` representing a time-series model. This represents a joint distribution over time-series and their parameters with batch shape `[b1, ..., bN]`.

- **num_results**: Integer number of Markov chain draws. Default value: 100.

- **num_warmup_steps**: Integer number of steps to take before starting to collect results. The warmup steps are also used to adapt the step size towards a target acceptance rate of 0.75. Default value: 50.

- **num_leapfrog_steps**: Integer number of steps to run the leapfrog integrator for. Total progress per HMC step is roughly proportional to `step_size * num_leapfrog_steps`. Default value: 15.

- **initial_state**: Optional Python list of Tensors, one for each model parameter, representing the initial state(s) of the Markov chain(s). These should have shape `tf$concat(list(chain_batch_shape))`. If NULL, the initial state is set automatically using a sample from a variational posterior. Default value: NULL.

- **initial_step_size**: list of tensors, one for each model parameter, representing the step size for the leapfrog integrator. Must broadcast with the shape of `initial_state`. Larger step sizes lead to faster progress, but too-large step sizes make rejection exponentially more likely. If NULL, the step size is set automatically using the standard deviation of a variational posterior. Default value: NULL.
chain_batch_shape

Batch shape (list or int) of chains to run in parallel. Default value: list()
(i.e., a single chain).

num_variational_steps

int number of steps to run the variational optimization to determine the initial
state and step sizes. Default value: 150.

variational_optimizer

Optional tf$train$Optimizer instance to use in the variational optimization.
If NULL, defaults to tf$train$AdamOptimizer(0.1). Default value: NULL.

variational_sample_size

integer number of Monte Carlo samples to use in estimating the variational di-
vergence. Larger values may stabilize the optimization, but at higher cost per
step in time and memory. Default value: 1.

seed

integer to seed the random number generator.

name

name prefixed to ops created by this function. Default value: NULL (i.e., ‘fit_with_hmc’).

Details

This method attempts to provide a sensible default approach for fitting StructuralTimeSeries models
using HMC. It first runs variational inference as a fast posterior approximation, and initializes the
HMC sampler from the variational posterior, using the posterior standard deviations to set per-
variable step sizes (equivalently, a diagonal mass matrix). During the warmup phase, it adapts the
step size to target an acceptance rate of 0.75, which is thought to be in the desirable range for
optimal mixing (Betancourt et al., 2014).

Value

list of:

- samples: list of Tensors representing posterior samples of model parameters, with shapes
  [concat([num_results], chain_batch_shape, param.prior.batch_shape, param.prior.event_shape)] for
  param in model.parameters.

- kernel_results: A (possibly nested) list of Tensors representing internal calculations made
  within the HMC sampler.

References

- Radford Neal. MCMC Using Hamiltonian Dynamics. *Handbook of Markov Chain Monte
  Carlo*, 2011.

- M.J. Betancourt, Simon Byrne, and Mark Girolami. Optimizing The Integrator Step Size for
  Hamiltonian Monte Carlo.

See Also

Other sts-functions: sts_build_factored_surrogate_posterior(), sts_build_factored_variational_loss(),
sts_decompose_by_component(), sts_decompose_forecast_by_component(), sts_forecast(),
sts_one_step_predictive(), sts_sample_uniform_initial_state()
Examples

```r
observed_time_series <-
  rep(c(3.5, 4.1, 4.5, 3.9, 2.4, 2.1, 1.2), 5) +
  rep(c(1.1, 1.5, 2.4, 3.1, 4.0), each = 7) %>%
  tensorflow::tf$convert_to_tensor(dtype = tensorflow::tf$float64)
day_of_week <- observed_time_series %>% sts_seasonal(num_seasons = 7)
local_linear_trend <- observed_time_series %>% sts_local_linear_trend()
model <- observed_time_series %>%
  sts_sum(components = list(day_of_week, local_linear_trend))
states_and_results <- observed_time_series %>%
  sts_fit_with_hmc(
    model,
    num_results = 10,
    num_warmup_steps = 5,
    num_variational_steps = 15)
```

### sts_forecast

Construct predictive distribution over future observations

**Description**

Given samples from the posterior over parameters, return the predictive distribution over future observations for `num_steps_forecast` timesteps.

**Usage**

```r
sts_forecast(
  observed_time_series, 
  model, 
  parameter_samples, 
  num_steps_forecast 
)
```

**Arguments**

- `observed_time_series`  
  float tensor of shape `concat([sample_shape, model.batch_shape, [num_timesteps, 1]])`  
  where `sample_shape` corresponds to i.i.d. observations, and the trailing `[1]` dimension may (optionally) be omitted if `num_timesteps > 1`. May optionally be an instance of `sts_masked_time_series`, which includes a mask tensor to specify timesteps with missing observations.

- `model`  
  An instance of `StructuralTimeSeries` representing a time-series model. This represents a joint distribution over time-series and their parameters with batch shape `[b1, ..., bN]`. 
`parameter_samples`  
list of tensors representing posterior samples of model parameters, with  
shapes `list(tf$concat(list(list(num_posterior_draws), param<1>$prior$batch_shape, param<1>$prior$event_shape), list(list(num_posterior_draws), param<2>$prior$batch_shape, param<2>$prior$event_shape), ... )`  
for all model parameters. This may optionally also be a named list mapping parameter names to tensor values.

`num_steps_forecast`  
scalar integer tensor number of steps to forecast

**Value**

`forecast_dist` a `tfd_mixture_same_family` instance with event shape `list(num_steps_forecast,1)`  
and batch shape `tf$concat(list(sample_shape,model$batch_shape))`, with `num_posterior_draws` mixture components.

**See Also**

Other `sts`-functions: `sts_build_factored_surrogate_posterior()`, `sts_build_factored_variational_loss()`,  
`sts_decompose_by_component()`, `sts_decompose_forecast_by_component()`, `sts_fit_with_hmc()`,  
`sts_one_step_predictive()`, `sts_sample_uniform_initial_state()`

**Examples**

```r
observed_time_series <-
  rep(c(3.5, 4.1, 4.5, 3.9, 2.4, 2.1, 1.2), 5) +
  rep(c(1.1, 1.5, 2.4, 3.1, 4.0), each = 7) %>%
  tensorflow::tf$convert_to_tensor(dtype = tensorflow::tf$float64)
day_of_week <- observed_time_series %>% sts_seasonal(num_seasons = 7)
local_linear_trend <- observed_time_series %>% sts_local_linear_trend()
model <- observed_time_series %>%
  sts_sum(components = list(day_of_week, local_linear_trend))
states_and_results <- observed_time_series %>%
  sts_fit_with_hmc(model,  
                   num_results = 10,  
                   num_warmup_steps = 5,  
                   numVariationalSteps = 15)
samples <- states_and_results[[1]]
preds <- observed_time_series %>%
  sts_forecast(model,  
               parameter_samples = samples,  
               num_steps_forecast = 50)
predictions <- preds %>% tfd_sample(10)
```
**sts_linear_regression**  
Formal representation of a linear regression from provided covariates.

**Description**

This model defines a time series given by a linear combination of covariate time series provided in a design matrix:

$$\text{observed\_time\_series} \leftarrow \text{tf\$matmul(design\_matrix, weights)}$$

**Usage**

```
sts_linear_regression(design_matrix, weights_prior = NULL, name = NULL)
```

**Arguments**

- **design_matrix** float tensor of shape `tf$concat(list(batch_shape, list(num_timesteps, num_features)))`. This may also optionally be an instance of `tf$linalg$LinearOperator`.
- **weights_prior** Distribution representing a prior over the regression weights. Must have event shape `list(num_features)` and batch shape broadcastable to the design matrix’s batch_shape. Alternately, event_shape may be scalar (list()), in which case the prior is internally broadcast as `tfd_transformed_distribution(weights_prior, tfb_identity(), event_shape = list(num_features), batch_shape = design_matrix$batch_shape)`. If NULL, defaults to `tfd_student_t(df = 5, loc = 0, scale = 10)`, a weakly-informative prior loosely inspired by the *Stan prior choice recommendations*. Default value: NULL.
- **name** the name of this model component. Default value: ’LinearRegression’.

**Details**

The design matrix has shape `list(num_timesteps, num_features)`. The weights are treated as an unknown random variable of size `list(num_features)` (both components also support batch shape), and are integrated over using the same approximate inference tools as other model parameters, i.e., generally HMC or variational inference.

This component does not itself include observation noise; it defines a deterministic distribution with mass at the point `tf$matmul(design_matrix, weights)`. In practice, it should be combined with observation noise from another component such as `sts_sum`, as demonstrated below.

**Value**

an instance of `StructuralTimeSeries`. 
See Also

For usage examples see `sts_fit_with_hmc()`, `sts_forecast()`, `sts_decompose_by_component()`.

Other `sts`: `sts_additive_state_space_model()`, `sts_autoregressive_state_space_model()`, `sts_autoregressive()`, `sts_constrained_seasonal_state_space_model()`, `sts_dynamic_linear_regression_state_space_model()`, `sts_dynamic_linear_regression()`, `sts_local_level_state_space_model()`, `sts_local_level()`, `sts_local_linear_trend_state_space_model()`, `sts_local_linear_trend()`, `sts_seasonal_state_space_model()`, `sts_seasonal()`, `sts_semi_local_linear_trend_state_space_model()`, `sts_semi_local_linear_trend()`, `sts_smooth_seasonal_state_space_model()`, `sts_smooth_seasonal()`, `sts_sparse_linear_regression()`, `sts_sum()`

---

**sts_local_level**

*Formal representation of a local level model*

---

**Description**

The local level model posits a level evolving via a Gaussian random walk:

\[
\text{level}[t] = \text{level}[t-1] + \text{Normal}(0, \text{level_scale})
\]

**Usage**

```r
sts_local_level(
  observed_time_series = NULL,
  level_scale_prior = NULL,
  initial_level_prior = NULL,
  name = NULL
)
```

**Arguments**

- `observed_time_series`:
  - `optional float tensor of shape batch_shape + [T, 1]` (omitting the trailing unit dimension is also supported when \( T > 1 \)), specifying an observed time series.
  - Any priors not explicitly set will be given default values according to the scale of the observed time series (or batch of time series). May optionally be an instance of `sts_masked_time_series`, which includes a mask tensor to specify timesteps with missing observations. Default value: `NULL`.

- `level_scale_prior`:
  - `optional tfp$distribution instance specifying a prior on the level_scale parameter. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL`.

- `initial_level_prior`:
  - `optional tfp$distribution instance specifying a prior on the initial level. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL`.

- `name`:
  - `the name of this model component. Default value: 'LocalLevel'`.
sts_local_level_state_space_model

Details

The latent state is $[\text{level}]$. We observe a noisy realization of the current level: $f[t] = \text{level}[t] + \text{Normal}(0., \text{observation_noise_scale})$ at each timestep.

Value

an instance of StructuralTimeSeries.

See Also

For usage examples see \texttt{sts_fit_with_hmc()}, \texttt{sts_forecast()}, \texttt{sts_decompose_by_component()}.

Other \texttt{sts}: \texttt{sts_additive_state_space_model()}, \texttt{sts_autoregressive_state_space_model()}, \texttt{sts_autoregressive()}, \texttt{sts_constrained_seasonal_state_space_model()}, \texttt{sts_dynamic_linear_regression_state_space_model()}, \texttt{sts_dynamic_linear_regression()}, \texttt{sts_linear_regression()}, \texttt{sts_local_level_state_space_model()}, \texttt{sts_local_linear_trend_state_space_model()}, \texttt{sts_local_linear_trend()}, \texttt{sts_seasonal_state_space_model()}, \texttt{sts_seasonal()}, \texttt{sts_semi_local_linear_trend_state_space_model()}, \texttt{sts_semi_local_linear_trend()}, \texttt{sts_smooth_seasonal_state_space_model()}, \texttt{sts_smooth_seasonal()}, \texttt{sts_sparse_linear_regression()}, \texttt{sts_sum()}

\begin{verbatim}
  sts_local_level_state_space_model(num_timesteps, level_scale, initial_state_prior
observation_noise_scale = 0,
initial_step = 0, validate_args = FALSE,
allow_nan_stats = TRUE,
name = NULL)
\end{verbatim}

Description

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$. The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see \texttt{tfd_linear_gaussian_state_space_model} for details. The local level model is a special case of a linear Gaussian SSM, in which the latent state posits a level evolving via a Gaussian random walk:

$\text{level}[t] = \text{level}[t-1] + \text{Normal}(0., \text{level_scale})$

Usage

\begin{verbatim}
  sts_local_level_state_space_model(num_timesteps, level_scale, initial_state_prior
observation_noise_scale = 0,
initial_step = 0, validate_args = FALSE,
allow_nan_stats = TRUE,
name = NULL)
\end{verbatim}
Argument

**num_timesteps**  
Scalar integer tensor number of timesteps to model with this distribution.

**level_scale**  
Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the level transitions.

**initial_state_prior**  
instance of `tfd_multivariate_normal` representing the prior distribution on latent states. Must have event shape `[1]` (as `tfd_linear_gaussian_state_space_model` requires a rank-1 event shape).

**observation_noise_scale**  
Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise.

**initial_step**  
Optional scalar integer tensor specifying the starting timestep. Default value: 0.

**validate_args** logical. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.

**allow_nan_stats** logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.

**name**  
string name prefixed to ops created by this class. Default value: "LocalLevelStateSpaceModel".

Details

The latent state is `[level]` and `[level]` is observed (with noise) at each timestep.

The parameters `level_scale` and `observation_noise_scale` are each (a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these parameters and of the `initial_state_prior`.

Mathematical Details

The local level model implements a `tfp$linear_gaussian_state_space_model` with `latent_size = 1` and `observation_size = 1`, following the transition model:

transition\_matrix = `[[1]]`
transition\_noise ~ N(loc = 0, scale = diag([level\_scale]))

which implements the evolution of level described above, and the observation model:

observation\_matrix = `[[1]]`
observation\_noise ~ N(loc = 0, scale = observation\_noise\_scale)

Value

an instance of `LinearGaussianStateSpaceModel`. 
See Also

Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model(),
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression()
sts_dynamic_linear_regression(), sts_linear_regression(), sts_local_level(), sts_local_linear_trend()
sts_local_linear_trend(), sts_seasonal_state_space_model(), sts_seasonal(), sts_semi_local_linear_trend()
sts_semi_local_linear_trend(), sts_smooth_seasonal_state_space_model(), sts_smooth_seasonal(),
sts_sparse_linear_regression(), sts_sum()

sts_local_linear_trend

Formal representation of a local linear trend model

Description

The local linear trend model posits a level and slope, each evolving via a Gaussian random walk:

\[
\text{level}[t] = \text{level}[t-1] + \text{slope}[t-1] + \text{Normal}(0., \text{level_scale})
\]
\[
\text{slope}[t] = \text{slope}[t-1] + \text{Normal}(0., \text{slope_scale})
\]

Usage

sts_local_linear_trend(
    observed_time_series = NULL,
    level_scale_prior = NULL,
    slope_scale_prior = NULL,
    initial_level_prior = NULL,
    initial_slope_prior = NULL,
    name = NULL
)

Arguments

observed_time_series
    optional float tensor of shape batch_shape + [T, 1] (omitting the trailing unit
dimension is also supported when T > 1), specifying an observed time series.
    Any priors not explicitly set will be given default values according to the scale
    of the observed time series (or batch of time series). May optionally be an in-
    stance of sts_masked_time_series, which includes a mask tensor to specify
timesteps with missing observations. Default value: NULL.

level_scale_prior
    optional tfp$Distribution instance specifying a prior on the level_scale
    parameter. If NULL, a heuristic default prior is constructed based on the provided
    observed_time_series. Default value: NULL.

erslope_scale_prior
    optional tfd$Distribution instance specifying a prior on the slope_scale
    parameter. If NULL, a heuristic default prior is constructed based on the provided
    observed_time_series. Default value: NULL.
initial_level_prior
optional tfp$distribution instance specifying a prior on the initial level. If NULL, a heuristic default prior is constructed based on the provided observed_time_series.
Default value: NULL.

initial_slope_prior
optional tfd$Distribution instance specifying a prior on the initial slope. If NULL, a heuristic default prior is constructed based on the provided observed_time_series.
Default value: NULL.

name
the name of this model component. Default value: 'LocalLinearTrend'.

Details
The latent state is the two-dimensional tuple [level, slope]. At each timestep we observe a noisy realization of the current level: 
\[ f[t] = \text{level}[t] + \text{Normal}(0,\text{observation_noise_scale}) \]
This model is appropriate for data where the trend direction and magnitude (latent slope) is consistent within short periods but may evolve over time.

Note that this model can produce very high uncertainty forecasts, as uncertainty over the slope compounds quickly. If you expect your data to have nonzero long-term trend, i.e. that slopes tend to revert to some mean, then the SemiLocalLinearTrend model may produce sharper forecasts.

Value
an instance of StructuralTimeSeries.

See Also
For usage examples see sts_fit_with_hmc(), sts_forecast(), sts_decompose_by_component().
Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model().
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state_space_model(), sts_local_linear_trend_state_space_model(), sts_seasonal_state_space_model(),
sts_smooth_seasonal_state_space_model(), sts_sum()

Description
A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model \( p(z[t+1] | z[t]) \). At each timestep, we observe a value sampled from an observation model conditioned on the current state, \( p(x[t] | z[t]) \). The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see tfd_linear_gaussian_state_space_model for details.
sts_local_linear_trend_state_space_model

Usage

sts_local_linear_trend_state_space_model(
    num_timesteps,
    level_scale,
    slope_scale,
    initial_state_prior,
    observation_noise_scale = 0,
    initial_step = 0,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = NULL
)

Arguments

num_timesteps Scalar integer tensor number of timesteps to model with this distribution.
level_scale Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the level transitions.
slope_scale Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the slope transitions.
initial_state_prior instance of tfd_multivariate_normal representing the prior distribution on latent states. Must have event shape [1](as tfd_linear_gaussian_state_space_model requires a rank-1 event shape).
observation_noise_scale Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise.
initial_step Optional scalar integer tensor specifying the starting timestep. Default value: 0.
validate_args logical. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.
allow_nan_stats logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.
name string prefixed to ops created by this class. Default value: "LocalLinearTrendStateSpaceModel".

Details

The local linear trend model is a special case of a linear Gaussian SSM, in which the latent state posits a level and slope, each evolving via a Gaussian random walk:

level[t] = level[t-1] + slope[t-1] + Normal(0., level_scale)
slope[t] = slope[t-1] + Normal(0., slope_scale)
The latent state is the two-dimensional tuple \([\text{level}, \text{slope}]\). The \text{level} is observed at each timestep. The parameters \text{level\_scale}, \text{slope\_scale}, and \text{observation\_noise\_scale} are each (a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these parameters and of the \text{initial\_state\_prior}.

Mathematical Details

The linear trend model implements a \text{tfd\_linear\_gaussian\_state\_space\_model} with \text{latent\_size} = 2 and \text{observation\_size} = 1, following the transition model:

\[
\text{transition\_matrix} = \begin{bmatrix} 1. & 1. \\ 0. & 1. \end{bmatrix}
\]

\[
\text{transition\_noise} \sim \text{N}(\text{loc} = 0, \text{scale} = \text{diag}([\text{level\_scale}, \text{slope\_scale}])))
\]

which implements the evolution of \([\text{level, slope}]\) described above, and the observation model:

\[
\text{observation\_matrix} = \begin{bmatrix} 1. & 0. \end{bmatrix}
\]

\[
\text{observation\_noise} \sim \text{N}(\text{loc} = 0, \text{scale} = \text{observation\_noise\_scale})
\]

which picks out the first latent component, i.e., the \text{level}, as the observation at each timestep.

Value

an instance of \text{LinearGaussianStateSpaceModel}.

See Also

Other \text{sts}: \text{sts\_additive\_state\_space\_model()}, \text{sts\_autoregressive\_state\_space\_model()}, \text{sts\_autoregressive()}, \text{sts\_constrained\_seasonal\_state\_space\_model()}, \text{sts\_dynamic\_linear\_regression\_state\_space\_model()}, \text{sts\_dynamic\_linear\_regression()}, \text{sts\_linear\_regression()}, \text{sts\_local\_level\_state\_space\_model()}, \text{sts\_local\_level()}, \text{sts\_local\_linear\_trend()}, \text{sts\_seasonal\_state\_space\_model()}, \text{sts\_seasonal()}, \text{sts\_semi\_local\_linear\_trend\_state\_space\_model()}, \text{sts\_semi\_local\_linear\_trend()}, \text{sts\_smooth\_seasonal\_state\_space\_model()}, \text{sts\_smooth\_seasonal()}, \text{sts\_semi\_local\_linear\_trend\_state\_space\_model()}, \text{sts\_semi\_local\_linear\_trend()}, \text{sts\_smooth\_seasonal\_state\_space\_model()}, \text{sts\_smooth\_seasonal()}, \text{sts\_sparse\_linear\_regression()}, \text{sts\_sum}()

\text{sts\_one\_step\_predictive}  

\textit{Compute one-step-ahead predictive distributions for all timesteps}

Description

Given samples from the posterior over parameters, return the predictive distribution over observations at each time \(T\), given observations up through time \(T-1\).

Usage

\begin{verbatim}
sts_one_step_predictive(  
    observed_time_series,  
    model,  
    parameter_samples,  
    timesteps_are_event_shape = TRUE
)
\end{verbatim}
**sts_sample_uniform_initial_state**

Initialize from a uniform \([-2, 2]\) distribution in unconstrained space.

**Description**

Initialize from a uniform \([-2, 2]\) distribution in unconstrained space.

**Usage**

```r
sts_sample_uniform_initial_state(
  parameter,
  return_constrained = TRUE,
  init_sample_shape = list(),
  seed = NULL
)
```
**Arguments**

- **parameter**: sts$Parameter named tuple instance.
- **return_constrained**: if TRUE, re-applies the constraining bijector to return initializations in the original domain. Otherwise, returns initializations in the unconstrained space. Default value: TRUE.
- **init_sample_shape**: sample_shape of the sampled initializations. Default value: list().
- **seed**: integer to seed the random number generator.

**Value**

uniform_initializer Tensor of shape concat([init_sample_shape, parameter.prior.batch_shape, transformed_event_shape]), where transformed_event_shape is parameter.prior.event_shape, if return_constrained=TRUE, and otherwise it is parameter$bijector$inverse_event_shape(parameter$prior$event_shape).

**See Also**

Other sts-functions: `sts_build_factored_surrogate_posterior()`, `sts_build_factored_variational_loss()`, `sts_decompose_by_component()`, `sts_decompose_forecast_by_component()`, `sts_fit_with_hmc()`, `sts_forecast()`, `sts_one_step_predictive()`

---

**sts_seasonal**

*Formal representation of a seasonal effect model.*

**Description**

A seasonal effect model posits a fixed set of recurring, discrete 'seasons', each of which is active for a fixed number of timesteps and, while active, contributes a different effect to the time series. These are generally not meteorological seasons, but represent regular recurring patterns such as hour-of-day or day-of-week effects. Each season lasts for a fixed number of timesteps. The effect of each season drifts from one occurrence to the next following a Gaussian random walk:

**Usage**

```r
sts_seasonal(
  observed_time_series = NULL,
  num_seasons,
  num_steps_per_season = 1,
  drift_scale_prior = NULL,
  initial_effect_prior = NULL,
  constrain_mean_effect_to_zero = TRUE,
  name = NULL
)
```
Arguments

observed_time_series
optional float tensor of shape batch_shape + [T, 1] (omitting the trailing unit
dimension is also supported when T > 1), specifying an observed time series.
Any priors not explicitly set will be given default values according to the scale
of the observed time series (or batch of time series). May optionally be an in-
stance of sts_masked_time_series, which includes a mask tensor to specify
timesteps with missing observations. Default value: NULL.

num_seasons
Scalar integer number of seasons.

num_steps_per_season
integer number of steps in each season. This may be either a scalar (shape []),
in which case all seasons have the same length, or an array of shape [num_seasons],
in which seasons have different length, but remain constant around different cy-
cles, or an array of shape [num_cycles, num_seasons], in which num_steps_per_season
for each season also varies in different cycle (e.g., a 4 years cycle with leap day).
Default value: 1.

drift_scale_prior
optional tfd$Distribution instance specifying a prior on the drift_scale
parameter. If NULL, a heuristic default prior is constructed based on the provided
observed_time_series. Default value: NULL.

initial_effect_prior
optional tfd$Distribution instance specifying a normal prior on the initial
effect of each season. This may be either a scalar tfd_normal prior, in which
case it applies independently to every season, or it may be multivariate normal
(e.g., tfd_multivariate_normal_diag) with event shape [num_seasons], in
which case it specifies a joint prior across all seasons. If NULL, a heuristic default
prior is constructed based on the provided observed_time_series. Default
value: NULL.

constrain_mean_effect_to_zero
if TRUE, use a model parameterization that constrains the mean effect across
all seasons to be zero. This constraint is generally helpful in identifying the
contributions of different model components and can lead to more interpretable
posterior decompositions. It may be undesirable if you plan to directly examine
the latent space of the underlying state space model. Default value: TRUE.

name
the name of this model component. Default value: 'Seasonal'.

Details

effects[season, occurrence[i]] = (  
effects[season, occurrence[i-1]] + Normal(loc=0., scale=drift_scale))

The drift_scale parameter governs the standard deviation of the random walk; for example, in a
day-of-week model it governs the change in effect from this Monday to next Monday.

Value

an instance of StructuralTimeSeries.
See Also

For usage examples see `sts_fit_with_hmc()`, `sts_forecast()`, `sts_decompose_by_component()`.

Other `sts`: `sts_additive_state_space_model()`, `sts_autoregressive_state_space_model()`, `sts_autoregressive()`, `sts_constrained_seasonal_state_space_model()`, `sts_dynamic_linear_regression_state_space_model()`, `sts_dynamic_linear_regression()`, `sts_linear_regression()`, `sts_local_level_state_space_model()`, `sts_local_level()`, `sts_local_linear_trend_state_space_model()`, `sts_local_linear_trend()`, `sts_seasonal_state_space_model()`, `sts_semi_local_linear_trend_state_space_model()`, `sts_semi_local_linear_trend()`, `sts_smooth_seasonal_state_space_model()`, `sts_smooth_seasonal()`, `sts_sparse_linear_regression()`, `sts_sum()`

---

`sts_seasonal_state_space_model`

*State space model for a seasonal effect.*

---

**Description**

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$. The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see `tfd_linear_gaussian_state_space_model` for details.

**Usage**

```r
sts_seasonal_state_space_model(
  num_timesteps,  # Scalar integer tensor number of timesteps to model with this distribution.
  num_seasons,    # Scalar integer number of seasons.
  drift_scale,    # Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the change in effect between consecutive occurrences of a given season. This is assumed to be the same for all seasons.
  initial_state_prior,
  observation_noise_scale = 0,
  num_steps_per_season = 1,
  initial_step = 0,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = NULL
)
```

**Arguments**

- `num_timesteps`
  - Scalar integer tensor
  - Number of timesteps to model with this distribution.

- `num_seasons`
  - Scalar integer
  - Number of seasons.

- `drift_scale`
  - Scalar (any additional dimensions are treated as batch dimensions)
  - Float tensor indicating the standard deviation of the change in effect between consecutive occurrences of a given season. This is assumed to be the same for all seasons.
initial_state_prior
instance of tfd_multivariate_normal representing the prior distribution on latent states; must have event shape [num_seasons].

observation_noise_scale
Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise.

num_steps_per_season
integer number of steps in each season. This may be either a scalar (shape []), in which case all seasons have the same length, or an array of shape [num_seasons], in which seasons have different length, but remain constant around different cycles, or an array of shape [num_cycles, num_seasons], in which num_steps_per_season for each season also varies in different cycle (e.g., a 4 years cycle with leap day). Default value: 1.

initial_step
Optional scalar integer tensor specifying the starting timestep. Default value: 0.

validate_args
logical. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.

allow_nan_stats
logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.

name
string prefixed to ops created by this class. Default value: "SeasonalStateSpaceModel".

Details
A seasonal effect model is a special case of a linear Gaussian SSM. The latent states represent an unknown effect from each of several 'seasons'; these are generally not meteorological seasons, but represent regular recurring patterns such as hour-of-day or day-of-week effects. The effect of each season drifts from one occurrence to the next, following a Gaussian random walk:

effects[season, occurrence[i]] = (effects[season, occurrence[i-1]] + Normal(loc=0., scale=drift_scale))

The latent state has dimension num_seasons, containing one effect for each seasonal component. The parameters drift_scale and observation_noise_scale are each (a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these parameters and of the initial_state_prior. Note: there is no requirement that the effects sum to zero.

Mathematical Details
The seasonal effect model implements a tfd_linear_gaussian_state_space_model with latent_size = num_seasons and observation_size = 1. The latent state is organized so that the current seasonal effect is always in the first (zeroth) dimension. The transition model rotates the latent state to shift to a new effect at the end of each season:

transition_matrix[t] = (permutation_matrix([1, 2, ..., num_seasons-1, 0]))
if season_is_changing(t)
else eye(num_seasons)
transition_noise[t] ~ Normal(loc=0., scale_diag=(
    [drift_scale, 0, ..., 0]
    if season_is_changing(t)
    else [0, 0, ..., 0]))

where season_is_changing(t) is True if t `mod` sum(num_steps_per_season) is in the set of final days for each season, given by cumsum(num_steps_per_season) -1. The observation model always picks out the effect for the current season, i.e., the first element of the latent state:

observation_matrix = [[1., 0., ..., 0.]]
observation_noise ~ Normal(loc=0, scale=observation_noise_scale)

Value
an instance of LinearGaussianStateSpaceModel.

See Also
Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model(),
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state_space_model(),
sts_dynamic_linear_regression(), sts_linear_regression(), sts_local_level_state_space_model(),
sts_local_level(), sts_local_linear_trend_state_space_model(), sts_local_linear_trend(),
sts_seasonal(), sts_semi_local_linear_trend_state_space_model(), sts_semi_local_linear_trend(),
sts_smooth_seasonal_state_space_model(), sts_smooth_seasonal(), sts_sparse_linear_regression(),
sts_sum()

sts_semi_local_linear_trend

Formal representation of a semi-local linear trend model.

Description
Like the sts_local_linear_trend model, a semi-local linear trend posits a latent level and slope, with the level component updated according to the current slope plus a random walk:

Usage

sts_semi_local_linear_trend(
    observed_time_series = NULL,
    level_scale_prior = NULL,
    slope_mean_prior = NULL,
    slope_scale_prior = NULL,
    autoregressive_coef_prior = NULL,
    initial_level_prior = NULL,
    initial_slope_prior = NULL,
    constrain_ar_coef_stationary = TRUE,
    constrain_ar_coef_positive = FALSE,
    name = NULL
)
Arguments

observed_time_series
optional float tensor of shape batch_shape + [T, 1] (omitting the trailing unit dimension is also supported when T > 1), specifying an observed time series. Any priors not explicitly set will be given default values according to the scale of the observed time series (or batch of time series). May optionally be an instance of sts_masked_time_series, which includes a mask tensor to specify timesteps with missing observations. Default value: NULL.

level_scale_prior
optional tfp$distribution instance specifying a prior on the level_scale parameter. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

slope_mean_prior
optional tfd$Distribution instance specifying a prior on the slope_mean parameter. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

elevel_slope_scale_prior
optional tfd$Distribution instance specifying a prior on the slope_scale parameter. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

autoregressive_coef_prior
optional tfd$Distribution instance specifying a prior on the autoregressive_coef parameter. If NULL, the default prior is a standard Normal(0, 1). Note that the prior may be implicitly truncated by constrain_ar_coef_stationary and/or constrain_ar_coef_positive. Default value: NULL.

initial_level_prior
optional tfp$distribution instance specifying a prior on the initial level. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

initial_slope_prior
optional tfd$Distribution instance specifying a prior on the initial slope. If NULL, a heuristic default prior is constructed based on the provided observed_time_series. Default value: NULL.

constrain_ar_coef_stationary
if TRUE, perform inference using a parameterization that restricts autoregressive_coef to the interval (-1, 1), or (0, 1) if force_positive_ar_coef is also TRUE, corresponding to stationary processes. This will implicitly truncate the support of autoregressive_coef_prior. Default value: TRUE.

constrain_ar_coef_positive
if TRUE, perform inference using a parameterization that restricts autoregressive_coef to be positive, or in (0, 1) if constrain_ar_coef_stationary is also TRUE. This will implicitly truncate the support of autoregressive_coef_prior. Default value: FALSE.

name
the name of this model component. Default value: ‘SemiLocalLinearTrend’.

Details

level[t] = level[t-1] + slope[t-1] + Normal(0., level_scale)
The slope component in a `sts_semi_local_linear_trend` model evolves according to a first-order autoregressive (AR1) process with potentially nonzero mean:

\[
slope[t] = (\text{slope_mean} + \text{autoregressive_coef} \times (\text{slope}[t-1] - \text{slope_mean}) + \text{Normal}(0., \text{slope_scale}))
\]

Unlike the random walk used in `LocalLinearTrend`, a stationary AR1 process (coefficient in \((-1, 1)\)) maintains bounded variance over time, so a `SemiLocalLinearTrend` model will often produce more reasonable uncertainties when forecasting over long timescales.

**Value**

an instance of `StructuralTimeSeries`.

**See Also**

For usage examples see `sts_fit_with_hmc()`, `sts_forecast()`, `sts_decompose_by_component()`.

Other `sts`:

- `sts_additive_state_space_model()`
- `sts_autoregressive_state_space_model()`
- `sts_autoregressive()`
- `sts_constrained_seasonal_state_space_model()`
- `sts_dynamic_linear_regression_state_space_model()`
- `sts_dynamic_linear_regression()`
- `sts_linear_regression()`
- `sts_local_level_state_space_model()`
- `sts_local_level()`
- `sts_local_linear_trend_state_space_model()`
- `sts_local_linear_trend()`
- `sts_seasonal_state_space_model()`
- `sts_seasonal()`
- `sts_semi_local_linear_trend_state_space_model()`
- `sts_semi_local_linear_trend()`
- `sts_smooth_seasonal_state_space_model()`
- `sts_smooth_seasonal()`
- `sts_sparse_linear_regression()`
- `sts_sum()`

---

`sts_semi_local_linear_trend_state_space_model`

*State space model for a semi-local linear trend.*

**Description**

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model \(p(z[t+1] | z[t])\). At each timestep, we observe a value sampled from an observation model conditioned on the current state, \(p(x[t] | z[t])\). The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see `tfd_linear_gaussian_state_space_model` for details.

**Usage**

```python
sts_semi_local_linear_trend_state_space_model(
    num_timesteps,
    level_scale,  # Required
    slope_mean,  # Required
    slope_scale,  # Required
    autoregressive_coef=0.5,  # Optional, default is 0.5
    initial_state_prior=
)```
observation_noise_scale = 0,
initial_step = 0,
validate_args = FALSE,
allow_nan_stats = TRUE,
name = NULL
)

Arguments

num_timesteps  Scalar integer tensor number of timesteps to model with this distribution.
level_scale  Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the level transitions.
slope_mean  Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the expected long-term mean of the latent slope.
slope_scale  Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the slope transitions.
autoregressive_coef  Scalar (any additional dimensions are treated as batch dimensions) float tensor defining the AR1 process on the latent slope.
initial_state_prior  instance of tfd_multivariate_normal representing the prior distribution on latent states. Must have event shape [1](as tfd_linear_gaussian_state_space_model requires a rank-1 event shape).
observation_noise_scale  Scalar (any additional dimensions are treated as batch dimensions) float tensor indicating the standard deviation of the observation noise.
initial_step  Optional scalar integer tensor specifying the starting timestep. Default value: 0.
validate_args  logical. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed. Default value: FALSE.
allow_nan_stats  logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is undefined for any batch member. If TRUE, batch members with valid parameters leading to undefined statistics will return NaN for this statistic. Default value: TRUE.
name  string‘ prefixed to ops created by this class. Default value: “SemiLocalLinearTrendStateSpaceModel”.

Details

The semi-local linear trend model is a special case of a linear Gaussian SSM, in which the latent state posits a level and slope. The level evolves via a Gaussian random walk centered at the current slope, while the slope follows a first-order autoregressive (AR1) process with mean slope_mean:
level[t] = level[t-1] + slope[t-1] + Normal(0, level_scale)
slope[t] = (slope_mean + autoregressive_coef * (slope[t-1] - slope_mean) + Normal(0., slope_scale))

The latent state is the two-dimensional tuple [level, slope]. The level is observed at each timestep. The parameters level_scale, slope_mean, slope_scale, autoregressive_coef, and observation_noise_scale are each (a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these parameters and of the initial_state_prior.

Mathematical Details

The semi-local linear trend model implements a tfp.distributions.LinearGaussianStateSpaceModel with latent_size = 2 and observation_size = 1, following the transition model:

transition_matrix = [[1., 1.]
[0., autoregressive_coef]]
transition_noise ~ N(loc=slope_mean - autoregressive_coef * slope_mean, scale=diag([level_scale, slope_scale]))

which implements the evolution of [level, slope] described above, and the observation model:

observation_matrix = [[1., 0.]]
observation_noise ~ N(loc=0, scale=observation_noise_scale)

which picks out the first latent component, i.e., the level, as the observation at each timestep.

Value

an instance of LinearGaussianStateSpaceModel.

See Also

Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model(),
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state_space_model(),
sts_dynamic_linear_regression(), sts_linear_regression(), sts_local_level_state_space_model(),
sts_local_level(), sts_local_linear_trend_state_space_model(), sts_local_linear_trend(),
sts_seasonal_state_space_model(), sts_seasonal(), sts_smooth_seasonal_state_space_model(),
sts_smooth_seasonal(), sts_sparse_linear_regression(), sts_sum()

sts_smooth_seasonal  Formal representation of a smooth seasonal effect model

Description

The smooth seasonal model uses a set of trigonometric terms in order to capture a recurring pattern whereby adjacent (in time) effects are similar. The model uses frequencies calculated via:
sts_smooth_seasonal

Usage

sts_smooth_seasonal(
    period,
    frequency_multipliers,
    allow_drift = TRUE,
    drift_scale_prior = NULL,
    initial_state_prior = NULL,
    observed_time_series = NULL,
    name = NULL
)

Arguments

period positive scalar float Tensor giving the number of timesteps required for the longest cyclic effect to repeat.

drft-scale_prior

allow_drift optional logical specifying whether the seasonal effects can drift over time. Setting this to FALSE removes the drift_scale parameter from the model. This is mathematically equivalent to drift_scale_prior = tfd.Deterministic(0.), but removing drift directly is preferred because it avoids the use of a degenerate prior. Default value: TRUE.

initial_state_prior

observed_time_series

name the name of this model component. Default value: 'LocalLinearTrend'.

Details

frequencies[j] = 2. * pi * frequency_multipliers[j] / period
and then posits two latent states for each frequency. The two latent states associated with frequency $j$ drift over time via:

$$
effect[t] = (effect[t-1] \times \cos(frequencies[j]) +
\quad auxiliary[t-1] \times \sin(frequencies[j]) +
\quad \text{Normal}(0., \text{drift_scale})
$$

$$auxiliary[t] = (-effect[t-1] \times \sin(frequencies[j]) +
\quad auxiliary[t-1] \times \cos(frequencies[j]) +
\quad \text{Normal}(0., \text{drift_scale})$$

where effect is the smooth seasonal effect and auxiliary only appears as a matter of construction. The interpretation of auxiliary is thus not particularly important.

Value

an instance of StructuralTimeSeries.

See Also

For usage examples see `sts_fit_with_hmc()`, `sts_forecast()`, `sts_decompose_by_component()`.

Other sts: `sts_additive_state_space_model()`, `sts_autoregressive_state_space_model()`,
`sts_autoregressive()`, `sts_constrained_seasonal_state_space_model()`,
`sts_dynamic_linear_regression_state_space_model()`, `sts_dynamic_linear_regression()`,
`sts_local_level_state_space_model()`, `sts_local_level()`,
`sts_local_linear_trend_state_space_model()`, `sts_local_linear_trend()`,
`sts_seasonal_state_space_model()`, `sts_seasonal()`,
`sts_semi_local_linear_trend_state_space_model()`,
`sts_semi_local_linear_trend()`, `sts_smooth_seasonal_state_space_model()`,
`sts_sparse_linear_regression()`,
`sts_sum()`

---

**sts_smooth_seasonal_state_space_model**

*State space model for a smooth seasonal effect*

### Description

A state space model (SSM) posits a set of latent (unobserved) variables that evolve over time with dynamics specified by a probabilistic transition model $p(z[t+1] | z[t])$. At each timestep, we observe a value sampled from an observation model conditioned on the current state, $p(x[t] | z[t])$.

The special case where both the transition and observation models are Gaussians with mean specified as a linear function of the inputs, is known as a linear Gaussian state space model and supports tractable exact probabilistic calculations; see `tfp$\text{distributions}$LinearGaussianStateSpaceModel` for details. A smooth seasonal effect model is a special case of a linear Gaussian SSM. It is the sum of a set of "cyclic" components, with one component for each frequency:

$$frequencies[j] = 2. \times \pi \times frequency\_multipliers[j] / \text{period}$$

Each cyclic component contains two latent states which we denote effect and auxiliary. The two latent states for component $j$ drift over time via:
\[
\text{effect}[t] = (\text{effect}[t-1] \ast \cos(\text{frequencies}[j]) + \\
\text{auxiliary}[t-] \ast \sin(\text{frequencies}[j]) + \\
\text{Normal}(0., \text{drift_scale}))
\]

\[
\text{auxiliary}[t] = (-\text{effect}[t-1] \ast \sin(\text{frequencies}[j]) + \\
\text{auxiliary}[t-] \ast \cos(\text{frequencies}[j]) + \\
\text{Normal}(0., \text{drift_scale}))
\]

**Usage**

\[
\text{sts_smooth_seasonal_state_space_model}( \\
\text{num_timesteps,} \\
\text{period,} \\
\text{frequency_multipliers,} \\
\text{drift_scale,} \\
\text{initial_state_prior,} \\
\text{observation_noise_scale = 0,} \\
\text{initial_step = 0,} \\
\text{validate_args = FALSE,} \\
\text{allow_nan_stats = TRUE,} \\
\text{name = NULL}
\)

**Arguments**

- **num_timesteps**: Scalar integer Tensor number of timesteps to model with this distribution.
- **period**: positive scalar float Tensor giving the number of timesteps required for the longest cyclic effect to repeat.
- **frequency_multipliers**: One-dimensional float Tensor listing the frequencies (cyclic components) included in the model, as multipliers of the base/fundamental frequency \(2 \ast \pi / \text{period}\). Each component is specified by the number of times it repeats per period, and adds two latent dimensions to the model. A smooth seasonal model that can represent any periodic function is given by \(\text{frequency_multipliers} = [1, 2, \ldots, \text{floor}(\text{period} / 2)]\). However, it is often desirable to enforce a smoothness assumption (and reduce the computational burden) by dropping some of the higher frequencies.
- **drift_scale**: Scalar (any additional dimensions are treated as batch dimensions) float Tensor indicating the standard deviation of the latent state transitions.
- **initial_state_prior**: instance of \texttt{tfd\$MultivariateNormal} representing the prior distribution on latent states. Must have event shape \([\text{num_features}]\).
- **observation_noise_scale**: Scalar (any additional dimensions are treated as batch dimensions) float Tensor indicating the standard deviation of the observation noise. Default value: 0.
- **initial_step**: scalar integer Tensor specifying the starting timestep. Default value: 0.
- **validate_args**: logical. Whether to validate input with asserts. If \texttt{validate_args} is \texttt{FALSE}, and the inputs are invalid, correct behavior is not guaranteed. Default value: \texttt{FALSE}.
allow_nan_stats

logical. If FALSE, raise an exception if a statistic (e.g. mean/mode/etc...) is
undefined for any batch member. If TRUE, batch members with valid parameters
leading to undefined statistics will return NaN for this statistic. Default value:
TRUE.

name

string prefixed to ops created by this class. Default value: "LocalLinearTrend-
StateSpaceModel".

Details

The auxiliary latent state only appears as a matter of construction and thus its interpretation is not
particularly important. The total smooth seasonal effect is the sum of the effect values from each
of the cyclic components. The parameters drift_scale and observation_noise_scale are each
(a batch of) scalars. The batch shape of this Distribution is the broadcast batch shape of these
parameters and of the initial_state_prior.

Mathematical Details

The smooth seasonal effect model implements a tfp$distributions$LinearGaussianStateSpaceModel
with latent_size = 2 * len(frequency_multipliers) and observation_size = 1. The latent
state is the concatenation of the cyclic latent states which themselves comprise an effect and an
auxiliary state. The transition matrix is a block diagonal matrix where block j is:

$$transition_matrix[j] = \begin{bmatrix}
\cos(frequencies[j]), \sin(frequencies[j])
\end{bmatrix}
\begin{bmatrix}
-sin(frequencies[j]), \cos(frequencies[j])
\end{bmatrix}$$

The observation model picks out the cyclic effect values from the latent state:

$$observation_matrix = \begin{bmatrix}
1., 0., 1., 0., ..., 1., 0.
\end{bmatrix}$$

observation_noise ~ Normal(loc=0, scale=observation_noise_scale)

For further mathematical details please see Harvey (1990).

Value

an instance of LinearGaussianStateSpaceModel.

references

• Harvey, A. Forecasting, Structural Time Series Models and the Kalman Filter. Cambridge:

See Also

Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model(),
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state
seasonal_state_space_model(), sts_seasonal(), sts_semi_local_linear_trend_state_space_model()
Description

This model defines a time series given by a sparse linear combination of covariate time series provided in a design matrix:

Usage

```r
sts_sparse_linear_regression(
  design_matrix,
  weights_prior_scale = 0.1,
  weights_batch_shape = NULL,
  name = NULL
)
```

Arguments

- `design_matrix`: float tensor of shape `tf$concat(list(batch_shape,list(num_timesteps,num_features)))`. This may also optionally be an instance of `tf$linalg$LinearOperator`.
- `weights_prior_scale`: float Tensor defining the scale of the Horseshoe prior on regression weights. Small values encourage the weights to be sparse. The shape must broadcast with `weights_batch_shape`. Default value: 0.1.
- `weights_batch_shape`: if NULL, defaults to `design_matrix$batch_shape$tf$.tensor()`. Must broadcast with the batch shape of `design_matrix`. Default value: NULL.
- `name`: the name of this model component. Default value: 'LinearRegression'.

Details

```r
observed_time_series <- tf$matmul(design_matrix, weights)
```

This is identical to `sts_linear_regression`, except that `sts_sparse_linear_regression` uses a parameterization of a Horseshoe prior to encode the assumption that many of the weights are zero, i.e., many of the covariate time series are irrelevant. See the mathematical details section below for further discussion. The prior parameterization used by `sts_sparse_linear_regression` is more suitable for inference than that obtained by simply passing the equivalent `tfd_horseshoe` prior to `sts_linear_regression`; when sparsity is desired, `sts_sparse_linear_regression` will likely yield better results.

This component does not itself include observation noise; it defines a deterministic distribution with mass at the point `tf$matmul(design_matrix, weights)`. In practice, it should be combined with observation noise from another component such as `sts_sum`.

Mathematical Details

The basic horseshoe prior Carvalho et al. (2009) is defined as a Cauchy-normal scale mixture:
```plaintext
scales[i] ~ HalfCauchy(loc=0, scale=1)
weights[i] ~ Normal(loc=0., scale=scales[i] * global_scale)
```

The Cauchy scale parameters puts substantial mass near zero, encouraging weights to be sparse, but their heavy tails allow weights far from zero to be estimated without excessive shrinkage. The horseshoe can be thought of as a continuous relaxation of a traditional ‘spike-and-slab’ discrete sparsity prior, in which the latent Cauchy scale mixes between ‘spike’ (scales[i] \(\approx\) 0) and ‘slab’ (scales[i] \(\gg\) 0) regimes.

Following the recommendations in Piironen et al. (2017), SparseLinearRegression implements a horseshoe with the following adaptations:

- The Cauchy prior on scales[i] is represented as an InverseGamma-Normal compound.
- The global_scale parameter is integrated out following a Cauchy(0, scale=weights_prior_scale) hyperprior, which is also represented as an InverseGamma-Normal compound.
- All compound distributions are implemented using a non-centered parameterization. The compound, non-centered representation defines the same marginal prior as the original horseshoe (up to integrating out the global scale), but allows samplers to mix more efficiently through the heavy tails; for variational inference, the compound representation implicitly expands the representational power of the variational model.

Note that we do not yet implement the regularized (‘Finnish’) horseshoe, proposed in Piironen et al. (2017) for models with weak likelihoods, because the likelihood in STS models is typically Gaussian, where it’s not clear that additional regularization is appropriate. If you need this functionality, please email tfprobability@tensorflow.org.

The full prior parameterization implemented in SparseLinearRegression is as follows:

```
Sample global_scale from Cauchy(0, scale=weights_prior_scale).
global_scale_variance ~ InverseGamma(alpha=0.5, beta=0.5)
global_scale_noncentered ~ HalfNormal(loc=0, scale=1)
local_scales = global_scale_noncentered *
sqrt(global_scale_variance) *
weights_prior_scale
Sample local_scales from Cauchy(0, 1).
local_scale_variances[i] ~ InverseGamma(alpha=0.5, beta=0.5)
local_scales_noncentered[i] ~ HalfNormal(loc=0, scale=1)
local_scales[i] = local_scales_noncentered[i] * sqrt(local_scale_variances[i])
weights[i] ~ Normal(loc=0., scale=local_scales[i] * global_scale)
```

Value

an instance of StructuralTimeSeries.

References

- Carvalho, C., Polson, N. and Scott, J. Handling Sparsity via the Horseshoe. AISTATS (2009).
See Also

For usage examples see `sts_fit_with_hmc()`, `sts_forecast()`, `sts_decompose_by_component()`.

Other `sts`: `sts_additive_state_space_model()`, `sts_autoregressive_state_space_model()`,
`sts_constrained_seasonal_state_space_model()`, `sts_dynamic_linear_regression_state_space_model()`,
`sts_local_level_state_space_model()`, `sts_local_linear_trend_state_space_model()`,
`sts_seasonal_state_space_model()`, `sts_seasonal()`, `sts_semi_local_linear_trend_state_space_model()`,
`sts_semi_local_linear_trend()`, `sts_smooth_seasonal_state_space_model()`, `sts_smooth_seasonal()`,
`sts_sum()`.

---

**sts_sum**  
*Sum of structural time series components.*

**Description**

This class enables compositional specification of a structural time series model from basic components. Given a list of component models, it represents an additive model, i.e., a model of time series that may be decomposed into a sum of terms corresponding to the component models.

**Usage**

```r
sts_sum(
  observed_time_series = NULL,
  components,
  constant_offset = NULL,
  observation_noise_scale_prior = NULL,
  name = NULL
)
```

**Arguments**

- **observed_time_series**
  optional float tensor of shape batch_shape + [T, 1] (omitting the trailing unit dimension is also supported when T > 1), specifying an observed time series. Any priors not explicitly set will be given default values according to the scale of the observed time series (or batch of time series). May optionally be an instance of `sts_masked_time_series`, which includes a mask tensor to specify timesteps with missing observations. Default value: `NULL`.

- **components**
  list of one or more `StructuralTimeSeries` instances. These must have unique names.

- **constant_offset**
  optional scalar float tensor, or batch of scalars, specifying a constant value added to the sum of outputs from the component models. This allows the components to model the shifted series `observed_time_series - constant_offset`. If `NULL`, this is set to the mean of the provided `observed_time_series`. Default value: `NULL`.
observation_noise_scale_prior
optional tfd$Distribution instance specifying a prior on observation_noise_scale.
If NULL, a heuristic default prior is constructed based on the provided observed_time_series.
Default value: NULL.

name
string name of this model component; used as name_scope for ops created by this class. Default value: 'Sum'.

Details
Formally, the additive model represents a random process g[t] = f1[t] + f2[t] + ... + fN[t] + eps[t], where the f's are the random processes represented by the components, and eps[t] ~ Normal(loc=0, scale=observation_noise_scale) is an observation noise term. See the AdditiveStateSpaceModel documentation for mathematical details.

This model inherits the parameters (with priors) of its components, and adds an observation_noise_scale parameter governing the level of noise in the observed time series.

Value
an instance of StructuralTimeSeries.

See Also
For usage examples see sts_fit_with_hmc(), sts_forecast(), sts_decompose_by_component().

Other sts: sts_additive_state_space_model(), sts_autoregressive_state_space_model().
sts_autoregressive(), sts_constrained_seasonal_state_space_model(), sts_dynamic_linear_regression_state_space_model(),
sts_dynamic_linear_regression(), sts_linear_regression(), sts_local_level_state_space_model(),
sts_local_level(), sts_local_linear_trend_state_space_model(), sts_local_linear_trend(),
sts_seasonal_state_space_model(), sts_seasonal(), sts_semi_local_linear_trend_state_space_model(),
sts_semi_local_linear_trend(), sts_smooth_seasonal_state_space_model(), sts_smooth_seasonal(),
sts_sparse_linear_regression()

---

tfb_absolute_value

Computes $Y = g(X) = \text{Abs}(X)$, element-wise.

Description
This non-injective bijector allows for transformations of scalar distributions with the absolute value function, which maps (-inf, inf) to [0, inf).

- For $y$ in (0, inf), $\text{tfb\_absolute\_value}\$inverse$(y)$ returns the set inverse $\{x \in (-\inf, \inf) : |x| = y\}$ as a tuple, $-y, y$. $\text{tfb\_absolute\_value}\$inverse$(0)$ returns 0, 0, which is not the set inverse (the set inverse is the singleton $\{0\}$), but "works" in conjunction with TransformedDistribution to produce a left semi-continuous pdf. For $y < 0$, $\text{tfb\_absolute\_value}\$inverse$(y)$ happily returns the wrong thing, $-y$. This is done for efficiency. If validate_args == TRUE, $y < 0$ will raise an exception.
Usage

tfb_absolute_value(validate_args = FALSE, name = "absolute_value")

Arguments

validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfbAscending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outter_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_csum(), tfb_discrete_cosine_transform(), tfb_exp(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tril(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inverse(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tril(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_orthogonal(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tril(), tfb_scale_tril(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

tfb_affine Affine bijector

description

This Bijector is initialized with shift Tensor and scale arguments, giving the forward operation: \( Y = g(X) = \text{scale} \odot X + \text{shift} \) where the scale term is logically equivalent to: \( \text{scale} = \text{scale}_\text{identity_multiplier} \ast \text{tf.diag(tf.ones(d))} \)

Usage

tfb_affine(
  shift = NULL,
  scale_identity_multiplier = NULL,
  scale_diag = NULL,
scale_tril = NULL,
scale_perturb_factor = NULL,
scale_perturb_diag = NULL,
adjoint = FALSE,
validate_args = FALSE,
name = "affine",
dtype = NULL
)

Arguments

shift
Floating-point Tensor. If this is set to NULL, no shift is applied.
scale_identity_multiplier
floating point rank 0 Tensor representing a scaling done to the identity matrix. When scale_identity_multiplier = scale_diag = scale_tril = NULL then scale += IdentityMatrix. Otherwise no scaled-identity-matrix is added to scale.
scale_diag
Floating-point Tensor representing the diagonal matrix. scale_diag has shape [N1, N2, ... k], which represents a k x k diagonal matrix. When NULL no diagonal term is added to scale.
scale_tril
Floating-point Tensor representing the lower triangular matrix. scale_tril has shape [N1, N2, ... k, k], which represents a k x k lower triangular matrix. When NULL no scale_tril term is added to scale. The upper triangular elements above the diagonal are ignored.
scale_perturb_factor
Floating-point Tensor representing factor matrix with last two dimensions of shape (k, r). When NULL, no rank-r update is added to scale.
scale_perturb_diag
Floating-point Tensor representing the diagonal matrix. scale_perturb_diag has shape [N1, N2, ... r], which represents an r x r diagonal matrix. When NULL low rank updates will take the form scale_perturb_factor * scale_perturb_factor.T.
adjoint
Logical indicating whether to use the scale matrix as specified or its adjoint. Default value: FALSE.
validate_args
Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
name
name prefixed to Ops created by this class.
dtype
tf$DType to prefer when converting args to Tensors. Else, we fall back to a common dtype inferred from the args, finally falling back to float32.

Details

If NULL of scale_identity_multiplier, scale_diag, or scale_tril are specified then scale += IdentityMatrix. Otherwise specifying a scale argument has the semantics of scale += Expand(arg), i.e., scale_diag != NULL means scale += tf$diag(scale_diag).

Value

a bijector instance.
See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors:
- `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`,
- `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`,
- `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`,
- `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`,
- `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`,
- `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`,
- `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`,
- `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`,
- `tfb_orderd()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`,
- `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`,
- `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`,
- `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`,
- `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`,
- `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`,
- `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

---

**tfb_affine_linear_operator**

**Computes** $Y = g(X; \text{shift}, \text{scale}) = \text{scale} @ X + \text{shift}$

**Description**

`shift` is a numeric Tensor and `scale` is a LinearOperator. If `X` is a scalar then the forward transformation is: $\text{scale} * X + \text{shift}$ where $*$ denotes broadcasted elementwise product.

**Usage**

```python
tfb_affine_linear_operator(
    shift = NULL,
    scale = NULL,
    adjoint = FALSE,
    validate_args = FALSE,
    name = "affine_linear_operator"
)
```

**Arguments**

- **shift**: Floating-point Tensor.
- **scale**: Subclass of LinearOperator. Represents the (batch) positive definite matrix $M$ in $\mathbb{R}^{k \times k}$.
- **adjoint**: Logical indicating whether to use the scale matrix as specified or its adjoint. Default value: `FALSE`.
- **validate_args**: Logical, default `FALSE`. Whether to validate input with asserts. If `validate_args` is `FALSE`, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.
tfb_ascending

Maps unconstrained R^n to R^n in ascending order.

Description

Both the domain and the codomain of the mapping is [-inf, inf]^n, however, the input of the inverse mapping must be strictly increasing. On the last dimension of the tensor, the Ascending bijector performs: 

\[ y = \text{tfcumsum}([x[0], \text{tfexp}(x[1]), \text{tfexp}(x[2]), ..., \text{tfexp}(x[-1])]) \]

Usage

```r
tfb_ascending(validate_args = FALSE, name = "ascending")
```

Arguments

- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

Value

a bijector instance.
tfb_batch_normalization

Computes $Y = g(X)$ s.t. $X = g^{-1}(Y) = (Y - \text{mean}(Y)) / \text{std}(Y)$

Description

Applies Batch Normalization (Ioffe and Szegedy, 2015) to samples from a data distribution. This can be used to stabilize training of normalizing flows (Papamakarios et al., 2016; Dinh et al., 2017)

Usage

```r
tfb_batch_normalization(
    batchnorm_layer = NULL,
    training = TRUE,
    validate_args = FALSE,
    name = "batch_normalization"
)
```

Arguments

- **batchnorm_layer**: tf$layers$BatchNormalization layer object. If NULL, defaults to tf$layers$BatchNormalization(\text{gamma_constraint}=tf$nn$relu(x) + 1e-6). This ensures positivity of the scale variable.
- **training**: If TRUE, updates running-average statistics during call to inverse().
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(),
tfb_affine(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(),
tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform,
tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(),
tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(),
tfb_inverse(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(),
tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(),
tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(),
tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(),
tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(),
tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(),
tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(),
tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
When training Deep Neural Networks (DNNs), it is common practice to normalize or whiten features by shifting them to have zero mean and scaling them to have unit variance.

The `inverse()` method of the BatchNormalization bijector, which is used in the log-likelihood computation of data samples, implements the normalization procedure (shift-and-scale) using the mean and standard deviation of the current minibatch.

Conversely, the `forward()` method of the bijector de-normalizes samples (e.g. $X \ast \text{std}(Y) + \text{mean}(Y)$) with the running-average mean and standard deviation computed at training-time. De-normalization is useful for sampling.

During training time, BatchNormalization.inverse and BatchNormalization.forward are not guaranteed to be inverses of each other because `inverse(y)` uses statistics of the current minibatch, while `forward(x)` uses running-average statistics accumulated from training. In other words, `tfb_batch_normalization().inverse(tfb_batch_normalization().forward(...))` and `tfb_batch_normalization().forward(tfb_batch_normalization().inverse(...))` will be identical when training=FALSE but may be different when training=TRUE.

Value

A bijector instance.

References


See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
**tfb_blockwise**

*Bijector which applies a list of bijectors to blocks of a Tensor*

**Description**

More specifically, given \([F_0, F_1, \ldots, F_n]\) which are scalar or vector bijectors this bijector creates a transformation which operates on the vector \([x_0, \ldots, x_n]\) with the transformation \([F_0(x_0), F_1(x_1), \ldots, F_n(x_n)]\) where \(x_0, \ldots, x_n\) are blocks (partitions) of the vector.

**Usage**

```r
tfb_blockwise(
  bijectors,
  block_sizes = NULL,
  validate_args = FALSE,
  name = NULL
)
```

**Arguments**

- **bijectors**: A non-empty list of bijectors.
- **block_sizes**: A 1-D integer Tensor with each element signifying the length of the block of the input vector to pass to the corresponding bijector. The length of block_sizes must be equal to the length of bijectors. If left as NULL, a vector of 1’s is used.
- **validate_args**: Logical indicating whether arguments should be checked for correctness.
- **name**: String, name given to ops managed by this object. Default: E.g., `tfb_blockwise(list(tfb_exp(), tfb_softplus()))$name` == "blockwise_of_exp_and_softplus".

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`,
**tfb_chain**

A Bijector which applies a sequence of bijectors

### Description

Bijector which applies a sequence of bijectors

### Usage

```r
tfb_chain(
  bijectors = NULL,
  validate_args = FALSE,
  validate_event_size = TRUE,
  parameters = NULL,
  name = NULL
)
```

### Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>bijectors</td>
<td>list of bijector instances. An empty list makes this bijector equivalent to the Identity bijector.</td>
</tr>
<tr>
<td>validate_args</td>
<td>Logical indicating whether arguments should be checked for correctness.</td>
</tr>
<tr>
<td>validate_event_size</td>
<td>Checks that bijectors are not applied to inputs with incomplete support (that is, inputs where one or more elements are a deterministic transformation of the others). For example, the following LDJ would be incorrect: ( \text{tfb_chain(list(\text{tfb_scale()}, \text{tfb_softmax_centered}())} ) The jacobian contribution from <code>tfb_scale()</code> applies to a 2-dimensional input, but the output from <code>tfb_softmax_centered()</code> is a 1-dimensional input embedded in a 2-dimensional space. Setting <code>validate_event_size=TRUE</code> (default) prints warnings in these cases. When <code>validate_args</code> is also <code>TRUE</code>, the warning is promoted to an exception.</td>
</tr>
<tr>
<td>parameters</td>
<td>Locals dict captured by subclass constructor, to be used for copy/slice re-instantiation operators.</td>
</tr>
<tr>
<td>name</td>
<td>String, name given to ops managed by this object. Default: E.g., <code>tfb\_chain(list(\text{tfb\_exp()}, \text{tfb\_softplus}()))</code> == &quot;chain_of_exp_of_softplus&quot;.</td>
</tr>
</tbody>
</table>

### Value

A bijector instance.
See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(),
tfb_affine(), tfbAscending(), tfb_batch_normalization(), tfb_blockwise(), tfb_cholesky_outer_product(),
tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform,
tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(),
tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inverse(),
tfb_ironv(), tfb_ironv_log_det(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(),
tfb_intron_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(),
tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(),
tfb_ironed(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(),
tfb_relay_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(),
tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(),
tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_shift(), tfb_sigmoid(), tfb_sinh_arccosh(), tfb_sinh(), tfb_softmax_centered(),
tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(),
tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

---

tfb_cholesky_outer_product

Computes \( g(X) = X @ X^T \) where \( X \) is lower-triangular, positive-diagonal matrix

Description

Note: the upper-triangular part of \( X \) is ignored (whether or not its zero).

Usage

```python
tfb_cholesky_outer_product(
    validate_args = FALSE,
    name = "cholesky_outer_product"
)
```

Arguments

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

Details

The surjectivity of \( g \) as a map from the set of \( n \times n \) positive-diagonal lower-triangular matrices to the set of SPD matrices follows immediately from executing the Cholesky factorization algorithm on an SPD matrix \( A \) to produce a positive-diagonal lower-triangular matrix \( L \) such that \( A = L @ L^T \).
To prove the injectivity of $g$, suppose that $L_1$ and $L_2$ are lower-triangular with positive diagonals and satisfy $A = L_1 \cdot L_1^T = L_2 \cdot L_2^T$. Then $\text{inv}(L_1) \cdot A \cdot \text{inv}(L_1)^T = [\text{inv}(L_1) \cdot L_2] \cdot [\text{inv}(L_1) \cdot L_2]^T = I$. Setting $L_3 := \text{inv}(L_1) \cdot L_2$, that $L_3$ is a positive-diagonal lower-triangular matrix follows from $\text{inv}(L_1)$ being positive-diagonal lower-triangular (which follows from the diagonal of a triangular matrix being its spectrum), and that the product of two positive-diagonal lower-triangular matrices is another positive-diagonal lower-triangular matrix. A simple inductive argument (proceeding one column of $L_3$ at a time) shows that, if $I = L_3 \cdot L_3^T$, with $L_3$ being lower-triangular with positive-diagonal, then $L_3 = I$. Thus, $L_1 = L_2$, proving injectivity of $g$.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_expm1()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordinal()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfbTranspose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

---

**tfb_cholesky_to_inv_cholesky**

*Maps the Cholesky factor of $M$ to the Cholesky factor of $M^{-1}$*

---

**Description**

The forward and inverse calculations are conceptually identical to: 

```r
forward <- function(x) tf$cholesky(tf$linalg$inv(tf$matmul(x, x, adjoint_b = TRUE)))
inverse = forward
```

However, the actual calculations exploit the triangular structure of the matrices.

**Usage**

```r
tfb_cholesky_to_inv_cholesky(
  validate_args = FALSE,
  name = "cholesky_to_inv_cholesky"
)
```
**tfb_correlation_cholesky**

**Map unconstrained reals to Cholesky-space correlation matrices.**

**Arguments**

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inverse()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamyCDF()`, `tfb_lambertw_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_diag()`, `tfb_matvec_linear_operator()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_sinhaw()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

**Description**

This bijector is a mapping between $\mathbb{R}^n$ and the n-dimensional manifold of Cholesky-space correlation matrices embedded in $\mathbb{R}^{m^2}$, where $n$ is the $(m - 1)^{th}$ triangular number; i.e. $n = 1 + 2 + \ldots + (m - 1)$.

**Usage**

```
tfb_correlation_cholesky(validate_args = FALSE, name = "correlation_cholesky")
```

**Arguments**

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.
Details

Mathematical Details

The image of unconstrained reals under the CorrelationCholesky bijector is the set of correlation matrices which are positive definite. A correlation matrix can be characterized as a symmetric positive semidefinite matrix with 1s on the main diagonal. However, the correlation matrix is positive definite if no component can be expressed as a linear combination of the other components. For a lower triangular matrix $L$ to be a valid Cholesky-factor of a positive definite correlation matrix, it is necessary and sufficient that each row of $L$ have unit Euclidean norm. To see this, observe that if $L_{i}$ is the ith row of the Cholesky factor corresponding to the correlation matrix $R$, then the ith diagonal entry of $R$ satisfies:

$$1 = R_{i,i} = L_{i} \cdot L_{i} = ||L_{i}||^2$$

where $\cdot$ is the dot product of vectors and $\| \cdot \|$ denotes the Euclidean norm. Furthermore, observe that $R_{i,j}$ lies in the interval $[-1, 1]$. By the Cauchy-Schwarz inequality:

$$|R_{i,j}| = |L_{i} \cdot L_{j}| \leq ||L_{i}|| \cdot ||L_{j}|| = 1$$

This is a consequence of the fact that $R$ is symmetric positive definite with 1s on the main diagonal. The LKJ distribution with input_output_cholesky=TRUE generates samples from (and computes log-densities on) the set of Cholesky factors of positive definite correlation matrices. The CorrelationCholesky bijector provides a bijective mapping from unconstrained reals to the support of the LKJ distribution.

Value

a bijector instance.

References


See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfbAscending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_scatter().
tfb_cumsum() Computes the cumulative sum of a tensor along a specified axis.

Description
Computes the cumulative sum of a tensor along a specified axis.

Usage
```
tfb_cumsum(axis = -1, validate_args = FALSE, name = "cumsum")
```

Arguments
- **axis** int indicating the axis along which to compute the cumulative sum. Note that positive (and zero) values are not supported.
- **validate_args** Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name** name prefixed to Ops created by this class.

Value
- a bijector instance.

See Also
For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_discrete_cosine_transform(), tfb_expr(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_discrete_cosine_transform

Computes \( Y = g(X) = \text{DCT}(X) \), where DCT type is indicated by the type arg.

Description

The discrete cosine transform efficiently applies a unitary DCT operator. This can be useful for mixing and decorrelating across the innermost event dimension. The inverse \( X = g^{-1}(Y) = \text{IDCT}(Y) \), where IDCT is DCT-III for type==2. This bijector can be interleaved with Affine bijectors to build a cascade of structured efficient linear layers as in Moczulski et al., 2016. Note that the operator applied is orthonormal (i.e. norm='ortho').

Usage

```r
tfb_discrete_cosine_transform(
  validate_args = FALSE,
  dct_type = 2,
  name = "dct"
)
```

Arguments

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `dct_type` integer, the DCT type performed by the forward transformation. Currently, only 2 and 3 are supported.
- `name` name prefixed to Ops created by this class.

Value

a bijector instance.

References


See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`. Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfbAscending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_chol_sky_outer_product()`, `tfb_chol_sky_to_inv_chol_sky()`, `tfb_correlation_chol_sky()`, `tfb_cumsum()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`. 
tfb_exp Computes \( Y = \exp(X) \)

### Description
Computes \( Y = \exp(X) \)

### Usage
```r
tfb_exp(validate_args = FALSE, name = "exp")
```

### Arguments
- **validate_args** Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name** name prefixed to Ops created by this class.

### Value
a bijector instance.

### See Also
For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diagonal()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
tfb_expm1

Computes $Y = g(X) = \exp(X) - 1$

Description
This Bijector is no different from tfb_chain(list(tfb_affine_scalar(shift=-1),tfb_exp())). However, this makes use of the more numerically stable routines tf$\mathbf{math}$expm1 and tf$\mathbf{log1p}$.

Usage

tfb_expm1(validate_args = FALSE, name = "expm1")

Arguments

validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name name prefixed to Ops created by this class.

Details
Note: the expm1(.) is applied element-wise but the Jacobian is a reduction over the event space.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inform(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_shift(), tfb_softmax(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_ffjord

Implements a continuous normalizing flow $X \rightarrow Y$ defined via an ODE.

Description

This bijector implements a continuous dynamics transformation parameterized by a differential equation, where initial and terminal conditions correspond to domain ($X$) and image ($Y$) i.e.

Usage

```python
tfb_ffjord(
    state_time_derivative_fn,
    ode_solve_fn = NULL,
    trace_augmentation_fn = tfp$bijectors$ffjord$trace_jacobian_hutchinson,
    initial_time = 0,
    final_time = 1,
    validate_args = FALSE,
    dtype = tf$float32,
    name = "ffjord"
)
```

Arguments

- **state_time_derivative_fn**: function taking arguments `time` (a scalar representing time) and `state` (a Tensor representing the state at given time) returning the time derivative of the state at given time.
- **ode_solve_fn**: function taking arguments `ode_fn` (same as `state_time_derivative_fn` above), `initial_time` (a scalar representing the initial time of integration), `initial_state` (a Tensor of floating dtype represents the initial state) and `solution_times` (1D Tensor of floating dtype representing time at which to obtain the solution) returning a Tensor of shape `[time_axis, initial_state$shape]`. Will take `final_time` as the `solution_times` argument and `state_time_derivative_fn` as `ode_fn` argument. If NULL a DormandPrince solver from `tfp$math$ode` is used. Default value: NULL
- **trace_augmentation_fn**: function taking arguments `ode_fn` (function same as `state_time_derivative_fn` above), `state_shape` (TensorShape of a the state), `dtype` (same as dtype of the state) and returning a function taking arguments `time` (a scalar representing the time at which the function is evaluated), `state` (a Tensor representing the state at given time) that computes a tuple (`ode_fn(time, state), jacobian_trace_estimation`). `jacobian_trace_estimation` should represent trace of the jacobian of `ode_fn` with respect to `state`. `state_time_derivative_fn` will be passed as `ode_fn` argument. Default value: `tfp$bijectors$ffjord$trace_jacobian_hutchinson`
- **initial_time**: Scalar float representing time to which the $x$ value of the bijector corresponds to. Passed as `initial_time` to `ode_solve_fn`. For default solver can be float or floating scalar Tensor. Default value: 0.
final_time  Scalar float representing time to which the $y$ value of the bijector corresponds to. Passed as solution_times to ode_solve_fn. For default solver can be float or floating scalar Tensor. Default value: 1.

validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

dtype  tf$DType$ to prefer when converting args to Tensors. Else, we fall back to a common dtype inferred from the args, finally falling back to float32.

name  name prefixed to Ops created by this class.

Details

d/dt[state(t)] = state_time_derivative_fn(t, state(t))
state(initial_time) = X
state(final_time) = Y

For this transformation the value of log_det_jacobian follows another differential equation, reducing it to computation of the trace of the jacobian along the trajectory

state_time_derivative = state_time_derivative_fn(t, state(t))
d/dt[log_det_jac(t)] = Tr(jacobian(state_time_derivative, state(t)))

FFJORD constructor takes two functions ode_solve_fn and trace_augmentation_fn arguments that customize integration of the differential equation and trace estimation.

Differential equation integration is performed by a call to ode_solve_fn.

Custom ode_solve_fn must accept the following arguments:

- ode_fn(time, state): Differential equation to be solved.
- initial_time: Scalar float or floating Tensor representing the initial time.
- initial_state: Floating Tensor representing the initial state.
- solution_times: 1D floating Tensor of solution times.

And return a Tensor of shape [solution_times$shape, initial_state$shape] representing state values evaluated at solution_times. In addition ode_solve_fn must support nested structures. For more details see the interface of tfp$math$ode$Solver$solve().

Trace estimation is computed simultaneously with state_time_derivative using augmented_state_time_derivative_fn that is generated by trace_augmentation_fn. trace_augmentation_fn takes state_time_derivative_fn, state.shape and state.dtype arguments and returns a augmented_state_time_derivative_fn callable that computes both state_time_derivative and unreduced trace_estimation.

Custom ode_solve_fn and trace_augmentation_fn examples:

# custom_solver_fn: `function(f, t_initial, t_solutions, y_initial, ...)`
# ... : Additional arguments to pass to custom_solver_fn.
ode_solve_fn <- function(ode_fn, initial_time, initial_state, solution_times) {
  custom_solver_fn(ode_fn, initial_time, solution_times, initial_state, ...)
}
ffjord <- tfb_ffjord(state_time_derivative_fn, ode_solve_fn = ode_solve_fn)
# state_time_derivative_fn: `function(time, state)`
# trace_jac_fn: `function(time, state)` uncomputed jacobian trace function
trace_augmentation_fn <- function(ode_fn, state_shape, state_dtype) {
  augmented_ode_fn <- function(time, state) {
    list(ode_fn(time, state), trace_jac_fn(time, state))
  }
  augmented_ode_fn
}

ffjord <- tfb_ffjord(state_time_derivative_fn, trace_augmentation_fn = trace_augmentation_fn)

For more details on FFJORD and continuous normalizing flows see Chen et al. (2018), Grathwohl et al. (2018).

Value

a bijector instance.

References


See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_exp()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_orthogonal_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`. 
**tfb_fill_scale_tri_l**  
Transforms unconstrained vectors to TriL matrices with positive diagonal

**Description**

This is implemented as a simple tfb_chain of tfb_fill_triangular followed by tfb_transform_diagonal, and provided mostly as a convenience. The default setup is somewhat opinionated, using a Softplus transformation followed by a small shift (1e-5) which attempts to avoid numerical issues from zeros on the diagonal.

**Usage**

```python
tfb_fill_scale_tri_l(
    diag_bijector = NULL,
    diag_shift = 1e-05,
    validate_args = FALSE,
    name = "fill_scale_tril"
)
```

**Arguments**

- **diag_bijector**: Bijector instance, used to transform the output diagonal to be positive. Default value: NULL (i.e., tfb_softplus()).
- **diag_shift**: Float value broadcastable and added to all diagonal entries after applying the diag_bijector. Setting a positive value forces the output diagonal entries to be positive, but prevents inverting the transformation for matrices with diagonal entries less than this value. Default value: 1e-5.
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian(). Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(),
tfb_fill_triangular

Transforms vectors to triangular

Description

Triangular matrix elements are filled in a clockwise spiral. Given input with shape batch_shape + [d], produces output with shape batch_shape + [n, n], where n = (-1 + sqrt(1 + 8 * d))/2. This follows by solving the quadratic equation d = 1 + 2 + ... + n = n * (n + 1)/2.

Usage

tfb_fill_triangular(
    upper = FALSE,
    validate_args = FALSE,
    name = "fill_triangular"
)

Arguments

upper Logical representing whether output matrix should be upper triangular (TRUE) or lower triangular (FALSE, default).

validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale_matvec_diagonal(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_forward

Returns the forward Bijector evaluation, i.e., $X = g(Y)$.

Description

Returns the forward Bijector evaluation, i.e., $X = g(Y)$.

Usage

tfb_forward(bijector, x, name = "forward")

Arguments

- bijector: The bijector to apply
- x: Tensor. The input to the "forward" evaluation.
- name: name of the operation

Value

a tensor

See Also

Other bijector_methods: tfb_forward_log_det_jacobian(), tfb_inverse_log_det_jacobian(), tfb_inverse()

Examples

b <- tfb_affine_scalar(shift = 1, scale = 2)
x <- 10
b %>% tfb_forward(x)
tbf_forward_log_det_jacobian

Returns the result of the forward evaluation of the log determinant of the Jacobian

Description

Returns the result of the forward evaluation of the log determinant of the Jacobian

Usage

\[
tfb_forward_log_det_jacobian(
    bijector,
    x,
    event_ndims,
    name = "forward_log_det_jacobian"
)
\]

Arguments

- `bijector`: The bijector to apply
- `x`: Tensor. The input to the "forward" Jacobian determinant evaluation.
- `event_ndims`: Number of dimensions in the probabilistic events being transformed. Must be greater than or equal to \(\text{bijector}^{-1}\text{forward_min_event_ndims}\). The result is summed over the final dimensions to produce a scalar Jacobian determinant for each event, i.e. it has shape \(x\text{shape} - \text{event_ndims}\) dimensions.
- `name`: name of the operation

Value

A tensor

See Also

Other bijector methods: `tfb_forward()`, `tfb_inverse_log_det_jacobian()`, `tfb_inverse()`

Examples

\[
b <- \text{tfb\_affine\_scalar(shift = 1, scale = 2)}
x <- 10
b \%\% tbf\_forward\_log\_det\_jacobian(x, \text{event_ndims} = 0)
\]
tfb_glow

Implements the Glow Bijector from Kingma & Dhariwal (2018).

Description

Overview: Glow is a chain of bijectors which transforms a rank-1 tensor (vector) into a rank-3 tensor (e.g. an RGB image). Glow does this by chaining together an alternating series of "Blocks," "Squeezes," and "Exits" which are each themselves special chains of other bijectors. The intended use of Glow is as part of a tfd_transformed_distribution, in which the base distribution over the vector space is used to generate samples in the image space. In the paper, an Independent Normal distribution is used as the base distribution.

Usage

```r
tfb_glow(
  output_shape = c(32, 32, 3),
  num_glow_blocks = 3,
  num_steps_per_block = 32,
  coupling_bijector_fn = NULL,
  exit_bijector_fn = NULL,
  grab_after_block = NULL,
  use_actnorm = TRUE,
  seed = NULL,
  validate_args = FALSE,
  name = "glow"
)
```

Arguments

- **output_shape**: A list of integers, specifying the event shape of the output, of the bijectors forward pass (the image). Specified as [H, W, C]. Default Value: (32, 32, 3)
- **num_glow_blocks**: An integer, specifying how many downsampling levels to include in the model. This must divide equally into both H and W, otherwise the bijector would not be invertible. Default Value: 3
- **num_steps_per_block**: An integer specifying how many Affine Coupling and 1x1 convolution layers to include at each level of the spatial hierarchy. Default Value: 32 (i.e. the value used in the original glow paper).
- **coupling_bijector_fn**: A function which takes the argument input_shape and returns a callable neural network (e.g. a keras_model_sequential()). The network should either return a tensor with the same event shape as input_shape (this will employ additive coupling), a tensor with the same height and width as input_shape but twice the number of channels (this will employ affine coupling), or a bijector which takes in a tensor with event shape input_shape, and returns a tensor with shape input_shape.
exit_bijcector_fn

Similar to coupling_bijcector_fn, exit_bijcector_fn is a function which takes the argument `input_shape` and `output_chan` and returns a callable neural network. The neural network it returns should take a tensor of shape `input_shape` as the input, and return one of three options: A tensor with `output_chan` channels, a tensor with `2 * output_chan` channels, or a bijector. Additional details can be found in the documentation for ExitBijector.

grab_after_block

A tuple of floats, specifying what fraction of the remaining channels to remove following each glow block. Glow will take the integer floor of this number multiplied by the remaining number of channels. The default is half at each spatial hierarchy. Default value: None (this will take out half of the channels after each block).

use_actnorm

A boolean deciding whether or not to use actnorm. Data-dependent initialization is used to initialize this layer. Default value: FALSE

seed

A seed to control randomness in the 1x1 convolution initialization. Default value: NULL (i.e., non-reproducible sampling).

validate_args

Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name

name prefixed to Ops created by this class.

Details

A "Block" (implemented as the GlowBlock Bijector) performs much of the transformations which allow glow to produce sophisticated and complex mappings between the image space and the latent space and therefore achieve rich image generation performance. A Block is composed of `num_steps_per_block` steps, which are each implemented as a Chain containing an ActivationNormalization (ActNorm) bijector, followed by an (invertible) OneByOneConv bijector, and finally a coupling bijector. The coupling bijector is an instance of a RealNVP bijector, and uses the coupling_bijcector_fn function to instantiate the coupling bijector function which is given to the RealNVP. This function returns a bijector which defines the coupling (e.g. Shift(Scale) for affine coupling or Shift for additive coupling).

A "Squeeze" converts spatial features into channel features. It is implemented using the Expand bijector. The difference in names is due to the fact that the forward function from glow is meant to ultimately correspond to sampling from a tfp$util$TransformedDistribution object, which would use Expand (Squeeze is just Invert(Expand)). The Expand bijector takes a tensor with shape [H, W, C] and returns a tensor with shape [2H, 2W, C / 4], such that each 2x2x1 spatial tile in the output is composed from a single 1x1x4 tile in the input tensor, as depicted in the figure below.

Forward pass (Expand)
Inverse pass (Squeeze) This is implemented using a chain of \texttt{Reshape} -> \texttt{Transpose} -> \texttt{Reshape} bijectors. Note that on an inverse pass through the bijector, each Squeeze will cause the width/height of the image to decrease by a factor of 2. Therefore, the input image must be evenly divisible by 2 at least num\_glow\_blocks times, since it will pass through a Squeeze step that many times.

An "Exit" is simply a junction at which some of the tensor "exits" from the glow bijector and therefore avoids any further alteration. Each exit is implemented as a Blockwise bijector, where some channels are given to the rest of the glow model, and the rest are given to a bypass implemented using the \texttt{Identity} bijector. The fraction of channels to be removed at each exit is determined by the grab\_after\_block arg, indicates the fraction of remaining channels which join the identity bypass. The fraction is converted to an integer number of channels by multiplying by the remaining number of channels and rounding. Additionally, at each exit, glow couples the tensor exiting the highway to the tensor continuing onward. This makes small scale features in the image dependent on larger scale features, since the larger scale features dictate the mean and scale of the distribution over the smaller scale features. This coupling is done similarly to the Coupling bijector in each step of the flow (i.e. using a RealNVP bijector). However for the exit bijector, the coupling is instantiated using exit\_bijector\_fn rather than coupling bijector fn, allowing for different behaviors between standard coupling and exit coupling. Also note that because the exit utilizes a coupling bijector, there are two special cases (all channels exiting and no channels exiting). The full Glow bijector consists of num\_glow\_blocks Blocks each of which contains num\_steps\_per\_block steps. Each step implements a coupling using bijector\_coupling\_fn. Between blocks, glow converts between spatial pixels and channels using the Expand Bijector, and splits channels out of the bijector using the Exit Bijector. The channels which have exited continue onward through Identity bijectors and those which have not exited are given to the next block. After passing through all Blocks, the tensor is reshaped to a rank-1 tensor with the same number of elements. This is where the distribution will be defined. A schematic diagram of Glow is shown below. The forward function of the bijector starts from the bottom and goes upward, while the inverse function starts from the top and proceeds downward.

Value

a bijector instance.

```python
# Glow Schematic Diagram
Input Image shape = [H, W, C] \t/\t-
| Expand Bijector turns spatial / dimensions into channels. |
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tfn_gompertz_cdf

<table>
<thead>
<tr>
<th>XX</th>
<th>Step of flow</th>
<th>X</th>
<th>Exit bijector</th>
<th>V</th>
<th>Expand bijector</th>
<th>!=</th>
<th>Identity bijector</th>
<th>up</th>
<th>Inverse pass</th>
<th>dn</th>
</tr>
</thead>
</table>

| H, W, C | R: H, W, 2C |
| 2H, 2W, C / 4 | R: 2H, 2W, 2C / 4 |
| H, W, C | R: H, W, 2C |
| H * W * C | R: H * W * 2C |

References


See Also

See Also for usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expml(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tril(), tfb_fill_triangular(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tril(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

---

tfn_gompertz_cdf

Compute $Y = g(X) = 1 - \exp(-c \cdot (\exp(rate \cdot X) - 1)$, the Gompertz CDF.

Description

This bijector maps inputs from $[-\infty, \infty]$ to $[0, \infty]$. The inverse of the bijector applied to a uniform random variable $X \sim U(0, 1)$ gives back a random variable with the Gompertz distribution:

$Y \sim \text{GompertzCDF}(\text{concentration}, \text{rate})$

$\text{pdf}(y; c, r) = r \cdot c \cdot \exp(r \cdot y + c - c \cdot \exp(-c \cdot \exp(r \cdot y)))$

Note: Because the Gompertz distribution concentrates its mass close to zero, for larger rates or larger concentrations, bijector.forward will quickly saturate to 1.
tfb_gompertz_cdf

Usage

tfb_gompertz_cdf(
    concentration,
    rate,
    validate_args = FALSE,
    name = "gompertz_cdf"
)

Arguments

concentration Positive Float-like Tensor that is the same dtype and is broadcastable with concentration. This is $c$ in $Y = g(X) = 1 - \exp(-c \cdot (\exp(rate \cdot X) - 1)$.
rate Positive Float-like Tensor that is the same dtype and is broadcastable with concentration. This is rate in $Y = g(X) = 1 - \exp(-c \cdot (\exp(rate \cdot X) - 1)$.
validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
name name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascend(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_csum(), tfb_discrete_cosine_transform(), tfb_exp(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_gluon(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_ru(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb-rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_ru(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sin(), tfb_softmax_centered(), tfb_sinhplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_gumbel Computes $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$

**Description**

This bijector maps inputs from $[-\infty, \infty]$ to $[0, 1]$. The inverse of the bijector applied to a uniform random variable $X \sim U(0, 1)$ gives back a random variable with the Gumbel distribution:

**Usage**

```r
tfb_gumbel(loc = 0, scale = 1, validate_args = FALSE, name = "gumbel")
```

**Arguments**

- `loc`: Float-like Tensor that is the same dtype and is broadcastable with `scale`. This is $\text{loc}$ in $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$.
- `scale`: Positive Float-like Tensor that is the same dtype and is broadcastable with `loc`. This is scale in $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$.
- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

**Details**

$Y \sim \text{Gumbel}(\text{loc}, \text{scale})$

\[
\text{pdf}(y; \text{loc}, \text{scale}) = \frac{\exp(-((y - \text{loc}) / \text{scale} + \exp(-(y - \text{loc}) / \text{scale}))}{\text{scale}}
\]

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diagonal()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`,
tfb_gumbel_cdf

Compute $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$, the Gumbel CDF.

**Description**

This bijector maps inputs from $[-\infty, \infty]$ to $[0, 1]$. The inverse of the bijector applied to a uniform random variable $X \sim U(0, 1)$ gives back a random variable with the Gumbel distribution:

**Usage**

```r
tfb_gumbel_cdf(loc = 0, scale = 1, validate_args = FALSE, name = "gumbel_cdf")
```

**Arguments**

- `loc`: Float-like Tensor that is the same dtype and is broadcastable with `scale`. This is $\text{loc}$ in $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$.
- `scale`: Positive Float-like Tensor that is the same dtype and is broadcastable with `loc`. This is $\text{scale}$ in $Y = g(X) = \exp(-\exp(-(X - \text{loc}) / \text{scale}))$.
- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

**Details**

$Y \sim \text{GumbelCDF}(\text{loc}, \text{scale})$

$$\text{pdf}(y; \text{loc}, \text{scale}) = \exp(-\frac{(y - \text{loc})}{\text{scale}} + \exp(-\frac{(y - \text{loc})}{\text{scale}})) / \text{scale}$$

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`. 
### tfb_identity

Computes $Y = g(X) = X$

**Description**

Computes $Y = g(X) = X$

**Usage**

```r
tfb_identity(validate_args = FALSE, name = "identity")
```

**Arguments**

- **validate_args**  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**  name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`. Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_acceptance()`, `tfb_block_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_gumbel()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_mixed_lognormal()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diagonal()`, `tfb_scale_matvec_linear_operator()`, `tfb_shifted_gompertz_cdf()`, `tfb_shifted_gompertz_cdf()`, `tfb_shifted_gompertz_cdf()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
Bijector constructed from custom functions

**Description**

Bijector constructed from custom functions

**Usage**

```r
tfb_inline(
    forward_fn = NULL,
    inverse_fn = NULL,
    inverse_log_det_jacobian_fn = NULL,
    forward_log_det_jacobian_fn = NULL,
    forward_event_shape_fn = NULL,
    forward_event_shape_tensor_fn = NULL,
    inverse_event_shape_fn = NULL,
    inverse_event_shape_tensor_fn = NULL,
    is_constant_jacobian = NULL,
    validate_args = FALSE,
    forward_min_event_ndims = NULL,
    inverse_min_event_ndims = NULL,
    name = "inline"
)
```

**Arguments**

- `forward_fn`: Function implementing the forward transformation.
- `inverse_fn`: Function implementing the inverse transformation.
- `inverse_log_det_jacobian_fn`: Function implementing the log_det_jacobian of the forward transformation.
- `forward_log_det_jacobian_fn`: Function implementing the log_det_jacobian of the inverse transformation.
- `forward_event_shape_fn`: Function implementing non-identical static event shape changes. Default: shape is assumed unchanged.
- `forward_event_shape_tensor_fn`: Function implementing non-identical event shape changes. Default: shape is assumed unchanged.
- `inverse_event_shape_fn`: Function implementing non-identical static event shape changes. Default: shape is assumed unchanged.
- `inverse_event_shape_tensor_fn`: Function implementing non-identical event shape changes. Default: shape is assumed unchanged.
**tfb_inverse**  

Returns the inverse Bijector evaluation, i.e., $X = g^{-1}(Y)$.

**Description**  

Returns the inverse Bijector evaluation, i.e., $X = g^{-1}(Y)$.

**Usage**  

tfb_inverse(bijector, y, name = "inverse")
tfb_inverse_log_det_jacobian

**Arguments**

- **bijector**: The bijector to apply
- **y**: Tensor. The input to the "inverse" evaluation.
- **name**: name of the operation

**Value**

a tensor

**See Also**

Other bijector methods: `tfb_forward_log_det_jacobian()`, `tfb_forward()`, `tfb_inverse_log_det_jacobian()`

**Examples**

```r
b <- tfb_affine_scalar(shift = 1, scale = 2)
x <- 10
y <- b %>% tfb_forward(x)
b %>% tfb_inverse(y)
```

---

**tfb_inverse_log_det_jacobian**

*Returns the result of the inverse evaluation of the log determinant of the Jacobian*

**Description**

Returns the result of the inverse evaluation of the log determinant of the Jacobian

**Usage**

```r
tfb_inverse_log_det_jacobian(
  bijector,
  y,
  event_ndims,
  name = "inverse_log_det_jacobian"
)
```

**Arguments**

- **bijector**: The bijector to apply
- **y**: Tensor. The input to the "inverse" Jacobian determinant evaluation.
- **event_ndims**: Number of dimensions in the probabilistic events being transformed. Must be greater than or equal to bijector$inverse_min_event_ndims. The result is summed over the final dimensions to produce a scalar Jacobian determinant for each event, i.e. it has shape x$shape$ndims - event_ndims dimensions.
- **name**: name of the operation
tfb_invert

Value

a tensor

See Also

Other bijector_methods: tfb_forward_log_det_jacobian(), tfb_forward(), tfb_inverse()

Examples

```r
b <- tfb_affine_scalar(shift = 1, scale = 2)
x <- 10
y <- b %>% tfb_forward(x)
b %>% tfb_inverse_log_det_jacobian(y, event_ndims = 0)
```

---

**tfb_invert**  
*Bijector which inverts another Bijector*

Description

Creates a Bijector which swaps the meaning of inverse and forward. Note: An inverted bijector’s inverse_log_det_jacobian is often more efficient if the base bijector implements _forward_log_det_jacobian_. If _forward_log_det_jacobian_ is not implemented then the following code is used: $y = b^{-1}(x)$  
$-b^{-1}\text{log\_det\_jacobian}(y)$

Usage

```r
tfb_invert(bijector, validate_args = FALSE, name = NULL)
```

Arguments

- **bijector**  
  Bijector instance.
- **validate_args**  
  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**  
  name prefixed to Ops created by this class.

Value

a bijector instance.
**tfb_iterated_sigmoid_centered**

**Bijector which applies a Stick Breaking procedure.**

**Description**

Bijector which applies a Stick Breaking procedure.

**Usage**

```r
tfb_iterated_sigmoid_centered(validate_args = FALSE, name = "iterated_sigmoid")
```

**Arguments**

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_sofplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
tfb_kumaraswamy

Computes \( Y = g(X) = (1 - (1 - X)^{(1 / b)})^{(1 / a)} \), with \( X \) in \([0, 1]\).

**Description**

This bijector maps inputs from \([0, 1]\) to \([0, 1]\). The inverse of the bijector applied to a uniform random variable \( X \sim U(0, 1) \) gives back a random variable with the Kumaraswamy distribution: \( Y \sim \text{Kumaraswamy}(a, b) \)

\[
\text{pdf}(y; a, b, 0 \leq y \leq 1) = a \times b \times y^{(a - 1)} \times (1 - y^a)^{(b - 1)}
\]

**Usage**

```python
tfb_kumaraswamy(
    concentration1 = NULL,
    concentration0 = NULL,
    validate_args = FALSE,
    name = "kumaraswamy"
)
```

**Arguments**

- `concentration1` float scalar indicating the transform power, i.e., \( Y = g(X) = (1 - (1 - X)^{(1 / b)})^{(1 / a)} \) where \( a \) is concentration1.
- `concentration0` float scalar indicating the transform power, i.e., \( Y = g(X) = (1 - (1 - X)^{(1 / b)})^{(1 / a)} \) where \( b \) is concentration0.
- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

**Value**

- a bijector instance.
tfb_kumaraswamy_cdf

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(),
tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(),
tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(),
tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(),
tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(),
tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(),
tfb_kumaraswamy_cdf(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(),
tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(),
tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(),
tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(),
tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(),
tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(),
tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(),
tfbTranspose(), tfb_weibull_cdf(), tfb_weibull()

---

tfb_kumaraswamy_cdf  Computes Y = g(X) = (1 − (1 − X)**(1 / b))**((1 / a)), with X in [0, 1]

Description

This bijector maps inputs from [0, 1] to [0, 1]. The inverse of the bijector applied to a uniform random variable X ~ U(0, 1) gives back a random variable with the Kumaraswamy distribution: Y ~ Kumaraswamy(a, b) pdf(y; a, b, 0 <= y <= 1) = a * b * y ** (a - 1) * (1 - y**a) ** (b - 1)

Usage

```python
tfb_kumaraswamy_cdf(
    concentration1 = 1,
    concentration0 = 1,
    validate_args = FALSE,
    name = "kumaraswamy_cdf"
)
```

Arguments

- **concentration1**: float scalar indicating the transform power, i.e., Y = g(X) = (1 - (1 - X)**(1/b))**(1/a) where a is concentration1.
- **concentration0**: float scalar indicating the transform power, i.e., Y = g(X) = (1 - (1 - X)**(1/b))**(1/a) where b is concentration0.
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.
Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfbAscending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

tfb_lambert_w_tail  LambertWTail transformation for heavy-tail Lambert W x F random variables.

Description

A random variable Y has a Lambert W x F distribution if W(τ)(Y) = X has distribution F, where τ = (shift, scale, tail) parameterizes the inverse transformation.

Usage

tfb_lambert_w_tail(
  shift = NULL,
  scale = NULL,
  tailweight = NULL,
  validate_args = FALSE,
  name = "lambertw_tail"
)

Arguments

shift  Floating point tensor; the shift for centering (uncentering) the input (output) random variable(s).

scale  Floating point tensor; the scaling (unscaling) of the input (output) random variable(s). Must contain only positive values.
tfb_masked_autoregressive_default_template

**tailweight**
Floating point tensor; the tail behaviors of the output random variable(s). Must contain only non-negative values.

**validate_args**
Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

**name**
name prefixed to Ops created by this class.

**Details**
This bijector defines the transformation underlying Lambert W x F distributions that transform an input random variable to an output random variable with heavier tails. It is defined as $Y = (U \times \exp(0.5 \times \text{tail} \times U^2)) \times \text{scale} + \text{shift}$, where $U = (X - \text{shift}) / \text{scale}$ is a shifted/scaled input random variable, and tail $\geq 0$ is the tail parameter.

Attributes:
- shift: shift to center (uncenter) the input data.
- scale: scale to normalize (de-normalize) the input data.
- tailweight: Tail parameter delta of heavy-tail transformation; must be $\geq 0$.

**Value**
a bijector instance.

**See Also**
For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors:
- `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_exp1()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_pdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_independent()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

**Description**
This will be wrapped in a make_template to ensure the variables are only created once. It takes the input and returns the loc ("mu" in Germain et al. (2015)) and log_scale ("alpha" in Germain et al. (2015)) from the MADE network.
Usage

tfb_masked_autoregressive_default_template(
    hidden_layers,
    shift_only = FALSE,
    activation = tf$nn$relu,
    log_scale_min_clip = -5,
    log_scale_max_clip = 3,
    log_scale_clip_gradient = FALSE,
    name = NULL,
...
)

Arguments

  hidden_layers  list-like of non-negative integer, scalars indicating the number of units in each
                hidden layer. Default: list(512,512).
  shift_only     logical indicating if only the shift term shall be computed. Default: FALSE.
  activation     Activation function (callable). Explicitly setting to NULL implies a linear acti-
                vation.
  log_scale_min_clip  float-like scalar Tensor, or a Tensor with the same shape as log_scale. The mini-
                      mum value to clip by. Default: -5.
  log_scale_max_clip  float-like scalar Tensor, or a Tensor with the same shape as log_scale. The max-
                      imum value to clip by. Default: 3.
  log_scale_clip_gradient  logical indicating that the gradient of tf$clip\_by\_value should be preserved. De-
                          fault: FALSE.
  name           A name for ops managed by this function. Default: "tfb_masked_autoregressive_default_template".
  ...            tf$layers$dense arguments

Details

Warning: This function uses masked_dense to create randomly initialized tf$Variables. It is pre-
        sumed that these will be fit, just as you would any other neural architecture which uses tf$layers$dense.

About Hidden Layers Each element of hidden_layers should be greater than the input_depth (i.e.,
        input_depth = tf$shape(input)[[-1] where input is the input to the neural network). This is
        necessary to ensure the autoregressivity property.

About Clipping This function also optionally clips the log_scale (but possibly not its gradient).
        This is useful because if log_scale is too small/large it might underflow/overflow making it im-
        possible for the MaskedAutoregressiveFlow bijector to implement a bijection. Additionally, the
        log_scale_clip_gradient bool indicates whether the gradient should also be clipped. The default
        does not clip the gradient; this is useful because it still provides gradient information (for fit-
        ting) yet solves the numerical stability problem. I.e., log_scale_clip_gradient = FALSE means
        grad[exp(clip(x))] = grad[x] exp(clip(x)) rather than the usual grad[clip(x)] exp(clip(x)).
Value

- shift: Float-like Tensor of shift terms
- log_scale: Float-like Tensor of log(scale) terms

References


See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_inverse(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

tfb_masked_autoregressive_flow

Affine MaskedAutoregressiveFlow bijector

description

The affine autoregressive flow (Papamakarios et al., 2016) provides a relatively simple framework for user-specified (deep) architectures to learn a distribution over continuous events. Regarding terminology,

Usage

tfb_masked_autoregressive_flow(
    shift_and_log_scale_fn,
    is_constant_jacobian = FALSE,
unroll_loop = FALSE,
event_ndims = 1L,
validate_args = FALSE,
name = NULL
)

Arguments

shift_and_log_scale_fn
Function which computes shift and log_scale from both the forward domain (x) and the inverse domain (y). Calculation must respect the "autoregressive property". Suggested default: tfb_masked_autoregressive_default_template(hidden_layers=...). Typically the function contains tf$variables and is wrapped using tf$make_template. Returning NULL for either (both) shift, log_scale is equivalent to (but more efficient than) returning zero.

is_constant_jacobian
Logical, default: FALSE. When TRUE the implementation assumes log_scale does not depend on the forward domain (x) or inverse domain (y) values. (No validation is made; is_constant_jacobian=FALSE is always safe but possibly computationally inefficient.)

unroll_loop
Logical indicating whether the tf$while_loop in _forward should be replaced with a static for loop. Requires that the final dimension of x be known at graph construction time. Defaults to FALSE.

event_ndims
integer, the intrinsic dimensionality of this bijector. 1 corresponds to a simple vector autoregressive bijector as implemented by the tfb_masked_autoregressive_default_template. 2 might be useful for a 2D convolutional shift_and_log_scale_fn and so on.

validate_args
Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, the inputs are invalid, correct behavior is not guaranteed.

name
name prefixed to Ops created by this class.

Details

"Autoregressive models decompose the joint density as a product of conditionals, and model each conditional in turn. Normalizing flows transform a base density (e.g. a standard Gaussian) into the target density by an invertible transformation with tractable Jacobian." (Papamakarios et al., 2016)

In other words, the "autoregressive property" is equivalent to the decomposition, p(x) = prod{ p(x[perm[i]] | x[perm[0:i]]) : i=0, ..., d } where perm is some permutation of {0, ..., d}. In the simple case where the permutation is identity this reduces to:
p(x) = prod{ p(x[i] | x[0:i]) : i=0, ..., d }. The provided shift_and_log_scale_fn, tfb_masked_autoregressive_default_template, achieves this property by zeroing out weights in its masked_dense layers. In TensorFlow Probability, "normalizing flows" are implemented as tfp.bijectors.Bijectors. The forward "autoregression" is implemented using a tf.while_loop and a deep neural network (DNN) with masked weights such that the autoregressive property is automatically met in the inverse. A TransformedDistribution using MaskedAutoregressiveFlow(...) uses the (expensive) forward-mode calculation to draw samples and the (cheap) reverse-mode calculation to compute log-probabilities. Conversely, a TransformedDistribution using Invert(MaskedAutoregressiveFlow(...)) uses the (expensive) forward-mode calculation to compute log-probabilities and the (cheap) reverse-mode calculation to compute samples.
Given a shift_and_log_scale_fn, the forward and inverse transformations are (a sequence of) affine transformations. A "valid" shift_and_log_scale_fn must compute each shift (aka loc or "mu" in Germain et al. (2015)) and log(scale) (aka "alpha" in Germain et al. (2015)) such that each are broadcastable with the arguments to forward and inverse, i.e., such that the calculations in forward, inverse below are possible.

For convenience, tfb_masked_autoregressive_default_template is offered as a possible shift_and_log_scale_fn function. It implements the MADE architecture (Germain et al., 2015). MADE is a feed-forward network that computes a shift and log(scale) using masked_dense layers in a deep neural network. Weights are masked to ensure the autoregressive property. It is possible that this architecture is suboptimal for your task. To build alternative networks, either change the arguments to tfb_masked_autoregressive_default_template, use the masked_dense function to roll-out your own, or use some other architecture, e.g., using tf.layers. Warning: no attempt is made to validate that the shift_and_log_scale_fn enforces the "autoregressive property".

Assuming shift_and_log_scale_fn has valid shape and autoregressive semantics, the forward transformation is

```python
def forward(x):
    y = zeros_like(x)
    event_size = x.shape[-event_dims:].num_elements()
    for _ in range(event_size):
        shift, log_scale = shift_and_log_scale_fn(y)
        y = x * tf.exp(log_scale) + shift
    return y
```

and the inverse transformation is

```python
def inverse(y):
    shift, log_scale = shift_and_log_scale_fn(y)
    return (y - shift) / tf.exp(log_scale)
```

Notice that the inverse does not need a for-loop. This is because in the forward pass each calculation of shift and log_scale is based on the y calculated so far (not x). In the inverse, the y is fully known, thus is equivalent to the scaling used in forward after event_size passes, i.e., the "last" y used to compute shift, log_scale. (Roughly speaking, this also proves the transform is bijective.)

Value

a bijector instance.

References

tfb_masked_dense

Description

Analogous to tf$layers$dense.

Usage

```r
tfb_masked_dense(
  inputs,
  units,
  num_blocks = NULL,
  exclusive = FALSE,
  kernel_initializer = NULL,
  reuse = NULL,
  name = NULL,
...)
```

Arguments

- **inputs**: Tensor input.
- **units**: integer scalar representing the dimensionality of the output space.
- **num_blocks**: integer scalar representing the number of blocks for the MADE masks.
- **exclusive**: logical scalar representing whether to zero the diagonal of the mask, used for the first layer of a MADE.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
tfb_masked_dense

kernel_initializer
Initializer function for the weight matrix. If NULL (default), weights are initialized using the tf$glorot_random_initializer

reuse
logical scalar representing whether to reuse the weights of a previous layer by the same name.

name
string used to describe ops managed by this function.

... tf$layers$dense arguments

Details
See Germain et al. (2015) for detailed explanation.

Value
tensor

References

See Also
For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_matrix_inverse_tri_l

Computes \( g(L) = \text{inv}(L) \), where \( L \) is a lower-triangular matrix

Description

\( L \) must be nonsingular; equivalently, all diagonal entries of \( L \) must be nonzero. The input must have rank \( \geq 2 \). The input is treated as a batch of matrices with batch shape \( \text{input.shape}[:-2] \), where each matrix has dimensions \( \text{input.shape}[-2] \) by \( \text{input.shape}[-1] \) (hence \( \text{input.shape}[-2] \) must equal \( \text{input.shape}[-1] \)).

Usage

```
tfb_matrix_inverse_tri_l(validate_args = FALSE, name = "matrix_inverse_tril")
```

Arguments

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`.

Other bijectors: `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
Matrix-vector multiply using LU decomposition

Description

This bijector is identical to the "Convolution1x1" used in Glow (Kingma and Dhariwal, 2018).

Usage

```r
tfb_matvec_lu(lower_upper, permutation, validate_args = FALSE, name = NULL)
```

Arguments

- `lower_upper`: The LU factorization as returned by `tf$linalg$lu`.
- `permutation`: The LU factorization permutation as returned by `tf$linalg$lu`.
- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

Details

Warning: this bijector never verifies the scale matrix (as parameterized by LU decomposition) is invertible. Ensuring this is the case is the caller’s responsibility.

Value

a bijector instance.

References


See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`. Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`. 
tfb_normal_cdf

Computes $Y = g(X) = \text{NormalCDF}(x)$

description
This bijector maps inputs from $[-\infty, \infty]$ to $[0, 1]$. The inverse of the bijector applied to a uniform random variable $X \sim U(0, 1)$ gives back a random variable with the Normal distribution:

usage
```python
tfb_normal_cdf(validate_args = FALSE, name = "normal")
```

arguments
- **validate_args** Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name** name prefixed to Ops created by this class.

details
$Y \sim \text{Normal}(0, 1)$

\[
\text{pdf}(y; 0., 1.) = \frac{1}{\sqrt{2 \cdot \pi}} \exp(-y^2 / 2)
\]

value
a bijector instance.

see also
For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine()`, `tfb_affine_scalar()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked Dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`,
tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(),
tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(),
tfbtranspose(), tfb_weibull_cdf(), tfb_weibull()

tfb_ordered

Bijector which maps a tensor $x_k$ that has increasing elements in the last dimension to an unconstrained tensor $y_k$

Description

Both the domain and the codomain of the mapping is $[-\infty, \infty]$, however, the input of the forward mapping must be strictly increasing. The inverse of the bijector applied to a normal random vector $y \sim N(0,1)$ gives back a sorted random vector with the same distribution $x \sim N(0,1)$ where $x = \text{sort}(y)$

Usage

```r
tfb_ordered(validate_args = FALSE, name = "ordered")
```

Arguments

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

Details

On the last dimension of the tensor, Ordered bijector performs:

$$y[0] = x[0]$$
$$y[1:] = \text{tflog}(x[1:] - x[:-1])$$

Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`,
`tfb_affine()`, `tfbAscending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`,
`tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`,
`tfb_cusum()`, `tfb_continuous_cosine_transform()`, `tfb_exp()`, `tfb_expm1()`, `tfb_ffjord()`,
`tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`,
`tfb_gumbel()`, `tfb_identity()`, `tfb_inverse()`, `tfb_iterated_sigmoid_centered()`,
`tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`,
`tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`,
`tfb_matrixvec_lu()`, `tfb_normal_cdf()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`,
`tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`,
tfb_pad

Pads a value to the event_shape of a Tensor.

Description

The semantics of bijector_pad generally follow that of tf$pad() except that bijector_pad's paddings argument applies to the rightmost dimensions. Additionally, the new argument axis enables overriding the dimensions to which paddings is applied. Like paddings, the axis argument is also relative to the rightmost dimension and must therefore be negative. The argument paddings is a vector of integer pairs each representing the number of left and/or right constant_values to pad to the corresponding rightmost dimensions. That is, unless axis is specified, specifying k different paddings means the rightmost k dimensions will be "grown" by the sum of the respective paddings row. When axis is specified, it indicates the dimension to which the corresponding padding element is applied. By default axis is NULL which means it is logically equivalent to \texttt{range(start=-length(paddings), limit=0)}, i.e., the rightmost dimensions.

Usage

```r
tfb_pad(
  paddings = list(c(0, 1)),
  mode = "CONSTANT",
  constant_values = 0,
  axis = NULL,
  validate_args = FALSE,
  name = NULL
)
```

Arguments

- **paddings**: A vector-shaped Tensor of integer pairs representing the number of elements to pad on the left and right, respectively. Default value: list(reticulate::tuple(0L, 1L)).
- **mode**: One of 'CONSTANT', 'REFLECT', or 'SYMMETRIC' (case-insensitive). For more details, see tf$pad.
- **constant_values**: In 'CONSTANT' mode, the scalar pad value to use. Must be same type as tensor. For more details, see tf$pad.
- **axis**: The dimensions for which paddings are applied. Must be 1:1 with paddings or NULL. Default value: NULL (i.e., tf$range(start = -length(paddings), limit = 0)).
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.
tfb_permute

Permutes the rightmost dimension of a Tensor

Description
Permutes the rightmost dimension of a Tensor

Usage
```r
tfb_permute(permutation, axis = -1L, validate_args = FALSE, name = NULL)
```

Arguments
- **permutation**: An integer-like vector-shaped Tensor representing the permutation to apply to the axis dimension of the transformed Tensor.
- **axis**: Scalar integer Tensor representing the dimension over which to tf$gather. axis must be relative to the end (reading left to right) thus must be negative. Default value: -1 (i.e., right-most).
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

Value
a bijector instance.

See Also
For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(),
tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(),
tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(),
tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expml(), tfb_exp(), tfb_ffjord(),
tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(),
tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(),
tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(),
tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(),
tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_permute(), tfb_power_transform(),
tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(),
tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(),
tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(),
tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(),
tfbTranspose(), tfb_weibull_cdf(), tfb_weibull()
tfb_power_transform

Computes \( Y = g(X) = (1 + X \times c)^{1 / c} \), where \( X \geq -1 / c \).

**Description**

The power transform maps inputs from \([0, \infty)\) to \([-1/c, \infty)\); this is equivalent to the inverse of this bijector. This bijector is equivalent to the Exp bijector when \( c=0 \).

**Usage**

```python
tfb_power_transform(power, validate_args = FALSE, name = "power_transform")
```

**Arguments**

- **power**: float scalar indicating the transform power, i.e., \( Y = g(X) = (1 + X \times c)^{1 / c} \) where \( c \) is the power.
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

**Value**

a bijector instance.
See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_rational_quadratic_spline()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

---

tfb_rational_quadratic_spline

A piecewise rational quadratic spline, as developed in Conor et al.(2019).

Description

This transformation represents a monotonically increasing piecewise rational quadratic function. Outside of the bounds of knot_x/knot_y, the transform behaves as an identity function.

Usage

```r
tfb_rational_quadratic_spline(
  bin_widths,
  bin_heights,
  knot_slopes,
  range_min = -1,
  validate_args = FALSE,
  name = NULL
)
```

Arguments

- **bin_widths**
  The widths of the spans between subsequent knot x positions, a floating point Tensor. Must be positive, and at least 1-D. Innermost axis must sum to the same value as `bin_heights`. The knot x positions will be a first at `range_min`, followed by knots at `range_min + cumsum(bin_widths, axis=-1)`. 

**bin_heights**
The heights of the spans between subsequent knot positions, a floating point Tensor. Must be positive, and at least 1-D. Innermost axis must sum to the same value as bin_widths. The knot positions will be a first at range_min, followed by knots at range_min + cumsum(bin_heights, axis=-1).

**knot_slopes**
The slope of the spline at each knot, a floating point Tensor. Must be positive. 1s are implicitly padded for the first and last implicit knots corresponding to range_min and range_min + sum(bin_widths, axis=-1). Innermost axis size should be 1 less than that of bin_widths/bin_heights, or 1 for broadcasting.

**range_min**
The x/y position of the first knot, which has implicit slope 1. range_max is implicit, and can be computed as range_min + sum(bin_widths, axis=-1). Scalar floating point Tensor.

**validate_args**
Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

**name**
name prefixed to Ops created by this class.

**Details**
Typically this bijector will be used as part of a chain, with splines for trailing x dimensions conditioned on some of the earlier x dimensions, and with the inverse then solved first for unconditioned dimensions, then using conditioning derived from those inverses, and so forth.

For each argument, the innermost axis indexes bins/knots and batch axes index axes of x/y spaces. A RationalQuadraticSpline with a separate transform for each of three dimensions might have bin_widths shaped [3, 32]. To use the same spline for each of x’s three dimensions we may broadcast against x and use a bin_widths parameter shaped [32]. Parameters will be broadcast against each other and against the input x/ys, so if we want fixed slopes, we can use kwarg knot_slopes=1. A typical recipe for acquiring compatible bin widths and heights would be:

```r
nbins <- unconstrained_vector$shape[-1]
range_min <- 1
range_max <- 1
min_bin_size = 1e-2
scale <- range_max - range_min - nbins * min_bin_size
bin_widths = tf$math$softmax(unconstrained_vector) * scale + min_bin_size
```

**Value**
a bijector instance.

**References**
tfb_rayleigh_cdf

Compute \( Y = g(X) = 1 - \exp(-\frac{(X/l)^2}{2}), X \geq 0 \).

Description

This bijector maps inputs from \([0, \infty]\) to \([0, 1]\). The inverse of the bijector applied to a uniform random variable \( X \sim U(0, 1) \) gives back a random variable with the Rayleigh distribution:

\[
Y \sim \text{Rayleigh}(scale)
\]

\[
\text{pdf}(y; \text{scale}, y \geq 0) = \frac{1}{\text{scale}} \times \frac{y}{\text{scale}} \times \exp(-\frac{(y/\text{scale})^2}{2})
\]

Usage

```python
tfb_rayleigh_cdf(scale, validate_args = FALSE, name = "rayleigh_cdf")
```

Arguments

- `scale` (Positive floating-point tensor. This is in \( Y = g(X) = 1 - \exp(-\frac{(X/l)^2}{2}), X \geq 0 \).)
- `validate_args` (Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.)
- `name` (name prefixed to Ops created by this class.)

Details

Likewise, the forward of this bijector is the Rayleigh distribution CDF.

Value

A bijector instance.
Real NVP affine coupling layer for vector-valued events

Real NVP models a normalizing flow on a D-dimensional distribution via a single D-d-dimensional conditional distribution (Dinh et al., 2017): $y_{[d:D]} = x_{[d:D]} * \exp(\log\_scale\_fn(x_{[0:d]})) + \text{shift}\_fn(x_{[0:d]})$ $y_{[0:d]} = x_{[0:d]}$ The last D-d units are scaled and shifted based on the first d units only, while the first d units are ’masked’ and left unchanged. Real NVP’s shift_and_log_scale_fn computes vector-valued quantities. For scale-and-shift transforms that do not depend on any masked units, i.e. $d=0$, use the tfb_affine bijector with learned parameters instead. Masking is currently only supported for base distributions with event_ndims=1. For more sophisticated masking schemes like checkerboard or channel-wise masking (Papamakarios et al., 2016), use the tfb_permute bijector to re-order desired masked units into the first d units. For base distributions with event_ndims > 1, use the tfb_reshape bijector to flatten the event shape.

Usage

tfb_real_nvp(
    num_masked,
    shift_and_log_scale_fn,
    is_constant_jacobian = FALSE,
    validate_args = FALSE,
    name = NULL
)
Arguments

num_masked  integer indicating that the first d units of the event should be masked. Must be in the closed interval [1, D-1], where D is the event size of the base distribution.

shift_and_log_scale_fn  Function which computes shift and log_scale from both the forward domain (x) and the inverse domain (y). Calculation must respect the "autoregressive property". Suggested default: tfb_real_nvp_default_template(hidden_layers=...). Typically the function contains tf$Variables and is wrapped using tf$make_template. Returning NULL for either (both) shift, log_scale is equivalent to (but more efficient than) returning zero.

is_constant_jacobian  Logical, default: FALSE. When TRUE the implementation assumes log_scale does not depend on the forward domain (x) or inverse domain (y) values. (No validation is made; is_constant_jacobian=FALSE is always safe but possibly computationally inefficient.)

validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name  name prefixed to Ops created by this class.

Details

Recall that the MAF bijector (Papamakarios et al., 2016) implements a normalizing flow via an autoregressive transformation. MAF and IAF have opposite computational tradeoffs - MAF can train all units in parallel but must sample units sequentially, while IAF must train units sequentially but can sample in parallel. In contrast, Real NVP can compute both forward and inverse computations in parallel. However, the lack of an autoregressive transformations makes it less expressive on a per-bijector basis.

A "valid" shift_and_log_scale_fn must compute each shift (aka loc or "mu" in Papamakarios et al. (2016) and log(scale) (aka "alpha" in Papamakarios et al. (2016)) such that each are broadcastable with the arguments to forward and inverse, i.e., such that the calculations in forward, inverse below are possible. For convenience, real_nvp_default_nvp is offered as a possible shift_and_log_scale_fn function.

NICE (Dinh et al., 2014) is a special case of the Real NVP bijector which discards the scale transformation, resulting in a constant-time inverse-log-determinant-Jacobian. To use a NICE bijector instead of Real NVP, shift_and_log_scale_fn should return (shift, NULL), and is_constant_jacobian should be set to TRUE in the RealNVP constructor. Calling tfb_real_nvp_default_template with shift_only=TRUE returns one such NICE-compatible shift_and_log_scale_fn function.

Caching: the scalar input depth D of the base distribution is not known at construction time. The first call to any of forward(x), inverse(x), inverse_log_det_jacobian(x), or forward_log_det_jacobian(x) memoizes D, which is re-used in subsequent calls. This shape must be known prior to graph execution (which is the case if using tf$layers).

Value

a bijector instance.
tfb_real_nvp_default_template

Build a scale-and-shift function using a multi-layer neural network

Description

This will be wrapped in a make_template to ensure the variables are only created once. It takes the d-dimensional input \(x[0:d]\) and returns the \(D-d\) dimensional outputs \(\text{loc} \) ("mu") and \(\text{log_scale} \) ("alpha").

Usage

```python
tfb_real_nvp_default_template(
    hidden_layers,
    shift_only = FALSE,
    activation = tf$nn$relu,
)```

References

```python
name = NULL,
...
"

Arguments

- **hidden_layers**: list-like of non-negative integer, scalars indicating the number of units in each hidden layer. Default: list(512, 512).
- **shift_only**: logical indicating if only the shift term shall be computed (i.e. NICE bijector). Default: FALSE.
- **activation**: Activation function (callable). Explicitly setting to NULL implies a linear activation.
- **name**: A name for ops managed by this function. Default: "tfb_real_nvp_default_template".
...
```

tfb$layers$dense arguments

Details

The default template does not support conditioning and will raise an exception if condition_kwargs are passed to it. To use conditioning in real nvp bijector, implement a conditioned shift/scale template that handles the condition_kwargs.

Value

- list of:
  - **shift**: Float-like Tensor of shift terms
  - **log_scale**: Float-like Tensor of log(scale) terms

References


See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfbAscending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outter_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadric_spline(), tfb_rayleigh_cdf(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_reciprocal

A Bijector that computes \( b(x) = 1. \div x \)

Description

A Bijector that computes \( b(x) = 1. \div x \)

Usage

```r
tfb_reciprocal(validate_args = FALSE, name = "reciprocal")
```

Arguments

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`. Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tril()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inlin()`}, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tril()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tril()`, `tfb_scale_tril()`, `tfb_sharded_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
tfb_reshape  
Reshapes the event_shape of a Tensor

Description

The semantics generally follow that of `tf$reshape()`, with a few differences:

- The user must provide both the input and output shape, so that the transformation can be inverted. If an input shape is not specified, the default assumes a vector-shaped input, i.e., `event_shape_in = list(-1)`.
- The Reshape bijector automatically broadcasts over the leftmost dimensions of its input (sample_shape and batch_shape); only the rightmost `event_ndims_in` dimensions are reshaped. The number of dimensions to reshape is inferred from the provided `event_shape_in` (`event_ndims_in = length(event_shape_in)`).

Usage

```r
tfb_reshape(
  event_shape_out,
  event_shape_in = c(-1),
  validate_args = FALSE,
  name = NULL
)
```

Arguments

- `event_shape_out`  
  An integer-like vector-shaped Tensor representing the event shape of the transformed output.
- `event_shape_in`  
  An optional integer-like vector-shape Tensor representing the event shape of the input. This is required in order to define inverse operations; the default of list(-1) assumes a vector-shaped input.
- `validate_args`  
  Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`  
  name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`.
### tfb_scale

Compute $Y = g(X; \text{scale}) = \text{scale} \times X$.

#### Description

Examples:

```r
Y <- 2 * X
b <- tfb_scale(scale = 2)
```

#### Usage

```r
tfb_scale(
  scale = NULL,
  log_scale = NULL,
  validate_args = FALSE,
  name = "scale"
)
```

#### Arguments

- **scale**
  - Floating-point Tensor.

- **log_scale**
  - Floating-point Tensor. Logarithm of the scale. If this is set to NULL, no scale is applied. This should not be set if `scale` is set.

- **validate_args**
  - Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

- **name**
  - name prefixed to Ops created by this class.

#### Value

a bijector instance.
tfb_scale_matvec_diag

Compute \( Y = g(X; \text{scale}) = \text{scale} \odot X \)

**Description**

In TF parlance, the scale term is logically equivalent to:

\[
\text{scale} = \text{tf}$\text{diag}$(scale_diag)
\]

The scale term is applied without materializing a full dense matrix.

**Usage**

```r
tfb_scale_matvec_diag(
  scale_diag,
  adjoint = FALSE,
  validate_args = FALSE,
  name = "scale_matvec_diag",
  dtype = NULL
)
```

**Arguments**

- `scale_diag` (Floating-point Tensor representing the diagonal matrix. `scale_diag` has shape \([N1, N2, \ldots, k]\), which represents a \(k \times k\) diagonal matrix.

- `adjoint` (logical indicating whether to use the scale matrix as specified or its adjoint. Default value: FALSE.)
tfb_scale_matvec_linear_operator

validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name  name prefixed to Ops created by this class.

dtype  tf$DType to prefer when converting args to Tensors. Else, we fall back to a common dtype inferred from the args, finally falling back to float32.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tril(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tril(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

Compute $Y = g(X; \text{scale}) = \text{scale} @ X$.

Description

scale is a LinearOperator. If X is a scalar then the forward transformation is: scale $\ast X$ where $\ast$ denotes broadcasted elementwise product.

Usage

tfb_scale_matvec_linear_operator(
    scale,
    adjoint = FALSE,
    validate_args = FALSE,
    name = "scale_matvec_linear_operator"
)
tfb_scale_matvec_lu

Matrix-vector multiply using LU decomposition.

Description

This bijector is identical to the "Convolution1x1" used in Glow (Kingma and Dhariwal, 2018).

Usage

```python
tfb_scale_matvec_lu(
    lower_upper,
    permutation,
    validate_args = FALSE,
    name = NULL
)```
tfb_scale_matvec_tri_l

Arguments

lower_upper The LU factorization as returned by tf$linalg$lu.
permutation The LU factorization permutation as returned by tf$linalg$lu.
validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
name name prefixed to Ops created by this class.

Value

a bijector instance.

References


See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_exp(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arccosh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()

Compute $Y = g(X; scale) = scale @ X$.

Description

The scale term is presumed lower-triangular and non-singular (ie, no zeros on the diagonal), which permits efficient determinant calculation (linear in matrix dimension, instead of cubic).
tfb_scale_matvec_tri_l

Usage

tfb_scale_matvec_tri_l(
  scale_tril,
  adjoint = FALSE,
  validate_args = FALSE,
  name = "scale_matvec_tril",
  dtype = NULL
)

Arguments

scale_tril  Floating-point Tensor representing the lower triangular matrix. scale_tril has shape [N1, N2, ... k, k], which represents a k x k lower triangular matrix. When NULL no scale_tril term is added to scale. The upper triangular elements above the diagonal are ignored.

adjoint  logical indicating whether to use the scale matrix as specified or its adjoint. Note that lower-triangularity is taken into account first: the region above the diagonal of scale_tril is treated as zero (irrespective of the adjoint setting). A lower-triangular input with adjoint=TRUE will behave like an upper triangular transform. Default value: FALSE.

validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name  name prefixed to Ops created by this class.

dtype  tf$DType to prefer when converting args to Tensors. Else, we fall back to a common dtype inferred from the args, finally falling back to float32.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expml(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_vjp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
**tfb_scale_tri_l**

Transforms unconstrained vectors to TriL matrices with positive diagonal

**Description**

This is implemented as a simple tfb_chain of tfb_fill_triangular followed by tfb_transform_diagonal, and provided mostly as a convenience. The default setup is somewhat opinionated, using a Softplus transformation followed by a small shift (1e-5) which attempts to avoid numerical issues from zeros on the diagonal.

**Usage**

```r
tfb_scale_tri_l(
  diag_bijector = NULL,
  diag_shift = 1e-05,
  validate_args = FALSE,
  name = "scale_tril"
)
```

**Arguments**

- `diag_bijector`: Bijector instance, used to transform the output diagonal to be positive. Default value: NULL (i.e., tfb_softplus()).
- `diag_shift`: Float value broadcastable and added to all diagonal entries after applying the `diag_bijector`. Setting a positive value forces the output diagonal entries to be positive, but prevents inverting the transformation for matrices with diagonal entries less than this value. Default value: 1e-5.
- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`. Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`. 
tfb_shift

Compute $Y = g(X; \text{shift}) = X + \text{shift}$.

**Description**
where `shift` is a numeric Tensor.

**Usage**

```r
tfb_shift(shift, validate_args = FALSE, name = "shift")
```

**Arguments**

- `shift` floating-point tensor
- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

**Value**
a bijector instance.

**See Also**
For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

The other bijectors:
- `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`,
- `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`,
- `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`,
- `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`,
- `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`,
- `tfb_gumbel()`, `tfb_identity()`, `tfb_inplace()` , `tfb_iterated_sigmoid_centered()`,
- `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`,
- `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`,
- `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`,
- `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`,
- `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`,
- `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`,
- `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`,
- `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`,
- `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`.
tfb_shifted_gompertz_cdf

Compute \( Y = g(X) = (1 - \exp(-\text{rate} \times X)) \times \exp(-c \times \exp(-\text{rate} \times X)) \)

**Description**

This bijector maps inputs from \([-\infty, \infty]\) to \([0, \infty]\). The inverse of the bijector applied to a uniform random variable \( X \sim U(0, 1) \) gives back a random variable with the **Shifted Gompertz distribution**: 

\[
Y \sim \text{ShiftedGompertzCDF}(\text{concentration}, \text{rate})
\]

\[
\text{pdf}(y; c, r) = r \times \exp(-r \times y - \exp(-r \times y) / c) \times (1 + (1 - \exp(-r \times y)) / c)
\]

**Usage**

```python
tfb_shifted_gompertz_cdf(
    concentration,
    rate,
    validate_args = FALSE,
    name = "shifted_gompertz_cdf"
)
```

**Arguments**

- **concentration**: Positive Float-like Tensor that is the same dtype and is broadcastable with concentration. This is \( c \) in \( Y = g(X) = (1 - \exp(-\text{rate} \times X)) \times \exp(-c \times \exp(-\text{rate} \times X)) \).
- **rate**: Positive Float-like Tensor that is the same dtype and is broadcastable with concentration. This is \( \text{rate} \) in \( Y = g(X) = (1 - \exp(-\text{rate} \times X)) \times \exp(-c \times \exp(-\text{rate} \times X)) \).
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

**Details**

Note: Even though this is called ShiftedGompertzCDF, when applied to the Uniform distribution, this is not the same as applying a GompertzCDF with a Shift bijector (i.e. the Shifted Gompertz distribution is not the same as a Gompertz distribution with a location parameter).

Note: Because the Shifted Gompertz distribution concentrates its mass close to zero, for larger rates or larger concentrations, bijector$forward will quickly saturate to 1.
tfb_sigmoid

Computes $Y = g(X) = 1 / (1 + \exp(-X))$

Description
Computes $Y = g(X) = 1 / (1 + \exp(-X))$

Usage
`tfb_sigmoid(validate_args = FALSE, name = "sigmoid")`

Arguments
- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

Value
a bijector instance.
See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

---

tfb_sinh

**Bijector that computes** $Y = \sinh(X)$.

---

**Description**

Bijector that computes $Y = \sinh(X)$.

**Usage**

```r
tfb_sinh(validate_args = FALSE, name = "sinh")
```

**Arguments**

- `validate_args` Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name` name prefixed to Ops created by this class.

**Value**

a bijector instance.

**See Also**

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expml()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_scale()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_split()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`
tfb_sinh_arcsinh

Computes \( Y = g(X) = \text{Sinh}( (\text{Arcsinh}(X) + \text{skewness}) \times \text{tailweight} ) \)

**Description**

For skewness in \((-\infty, \infty)\) and tailweight in \((0, \infty)\), this transformation is a diffeomorphism of the real line \((-\infty, \infty)\). The inverse transform is \( X = g^{-1}(Y) = \text{Sinh}( \text{ArcSinh}(Y) / \text{tailweight} - \text{skewness} ) \). The SinhArcsinh transformation of the Normal is described in [Sinh-arcsinh distributions](#).

**Usage**

```r
tfb_sinh_arcsinh(
  skewness = NULL,
  tailweight = NULL,
  validate_args = FALSE,
  name = "SinhArcsinh"
)
```

**Arguments**

- **skewness**: Skewness parameter. Float-type Tensor. Default is 0 of type float32.
- **tailweight**: Tailweight parameter. Positive Tensor of same dtype as skewness and broadcastable shape. Default is 1 of type float32.
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

**Details**

This Bijector allows a similar transformation of any distribution supported on \((-\infty, \infty)\).

**Value**

a bijector instance.
Meaning of the parameters

- If skewness = 0 and tailweight = 1, this transform is the identity.
- Positive (negative) skewness leads to positive (negative) skew.
- Positive skew means, for unimodal X centered at zero, the mode of Y is "tilted" to the right.
- Positive skew means positive values of Y become more likely, and negative values become less likely.
- Larger (smaller) tailweight leads to fatter (thinner) tails.
- Fatter tails mean larger values of |Y| become more likely.
- If X is a unit Normal, tailweight < 1 leads to a distribution that is "flat" around Y = 0, and a very steep drop-off in the tails.
- If X is a unit Normal, tailweight > 1 leads to a distribution more peaked at the mode with heavier tails. To see the argument about the tails, note that for |X| » 1 and |X| » (|skewness| * tailweight) we have Y approx 0.5 X |tailweight| exp(sign(X) skewness * tailweight).

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(), tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(), tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(), tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(), tfb_gumbel(), tfb_identity(), tfb_invert(), tfb_iterated_sigmoid_centered(), tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(), tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(), tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(), tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(), tfb_real_nvp(), tfb_reciprocal(), tfb_reshape(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(), tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scaled(), tfb_shifted_gompertz_cdf(), tfb_shift(), tfb_sigmoid(), tfb_sinh(), tfb_softmax_centered(), tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_tanh(), tfb_transform_diagonal(), tfb transpose(), tfb_weibull_cdf(), tfb_weibull()

tfb_softmax_centered  Computes Y = g(X) = exp([X 0]) / sum(exp([X 0]))

Description

To implement softmax as a bijection, the forward transformation appends a value to the input and the inverse removes this coordinate. The appended coordinate represents a pivot, e.g., softmax(x) = exp(x-c) / sum(exp(x-c)) where c is the implicit last coordinate.

Usage

tfb_softmax_centered(validate_args = FALSE, name = "softmax_centered")
tfb_softplus

Computes $Y = g(X) = \log[1 + \exp(X)]$

Description

The softplus Bijector has the following two useful properties:

- The domain is the positive real numbers
- softplus(x) approx x, for large x, so it does not overflow as easily as the Exp Bijector.
Usage

tfb_softplus(
    hinge_softness = NULL,
    low = NULL,
    validate_args = FALSE,
    name = "softplus"
)

Arguments

hinge_softness  Nonzero floating point Tensor. Controls the softness of what would otherwise
                be a kink at the origin. Default is 1.0.

low  Nonzero floating point tensor, lower bound on output values. Implicitly zero
       if NULL. Otherwise, the transformation \( y = \text{softplus}(x) + \text{low} \) is implemented.
       This is equivalent to a tfb_chain(list(tfb_shift(low), tfb_softplus()))
       bijector and is provided for convenience.

validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args
                is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name  name prefixed to Ops created by this class.

Details

The optional nonzero hinge_softness parameter changes the transition at zero. With hinge_softness
= c, the bijector is:

\[
f_c(x) := c \times g(x / c) = c \times \log[1 + \exp(x / c)].
\]

For large \( x \gg 1 \),

\[
c \times \log[1 + \exp(x / c)] \approx c \times \log[\exp(x / c)] = x
\]

so the behavior for large \( x \) is the same as the standard softplus.
As \( c > 0 \) approaches 0 from the right, \( f_c(x) \) becomes less and less soft,
approaching \( \max(0, x) \).
* \( c = 1 \) is the default.
* \( c > 0 \) but small means \( f(x) \approx \text{ReLu}(x) = \max(0, x) \).
* \( c < 0 \) flips sign and reflects around the y-axis: \( f_{-c}(x) = -f_c(-x) \).
* \( c = 0 \) results in a non-bijective transformation and triggers an exception.
Note: \( \log(.) \) and \( \exp(.) \) are applied element-wise but the Jacobian is a reduction over the event space.

\[
[1 + \exp(x / c)]: R:1\%20+\%20\exp(x\%20/\%20c)
\]
\[
[1 + \exp(x / c)]: R:1\%20+\%20\exp(x\%20/\%20c)
\]
\[
[\exp(x / c)]: R:exp(x\%20/\%20c)
\]
Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_ascending()`, `tfb_blockwise()`, `tfb_batch_normalization()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`.

Usage

```python
tfb_softsign(validate_args = FALSE, name = "softsign")
```

Arguments

- `validate_args`: Logical, default FALSE. Whether to validate input with asserts. If `validate_args` is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- `name`: name prefixed to Ops created by this class.

Description

The softsign Bijector has the following two useful properties:

- The domain is all real numbers
- `softsign(x)` approx `sgn(x)`, for large `|x|`.

**Computes** $Y = g(X) = X / (1 + |X|)$
**tfb_split**

Split a Tensor event along an axis into a list of Tensors.

**Description**

The inverse of split concatenates a list of Tensors along axis.

**Usage**

tfb_split(num_or_size_splits, axis = -1, validate_args = FALSE, name = "split")

**Arguments**

- **num_or_size_splits**
  
  Either an integer indicating the number of splits along axis or a 1-D integer Tensor or Python list containing the sizes of each output tensor along axis. If a list/Tensor, it may contain at most one value of -1, which indicates a split size that is unknown and determined from input.

- **axis**
  
  A negative integer or scalar int32 Tensor. The dimension along which to split. Must be negative to enable the bijector to support arbitrary batch dimensions. Defaults to -1 (note that this is different from the tf$split default of 0). Must be statically known.

- **validate_args**
  
  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

- **name**
  
  name prefixed to Ops created by this class.

**Value**

a bijector instance.
tbf_square

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_choloperator()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvecLu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvecLu()`, `tfb_scale_matvec_tri_l()`, `tfb_scale_tri_l()`, `tfb_shifted_gompertz_cdf()`, `tfb_shift()`, `tfb_sigmoid()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`, `tfb_softplus()`, `tfb_softsign()`, `tfb_square()`, `tfb_tanh()`, `tfb_transform_diagonal()`, `tfb_transpose()`, `tfb_weibull_cdf()`, `tfb_weibull()`

---

tbf_square

Computes $g(X) = X^2$; $X$ is a positive real number.

---

Description

$g$ is a bijection between the non-negative real numbers ($\mathbb{R}_+$) and the non-negative real numbers.

Usage

```python
import tensorflow.bijectors as tfb

tfb.square(validate_args = FALSE, name = "square")
```

Arguments

- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

- **name**: name prefixed to Ops created by this class.

Value

A bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_affine_linear_operator()`, `tfb_affine_scalar()`, `tfb_affine()`, `tfb_ascending()`, `tfb_batch_normalization()`, `tfb_blockwise()`, `tfb_chain()`, `tfb_choloperator()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_expm1()`, `tfb_exp()`, `tfb_ffjord()`,
tfb_tanh

Computes $Y = \tanh(X)$

description

$Y = \tanh(X)$, therefore $Y$ in $(-1, 1)$.

Usage

tfb_tanh(validate_args = FALSE, name = "tanh")

Arguments

validate_args Logical, default FALSE. Whether to validate input with asserts. If validate_args
is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

name name prefixed to Ops created by this class.

details

This can be achieved by an affine transform of the Sigmoid bijector, i.e., it is equivalent to

```
tfb_chain(list(tfb_affine(shift = -1, scale = 2), tfb_sigmoid(), tfb_affine(scale = 2)))
```

However, using the Tanh bijector directly is slightly faster and more numerically stable.

value

a bijector instance.

see also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(),
  tfb_affine(), tfb_ascending(), tfb_batch_normalization(), tfb_blockwise(), tfb_chain(),
  tfb_cholesky_outer_product(), tfb_cholesky_to_inv_cholesky(), tfb_correlation_cholesky(),
  tfb_cumsum(), tfb_discrete_cosine_transform(), tfb_expm1(), tfb_exp(), tfb_ffjord(),
  tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(),
Applies a Bijector to the diagonal of a matrix

Description

Applies a Bijector to the diagonal of a matrix

Usage

tfb_transform_diagonal(
    diag_bijector,
    validate_args = FALSE,
    name = "transform_diagonal"
)

Arguments

diag_bijector  Bijector instance used to transform the diagonal.
validate_args  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
name           name prefixed to Ops created by this class.

Value

a bijector instance.

See Also

For usage examples see tfb_forward(), tfb_inverse(), tfb_inverse_log_det_jacobian().

Other bijectors: tfb_absolute_value(), tfb_affine_linear_operator(), tfb_affine_scalar(), tfb_affine(), tfb_ascending(), tfb_exp(), tfb_expm(), tfb_ffjord(),
tfb_fill_scale_tri_l(), tfb_fill_triangular(), tfb_glow(), tfb_gompertz_cdf(), tfb_gumbel_cdf(),
tfb_gumbel(), tfb_identity(), tfb_inline(), tfb_inverse(), tfb_iterated_sigmoid_centered(),
tfb_kumaraswamy_cdf(), tfb_kumaraswamy(), tfb_lambert_w_tail(), tfb_masked_autoregressive_default_template(),
tfb_masked_autoregressive_flow(), tfb_masked_dense(), tfb_matrix_inverse_tri_l(),
tfb_matvec_lu(), tfb_normal_cdf(), tfb_ordered(), tfb_pad(), tfb_permute(), tfb_power_transform(),
tfb_rational_quadratic_spline(), tfb_rayleigh_cdf(), tfb_real_nvp_default_template(),
tfb_real_nvp(), tfb_reciprocal(), tfb_scale_matvec_diag(), tfb_scale_matvec_linear_operator(),
tfb_scale_matvec_lu(), tfb_scale_matvec_tri_l(), tfb_scale_tri_l(), tfb_scale(), tfb_shifted_gompertz_cdf(),
tfb_shift(), tfb_sigmoid(), tfb_sinh_arcsinh(), tfb_sinh(), tfb_softmax_centered(),
tfb_softplus(), tfb_softsign(), tfb_split(), tfb_square(), tfb_transform_diagonal(),
tfb_transpose(), tfb_weibull_cdf(), tfb_weibull()
tfb_transpose

Computes $Y = g(X) = \text{transposeightmost
dims}(X, \rightmost\perm)$

**Description**

This bijector is semantically similar to tf.transpose except that it transposes only the rightmost "event" dimensions. That is, unlike tf$\text{transpose}$ the perm argument is itself a permutation of tf$\text{rank}(\rightmost\transposed\ndims)$ rather than tf$\text{rank}(x)$, i.e., users specify the (rightmost) dimensions to permute, not all dimensions.

**Usage**

```r
tfb_transpose(
  perm = NULL,
  rightmost_transposed_ndims = NULL,
  validate_args = FALSE,
  name = "transpose"
)
```

**Arguments**

- **perm**
  Positive integer vector-shaped Tensor representing permutation of rightmost dims (for forward transformation). Note that the 0th index represents the first of the rightmost dims and the largest value must be rightmost_transposed\ndims - 1 and corresponds to tf$\text{rank}(x) - 1$. Only one of perm and rightmost_transposed\ndims can (and must) be specified. Default value: tf$\text{range}(\text{start}=\rightmost\transposed\ndims, \text{limit}=-1, \text{delta}=-1)$.

- **rightmost_transposed_ndims**
  Positive integer scalar-shaped Tensor representing the number of rightmost dimensions to permute. Only one of perm and rightmost_transposed\ndims can (and must) be specified. Default value: tf$\text{size}(\perm)$.

- **validate_args**
  Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.

- **name**
  name prefixed to Ops created by this class.
The actual (forward) transformation is:
\[
\text{sample\_batch\_ndims} = \text{tf\$rank}(x) - \text{tf\$size}(\text{perm}) \\
\text{perm} = \text{tf\$concat}\left(\left[\text{tf\$range}(\text{sample\_batch\_ndims}), \text{sample\_batch\_ndims} + \text{perm}\right]\right), \text{axis}=0 \\
\text{tf\$transpose}(x, \text{perm})
\]

Value

a bijector instance.

See Also

For usage examples see \texttt{tfb\_forward()}, \texttt{tfb\_inverse()}, \texttt{tfb\_inverse\_log\_det\_jacobian()}. Other bijectors: \texttt{tfb\_absolute\_value()}, \texttt{tfb\_affine\_linear\_operator()}, \texttt{tfb\_affine\_scalar()}, \texttt{tfb\_ascending()}, \texttt{tfb\_batch\_normalization()}, \texttt{tfb\_blockwise()}, \texttt{tfb\_chain()}, \texttt{tfb\_cholesky\_outer\_product()}, \texttt{tfb\_cholesky\_to\_inv\_cholesky()}, \texttt{tfb\_correlation\_cholesky()}, \texttt{tfb\_cumsum()}, \texttt{tfb\_discrete\_cosine\_transform()}, \texttt{tfb\_expm1()}, \texttt{tfb\_exp()}, \texttt{tfb\_ffjord()}, \texttt{tfb\_fill\_scale\_tri\_l()}, \texttt{tfb\_fill\_triangular()}, \texttt{tfb\_glow()}, \texttt{tfb\_gompertz\_cdf()}, \texttt{tfb\_gumbel\_cdf()}, \texttt{tfb\_gumbel()}, \texttt{tfb\_identity()}, \texttt{tfb\_inline()}, \texttt{tfb\_invert()}, \texttt{tfb\_iterated\_sigmoid\_centered()}, \texttt{tfb\_kumaraswamy\_cdf()}, \texttt{tfb\_kumaraswamy()}, \texttt{tfb\_lambert\_w\_tail()}, \texttt{tfb\_masked\_autoregressive\_default\_template()}, \texttt{tfb\_masked\_autoregressive\_flow()}, \texttt{tfb\_masked\_dense()}, \texttt{tfb\_matrix\_inverse\_tri\_l()}, \texttt{tfb\_matvec\_lu()}, \texttt{tfb\_normal\_cdf()}, \texttt{tfb\_ordered()}, \texttt{tfb\_pad()}, \texttt{tfb\_permute()}, \texttt{tfb\_power\_transform()}, \texttt{tfb\_rational\_quadratic\_spline()}, \texttt{tfb\_rayleigh\_cdf()}, \texttt{tfb\_real\_nvp\_default\_template()}, \texttt{tfb\_real\_nvp()}, \texttt{tfb\_reciprocal()}, \texttt{tfb\_reshape()}, \texttt{tfb\_scale\_matvec\_diag()}, \texttt{tfb\_scale\_matvec\_linear\_operator()}, \texttt{tfb\_scale\_matvec\_lu()}, \texttt{tfb\_scale\_matvec\_tri\_l()}, \texttt{tfb\_scale\_tri\_l()}, \texttt{tfb\_scale()}, \texttt{tfb\_shifted\_gompertz\_cdf()}, \texttt{tfb\_sigmoid()}, \texttt{tfb\_sinh\_arcsinh()}, \texttt{tfb\_sinh()}, \texttt{tfb\_softmax\_centered()}, \texttt{tfb\_softplus()}, \texttt{tfb\_softsign()}, \texttt{tfb\_split()}, \texttt{tfb\_square()}, \texttt{tfb\_tanh()}, \texttt{tfb\_transform\_diagonal()}, \texttt{tfb\_weibull\_cdf()}, \texttt{tfb\_weibull()}

---

**tfb\_weibull**

*Computes* \( Y = g(X) = 1 - \exp\left(-\frac{X}{\text{scale}}\right)^\text{concentration} \)

*where* \( X \geq 0 \)

**Description**

This bijector maps inputs from \([0, \infty]\) to \([0, 1]\). The inverse of the bijector applied to a uniform random variable \( X \sim U(0, 1) \) gives back a random variable with the Weibull distribution:

**Usage**

```python
  tfb_weibull(
    scale = 1,
    concentration = 1,
    validate_args = FALSE,
    name = "weibull"
)```
tfb_weibull_cdf  Compute \( Y = g(X) = 1 - \exp((-X / \text{scale})^{\text{concentration}}) \), \( X \geq 0 \).

description
This bijector maps inputs from [0, inf] to [0, 1]. The inverse of the bijector applied to a uniform random variable \( X \sim U(0, 1) \) gives back a random variable with the Weibull distribution.
\( Y \sim \text{Weibull}(\text{scale}, \text{concentration}) \)

\[
\text{pdf}(y; \text{scale}, \text{concentration}, y \geq 0) = \\
\left( \frac{\text{concentration}}{\text{scale}} \right) \times (y / \text{scale})^{(\text{concentration} - 1)} \times \\
\exp\left(-\frac{y}{\text{scale}}\right)^{\text{concentration}}
\]

Usage

```python
tfb_weibull_cdf(
    scale = 1,
    concentration = 1,
    validate_args = FALSE,
    name = "weibull_cdf"
)
```

Arguments

- **scale**: Positive Float-type Tensor that is the same dtype and is broadcastable with concentration. This is \( l \) in \( Y = g(X) = 1 - \exp\left(-\frac{x}{l}\right)^k \).
- **concentration**: Positive Float-type Tensor that is the same dtype and is broadcastable with scale. This is \( k \) in \( Y = g(X) = 1 - \exp\left(-\frac{x}{l}\right)^k \).
- **validate_args**: Logical, default FALSE. Whether to validate input with asserts. If validate_args is FALSE, and the inputs are invalid, correct behavior is not guaranteed.
- **name**: name prefixed to Ops created by this class.

Details

Likewise, the forward of this bijector is the Weibull distribution CDF.

Value

a bijector instance.

See Also

For usage examples see `tfb_forward()`, `tfb_inverse()`, `tfb_inverse_log_det_jacobian()`.

Other bijectors: `tfb_absolute_value()`, `tfb_ascending()`, `tfb_block_normalization()`, `tfb_batch_normalization()`, `tfb_chain()`, `tfb_cholesky_outer_product()`, `tfb_cholesky_to_inv_cholesky()`, `tfb_correlation_cholesky()`, `tfb_cumsum()`, `tfb_discrete_cosine_transform()`, `tfb_exp()`, `tfb_expml()`, `tfb_ffjord()`, `tfb_fill_scale_tri_l()`, `tfb_fill_triangular()`, `tfb_glow()`, `tfb_gompertz_cdf()`, `tfb_gumbel_cdf()`, `tfb_gumbel()`, `tfb_identity()`, `tfb_inline()`, `tfb_invert()`, `tfb_iterated_sigmoid_centered()`, `tfb_kumaraswamy_cdf()`, `tfb_kumaraswamy()`, `tfb_lambert_w_tail()`, `tfb_masked_autoregressive_default_template()`, `tfb_masked_autoregressive_flow()`, `tfb_masked_dense()`, `tfb_matrix_inverse_tri_l()`, `tfb_matvec_lu()`, `tfb_normal_cdf()`, `tfb_ordered()`, `tfb_pad()`, `tfb_permute()`, `tfb_power_transform()`, `tfb_rational_quadratic_spline()`, `tfb_rayleigh_cdf()`, `tfb_real_nvp_default_template()`, `tfb_real_nvp()`, `tfb_reciprocal()`, `tfb_reshape()`, `tfb_scale_matvec_diag()`, `tfb_scale_matvec_linear_operator()`, `tfb_scale_matvec_lu()`, `tfb_shift()`, `tfb_sign()`, `tfb_sinh_arcsinh()`, `tfb_sinh()`, `tfb_softmax_centered()`. 
tfd_autoregressive

**Autoregressive distribution**

**Description**

The Autoregressive distribution enables learning (often) richer multivariate distributions by repeatedly applying a diffeomorphic transformation (such as implemented by Bijectors).

**Usage**

```python
tfd_autoregressive(
    distribution_fn,
    sample0 = NULL,
    num_steps = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Autoregressive"
)
```

**Arguments**

- **distribution_fn**
  Function which constructs a `tfd$Distribution`-like instance from a `Tensor` (e.g., `sample0`). The function must respect the "autoregressive property", i.e., there exists a permutation of event such that each coordinate is a diffeomorphic function of on preceding coordinates.

- **sample0**
  Initial input to `distribution_fn`, used to build the distribution in `__init__` which in turn specifies this distribution's properties, e.g., `event_shape`, `batch_shape`, `dtype`. If unspecified, then `distribution_fn` should be default constructable.

- **num_steps**
  Number of times `distribution_fn` is composed from samples, e.g., `num_steps=2` implies `distribution_fn(distribution_fn(sample0)$sample(n))$sample()`.

- **validate_args**
  Logical, default `FALSE`. When `TRUE` distribution parameters are checked for validity despite possibly degrading runtime performance. When `FALSE` invalid inputs may silently render incorrect outputs. Default value: `FALSE`.

- **allow_nan_stats**
  Logical, default `TRUE`. When `TRUE`, statistics (e.g., mean, mode, variance) use the value `NaN` to indicate the result is undefined. When `FALSE`, an exception is raised if one or more of the statistic's batch members are undefined.

- **name**
  name prefixed to Ops created by this class.
Details

Regarding terminology, "Autoregressive models decompose the joint density as a product of conditionals, and model each conditional in turn. Normalizing flows transform a base density (e.g. a standard Gaussian) into the target density by an invertible transformation with tractable Jacobian." (Papamakarios et al., 2016)

In other words, the "autoregressive property" is equivalent to the decomposition, \( p(x) = \prod \{ p(x[i] | x[0:i]) : i=0, \ldots, d \} \).

The provided `shift_and_log_scale_fn`, `tfb_masked_autoregressive_default_template`, achieves this property by zeroing out weights in its `masked_dense` layers. Practically speaking the autoregressive property means that there exists a permutation of the event coordinates such that each coordinate is a diffeomorphic function of only preceding coordinates (van den Oord et al., 2016).

Mathematical Details

The probability function is

\[
\text{prob}(x; \text{fn}, n) = \text{fn}(x).\text{prob}(x)
\]

And a sample is generated by

\[
x = \text{fn}(\ldots\text{fn}(\text{fn}(x0).\text{sample()}).\text{sample()}).\text{sample()}
\]

where the ellipses (\( \ldots \)) represent \( n-2 \) composed calls to \( \text{fn} \), \( \text{fn} \) constructs a `tfd$Distribution`-like instance, and \( x0 \) is a fixed initializing Tensor.

Value

a distribution instance.

References


See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_batch_reshape

Batch-Reshaping distribution

Description

This "meta-distribution" reshapess the batch dimensions of another distribution.

Usage

```r
tfd_batch_reshape(
  distribution,
  batch_shape,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = NULL
)
```

Arguments

distribution The base distribution instance to reshape. Typically an instance of Distribution.
batch_shape Positive integer-like vector-shaped Tensor representing the new shape of the batch dimensions. Up to one dimension may contain -1, meaning the remainder of the batch size.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
name name prefixed to Ops created by this class.
The Bates distribution is the distribution of the average of total_count independent samples from Uniform(low, high). It is parameterized by the interval bounds low and high, and total_count, the number of samples. Although some care has been taken to avoid numerical issues, the pdf, cdf, and log versions thereof may still exhibit numerical instability. They are relatively stable near the tails; however near the mode they are unstable if total_count is greater than about 75 for tf$float64$, 25 for tf$float32$, and 7 for tf$float16$. Beyond these limits a warning will be shown if validate_args=FALSE; otherwise an exception is thrown. For high total_count, consider using a Normal approximation.
Usage

tfd_bates(
    total_count,
    low = 0,
    high = 1,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Bates"
)

Arguments

total_count  Non-negative integer-valued Tensor with shape broadcastable to the batch shape
[N1,...,Nm], m >= 0. This controls the number of samples of Uniform(low,high)
to take the mean of.

low          Floating point Tensor representing the lower bounds of the support. Should be
broadcastable to [N1,...,Nm] with m >= 0, the same dtype as total_count, and
low < high component-wise, after broadcasting. Defaults to 0.

high         Floating point Tensor representing the upper bounds of the support. Should be
broadcastable to [N1,...,Nm] with m >= 0, the same dtype as total_count, and
low < high component-wise, after broadcasting. Defaults to 1.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for
validity despite possibly degrading runtime performance. When FALSE invalid
inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic’s batch members are undefined.

name         name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is supported in the interval [low, high]. If [low, high] is the
unit interval [0, 1], the pdf is,

\[ \text{pdf}(x; n, 0, 1) = \frac{(n / (n-1)!) \sum_{k=0}^{j} (-1)^k \binom{n}{k} (nx - k)^{n-1}}{n!} \]

where

- \( \text{total_count} = n \)
- \( j = \text{floor}(nx) \)
- \( n! \) is the factorial of \( n \)
- \( \binom{n}{k} \) is the binomial coefficient \( n! / (k!(n - k)!). \)

For arbitrary intervals [low, high], the pdf is,

\[ \text{pdf}(x; n, \text{low}, \text{high}) = \text{pdf}(x - \text{low}) / (\text{high} - \text{low}); n, 0, 1) / (\text{high} - \text{low}) \]
Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


tfd_bernoulli  Bernoulli distribution

Description

The Bernoulli distribution with `probs` parameter, i.e., the probability of a 1 outcome (vs a 0 outcome).

Usage

tfd_bernoulli(
    logits = NULL,
    probs = NULL,
    dtype = tf$int32,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Bernoulli"
)
Arguments

logits  
An N-D Tensor representing the log-odds of a 1 event. Each entry in the Tensor  
parametrizes an independent Bernoulli distribution where the probability of an  
event is sigmoid(logits). Only one of logits or probs should be passed in.

probs  
An N-D Tensor representing the probability of a 1 event. Each entry in the  
Tensor parameterizes an independent Bernoulli distribution. Only one of logits  
or probs should be passed in.

dtype  
The type of the event samples. Default: int32.

validate_args  
Logical, default FALSE. When TRUE distribution parameters are checked for  
validity despite possibly degrading runtime performance. When FALSE invalid  
inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use  
the value NaN to indicate the result is undefined. When FALSE, an exception is  
raised if one or more of the statistic’s batch members are undefined.

name  
name prefixed to Ops created by this class.

Value  
a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions:  
tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_beta_binomial(),  
tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(),  
tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(),  
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),  
tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),  
tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),  
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),  
tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(),  
tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),  
tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space,  
tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_mixture(), tfd_mixture_same_family(),  
tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(),  
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),  
tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),  
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature,  
tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),  
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(),  
tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution,  
tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_variational_gaussian,  
tfd_vector_diffeomixture(), tfd_vector_exponential_diagonal(), tfd_vector_exponential_linear_operator(),  
tfd_vector_laplace_diagonal(), tfd_vector_laplace_linear_operator(), tfd_vector_sin_arcsinh_diagonal(),  
tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(),  
tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
Description

The Beta distribution is defined over the (0, 1) interval using parameters concentration1 (aka "alpha") and concentration0 (aka "beta").

Usage

tfd_beta(
    concentration1 = NULL,
    concentration0 = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Beta"
)

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>concentration1</td>
<td>Positive floating-point Tensor indicating mean number of successes; aka &quot;alpha&quot;. Implies self$dtype and self$batch_shape, i.e., concentration1$shape = [N1, N2, ..., Nm] = self$batch_shape.</td>
</tr>
<tr>
<td>concentration0</td>
<td>Positive floating-point Tensor indicating mean number of failures; aka &quot;beta&quot;. Otherwise has same semantics as concentration1.</td>
</tr>
<tr>
<td>validate_args</td>
<td>Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.</td>
</tr>
<tr>
<td>allow_nan_stats</td>
<td>Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.</td>
</tr>
<tr>
<td>name</td>
<td>name prefixed to Ops created by this class.</td>
</tr>
</tbody>
</table>

Details

Mathematical Details

The probability density function (pdf) is,

\[
pdf(x; \alpha, \beta) = x^{(\alpha - 1)} (1 - x)^{\beta - 1} / Z
\]

\[
Z = \frac{\Gamma(\alpha) \Gamma(\beta)}{\Gamma(\alpha + \beta)}
\]

where:

- concentration1 = alpha,
- concentration0 = beta,
- Z is the normalization constant, and,
Gamma is the gamma function. The concentration parameters represent mean total counts of a 1 or a 0, i.e.,

\[
\text{concentration}_1 = \alpha = \text{mean} \times \text{total_concentration} \\
\text{concentration}_0 = \beta = (1. - \text{mean}) \times \text{total_concentration}
\]

where mean in (0, 1) and total_concentration is a positive real number representing a mean total_count = concentration_1 + concentration_0. Distribution parameters are automatically broadcast in all functions; see examples for details. Warning: The samples can be zero due to finite precision. This happens more often when some of the concentrations are very small. Make sure to round the samples to \( \text{np}$.finfo(dtype)$tiny before computing the density. Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in the paper Michael Figurnov, Shakir Mohamed, Andriy Mnih. Implicit Reparameterization Gradients, 2018

Value

a distribution instance.

See Also

For usage examples see e.g. \( \text{tfd_sample}() \), \( \text{tfd_log_prob}() \), \( \text{tfd_mean}() \).

Other distributions: \( \text{tfd_autoregressive}() \), \( \text{tfd_batch_reshape}() \), \( \text{tfd_bates}() \), \( \text{tfd_bernoulli}() \), \( \text{tfd_beta}() \), \( \text{tfd_beta_binomial}() \), \( \text{tfd_binomial}() \), \( \text{tfd_categorical}() \), \( \text{tfd_cauchy}() \), \( \text{tfd_chi2}() \), \( \text{tfd_chi}() \), \( \text{tfd_cholesky_lkj}() \), \( \text{tfd_continuous_bernoulli}() \), \( \text{tfd_deterministic}() \), \( \text{tfd_dirichlet}() \), \( \text{tfd_dirichlet_multinomial}() \), \( \text{tfd_deterministic}() \), \( \text{tfd_empirical}() \), \( \text{tfd_exp_gamma}() \), \( \text{tfd_exp_inverse_gamma}() \), \( \text{tfd_exponential}() \), \( \text{tfd_finite}() \), \( \text{tfd_gamma}() \), \( \text{tfd_gamma_gamma}() \), \( \text{tfd_gaussian_process}() \), \( \text{tfd_gaussian_process_regression_model}() \), \( \text{tfd_gaussian_process_regression_field}() \), \( \text{tfd_half_cauchy}() \), \( \text{tfd_half_normal}() \), \( \text{tfd_hidden_markov_model}() \), \( \text{tfd_horseshoe}() \), \( \text{tfd_independent}() \), \( \text{tfd_inverse_gamma}() \), \( \text{tfd_inverse_gaussian}() \), \( \text{tfd_johnson_s_u}() \), \( \text{tfd_joint_distribution_named}() \), \( \text{tfd_joint_distribution_named_auto_batched}() \), \( \text{tfd_joint_distribution_sequential}() \), \( \text{tfd_joint_distribution_sequential_auto_batched}() \), \( \text{tfd_kumaraswamy}() \), \( \text{tfd_laplace}() \), \( \text{tfd_linear_gaussian_state_space_model}() \), \( \text{tfd_lkj}() \), \( \text{tfd_logistic}() \), \( \text{tfd_log_normal}() \), \( \text{tfd_logistic}() \), \( \text{tfd_mixtured_distribution}() \), \( \text{tfd_mixture}() \), \( \text{tfd_multinomial}() \), \( \text{tfd_multivariate_normal_diag_plus_low_rank}() \), \( \text{tfd_multivariate_normal_full_covariance}() \), \( \text{tfd_multivariate_normal_linear_operator}() \), \( \text{tfd_multivariate_normal_tri_l}() \), \( \text{tfd_multivariate_student_t_linear_operator}() \), \( \text{tfd_negative_binomial}() \), \( \text{tfd_normal}() \), \( \text{tfd_one_hot_categorical}() \), \( \text{tfd_pareto}() \), \( \text{tfd_pixel_cnn}() \), \( \text{tfd_poisson_log_normal_quadrature}() \), \( \text{tfd_poisson}() \), \( \text{tfd_power_spherical}() \), \( \text{tfd_probit_bernoulli}() \), \( \text{tfd_quantized}() \), \( \text{tfd_quantized_stochastic}() \), \( \text{tfd_relaxed_bernoulli}() \), \( \text{tfd_relaxed_one_hot_categorical}() \), \( \text{tfd_sample_distribution}() \), \( \text{tfd_sinh_arcsinh}() \), \( \text{tfd_spherical_uniform}() \), \( \text{tfd_student_t_process}() \), \( \text{tfd_transformed_distribution}() \), \( \text{tfd_triangular}() \), \( \text{tfd_truncated_cauchy}() \), \( \text{tfd_truncated_normal}() \), \( \text{tfd_uniform}() \), \( \text{tfd_von_mises_fisher}() \), \( \text{tfd_von_mises}() \), \( \text{tfd_weibull}() \), \( \text{tfd_wishart_linear_operator}() \), \( \text{tfd_wishart_tri_l}() \), \( \text{tfd_wishart}() \), \( \text{tfd_zipf}() \).
The Beta-Binomial distribution is parameterized by (a batch of) `total_count` parameters, the number of trials per draw from Binomial distributions where the probabilities of success per trial are drawn from underlying Beta distributions; the Beta distributions are parameterized by `concentration1` (aka 'alpha') and `concentration0` (aka 'beta'). Mathematically, it is (equivalent to) a special case of the Dirichlet-Multinomial over two classes, although the computational representation is slightly different: while the Beta-Binomial is a distribution over the number of successes in `total_count` trials, the two-class Dirichlet-Multinomial is a distribution over the number of successes and failures.

Usage

```python
  tfd_beta_binomial(
    total_count, concentration1, concentration0, validate_args = FALSE,
    allow_nan_stats = TRUE, name = "BetaBinomial"
  )
```

Arguments

- `total_count`: Non-negative integer-valued tensor, whose dtype is the same as `concentration1` and `concentration0`. The shape is broadcastable to `[N1, ..., Nm]` with `m >= 0`. When `total_count` is broadcast with `concentration1` and `concentration0`, it defines the distribution as a batch of `N1 x ... x Nm` different Beta-Binomial distributions. Its components should be equal to integer values.

- `concentration1`: Positive floating-point `Tensor` indicating mean number of successes. Specifically, the expected number of successes is `total_count * concentration1 / (concentration1 + concentration0)`.

- `concentration0`: Positive floating-point `Tensor` indicating mean number of failures; see description of `concentration1` for details.

- `validate_args`: Logical, default `FALSE`. When `TRUE` distribution parameters are checked for validity despite possibly degrading runtime performance. When `FALSE` invalid inputs may silently render incorrect outputs. Default value: `FALSE`.

- `allow_nan_stats`: Logical, default `TRUE`. When `TRUE`, statistics (e.g., mean, mode, variance) use the value `NaN` to indicate the result is undefined. When `FALSE`, an exception is raised if one or more of the statistic’s batch members are undefined.

- `name`: name prefixed to Ops created by this class.
Details

Mathematical Details

The Beta-Binomial is a distribution over the number of successes in total_count independent Binomial trials, with each trial having the same probability of success, the underlying probability being unknown but drawn from a Beta distribution with known parameters. The probability mass function (pmf) is,

$$\text{pmf}(k; n, a, b) = \frac{\text{Beta}(k + a, n - k + b)}{Z}$$

$$Z = \frac{(k! \ (n - k)! \ / \ n!)}{\text{Beta}(a, b)}$$

where:

- concentration1 = $a > 0$,
- concentration0 = $b > 0$,
- total_count = $n$, $a$ a positive integer,
- $n!$ is $n$ factorial,
- $\text{Beta}(x, y) = \Gamma(x) \Gamma(y) / \Gamma(x + y)$ is the beta function, and
- $\Gamma$ is the gamma function.

Dirichlet-Multinomial is a compound distribution, i.e., its samples are generated as follows.

1. Choose success probabilities: $\text{probs} \sim \text{Beta(\text{concentration1}, \text{concentration0})}$
2. Draw integers representing the number of successes: $\text{counts} \sim \text{Binomial(\text{total_count}, \text{probs})}$

Distribution parameters are automatically broadcast in all functions; see examples for details.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_multivariate_normal_tril(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature
Binomial distribution

This distribution is parameterized by `probs`, a (batch of) probabilities for drawing a 1 and `total_count`, the number of trials per draw from the Binomial.

**Usage**

```r
  tfd_binomial(
    total_count,
    logits = NULL,
    probs = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Beta"
  )
```

**Arguments**

- **total_count**: Non-negative floating point tensor with shape broadcastable to `[N1,..., Nm]` with `m >= 0` and the same dtype as `probs` or `logits`. Defines this as a batch of `N1 x ... x Nm` different Binomial distributions. Its components should be equal to integer values.
- **logits**: Floating point tensor representing the log-odds of a positive event with shape broadcastable to `[N1,..., Nm] m >= 0`, and the same dtype as `total_count`. Each entry represents logits for the probability of success for independent Binomial distributions. Only one of `logits` or `probs` should be passed in.
- **probs**: Positive floating point tensor with shape broadcastable to `[N1,..., Nm] m >= 0`, `probs` in `[0, 1]`. Each entry represents the probability of success for independent Binomial distributions. Only one of `logits` or `probs` should be passed in.
- **validate_args**: Logical, default `FALSE`. When `TRUE` distribution parameters are checked for validity despite possibly degrading runtime performance. When `FALSE` invalid inputs may silently render incorrect outputs. Default value: `FALSE`.

allow_nan_stats

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name

name prefixed to Ops created by this class.

Details

Mathematical Details

The Binomial is a distribution over the number of 1’s in total_count independent trials, with each trial having the same probability of 1, i.e., probs.

The probability mass function (pmf) is,

\[
\text{pmf}(k; \ n, p) = p^k (1 - p)^{(n - k)} / Z \\
Z = k! (n - k)! / n!
\]

where:

- total_count = n,
- probs = p,
- Z is the normalizing constant, and,
- n! is the factorial of n.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space(), tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixtures(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_tri_l(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(), tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(), tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(), tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(), tfd_tucker(), tfd_uniform(), tfd_vector_bernoulli(), tfd_vector_categorical(), tfd_vector_one_hot_categorical(), tfd_von_mises_fisher(), tfd_wishart_tril(), tfd_wishart(), tfd_zipf().
### tfd_blockwise

**Blockwise distribution**

#### Description
Blockwise distribution

#### Usage
```
tfd_blockwise(
  distributions,
  dtype_override = NULL,
  validate_args = FALSE,
  allow_nan_stats = FALSE,
  name = "Blockwise"
)
```

#### Arguments
- **distributions**: list of Distribution instances. All distribution instances must have the same batch_shape and all must have `event_ndims==1`, i.e., be vector-variate distributions.
- **dtype_override**: samples of distributions will be cast to this dtype. If unspecified, all distributions must have the same dtype. Default value: NULL (i.e., do not cast).
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: name prefixed to Ops created by this class.

#### Value
a distribution instance.

#### See Also
For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.
Description
The Categorical distribution is parameterized by either probabilities or log-probabilities of a set of K classes. It is defined over the integers \{0, 1, ..., K-1\}.

Usage
tfd_categorical(
  logits = NULL,
  probs = NULL,
  dtype = tf$int32,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Categorical"
)

Arguments
- **logits**: An N-D Tensor, \(N \geq 1\), representing the log probabilities of a set of Categorical distributions. The first \(N-1\) dimensions index into a batch of independent distributions and the last dimension represents a vector of logits for each class. Only one of logits or probs should be passed in.
- **probs**: An N-D Tensor, \(N \geq 1\), representing the probabilities of a set of Categorical distributions. The first \(N-1\) dimensions index into a batch of independent distributions and the last dimension represents a vector of probabilities for each class. Only one of logits or probs should be passed in.
- **dtype**: The type of the event samples (default: int32).
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details
The Categorical distribution is closely related to the OneHotCategorical and Multinomial distributions. The Categorical distribution can be intuited as generating samples according to \arg\max\{ OneHotCategorical(probs) \} itself being identical to \arg\max\{ Multinomial(probs, total_count=1) \}.

Mathematical Details
The probability mass function (pmf) is,
\[ \text{pmf}(k; \pi) = \prod_j \pi_j^{[k == j]} \]

**Pitfalls**

The number of classes, \( K \), must not exceed:

- the largest integer representable by `self.dtype`, i.e., \( 2^{(\text{mantissa_bits}+1)} \) (IEEE 754),
- the maximum Tensor index, i.e., \( 2^{31}-1 \).

Note: This condition is validated only when `validate_args = TRUE`.

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_cauchy()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gamma()`, `tfd_generalized_normal()`...

**tfd_cauchy**

Cauchy distribution with location \( \text{loc} \) and scale \( \text{scale} \)

**Description**

Mathematical details
tfd_cauchy

Usage

tfd_cauchy(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Cauchy"
)

Arguments

loc
Floating point tensor; the modes of the distribution(s).

scale
Floating point tensor; the locations of the distribution(s). Must contain only positive values.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

details

The probability density function (pdf) is,

\[
    \text{pdf}(x; \text{loc}, \text{scale}) = \frac{1}{\pi \text{scale} (1 + z^2)}
\]

where \( z = (x - \text{loc}) / \text{scale} \)

where \( \text{loc} \) is the location, and \( \text{scale} \) is the scale. The Cauchy distribution is a member of the location-scale family, i.e. \( Y \sim \text{Cauchy}(\text{loc}, \text{scale}) \) is equivalent to,

\[
    X \sim \text{Cauchy}(\text{loc}=0, \text{scale}=1)
\]

\[
    Y = \text{loc} + \text{scale} \times X
\]

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential().
tfd_cdf

Cumulative distribution function. Given random variable $X$, the cumulative distribution function $cdf$ is: $cdf(x) := P[X \leq x]$

Description

Cumulative distribution function. Given random variable $X$, the cumulative distribution function $cdf$ is: $cdf(x) := P[X \leq x]$

Usage

tfd_cdf(distribution, value, ...)

Arguments

distribution
The distribution being used.
value
float or double Tensor.
...
Additional parameters passed to Python.

Value

a Tensor of shape sample_shape(x) + self$batch_shape with values of type self$dtype.

See Also

Other distribution methods: tfd_covariance(), tfd_cross_entropy(), tfd_entropy(), tfd_kl_divergence(), tfd_log_cdf(), tfd_log_prob(), tfd_log_survival_function(), tfd_mean(), tfd_mode(), tfd_prob(), tfd_quantile(), tfd_sample(), tfd_stddev(), tfd_survival_function(), tfd_variance()
Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
x <- d %>% tfd_sample()
d %>% tfd_cdf(x)

Chi distribution

Description

The Chi distribution is defined over nonnegative real numbers and uses a degrees of freedom ("df")
parameter.

Usage

tfd_chis(df, validate_args = FALSE, allow_nan_stats = TRUE, name = "Chi")

Arguments

df Floating point tensor, the degrees of freedom of the distribution(s). df must
contain only positive values.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for
validity despite possibly degrading runtime performance. When FALSE invalid
inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic`s batch members are undefined.
name name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

dpdf(x; df, x >= 0) = x**(df - 1) exp(-0.5 x**2) / Z
Z = 2**(0.5 df - 1) Gamma(0.5 df)

where:

• df denotes the degrees of freedom,
• Z is the normalization constant, and,
• Gamma is the gamma function.

The Chi distribution is a transformation of the Chi2 distribution; it is the distribution of the positive
square root of a variable obeying a Chi distribution.
The Chi2 distribution is defined over positive real numbers using a degrees of freedom ("df") parameter.

Usage

tfd_chi2(df, validate_args = FALSE, allow_nan_stats = TRUE, name = "Chi2")

Arguments

df Floating point tensor, the degrees of freedom of the distribution(s). df must contain only positive values.
validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
Mathematical Details
The probability density function (pdf) is,

\[
pdf(x; \text{df}, x > 0) = x^{(0.5 \text{df} - 1)} \exp(-0.5 x) / Z
\]

\[
Z = 2^{(0.5 \text{df})} \Gamma(0.5 \text{df})
\]

where

- \text{df} denotes the degrees of freedom,
- \text{Z} is the normalization constant, and,
- \Gamma is the gamma function. The Chi2 distribution is a special case of the Gamma distribution, i.e.,

\[
\text{Chi2}(\text{df}) = \Gamma(\text{concentration}=0.5 \times \text{df}, \text{rate}=0.5)
\]

Value
a distribution instance.

See Also
For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batchreshape(), tfd_bates(), tfd_bernoulli(),
tfd_binomial(), tfd_binvbinomial(), tfd_categorical(), tfd_cauchy(), tfd_chi(),
tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(),
tfd_dirichlet_multinomial(), tfd_dirichlet_lkj(), tfd_dirichlet_multinomial(),
tfddirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gamma(),
tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(),
tfd_half_normal(), tfd_hidden_markov(), tfd_horseshoe(), tfd_bernoulli(),
tfd_inverse_gaussian(), tfd_inverse_gaussian(), tfd_johnson(),
tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named_auto_batched(),
tfd_joint_distribution_named_num_dense(), tfd_joint_distribution_named_auto_batched(),
tfd_kumaraswamy(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space(),
tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture(),
tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(),
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_normal_tril(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal,
tfd_cholesky_lkj

The CholeskyLKJ distribution on cholesky factors of correlation matrices

Description

This is a one-parameter family of distributions on cholesky factors of correlation matrices. In other words, if \( X \sim \text{CholeskyLKJ}(c) \), then \( X @ X^T \sim \text{LKJ}(c) \). For more details on the LKJ distribution, see `tfd_lkj`.

Usage

```r
tfd_cholesky_lkj(
  dimension,
  concentration,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "CholeskyLKJ"
)
```

Arguments

- `dimension` integer. The dimension of the correlation matrices to sample.
- `concentration` float or double Tensor. The positive concentration parameter of the CholeskyLKJ distributions.
- `validate_args` Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- `allow_nan_stats` Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- `name` name prefixed to Ops created by this class.

Value

- a distribution instance.
Continuous Bernoulli distribution.

This distribution is parameterized by probs, a (batch of) parameters taking values in (0, 1). Note that, unlike in the Bernoulli case, probs does not correspond to a probability, but the same name is used due to the similarity with the Bernoulli.

Usage

tfd_continuous_bernoulli(
  logits = NULL,
  probs = NULL,
  dtype = tf$float32,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "ContinuousBernoulli"
)
Arguments

logits
An N-D Tensor. Each entry in the Tensor parameterizes an independent continuous Bernoulli distribution with parameter sigmoid(logits). Only one of logits or probs should be passed in. Note that this does not correspond to the log-odds as in the Bernoulli case.

probs
An N-D Tensor representing the parameter of a continuous Bernoulli. Each entry in the Tensor parameterizes an independent continuous Bernoulli distribution. Only one of logits or probs should be passed in. Note that this also does not correspond to a probability as in the Bernoulli case.

dtype
The type of the event samples. Default: float32.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

Mathematical Details

The continuous Bernoulli is a distribution over the interval [0, 1], parameterized by probs in (0, 1). The probability density function (pdf) is,

\[
p(df(x; \text{probs}) = \text{probs}^x \times (1 - \text{probs})^{1 - x} \times C(\text{probs})
\]

\[
C(\text{probs}) = \begin{cases} 
2 \times \text{atanh}(1 - 2 \times \text{probs}) / (1 - 2 \times \text{probs}) & \text{if } \text{probs} \neq 0.5 \\
2 & \text{else}
\end{cases}
\]

While the normalizing constant \(C(\text{probs})\) is a continuous function of \(\text{probs}\) (even at \(\text{probs} = 0.5\)), computing it at values close to 0.5 can result in numerical instabilities due to 0/0 errors. A Taylor approximation of \(C(\text{probs})\) is thus used for values of \(\text{probs}\) in a small interval \([\text{lims}[0], \text{lims}[1]]\) around 0.5. For more details, see Loaiza-Ganem and Cunningham (2019). NOTE: Unlike the Bernoulli, numerical instabilities can happen for \(\text{probs}\) very close to 0 or 1. Current implementation allows any value in (0, 1), but this could be changed to (1e-6, 1-1e-6) to avoid these issues.

Value

a distribution instance.

References

tfd_covariance

Covariance.

Description

Covariance is (possibly) defined only for non-scalar-event distributions. For example, for a length-k, vector-valued distribution, it is calculated as, Cov[i,j] = Covariance(X_i, X_j) = E[(X_i - E[X_i])(X_j - E[X_j])] where Cov is a (batch of) k x k matrix, 0 <= (i, j) < k, and E denotes expectation.

Usage

tfd_covariance(distribution, ...)

Arguments

distribution The distribution being used.

... Additional parameters passed to Python.
Details

Alternatively, for non-vector, multivariate distributions (e.g., matrix-valued, Wishart), Covariance shall return a (batch of) matrices under some vectorization of the events, i.e., Cov[i, j] = Covariance(Vec(X)_i, Vec(X)_j) = [as above] where Cov is a (batch of) k x k matrices, 0 <= (i, j) < k = reduce_prod(event_shape), and Vec is some function mapping indices of this distribution’s event dimensions to indices of a length-k vector.

Value

Floating-point Tensor with shape [B1, ..., Bn, k, k] where the first n dimensions are batch coordinates and k = reduce_prod(self.event_shape).

See Also

Other distribution methods: tfd_cdf(), tfd_cross_entropy(), tfd_entropy(), tfd_kl_divergence(), tfd_log_cdf(), tfd_log_prob(), tfd_log_survival_function(), tfd_mean(), tfd_mode(), tfd_prob(), tfd_quantile(), tfd_sample(), tfd_stddev(), tfd_survival_function(), tfd_variance()

Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_variance()

tfd_cross_entropy

Computes the (Shannon) cross entropy.

Description

Denote this distribution (self) by P and the other distribution by Q. Assuming P, Q are absolutely continuous with respect to one another and permit densities p(x) dr(x) and q(x) dr(x), (Shannon) cross entropy is defined as: H[P, Q] = E_p[-log q(X)] = -int_F p(x) log q(x) dr(x) where F denotes the support of the random variable X ~ P.

Usage

tfd_cross_entropy(distribution, other, name = "cross_entropy")

Arguments

distribution The distribution being used.
other tfp$Distributions$Distribution instance.
name String prepended to names of ops created by this function.
Value

cross_entropy: self.dtype Tensor with shape [B1, ..., Bn] representing n different calculations of (Shannon) cross entropy.

See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

Examples

d1 <- tfd_normal(loc = 1, scale = 1)
d2 <- tfd_normal(loc = 2, scale = 1)
d1 %>% tfd_cross_entropy(d2)

---

**tfd_deterministic**  
Scalar Deterministic distribution on the real line

Description

The scalar Deterministic distribution is parameterized by a (batch) point `loc` on the real line. The distribution is supported at this point only, and corresponds to a random variable that is constant, equal to `loc`. See Degenerate rv.

Usage

tfd_deterministic(
  loc,
  atol = NULL,
  rtol = NULL,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Deterministic"
)

Arguments

- **loc**: Numeric Tensor of shape [B1, ..., Bb], with b >= 0. The point (or batch of points) on which this distribution is supported.
- **atol**: Non-negative Tensor of same dtype as `loc` and broadcastable shape. The absolute tolerance for comparing closeness to `loc`. Default is 0.
- **rtol**: Non-negative Tensor of same dtype as `loc` and broadcastable shape. The relative tolerance for comparing closeness to `loc`. Default is 0.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.

Details

Mathematical Details

The probability mass function (pmf) and cumulative distribution function (cdf) are

\[
\text{pmf}(x; \text{loc}) = 1, \text{ if } x == \text{loc}, \text{ else } 0 \\
\text{cdf}(x; \text{loc}) = 1, \text{ if } x >= \text{loc}, \text{ else } 0
\]

Value

a distribution instance.

See Also

For usage examples see e.g. \texttt{tfd_sample()}, \texttt{tfd_log_prob()}, \texttt{tfd_mean()}. Other distributions: \texttt{tfd_autoregressive()}, \texttt{tfd_batch_reshape()}, \texttt{tfd_bates()}, \texttt{tfd_bernoulli()}, \texttt{tfd_beta_binomial()}, \texttt{tfd_beta()}, \texttt{tfd_binomial()}, \texttt{tfd_categorical()}, \texttt{tfd_cauchy()}, \texttt{tfd_chi2()}, \texttt{tfd_chi()}, \texttt{tfd_cholesky_lkj()}, \texttt{tfd_continuous_bernoulli()}, \texttt{tfd_dirichlet_multinomial()}, \texttt{tfd_dirichlet()}, \texttt{tfd_empirical()}, \texttt{tfd_exp_gamma()}, \texttt{tfd_exp_inverse_gamma()}, \texttt{tfd_exponential()}, \texttt{tfd_gamma_gamma()}, \texttt{tfd_gamma()}, \texttt{tfd_gaussian_process_regression_model()}, \texttt{tfd_gaussian_process()}, \texttt{tfd_generalized_normal()}, \texttt{tfd_geometric()}, \texttt{tfd_gumbel()}, \texttt{tfd_half_cauchy()}, \texttt{tfd_half_normal()}, \texttt{tfd_hidden_markov_model()}, \texttt{tfd_horseshoe()}, \texttt{tfd_independent()}, \texttt{tfd_inverse_gamma()}, \texttt{tfd_inverse_gaussian()}, \texttt{tfd_johnson_s_u()}, \texttt{tfd_joint_distribution_named_auto_batched()}, \texttt{tfd_joint_distribution_named_sequence_auto_batched()}, \texttt{tfd_joint_distribution_sequence_auto_batched()}, \texttt{tfd_kumaraswamy()}, \texttt{tfd_kumaraswamy()}, \texttt{tfd_laplace()}, \texttt{tfd_linear_gaussian_state_space_model()}, \texttt{tfd_lkj()}, \texttt{tfd_logistic()}, \texttt{tfd_log_normal()}, \texttt{tfd_lognormal()}, \texttt{tfd_mixture_same_family()}, \texttt{tfd_mixture_normal_diag_plus_low_rank()}, \texttt{tfd_mixture_normal_diag()}, \texttt{tfd_mixture_normal_tril()}, \texttt{tfd_mixture_student_t_linear_operator()}, \texttt{tfd_multinomial()}, \texttt{tfd_normal()}, \texttt{tfd_one_hot_categorical()}, \texttt{tfd_pareto()}, \texttt{tfd_pixel_cnn()}, \texttt{tfd_poisson_log_normal_quadrature_compound()}, \texttt{tfd_poisson()}, \texttt{tfd_power_spherical()}, \texttt{tfd_probit_bernoulli()}, \texttt{tfd_quantized()}, \texttt{tfd_relaxed_bernoulli()}, \texttt{tfd_relaxed_one_hot_categorical()}, \texttt{tfd_sample_distribution()}, \texttt{tfd_sinh_arcsinh()}, \texttt{tfd_skellam()}, \texttt{tfd_spherical_uniform()}, \texttt{tfd_student_t_process()}, \texttt{tfd_student_t()}, \texttt{tfd_transformed_distribution()}, \texttt{tfd_triangular()}, \texttt{tfd_truncated_cauchy()}, \texttt{tfd_truncated_normal()}, \texttt{tfd_uniform()}, \texttt{tfd_variational_gaussian()}, \texttt{tfd_vector_diffeomixture()}, \texttt{tfd_vector_exponential_diag()}, \texttt{tfd_vector_exponential_linear_operator()}, \texttt{tfd_vector_laplace_diag()}, \texttt{tfd_vector_laplace_linear_operator()}, \texttt{tfd_vector_sin_arcsinh_diagonal()}, \texttt{tfd_von_mises_fisher()}, \texttt{tfd_von_mises()}, \texttt{tfd_weibull()}, \texttt{tfd_wishart_linear_operator()}, \texttt{tfd_wishart_tri_l()}, \texttt{tfd_wishart()}, \texttt{tfd_zipf()}
Description

The Dirichlet distribution is defined over the \((k-1)\)-simplex using a positive, length-\(k\) vector concentration \((k > 1)\). The Dirichlet is identically the Beta distribution when \(k = 2\).

Usage

tfd_dirichlet(
    concentration,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Dirichlet"
)

Arguments

- **concentration**: Positive floating-point Tensor indicating mean number of class occurrences; aka "alpha". Implies \(\text{self$dtype}\), \(\text{self$batch_shape}\), \(\text{self$event_shape}\), i.e., if concentration$shape = [N1, N2, ..., Nm, k] then batch_shape = [N1, N2, ..., Nm] and event_shape = [k].
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details

Mathematical Details

The Dirichlet is a distribution over the open \((k-1)\)-simplex, i.e.,

\[ S^{k-1} = \{ (x_0, \ldots, x_{k-1}) \in \mathbb{R}^k : \text{sum}_j x_j = 1 \text{ and all}_j x_j > 0 \} \]

The probability density function (pdf) is,

\[
\text{pdf}(x; \alpha) = \frac{\prod_j x_j^{\alpha_j - 1}}{Z}
\]

\[ Z = \frac{\prod_j \Gamma(\alpha_j)}{\Gamma(\text{sum}_j \alpha_j)} \]

where:

- \(x\) in \(S^{k-1}\), i.e., the \((k-1)\)-simplex,
concentration = alpha = [alpha_0, ..., alpha_{k-1}], alpha_j > 0

- Z is the normalization constant aka the multivariate beta function, and,
- Gamma is the gamma function.

The concentration represents mean total counts of class occurrence, i.e.,

concentration = alpha = mean * total_concentration

where mean in S^{k-1} and total_concentration is a positive real number representing a mean total count. Distribution parameters are automatically broadcast in all functions; see examples for details. Warning: Some components of the samples can be zero due to finite precision. This happens more often when some of the concentrations are very small. Make sure to round the samples to np.finfo(dtype).tiny before computing the density. Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in the paper Michael Figurnov, Shakir Mohamed, Andriy Mnih. Implicit Reparameterization Gradients, 2018

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
The Dirichlet-Multinomial distribution is parameterized by a (batch of) length-\(K\) concentration vectors \((K > 1)\) and a \(\text{total\_count}\) number of trials, i.e., the number of trials per draw from the DirichletMultinomial. It is defined over a (batch of) length-\(K\) vector counts such that \(\text{tf}\_\text{reduce\_sum}(\text{counts}, -1) = \text{total\_count}\). The Dirichlet-Multinomial is identically the Beta-Binomial distribution when \(K = 2\).

```r
f1234567890

Usage

tfd_dirichlet_multinomial(
  total_count,
  concentration,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "DirichletMultinomial"
)

Arguments

total_count Non-negative floating point tensor, whose dtype is the same as concentration. The shape is broadcastable to \([N1, ..., Nm]\) with \(m \geq 0\). Defines this as a batch of \(N1 \times ... \times Nm\) different Dirichlet multinomial distributions. Its components should be equal to integer values.

concentration Positive floating point tensor, whose dtype is the same as \(n\) with shape broadcastable to \([N1, ..., Nm, K]\) \(m \geq 0\). Defines this as a batch of \(N1 \times ... \times Nm\) different \(K\) class Dirichlet multinomial distributions.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.

Details

Mathematical Details

The Dirichlet-Multinomial is a distribution over \(K\)-class counts, i.e., a length-\(K\) vector of non-negative integer counts \(n = [n_0, ..., n_{(K-1)}]\).

The probability mass function (pmf) is,
pmf(n; alpha, N) = Beta(alpha + n) / (prod_j n_j!) / Z
Z = Beta(alpha) / N!

where:
- concentration = alpha = [alpha_0, ..., alpha_{K-1}], alpha_j > 0,
- total_count = N, N a positive integer,
- N! is N factorial, and,
- Beta(x) = prod_j Gamma(x_j) / Gamma(sum_j x_j) is the multivariate beta function, and,
- Gamma is the gamma function.

Dirichlet-Multinomial is a compound distribution, i.e., its samples are generated as follows.
1. Choose class probabilities: probs = [p_0,...,p_{K-1}] ~ Dir(concentration)
2. Draw integers: counts = [n_0,...,n_{K-1}] ~ Multinomial(total_count, probs)

The last concentration dimension parametrizes a single Dirichlet-Multinomial distribution. When calling distribution functions (e.g., dist$prob(counts)), concentration, total_count and counts are broadcast to the same shape. The last dimension of counts corresponds single Dirichlet-Multinomial distributions. Distribution parameters are automatically broadcast in all functions; see examples for details.

Pitfalls The number of classes, K, must not exceed:
- the largest integer representable by self$dtype, i.e., 2**(mantissa_bits+1) (IEE754),
- the maximum Tensor index, i.e., 2**31-1.

Note: This condition is validated only when validate_args = TRUE.

Value
a distribution instance.

See Also
For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space(), tfd_lkj(), tfd_log_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_multipartnormal(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature,
tfd_doublesided_maxwell

Double-sided Maxwell distribution.

Description

This distribution is useful to compute measure valued derivatives for Gaussian distributions. See Mohamed et al. (2019) for more details.

Usage

tfd_doublesided_maxwell(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "doublesided_maxwell"
)

Arguments

loc
    Floating point tensor; location of the distribution

scale
    Floating point tensor; the scales of the distribution. Must contain only positive values.

validate_args
    Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
    Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
    string prefixed to Ops created by this class. Default value: ‘doublesided_maxwell’.
Details

Mathematical details

The double-sided Maxwell distribution generalizes the Maxwell distribution to the entire real line.

\[ \text{pdf}(x; \mu, \sigma) = \frac{1}{\sigma \sqrt{2 \pi}} \left(\frac{x-\mu}{\sigma}\right)^2 \exp\left(-0.5 \left(\frac{x-\mu}{\sigma}\right)^2\right) \]

where \( \text{loc} = \mu \) and \( \text{scale} = \sigma \). The DoublesidedMaxwell distribution is a member of the location-scale family, i.e., it can be constructed as,

\[ X \sim \text{DoublesidedMaxwell}(\text{loc}=0, \text{scale}=1) \]
\[ Y = \text{loc} + \text{scale} \times X \]

The double-sided Maxwell is a symmetric distribution that extends the one-sided maxwell from \( \mathbb{R}^+ \) to the entire real line. Their densities are therefore the same up to a factor of 0.5.

It has several methods for generating random variates from it. The version here uses 3 Gaussian variates and a uniform variate to generate the samples The sampling path is:

\( \mu + \sigma\times \text{sgn}(U-0.5)\times \sqrt{X^2 + Y^2 + Z^2} \), \( U \sim \text{Unif} \); \( X,Y,Z \sim \mathcal{N}(0,1) \)

In the sampling process above, the random variates generated by \( \sqrt{X^2 + Y^2 + Z^2} \) are samples from the one-sided Maxwell (or Maxwell-Boltzmann) distribution.

Value

a distribution instance.

References

- Mohamed, et all, "Monte Carlo Gradient Estimation in Machine Learning.", 2019

See Also

For usage examples see e.g. \texttt{tfd_sample()}, \texttt{tfd_log_prob()}, \texttt{tfd_mean()}.

---

tfd_empirical

**Empirical distribution**

Description

The Empirical distribution is parameterized by a (batch) multiset of samples. It describes the empirical measure (observations) of a variable. Note: some methods (log_prob, prob, cdf, mode, entropy) are not differentiable with regard to samples.
tfd_empirical

Usage
tfd_empirical(
samples,
  event_ndims = 0,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Empirical"
)

Arguments

samples        Numeric Tensor of shape [B1, ..., Bk, S, E1, ..., En], k, n >= 0. Samples or batches of samples on which the distribution is based. The first k dimensions index into a batch of independent distributions. Length of S dimension determines number of samples in each multiset. The last n dimension represents samples for each distribution. n is specified by argument event_ndims.

event_ndims    int32, default 0, number of dimensions for each event. When 0 this distribution has scalar samples. When 1 this distribution has vector-like samples.

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name           name prefixed to Ops created by this class.

Details

Mathematical Details
The probability mass function (pmf) and cumulative distribution function (cdf) are

\[ \text{pmf}(k; s_1, \ldots, s_n) = \sum_i I(k)^{k == s_i} / n \]
\[ I(k)^{k == s_i} = 1, \text{if k == s_i, else 0}. \]
\[ \text{cdf}(k; s_1, \ldots, s_n) = \sum_i I(k)^{k >= s_i} / n \]
\[ I(k)^{k >= s_i} = 1, \text{if k >= s_i, else 0}. \]

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_entropy

Shannon entropy in nats.

Description
Shannon entropy in nats.

Usage

tfd_entropy(distribution, ...)

Arguments

distribution  The distribution being used.
...           Additional parameters passed to Python.

Value

a Tensor of shape sample_shape(x) + self$batch_shape with values of type self$dtype.

See Also

Other distribution_methods: tfd_cdf(), tfd_covariance(), tfd_cross_entropy(), tfd_kl_divergence(),
tfd_log_cdf(), tfd_log_prob(), tfd_log_survival_function(), tfd_mean(), tfd_mode(),
tfd_prob(), tfd_quantile(), tfd_sample(), tfd_stddev(), tfd_survival_function(), tfd_variance()
Examples

```r
d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_entropy()
```

---

**tfd_exponential  Exponential distribution**

**Description**

The Exponential distribution is parameterized by an event rate parameter.

**Usage**

```r
tfd_exponential(
  rate,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Exponential"
)
```

**Arguments**

- `rate`  Floating point tensor, equivalent to 1 / mean. Must contain only positive values.
- `validate_args`  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- `allow_nan_stats`  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- `name`  name prefixed to Ops created by this class.

**Details**

Mathematical Details

The probability density function (pdf) is,

\[
\text{pdf}(x; \lambda, x > 0) = \exp(-\lambda x) / Z
\]

\[
Z = 1 / \lambda
\]

where rate = lambda and Z is the normalizing constant.

The Exponential distribution is a special case of the Gamma distribution, i.e.,

Exponential(rate) = Gamma(concentration=1., rate)
The Exponential distribution uses a rate parameter, or "inverse scale", which can be intuited as,

\[ X \sim \text{Exponential}(\text{rate}=1) \]
\[ Y = \frac{X}{\text{rate}} \]

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`,
`tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`,
`tfd_chi()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet()`,
`tfd_dirichlet_multinomial()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_gamma()`,
`tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`, `tfd_generalized_normal()`,
`tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`, `tfd_hidden_markov_model()`,
`tfd_horseshoe()`, `tfd_independent()`, `tfd_inverse_gamma()`, `tfd_inverse_gaussian()`, `tfd_johnson_s_u()`,
`tfd_joint_distribution_named_auto_batched()`, `tfd_joint_distribution_named()`, `tfd_joint_distribution_sequential()`,
`tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`,
`tfd_lkj()`, `tfd_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_mixture_same_family()`,
`tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal_diag()`,
`tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`,
`tfd_multiplicative_normal_tril()`, `tfd_multiplicative_student_t_linear_operator()`, `tfd_negative_binomial()`,
`tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_variational_distribution()`,
`tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`,
`tfd_relaxed_one_hot_categorical()`, `tfd_sample_distribution()`, `tfd_sinh_arcsinh()`,
`tfd_skellam()`, `tfd_spherical_uniform()`, `tfd_student_t_process()`, `tfd_student_t()`, `tfd_transformed_distribution()`,
`tfd_triangular()`, `tfd_truncated_cauchy()`, `tfd_truncated_normal()`, `tfd_uniform()`, `tfd_von_mises()`,
`tfd_vector_diffeomixture()`, `tfd_vector_exponential_diag()`, `tfd_vector_exponential_linear_operator()`,
`tfd_vector_laplace_diag()`, `tfd_vector_laplace_linear_operator()`, `tfd_vector_sinh_arcsinh_diag()`,
`tfd_von_mises_fisher()`, `tfd_von_mises()`, `tfd_weibull()`, `tfd_wishart_linear_operator()`,
`tfd_wishart_tril()`, `tfd_wishart()`, `tfd_zipf()`

Description

The ExpGamma distribution is defined over the real line using parameters concentration (aka "alpha") and rate (aka "beta"). This distribution is a transformation of the Gamma distribution such that \( X \sim \text{ExpGamma}(\cdot) \Rightarrow \exp(X) \sim \text{Gamma}(\cdot) \).
**tfd_exp_gamma**

**Usage**

```python
tfd_exp_gamma(
    concentration,
    rate = NULL,
    log_rate = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "ExpGamma"
)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>concentration</td>
<td>Floating point tensor, the concentration params of the distribution(s). Must contain only positive values.</td>
</tr>
<tr>
<td>rate</td>
<td>Floating point tensor, the inverse scale params of the distribution(s). Must contain only positive values. Mutually exclusive with log_rate.</td>
</tr>
<tr>
<td>log_rate</td>
<td>Floating point tensor, natural logarithm of the inverse scale params of the distribution(s). Mutually exclusive with rate.</td>
</tr>
<tr>
<td>validate_args</td>
<td>Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.</td>
</tr>
<tr>
<td>allow_nan_stats</td>
<td>Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.</td>
</tr>
<tr>
<td>name</td>
<td>name prefixed to Ops created by this class.</td>
</tr>
</tbody>
</table>

**Details**

**Mathematical Details**

The probability density function (pdf) can be derived from the change of variables rule (since the distribution is logically equivalent to tfb_log()(tfd_gamma(..))):

\[
pdf(x; \alpha, \beta > 0) = \exp(x)^{\alpha - 1} \exp(-\exp(x) \beta) / Z + x
\]

\[
Z = \text{Gamma}(\alpha) \beta^{-\alpha}
\]

where:

- concentration = alpha, alpha > 0,
- rate = beta, beta > 0,
- Z is the normalizing constant of the corresponding Gamma distribution, and
- Gamma is the **gamma function**.

The cumulative density function (cdf) is,

\[
cdf(x; \alpha, \beta, x) = \text{GammaInc}(\alpha, \beta \exp(x)) / \text{Gamma}(\alpha)
\]
where GammaInc is the lower incomplete Gamma function.

Distribution parameters are automatically broadcast in all functions. Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in Figurnov et al., 2018.

Value

A distribution instance.

References


See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_log_probs(), tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadtree(), tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(), tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(), tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(), tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_variational_gaussian_process(), tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(), tfd_vector_laplace_diag(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh_diag(), tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(), tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()

tfd_exp_inverse_gamma  ExpInverseGamma distribution.

Description

The ExpInverseGamma distribution is defined over the real numbers such that X ~ ExpInverseGamma(.) => exp(X) ~ InverseGamma(.). The distribution is logically equivalent to tfb_log()(tfd_inverse_gamma(.)), but can be sampled with much better precision.
Usage

tfd_exp_inverse_gamma(
    concentration,
    scale = NULL,
    log_scale = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "ExpGamma"
)

Arguments

concentration  Floating point tensor, the concentration params of the distribution(s). Must contain only positive values.

scale  Floating point tensor, the scale params of the distribution(s). Must contain only positive values. Mutually exclusive with log_scale.

log_scale  Floating point tensor, the natural logarithm of the scale params of the distribution(s). Mutually exclusive with scale.

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name  name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is very similar to ExpGamma,

\[
pdf(x; \alpha, \beta > 0) = \exp(-x)^{\alpha-1} \exp(-\exp(-x) \beta) / Z - x
\]

\[
Z = \text{Gamma}(\alpha) \beta^{-\alpha}
\]

where:

- concentration = \alpha,
- scale = \beta,
- Z is the normalizing constant, and,
- Gamma is the gamma function.

The cumulative density function (cdf) is,

\[
cdf(x; \alpha, \beta, x) = 1 - \text{GammaInc}(\alpha, \beta \exp(-x)) / \text{Gamma}(\alpha)
\]
where \( \Gamma_{\text{Inc}} \) is the \textit{upper incomplete Gamma function}.

Distribution parameters are automatically broadcast in all functions. Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in Figurnov et al, 2018.

**Value**

A distribution instance.

**References**


**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Description

ExpRelaxedOneHotCategorical distribution with temperature and logits.

Usage

tfd_exp_relaxed_one_hot_categorical(
    temperature,
    logits = NULL,
    probs = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "ExpRelaxedOneHotCategorical"
)

Arguments

temperature An 0-D Tensor, representing the temperature of a set of ExpRelaxedCategorical distributions. The temperature should be positive.

logits An N-D Tensor, N >= 1, representing the log probabilities of a set of ExpRelaxedCategorical distributions. The first N - 1 dimensions index into a batch of independent distributions and the last dimension represents a vector of logits for each class. Only one of logits or probs should be passed in.

probs An N-D Tensor, N >= 1, representing the probabilities of a set of ExpRelaxedCategorical distributions. The first N - 1 dimensions index into a batch of independent distributions and the last dimension represents a vector of probabilities for each class. Only one of logits or probs should be passed in.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
tfd_finite_discrete  

The finite discrete distribution.

Description

The FiniteDiscrete distribution is parameterized by either probabilities or log-probabilities of a set of \( K \) possible outcomes, which is defined by a strictly ascending list of \( K \) values.

Usage

```r
  tfd_finite_discrete(
    outcomes, 
    logits = NULL, 
    probs = NULL, 
    rtol = NULL, 
    atol = NULL, 
    validate_args = FALSE, 
    allow_nan_stats = TRUE, 
    name = "FiniteDiscrete"
  )
```

Arguments

- **outcomes**: A 1-D floating or integer Tensor, representing a list of possible outcomes in strictly ascending order.
- **logits**: A floating N-D Tensor, \( N \geq 1 \), representing the log probabilities of a set of FiniteDiscrete distributions. The first \( N - 1 \) dimensions index into a batch of independent distributions and the last dimension represents a vector of logits for each discrete value. Only one of logits or probs should be passed in.
- **probs**: A floating N-D Tensor, \( N \geq 1 \), representing the probabilities of a set of FiniteDiscrete distributions. The first \( N - 1 \) dimensions index into a batch of independent distributions and the last dimension represents a vector of probabilities for each discrete value. Only one of logits or probs should be passed in.
- **rtol**: Tensor with same dtype as outcomes. The relative tolerance for floating number comparison. Only effective when outcomes is a floating Tensor. Default is \( 10 \times \text{eps} \).
- **atol**: Tensor with same dtype as outcomes. The absolute tolerance for floating number comparison. Only effective when outcomes is a floating Tensor. Default is \( 10 \times \text{eps} \).
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
tfd_gamma

name string prefixed to Ops created by this class.

Details

Note: log_prob, prob, cdf, mode, and entropy are differentiable with respect to logits or probs but not with respect to outcomes.

Mathematical Details

The probability mass function (pmf) is,

$$pmf(x; \mathbf{pi}, \mathbf{qi}) = \prod_j \mathbf{pi}_j^{[x == \mathbf{qi}_j]}$$

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_gamma

**Gamma distribution**

Description

The Gamma distribution is defined over positive real numbers using parameters concentration (aka "alpha") and rate (aka "beta").

Usage

```r
  tfd_gamma(
    concentration,
    rate,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Gamma"  
  )
```

Arguments

- **concentration**: Floating point tensor, the concentration params of the distribution(s). Must contain only positive values.
- **rate**: Floating point tensor, the inverse scale params of the distribution(s). Must contain only positive values.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
pdf(x; \alpha, \beta, x > 0) = x^{\alpha - 1} \exp(-x \beta) / Z
\]

\[
Z = \Gamma(\alpha) \beta^{-\alpha}
\]

where

- concentration = \alpha, \alpha > 0,
- rate = \beta, \beta > 0,
- \Gamma is the normalizing constant, and,
- \Gamma is the gamma function.

The cumulative density function (cdf) is,

\[
cdf(x; \alpha, \beta, x > 0) = \Gamma(\alpha, \beta x) / \Gamma(\alpha)
\]

where \Gamma is the lower incomplete Gamma function. The parameters can be intuited via their relationship to mean and stddev,

\[
\text{concentration} = \alpha = (\text{mean} / \text{stddev})**2
\]
\[
\text{rate} = \beta = \text{mean} / \text{stddev}**2 = \text{concentration} / \text{mean}
\]

Distribution parameters are automatically broadcast in all functions; see examples for details.

Warning: The samples of this distribution are always non-negative. However, the samples that are smaller than \text{npfinfo(dtype)}$\text{tiny}$ are rounded to this value, so it appears more often than it should. This should only be noticeable when the concentration is very small, or the rate is very large. See note in \text{tf}\$\text{random.gamma}$ docstring. Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in the paper Michael Figurnov, Shakir Mohamed, Andriy Mnih. Implicit Reparameterization Gradients, 2018

Value

a distribution instance.
**tfd_gamma_gamma**  

**Description**

Gamma-Gamma is a **compound distribution** defined over positive real numbers using parameters concentration, mixing_concentration and mixing_rate.

**Usage**

```python
  tfd_gamma_gamma(  
    concentration,  
    mixing_concentration,  
    mixing_rate,  
    validate_args = FALSE,  
    allow_nan_stats = TRUE,  
    name = "GammaGamma"
  )
```
Arguments

- **concentration**: Floating point tensor, the concentration params of the distribution(s). Must contain only positive values.
- **mixing_concentration**: Floating point tensor, the concentration params of the mixing Gamma distribution(s). Must contain only positive values.
- **mixing_rate**: Floating point tensor, the rate params of the mixing Gamma distribution(s). Must contain only positive values.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details

This distribution is also referred to as the beta of the second kind (B2), and can be useful for transaction value modeling, as in Fader and Hardi, 2013.

Mathematical Details

It is derived from the following Gamma-Gamma hierarchical model by integrating out the random variable beta.

\[
\begin{align*}
\text{beta} & \sim \text{Gamma}(\alpha_0, \beta_0) \\
X | \text{beta} & \sim \text{Gamma}(\alpha, \beta)
\end{align*}
\]

where

- concentration = \( \alpha \)
- mixing_concentration = \( \alpha_0 \)
- mixing_rate = \( \beta_0 \)

The probability density function (pdf) is

\[
\text{pdf}(x; \alpha, \alpha_0, \beta_0) = Z \times (x + \beta_0)^{\alpha + \alpha_0}
\]

where the normalizing constant \( Z = \text{Beta}(\alpha, \alpha_0) \times \beta_0^{\alpha_0} \). Samples of this distribution are reparameterized as samples of the Gamma distribution are reparameterized using the technique described in (Figurnov et al., 2018).

@section References:

Marginal distribution of a Gaussian process at finitely many points.

Description

A Gaussian process (GP) is an indexed collection of random variables, any finite collection of which are jointly Gaussian. While this definition applies to finite index sets, it is typically implicit that the index set is infinite; in applications, it is often some finite dimensional real or complex vector space. In such cases, the GP may be thought of as a distribution over (real- or complex-valued) functions defined over the index set.

Usage

```python
tfd_gaussian_process(
    kernel,
    index_points,
    mean_fn = NULL,
)```
observation_noise_variance = 0,
jitter = 1e-06,
validate_args = FALSE,
allow_nan_stats = FALSE,
name = "GaussianProcess"
}

Arguments

**kernel**
PositiveSemidefiniteKernel-like instance representing the GP’s covariance function.

**index_points**
float Tensor representing finite (batch of) vector(s) of points in the index set over which the GP is defined. Shape has the form \([b1, ..., bB, e1, f1, ..., fF]\) where \(F\) is the number of feature dimensions and must equal \(\text{kernel.feature_ndims}\) and \(e1\) is the number (size) of index points in each batch (we denote it \(e1\) to distinguish it from the number of inducing index points, denoted \(e2\) below). Ultimately the GaussianProcess distribution corresponds to an \(e1\)-dimensional multivariate normal. The batch shape must be broadcastable with \(\text{kernel.batch_shape}\), the batch shape of \(\text{inducing_index_points}\), and any batch dims yielded by \(\text{mean_fn}\).

**mean_fn**
function that acts on index points to produce a (batch of) vector(s) of mean values at those index points. Takes a Tensor of shape \([b1, ..., bB, f1, ..., fF]\) and returns a Tensor whose shape is (broadcastable with) \([b1, ..., bB]\). Default value: NULL implies constant zero function.

**observation_noise_variance**
float Tensor representing the variance of the noise in the Normal likelihood distribution of the model. May be batched, in which case the batch shape must be broadcastable with the shapes of all other batched parameters (\(\text{kernel.batch_shape}\), \(\text{index_points}\), etc.). Default value: 0.

**jitter**
float scalar Tensor added to the diagonal of the covariance matrix to ensure positive definiteness of the covariance matrix. Default value: 1e-6.

**validate_args**
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

**allow_nan_stats**
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

**name**
name prefixed to Ops created by this class.

Details

Just as Gaussian distributions are fully specified by their first and second moments, a Gaussian process can be completely specified by a mean and covariance function. Let \(S\) denote the index set and \(\mathcal{K}\) the space in which each indexed random variable takes its values (again, often \(\mathbb{R}\) or \(\mathbb{C}\)). The mean function is then a map \(m: S \to \mathcal{K}\), and the covariance function, or kernel, is a positive-definite
function $k: (S \times S) \rightarrow K$. The properties of functions drawn from a GP are entirely dictated (up to translation) by the form of the kernel function.

This Distribution represents the marginal joint distribution over function values at a given finite collection of points $[x[1], ..., x[N]]$ from the index set $S$. By definition, this marginal distribution is just a multivariate normal distribution, whose mean is given by the vector $[m(x[1]), ..., m(x[N])]$ and whose covariance matrix is constructed from pairwise applications of the kernel function to the given inputs:

$$
\begin{bmatrix}
  k(x[1], x[1]) & k(x[1], x[2]) & \cdots & k(x[1], x[N]) \\
  k(x[2], x[1]) & k(x[2], x[2]) & \cdots & k(x[2], x[N]) \\
  \vdots & \vdots & \ddots & \vdots \\
  k(x[N], x[1]) & k(x[N], x[2]) & \cdots & k(x[N], x[N])
\end{bmatrix}
$$

For this to be a valid covariance matrix, it must be symmetric and positive definite; hence the requirement that $k$ be a positive definite function (which, by definition, says that the above procedure will yield PD matrices).

We also support the inclusion of zero-mean Gaussian noise in the model, via the `observation_noise_variance` parameter. This augments the generative model to

$$
f \sim \text{GP}(m, k) \\
(y[i] | f, x[i]) \sim \text{Normal}(f(x[i]), s)
$$

where

- $m$ is the mean function
- $k$ is the covariance kernel function
- $f$ is the function drawn from the GP
- $x[i]$ are the index points at which the function is observed
- $y[i]$ are the observed values at the index points
- $s$ is the scale of the observation noise.

Note that this class represents an unconditional Gaussian process; it does not implement posterior inference conditional on observed function evaluations. This class is useful, for example, if one wishes to combine a GP prior with a non-conjugate likelihood using MCMC to sample from the posterior.

Mathematical Details

The probability density function (pdf) is a multivariate normal whose parameters are derived from the GP’s properties:

$$
\text{pdf}(x; \text{index_points}, \text{mean_fn}, \text{kernel}) = \exp(-0.5 * y) / Z
$$

$K = (\text{kernel.matrix}(\text{index_points}, \text{index_points}) +
(\text{observation_noise_variance} + \text{jitter}) \times \text{eye(N)})$

$y = (x - \text{mean_fn}(\text{index_points}))^T @ K @ (x - \text{mean_fn}(\text{index_points}))$

$Z = (2 \times \pi)^{(N / 2)} \times \text{det}(K)^{(1 / 2)}$

where:
• index_points are points in the index set over which the GP is defined,
• mean_fn is a callable mapping the index set to the GP's mean values,
• kernel is PositiveSemidefiniteKernel-like and represents the covariance function of the
  GP,
• observation_noise_variance represents (optional) observation noise.
• jitter is added to the diagonal to ensure positive definiteness up to machine precision (other-
  wise Cholesky-decomposition is prone to failure),
• eye(N) is an N-by-N identity matrix.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_chisq(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(),
tfd_dirichlet_multinomial(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gama(), tfd_gaussian_process_regression_model(), tfd_generalized_normal(),
tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(),
tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(),
tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential(),
tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(),
tfd_lkj(), tfd_logistic(), tfd_multinomial(), tfd_multivariate_normal_diag(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_full_covariance(),
tfd_multivariate_normal_full_correlation(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_normal_tril(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(),
tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(),
tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribute(),
tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_von_mises_fisher(),
tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(),
tfd_vector_laplace_diag(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh(),
tfd_von_mises(), tfd_von_mises_fisher(), tfd_weibull(), tfd_wishart_linear_operator(),
tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()

---

**tfd_gaussian_process_regression_model**

Posterior predictive distribution in a conjugate GP regression model.

---

**Description**

Posterior predictive distribution in a conjugate GP regression model.
Usage

tfd_gaussian_process_regression_model(
    kernel,
    index_points = NULL,
    observation_index_points = NULL,
    observations = NULL,
    observation_noise_variance = 0,
    predictive_noise_variance = NULL,
    mean_fn = NULL,
    jitter = 1e-06,
    validate_args = FALSE,
    allow_nan_stats = FALSE,
    name = "GaussianProcessRegressionModel"
)

Arguments

kernel PositiveSemidefiniteKernel-like instance representing the GP's covariance function.

index_points float Tensor representing finite (batch of) vector(s) of points in the index set over which the GP is defined. Shape has the form \([b_1, ..., b_B, e_1, f_1, ..., f_F]\) where F is the number of feature dimensions and must equal kernel$feature_ndims and e_1 is the number (size) of index points in each batch (we denote it e_1 to distinguish it from the number of inducing index points, denoted e_2 below). Ultimately the GaussianProcess distribution corresponds to an e_1-dimensional multivariate normal. The batch shape must be broadcastable with kernel$batch_shape, the batch shape of inducing_index_points, and any batch dims yielded by mean_fn.

observation_index_points Tensor representing finite collection, or batch of collections, of points in the index set for which some data has been observed. Shape has the form \([b_1, ..., b_B, e, f_1, ..., f_F]\) where F is the number of feature dimensions and must equal kernel$feature_ndims, and e is the number (size) of index points in each batch. \([b_1, ..., b_B, e]\) must be broadcastable with the shape of observations, and \([b_1, ..., b_B]\) must be broadcastable with the shapes of all other batched parameters (kernel.batch_shape, index_points, etc). The default value is None, which corresponds to the empty set of observations, and simply results in the prior predictive model (a GP with noise of variance predictive_noise_variance).

observations Tensor representing collection, or batch of collections, of observations corresponding to observation_index_points. Shape has the form \([b_1, ..., b_B, e]\), which must be broadcastable with the batch and example shapes of observation_index_points. The batch shape \([b_1, ..., b_B]\) must be broadcastable with the shapes of all other batched parameters (kernel.batch_shape, index_points, etc.). The default value is None, which corresponds to the empty set of observations, and simply results in the prior predictive model (a GP with noise of variance predictive_noise_variance).

observation_noise_variance float Tensor representing the variance of the noise in the Normal likelihood
distribution of the model. May be batched, in which case the batch shape must be broadcastable with the shapes of all other batched parameters (kernel$batch_shape, index_points, etc.). Default value: 0.

predictive_noise_variance

Tensor representing the variance in the posterior predictive model. If None, we simply re-use observation_noise_variance for the posterior predictive noise. If set explicitly, however, we use this value. This allows us, for example, to omit predictive noise variance (by setting this to zero) to obtain noiseless posterior predictions of function values, conditioned on noisy observations.

mean_fn

callable that acts on index_points to produce a collection, or batch of collections, of mean values at index_points. Takes a Tensor of shape \([b1, ..., bB, f1, ..., fF]\) and returns a Tensor whose shape is broadcastable with \([b1, ..., bB]\). Default value: None implies the constant zero function.

jitter

float scalar Tensor added to the diagonal of the covariance matrix to ensure positive definiteness of the covariance matrix. Default value: 1e-6.

validate_args

Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name

name prefixed to Ops created by this class.

Value

da distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(), tfd_dirichlet_multinomial(), tfd_dirichlet_multivariate(), tfd_empirical(), tfd_exp_inverse_gamma(), tfd_expontential(), tfd_gamma(), tfd_gamma(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_sinh_arcsinh(), tfd_neg_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(), tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(), tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_student_t(), tfd_transformed_distribution(),
The Generalized Normal distribution.

Description

The Generalized Normal (or Generalized Gaussian) generalizes the Normal distribution with an additional shape parameter. It is parameterized by location `loc`, scale `scale` and shape `power`.

Usage

tfd_generalized_normal(
  loc,
  scale,
  power,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "GeneralizedNormal"
)

Arguments

- **loc**: Floating point tensor; the means of the distribution(s).
- **scale**: Floating point tensor; the scale of the distribution(s). Must contain only positive values.
- **power**: Floating point tensor; the shape parameter of the distribution(s). Must contain only positive values. `loc`, `scale` and `power` must have compatible shapes for broadcasting.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.
Details

Mathematical details

The probability density function (pdf) is,

\[
\text{pdf}(x; \text{loc}, \text{scale}, \text{power}) = \frac{1}{2 \times \text{scale} \times \Gamma(1 + 1 / \text{power})} \times \\
\exp(-(|x - \text{loc}| / \text{scale}) ^ \text{power})
\]

where \(\text{loc}\) is the mean, \(\text{scale}\) is the scale, and, \(\text{power}\) is the shape parameter. If the power is above two, the distribution becomes platykurtic. A power equal to two results in a Normal distribution. A power smaller than two produces a leptokurtic (heavy-tailed) distribution. Mean and scale behave the same way as in the equivalent Normal distribution.


Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions:

tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(),
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(),
tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(),
tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(),
tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(),
tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(),
tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(),
tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(),
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_normal_tril(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(),
tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinhcsech(),
tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(),
tfd_transformed_distribution(), tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(),
tfd_uniform(), tfd_variational_gaussian_process(),
tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(),
tfd_vector_laplace_diag(), tfd_vector_laplace_linear_operator(),
tfd_vector_sinh_arcsinh_diag(),
tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(),
tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
The Generalized Pareto distribution.

Description
The Generalized Pareto distributions are a family of continuous distributions on the reals. Special cases include Exponential (when \( \text{loc} = 0 \), \( \text{concentration} = 0 \)), Pareto (when \( \text{concentration} > 0 \), \( \text{loc} = \text{scale} / \text{concentration} \)), and Uniform (when \( \text{concentration} = -1 \)).

Usage
```
tfd_generalized_pareto(
  loc,
  scale,
  concentration,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = NULL
)
```

Arguments
- **loc**: The location / shift of the distribution. GeneralizedPareto is a location-scale distribution. This parameter lower bounds the distribution’s support. Must broadcast with `scale`, `concentration`. Floating point `Tensor`.
- **scale**: The scale of the distribution. GeneralizedPareto is a location-scale distribution, so doubling the scale doubles a sample and halves the density. Strictly positive floating point `Tensor`. Must broadcast with `loc`, `concentration`.
- **concentration**: The shape parameter of the distribution. The larger the magnitude, the more the distribution concentrates near `loc` (for `concentration >= 0`) or near `loc - (scale/concentration)` (for `concentration < 0`). Floating point `Tensor`.
- **validate_args**: Logical, default `FALSE`. When `TRUE` distribution parameters are checked for validity despite possibly degrading runtime performance. When `FALSE` invalid inputs may silently render incorrect outputs. Default value: `FALSE`.
- **allow_nan_stats**: Logical, default `TRUE`. When `TRUE`, statistics (e.g., mean, mode, variance) use the value `NaN` to indicate the result is undefined. When `FALSE`, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details
This distribution is often used to model the tails of other distributions. As a member of the location-scale family, \( X \sim \text{GeneralizedPareto}(\text{loc}=\text{loc}, \text{scale}=\text{scale}, \text{concentration}=\text{conc}) \) maps to \( Y \sim \text{GeneralizedPareto}(\text{loc}=0, \text{scale}=1, \text{concentration}=\text{conc}) \) via \( Y = (X - \text{loc}) / \text{scale} \).
For positive concentrations, the distribution is equivalent to a hierarchical Exponential-Gamma model with $X|\text{rate} \sim \text{Exponential}(\text{rate})$ and $\text{rate} \sim \text{Gamma}(\text{concentration}=1/\text{concentration},\text{scale}=\text{scale}/\text{concentration})$. In the following, samps1 and samps2 are identically distributed:

```r
genp <- tfd_generalized_pareto(loc = 0, scale = scale, concentration = conc)
samps1 <- genp %>% tfd_sample(1000)
jd <- tfd_joint_distribution_named(
  list(
    rate = tfd_gamma(1 / genp$concentration, genp$scale / genp$concentration),
    x = function(rate) tfd_exponential(rate))
samps2 <- jd %>% tfd_sample(1000) %>% .$x
```

The support of the distribution is always lower bounded by loc. When concentration < 0, the support is also upper bounded by loc + scale / abs(concentration).

**Mathematical Details**

The probability density function (pdf) is,

$$
\text{pdf}(x; \mu, \sigma, \text{shp}, x > \mu) = \frac{(1 + \text{shp} \times (x - \mu) / \sigma)^{(-1 / \text{shp}) - 1}}{\sigma}
$$

where:

- concentration = shp, any real value,
- scale = sigma, sigma > 0,
- loc = mu.

The cumulative density function (cdf) is,

$$
\text{cdf}(x; \mu, \sigma, \text{shp}, x > \mu) = 1 - (1 + \text{shp} \times (x - \mu) / \sigma)^{(-1 / \text{shp})}
$$

Distribution parameters are automatically broadcast in all functions; see examples for details. Samples of this distribution are reparameterized (pathwise differentiable).

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`. 
**tfd_geometric**  
**Geometric distribution**

**Description**

The Geometric distribution is parameterized by $p$, the probability of a positive event. It represents the probability that in $k + 1$ Bernoulli trials, the first $k$ trials failed, before seeing a success. The pmf of this distribution is:

**Usage**

```python
  tfd_geometric(
    logits = NULL,
    probs = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Geometric"
  )
```

**Arguments**

- `logits` Floating-point Tensor with shape $[B1, ..., Bb]$ where $b >= 0$ indicates the number of batch dimensions. Each entry represents logits for the probability of success for independent Geometric distributions and must be in the range (-inf, inf]. Only one of `logits` or `probs` should be specified.

- `probs` Positive floating-point Tensor with shape $[B1, ..., Bb]$ where $b >= 0$ indicates the number of batch dimensions. Each entry represents the probability of success for independent Geometric distributions and must be in the range $(0, 1]$. Only one of `logits` or `probs` should be specified.

- `validate_args` Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- `allow_nan_stats` Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

- `name` name prefixed to Ops created by this class.

**Details**

Mathematical Details

$$pmf(k; p) = (1 - p)^k \times p$$

where:

- $p$ is the success probability, $0 < p \leq 1$, and,
- $k$ is a non-negative integer.
Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


tfd_gumbel

Scalar Gumbel distribution with location loc and scale parameters

Description

Mathematical details

Usage

tfd_gumbel(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Gumbel"
)
Arguments

loc
Floating point tensor, the means of the distribution(s).

scale
Floating point tensor, the scales of the distribution(s). ‘scale’ must contain only positive values.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
The probability density function (pdf) of this distribution is,

$$pdf(x; mu, sigma) = \exp(-\frac{x - mu}{sigma} - \exp(-\frac{x - mu}{sigma})) / sigma$$

where loc = mu and scale = sigma.

The cumulative density function of this distribution is, cdf(x; mu, sigma) = \exp(-\exp(-\frac{x - mu}{sigma})

The Gumbel distribution is a member of the location-scale family, i.e., it can be constructed as,

$$X \sim \text{Gumbel}(\text{loc}=0, \text{scale}=1)$$

$$Y = \text{loc} + \text{scale} \times X$$

Value
a distribution instance.

See Also
Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli().
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(),
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_generalized_normal(), tfd_geometric(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(),
tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(),
tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential(),
tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(),
tfd_lkj(), tfd_log_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture(),
tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(),
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(),
tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli().
tfd_half_cauchy

**Half-Cauchy distribution**

**Description**

The half-Cauchy distribution is parameterized by a \( \text{loc} \) and a \( \text{scale} \) parameter. It represents the right half of the two symmetric halves in a Cauchy distribution.

**Usage**

```r
(tfd_half_cauchy(loc, scale, validate_args = FALSE, allow_nan_stats = TRUE, name = "HalfCauchy")
```

**Arguments**

- **loc**
  - Floating-point Tensor; the location(s) of the distribution(s).

- **scale**
  - Floating-point Tensor; the scale(s) of the distribution(s). Must contain only positive values.

- **validate_args**
  - Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **allow_nan_stats**
  - Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

- **name**
  - name prefixed to Ops created by this class.

**Details**

Mathematical Details

The probability density function (pdf) for the half-Cauchy distribution is given by

\[
\text{pdf}(x; \text{loc}, \text{scale}) = \frac{2}{\pi \text{scale} \left(1 + z^2\right)}
\]

\[
z = \frac{(x - \text{loc})}{\text{scale}}
\]
where \( \text{loc} \) is a scalar in \( \mathbb{R} \) and \( \text{scale} \) is a positive scalar in \( \mathbb{R} \). The support of the distribution is given by the interval \([\text{loc}, \infty)\).

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_chi()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet_multivariate_normal_diag()`, `tfd_dirichlet_multivariate_normal_full_covariance()`, `tfd_dirichlet_multivariate_normal_linear_operator()`, `tfd_dirichlet_multivariate_tri_l()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_diag_plus_low_rank()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichlet_multivariate_normal_tril()`, `tfd_dirichlet_multivariate_student_t_linear_operator()`, `tfd_dirichle...
Arguments

**scale**
Floating point tensor; the scales of the distribution(s). Must contain only positive values.

**validate_args**
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

**allow_nan_stats**
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

**name**
name prefixed to Ops created by this class.

Details

The half normal is a transformation of a centered normal distribution. If some random variable \( X \) has normal distribution,

\[
X \sim \text{Normal}(0.0, \text{scale})
\]

\[
Y = |X|
\]

Then \( Y \) will have half normal distribution. The probability density function (pdf) is:

\[
pdf(x; \text{scale}, x > 0) = \sqrt{2} / (\text{scale} \times \sqrt{\pi}) \times \exp(- 1/2 \times (x / \text{scale})^2))
\]

Where \( \text{scale} = \sigma \) is the standard deviation of the underlying normal distribution.

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`. Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_bimomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_chi()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`, `tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_hidden_markov_model()`, `tfd_horseshoe()`, `tfd_independent()`, `tfd_inverse_gamma()`, `tfd_inverse_gaussian()`, `tfd_johnson_s_u()`, `tfd_joint_distribution_named_auto_batched()`, `tfd_joint_distribution_named()`, `tfd_joint_distribution_sequential()`, `tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`, `tfd_lkj()`, `tfd_log_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_mixture_same_family()`, `tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal()`, `tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_normal_tril()`, `tfd_mixture_student_t_linear_operator()`, `tfd_negative_binomial()`, `tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_compound()`, `tfd_poisson()`, `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`.
tfd_hidden_markov_model

Hidden Markov model distribution

Description
The HiddenMarkovModel distribution implements a (batch of) hidden Markov models where the initial states, transition probabilities and observed states are all given by user-provided distributions.

Usage
```r
r
```

Arguments
```r
initial_distribution
A Categorical-like instance. Determines probability of first hidden state in Markov chain. The number of categories must match the number of categories of transition_distribution as well as both the rightmost batch dimension of transition_distribution and the rightmost batch dimension of observation_distribution.

transition_distribution
A Categorical-like instance. The rightmost batch dimension indexes the probability distribution of each hidden state conditioned on the previous hidden state.

observation_distribution
A tfp$distributions$Distribution-like instance. The rightmost batch dimension indexes the distribution of each observation conditioned on the corresponding hidden state.

num_steps
The number of steps taken in Markov chain. An integer.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

```
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
This model assumes that the transition matrices are fixed over time. In this model, there is a sequence of integer-valued hidden states: \(z[0], z[1], ..., z[num\_steps - 1]\) and a sequence of observed states: \(x[0], ..., x[num\_steps - 1]\).

The distribution of \(z[0]\) is given by \texttt{initial\_distribution}. The conditional probability of \(z[i + 1]\) given \(z[i]\) is described by the batch of distributions in \texttt{transition\_distribution}. For a batch of hidden Markov models, the coordinates before the rightmost one of the \texttt{transition\_distribution} batch correspond to indices into the hidden Markov model batch. The rightmost coordinate of the batch is used to select which distribution \(z[i + 1]\) is drawn from. The distributions corresponding to the probability of \(z[i + 1]\) conditional on \(z[i] == k\) is given by the elements of the batch whose rightmost coordinate is \(k\).

Similarly, the conditional distribution of \(z[i]\) given \(x[i]\) is given by the batch of \texttt{observation\_distribution}. When the rightmost coordinate of \texttt{observation\_distribution} is \(k\) it gives the conditional probabilities of \(x[i]\) given \(z[i] == k\). The probability distribution associated with the \texttt{HiddenMarkovModel} distribution is the marginal distribution of \(x[0], ..., x[num\_steps - 1]\).

Value
a distribution instance.

See Also
For usage examples see e.g. \texttt{tfd\_sample()}, \texttt{tfd\_log\_prob()}, \texttt{tfd\_mean()}.

Other distributions: \texttt{tfd\_autoregressive()}, \texttt{tfd\_batch\_reshape()}, \texttt{tfd\_bates()}, \texttt{tfd\_bernoulli()}, \texttt{tfd\_beta\_binomial()}, \texttt{tfd\_beta()}, \texttt{tfd\_binomial()}, \texttt{tfd\_categorical()}, \texttt{tfd\_cauchy()}, \texttt{tfd\_chi2()}, \texttt{tfd\_chi()}, \texttt{tfd\_cholesky\_lkj()}, \texttt{tfd\_continuous\_bernoulli()}, \texttt{tfd\_deterministic()}, \texttt{tfd\_dirichlet\_multinomial()}, \texttt{tfd\_dirichlet()}, \texttt{tfd\_empirical()}, \texttt{tfd\_exp\_gamma()}, \texttt{tfd\_exp\_inverse\_gamma()}, \texttt{tfd\_exponential()}, \texttt{tfd\_gamma\_gamma()}, \texttt{tfd\_gamma\_gamma\_process\_regression\_model()}, \texttt{tfd\_gaussian\_process\_regression\_model()}, \texttt{tfd\_generalized\_normal()}, \texttt{tfd\_geometric()}, \texttt{tfd\_gumbel()}, \texttt{tfd\_half\_cauchy()}, \texttt{tfd\_half\_normal()}, \texttt{tfd\_horseshoe()}, \texttt{tfd\_independent()}, \texttt{tfd\_inverse\_gamma()}, \texttt{tfd\_inverse\_gaussian()}, \texttt{tfd\_johnson\_s\_u()}, \texttt{tfd\_joint\_distribution\_named\_auto\_batched()}, \texttt{tfd\_joint\_distribution\_named\_auto\_batched()}, \texttt{tfd\_joint\_distribution\_named\_auto\_batched()}, \texttt{tfd\_joint\_distribution\_sequential\_auto\_batched()}, \texttt{tfd\_kumaraswamy()}, \texttt{tfd\_laplace()}, \texttt{tfd\_linear\_gaussian\_state\_space\_model\_full\_covariance\_auto\_batched()}, \texttt{tfd\_log\_logistic()}, \texttt{tfd\_log\_normal()}, \texttt{tfd\_logistic()}, \texttt{tfd\_mixture\_same\_family\_auto\_batched()}, \texttt{tfd\_multinomial()}, \texttt{tfd\_multivariate\_normal\_diag\_plus\_low\_rank\_auto\_batched()}, \texttt{tfd\_multivariate\_normal\_full\_covariance\_auto\_batched()}, \texttt{tfd\_multivariate\_normal\_linear\_operator\_auto\_batched()}, \texttt{tfd\_multivariate\_student\_t\_linear\_operator\_auto\_batched()}, \texttt{tfd\_negative\_binomial()}, \texttt{tfd\_normal()}, \texttt{tfd\_one\_hot\_categorical\_auto\_batched()}, \texttt{tfd\_pareto()}, \texttt{tfd\_pixel\_cnn()}, \texttt{tfd\_poisson\_log\_normal\_quadrature\_auto\_batched()}, \texttt{tfd\_poisson\_log\_normal\_quadrature\_auto\_batched()}, \texttt{tfd\_power\_spherical()}, \texttt{tfd\_probit\_bernoulli()}, \texttt{tfd\_quantized()}, \texttt{tfd\_relaxed\_bernoulli()}, \texttt{tfd\_relaxed\_one\_hot\_categorical\_auto\_batched()}, \texttt{tfd\_sample\_distribution\_auto\_batched()}, \texttt{tfd\_sinh\_arcsinh\_auto\_batched()}, \texttt{tfd\_skellam\_auto\_batched()}, \texttt{tfd\_spherical\_uniform\_auto\_batched()}, \texttt{tfd\_student\_t\_process\_auto\_batched()}, \texttt{tfd\_student\_t\_process\_auto\_batched()}, \texttt{tfd\_transformed\_distribution\_auto\_batched()}, \texttt{tfd\_triangular\_auto\_batched()}, \texttt{tfd\_truncated\_cauchy\_auto\_batched()}, \texttt{tfd\_truncated\_normal\_auto\_batched()}, \texttt{tfd\_uniform\_auto\_batched()}, \texttt{tfd\_variational\_gaussian\_process\_regression\_model\_auto\_batched()}.
**tfd_horseshoe**

**Horseshoe distribution**

**Description**

The so-called 'horseshoe' distribution is a Cauchy-Normal scale mixture, proposed as a sparsity-inducing prior for Bayesian regression. It is symmetric around zero, has heavy (Cauchy-like) tails, so that large coefficients face relatively little shrinkage, but an infinitely tall spike at 0, which pushes small coefficients towards zero. It is parameterized by a positive scalar scale parameter: higher values yield a weaker sparsity-inducing effect.

**Usage**

```r
  tfd_horseshoe(
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Horseshoe"
  )
```

**Arguments**

- `scale`:
  Floating point tensor; the scales of the distribution(s). Must contain only positive values.

- `validate_args`:
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- `allow_nan_stats`:
  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

- `name`:
  name prefixed to Ops created by this class.

**Details**

Mathematical details

The Horseshoe distribution is centered at zero, with scale parameter $\lambda$. It is defined by:

$horseshoe(scale = \lambda) \sim \text{Normal}(0, \lambda \ast \sigma)$

where $\sigma \sim \text{half_cauchy}(0,1)$
tfd_independent

Independent distribution from batch of distributions

Description

This distribution is useful for regarding a collection of independent, non-identical distributions as a single random variable. For example, the Independent distribution composed of a collection of Bernoulli distributions might define a distribution over an image (where each Bernoulli is a distribution over each pixel).
tfd_independent

Usage
tfd_independent(
distribution,
reinterpreted_batch_ndims = NULL,
validate_args = FALSE,
name = paste0("Independent", distribution$name)
)

Arguments
distribution The base distribution instance to transform. Typically an instance of Distribution
reinterpreted_batch_ndims Scalar, integer number of rightmost batch dims which will be regarded as event
dims. When NULL all but the first batch axis (batch axis 0) will be transferred
to event dimensions (analogous to tf$layers$flatten).
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for
validity despite possibly degrading runtime performance. When FALSE invalid
inputs may silently render incorrect outputs. Default value: FALSE.
name The name for ops managed by the distribution. Default value: Independent +
distribution.name.

Details
More precisely, a collection of \(B\) (independent) \(E\)-variate random variables \(\{X_1, \ldots, X_B\}\), can
be regarded as a \([B, E]\)-variate random variable \((X_1, \ldots, X_B)\) with probability \(p(x_1, \ldots, x_B)\)
= \(p_1(x_1) \ast \ldots \ast p_B(x_B)\) where \(p_b(X_b)\) is the probability of the \(b\)-th rv. More generally
\(B, E\) can be arbitrary shapes. Similarly, the Independent distribution specifies a distribution over
\([B, E]\)-shaped events. It operates by reinterpreting the rightmost batch dims as part of the event
dimensions. The \texttt{reinterpreted_batch_ndims} parameter controls the number of batch dims which
are absorbed as event dims; \texttt{reinterpreted_batch_ndims} <= \texttt{len(batch_shape)}. For example,
the \texttt{log_prob} function entails a \texttt{reduce_sum} over the rightmost \texttt{reinterpreted_batch_ndims} af-
ter calling the base distribution’s \texttt{log_prob}. In other words, since the batch dimension(s) index
independent distributions, the resultant multivariate will have independent components.

Mathematical Details
The probability function is,

\[
\text{prob}(x; \texttt{reinterpreted_batch_ndims}) = \\
\text{tf.reduce_prod(dist.prob(x), axis=-1-range(reinterpreted_batch_ndims))}
\]

Value
a distribution instance.

See Also
For usage examples see e.g. \texttt{tfd_sample()}, \texttt{tfd_log_prob()}, \texttt{tfd_mean()}. 

---

tfd_inverse_gamma

**InverseGamma distribution**

**Description**

The `InverseGamma` distribution is defined over positive real numbers using parameters concentration (aka "alpha") and scale (aka "beta").

**Usage**

```python
  tfd_inverse_gamma(
    concentration,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "InverseGamma"
  )
```

**Arguments**

- **concentration**  
  Floating point tensor, the concentration params of the distribution(s). Must contain only positive values.
scale

Floating point tensor, the scale params of the distribution(s). Must contain only positive values. This parameter was called rate before release 0.8.

validate_args

Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name

name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
\text{pdf}(x; \alpha, \beta, x > 0) = x^{(-\alpha - 1)} \exp(-\beta / x) / Z
\]

\[
Z = \Gamma(\alpha) \beta^{-\alpha}
\]

where:

- concentration = \(\alpha\),
- scale = \(\beta\),
- \(Z\) is the normalizing constant, and,
- Gamma is the gamma function.

The cumulative density function (cdf) is,

\[
\text{cdf}(x; \alpha, \beta, x > 0) = \frac{\Gamma(\alpha, \beta / x)}{\Gamma(\alpha)}
\]

where ‘\(\Gamma(\alpha, \beta / x)\)’ is the [upper incomplete Gamma function](https://en.wikipedia.org/wiki/Incomplete_gamma_function).

The parameters can be intuited via their relationship to mean and variance when these moments exist,

mean = \(\beta / (\alpha - 1)\) when \(\alpha > 1\)

variance = \(\beta^2 / (\alpha - 1)^2 / (\alpha - 2)\) when \(\alpha > 2\)

i.e., under the same conditions:

\[
\alpha = \text{mean}^2 / \text{variance} + 2 \quad \text{beta} = \text{mean} * (\text{mean}^2 / \text{variance} + 1)
\]

Distribution parameters are automatically broadcast in all functions; see examples for details.

Samples of this distribution are reparameterized (pathwise differentiable).

The derivatives are computed using the approach described in the paper


[gamma function]: R:gamma%20function

[upper incomplete Gamma function]: R:upper%20incomplete%20Gamma%20function

tfd_inverse_gaussian

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

**tfd_inverse_gaussian**  
Inverse Gaussian distribution

**Description**

The **inverse Gaussian distribution** is parameterized by a `loc` and a concentration parameter. It's also known as the Wald distribution. Some, e.g., the Python scapy package, refer to the special case when `loc` is 1 as the Wald distribution.

**Usage**

```python
tfd_inverse_gaussian(
    loc,
    concentration,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "InverseGaussian"
)
```
Arguments

loc
Floating-point Tensor, the loc params. Must contain only positive values.

concentration
Floating-point Tensor, the concentration params. Must contain only positive values.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

The “inverse” in the name does not refer to the distribution associated to the multiplicative inverse of a random variable. Rather, the cumulant generating function of this distribution is the inverse to that of a Gaussian random variable.

Mathematical Details

The probability density function (pdf) is,

\[
\text{pdf}(x; \mu, \lambda) = \left[\frac{\lambda}{2 \pi x^3}\right]^{0.5} \exp\left\{-\frac{\lambda(x - \mu)^2}{2 \mu^2 x}\right\}
\]

where

- loc = \mu
- concentration = \lambda.

The support of the distribution is defined on (0, infinity). Mapping to R and Python scipy’s parameterization:

- R: statmod::invgauss
- mean = loc
- shape = concentration
- dispersion = 1 / concentration. Used only if shape is NULL.

- Python: scipy.stats.invgauss
- mu = loc / concentration
- scale = concentration

Value

a distribution instance.
See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

### Description

This distribution has parameters: shape parameters skewness and tailweight, location loc, and scale.

### Usage

```python
  tfd_johnson_s_u(
    skewness,
    tailweight,
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = NULL
  )
```
Arguments

- **skewness**: Floating-point Tensor. Skewness of the distribution(s).
- **tailweight**: Floating-point Tensor. Tail weight of the distribution(s). tailweight must contain only positive values.
- **loc**: Floating-point Tensor. The mean(s) of the distribution(s).
- **scale**: Floating-point Tensor. The scaling factor(s) for the distribution(s). Note that scale is not technically the standard deviation of this distribution but has semantics more similar to standard deviation than variance.

- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

- **name**: name prefixed to Ops created by this class.

Details

Mathematical details

The probability density function (pdf) is,

\[
pdf(x; s, t, xi, sigma) = \exp(-0.5 (s + t \arcsinh(y))**2) / Z
\]

where,

- \(s = \text{skewness}\)
- \(t = \text{tailweight}\)
- \(y = (x - xi) / \text{sigma}\)
- \(Z = \sigma \sqrt{2 \pi} \sqrt{1 + y**2} / t\)

where:

- \(\text{loc} = xi\),
- \(\text{scale} = \text{sigma}\), and,
- \(Z\) is the normalization constant. The JohnsonSU distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X \sim \text{JohnsonSU}(\text{skewness}, \text{tailweight}, \text{loc}=0, \text{scale}=1)
\]

\[
Y = \text{loc} + \text{scale} \times X
\]

Value

a distribution instance.
See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gamma_gammas()`, `tfd_gamma()`, `tfd_gaussian_regression_model()`, `tfd_gaussian_process()`, `tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`, `tfd_hidden_markov_model()`, `tfd_horseshoe()`, `tfd_independent()`, `tfd_inverse_gamma()`, `tfd_inverse_gaussian()`, `tfd_joint_distribution_named_auto_batched()`, `tfd_joint_distribution_named()`, `tfd_joint_distribution_sequential_auto_batched()`, `tfd_joint_distribution_sequential()`, `tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`, `tfd_lkj()`, `tfd_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_logistic()`, `tfd_mixure_same_family()`, `tfd_mixure()`, `tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal_diag()`, `tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_normal_tri_l()`, `tfd_multivariate_student_t_linear_operator()`, `tfd_negative_binomial()`, `tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_compound()`, `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`, `tfd_skellam()`, `tfd_spherical_uniform()`, `tfd_student_t_process()`, `tfd_student_t()`, `tfd_truncated_cauchy()`, `tfd_truncated_normal()`, `tfd_uniform()`, `tfd_von_mises()`, `tfd_von_mises_fisher()`, `tfd_weibull()`, `tfd_wishart_linear_operator()`, `tfd_wishart_tri_l()`, `tfd_wishart()`, `tfd_zipf()`

tfd_joint_distribution_named

Joint distribution parameterized by named distribution-making functions.

Description

This distribution enables both sampling and joint probability computation from a single model specification. A joint distribution is a collection of possibly interdependent distributions. Like `JointDistributionSequential`, `JointDistributionNamed` is parameterized by several distribution-making functions. Unlike `JointDistributionNamed`, each distribution-making function must have its own key. Additionally every distribution-making function’s arguments must refer to only specified keys.

Usage

tfd_joint_distribution_named(model, validate_args = FALSE, name = NULL)
Arguments

model: named list of distribution-making functions each with required args corresponding only to other keys in the named list.

validate_args: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

name: The name for ops managed by the distribution. Default value: "JointDistributionNamed".

Details

Mathematical Details

Internally JointDistributionNamed implements the chain rule of probability. That is, the probability function of a length-d vector \( x \) is,

\[
p(x) = \prod_{i=0}^{d-1} p(x_i \mid x_{<i})
\]

The JointDistributionNamed is parameterized by a dict (or namedtuple) composed of either:

1. tfp$distributions$Distribution-like instances or,
2. functions which return a tfp$distributions$Distribution-like instance. The "conditioned on" elements are represented by the function's required arguments; every argument must correspond to a key in the named distribution-making functions. Distribution-makers which are directly a Distribution-like instance are allowed for convenience and semantically identical a zero argument function. When the maker takes no arguments it is preferable to directly provide the distribution instance.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),

- tfd_beta_binomial()
- tfd_beta()
- tfd_binomial()
- tfd_categorical()
- tfd_cauchy()
- tfd_chi()
- tfd_cholesky_lkj()
- tfd_continuous_bernoulli()
- tfd_deterministic()
- tfd_dirichlet_multinomial()
- tfd_dirichlet() (alongside tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
- tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
- tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),
- tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),
- tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto=batched(),
- tfd_joint_distribution_sequential_auto=batched(), tfd_joint_distribution_sequential(),
- tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(),
- tfd_log_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixtureSameFamily(), tfd_mixture(),
- tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(),
- tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linearoperator(),
- tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linearoperator(), tfd_negative_binomial()
tfd_joint_distribution_named_auto_batched
Joint distribution parameterized by named distribution-making functions.

Description
This class provides automatic vectorization and alternative semantics for `tfd_joint_distribution_named()`, which in many cases allows for simplifications in the model specification.

Usage
```
tfd_joint_distribution_named_auto_batched(
    model,
    batch_ndims = 0,
    use_vectorized_map = TRUE,
    validate_args = FALSE,
    name = NULL
)
```

Arguments
- **model**: A generator that yields a sequence of `tfd$Distribution`-like instances.
- **batch_ndims**: integer Tensor number of batch dimensions. The batch_shapes of all component distributions must be such that the prefixes of length `batch_ndims` broadcast to a consistent joint batch shape. Default value: 0.
- **use_vectorized_map**: logical. Whether to use `tf$vectorized_map` to automatically vectorize evaluation of the model. This allows the model specification to focus on drawing a single sample, which is often simpler, but some ops may not be supported. Default value: TRUE.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **name**: name prefixed to Ops created by this class.
Details

Automatic vectorization

Auto-vectorized variants of JointDistribution allow the user to avoid explicitly annotating a model’s vectorization semantics. When using manually-vectorized joint distributions, each operation in the model must account for the possibility of batch dimensions in Distributions and their samples. By contrast, auto-vectorized models need only describe a single sample from the joint distribution; any batch evaluation is automated using `tf$vectorized_map` as required. In many cases this allows for significant simplifications. For example, the following manually-vectorized

tfd_joint_distribution_named() model:

```r
model <- tfd_joint_distribution_sequential(
  list(
    x = tfd_normal(loc = 0, scale = tf$ones(3L)),
    y = tfd_normal(loc = 0, scale = 1),
    z = function(y, x) {
      tfd_normal(loc = x[reticulate::py_ellipsis(), 1:2] + y[reticulate::py_ellipsis(), tf$newaxis], scale = 1)
    }
  )
)
```

can be written in auto-vectorized form as

```r
model <- tfd_joint_distribution_sequential_auto_batched(
  list(
    x = tfd_normal(loc = 0, scale = tf$ones(3L)),
    y = tfd_normal(loc = 0, scale = 1),
    z = function(y, x) {tfd_normal(loc = x[1:2] + y, scale = 1)}
  )
)
```

in which we were able to avoid explicitly accounting for batch dimensions when indexing and slicing computed quantities in the third line. Note: auto-vectorization is still experimental and some TensorFlow ops may be unsupported. It can be disabled by setting `use_vectorized_map=FALSE`.

Alternative batch semantics This class also provides alternative semantics for specifying a batch of independent (non-identical) joint distributions. Instead of simply summing the `log_probs` of component distributions (which may have different shapes), it first reduces the component `log_probs` to ensure that `jd$log_prob(jd$sample())` always returns a scalar, unless `batch_ndims` is explicitly set to a nonzero value (in which case the result will have the corresponding tensor rank).

The essential changes are:

- An event of `JointDistributionNamedAutoBatched` is the list of tensors produced by `$sample()`; thus, the `event_shape` is the list containing the shapes of sampled tensors. These combine both the event and batch dimensions of the component distributions. By contrast, the event shape of a base `JointDistributions` does not include batch dimensions of component distributions.
- The `batch_shape` is a global property of the entire model, rather than a per-component property as in base `JointDistributions`. The global batch shape must be a prefix of the batch shapes of each component; the length of this prefix is specified by an optional argument `batch_ndims`. If `batch_ndims` is not specified, the model has batch shape `()`.
tfd_joint_distribution_sequential

Joint distribution parameterized by distribution-making functions

Description

This distribution enables both sampling and joint probability computation from a single model specification.

Usage

tfd_joint_distribution_sequential(model, validate_args = FALSE, name = NULL)

Arguments

model list of either tfp$distributions$Distribution instances and/or functions which take the k previous distributions and returns a new tfp$distributions$Distribution instance.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

name name prefixed to Ops created by this class.

Details
A joint distribution is a collection of possibly interdependent distributions. Like tf.keras.Sequential, the JointDistributionSequential can be specified via a list of functions (each responsible for making a tfp.distributions.Distribution-like instance). Unlike tf.keras.Sequential, each function can depend on the output of all previous elements rather than only the immediately previous.

Mathematical Details
The JointDistributionSequential implements the chain rule of probability. That is, the probability function of a length-d vector x is,

\[ p(x) = \prod\{ p(x[i] | x[:i]) : i = 0, \ldots, (d - 1) \} \]

The JointDistributionSequential is parameterized by a list comprised of either:

1. tfp.distributions.Distribution-like instances or,
2. callables which return a tfp.distributions.Distribution-like instance. Each list element implements the i-th full conditional distribution, p(x[i] | x[:i]). The "conditioned on" elements are represented by the callable’s required arguments. Directly providing a Distribution-like instance is a convenience and is semantically identical a zero argument callable. Denote the i-th callables non-default arguments as args[i]. Since the callable is the conditional manifest, 0 <= len(args[i]) <= i - 1. When len(args[i]) < i - 1, the callable only depends on a subset of the previous distributions, specifically those at indexes: range(i - 1, i - 1 - num_args[i], -1).

Name resolution: The names of JointDistributionSequential components are defined by explicit-name arguments passed to distributions (tfd.Normal(0., 1., name='x')) and/or by the argument names in distribution-making functions (lambda x: tfd.Normal(x., 1.)). Both approaches may be used in the same distribution, as long as they are consistent; referring to a single component by multiple names will raise a ValueError. Unnamed components will be assigned a dummy name.

Value
a distribution instance.

See Also
For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process().
Joint distribution parameterized by distribution-making functions.

Description

This class provides automatic vectorization and alternative semantics for \texttt{tfd\_joint\_distribution\_sequential()}, which in many cases allows for simplifications in the model specification.

Usage

```r
\texttt{tfd\_joint\_distribution\_sequential\_auto\_batched(}
  \texttt{model,}
  \texttt{batch_ndims = 0,}
  \texttt{use\_vectorized\_map = TRUE,}
  \texttt{validate\_args = FALSE,}
  \texttt{name = NULL}
)```

Arguments

- **model**: A generator that yields a sequence of \texttt{tfd\$Distribution}-like instances.
- **batch_ndims**: integer Tensor number of batch dimensions. The batch shapes of all component distributions must be such that the prefixes of length \texttt{batch\_ndims} broadcast to a consistent joint batch shape. Default value: 0.
use_vectorized_map

logical. Whether to use \texttt{tf$vectorized\_map} to automatically vectorize evaluation of the model. This allows the model specification to focus on drawing a single sample, which is often simpler, but some ops may not be supported. Default value: TRUE.

validate_args

Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

name

name prefixed to Ops created by this class.

Details

Automatic vectorization

Auto-vectorized variants of JointDistribution allow the user to avoid explicitly annotating a model's vectorization semantics. When using manually-vectorized joint distributions, each operation in the model must account for the possibility of batch dimensions in Distributions and their samples. By contrast, auto-vectorized models need only describe a single sample from the joint distribution; any batch evaluation is automated using \texttt{tf$vectorized\_map} as required. In many cases this allows for significant simplifications. For example, the following manually-vectorized \texttt{tfd\_joint\_distribution\_sequential()} model:

```r
model <- tfd\_joint\_distribution\_sequential(
  list(
    tfd\_normal(loc = 0, scale = tf$ones(3L)),
    tfd\_normal(loc = 0, scale = 1),
    function(y, x) {
      tfd\_normal(loc = x[reticulate::py\_ellipsis(), 1:2] + y[reticulate::py\_ellipsis(), tf$\texttt{newaxis}], scale = 1)
    }
  )
)
```

can be written in auto-vectorized form as

```r
model <- tfd\_joint\_distribution\_sequential\_auto\_batched(
  list(
    tfd\_normal(loc = 0, scale = tf$ones(3L)),
    tfd\_normal(loc = 0, scale = 1),
    function(y, x) {tfd\_normal(loc = x[1:2] + y, scale = 1)}
  )
)
```

in which we were able to avoid explicitly accounting for batch dimensions when indexing and slicing computed quantities in the third line. Note: auto-vectorization is still experimental and some TensorFlow ops may be unsupported. It can be disabled by setting \texttt{use\_vectorized\_map}=FALSE.

Alternative batch semantics

This class also provides alternative semantics for specifying a batch of independent (non-identical) joint distributions. Instead of simply summing the \texttt{log\_probs} of component distributions (which may have different shapes), it first reduces the component \texttt{log\_probs} to
ensure that \( \log \text{prob}(\text{sample()}) \) always returns a scalar, unless \( \text{batch_ndims} \) is explicitly set to a nonzero value (in which case the result will have the corresponding tensor rank).

The essential changes are:

- An event of \( \text{JointDistributionSequentialAutoBatched} \) is the list of tensors produced by \$\text{sample}(); thus, the event_shape is the list containing the shapes of sampled tensors. These combine both the event and batch dimensions of the component distributions. By contrast, the event shape of a base \( \text{JointDistribution} \)s does not include batch dimensions of component distributions.

- The batch_shape is a global property of the entire model, rather than a per-component property as in base \( \text{JointDistribution} \)s. The global batch shape must be a prefix of the batch shapes of each component; the length of this prefix is specified by an optional argument \( \text{batch_ndims} \). If \( \text{batch_ndims} \) is not specified, the model has batch shape ().

Value

A distribution instance.

See Also

For usage examples see e.g. \( \text{tfd_sample()} \), \( \text{tfd_log_prob()} \), \( \text{tfd_mean()} \).

Other distributions: \( \text{tfd_autoregressive()} \), \( \text{tfd_batch_reshape()} \), \( \text{tfd_bates()} \), \( \text{tfd_bernoulli()} \), \( \text{tfd_beta_binomial()} \), \( \text{tfd_beta()} \), \( \text{tfd_binomial()} \), \( \text{tfd_categorical()} \), \( \text{tfd_cauchy()} \), \( \text{tfd_chisq()} \), \( \text{tfd_chisquare()} \), \( \text{tfd_continuous_bernoulli()} \), \( \text{tfd_dirichlet()} \), \( \text{tfd_empirical()} \), \( \text{tfd_exp_gamma()} \), \( \text{tfd_exp_inverse_gamma()} \), \( \text{tfd_exponential()} \), \( \text{tfd_gamma_gamma()} \), \( \text{tfd_gamma()} \), \( \text{tfd_gaussian_process_model()} \), \( \text{tfd_gaussian_process()} \), \( \text{tfd_gaussian_process_regression_model()} \), \( \text{tfd_generalized_normal()} \), \( \text{tfd_geometric()} \), \( \text{tfd_gumbel()} \), \( \text{tfd_half_cauchy()} \), \( \text{tfd_half_normal()} \), \( \text{tfd_hidden_markov_model()} \), \( \text{tfd_horseshoe()} \), \( \text{tfd_independent()} \), \( \text{tfd_inverse_gamma()} \), \( \text{tfd_inverse_gaussian()} \), \( \text{tfd_johnson_s_u()} \), \( \text{tfd_joint_distribution_named_auto_batched()} \), \( \text{tfd_joint_distribution_named()} \), \( \text{tfd_joint_distribution_sequential()} \), \( \text{tfd_kumaraswamy()} \), \( \text{tfd_laplace()} \), \( \text{tfd_linear_gaussian_state_space_model()} \), \( \text{tfd_lkj()} \), \( \text{tfd_logistic()} \), \( \text{tfd_log_normal()} \), \( \text{tfd_logistic()} \), \( \text{tfd_mixture_same_family()} \), \( \text{tfd_mixure()} \), \( \text{tfd_multinomial()} \), \( \text{tfd_multivariate_normal_diag_plus_low_rank()} \), \( \text{tfd_multivariate_normal_diag()} \), \( \text{tfd_multivariate_normal()} \), \( \text{tfd_multivariate_normal_linear_operator()} \), \( \text{tfd_multivariate_student_t()} \), \( \text{tfd_negative_binomial()} \), \( \text{tfd_normal()} \), \( \text{tfd_one_hot_categorical()} \), \( \text{tfd_pareto()} \), \( \text{tfd_pixel_cnn()} \), \( \text{tfd_poisson_log_normal_quadrature_compound()} \), \( \text{tfd_power_spherical()} \), \( \text{tfd_probit_bernoulli()} \), \( \text{tfd_quantized()} \), \( \text{tfd_relaxed_bernoulli()} \), \( \text{tfd_relaxed_one_hot_categorical()} \), \( \text{tfd_sample_distribution()} \), \( \text{tfd_sigmoid}() \), \( \text{tfd_sinh_arcsinh()} \), \( \text{tfd_spherical_uniform()} \), \( \text{tfd_student_t_process()} \), \( \text{tfd_student_t()} \), \( \text{tfd_transformed_distribution()} \), \( \text{tfd_triangular()} \), \( \text{tfd_truncated_cauchy()} \), \( \text{tfd_truncated_normal()} \), \( \text{tfd_uniform()} \), \( \text{tfd_variational_gaussian_process()} \), \( \text{tfd_vector_diffeomixture()} \), \( \text{tfd_vector_exponential()} \), \( \text{tfd_vector_variational_gaussian_process()} \), \( \text{tfd_vector_cholesky_lkj()} \), \( \text{tfd_vector_laplace_diag()} \), \( \text{tfd_vector_laplace_linear_operator()} \), \( \text{tfd_vector_sinh_arcsinh_diag()} \), \( \text{tfd_von_mises_fisher()} \), \( \text{tfd_von_mises()} \), \( \text{tfd_weibull()} \), \( \text{tfd_wishart_linear_operator()} \), \( \text{tfd_wishart_tri_l()} \), \( \text{tfd_wishart()} \), \( \text{tfd_zipf()} \)
tfd_kl_divergence Computes the Kullback–Leibler divergence.

Description

Denote this distribution by p and the other distribution by q. Assuming p, q are absolutely continuous with respect to reference measure r, the KL divergence is defined as: \( KL[p, q] = \int p(x) \log(p(x)/q(x)) \, dr(x) \) = \(- \int_F p(x) \log q(x) \, dr(x) + \int_F p(x) \log p(x) \, dr(x) = H[p, q] - H[p] \) where F denotes the support of the random variable \( X \sim p \), \( H[., .] \) denotes (Shannon) cross entropy, and \( H[\cdot] \) denotes (Shannon) entropy.

Usage

tfd_kl_divergence(distribution, other, name = "kl_divergence")

Arguments

distribution The distribution being used.
other tfp$Distributions$Distribution instance.
name String prepended to names of ops created by this function.

Value

self$dtype Tensor with shape \([B_1, ..., B_n]\) representing n different calculations of the Kullback-Leibler divergence.

See Also

Other distribution methods: tfd_cdf(), tfd_covariance(), tfd_cross_entropy(), tfd_entropy(), tfd_log_cdf(), tfd_log_prob(), tfd_log_survival_function(), tfd_mean(), tfd_mode(), tfd_prob(), tfd_quantile(), tfd_sample(), tfd_stddev(), tfd_survival_function(), tfd_variance()

Examples

d1 <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d2 <- tfd_normal(loc = c(1.5, 2), scale = c(1, 0.5))
d1 %>% tfd_kl_divergence(d2)
The Kumaraswamy distribution is defined over the (0, 1) interval using parameters concentration1 (aka "alpha") and concentration0 (aka "beta"). It has a shape similar to the Beta distribution, but is easier to reparameterize.

Usage

```r
tfd_kumaraswamy(
  concentration1 = 1,
  concentration0 = 1,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Kumaraswamy"
)
```

Arguments

- **concentration1**: Positive floating-point Tensor indicating mean number of successes; aka "alpha". Implies `self$dtype` and `self$batch_shape`, i.e., `concentration1$shape = [N1, N2, ..., Nm] = self$batch_shape`.
- **concentration0**: Positive floating-point Tensor indicating mean number of failures; aka "beta". Otherwise has same semantics as `concentration1`.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

```
pdf(x; alpha, beta) = alpha * beta * x**(alpha - 1) * (1 - x**alpha)**(beta - 1)
```

where:

- concentration1 = alpha,
- concentration0 = beta. Distribution parameters are automatically broadcast in all functions.
Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


tfd_laplace

Laplace distribution with location loc and scale parameters

Description

Mathematical details

Usage

tfd_laplace(
  loc,
  scale,
  validate_args = FALSE,  
  allow_nan_stats = TRUE,  
  name = "Laplace"
)
Arguments

loc       Floating point tensor which characterizes the location (center) of the distribution.
scale    Positive floating point tensor which characterizes the spread of the distribution.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
name     name prefixed to Ops created by this class.

Details

The probability density function (pdf) of this distribution is,

\[
pdf(x; \mu, \sigma) = \frac{\exp(-|x - \mu| / \sigma)}{Z}
\]

\[
Z = 2 \sigma
\]

where loc = \mu, scale = \sigma, and Z is the normalization constant.

Note that the Laplace distribution can be thought of two exponential distributions spliced together "back-to-back." The Laplace distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X \sim \text{Laplace}(\text{loc}=0, \text{scale}=1)
\]

\[
Y = \text{loc} + \text{scale} \times X
\]

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_linear_gaussian_state_space_model

Observation distribution from a linear Gaussian state space model

Description

The state space model, sometimes called a Kalman filter, posits a latent state vector $z_t$ of dimension $latent\_size$ that evolves over time following linear Gaussian transitions, $z_{t+1} = F * z_t + N(b; Q)$ for transition matrix $F$, bias $b$ and covariance matrix $Q$. At each timestep, we observe a noisy projection of the latent state $x_t = H * z_t + N(c; R)$. The transition and observation models may be fixed or may vary between timesteps.

Usage

```r
  tfd_linear_gaussian_state_space_model(
    num_timesteps,
    transition_matrix,
    transition_noise,
    observation_matrix,
    observation_noise,
    initial_state_prior,
    initial_step = 0L,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "LinearGaussianStateSpaceModel"
  )
```

Arguments

- `num_timesteps` Integer Tensor total number of timesteps.
- `transition_matrix` A transition operator, represented by a Tensor or LinearOperator of shape [latent\_size, latent\_size], or by a callable taking as argument a scalar integer Tensor $t$ and returning a Tensor or LinearOperator representing the transition operator from latent state at time $t$ to time $t+1$. 
transition_noise
An instance of `tfd.MultivariateNormalLinearOperator` with event shape [latent_size], representing the mean and covariance of the transition noise model, or a callable taking as argument a scalar integer Tensor t and returning such a distribution representing the noise in the transition from time t to time t + 1.

observation_matrix
An observation operator, represented by a Tensor or LinearOperator of shape [observation_size, latent_size], or by a callable taking as argument a scalar integer Tensor t and returning a timestep-specific Tensor or LinearOperator.

observation_noise
An instance of `tfd.MultivariateNormalLinearOperator` with event shape [observation_size], representing the mean and covariance of the observation noise model, or a callable taking as argument a scalar integer Tensor t and returning a timestep-specific noise model.

initial_state_prior
An instance of `MultivariateNormalLinearOperator` representing the prior distribution on latent states; must have event shape [latent_size].

initial_step
optional integer specifying the time of the first modeled timestep. This is added as an offset when passing timesteps t to (optional) callables specifying timestep-specific transition and observation models.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
This Distribution represents the marginal distribution on observations, p(x). The marginal log_prob is computed by Kalman filtering, and sample by an efficient forward recursion. Both operations require time linear in T, the total number of timesteps.

Shapes
The event shape is [num_timesteps, observation_size], where observation_size is the dimension of each observation x_t. The observation and transition models must return consistent shapes. This implementation supports vectorized computation over a batch of models. All of the parameters (prior distribution, transition and observation operators and noise models) must have a consistent batch shape.

Time-varying processes
Any of the model-defining parameters (prior distribution, transition and observation operators and noise models) may be specified as a callable taking an integer timestep t and returning a time-dependent value. The dimensionality (latent_size and observation_size) must be the same at all timesteps.
Importantly, the timestep is passed as a Tensor, not a Python integer, so any conditional behavior must occur inside the TensorFlow graph. For example, suppose we want to use a different transition model on even days than odd days. It does not work to write

```r
transition_matrix <- function(t) {
  if(t %% 2 == 0) even_day_matrix else odd_day_matrix
}
```

since the value of t is not fixed at graph-construction time. Instead we need to write

```r
transition_matrix <- function(t) {
  tf$cond(tf$equal(tf$mod(t, 2), 0), function() even_day_matrix, function() odd_day_matrix)
}
```

so that TensorFlow can switch between operators appropriately at runtime.

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_lkj

**LJK distribution on correlation matrices**

**Description**

This is a one-parameter of distributions on correlation matrices. The probability density is proportional to the determinant raised to the power of the parameter: \( \text{pdf}(X; \eta) = Z(\eta) \times \det(X)^{(\eta - 1)} \), where \( Z(\eta) \) is a normalization constant. The uniform distribution on correlation matrices is the special case \( \eta = 1 \).

**Usage**

```python
  tfd_lkj(
      dimension,
      concentration,
      input_output_cholesky = FALSE,
      validate_args = FALSE,
      allow_nan_stats = TRUE,
      name = "LKJ"
  )
```

**Arguments**

- `dimension` \( \text{integer} \). The dimension of the correlation matrices to sample.
- `concentration` \( \text{float or double Tensor} \). The positive concentration parameter of the LKJ distributions. The pdf of a sample matrix \( X \) is proportional to \( \det(X)^{(\eta - 1)} \).
- `input_output_cholesky` \( \text{Logical} \). If TRUE, functions whose input or output have the semantics of samples assume inputs are in Cholesky form and return outputs in Cholesky form. In particular, if this flag is TRUE, input to log_prob is presumed of Cholesky form and output from sample is of Cholesky form. Setting this argument to TRUE is purely a computational optimization and does not change the underlying distribution. Additionally, validation checks which are only defined on the multiplied-out form are omitted, even if validate_args is TRUE. Default value: FALSE (i.e., input/output does not have Cholesky semantics).
- `validate_args` \( \text{Logical, default FALSE} \). When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- `allow_nan_stats` \( \text{Logical, default TRUE} \). When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- `name` \( \text{name prefixed to Ops created by this class} \).
**Details**

The distribution is named after Lewandowski, Kurowicka, and Joe, who gave a sampler for the distribution in Lewandowski, Kurowicka, Joe, 2009.

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

**tfd_logistic**

*Logistic distribution with location loc and scale parameters*

**Description**

Mathematical details
Usage

tfd_logistic(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Logistic"
)

Arguments

loc      Floating point tensor, the means of the distribution(s).
scale     Floating point tensor, the scales of the distribution(s). Must contain only positive values.
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
name name prefixed to Ops created by this class.

Details

The cumulative density function of this distribution is:

cdf(x; mu, sigma) = 1 / (1 + exp(-(x - mu) / sigma))

where loc = mu and scale = sigma.
The Logistic distribution is a member of the location-scale family, i.e., it can be constructed as,

X ~ Logistic(loc=0, scale=1)
Y = loc + scale * X

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chisq(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
The Logit-Normal distribution

Description

The Logit-Normal distribution models positive-valued random variables whose logit (i.e., sigmoid_inverse, i.e., \( \log(p) - \log(1-p) \)) is normally distributed with mean \( \text{loc} \) and standard deviation \( \text{scale} \). It is constructed as the sigmoid transformation, (i.e., \( 1 / (1 + \exp(-x)) \)) of a Normal distribution.

Usage

```r
  tfd_logit_normal(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "LogitNormal"
  )
```

Arguments

- **loc**: Floating point tensor; the means of the distribution(s).
- **scale**: Floating point tensor; the stddevs of the distribution(s). Must contain only positive values.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Value
a distribution instance.

See Also
For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

---

### Description

Given random variable X, the cumulative distribution function cdf is: `tfd_log_cdf(x) := Log[ P[X <= x] ]` Often, a numerical approximation can be used for `tfd_log_cdf(x)` that yields a more accurate answer than simply taking the logarithm of the cdf when x « -1.

### Usage

`tfd_log_cdf(distribution, value, ...)

### Arguments

distribution
The distribution being used.

value
float or double Tensor.

... Additional parameters passed to Python.

### Value

a Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

### See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

### Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
x <- d %>% tfd_sample()
d %>% tfd_log_cdf(x)
tfd_log_logistic

The log-logistic distribution.

Description

The LogLogistic distribution models positive-valued random variables whose logarithm is a logistic distribution with loc loc and scale scale. It is constructed as the exponential transformation of a Logistic distribution.

Usage

tfd_log_logistic(
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "LogLogistic"
)

Arguments

loc Floating-point Tensor; the loc of the underlying logistic distribution(s).
scale Floating-point Tensor; the scale of the underlying logistic distribution(s).
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
name name prefixed to Ops created by this class.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi(),
tfd_chi2(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma_gamma(), tfd_gamma(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd-half_normal(),
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma().
The LogNormal distribution models positive-valued random variables whose logarithm is normally distributed with mean $\text{loc}$ and standard deviation $\text{scale}$. It is constructed as the exponential transformation of a Normal distribution.

The LogNormal distribution models positive-valued random variables whose logarithm is normally distributed with mean $\text{loc}$ and standard deviation $\text{scale}$. It is constructed as the exponential transformation of a Normal distribution.

Usage

```r
tfd_log_normal(
  loc,
  scale,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "LogNormal"
)
```

```r
tfd_log_normal(
  loc,
  scale,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "LogNormal"
)```
Arguments

loc: Floating-point Tensor; the means of the underlying Normal distribution(s).

scale: Floating-point Tensor; the stddevs of the underlying Normal distribution(s).

validate_args: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name: name prefixed to Ops created by this class.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfdDeterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_log_normal(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(), tfd_log_logistic(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(), tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(), tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(), tfd_skellam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(), tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfdVariationalGaussianProcess(), tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(), tfd_vector_laplace_diag(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh_diag(), tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(), tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
**tfd_log_prob**  
*Log probability density/mass function.*

**Description**

Log probability density/mass function.

**Usage**

```
tfd_log_prob(distribution, value, ...)  
```

**Arguments**

- **distribution**: The distribution being used.
- **value**: float or double Tensor.
- **...**: Additional parameters passed to Python.

**Value**

a Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

**See Also**

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

**Examples**

```
d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))  
x <- d %>% tfd_sample()  
d %>% tfd_log_prob(x)
```

---

**tfd_log_survival_function**

*Log survival function.*

**Description**

Given random variable $X$, the survival function is defined: 

$$
tfd_log_survival_function(x) = \log[P[X > x]] = \log[1 - P[X <= x]] = \log[1 - \text{cdf}(x)]
$$
**tfd_mean**

**Usage**

```r
tfd_log_survival_function(distribution, value, ...)
```

**Arguments**

- **distribution**
  - The distribution being used.
- **value**
  - float or double Tensor.
- **...**
  - Additional parameters passed to Python.

**Details**

Typically, different numerical approximations can be used for the log survival function, which are more accurate than 1 - cdf(x) when x >> 1.

**Value**

a Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

**See Also**

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

**Examples**

```r
d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
x <- d %>% tfd_sample()
d %>% tfd_log_survival_function(x)
```

---

**tfd_mean**

*Mean.*

**Description**

Mean.

**Usage**

```r
tfd_mean(distribution, ...)
```

**Arguments**

- **distribution**
  - The distribution being used.
- **...**
  - Additional parameters passed to Python.
Value

A Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

Examples

```r
  d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
  d %>% tfd_mean()
```

---

**tfd_mixture**

*Mixture distribution*

Description

The `tfd_mixture` object implements batched mixture distributions. The mixture model is defined by a `Categorical` distribution (the mixture) and a list of `Distribution` objects.

Usage

```r
  tfd_mixture(
    cat,
    components,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Mixture"
  )
```

Arguments

- `cat`  
  A `Categorical` distribution instance, representing the probabilities of distributions.

- `components`  
  A list or tuple of `Distribution` instances. Each instance must have the same type, be defined on the same domain, and have matching `event_shape` and `batch_shape`.

- `validate_args`  
  Logical, default `FALSE`. When `TRUE` distribution parameters are checked for validity despite possibly degrading runtime performance. When `FALSE` invalid inputs may silently render incorrect outputs. Default value: `FALSE`.

- `allow_nan_stats`  
  Logical, default `TRUE`. When `TRUE`, statistics (e.g., mean, mode, variance) use the value `NaN` to indicate the result is undefined. When `FALSE`, an exception is raised if one or more of the statistic’s batch members are undefined.

- `name`  
  Name prefixed to Ops created by this class.
**Details**

Methods supported include `tfd_log_prob`, `tfd_prob`, `tfd_mean`, `tfd_sample`, and `entropy_lower_bound`.

**Value**

A distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


**Description**

The `MixtureSameFamily` distribution implements a (batch of) mixture distribution where all components are from different parameterizations of the same distribution type. It is parameterized by a Categorical "selecting distribution" (over \( k \) components) and a components distribution, i.e., a Distribution with a rightmost batch shape (equal to \([k]\)) which indexes each (batch of) component.
tfd_mixture_same_family

Usage

tfd_mixture_same_family(
    mixture_distribution,
    components_distribution,
    reparameterize = FALSE,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "MixtureSameFamily"
)

Arguments

mixture_distribution
  tfp$distributions$Categorical-like instance. Manages the probability of selecting components. The number of categories must match the rightmost batch dimension of the components_distribution. Must have either scalar batch_shape or batch_shape matching components_distribution$batch_shape[:]

components_distribution
  tfp$distributions$Distribution-like instance. Right-most batch dimension indexes components.

reparameterize
  Logical, default FALSE. Whether to reparameterize samples of the distribution using implicit reparameterization gradients (Figurnov et al., 2018). The gradients for the mixture logits are equivalent to the ones described by (Graves, 2016). The gradients for the components parameters are also computed using implicit reparameterization (as opposed to ancestral sampling), meaning that all components are updated every step. Only works when: (1) components_distribution is fully reparameterized; (2) components_distribution is either a scalar distribution or fully factorized (tfd.Independent applied to a scalar distribution); (3) batch shape has a known rank. Experimental, may be slow and produce infs/NaNs.

validate_args
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
  name prefixed to Ops created by this class.

Value

a distribution instance.

References


**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

**tfd_mode**

**Mode.**

**Description**

Mode.

**Usage**

`tfd_mode(distribution, ...)`

**Arguments**

- `distribution` The distribution being used.
- `...` Additional parameters passed to Python.
Value

A Tensor of shape \( \text{sample_shape}() + \text{self$batch_shape} \) with values of type \( \text{self$dtype} \).

See Also

Other distribution methods: \( \text{tfd_cdf()} \), \( \text{tfd_covariance()} \), \( \text{tfd_cross_entropy()} \), \( \text{tfd_entropy()} \), \( \text{tfd_kl_divergence()} \), \( \text{tfd_log_cdf()} \), \( \text{tfd_log_prob()} \), \( \text{tfd_log_survival_function()} \), \( \text{tfd_mean()} \), \( \text{tfd_prob()} \), \( \text{tfd_quantile()} \), \( \text{tfd_sample()} \), \( \text{tfd_stddev()} \), \( \text{tfd_survival_function()} \), \( \text{tfd_variance()} \).

Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_mode()

---

tfd_multinomial  
Multinomial distribution

Description

This Multinomial distribution is parameterized by \( \text{probs} \), a (batch of) length-\( K \) prob (probability) vectors (\( K > 1 \)) such that \( \text{tf.reduce_sum(probs,-1)} = 1 \), and a \( \text{total_count} \) number of trials, i.e., the number of trials per draw from the Multinomial. It is defined over a (batch of) length-\( K \) vector counts such that \( \text{tf$reduce_sum(counts,-1)} = \text{total_count} \). The Multinomial is identically the Binomial distribution when \( K = 2 \).

Usage

tfd_multinomial(
  total_count,
  logits = NULL,
  probs = NULL,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Multinomial"
)

Arguments

total_count  
Non-negative floating point tensor with shape broadcastable to \([N_1, \ldots, N_m]\) with \( m \geq 0 \). Defines this as a batch of \( N_1 \times \ldots \times N_m \) different Multinomial distributions. Its components should be equal to integer values.

logits  
Floating point tensor representing unnormalized log-probabilities of a positive event with shape broadcastable to \([N_1, \ldots, N_m, K]\) \( m \geq 0 \), and the same dtype as \( \text{total_count} \). Defines this as a batch of \( N_1 \times \ldots \times N_m \) different \( K \) class Multinomial distributions. Only one of \( \text{logits} \) or \( \text{probs} \) should be passed in.
probs

Positive floating point tensor with shape broadcastable to \([N_1, ..., N_m, K]\) and same dtype as `total_count`. Defines this as a batch of \(N_1 \times ... \times N_m\) different \(K\) class Multinomial distributions. `probs`'s components in the last portion of its shape should sum to 1. Only one of `logits` or `probs` should be passed in.

`validate_args`

Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

`allow_nan_stats`

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

`name`

name prefixed to Ops created by this class.

Details

Mathematical Details

The Multinomial is a distribution over \(K\)-class counts, i.e., a length-\(K\) vector of non-negative integer counts \(n = [n_0, ..., n_{K-1}]\). The probability mass function (pmf) is,

\[
pmf(n; \pi, N) = \prod_j (\pi_j)^{n_j} / Z
\]

\[
Z = (\prod_j n_j!) / N!
\]

where:

- \(probs = \pi = [\pi_0, ..., \pi_{K-1}]\), \(\pi_j > 0\), \(\sum_j \pi_j = 1\),
- \(total\_count = N\), \(N\) a positive integer,
- \(Z\) is the normalization constant, and,
- \(N!\) denotes \(N\) factorial.

Distribution parameters are automatically broadcast in all functions; see examples for details.

Pitfalls

The number of classes, \(K\), must not exceed:

- the largest integer representable by \texttt{self$\text{dtype}$}, i.e., \(2^{(\text{mantissa\_bits+1})}\) (IEE754),
- the maximum Tensor index, i.e., \(2^{*31-1}\).

Note: This condition is validated only when `validate_args = TRUE`.

Value

a distribution instance.
tfd_multivariate_normal_diag

Multivariate normal distribution on \( \mathbb{R}^k \)

**Description**

The Multivariate Normal distribution is defined over \( \mathbb{R}^k \) and parameterized by a (batch of) length-
\( k \) loc vector (aka "\( \mu \)") and a (batch of) \( k \times k \) scale matrix; covariance = scale \( \times \) scale.T. Where \( \times \) denotes matrix-multiplication.

**Usage**

```r
  tfd_multivariate_normal_diag(
    loc = NULL,
    scale_diag = NULL,
    scale_identity_multiplier = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "MultivariateNormalDiag"
  )
```

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Arguments

loc
Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape \([B1, ..., Bb, k]\) where \(b \geq 0\) and \(k\) is the event size.

scale_diag
Non-zero, floating-point Tensor representing a diagonal matrix added to scale. May have shape \([B1, ..., Bb, k]\) where \(b \geq 0\) and characterizes \(b\)-batches of \(k \times k\) diagonal matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

scale_identity_multiplier
Non-zero, floating-point Tensor representing a scaled-identity-matrix added to scale. May have shape \([B1, ..., Bb]\) where \(b \geq 0\) and characterizes \(b\)-batches of scaled \(k \times k\) identity matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

name
name prefixed to Ops created by this class.

Details

Mathematical Details
The probability density function (pdf) is,

\[
\text{pdf}(x; \text{loc}, \text{scale}) = \exp(-0.5 \ ||y||^2) / Z \\
y = \text{inv}(\text{scale}) @ (x - \text{loc}) \\
Z = (2 \pi)^{0.5 \times k} |\text{det}(\text{scale})|
\]

where:

- \(\text{loc}\) is a vector in \(\mathbb{R}^k\),
- \(\text{scale}\) is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} \otimes \text{scale}.T\),
- \(Z\) denotes the normalization constant, and,
- \(||y||^2\) denotes the squared Euclidean norm of \(y\).

A (non-batch) scale matrix is:

\[
\text{scale} = \text{diag}(\text{scale_diag} + \text{scale_identity_multiplier} \times \text{ones}(k))
\]

where:

- \(\text{scale_diag}\).shape = \([k]\), and,
- \(\text{scale_identity_multiplier}.\text{shape} = [].\)
The Multivariate Normal distribution is defined over \( \mathbb{R}^k \) and parameterized by a (batch of) length-\( k \) loc vector (aka "\( \mu \)"), and a (batch of) \( k \times k \) scale matrix; covariance = scale @ scale.T. Where @ denotes matrix-multiplication.
tfd_multivariate_normal_diag_plus_low_rank

Usage

tfd_multivariate_normal_diag_plus_low_rank(
  loc = NULL,
  scale_diag = NULL,
  scale_identity_multiplier = NULL,
  scale_perturb_factor = NULL,
  scale_perturb_diag = NULL,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "MultivariateNormalDiagPlusLowRank"
)

Arguments

loc
  Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified,
  may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

scale_diag
  Non-zero, floating-point Tensor representing a diagonal matrix added to scale.
  May have shape [B1, ..., Bb, k], b >= 0, and characterizes b-batches of k x k
  diagonal matrices added to scale. When both scale_identity_multiplier and
  scale_diag are NULL then scale is the Identity.

scale_identity_multiplier
  Non-zero, floating-point Tensor representing a scaled-identity-matrix added to
  scale. May have shape [B1, ..., Bb, k, b >= 0, and characterizes b-batches of scaled
  k x k identity matrices added to scale. When both scale_identity_multiplier and
  scale_diag are NULL then scale is the Identity.

scale_perturb_factor
  Floating-point Tensor representing a rank-r perturbation added to scale. May
  have shape [B1, ..., Bb, k, r], b >= 0, and characterizes b-batches of rank-r up-
  dates to scale. When NULL, no rank-r update is added to scale.

scale_perturb_diag
  Floating-point Tensor representing a diagonal matrix inside the rank-r perturba-
  tion added to scale. May have shape [B1, ..., Bb, r], b >= 0, and characterizes b-batches of r x r
  diagonal matrices inside the perturbation added to scale. When NULL, an identity matrix is used inside the perturbation. Can only be
  specified if scale_perturb_factor is also specified.

validate_args
  Logical, default FALSE. When TRUE distribution parameters are checked for
  validity despite possibly degrading runtime performance. When FALSE invalid
  inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
  the value NaN to indicate the result is undefined. When FALSE, an exception is
  raised if one or more of the statistic’s batch members are undefined.

name
  name prefixed to Ops created by this class.

Details

Mathematical Details
The probability density function (pdf) is,

\[
\text{pdf}(x; \text{loc}, \text{scale}) = \exp(-0.5 \ ||y||^2) / Z \\
y = \text{inv}(\text{scale}) @ (x - \text{loc}) \\
Z = (2 \pi)^{0.5k} |\det(\text{scale})|
\]

where:

- \text{loc} is a vector in \(\mathbb{R}^k\),
- \text{scale} is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} @ \text{scale}.T\),
- \(Z\) denotes the normalization constant, and,
- \(||y||^2\) denotes the squared Euclidean norm of \(y\).

A (non-batch) scale matrix is:

\[
\text{scale} = \text{diag}(\text{scale\_diag} + \text{scale\_identity\_multiplier \ ones(k)}) + \\
\text{scale\_perturb\_factor} @ \text{diag}(\text{scale\_perturb\_diag}) @ \text{scale\_perturb\_factor}.T
\]

where:

- \text{scale\_diag\_shape} = [k],
- \text{scale\_identity\_multiplier\_shape} = [],
- \text{scale\_perturb\_factor\_shape} = [k, r], typically \(k \gg r\), and,
- \text{scale\_perturb\_diag\_shape} = [r].

Additional leading dimensions (if any) will index batches. If both \text{scale\_diag} and \text{scale\_identity\_multiplier} are \text{NULL}, then \text{scale} is the Identity matrix. The MultivariateNormal distribution is a member of the \text{location-scale family}, i.e., it can be constructed as,

\[
X \sim \text{MultivariateNormal}(\text{loc}=0, \text{scale}=1) \quad \# \text{Identity scale, zero shift.} \\
Y = \text{scale} @ X + \text{loc}
\]

\text{Value}

a distribution instance.

\text{See Also}

For usage examples see e.g. \text{tfd\_sample()}, \text{tfd\_log\_prob()}, \text{tfd\_mean()}.

Other distributions: \text{tfd\_autoregressive()}, \text{tfd\_batch\_reshape()}, \text{tfd\_bates()}, \text{tfd\_bernoulli()}, \text{tfd\_beta\_binomial()}, \text{tfd\_beta()}, \text{tfd\_binomial()}, \text{tfd\_categorical()}, \text{tfd\_cauchy()}, \text{tfd\_chi2()}, \text{tfd\_chi()}, \text{tfd\_cholesky\_lkj()}, \text{tfd\_continuous\_bernoulli()}, \text{tfd\_deterministic()}, \text{tfd\_dirichlet\_multinomial()}, \text{tfd\_dirichlet()}, \text{tfd\_empirical()}, \text{tfd\_exp\_gamma()}, \text{tfd\_exp\_inverse\_gamma()}, \text{tfd\_exponential()}, \text{tfd\_gamma\_gamma()}, \text{tfd\_gamma()}, \text{tfd\_gaussian\_process\_regression\_model()}, \text{tfd\_gaussian\_process()}, \text{tfd\_generalized\_normal()}, \text{tfd\_geometric()}, \text{tfd\_gumbel()}, \text{tfd\_half\_cauchy()}, \text{tfd\_half\_normal()}, \text{tfd\_hidden\_markov\_model()}, \text{tfd\_horseshoe()}, \text{tfd\_independent()}, \text{tfd\_inverse\_gamma()}, \text{tfd\_inverse\_gaussian()}, \text{tfd\_johnson\_s\_u()}, \text{tfd\_joint\_distribution\_named\_auto\_batched()}, \text{tfd\_joint\_distribution\_named()}, \text{tfd\_joint\_distribution\_sequential\_auto\_batched()}, \text{tfd\_joint\_distribution\_sequential()}, \text{tfd\_kumaraswamy()}, \text{tfd\_laplace()}, \text{tfd\_linear\_gaussian\_state\_space\_model\_auto\_batched()}, \text{tfd\_linear\_gaussian\_state\_space\_model\_sequential\_auto\_batched()}, \text{tfd\_linear\_gaussian\_state\_space\_model\_sequential()}.
Multivariate normal distribution on $\mathbb{R}^k$

**Description**

The Multivariate Normal distribution is defined over $\mathbb{R}^k$ and parameterized by a (batch of) length-$k$ loc vector (aka "mu") and a (batch of) $k \times k$ scale matrix; covariance = scale @ scale. Where @ denotes matrix-multiplication.

**Usage**

tfd_multivariate_normal_full_covariance(  
  loc = NULL,  
  covariance_matrix = NULL,  
  validate_args = FALSE,  
  allow_nan_stats = TRUE,  
  name = "MultivariateNormalFullCovariance"
)

**Arguments**

- **loc**
  
  Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

- **covariance_matrix**
  
  Floating-point, symmetric positive definite Tensor of same dtype as loc. The strict upper triangle of covariance_matrix is ignored, so if covariance_matrix is not symmetric no error will be raised (unless validate_args is TRUE). covariance_matrix has shape [B1, ..., Bb, k, k] where b >= 0 and k is the event size.

- **validate_args**
  
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

Mathematical Details
The probability density function (pdf) is,

\[
pdf(x; \text{loc}, \text{scale}) = \exp(-0.5 ||y||^2) / Z
\]

\[
y = \text{inv}(\text{scale}) \odot (x - \text{loc})
\]

\[
Z = (2 \pi)^{0.5 k} |\det(\text{scale})|
\]

where:

- \text{loc} is a vector in \(\mathbb{R}^k\),
- \text{scale} is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} \odot \text{scale}^T\),
- \(Z\) denotes the normalization constant, and,
- ||y||^2 denotes the squared Euclidean norm of \(y\).

The MultivariateNormal distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X \sim \text{MultivariateNormal}(\text{loc}=0, \text{scale}=1) \quad \# \text{Identity scale, zero shift.}
\]

\[
Y = \text{scale} \odot X + \text{loc}
\]

The batch_shape is the broadcast shape between \text{loc} and \text{covariance_matrix} arguments. The event_shape is given by last dimension of the matrix implied by \text{covariance_matrix}. The last dimension of \text{loc} (if provided) must broadcast with this. A non-batch \text{covariance_matrix} matrix is a \(k \times k\) symmetric positive definite matrix. In other words it is (real) symmetric with all eigenvalues strictly positive. Additional leading dimensions (if any) will index batches.

Value

a distribution instance.

See Also

For usage examples see e.g. \text{tfd_sample()}, \text{tfd_log_prob()}, \text{tfd_mean()}.

Other distributions: \text{tfd_autoregressive()}, \text{tfd_batch_reshape()}, \text{tfd_bates()}, \text{tfd_bernoulli()}, \text{tfd_beta_binomial()}, \text{tfd_beta()}, \text{tfd_binomial()}, \text{tfd_categorical()}, \text{tfd_cauchy()}, \text{tfd_chisquare()}, \text{tfd_cholesky_lkj()}, \text{tfd_continuous_bernoulli()}, \text{tfd_deterministic()}, \text{tfd_dirichlet_multinomial()}, \text{tfd_dirichlet()}, \text{tfd_empirical()}, \text{tfd_exp_gamma()}, \text{tfd_exp_inverse_gamma()}, \text{tfd_exponential()}, \text{tfd_gamma_gamma()}, \text{tfd_gamma()}, \text{tfd_gaussian_process_regression_model()}, \text{tfd_gaussian_process()}, \text{tfd_generalized_normal()}, \text{tfd_geometric()}, \text{tfd_gumbel()}, \text{tfd_half_cauchy()}, \text{tfd_half_normal()}, \text{tfd_hidden_markov_model()}, \text{tfd_horseshoe()}, \text{tfd_independent()}, \text{tfd_inverse_gaussian()}, \text{tfd_inverse_gaussian()}, \text{tfd_johnson_s_u()}, \text{tfd_joint_distribution_named_auto_batched}().
tfd_multivariate_normal_linear_operator 

The multivariate normal distribution on R^k 

**Description**

The Multivariate Normal distribution is defined over R^k and parameterized by a (batch of) length-k loc vector (aka "mu") and a (batch of) k x k scale matrix; covariance = scale @ scale.T where @ denotes matrix-multiplication.

**Usage**

tfd_multivariate_normal_linear_operator(
    loc = NULL,
    scale = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "MultivariateNormalLinearOperator"
)

**Arguments**

- **loc**
  Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1,...,Bb,k] where b >= 0 and k is the event size.

- **scale**
  Instance of LinearOperator with same dtype as loc and shape [B1,...,Bb,k,k].

- **validate_args**
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **allow_nan_stats**
  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
name

name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
\begin{align*}
\text{pdf}(x; \text{loc}, \text{scale}) &= \exp(-0.5 ||y||^2) / Z \\
y &= \text{inv(scale)} @ (x - \text{loc}) \\
Z &= (2 \pi)^{0.5 k} |\det(\text{scale})|
\end{align*}
\]

where:

- \(\text{loc}\) is a vector in \(\mathbb{R}^k\),
- \(\text{scale}\) is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} @ \text{scale}.T\),
- \(Z\) denotes the normalization constant, and,
- \(||y||^2\) denotes the squared Euclidean norm of \(y\).

The MultivariateNormal distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X \sim \text{MultivariateNormal}(\text{loc} = \text{zero}, \text{scale} = 1) \quad \# \text{Identity scale, zero shift.}
Y = \text{scale} @ X + \text{loc}
\]

The batch_shape is the broadcast shape between loc and scale arguments. The event_shape is given by last dimension of the matrix implied by scale. The last dimension of loc (if provided) must broadcast with this. Recall that covariance = scale @ scale.T. Additional leading dimensions (if any) will index batches.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_dirichlet(), tfd_empirical(), tfd_exp gamle(), tfd_exp_inverse_gam me(), tfd_exponential(),
tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gam me(),
tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(),
tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),
tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space,
tfd_lkj(), tfd_log_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixt ure_same_family(),
tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_full_cova riance(), tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t,
The multivariate normal distribution on $\mathbb{R}^k$

Description

The Multivariate Normal distribution is defined over $\mathbb{R}^k$ and parameterized by a (batch of) length-\(k\) loc vector (aka "mu") and a (batch of) \(k \times k\) scale matrix; covariance = scale @ scale.T where @ denotes matrix-multiplication.

Usage

tfd_multivariate_normal_tri_l(
  loc = NULL,
  scale_tril = NULL,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "MultivariateNormalTriL"
)

Arguments

loc Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

scale_tril Floating-point, lower-triangular Tensor with non-zero diagonal elements. scale_tril has shape [B1, ..., Bb, k, k] where b >= 0 and k is the event size.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.
Details

Mathematical Details

The probability density function (pdf) is,

$$
\text{pdf}(x; \text{loc}, \text{scale}) = \exp\left(-0.5 \ ||y||^2\right) / Z \\
y = \text{inv}(\text{scale}) @ (x - \text{loc}) \\
Z = (2 \pi)^{0.5 \ k} |\det(\text{scale})|
$$

where:

- $\text{loc}$ is a vector in $\mathbb{R}^k$,
- $\text{scale}$ is a linear operator in $\mathbb{R}^{k \times k}$, $\text{cov} = \text{scale} @ \text{scale}.T$,
- $Z$ denotes the normalization constant, and,
- $||y||^2$ denotes the squared Euclidean norm of $y$.

A (non-batch) scale matrix is:

$$
\text{scale} = \text{scale}_{\text{tril}}
$$

where $\text{scale}_{\text{tril}}$ is lower-triangular $k \times k$ matrix with non-zero diagonal, i.e., $\text{tf}$$\text{diag}_\text{part}(\text{scale}_{\text{tril}}) \neq 0$. Additional leading dimensions (if any) will index batches.

The MultivariateNormal distribution is a member of the location-scale family, i.e., it can be constructed as,

$$
X \sim \text{MultivariateNormal}(\text{loc}=0, \text{scale}=1) \quad \# \text{Identity scale, zero shift.} \\
Y = \text{scale} @ X + \text{loc}
$$

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_multivariate_student_t_linear_operator

Multivariate Student's t-distribution on \( \mathbb{R}^k \)

Description

Mathematical Details

Usage

tfd_multivariate_student_t_linear_operator(
    df,
    loc,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "MultivariateStudentTLinearOperator"
)

Arguments

df
A positive floating-point Tensor. Has shape \([B_1, ..., B_b]\) where \(b \geq 0\).

loc
Floating-point Tensor. Has shape \([B_1, ..., B_b, k]\) where \(k\) is the event size.

scale
Instance of LinearOperator with a floating dtype and shape \([B_1, ..., B_b, k, k]\).

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.
Details

The probability density function (pdf) is,

$$pdf(x; df, loc, Sigma) = \frac{1 + ||y||^2 / df}{Z}$$

where,

$$y = \text{inv}(Sigma) (x - loc)$$

$$Z = \text{abs}(\text{det}(Sigma)) \sqrt{df \pi}^k \frac{\Gamma(0.5 df)}{\Gamma(0.5 (df + k))}$$

where:

- $df$ is a positive scalar.
- $loc$ is a vector in $\mathbb{R}^k$.
- $Sigma$ is a positive definite shape matrix in $\mathbb{R}^{k \times k}$, parameterized as $\text{scale} @ \text{scale}.T$ in this class.
- $Z$ denotes the normalization constant, and,
- $||y||^2$ denotes the squared Euclidean norm of $y$.

The Multivariate Student's t-distribution distribution is a member of the location-scale family, i.e., it can be constructed as,

$$X \sim \text{MultivariateT}(loc=0, scale=1) \quad \# \text{Identity scale, zero shift.}$$

$$Y = \text{scale} @ X + loc$$

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions:
- `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`,
- `tfd_beta_bimomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`,
- `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`,
- `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`,
- `tfd_gamma_gamma()`, `tfd_gamma()`, `tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`,
- `tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`,
- `tfd_hidden_markov_model()`, `tfd_horseshoe()`, `tfd_independent()`,
- `tfd_inverse_gaussian()`, `tfd_johnson_s_u()`, `tfd_joint_distribution_named_auto_batched()`,
- `tfd_joint_distribution_named()`, `tfd_joint_distribution_sequential_auto_batched()`,
- `tfd_joint_distribution_sequential()`, `tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`,
- `tfd_lkj()`, `tfd_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_mixture_same_family()`,
- `tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal_diag()`,
- `tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`,
- `tfd_multivariate_normal_tri_l()`, `tfd_negative_binomial()`, `tfd_normal()`, `tfd_one_hot_categorical()`,
- `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_compound()`, `tfd_poisson()`,
- `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`,
- `tfd_relaxed_one_hot_categorical()`, `tfd_sample_distribution()`, `tfd_sinh_arcsinh()`,
- `tfd_skellam()`, `tfd_spherical_uniform()`, `tfd_student_t_process()`, `tfd_student_t()`, `tfd_transformed_distribution()`.
tfd_negative_binomial

Description

The NegativeBinomial distribution is related to the experiment of performing Bernoulli trials in sequence. Given a Bernoulli trial with probability $p$ of success, the NegativeBinomial distribution represents the distribution over the number of successes $s$ that occur until we observe $f$ failures.

Usage

```r

```tfd_negative_binomial(`total_count`,
logits = NULL,
probs = NULL,
validate_args = FALSE,
allow_nan_stats = TRUE,
name = "NegativeBinomial"
)

Arguments

- **total_count**: Non-negative floating-point Tensor with shape broadcastable to `[B1,..., Bb]` with `b >= 0` and the same dtype as `probs` or `logits`. Defines this as a batch of `N1 x ... x Nm` different Negative Binomial distributions. In practice, this represents the number of negative Bernoulli trials to stop at (the `total_count` of failures), but this is still a valid distribution when `total_count` is a non-integer.
- **logits**: Floating-point Tensor with shape broadcastable to `[B1, ..., Bb]` where `b >= 0` indicates the number of batch dimensions. Each entry represents logits for the probability of success for independent Negative Binomial distributions and must be in the open interval (-inf, inf). Only one of `logits` or `probs` should be specified.
- **probs**: Positive floating-point Tensor with shape broadcastable to `[B1, ..., Bb]` where `b >= 0` indicates the number of batch dimensions. Each entry represents the probability of success for independent Negative Binomial distributions and must be in the open interval (0, 1). Only one of `logits` or `probs` should be specified.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
The probability mass function (pmf) is,
\[ \text{pmf}(s; f, p) = p^s (1 - p)^f / Z \]
\[ Z = s! (f - 1)! / (s + f - 1)! \]
where:
- \( \text{total_count} = f \),
- \( \text{probs} = p \),
- \( Z \) is the normalizing constant, and,
- \( n! \) is the factorial of \( n \).

Value
a distribution instance.

See Also
For usage examples see e.g. \( \text{tfd_sample()} \), \( \text{tfd_log_prob()} \), \( \text{tfd_mean()} \).
Other distributions: \( \text{tfd_autoregressive()} \), \( \text{tfd_batch_reshape()} \), \( \text{tfd_bates()} \), \( \text{tfd_bernoulli()} \),
\( \text{tfd_beta_binomial()} \), \( \text{tfd_beta()} \), \( \text{tfd_binomial()} \), \( \text{tfd_categorical()} \), \( \text{tfd_cauchy()} \), \( \text{tfd_chi2()} \),
\( \text{tfd_cholesky_lkj()} \), \( \text{tfd_continuous_bernoulli()} \), \( \text{tfd_deterministic()} \), \( \text{tfd_dirichlet()} \), \( \text{tfd_dirichlet_multinomial()} \),
\( \text{tfd_empirical()} \), \( \text{tfd_exp()} \), \( \text{tfd_exp_inverse()} \), \( \text{tfd_exponential()} \),
\( \text{tfd_gamma()} \), \( \text{tfd_gaussian_process()} \), \( \text{tfd_gaussian_process_regression_model()} \), \( \text{tfd_gamma_gamm()} \), \( \text{tfd_geometric()} \), \( \text{tfd_half_cauchy()} \), \( \text{tfd_half_normal()} \),
\( \text{tfd_hidden_markov_model()} \), \( \text{tfd_horseshoe()} \), \( \text{tfd_independent()} \), \( \text{tfd_inverse()} \),
\( \text{tfd_inverse_gaussian()} \), \( \text{tfd_johnson_s_u()} \), \( \text{tfd_joint_distribution_named()} \), \( \text{tfd_joint_distribution_named_auto_batched()} \),
\( \text{tfd_joint_distribution_sequential()} \), \( \text{tfd_kumaraswamy()} \), \( \text{tfd_laplace()} \), \( \text{tfd_linear_gaussian_state_space_model()} \),
\( \text{tfd_lkj()} \), \( \text{tfd_logistic()} \), \( \text{tfd_log_normal()} \), \( \text{tfd_logic()} \), \( \text{tfd_mixture_same_family()} \),
\( \text{tfd_mixture()} \), \( \text{tfd_multinomial()} \), \( \text{tfd_multivariate_normal_diag_plus_low_rank()} \), \( \text{tfd_multivariate_normal_full_c covariance()} \), \( \text{tfd_multivariate_normal_linear_operator()} \),
\( \text{tfd_one_hot_categorical()} \), \( \text{tfd_pareto()} \), \( \text{tfd_pixel_cnn()} \), \( \text{tfd_poisson_log_normal_quadrature_compound()} \),
\( \text{tfd_poisson()} \), \( \text{tfd_power_spherical()} \), \( \text{tfd_probit_bernoulli()} \), \( \text{tfd_quantized()} \), \( \text{tfd_relaxed_bernoulli()} \),
\( \text{tfd_relaxed_one_hot_categorical()} \), \( \text{tfd_sample_distribution()} \), \( \text{tfd_sinh_arcsinh()} \),
\( \text{tfd_skellam()} \), \( \text{tfd_spherical_uniform()} \), \( \text{tfd_student_t_process()} \), \( \text{tfd_student_t()} \), \( \text{tfd_transformed_distribution()} \),
\( \text{tfd_triangular()} \), \( \text{tfd_truncated_cauchy()} \), \( \text{tfd_truncated_normal()} \), \( \text{tfd_uniform()} \), \( \text{tfd_variational_gaussian()} \),
\( \text{tfd_vector_diffeomixture()} \), \( \text{tfd_vector_exponential_diag()} \), \( \text{tfd_vector_exponential_linear_operator()} \),
\( \text{tfd_vector_laplace_diag()} \), \( \text{tfd_vector_laplace_linear_operator()} \), \( \text{tfd_vector_sinh_arcsinh()} \),
\( \text{tfd_von_mises_fisher()} \), \( \text{tfd_von_mises()} \), \( \text{tfd_weibull()} \), \( \text{tfd_wishart_linear_operator()} \),
\( \text{tfd_wishart_tri_l()} \), \( \text{tfd_wishart()} \), \( \text{tfd_zipf()} \)
**tfd_normal**  
Normal distribution with loc and scale parameters

### Description
Mathematical details

### Usage
```
tfd_normal(  
  loc,  
  scale,  
  validate_args = FALSE,  
  allow_nan_stats = TRUE,  
  name = "Normal"  
)
```

### Arguments
- **loc**: Floating point tensor; the means of the distribution(s).
- **scale**: Floating point tensor; the stddevs of the distribution(s). Must contain only positive values.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

### Details
The probability density function (pdf) is,

```
pdf(x; mu, sigma) = exp(-0.5 (x - mu)**2 / sigma**2) / Z  
Z = (2 pi sigma**2)**0.5  
```

where loc = mu is the mean, scale = sigma is the std. deviation, and, Z is the normalization constant. The Normal distribution is a member of the location-scale family, i.e., it can be constructed as,

```
X ~ Normal(loc=0, scale=1)  
Y = loc + scale * X  
```
Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


tfd_one_hot_categorical

OneHotCategorical distribution

Description

The categorical distribution is parameterized by the log-probabilities of a set of classes. The difference between OneHotCategorical and Categorical distributions is that OneHotCategorical is a discrete distribution over one-hot bit vectors whereas Categorical is a discrete distribution over positive integers. OneHotCategorical is equivalent to Categorical except Categorical has event_dim=() while OneHotCategorical has event_dim=K, where K is the number of classes.

Usage

tfd_one_hot_categorical(
    logits = NULL,
tfd_one_hot_categorical

probs = NULL,
dtype = tf
$\text{int32},$
validate_args = FALSE,
allow_nan_stats = TRUE,
name = "OneHotCategorical"
)

Arguments

logits
An N-D Tensor, $N \geq 1$, representing the log probabilities of a set of Categorical distributions. The first $N - 1$ dimensions index into a batch of independent distributions and the last dimension represents a vector of logits for each class. Only one of logits or probs should be passed in.

probs
An N-D Tensor, $N \geq 1$, representing the probabilities of a set of Categorical distributions. The first $N - 1$ dimensions index into a batch of independent distributions and the last dimension represents a vector of probabilities for each class. Only one of logits or probs should be passed in.

dtype
The type of the event samples (default: int32).

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

This class provides methods to create indexed batches of OneHotCategorical distributions. If the provided logits or probs is rank 2 or higher, for every fixed set of leading dimensions, the last dimension represents one single OneHotCategorical distribution. When calling distribution functions (e.g. dist.prob(x)), logits and x are broadcast to the same shape (if possible). In all cases, the last dimension of logits, x represents single OneHotCategorical distributions.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal().
tfd_pareto

Pareto distribution

Description

The Pareto distribution is parameterized by a scale and a concentration parameter.

Usage

tfd_pareto(
    concentration,
    scale = 1,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Pareto"
)

Arguments

concentration
    Floating point tensor. Must contain only positive values.

scale
    Floating point tensor, equivalent to mode. scale also restricts the domain of
    this distribution to be in [scale, inf). Must contain only positive values. Default
    value: 1.

validate_args
    Logical, default FALSE. When TRUE distribution parameters are checked for
    validity despite possibly degrading runtime performance. When FALSE invalid
    inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
pdf(x; \alpha, \text{scale}, x \geq \text{scale}) = \alpha \times \text{scale}^{\alpha} / x^{(\alpha + 1)}
\]

where \(\text{concentration} = \alpha\).

Note that \(\text{scale}\) acts as a scaling parameter, since

\(\text{Pareto}(c, \text{scale}).pdf(x) = \text{Pareto}(c, 1.).pdf(x / \text{scale})\).

The support of the distribution is defined on \([\text{scale}, \infty)\).

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(),
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),
tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(),
tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),
tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(),
tfd_lkj(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_multinomial(),
tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_full_covariance(),
tfd_multivariate_normal_linear_operator(),
tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature_compound(),
tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sin_arcsinh(),
tfd_skelam(), tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(),
tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_von_mises(),
tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(),
tfd_vector_laplace_diagonal(), tfd_vector_laplace_linear_operator(), tfd_vector_student_t_linear_operator(),
tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(),
tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
The PERT distribution is a loc-scale family of Beta distributions fit onto a real interval between low and high values set by the user, along with a peak to indicate the expert’s most frequent prediction, and temperature to control how sharp the peak is.

Usage
```r
tfd_pert(
  low,
  peak,
  high,
  temperature = 4,
  validate_args = FALSE,
  allow_nan_stats = FALSE,
  name = "Pert"
)
```

Arguments
- **low**: lower bound
- **peak**: most frequent value
- **high**: upper bound
- **temperature**: controls the shape of the distribution
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details
The distribution is similar to a Triangular distribution (i.e. `tfd.Triangular`) but with a smooth peak.

Mathematical Details
In terms of a Beta distribution, PERT can be expressed as

\[
\text{PERT} \sim \text{loc} + \text{scale} * \text{Beta(\text{concentration}_1, \text{concentration}_0)}
\]
where

\begin{align*}
\text{loc} &= \text{low} \\
\text{scale} &= \text{high} - \text{low} \\
\text{concentration}_1 &= 1 + \text{temperature} \times (\text{peak} - \text{low}) / (\text{high} - \text{low}) \\
\text{concentration}_0 &= 1 + \text{temperature} \times (\text{high} - \text{peak}) / (\text{high} - \text{low}) \\
\text{temperature} &> 0
\end{align*}

The support is $[\text{low}, \text{high}]$. The peak must fit in that interval: $\text{low} < \text{peak} < \text{high}$. The temperature is a positive parameter that controls the shape of the distribution. Higher values yield a sharper peak. The standard PERT distribution is obtained when $\text{temperature} = 4$.

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_pixel_cnn

The Pixel CNN++ distribution

Description

Pixel CNN++ (Salimans et al., 2017) models a distribution over image data, parameterized by a neural network. It builds on Pixel CNN and Conditional Pixel CNN, as originally proposed by (van den Oord et al., 2016). The model expresses the joint distribution over pixels as the product of conditional distributions: $p(x|h) = \prod \{ p(x[i] | x[0:i], h) : i = 0, ..., d \}$, in which $p(x[i] | x[0:i], h) : i = 0, ..., d$ is the probability of the $i$-th pixel conditional on the pixels that preceded it in raster order (color channels in RGB order, then left to right, then top to bottom). $h$ is optional additional data on which to condition the image distribution, such as class labels or VAE embeddings. The Pixel CNN++ network enforces the dependency structure among pixels by applying a mask to the kernels of the convolutional layers that ensures that the values for each pixel depend only on other pixels up and to the left. Pixel values are modeled with a mixture of quantized logistic distributions, which can take on a set of distinct integer values (e.g. between 0 and 255 for an 8-bit image). Color intensity $v$ of each pixel is modeled as: $v \sim \sum q[i] \times \text{quantized_logistic(loc[i], scale[i]) : i = 0, ..., k}$, in which $k$ is the number of mixture components and the $q[i]$ are the Categorical probabilities over the components.

Usage

tfd_pixel_cnn(
    image_shape,
    conditional_shape = NULL,
    num_resnet = 5,
    num_hierarchies = 3,
num_filters = 160,
num_logistic_mix = 10,
receptive_field_dims = c(3, 3),
dropout_p = 0.5,
resnet_activation = "concat_elu",
use_weight_norm = TRUE,
use_data_init = TRUE,
high = 255,
low = 0,
dtype = tf$float32,
name = "PixelCNN"
)

Arguments

image_shape 3D TensorShape or tuple for the [height, width, channels] dimensions of the image.
conditional_shape TensorShape or tuple for the shape of the conditional input, or NULL if there is no conditional input.
num_resnet integer, the number of layers (shown in Figure 2 of https://arxiv.org/abs/1606.05328) within each highest-level block of Figure 2 of https://pdfs.semanticscholar.org/9e90/6792f67cbdda7b7777b69284a81044857656.pdf.
num_hierarchies integer, the number of highest-level blocks (separated by expansions/contractions of dimensions in Figure 2 of https://pdfs.semanticscholar.org/9e90/6792f67cbdda7b7777b69284a81044857656.pdf.)
num_filters integer, the number of convolutional filters.
num_logistic_mix integer, number of components in the logistic mixture distribution.
receptive_field_dims tuple, height and width in pixels of the receptive field of the convolutional layers above and to the left of a given pixel. The width (second element of the tuple) should be odd. Figure 1 (middle) of https://arxiv.org/abs/1606.05328 shows a receptive field of (3, 5) (the row containing the current pixel is included in the height). The default of (3, 3) was used to produce the results in https://pdfs.semanticscholar.org/9e90/6792f67cbdda7b7777b69284a81044857656.pdf.
dropout_p float, the dropout probability. Should be between 0 and 1.
resnet_activation string, the type of activation to use in the resnet blocks. May be 'concat_elu', 'elu', or 'relu'.
use_weight_norm logical, if TRUE then use weight normalization (works only in Eager mode).
use_data_init logical, if TRUE then use data-dependent initialization (has no effect if use_weight_norm is FALSE).
high integer, the maximum value of the input data (255 for an 8-bit image).
low integer, the minimum value of the input data.
dtype Data type of the Distribution.
name string, the name of the Distribution.
tfd_plackett_luce

Value

a distribution instance.

References


See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`,
`tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`,
`tfd_chi()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet()`,
`tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`,
`tfd_exp_normal()`, `tfd_exp_gamma()`, `tfd_exp_polygamma()`, `tfd_exp_tanh()`,
`tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`,
`tfd_half_normal()`, `tfd_hidden_markov_model()`, `tfd_horseshoe()`, `tfd_independent()`,
`tfd_inverse_normal()`, `tfd_inverse_gaussian()`, `tfd_johnson_s()`,
`tfd_joint_distribution_named_auto_batched()`, `tfd_joint_distribution_named()`,
`tfd_joint_distribution_sequential_auto_batched()`, `tfd_joint_distribution_sequential()`,
`tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`,
`tfd_lkj()`, `tfd_log_logistic()`, `tfd_log_normal()`, `tfd_logistic()`,
`tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`,
`tfd_multivariate_normal_diag()`, `tfd_multivariate_normal_full_covariance()`,
`tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_normal_tri_l()`,
`tfd_multivariate_student_t_linear_operator()`, `tfd_negative_binomial()`,
`tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_poisson_log_normal_quadrature_compound()`,
`tfd_poisson()`, `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`,
`tfd_relaxed_bernoulli()`, `tfd_relaxed_one_hot_categorical()`,
`tfd_sample_distribution()`, `tfd_sinh_arcsinh()`, `tfd_skellam()`,
`tfd_spherical_uniform()`, `tfd_student_t()`, `tfd_student_t_process()`,
`tfd_transformed_distribution()`, `tfd_triangular()`, `tfd_truncated_cauchy()`,
`tfd_truncated_normal()`, `tfd_uniform()`, `tfd_von_mises()`,
`tfd_vector_diffeomixture()`, `tfd_vector_exponential_diag()`,
`tfd_vector_exponential_linear_operator()`, `tfd_vector_laplace_diag()`,
`tfd_vector_laplace_linear_operator()`, `tfd_vector_sinh_arcsinh()`,
`tfd_von_mises_fisher()`, `tfd_wishart()`, `tfd_weibull()`, `tfd_wishart_linear_operator()`,
`tfd_wishart_tri_l()`, `tfd_wishart()`, `tfd_zipf()`
Description

The Plackett-Luce distribution is defined over permutations of fixed length. It is parameterized by a positive score vector of same length. This class provides methods to create indexed batches of PlackettLuce distributions. If the provided scores is rank 2 or higher, for every fixed set of leading dimensions, the last dimension represents one single PlackettLuce distribution. When calling distribution functions (e.g. dist.log_prob(x)), scores and x are broadcast to the same shape (if possible). In all cases, the last dimension of scores, x represents single PlackettLuce distributions.

Usage

tfd_plackett_luce(
  scores,
  dtype = tf$int32,
  validate_args = FALSE,
  allow_nan_stats = FALSE,
  name = "PlackettLuce"
)

Arguments

scores An N-D Tensor, N >= 1, representing the scores of a set of elements to be permuted. The first N -1 dimensions index into a batch of independent distributions and the last dimension represents a vector of scores for the elements.
dtype The type of the event samples (default: int32).
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
name name prefixed to Ops created by this class.

Details

Mathematical Details

The Plackett-Luce is a distribution over permutation vectors p of length k where the permutation p is an arbitrary ordering of k indices {0, 1, ..., k-1}.

The probability mass function (pmf) is,

\[ p \text{mf}(p; s) = \prod_i s_{p_i} / (Z - Z_i) \]

\[ Z = \sum_{j=0}^{k-1} s_j \]

\[ Z_i = \sum_{j=0}^{i-1} s_{p_j} \text{ for } i>0 \text{ and } 0 \text{ for } i=0 \]

where scores = s = [s_0, ..., s_{k-1}], s_i >= 0.

Samples from Plackett-Luce distribution are generated sequentially as follows.
Initialize normalization $N_0 = Z$
For $i$ in $\{0, 1, \ldots, k-1\}$
  1. Sample $i$-th element of permutation
     $p_i \sim \text{Categorical(probs=[s_0/N_i, \ldots, s_{k-1}/N_i])}$
  2. Update normalization
     $N_{i+1} = N_i - s_{p_i}$
  3. Mask out sampled index for subsequent rounds
     $s_{p_i} = 0$
Return $p$

Alternately, an equivalent way to sample from this distribution is to sort Gumbel perturbed log-scores (Aditya et al. 2019)

\[ p = \text{argsort}(\log s + g) \sim \text{PlackettLuce(s)} \]
\[ g = [g_0, \ldots, g_{k-1}], g_i \sim \text{Gumbel}(0, 1) \]

Value

a distribution instance.

References


See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

---

tfd_poisson  

<table>
<thead>
<tr>
<th>Poisson distribution</th>
</tr>
</thead>
</table>

Description

The Poisson distribution is parameterized by an event rate parameter.

Usage

```r
  tfd_poisson(
    rate = NULL,
    log_rate = NULL,
    interpolate_nondiscrete = TRUE,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Poisson"
  )
```
Arguments

rate  Floating point tensor, the rate parameter. rate must be positive. Must specify exactly one of rate and log_rate.

log_rate Floating point tensor, the log of the rate parameter. Must specify exactly one of rate and log_rate.

interpolate_nondiscrete Logical. When FALSE, log_prob returns -inf (and prob returns 0) for non-integer inputs. When TRUE, log_prob evaluates the continuous function k * log_rate -lgamma(k+1) -rate, which matches the Poisson pmf at integer arguments k (note that this function is not itself a normalized probability log-density). Default value: TRUE.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.

Details

Mathematical Details
The probability mass function (pmf) is,

\[
\text{pmf}(k; \lambda, k \geq 0) = \frac{\lambda^k / k!}{Z} \\
Z = \exp(\lambda).
\]

where rate = \lambda and Z is the normalizing constant.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chisquare(), tfd_chisquare_lagj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space...
tfd_poisson_log_normal_quadrature_compound

PoissonLogNormalQuadratureCompound distribution

Description

The PoissonLogNormalQuadratureCompound is an approximation to a Poisson-LogNormal compound distribution, i.e.,

\[ p(k \mid \text{loc}, \text{scale}) = \int_{\mathbb{R}_+} dl \, \text{LogNormal}(l \mid \text{loc}, \text{scale}) \, \text{Poisson}(k \mid l) \approx \sum \text{prob}[d] \, \text{Poisson}(k \mid \lambda(\text{grid}[d])) : d=0, \ldots, \text{deg}-1 \]

Usage

```r
tfd_poisson_log_normal_quadrature_compound(
  loc,
  scale,
  quadrature_size = 8,
  quadrature_fn = tfp$datasets$quadrature_scheme_lognormal_quantiles,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "PoissonLogNormalQuadratureCompound"
)
```

Arguments

- **loc**: float-like (batch of) scalar Tensor; the location parameter of the LogNormal prior.
- **scale**: float-like (batch of) scalar Tensor; the scale parameter of the LogNormal prior.
- **quadrature_size**: integer scalar representing the number of quadrature points.
quadrature_fn
Function taking loc, scale, quadrature_size, validate_args and returning
tuple(grid, probs) representing the LogNormal grid and corresponding
normalized weight. Default value: quadrature_scheme_lognormal_quantiles.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for
validity despite possibly degrading runtime performance. When FALSE invalid
inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
By default, the grid is chosen as quantiles of the LogNormal distribution parameterized by loc, scale
and the prob vector is [1. / quadrature_size] * quadrature_size.

In the non-approximation case, a draw from the LogNormal prior represents the Poisson rate pa-
rameter. Unfortunately, the non-approximate distribution lacks an analytical probability density
function (pdf). Therefore the PoissonLogNormalQuadratureCompound class implements an ap-
proximation based on quadrature. Note: although the PoissonLogNormalQuadratureCompound
is approximately the Poisson-LogNormal compound distribution, it is itself a valid distribution. Viz.,
it possesses a sample, log_prob, mean, variance, etc. which are all mutually consistent.

Mathematical Details
The PoissonLogNormalQuadratureCompound approximates a Poisson-LogNormal compound dis-
tribution. Using variable-substitution and numerical quadrature (default: based on LogNormal quan-
tiles) we can redefine the distribution to be a parameter-less convex combination of deg different
Poisson samples. That is, defined over positive integers, this distribution is parameterized by a
(batch of) loc and scale scalars.

The probability density function (pdf) is,

\[ \text{pdf}(k | \text{loc}, \text{scale}, \text{deg}) = \sum \{ \text{prob}[d] \text{Poisson}(k | \lambda = \exp(\text{grid}[d])) : d=0, \ldots, \text{deg}-1 \} \]

Note: probs returned by (optional) quadrature_fn are presumed to be either a length-quadrature_size
vector or a batch of vectors in 1-to-1 correspondence with the returned grid. (I.e., broadcasting is
only partially supported.)

Value
a distribution instance.

See Also
For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chil(),
tfd_chil(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential().
The Power Spherical distribution is a distribution over unit vectors on $S^{n-1}$. It serves as an alternative to the von Mises-Fisher distribution with a simpler (faster) log_prob calculation, as well as a reparameterizable sampler. In contrast, the Power Spherical distribution does have mean_direction as a point with zero density (and hence a neighborhood around that having arbitrarily small density), in contrast with the von Mises-Fisher distribution which has non-zero density everywhere. NOTE: mean_direction is not in general the mean of the distribution. For spherical distributions, the mean is generally not in the support of the distribution.

Usage

tfd_power_spherical(
    mean_direction,
    concentration,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "PowerSpherical"
)

Arguments

mean_direction  Floating-point Tensor with shape [B1, ... Bn, N]. A unit vector indicating the mode of the distribution, or the unit-normalized direction of the mean.
concentration  Floating-point Tensor having batch shape [B1, ... Bn] broadcastable with mean_direction. The level of concentration of samples around the mean_direction. concentration=0 indicates a uniform distribution over the unit hypersphere, and concentration=+inf indicates a Deterministic distribution (delta function) at mean_direction.

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

ame  name prefixed to Ops created by this class.

Details

Mathematical details

The probability density function (pdf) is,

\[pdf(x; \mu, \kappa) = C(\kappa) (1 + \mu^T x)^k\]

where,

\[C(\kappa) = 2^{a + b} \pi^b \Gamma(a) / \Gamma(a + b)\]

\[a = (n - 1) / 2 + k\]
\[b = (n - 1) / 2.\]

where

- mean_direction = \mu; a unit vector in \mathbb{R}^k,
- concentration = \kappa; scalar real \geq 0, concentration of samples around mean_direction, where 0 pertains to the uniform distribution on the hypersphere, and +inf indicates a delta function at mean_direction.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space...
tfd_prob() 

Probability density/mass function.

Description

Probability density/mass function.

Usage

tfd_prob(distribution, value, ...)

Arguments

distribution  The distribution being used.
value  float or double Tensor.
...  Additional parameters passed to Python.

Value

a Tensor of shape sample_shape(x) + self$batch_shape with values of type self$dtype.

See Also

Other distribution methods: tfd_cdf(), tfd_covariance(), tfd_cross_entropy(), tfd_entropy(),
tfd_kl_divergence(), tfd_log_cdf(), tfd_log_prob(), tfd_log_survival_function(), tfd_mean(),
tfd_mode(), tfd_quantile(), tfd_sample(), tfd_stddev(), tfd_survival_function(), tfd_variance()

Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
x <- d %>% tfd_sample()
d %>% tfd_prob(x)
tfd_probit_bernoulli ProbitBernoulli distribution.

Description

The ProbitBernoulli distribution with probs parameter, i.e., the probability of a 1 outcome (vs a 0 outcome). Unlike a regular Bernoulli distribution, which uses the logistic (aka 'sigmoid') function to go from the un-constrained parameters to probabilities, this distribution uses the CDF of the standard normal distribution:

\[
p(x=1; \text{probits}) = 0.5 \times (1 + \text{erf}(\text{probits} / \sqrt{2}))
\]

\[
p(x=0; \text{probits}) = 1 - p(x=1; \text{probits})
\]

Where erf is the error function. A typical application of this distribution is in probit regression.

Usage

tfd_probit_bernoulli(
    probits = NULL,
    probs = NULL,
    dtype = tf\$int32,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "ProbitBernoulli"
)

Arguments

probits An N-D Tensor representing the probit-odds of a 1 event. Each entry in the Tensor parameterizes an independent ProbitBernoulli distribution where the probability of an event is normal_cdf(probits). Only one of probits or probs should be passed in.

probs An N-D Tensor representing the probability of a 1 event. Each entry in the Tensor parameterizes an independent ProbitBernoulli distribution. Only one of probits or probs should be passed in.

dtype The type of the event samples. Default: int32.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.
### tfd_quantile

**Quantile function.** Aka "inverse cdf" or "percent point function".

#### Description

Given random variable $X$ and $p$ in $[0, 1]$, the quantile is: $\text{tfd_quantile}(p) := x$ such that $\mathbb{P}[X \leq x] = p$

#### Usage

```python

tfd_quantile(distribution, value, ...)  
```

#### Arguments

- **distribution**: The distribution being used.
- **value**: float or double Tensor.
- **...**: Additional parameters passed to Python.

### See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions:
tfd_quantized

Value

A Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_sample()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

Examples

```r
d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_quantile(0.5)
```

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>distribution</td>
<td>The base distribution class to transform. Typically an instance of Distribution.</td>
</tr>
<tr>
<td>low</td>
<td>Tensor with same dtype as this distribution and shape able to be added to samples. Should be a whole number. Default NULL. If provided, base distribution’s prob should be defined at low.</td>
</tr>
<tr>
<td>high</td>
<td>Tensor with same dtype as this distribution and shape able to be added to samples. Should be a whole number. Default NULL. If provided, base distribution’s prob should be defined at high -1. high must be strictly greater than low.</td>
</tr>
<tr>
<td>validate_args</td>
<td>Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.</td>
</tr>
<tr>
<td>name</td>
<td>name prefixed to Ops created by this class.</td>
</tr>
</tbody>
</table>
Details

1. Draw $X$
2. Set $Y \leftarrow \text{ceiling}(X)$
3. If $Y < \text{low}$, reset $Y \leftarrow \text{low}$
4. If $Y > \text{high}$, reset $Y \leftarrow \text{high}$
5. Return $Y$

Definition in Terms of the Probability Mass Function

Given scalar random variable $X$, we define a discrete random variable $Y$ supported on the integers as follows:

$$P[Y = j] := P[X \leq \text{low}], \text{ if } j = \text{low},$$
$$:= P[X > \text{high} - 1], \text{ if } j = \text{high},$$
$$:= 0, \text{ if } j < \text{low} \text{ or } j > \text{high},$$
$$:= P[j - 1 < X \leq j], \text{ all other } j.$$

Conceptually, without cutoffs, the quantization process partitions the real line $\mathbb{R}$ into half open intervals, and identifies an integer $j$ with the right endpoints:

$$R = \ldots (-\infty, -1](-1, 0](0, 1](1, 2](2, 3](3, 4] \ldots$$
$$j = \ldots -1 0 1 2 3 4 \ldots$$

$P[Y = j]$ is the mass of $X$ within the $j$th interval. If $\text{low} = 0$, and $\text{high} = 2$, then the intervals are redrawn and $j$ is re-assigned:

$$R = (-\infty, 0](0, 1](1, \infty)$$
$$j = 0 1 2$$

$P[Y = j]$ is still the mass of $X$ within the $j$th interval.

@section References:


Value

A distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batchreshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_chi()`, `tfd_cholksky_lkj()`, `tfd_continuous_bernoulli()`, `tfd deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`. 
tfd_relaxed_bernoulli

RelaxedBernoulli distribution with temperature and logits parameters

Description

The RelaxedBernoulli is a distribution over the unit interval (0,1), which continuously approximates a Bernoulli. The degree of approximation is controlled by a temperature: as the temperature goes to 0 the RelaxedBernoulli becomes discrete with a distribution described by the logits or probs parameters, as the temperature goes to infinity the RelaxedBernoulli becomes the constant distribution that is identically 0.5.

Usage

tfd_relaxed_bernoulli(
    temperature,
    logits = NULL,
    probs = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "RelaxedBernoulli"
)

Arguments

temperature An 0-D Tensor, representing the temperature of a set of RelaxedBernoulli distributions. The temperature should be positive.
logits  An N-D Tensor representing the log-odds of a positive event. Each entry in the Tensor parametrizes an independent RelaxedBernoulli distribution where the probability of an event is sigmoid(logits). Only one of logits or probs should be passed in.

probs  A N-D Tensor representing the probability of a positive event. Each entry in the Tensor parameterizes an independent Bernoulli distribution. Only one of logits or probs should be passed in.

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name  name prefixed to Ops created by this class.

Details

The RelaxedBernoulli distribution is a reparameterized continuous distribution that is the binary special case of the RelaxedOneHotCategorical distribution (Maddison et al., 2016; Jang et al., 2016). For details on the binary special case see the appendix of Maddison et al. (2016) where it is referred to as BinConcrete. If you use this distribution, please cite both papers.

Some care needs to be taken for loss functions that depend on the log-probability of RelaxedBernoullis, because computing log-probabilities of the RelaxedBernoulli can suffer from underflow issues. In many case loss functions such as these are invariant under invertible transformations of the random variables. The KL divergence, found in the variational autoencoder loss, is an example. Because RelaxedBernoullis are sampled by a Logistic random variable followed by a $\text{tf}\_sigmoid$ op, one solution is to treat the Logistic as the random variable and $\text{tf}\_sigmoid$ as downstream. The KL divergences of two Logistcs, which are always followed by a $\text{tf}\_sigmoid$ op, is equivalent to evaluating KL divergences of RelaxedBernoulli samples. See Maddison et al., 2016 for more details where this distribution is called the BinConcrete. An alternative approach is to evaluate Bernoulli log probability or KL directly on relaxed samples, as done in Jang et al., 2016. In this case, guarantees on the loss are usually violated. For instance, using a Bernoulli KL in a relaxed ELBO is no longer a lower bound on the log marginal probability of the observation. Thus care and early stopping are important.

Value

a distribution instance.

See Also

For usage examples see e.g. $\text{tfd}\_sample()$, $\text{tfd}\_log\_prob()$, $\text{tfd}\_mean()$.

Other distributions: $\text{tfd}\_autoregressive()$, $\text{tfd}\_batch\_reshape()$, $\text{tfd}\_bates()$, $\text{tfd}\_bernoulli()$, $\text{tfd}\_beta\_binomial()$, $\text{tfd}\_beta()$, $\text{tfd}\_binomial()$, $\text{tfd}\_categorical()$, $\text{tfd}\_cauchy()$, $\text{tfd}\_chi^2()$, $\text{tfd}\_chi()$, $\text{tfd}\_cholesky\_lkj()$, $\text{tfd}\_continuous\_bernoulli()$, $\text{tfd}\_deterministic()$, $\text{tfd}\_dirichlet\_multinomial()$, $\text{tfd}\_dirichlet()$, $\text{tfd}\_empirical()$, $\text{tfd}\_exp\_gamma()$, $\text{tfd}\_exp\_inverse\_gamma()$, $\text{tfd}\_exponential()$. 
tfd_relaxed_one_hot_categorical

RelaxedOneHotCategorical distribution with temperature and logits

Description

The RelaxedOneHotCategorical is a distribution over random probability vectors, vectors of positive real values that sum to one, which continuously approximates a OneHotCategorical. The degree of approximation is controlled by a temperature: as the temperature goes to 0 the RelaxedOneHotCategorical becomes discrete with a distribution described by the logits or probs parameters, as the temperature goes to infinity the RelaxedOneHotCategorical becomes the constant distribution that is identically the constant vector of (1/event_size, ..., 1/event_size). The RelaxedOneHotCategorical distribution was concurrently introduced as the Gumbel-Softmax (Jang et al., 2016) and Concrete (Maddison et al., 2016) distributions for use as a reparameterized continuous approximation to the Categorical one-hot distribution. If you use this distribution, please cite both papers.

Usage

```r
  tfd_relaxed_one_hot_categorical(
    temperature,
    logits = NULL,
    probs = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "RelaxedOneHotCategorical"
  )
```
Arguments

- **temperature**: An 0-D Tensor, representing the temperature of a set of RelaxedOneHotCategorical distributions. The temperature should be positive.

- **logits**: An N-D Tensor, N >= 1, representing the log probabilities of a set of RelaxedOneHotCategorical distributions. The first N - 1 dimensions index into a batch of independent distributions and the last dimension represents a vector of logits for each class. Only one of logits or probs should be passed in.

- **probs**: An N-D Tensor, N >= 1, representing the probabilities of a set of RelaxedOneHotCategorical distributions. The first N - 1 dimensions index into a batch of independent distributions and the last dimension represents a vector of probabilities for each class. Only one of logits or probs should be passed in.

- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

- **name**: name prefixed to Ops created by this class.

Value

a distribution instance.

References

- Eric Jang, Shixiang Gu, and Ben Poole. Categorical Reparameterization with Gumbel-Softmax. 2016.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_sample

Generate samples of the specified shape.

Description

Note that a call to `tfd_sample()` without arguments will generate a single sample.

Usage

```
tfd_sample(distribution, sample_shape = list(), ...)
```

Arguments

- **distribution**: The distribution being used.
- **sample_shape**: 0D or 1D int32 Tensor. Shape of the generated samples.
- **...**: Additional parameters passed to Python.

Value

a Tensor with prepended dimensions `sample_shape`.

See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_stddev()`, `tfd_survival_function()`, `tfd_variance()`

Examples

```
d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_sample()
```
Sample distribution via independent draws.

Description

This distribution is useful for reducing over a collection of independent, identical draws. It is otherwise identical to the input distribution.

Usage

```r
  tfd_sample_distribution(
    distribution,
    sample_shape = list(),
    validate_args = FALSE,
    name = NULL
  )
```

Arguments

- **distribution**: The base distribution instance to transform. Typically an instance of `Distribution`.
- **sample_shape**: integer scalar or vector Tensor representing the shape of a single sample.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **name**: The name for ops managed by the distribution. Default value: NULL (i.e., 'Sample' + distribution$name).

Details

Mathematical Details The probability function is,

\[ p(x) = \prod \{ p(x[i]) : i = 0, \ldots, (n - 1) \} \]

Value

- a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gamma_gamma()`, `tfd_gamma()`., `tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`.
Description

This distribution models a random variable, making use of a SinhArcsinh transformation (which has adjustable tailweight and skew), a rescaling, and a shift. The SinhArcsinh transformation of the Normal is described in great depth in Sinh-arcsinh distributions. Here we use a slightly different parameterization, in terms of tailweight and skewness. Additionally we allow for distributions other than Normal, and control over scale as well as a “shift” parameter loc.

Usage

tfd_sinh_arcsinh(loc, scale, skewness = NULL, tailweight = NULL, distribution = NULL, validate_args = FALSE, allow_nan_stats = TRUE, name = "SinhArcsinh")

Arguments

loc Floating-point Tensor.
scale Tensor of same dtype as loc.
skewness  
Skewness parameter. Default is 0.0 (no skew).

tailweight  
Tailweight parameter. Default is 1.0 (unchanged tailweight)

distribution  
tfd_distributions$Distribution-like instance. Distribution that is transformed to produce this distribution. Default is tfd_normal(0,1). Must be a scalar-batch, scalar-event distribution. Typically distribution$reparameterization_type = FULLY_REPARAMETERIZED or it is a function of non-trainable parameters. WARNING: If you backprop through a SinhArcsinh sample and distribution is not FULLY_REPARAMETERIZED yet is a function of trainable variables, then the gradient will be incorrect!

validate_args  
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name  
name prefixed to Ops created by this class.

Details

Mathematical Details

Given random variable \( Z \), we define the SinhArcsinh transformation of \( Z \), \( Y \), parameterized by (loc, scale, skewness, tailweight), via the relation:

\[
Y := \text{loc} + \text{scale} \times F(Z) \times \left( \frac{2}{F_0(2)} \right)
\]

\[
F(Z) := \text{Sinh} \left( (\text{Arcsinh}(Z) + \text{skewness}) \times \text{tailweight} \right)
\]

\[
F_0(Z) := \text{Sinh} \left( \text{Arcsinh}(Z) \times \text{tailweight} \right)
\]

This distribution is similar to the location-scale transformation \( L(Z) := \text{loc} + \text{scale} \times Z \) in the following ways:

- If \( \text{skewness} = 0 \) and \( \text{tailweight} = 1 \) (the defaults), \( F(Z) = Z \), and then \( Y = L(Z) \) exactly.
- \( \text{loc} \) is used in both to shift the result by a constant factor.
- The multiplication of \( \text{scale} \) by \( \frac{2}{F_0(2)} \) ensures that if \( \text{skewness} = 0 \) \( P[Y - \text{loc} \leq 2 \times \text{scale}] = P[L(Z) - \text{loc} \leq 2 \times \text{scale}] \). Thus it can be said that the weights in the tails of \( Y \) and \( L(Z) \) beyond \( \text{loc} + 2 \times \text{scale} \) are the same.

This distribution is different than \( \text{loc} + \text{scale} \times Z \) due to the reshaping done by \( F \):

- Positive (negative) skewness leads to positive (negative) skew.
- positive skew means, the mode of \( F(Z) \) is "tilted" to the right.
- positive skew means positive values of \( F(Z) \) become more likely, and negative values become less likely.
- Larger (smaller) tailweight leads to fatter (thinner) tails.
- Fatter tails mean larger values of \( |F(Z)| \) become more likely.
• tailweight < 1 leads to a distribution that is "flat" around $Y = \text{loc}$, and a very steep drop-off in the tails.

• tailweight > 1 leads to a distribution more peaked at the mode with heavier tails.

To see the argument about the tails, note that for $|Z| \gg 1$ and $|Z| \gg (|\text{skewness}| \times \text{tailweight})^\text{tailweight}$, we have $Y \approx 0.5 \times Z^{\text{tailweight}} e^{(\text{sign}(Z) \times \text{skewness} \times \text{tailweight})}$.

To see the argument regarding multiplying scale by $2 / F_0(2)$,

$$P[(Y - \text{loc}) / \text{scale} \leq 2] = P[F(Z) \times (2 / F_0(2)) \leq 2]$$
$$= P[F(Z) \leq F_0(2)]$$
$$= P[Z \leq 2] \quad \text{(if } F = F_0\text{).}$$

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Description

The Skellam distribution is parameterized by two rate parameters, \( \text{rate1} \) and \( \text{rate2} \). Its samples are defined as:

\[
x \sim \text{Poisson}(\text{rate1})
\]
\[
y \sim \text{Poisson}(\text{rate2})
\]
\[
z = x - y
\]
\[
z \sim \text{Skellam}(\text{rate1}, \text{rate2})
\]

where the samples \( x \) and \( y \) are assumed to be independent.

Usage

```r


tfd_skellam(
  rate1 = NULL,
  rate2 = NULL,
  log_rate1 = NULL,
  log_rate2 = NULL,
  force_probs_to_zero_outside_support = FALSE,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Skellam"
)
```

Arguments

- **rate1**
  - Floating point tensor, the first rate parameter. \( \text{rate1} \) must be positive. Must specify exactly one of \( \text{rate1} \) and \( \text{log_rate1} \).

- **rate2**
  - Floating point tensor, the second rate parameter. \( \text{rate2} \) must be positive. Must specify exactly one of \( \text{rate2} \) and \( \text{log_rate2} \).

- **log_rate1**
  - Floating point tensor, the log of the first rate parameter. Must specify exactly one \( \text{rate1} \) and \( \text{log_rate1} \).

- **log_rate2**
  - Floating point tensor, the log of the second rate parameter. Must specify exactly one \( \text{rate2} \) and \( \text{log_rate2} \).

- **force_probs_to_zero_outside_support**
  - logical. When TRUE, \( \text{log_prob} \) returns \(-\infty\) (and \( \text{prob} \) returns 0) for non-integer inputs. When FALSE, \( \text{log_prob} \) evaluates the Skellam pmf as a continuous function (note that this function is not itself a normalized probability log-density). Default value: FALSE.

- **validate_args**
  - Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
the value NaN to indicate the result is undefined. When FALSE, an exception is
raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
Mathematical Details The probability mass function (pmf) is,

\[ \text{pmf}(k; l_1, l_2) = \frac{(l_1 / l_2)^{k/2} \text{I}_k(2 \sqrt{l_1 l_2})}{Z} \]

where \( Z = \exp(l_1 + l_2) \).

where \( rate_1 = l_1 \), \( rate_2 = l_2 \), \( Z \) is the normalizing constant and \( \text{I}_k \) is the modified bessel function
of the first kind.

Value
a distribution instance.

See Also
For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_chii(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),
tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(),
tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),
tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_tfd_lkj(),
tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(),
tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(),
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_normal_tril(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature()
tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(),
tfd_spherical_uniform(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(),
tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfdVariationalGaussianApproximation(),
tfd_vector_diffeomixture(), tfd_vector_exponential_diag(), tfd_vector_exponential_linear_operator(),
tfd_vector_laplace_diag(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh_diag(),
tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(),
tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
The uniform distribution over unit vectors on $S^{n-1}$.

**Usage**

```r
tfd_spherical_uniform(
  dimension,
  batch_shape = list(),
  dtype = tf$float32,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "SphericalUniform"
)
```

**Arguments**

- **dimension**: integer. The dimension of the embedded space where the sphere resides.
- **batch_shape**: Positive integer-like vector-shaped Tensor representing the new shape of the batch dimensions. Default value: `[]`.
- **dtype**: dtype of the generated samples.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: name prefixed to Ops created by this class.

**Details**

Mathematical details

The probability density function (pdf) is,

$$pdf(x; n) = 1. / A(n)$$

where,

$$A(n) = 2 * \pi^{n / 2} / \Gamma(n / 2),$$

$\Gamma$ being the Gamma function.

where $n = \text{dimension}$; corresponds to $S^{n-1}$ embedded in $\mathbb{R}^n$. 

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),
tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(),
tfd_dirichlet_multinomial(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),
tfd_generalized_normal(), tfd_geometric(), tfd_half_cauchy(), tfd_half_normal(),
tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),
tfd_inverse_gaussian(), tfd_johnson_s(), tfd_joint_distribution_named_auto_batched(),
tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),
tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space(),
tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(),
tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(),
tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(),
tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(),
tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(),
tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(),
tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(),
tfd_skellam(), tfd_student_t_process(), tfd_student_t(), tfd_transformed_distribution(),
tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_variational_gaussian_2d(),
tfd_vector_diffeomixture(), tfd_vector_exponential_diagonal(), tfd_vector_exponential_linear_operator(),
tfd_vector_laplace_diagonal(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh_diagonal(),
tfd_von_mises_fisher(), tfd_von_mises(), tfd_weibull(), tfd_wishart_linear_operator(),
tfd_wishart(), tfd_zipf()
Value

A Tensor of shape `sample_shape(x) + self$batch_shape` with values of type `self$dtype`.

See Also

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_survival_function()`, `tfd_variance()`.

Examples

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
d %>% tfd_stddev()

---

tfd_student_t  Student's t-distribution

Description

This distribution has parameters: degree of freedom `df`, location `loc`, and `scale`.

Usage

`tfd_student_t(`
`df,`
`loc,`
`scale,`
`validate_args = FALSE,`
`allow_nan_stats = TRUE,`
`name = "StudentT"`
`)`

Arguments

df  Floating-point `Tensor`. The degrees of freedom of the distribution(s). `df` must contain only positive values.
loc  Floating-point `Tensor`. The mean(s) of the distribution(s).
scale  Floating-point `Tensor`. The scaling factor(s) for the distribution(s). Note that `scale` is not technically the standard deviation of this distribution but has semantics more similar to standard deviation than variance.
validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name

name prefixed to Ops created by this class.

Details

Mathematical details

The probability density function (pdf) is,

\[
pdf(x; df, mu, sigma) = \frac{(1 + y^2 / df)^{(-0.5(df + 1))}}{Z}
\]

where,

\[
y = (x - mu) / sigma
\]

\[
Z = abs(sigma) \sqrt{df \pi} \Gamma(0.5 df) / \Gamma(0.5 (df + 1))
\]

where:

- \( loc = mu \),
- \( scale = sigma \), and,
- \( Z \) is the normalization constant, and,
- \( \Gamma \) is the gamma function. The StudentT distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X \sim \text{StudentT}(df, loc=0, scale=1)
Y = loc + scale * X
\]

Notice that scale has semantics more similar to standard deviation than variance. However it is not actually the std. dev.; the Student’s t-distribution std. dev. is scale \( \sqrt{df / (df - 2)} \) when \( df > 2 \).

Samples of this distribution are reparameterized (pathwise differentiable). The derivatives are computed using the approach described in the paper Michael Figurnov, Shakir Mohamed, Andriy Mnih. Implicit Reparameterization Gradients, 2018

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample(), tfd_log_prob(), tfd_mean()`.

Other distributions: `tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binous(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chol()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gamma()`, `tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`, `tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`, `tfd_id()`, `tfd_multivariate_normal_diag()`, `tfd_multivariate_normal_tri_cov()`, `tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_bernoulli()`, `tfd_categorical()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_exponential()`, `tfd_gamma()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`.
tfd_student_t_process

Marginal distribution of a Student’s T process at finitely many points

Description

A Student’s T process (TP) is an indexed collection of random variables, any finite collection of which are jointly Multivariate Student’s T. While this definition applies to finite index sets, it is typically implicit that the index set is infinite; in applications, it is often some finite dimensional real or complex vector space. In such cases, the TP may be thought of as a distribution over (real- or complex-valued) functions defined over the index set.

Usage

```r
  tfd_student_t_process(
    df, 
    kernel, 
    index_points, 
    mean_fn = NULL, 
    jitter = 1e-06, 
    validate_args = FALSE, 
    allow_nan_stats = FALSE, 
    name = "StudentTProcess" 
  )
```

Arguments

- **df**
  - Positive Floating-point Tensor representing the degrees of freedom. Must be greater than 2.
kernel: PositiveSemidefiniteKernel-like instance representing the TP’s covariance function.

index_points: float Tensor representing finite (batch of) vector(s) of points in the index set over which the TP is defined. Shape has the form \([b_1, ..., b_B, e, f_1, ..., f_F]\) where \(F\) is the number of feature dimensions and must equal kernel.feature_ndims and \(e\) is the number (size) of index points in each batch. Ultimately this distribution corresponds to a \(e\)-dimensional multivariate Student’s T. The batch shape must be broadcastable with kernel.batch_shape and any batch dims yielded by mean_fn.

mean_fn: Function that acts on index_points to produce a (batch of) vector(s) of mean values at index_points. Takes a Tensor of shape \([b_1, ..., b_B, f_1, ..., f_F]\) and returns a Tensor whose shape is broadcastable with \([b_1, ..., b_B]\). Default value: NULL implies constant zero function.

jitter: float scalar Tensor added to the diagonal of the covariance matrix to ensure positive definiteness of the covariance matrix. Default value: 1e-6.

validate_args: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name: name prefixed to Ops created by this class.

Details

Just as Student’s T distributions are fully specified by their degrees of freedom, location and scale, a Student’s T process can be completely specified by a degrees of freedom parameter, mean function and covariance function.

Let \(S\) denote the index set and \(K\) the space in which each indexed random variable takes its values (again, often \(\mathbb{R}\) or \(\mathbb{C}\)). The mean function is then a map \(m: S \rightarrow K\), and the covariance function, or kernel, is a positive-definite function \(k: (S \times S) \rightarrow K\). The properties of functions drawn from a TP are entirely dictated (up to translation) by the form of the kernel function.

This distribution represents the marginal joint distribution over function values at a given finite collection of points \([x[1], ..., x[N]]\) from the index set \(S\). By definition, this marginal distribution is just a multivariate Student’s T distribution, whose mean is given by the vector \(\{m(x[1]), ..., m(x[N])\}\) and whose covariance matrix is constructed from pairwise applications of the kernel function to the given inputs:

\[
\begin{pmatrix}
k(x[1], x[1]) & k(x[1], x[2]) & \cdots & k(x[1], x[N]) \\
k(x[2], x[1]) & k(x[2], x[2]) & \cdots & k(x[2], x[N]) \\
\vdots & \vdots & \ddots & \vdots \\
k(x[N], x[1]) & k(x[N], x[2]) & \cdots & k(x[N], x[N])
\end{pmatrix}
\]

For this to be a valid covariance matrix, it must be symmetric and positive definite; hence the requirement that \(k\) be a positive definite function (which, by definition, says that the above procedure
will yield PD matrices). Note also we use a parameterization as suggested in Shat et al. (2014), which requires df to be greater than 2. This allows for the covariance for any finite dimensional marginal of the TP (a multivariate Student’s T distribution) to just be the PD matrix generated by the kernel.

Mathematical Details

The probability density function (pdf) is a multivariate Student’s T whose parameters are derived from the TP’s properties:

$$\text{pdf}(x; \text{df}, \text{index_points}, \text{mean_fn}, \text{kernel}) = \text{MultivariateStudentT}(\text{df}, \text{loc}, \text{K})$$

$$\text{K} = (\text{df} - 2) / \text{df} \times (\text{kernel.matrix(index_points, index_points)} + \text{jitter} \times \text{eye(N)})$$

$$\text{loc} = (x - \text{mean_fn(index_points)})^T @ \text{K} @ (x - \text{mean_fn(index_points)})$$

where:

- $\text{df}$ is the degrees of freedom parameter for the TP.
- $\text{index_points}$ are points in the index set over which the TP is defined,
- $\text{mean_fn}$ is a callable mapping the index set to the TP’s mean values,
- $\text{kernel}$ is $\text{PositiveSemidefiniteKernel}$-like and represents the covariance function of the TP,
- $\text{jitter}$ is added to the diagonal to ensure positive definiteness up to machine precision (otherwise Cholesky-decomposition is prone to failure),
- $\text{eye(N)}$ is an N-by-N identity matrix.

Value

a distribution instance.

References


See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(), tfd_dirichlet_multinomial(), tfd_dirichlet_multivariate(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_diag(), tfd multinormal_diag_plus_low_rank(), tfd multinormal_diag(), tfd_normal, tfd_normal_diag_plus_low_rank(), tfd_normal_diag(), tfd_normal_diag()
tfd_survival_function

**Survival function.**

**Description**

Given random variable X, the survival function is defined: \( \text{tfd_survival_function}(x) = \mathbb{P}[X > x] = 1 - \mathbb{P}[X \leq x] = 1 - \text{cdf}(x) \).

**Usage**

\[
\text{tfd_survival_function}(\text{distribution}, \text{value}, \ldots)
\]

**Arguments**

- **distribution**: The distribution being used.
- **value**: float or double Tensor.
- **...**: Additional parameters passed to Python.

**Value**

a Tensor of shape \( \text{sample_shape}(x) + \text{self$batch_shape} \) with values of type \( \text{self$dtype} \).

**See Also**

Other distribution methods: `tfd_cdf()`, `tfd_covariance()`, `tfd_cross_entropy()`, `tfd_entropy()`, `tfd_kl_divergence()`, `tfd_log_cdf()`, `tfd_log_prob()`, `tfd_log_survival_function()`, `tfd_mean()`, `tfd_mode()`, `tfd_prob()`, `tfd_quantile()`, `tfd_sample()`, `tfd_stddev()`, `tfd_variance()`

**Examples**

```r

d <- tfd_normal(loc = c(1, 2), scale = c(1, 0.5))
x <- d %>% tfd_sample()
d %>% tfd_survival_function(x)
```
A Transformed Distribution

A TransformedDistribution models \( p(y) \) given a base distribution \( p(x) \), and a deterministic, invertible, differentiable transform, \( Y = g(X) \). The transform is typically an instance of the Bijector class and the base distribution is typically an instance of the Distribution class.

Usage

tfd_transformed_distribution(
    distribution,
    bijector,
    batch_shape = NULL,
    event_shape = NULL,
    kwargs_split_fn = NULL,
    validate_args = FALSE,
    parameters = NULL,
    name = NULL
)

Arguments

distribution  The base distribution instance to transform. Typically an instance of Distribution.
bijector      The object responsible for calculating the transformation. Typically an instance of Bijector.
batch_shape   integer vector Tensor which overrides distribution batch_shape; valid only if distribution.is_scalar_batch().
event_shape   integer vector Tensor which overrides distribution event_shape; valid only if distribution.is_scalar_event().
kwargss_split_fn  Python callable which takes a kwargs dict and returns a tuple of kwargs dicts for each of the distribution and bijector parameters respectively. Default value: _default_kwargss_split_fn (i.e., lambda kwargs: (kwargs.get('distribution_kwargs', {}), kwargs.get('bijector_kwargs', {}))).
validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
parameters   Locals dict captured by subclass constructor, to be used for copy/slice re-instantiation operations.
name        The name for ops managed by the distribution. Default value: bijector.name + distribution.name.
Details

A Bijector is expected to implement the following functions:

- forward,
- inverse,
- inverse_log_det_jacobian.

The semantics of these functions are outlined in the Bijector documentation.

We now describe how a TransformedDistribution alters the input/outputs of a Distribution associated with a random variable (rv) \( X \). Write \( \text{cdf}(Y=y) \) for an absolutely continuous cumulative distribution function of random variable \( Y \); write the probability density function \( \text{pdf}(Y=y) = \frac{d}{dy_1,...,dy_k} \text{cdf}(Y=y) \) for its derivative wrt to \( Y \) evaluated at \( y \). Assume that \( Y = g(X) \) where \( g \) is a deterministic diffeomorphism, i.e., a non-random, continuous, differentiable, and invertible function. Write the inverse of \( g \) as \( X = g^{-1}(Y) \) and \( (J o g)(x) \) for the Jacobian of \( g \) evaluated at \( x \).

A TransformedDistribution implements the following operations:

- **sample** Mathematically: \( Y = g(X) \) Programmatically: `bijector.forward(distribution.sample(...))`
- **log_prob** Mathematically: \( (\log o \text{pdf})(Y=y) = (\log o \text{pdf} o g^\{-1\})(y) + (\log o \text{abs} o \text{det} o J o g^{\{-1\}})(y) \) Programmatically: `(distribution.log_prob(bijector.inverse(y)) + bijector.inverse_log_det_jacobian(y))`
- **log_cdf** Mathematically: \( (\log o \text{cdf})(Y=y) = (\log o \text{cdf} o g^\{-1\})(y) \) Programmatically: `distribution.log_cdf(bijector.inverse(x))`
- and similarly for: cdf, prob, log_survival_function, survival_function.

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

Other distributions: `tfd_autoregressive()`, `tfd_batch_reshape()`, `tfd_bates()`, `tfd_bernoulli()`, `tfd_beta_binomial()`, `tfd_beta()`, `tfd_binomial()`, `tfd_categorical()`, `tfd_cauchy()`, `tfd_chi2()`, `tfd_chi()`, `tfd_cholesky_lkj()`, `tfd_continuous_bernoulli()`, `tfd_deterministic()`, `tfd_dirichlet_multinomial()`, `tfd_dirichlet()`, `tfd_empirical()`, `tfd_exp_gamma()`, `tfd_exp_inverse_gamma()`, `tfd_exponential()`, `tfd_gamma_gamma()`, `tfd_gamma()`, `tfd_gaussian_process_regression_model()`, `tfd_gaussian_process()`, `tfd_generalized_normal()`, `tfd_geometric()`, `tfd_gumbel()`, `tfd_half_cauchy()`, `tfd_half_normal()`, `tfd_hidden_markov_model()`, `tfd_horseshoe()`, `tfd_independent()`, `tfd_inverse_gamma()`, `tfd_inverse_gaussian()`, `tfd_johnson_s_u()`, `tfd_joint_distribution_named_auto_batched()`, `tfd_joint_distribution_named()`, `tfd_joint_distribution_sequential_auto_batched()`, `tfd_joint_distribution_sequential()`, `tfd_kumaraswamy()`, `tfd_laplace()`, `tfd_linear_gaussian_state_space_model()`, `tfd_lkj()`, `tfd_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_mixture_same_family()`, `tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal_diag()`, `tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_normal_tri_l()`, `tfd_multivariate_student_t_linear_operator()`, `tfd_negative_binomial()`, `tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_compound()`, `tfd_poisson()`, `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`, `tfd_relaxed_one_hot_categorical()`, `tfd_sample_distribution()`, `tfd_sinh_arcsinh()`, `tfd_transformed_distribution`
tfd_triangular

Description

The parameters low, high and peak must be shaped in a way that supports broadcasting (e.g., high - low is a valid operation).

Usage

```r
tfd_triangular(
  low = 0,
  high = 1,
  peak = 0.5,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Triangular"
)
```

Arguments

- **low**: Floating point tensor, lower boundary of the output interval. Must have low < high. Default value: 0.
- **high**: Floating point tensor, upper boundary of the output interval. Must have low < high. Default value: 1.
- **peak**: Floating point tensor, mode of the output interval. Must have low <= peak and peak <= high. Default value: 0.5.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Value

a distribution instance.
The Truncated Cauchy distribution.

Description

The truncated Cauchy is a Cauchy distribution bounded between low and high (the pdf is 0 outside these bounds and renormalized). Samples from this distribution are differentiable with respect to loc and scale, but not with respect to the bounds low and high.

Usage

tfd_truncated_cauchy(
    loc,
scale,
low,
high,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "TruncatedCauchy"
)
Arguments

loc  Floating point tensor; the modes of the corresponding non-truncated Cauchy
     distribution(s).

scale  Floating point tensor; the scales of the distribution(s). Must contain only positive
        values.

low  float Tensor representing lower bound of the distribution’s support. Must be
     such that low < high.

high  float Tensor representing upper bound of the distribution’s support. Must be
      such that low < high.

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for
                validity despite possibly degrading runtime performance. When FALSE invalid
                inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use
                the value NaN to indicate the result is undefined. When FALSE, an exception is
                raised if one or more of the statistic’s batch members are undefined.

name  name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) of this distribution is:

\[
\text{pdf}(x; \text{loc}, \text{scale}, \text{low}, \text{high}) =
\begin{cases}
  1 / \left(\pi \times \text{scale} \times (1 + z^2) \times A\right) & \text{for low} \leq x \leq \text{high} \\
  0 & \text{otherwise}
\end{cases}
\]

where

\[
A = \text{CauchyCDF}\left(\frac{\text{high} - \text{loc}}{\text{scale}}\right) - \text{CauchyCDF}\left(\frac{\text{low} - \text{loc}}{\text{scale}}\right)
\]

where \(\text{CauchyCDF}\) is the cumulative density function of the Cauchy distribution with 0 mean and
unit variance. This is a scalar distribution so the event shape is always scalar and the dimensions of
the parameters define the batch_shape.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),
tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chisq(),
tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial,
tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),
tfd_gamma_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),

tfd_truncated_normal distribution

Description
The truncated normal is a normal distribution bounded between low and high (the pdf is 0 outside these bounds and renormalized). Samples from this distribution are differentiable with respect to loc, scale as well as the bounds, low and high, i.e., this implementation is fully reparameterizable. For more details, see here.

Usage
```r
  tfd_truncated_normal(
    loc,
    scale,
    low,
    high,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "TruncatedNormal"
  )
```

Arguments
- **loc**: Floating point tensor; the means of the distribution(s).
- **scale**: Floating point tensor; the stddevs of the distribution(s). Must contain only positive values.
tfd_truncated_normal

low float Tensor representing lower bound of the distribution's support. Must be such that low < high.

high float Tensor representing upper bound of the distribution's support. Must be such that low < high.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic's batch members are undefined.

name name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) of this distribution is:

\[
\text{pdf}(x; \text{loc}, \text{scale}, \text{low}, \text{high}) = \\
\begin{cases} 
(2 \pi)^{-0.5} \exp(-0.5 y^2) / (\text{scale} * z) & \text{for low} \leq x \leq \text{high} \\
0 & \text{otherwise}
\end{cases}
\]

\[
y = (x - \text{loc})/\text{scale}
\]

\[
z = \text{NormalCDF}((\text{high} - \text{loc}) / \text{scale}) - \text{NormalCDF}((\text{low} - \text{loc}) / \text{scale})
\]

where:

- \text{NormalCDF} is the cumulative density function of the Normal distribution with 0 mean and unit variance.

This is a scalar distribution so the event shape is always scalar and the dimensions of the parameters defined the batch_shape.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binary(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequence_auto_batched().
**tfd_uniform**

*Uniform distribution with low and high parameters*

**Description**

Mathematical Details

**Usage**

```python
tfd_uniform(
    low = 0,
    high = 1,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Uniform"
)
```

**Arguments**

- **low**: Floating point tensor, lower boundary of the output interval. Must have low < high.
- **high**: Floating point tensor, upper boundary of the output interval. Must have low < high.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.
The probability density function (pdf) is,

\[
pdf(x; a, b) = I[a \leq x < b] / Z
\]

\[
Z = b - a
\]

where

- \(low = a\),
- \(high = b\),
- \(Z\) is the normalizing constant, and
- \(I[predicate]\) is the indicator function for predicate.

The parameters low and high must be shaped in a way that supports broadcasting (e.g., \(high - low\) is a valid operation).

Value

A distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

tfd_variance

Variance.

Description

Variance is defined as, \( \text{Var} = \text{E}[(X - E[X])**2] \) where \( X \) is the random variable associated with this distribution, \( E \) denotes expectation, and \( \text{Var}\text{shape} = \text{batch\_shape} + \text{event\_shape} \).

Usage

\[
\text{tfd\_variance}(\text{distribution}, \ldots)
\]

Arguments

- **distribution**: The distribution being used.
- **...**: Additional parameters passed to Python.

Value

a Tensor of shape \text{sample\_shape(x)} + self\$batch\_shape with values of type self\$dtype.

See Also

Other distribution methods: tfd\_cdf(), tfd\_covariance(), tfd\_cross\_entropy(), tfd\_entropy(), tfd\_kl\_divergence(), tfd\_log\_cdf(), tfd\_log\_prob(), tfd\_log\_survival\_function(), tfd\_mean(), tfd\_mode(), tfd\_prob(), tfd\_quantile(), tfd\_sample(), tfd\_stddev(), tfd\_survival\_function()

Examples

\[
d <- \text{tfd\_normal}(\text{loc} = c(1, 2), \text{scale} = c(1, 0.5))
d \%&\% \text{tfd\_variance}()
\]
Description

This distribution implements the variational Gaussian process (VGP), as described in Titsias (2009) and Hensman (2013). The VGP is an inducing point-based approximation of an exact GP posterior. Ultimately, this Distribution class represents a marginal distribution over function values at a collection of index_points. It is parameterized by

- a kernel function,
- a mean function,
- the (scalar) observation noise variance of the normal likelihood,
- a set of index points,
- a set of inducing index points, and
- the parameters of the (full-rank, Gaussian) variational posterior distribution over function values at the inducing points, conditional on some observations.

Usage

tfd_variational_gaussian_process(
  kernel,
  index_points,
  inducing_index_points,
  variational_inducing_observations_loc,
  variational_inducing_observations_scale,
  mean_fn = NULL,
  observation_noise_variance = 0,
  predictive_noise_variance = 0,
  jitter = 1e-06,
  validate_args = FALSE,
  allow_nan_stats = FALSE,
  name = "VariationalGaussianProcess"
)

Arguments

- **kernel** PositiveSemidefiniteKernel-like instance representing the GP’s covariance function.
- **index_points** float Tensor representing finite (batch of) vector(s) of points in the index set over which the VGP is defined. Shape has the form [b1, ..., bB, e1, f1, ..., fF] where F is the number of feature dimensions and must equal kernel$feature_ndims and e1 is the number (size) of index points in each batch (we denote it e1 to distinguish it from the number of inducing index points, denoted e2 below). Ultimately the VariationalGaussianProcess distribution corresponds to an e1-dimensional multivariate normal. The batch shape must be broadcastable with kernel$batch_shape, the batch shape of inducing_index_points, and any batch dims yielded by mean_fn.
inducing_index_points
float Tensor of locations of inducing points in the index set. Shape has the form \([b_1, ..., b_B, e_2, f_1, ..., f_F]\), just like index_points. The batch shape components needn’t be identical to those of index_points, but must be broadcast compatible with them.

variational_inducing_observations_loc
float Tensor; the mean of the (full-rank Gaussian) variational posterior over function values at the inducing points, conditional on observed data. Shape has the form \([b_1, ..., b_B, e_2]\), where \(b_1, ..., b_B\) is broadcast compatible with other parameters’ batch shapes, and \(e_2\) is the number of inducing points.

variational_inducing_observations_scale
float Tensor; the scale matrix of the (full-rank Gaussian) variational posterior over function values at the inducing points, conditional on observed data. Shape has the form \([b_1, ..., b_B, e_2, e_2]\), where \(b_1, ..., b_B\) is broadcast compatible with other parameters and \(e_2\) is the number of inducing points.

mean_fn
function that acts on index points to produce a (batch of) vector(s) of mean values at those index points. Takes a Tensor of shape \([b_1, ..., b_B, f_1, ..., f_F]\) and returns a Tensor whose shape is (broadcastable with) \([b_1, ..., b_B]\). Default value: NULL implies constant zero function.

observation_noise_variance
float Tensor representing the variance of the noise in the Normal likelihood distribution of the model. May be batched, in which case the batch shape must be broadcastable with the shapes of all other batched parameters (kernel$batch_shape, index_points, etc.). Default value: 0.

predictive_noise_variance
float Tensor representing additional variance in the posterior predictive model. If NULL, we simply re-use observation_noise_variance for the posterior predictive noise. If set explicitly, however, we use the given value. This allows us, for example, to omit predictive noise variance (by setting this to zero) to obtain noiseless posterior predictions of function values, conditioned on noisy observations.

jitter
float scalar Tensor added to the diagonal of the covariance matrix to ensure positive definiteness of the covariance matrix. Default value: 1e-6.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
A VGP is "trained" by selecting any kernel parameters, the locations of the inducing index points, and the variational parameters. Titsias (2009) and Hensman (2013) describe a variational lower bound on the marginal log likelihood of observed data, which this class offers through the variational_loss
method (this is the negative lower bound, for convenience when plugging into a TF Optimizer’s minimize function). Training may be done in minibatches.

Titsias (2009) describes a closed form for the optimal variational parameters, in the case of sufficiently small observational data (ie, small enough to fit in memory but big enough to warrant approximating the GP posterior). A method to compute these optimal parameters in terms of the full observational data set is provided as a static method, optimal_variational_posterior. It returns a MultivariateNormalLinearOperator instance with optimal location and scale parameters.

Mathematical Details
Notation We will in general be concerned about three collections of index points, and it’ll be good to give them names:

- x[1], ..., x[N]: observation index points – locations of our observed data.
- z[1], ..., z[M]: inducing index points – locations of the “summarizing” inducing points
- t[1], ..., t[P]: predictive index points – locations where we are making posterior predictions based on observations and the variational parameters.

To lighten notation, we’ll use X, Z, T to denote the above collections. Similarly, we’ll denote by f(X) the collection of function values at each of the x[i], and by Y, the collection of (noisy) observed data at each x[i]. We’ll denote kernel matrices generated from pairs of index points as K_tt, K_xt, K_tz, etc, e.g.,

\[
K_{tz} = 
\begin{vmatrix}
    k(t[1], z[1]) & k(t[1], z[2]) & \cdots & k(t[1], z[M]) \\
    k(t[2], z[1]) & k(t[2], z[2]) & \cdots & k(t[2], z[M]) \\
    \cdots & \cdots & \cdots & \cdots \\
    k(t[P], z[1]) & k(t[P], z[2]) & \cdots & k(t[P], z[M]) 
\end{vmatrix}
\]

Preliminaries A Gaussian process is an indexed collection of random variables, any finite collection of which are jointly Gaussian. Typically, the index set is some finite-dimensional, real vector space, and indeed we make this assumption in what follows. The GP may then be thought of as a distribution over functions on the index set. Samples from the GP are functions on the whole index set; these can’t be represented in finite compute memory, so one typically works with the marginals at a finite collection of index points. The properties of the GP are entirely determined by its mean function m and covariance function k. The generative process, assuming a mean-zero normal likelihood with stddev sigma, is

\[
f \sim GP(m, k) \\
Y | f(X) \sim Normal(f(X), \sigma), \quad i = 1, \ldots, N
\]

In finite terms (ie, marginalizing out all but a finite number of f(X), sigma), we can write

\[
f(X) \sim MVN(loc=m(X), \text{cov}=K_{xx}) \\
Y | f(X) \sim Normal(f(X), \sigma), \quad i = 1, \ldots, N
\]

Posterior inference is possible in analytical closed form but becomes intractible as data sizes get large. See Rasmussen (2006) for details.

The VGP
The VGP is an inducing point-based approximation of an exact GP posterior, where two approximating assumptions have been made:
1. function values at non-inducing points are mutually independent conditioned on function values at the inducing points,
2. the (expensive) posterior over function values at inducing points conditional on observations is replaced with an arbitrary (learnable) full-rank Gaussian distribution,

$q(f(Z)) = \text{MVN}(\text{loc}=m, \text{scale}=S)$,

where $m$ and $S$ are parameters to be chosen by optimizing an evidence lower bound (ELBO). The posterior predictive distribution becomes

$q(f(T)) = \int df(Z) \ p(f(T) | f(Z)) \ q(f(Z)) = \text{MVN}(\text{loc} = A @ m, \text{scale} = B^{1/2})$

where

$A = K_{tz} @ K_{zz}^{-1}$

$B = K_{tt} - A @ (K_{zz} - S S^T) A^T$

The approximate posterior predictive distribution $q(f(T))$ is what the VariationalGaussianProcess class represents.

Model selection in this framework entails choosing the kernel parameters, inducing point locations, and variational parameters. We do this by optimizing a variational lower bound on the marginal log likelihood of observed data. The lower bound takes the following form (see Titsias (2009) and Hensman (2013) for details on the derivation):

$L(Z, m, S, Y) = \text{MVN}(\text{loc}=(K_{zx} @ K_{zz}^{-1}) @ m, \text{scale(diag)}=\sigma).\text{log}\_\text{prob}(Y) -$

$(\text{Tr}(K_{xx} - K_{zx} @ K_{xz} @ K_{zz}^{-1} @ K_{xz}) +$

$\text{Tr}(S @ S^T @ K_{zz}^{-1} @ K_{zx} @ K_{xz} @ K_{zz}^{-1})) / (2 * \sigma^2) -$

$\text{KL}(q(f(Z)) || p(f(Z))))$

where in the final KL term, $p(f(Z))$ is the GP prior on inducing point function values. This variational lower bound can be computed on minibatches of the full data set $(X, Y)$. A method to compute the negative variational lower bound is implemented as VariationalGaussianProcess$\text{variational\_loss}$.

Optimal variational parameters

As described in Titsias (2009), a closed form optimum for the variational location and scale parameters, $m$ and $S$, can be computed when the observational data are not prohibitively voluminous. The optimal_variational_posterior function to computes the optimal variational posterior distribution over inducing point function values in terms of the GP parameters (mean and kernel functions), inducing point locations, observation index points, and observations. Note that the inducing index point locations must still be optimized even when these parameters are known functions of the inducing index points. The optimal parameters are computed as follows:

$C = \sigma^2 - 2 (K_{zz} + K_{zx} @ K_{xz})^{-1}$

optimal Gaussian covariance: $K_{zz} @ C @ K_{zz}$

optimal Gaussian location: $\sigma^2 - 2 K_{zz} @ C @ K_{xz} @ Y$

Value

a distribution instance.
tfd_vector_deterministic

Vector Deterministic Distribution

Description
The VectorDeterministic distribution is parameterized by a batch point `loc` in R^k. The distribution is supported at this point only, and corresponds to a random variable that is constant, equal to `loc`.

Usage
```
tfd_vector_deterministic(loc, atol = NULL)
```
rtol = NULL,
validate_args = FALSE,
allow_nan_stats = TRUE,
name = "VectorDeterministic"
)

Arguments

loc
Numeric Tensor of shape [B1, ..., Bb, k], with b >= 0, k >= 0 The point (or batch of points) on which this distribution is supported.

atol
Non-negative Tensor of same dtype as loc and broadcastable shape. The absolute tolerance for comparing closeness to loc. Default is 0.

rtol
Non-negative Tensor of same dtype as loc and broadcastable shape. The relative tolerance for comparing closeness to loc. Default is 0.

validate_args
Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details

See Degenerate rv.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

tfd_vector_diffeomixture

VectorDiffeomixture distribution

Description

A vector diffeomixture (VDM) is a distribution parameterized by a convex combination of K component loc vectors, loc[k], k = 0,...,K-1, and K scale matrices scale[k], k = 0,..., K-1. It approximates the following compound distribution p(x) = int p(x | z) p(z) dz, where z is in the K-simplex, and p(x | z) := p(x | loc=sum_k z[k] loc[k], scale=sum_k z[k] scale[k])
tfd_vector_diffeomixture

Usage

tfd_vector_diffeomixture(
    mix_loc,
    temperature,
    distribution,
    loc = NULL,
    scale = NULL,
    quadrature_size = 8,
    quadrature_fn = tfp$distributions$quadrature_scheme_softmaxnormal_quantiles,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "VectorDiffeomixture"
)

Arguments

mix_loc float-like Tensor with shape [b1, ..., bB, K-1]. In terms of samples, larger mix_loc[...,k] => Z is more likely to put more weight on its kth component.

temperature float-like Tensor. Broadcastable with mix_loc. In terms of samples, smaller temperature means one component is more likely to dominate. I.e., smaller temperature makes the VDM look more like a standard mixture of K components.

distribution tfp$distributions$Distribution-like instance. Distribution from which iid samples are used as input to the selected affine transformation. Must be a scalar-batch, scalar-event distribution. Typically distribution$reparameterization_type = FULLY_REPARAMETERIZED or it is a function of non-trainable parameters. WARNING: If you backprop through a VectorDiffeomixture sample and the distribution is not FULLY_REPARAMETERIZED yet is a function of trainable variables, then the gradient will be incorrect!

loc Length-K list of float-type Tensors. The k-th element represents the shift used for the k-th affine transformation. If the k-th item is NULL, loc is implicitly 0. When specified, must have shape [B1, ..., Bb, d] where b >= 0 and d is the event size.

scale Length-K list of LinearOperators. Each should be positive-definite and operate on a d-dimensional vector space. The k-th element represents the scale used for the k-th affine transformation. LinearOperators must have shape [B1, ..., Bb, d, d], b >= 0, i.e., characterizes b-batches of d x d matrices

quadrature_size integer scalar representing number of quadrature points. Larger quadrature_size means q_N(x) better approximates p(x).

quadrature_fn Function taking normal_loc, normal_scale, quadrature_size, validate_args and returning tuple(grid,probs) representing the SoftmaxNormal grid and corresponding normalized weight. normalized) weight. Default value: quadrature_scheme_softmaxnormal_quantiles.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
The integral \(\int p(x | z) p(z) \, dz\) is approximated with a quadrature scheme adapted to the mixture density \(p(z)\). The \(N\) quadrature points \(z_{\{N, n\}}\) and weights \(w_{\{N, n\}}\) (which are non-negative and sum to 1) are chosen such that \(q_N(x) := \sum_{n=1}^N w_{\{n, N\}} p(x | z_{\{N, n\}}) \rightarrow p(x)\) as \(N \rightarrow \infty\).

Since \(q_N(x)\) is in fact a mixture (of \(N\) points), we may sample from \(q_N\) exactly. It is important to note that the VDM is defined as \(q_N\) above, and not \(p(x)\). Therefore, sampling and pdf may be implemented as exact (up to floating point error) methods.

A common choice for the conditional \(p(x | z)\) is a multivariate Normal. The implemented marginal \(p(z)\) is the SoftmaxNormal, which is a \(K-1\) dimensional Normal transformed by a SoftmaxCentered bijector, making it a density on the \(K\)-simplex. That is, \(Z = \text{SoftmaxCentered}(X), X = \text{Normal}(\text{mix_loc} / \text{temperature}, 1 / \text{temperature})\)

The default quadrature scheme chooses \(z_{\{N, n\}}\) as \(N\) midpoints of the quantiles of \(p(z)\) (generalized quantiles if \(K > 2\)). See Dillon and Langmore (2018) for more details.

About Vector distributions in TensorFlow.

The VectorDiffeomixture is a non-standard distribution that has properties particularly useful in variational Bayesian methods. Conditioned on a draw from the SoftmaxNormal, \(X | z\) is a vector whose components are linear combinations of affine transformations, thus is itself an affine transformation.

Note: The marginals \(X_1 | v, \ldots, X_d | v\) are not generally identical to some parameterization of distribution. This is due to the fact that the sum of draws from distribution are not generally itself the same distribution.

About Diffeomixtures and reparameterization.

The VectorDiffeomixture is designed to be reparameterized, i.e., its parameters are only used to transform samples from a distribution which has no trainable parameters. This property is important because backprop stops at sources of stochasticity. That is, as long as the parameters are used after the underlying source of stochasticity, the computed gradient is accurate. Reparameterization means that we can use gradient-descent (via backprop) to optimize Monte-Carlo objectives. Such objectives are a finite-sample approximation of an expectation and arise throughout scientific computing.

WARNING: If you backprop through a VectorDiffeomixture sample and the "base" distribution is both: not FULLY_REPARAMETERIZED and a function of trainable variables, then the gradient is not guaranteed correct!

Value
a distribution instance.
tfd_vector_exponential_diag

The vectorization of the Exponential distribution on \( \mathbb{R}^k \)

**Description**

The vector exponential distribution is defined over a subset of \( \mathbb{R}^k \), and parameterized by a (batch of) length-\( k \) `loc` vector and a (batch of) \( k \times k \) scale matrix: covariance = scale @ scale.T, where @ denotes matrix-multiplication.

**Usage**

```python
tfd_vector_exponential_diag(
    loc = NULL,
    scale_diag = NULL,
)```

**References**


**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

scale_identity_multiplier = NULL,
validate_args = FALSE,
allow_nan_stats = TRUE,
name = "VectorExponentialDiag"
)

Arguments

loc Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

scale_diag Non-zero, floating-point Tensor representing a diagonal matrix added to scale. May have shape [B1, ..., Bb, k], b >= 0, and characterizes b-batches of k x k diagonal matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

scale_identity_multiplier Non-zero, floating-point Tensor representing a scaled-identity-matrix added to scale. May have shape [B1, ..., Bb], b >= 0, and characterizes b-batches of scaled k x k identity matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

validate_args Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name name prefixed to Ops created by this class.

Details

Mathematical Details The probability density function (pdf) is defined over the image of the scale matrix + loc, applied to the positive half-space: Supp = {loc + scale @ x : x in R^k, x_1 > 0, ..., x_k > 0}. On this set,

pdf(y; loc, scale) = exp(-||x||_1) / Z, for y in Supp
x = inv(scale) @ (y - loc),
Z = |det(scale)|,

where:

- loc is a vector in R^k,
- scale is a linear operator in R^[k x k], cov = scale @ scale.T,
- Z denotes the normalization constant, and,
- ||x||_1 denotes the l1 norm of x, sum_i |x_i|. The VectorExponential distribution is a member of the location-scale family, i.e., it can be constructed as,

X = (X_1, ..., X_k), each X_i ~ Exponential(rate=1)
Y = (Y_1, ..., Y_k) = scale @ X + loc
About VectorExponential and Vector distributions in TensorFlow.

The VectorExponential is a non-standard distribution that has useful properties. The marginals $Y_1, ..., Y_k$ are not Exponential random variables, due to the fact that the sum of Exponential random variables is not Exponential. Instead, $Y$ is a vector whose components are linear combinations of Exponential random variables. Thus, $Y$ lives in the vector space generated by vectors of Exponential distributions. This allows the user to decide the mean and covariance (by setting loc and scale), while preserving some properties of the Exponential distribution. In particular, the tails of $Y_i$ will be (up to polynomial factors) exponentially decaying. To see this last statement, note that the pdf of $Y_i$ is the convolution of the pdf of $k$ independent Exponential random variables. One can then show by induction that distributions with exponential (up to polynomial factors) tails are closed under convolution.

The batch_shape is the broadcast shape between loc and scale arguments. The event_shape is given by last dimension of the matrix implied by scale. The last dimension of loc (if provided) must broadcast with this. Recall that covariance = 2 * scale @ scale.T. Additional leading dimensions (if any) will index batches. If both scale_diag and scale_identity_multiplier are NULL, then scale is the Identity matrix.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(), tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet(), tfd_dirichlet_multinomial(), tfd_dirichlet_categorical(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(), tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(), tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(), tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(), tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(), tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space_model(), tfd_lkj(), tfd_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(), tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diagonal(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal(), tfd_multivariate_normal_full_covariance(), tfd_multivariate_normal_linear_operator(), tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial(), tfd_normal(), tfd_one_hot_categorical(), tfd_pareto(), tfd_pixel_cnn(), tfd_poisson_log_normal_quadrature(), tfd_poisson(), tfd_power_spherical(), tfd_probit_bernoulli(), tfd_quantized(), tfd_relaxed_bernoulli(), tfd_relaxed_one_hot_categorical(), tfd_sample_distribution(), tfd_sinh_arcsinh(), tfd_sklam(), tfd_spherical_uniform(), tfd_student_t(), tfd_transformed_distribution(), tfd_triangular(), tfd_truncated_cauchy(), tfd_truncated_normal(), tfd_uniform(), tfd_variational_gaussianProcess(), tfd_vector_diffeomixture(), tfd_vector_exponential_linear_operator(), tfd_vector_laplace_diagonal(), tfd_vector_laplace_linear_operator(), tfd_vector_sinh_arcsinh_diag(), tfd_von_mises(), tfd_welbull(), tfd_wishart_linear_operator(), tfd_wishart_tri_l(), tfd_wishart(), tfd_zipf()
The vectorization of the Exponential distribution on $\mathbb{R}^k$

**Description**

The vector exponential distribution is defined over a subset of $\mathbb{R}^k$, and parameterized by a (batch of) length-$k$ `loc` vector and a (batch of) $k \times k$ `scale` matrix: covariance = `scale` @ `scale`.T, where @ denotes matrix-multiplication.

**Usage**

```python
tfd_vector_exponential_linear_operator(
    loc = NULL,
    scale = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "VectorExponentialLinearOperator"
)
```

**Arguments**

- `loc` Floating point tensor; the means of the distribution(s).
- `scale` Instance of LinearOperator with same dtype as `loc` and shape `[B1, ..., Bb, k, k]`.
- `validate_args` Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- `allow_nan_stats` Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- `name` name prefixed to Ops created by this class.

**Details**

Mathematical Details The probability density function (pdf) is

$$
pdf(y; \text{loc}, \text{scale}) = \exp(-||x||_1) / Z, \text{ for } y \text{ in } S(\text{loc}, \text{scale}),
$$

$$
x = \text{inv}(\text{scale}) @ (y - \text{loc}),
$$

$$
Z = |\text{det}(\text{scale})|,
$$

where:

- `loc` is a vector in $\mathbb{R}^k$,
- `scale` is a linear operator in $\mathbb{R}^{k \times k}$, cov = `scale` @ `scale`.T,
- $S = \{ \text{loc} + \text{scale} @ x : x \text{ in } \mathbb{R}^k, x_1 > 0, ..., x_k > 0 \}$, is an image of the positive half-space.
• $\|x\|_1$ denotes the $l_1$ norm of $x$, $\sum_i |x_i|$,
• $Z$ denotes the normalization constant.

The VectorExponential distribution is a member of the location-scale family, i.e., it can be constructed as,

$$X = (X_1, \ldots, X_k), \text{each } X_i \sim \text{Exponential}(\text{rate}=1)$$

$$Y = (Y_1, \ldots, Y_k) = \text{scale } \ast X + \text{loc}$$

About VectorExponential and Vector distributions in TensorFlow.

The VectorExponential is a non-standard distribution that has useful properties. The marginals $Y_1, \ldots, Y_k$ are not Exponential random variables, due to the fact that the sum of Exponential random variables is not Exponential. Instead, $Y$ is a vector whose components are linear combinations of Exponential random variables. Thus, $Y$ lives in the vector space generated by vectors of Exponential distributions. This allows the user to decide the mean and covariance (by setting $\text{loc}$ and $\text{scale}$), while preserving some properties of the Exponential distribution. In particular, the tails of $Y_i$ will be (up to polynomial factors) exponentially decaying. To see this last statement, note that the pdf of $Y_i$ is the convolution of the pdf of $k$ independent Exponential random variables. One can then show by induction that distributions with exponential (up to polynomial factors) tails are closed under convolution.

The batch_shape is the broadcast shape between $\text{loc}$ and $\text{scale}$ arguments. The event_shape is given by last dimension of the matrix implied by $\text{scale}$. The last dimension of $\text{loc}$ (if provided) must broadcast with this. Recall that covariance = $2 \ast \text{scale } \ast \text{scale}.T$. Additional leading dimensions (if any) will index batches.

#' @param loc Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().

Other distributions: tfd_autoregressive(), tfd_batch_reshape(), tfd_bates(), tfd_bernoulli(),

  tfd_beta_binomial(), tfd_beta(), tfd_binomial(), tfd_categorical(), tfd_cauchy(), tfd_chi2(),

  tfd_chisq(), tfd_cholesky_lkj(), tfd_continuous_bernoulli(), tfd_deterministic(), tfd_dirichlet()

  tfd_dirichlet_multinomial(), tfd_dirichlet(), tfd_empirical(), tfd_exp_gamma(), tfd_exp_inverse_gamma(), tfd_exponential(),

  tfd_gamma(), tfd_gamma(), tfd_gaussian_process_regression_model(), tfd_gaussian_process(),

  tfd_generalized_normal(), tfd_geometric(), tfd_gumbel(), tfd_half_cauchy(), tfd_half_normal(),

  tfd_hidden_markov_model(), tfd_horseshoe(), tfd_independent(), tfd_inverse_gamma(),

  tfd_inverse_gaussian(), tfd_johnson_s_u(), tfd_joint_distribution_named_auto_batched(),

  tfd_joint_distribution_named(), tfd_joint_distribution_sequential_auto_batched(),

  tfd_joint_distribution_sequential(), tfd_kumaraswamy(), tfd_laplace(), tfd_linear_gaussian_state_space

  tfd_lkj(), tfd_log_logistic(), tfd_log_normal(), tfd_logistic(), tfd_mixture_same_family(),

  tfd_mixture(), tfd_multinomial(), tfd_multivariate_normal_diag_plus_low_rank(), tfd_multivariate_normal_full_covariance(),

  tfd_multivariate_normal_linear_operator(),

  tfd_multivariate_normal_tri_l(), tfd_multivariate_student_t_linear_operator(), tfd_negative_binomial()
The vectorization of the Laplace distribution on $\mathbb{R}^k$

**Description**

The vector Laplace distribution is defined over $\mathbb{R}^k$, and parameterized by a (batch of) length-$k$ `loc` vector (the means) and a (batch of) $k \times k$ scale matrix: covariance = $2 \times \text{scale} \times \text{scale}^T$, where $\text{scale} \times \text{scale}^T$ denotes matrix-multiplication.

**Usage**

tfd_vector_laplace_diag(loc = NULL, scale_diag = NULL, scale_identity_multiplier = NULL, validate_args = FALSE, allow_nan_stats = TRUE, name = "VectorLaplaceDiag")

**Arguments**

- **loc**: Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape $[B1, ..., Bb, k]$ where $b \geq 0$ and $k$ is the event size.

- **scale_diag**: Non-zero, floating-point Tensor representing a diagonal matrix added to scale. May have shape $[B1, ..., Bb, k]$, $b \geq 0$, and characterizes $b$-batches of $k \times k$ diagonal matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

- **scale_identity_multiplier**: Non-zero, floating-point Tensor representing a scaled-identity-matrix added to scale. May have shape $[B1, ..., Bb]$, $b \geq 0$, and characterizes $b$-batches of scaled $k \times k$ identity matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
allow_nan_stats
Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name
name prefixed to Ops created by this class.

Details
Mathematical Details The probability density function (pdf) is,

\[
pdf(x; \text{loc}, \text{scale}) = \exp(-||y||_1) / Z
\]

\[
y = \text{inv}(\text{scale}) @ (x - \text{loc})
\]

\[
Z = 2^{*k} |\text{det}(\text{scale})|
\]

where:

- \text{loc} is a vector in \(\mathbb{R}^k\),
- \text{scale} is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} @ \text{scale}.^T\),
- \(Z\) denotes the normalization constant, and,
- \(||y||_1\) denotes the \(l_1\) norm of \(y\), \(\sum_i |y_i|\).

A (non-batch) scale matrix is:

\[
\text{scale} = \text{diag}(|\text{scale}_\text{diag} + \text{scale}_\text{identity}_\text{multiplier} \cdot \text{ones}(k)|)
\]

where:

- \text{scale}_\text{diag}.shape = [k], and,
- \text{scale}_\text{identity}_\text{multiplier}.shape = []. Additional leading dimensions (if any) will index batches. If both \text{scale}_\text{diag} and \text{scale}_\text{identity}_\text{multiplier} are NULL, then scale is the Identity matrix.

About VectorLaplace and Vector distributions in TensorFlow
The VectorLaplace is a non-standard distribution that has useful properties. The marginals \(Y_1, \ldots, Y_k\) are \textit{not} Laplace random variables, due to the fact that the sum of Laplace random variables is not Laplace. Instead, \(Y\) is a vector whose components are linear combinations of Laplace random variables. Thus, \(Y\) lives in the vector space generated by vectors of Laplace distributions. This allows the user to decide the mean and covariance (by setting \text{loc} and \text{scale}), while preserving some properties of the Laplace distribution. In particular, the tails of \(Y_i\) will be (up to polynomial factors) exponentially decaying. To see this last statement, note that the pdf of \(Y_i\) is the convolution of the pdf of \(k\) independent Laplace random variables. One can then show by induction that distributions with exponential (up to polynomial factors) tails are closed under convolution.

Value

a distribution instance.
See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


`tfd_lkj()`, `tfd_logistic()`, `tfd_log_normal()`, `tfd_logistic()`, `tfd_mixture_same_family()`, `tfd_mixture()`, `tfd_multinomial()`, `tfd_multivariate_normal_diag_plus_low_rank()`, `tfd_multivariate_normal_diag()`, `tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_normal_full_covariance()`, `tfd_multivariate_normal_linear_operator()`, `tfd_multivariate_student_t_linear_operator()`, `tfd_negative_binomial()`, `tfd_normal()`, `tfd_one_hot_categorical()`, `tfd_pareto()`, `tfd_pixel_cnn()`, `tfd_poisson_log_normal_quadrature_compound()`, `tfd_power_spherical()`, `tfd_probit_bernoulli()`, `tfd_quantized()`, `tfd_relaxed_bernoulli()`, `tfd_relaxed_one_hot_categorical()`, `tfd_sample_distribution()`, `tfd_sinh_arcsinh()`, `tfd_skellam()`, `tfd_spherical_uniform()`, `tfd_student_t_process()`, `tfd_student_t()`, `tfd_transformed_distribution()`, `tfd_triangular()`, `tfd_truncated_cauchy()`, `tfd_truncated_normal()`, `tfd_uniform()`, `tfd_von_mises_fisher()`, `tfd_vector_diffeomixture()`, `tfd_vector_exponential_diag()`, `tfd_vector_exponential_linear_operator()`, `tfd_vector_laplace_linear_operator()`, `tfd_vector_sinh_arcsinh_diag()`, `tfd_von_mises()`, `tfd_weibull()`, `tfd_wishart_linear_operator()`, `tfd_wishart_tri_l()`, `tfd_wishart()`, `tfd_zipf()`

---

tfd_vector_laplace_linear_operator

The vectorization of the Laplace distribution on \( \mathbb{R}^k \)

Description

The vector laplace distribution is defined over \( \mathbb{R}^k \), and parameterized by a (batch of) length-k loc vector (the means) and a (batch of) k x k scale matrix: covariance = 2 * scale @ scale.T, where @ denotes matrix-multiplication.

Usage

tfd_vector_laplace_linear_operator(
    loc = NULL,
    scale = NULL,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "VectorLaplaceLinearOperator"
)
Arguments

- **loc**: Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape \([B_1, ..., B_b, k]\) where \(b \geq 0\) and \(k\) is the event size.
- **scale**: Instance of LinearOperator with same dtype as loc and shape \([B_1, ..., B_b, k, k]\).
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details

Mathematical Details The probability density function (pdf) is,

\[
pdf(x; \text{loc}, \text{scale}) = \exp(-||y||_1) / Z,
\]

\[
y = \text{inv}(\text{scale}) @ (x - \text{loc}),
\]

\[
Z = 2**k |\det(\text{scale})|,
\]

where:

- \(\text{loc}\) is a vector in \(\mathbb{R}^k\),
- \(\text{scale}\) is a linear operator in \(\mathbb{R}^{k \times k}\), \(\text{cov} = \text{scale} @ \text{scale}\cdot T\),
- \(Z\) denotes the normalization constant, and,
- \(||y||_1\) denotes the \(l1\) norm of \(y\), \('\sum_i |y_i|'\).

The \text{VectorLaplace} distribution is a member of the location-scale family, i.e., it can be constructed as,

\[
X = (X_1, ..., X_k), \text{each } X_i \sim \text{Laplace}(\text{loc}=0, \text{scale}=1)
\]

\[
Y = (Y_1, ..., Y_k) = \text{scale} @ X + \text{loc}
\]

About \text{VectorLaplace} and \text{Vector} distributions in TensorFlow

The \text{VectorLaplace} is a non-standard distribution that has useful properties. The marginals \(Y_1, ..., Y_k\) are not Laplace random variables, due to the fact that the sum of Laplace random variables is not Laplace. Instead, \(Y\) is a vector whose components are linear combinations of Laplace random variables. Thus, \(Y\) lives in the vector space generated by vectors of Laplace distributions. This allows the user to decide the mean and covariance (by setting \(\text{loc}\) and \(\text{scale}\)), while preserving some properties of the Laplace distribution. In particular, the tails of \(Y_i\) will be (up to polynomial factors) exponentially decaying. To see this last statement, note that the pdf of \(Y_i\) is the convolution of the pdf of \(k\) independent Laplace random variables. One can then show by induction that distributions with exponential (up to polynomial factors) tails are closed under convolution.

The batch_shape is the broadcast shape between \(\text{loc}\) and \(\text{scale}\) arguments. The event_shape is given by last dimension of the matrix implied by \(\text{scale}\). The last dimension of \(\text{loc}\) (if provided) must broadcast with this. Recall that \(\text{covariance} = 2 \ast \text{scale} @ \text{scale}\cdot T\). Additional leading dimensions (if any) will index batches.
**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

**tfd_vector_sinh_arcsinh_diag**

_The (diagonal) SinhArcsinh transformation of a distribution on \( \mathbb{R}^k \)_

**Description**

This distribution models a random vector \( Y = (Y_1, \ldots, Y_k) \), making use of a SinhArcsinh transformation (which has adjustable tailweight and skew), a rescaling, and a shift. The SinhArcsinh transformation of the Normal is described in great depth in Sinh-arcsinh distributions. Here we use a slightly different parameterization, in terms of tailweight and skewness. Additionally we allow for distributions other than Normal, and control over scale as well as a "shift" parameter \( \text{loc} \).

**Usage**

```r
  tfd_vector_sinh_arcsinh_diag(
  loc = NULL,
)```

Arguments

loc  Floating-point Tensor. If this is set to NULL, loc is implicitly 0. When specified, may have shape [B1, ..., Bb, k] where b >= 0 and k is the event size.

scale_diag  Non-zero, floating-point Tensor representing a diagonal matrix added to scale. May have shape [B1, ..., Bb, k], b >= 0, and characterizes b-batches of k x k diagonal matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

scale_identity_multiplier  Non-zero, floating-point Tensor representing a scale-identity-matrix added to scale. May have shape [B1, ..., Bb], b >= 0, and characterizes b-batches of scale k x k identity matrices added to scale. When both scale_identity_multiplier and scale_diag are NULL then scale is the Identity.

skewness  Skewness parameter. floating-point Tensor with shape broadcastable with event_shape.

tailweight  Tailweight parameter. floating-point Tensor with shape broadcastable with event_shape.

distribution tf$distributions$Distribution-like instance. Distribution from which k iid samples are used as input to transformation F. Default is tf$d_normal(loc = 0, scale = 1). Must be a scalar-batch, scalar-event distribution. Typically distribution$reparameterization_type = FULLY_REPARAMETERIZED or it is a function of non-trainable parameters. WARNING: If you backprop through a VectorSinhArcsinhDiag sample and distribution is not FULLY_REPARAMETERIZED yet is a function of trainable variables, then the gradient will be incorrect!

validate_args  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

allow_nan_stats  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

name  name prefixed to Ops created by this class.

Details

Mathematical Details

Given iid random vector Z = (Z1,...,Zk), we define the VectorSinhArcsinhDiag transformation of Z, Y, parameterized by (loc, scale, skewness, tailweight), via the relation (with @ denoting matrix multiplication):
Y := loc + scale @ F(Z) * (2 / F_0(Z))
F(Z) := Sinh((Arcsinh(Z) + skewness) * tailweight)
F_0(Z) := Sinh(Arcsinh(Z) * tailweight)

This distribution is similar to the location-scale transformation
L(Z) := loc + scale @ Z in the following ways:

- If skewness = 0 and tailweight = 1 (the defaults), F(Z) = Z, and then Y = L(Z) exactly.
- loc is used in both to shift the result by a constant factor.
- The multiplication of scale by 2 / F_0(Z) ensures that if skewness = 0 P[Y - loc <= 2 * scale] = P[L(Z) - loc <= 2 * scale]. Thus it can be said that the weights in the tails of Y and L(Z) beyond loc + 2 * scale are the same. This distribution is different than loc + scale @ Z due to the reshaping done by F:
  - Positive (negative) skewness leads to positive (negative) skew.
  - Positive skew means, the mode of F(Z) is "tilted" to the right.
  - Positive skew means positive values of F(Z) become more likely, and negative values become less likely.
  - Larger (smaller) tailweight leads to fatter (thinner) tails.
  - Fatter tails mean larger values of |F(Z)| become more likely.
  - tailweight < 1 leads to a distribution that is "flat" around Y = loc, and a very steep drop-off in the tails.
  - tailweight > 1 leads to a distribution more peaked at the mode with heavier tails. To see the argument about the tails, note that for |Z| >> 1 and |Z| >> (|skewness| * tailweight)**tailweight, we have Y approx 0.5 Z**tailweight e**(sign(Z) skewness * tailweight).

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
tfd_von_mises

The von Mises distribution over angles

**Description**

The von Mises distribution is a univariate directional distribution. Similarly to Normal distribution, it is a maximum entropy distribution. The samples of this distribution are angles, measured in radians. They are 2 pi-periodic: \( x = 0 \) and \( x = 2\pi \) are equivalent. This means that the density is also 2 pi-periodic. The generated samples, however, are guaranteed to be in \([-\pi, \pi)\) range. When concentration = 0, this distribution becomes a Uniform distribution on the \([-\pi, \pi)\) domain.

**Usage**

```r
  tfd_von_mises(
    loc,
    concentration,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "VonMises"
  )
```

**Arguments**

- **loc**
  Floating point tensor, the circular means of the distribution(s).

- **concentration**
  Floating point tensor, the level of concentration of the distribution(s) around loc. Must take non-negative values. concentration = 0 defines a Uniform distribution, while concentration = +inf indicates a Deterministic distribution at loc.

- **validate_args**
  Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- **allow_nan_stats**
  Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

- **name**
  name prefixed to Ops created by this class.
Details

The von Mises distribution is a special case of von Mises-Fisher distribution for n=2. However, the TFP’s VonMisesFisher implementation represents the samples and location as (x, y) points on a circle, while VonMises represents them as scalar angles.

Mathematical details The probability density function (pdf) of this distribution is,

$$p(x; \text{loc}, \text{concentration}) = \frac{\exp(\text{concentration} \cos(x - \text{loc}))}{Z}$$

$$Z = 2 \pi I_0(\text{concentration})$$

where:

- $I_0(\text{concentration})$ is the modified Bessel function of order zero;
- $\text{loc}$ the circular mean of the distribution, a scalar. It can take arbitrary values, but it is $2\pi$-periodic: $\text{loc}$ and $\text{loc} + 2\pi$ result in the same distribution.
- $\text{concentration} \geq 0$ parameter is the concentration parameter. When $\text{concentration} = 0$, this distribution becomes a Uniform distribution on $[-\pi, \pi)$.

The parameters $\text{loc}$ and concentration must be shaped in a way that supports broadcasting (e.g. $\text{loc} + \text{concentration}$ is a valid operation).

Value

a distribution instance.

See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.

The von Mises-Fisher distribution over unit vectors on $S^{n-1}$

**Description**

The von Mises-Fisher distribution is a directional distribution over vectors on the unit hypersphere $S^{n-1}$ embedded in $n$ dimensions ($\mathbb{R}^n$).

**Usage**

```python
tfd_von_mises_fisher(
    mean_direction,
    concentration,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "VonMisesFisher"
)
```

**Arguments**

- `mean_direction`: Floating-point Tensor with shape [B1, ... Bn, D]. A unit vector indicating the mode of the distribution, or the unit-normalized direction of the mean. (This is not in general the mean of the distribution; the mean is not generally in the support of the distribution.) NOTE: D is currently restricted to <= 5.

- `concentration`: Floating-point Tensor having batch shape [B1, ... Bn] broadcastable with mean_direction. The level of concentration of samples around the mean_direction. concentration=0 indicates a uniform distribution over the unit hypersphere, and concentration=+inf indicates a Deterministic distribution (delta function) at mean_direction.

- `validate_args`: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

- `allow_nan_stats`: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

- `name`: name prefixed to Ops created by this class.

**Details**

Mathematical details The probability density function (pdf) is,

$$
\text{pdf}(x; \mu, \kappa) = C(\kappa) \exp(\kappa \ast \mu^T x)
$$

where,

- $C(\kappa) = \frac{(2 \pi)^{-n/2} \kappa^{n/2-1}}{I_{n/2-1}(\kappa)}$, $I_v(z)$ being the modified Bessel function of the first kind of order $v$
where:

- **mean_direction** = \( \mu \); a unit vector in \( \mathbb{R}^k \),
- **concentration** = \( \kappa \); scalar real \( \geq 0 \), concentration of samples around **mean_direction**, where 0 pertains to the uniform distribution on the hypersphere, and \( \infty \) indicates a delta function at **mean_direction**.

**NOTE:** Currently only \( n \) in 2, 3, 4, 5 are supported. For \( n=5 \) some numerical instability can occur for low concentrations (<.01).

**Value**

a distribution instance.

**See Also**

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`. 

Description

The probability density function (pdf) of this distribution is,

$$pdf(x; \lambda, k) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k - 1} \exp\left(-\left(\frac{x}{\lambda}\right)^k\right)$$

where concentration = k and scale = lambda. The cumulative density function of this distribution is,

$$cdf(x; \lambda, k) = 1 - \exp\left(-\left(\frac{x}{\lambda}\right)^k\right)$$

The Weibull distribution includes the Exponential and Rayleigh distributions as special cases:

Exponential(rate) = Weibull(concentration=1., 1./rate)

Rayleigh(scale) = Weibull(concentration=2., sqrt(2.) * scale)

Usage

tfd_weibull(
    concentration,
    scale,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "Weibull"
)

Arguments

- concentration: Positive Float-type Tensor, the concentration param of the distribution. Must contain only positive values.
- scale: Positive Float-type Tensor, the scale param of the distribution. Must contain only positive values.
- validate_args: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- allow_nan_stats: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- name: name prefixed to Ops created by this class.

Value

a distribution instance.
tfd_wishart

The matrix Wishart distribution on positive definite matrices

Description

This distribution is defined by a scalar number of degrees of freedom df and an instance of LinearOperator, which provides matrix-free access to a symmetric positive definite operator, which defines the scale matrix.

Usage

tfd_wishart(
  df,
  scale = NULL,
  scale_tril = NULL,
  input_output_cholesky = FALSE,
  validate_args = FALSE,
  allow_nan_stats = TRUE,
  name = "Wishart"
)
Arguments

- **df**: float or double tensor, the degrees of freedom of the distribution(s). df must be greater than or equal to k.

- **scale**: float or double Tensor. The symmetric positive definite scale matrix of the distribution. Exactly one of scale and 'scale_tril must be passed.

- **scale_tril**: float or double Tensor. The Cholesky factorization of the symmetric positive definite scale matrix of the distribution. Exactly one of scale and 'scale_tril must be passed.

**input_output_cholesky**

Logical. If TRUE, functions whose input or output have the semantics of samples assume inputs are in Cholesky form and return outputs in Cholesky form. In particular, if this flag is TRUE, input to log_prob is presumed of Cholesky form and output from sample, mean, and mode are of Cholesky form. Setting this argument to TRUE is purely a computational optimization and does not change the underlying distribution; for instance, mean returns the Cholesky of the mean, not the mean of Cholesky factors. The variance and stddev methods are unaffected by this flag. Default value: FALSE (i.e., input/output does not have Cholesky semantics).

**validate_args**

Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

**allow_nan_stats**

Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

**name**

name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
pdf(X; df, scale) = \det(X)^{0.5 (df-k-1)} \exp(-0.5 \ tr[\inv(scale) X]) / Z
\]

where:

- df >= k denotes the degrees of freedom,
- scale is a symmetric, positive definite, k x k matrix,
- Z is the normalizing constant, and,
- Gamma_k is the multivariate Gamma function.

Value

a distribution instance.
See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


tfd_wishart_linear_operator

The matrix Wishart distribution on positive definite matrices

Description

This distribution is defined by a scalar number of degrees of freedom df and an instance of LinearOperator, which provides matrix-free access to a symmetric positive definite operator, which defines the scale matrix.

Usage

```python
tfd_wishart_linear_operator(
    df,
    scale,
    input_output_cholesky = FALSE,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "WishartLinearOperator"
)
```
Arguments

**df** float or double tensor, the degrees of freedom of the distribution(s). df must be greater than or equal to k.

**scale** float or double instance of LinearOperator.

**input_output_cholesky** Logical. If TRUE, functions whose input or output have the semantics of samples assume inputs are in Cholesky form and return outputs in Cholesky form. In particular, if this flag is TRUE, input to log_prob is presumed of Cholesky form and output from sample, mean, and mode are of Cholesky form. Setting this argument to TRUE is purely a computational optimization and does not change the underlying distribution; for instance, mean returns the Cholesky of the mean, not the mean of Cholesky factors. The variance and stddev methods are unaffected by this flag. Default value: FALSE (i.e., input/output does not have Cholesky semantics).

**validate_args** Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.

**allow_nan_stats** Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.

**name** name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
    \text{pdf}(X; \text{df}, \text{scale}) = \frac{\det(X)^{0.5 (\text{df}-k-1)} \exp(-0.5 \text{tr}(\text{inv}(\text{scale}) X))}{Z}
\]

\[
    Z = 2^{0.5 \text{df} k} \left|\det(\text{scale})\right|^{0.5 \text{df}} \Gamma_k(0.5 \text{df})
\]

where:

- \( \text{df} \geq k \) denotes the degrees of freedom,
- \( \text{scale} \) is a symmetric, positive definite, \( k \times k \) matrix,
- \( Z \) is the normalizing constant, and,
- \( \Gamma_k \) is the multivariate Gamma function.

Value

a distribution instance.
tfd_wishart_tri_l

The matrix Wishart distribution parameterized with Cholesky factors.

Description

This distribution is defined by a scalar degrees of freedom df and a scale matrix, expressed as a lower triangular Cholesky factor.

Usage

tfd_wishart_tri_l(df,
    scale_tril,
    input_output_cholesky = FALSE,
    validate_args = FALSE,
    allow_nan_stats = TRUE,
    name = "WishartTriL"
)
Arguments

- **df**: float or double tensor, the degrees of freedom of the distribution(s). df must be greater than or equal to k.
- **scale_tril**: float or double Tensor. The Cholesky factorization of the symmetric positive definite scale matrix of the distribution.
- **input_output_cholesky**: Logical. If TRUE, functions whose input or output have the semantics of samples assume inputs are in Cholesky form and return outputs in Cholesky form. In particular, if this flag is TRUE, input to log_prob is presumed of Cholesky form and output from sample, mean, and mode are of Cholesky form. Setting this argument to TRUE is purely a computational optimization and does not change the underlying distribution; for instance, mean returns the Cholesky of the mean, not the mean of Cholesky factors. The variance and stddev methods are unaffected by this flag. Default value: FALSE (i.e., input/output does not have Cholesky semantics).
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Logical, default TRUE. When TRUE, statistics (e.g., mean, mode, variance) use the value NaN to indicate the result is undefined. When FALSE, an exception is raised if one or more of the statistic’s batch members are undefined.
- **name**: name prefixed to Ops created by this class.

Details

Mathematical Details

The probability density function (pdf) is,

\[
pdf(X; \text{df}, \text{scale}) = \text{det}(X)^{(0.5 (\text{df}-k-1))} \exp\left(-0.5 \text{ tr}\left[\text{inv}(\text{scale}) X\right]\right) / Z
\]

\[
Z = 2^{(0.5 \text{ df} k)} |\text{det}(	ext{scale})|^{(0.5 \text{ df})} \text{Gamma}_k(0.5 \text{ df})
\]

where:

- df \(\geq\) k denotes the degrees of freedom,
- scale is a symmetric, positive definite, k x k matrix,
- Z is the normalizing constant, and,
- Gamma_k is the multivariate Gamma function.

Value

a distribution instance.
See Also

For usage examples see e.g. `tfd_sample()`, `tfd_log_prob()`, `tfd_mean()`.


---

**tfd_zipf** | **Zipf distribution**

**Description**

The Zipf distribution is parameterized by a power parameter.

**Usage**

```python
import tensorflow_probability as tfd

tfd_zipf(
    power,
    dtype = tf.int32,
    interpolate_nondiscrete = True,
    sample_maximum_iterations = 100,
    validate_args = False,
    allow_nan_stats = False,
    name = "Zipf"
)
```
Arguments

- **power**: Float like Tensor representing the power parameter. Must be strictly greater than 1.
- **dtype**: The dtype of Tensor returned by sample. Default value: tf$int32$.
- **interpolate_nondiscrete**: Logical. When FALSE, log_prob returns -inf (and prob returns 0) for non-integer inputs. When TRUE, log_prob evaluates the continuous function \(-power \log(k) - \log(zeta(power))\), which matches the Zipf pmf at integer arguments \(k\) (note that this function is not itself a normalized probability log-density). Default value: TRUE.
- **sample_maximum_iterations**: Maximum number of iterations of allowable iterations in sample. When validate_args=TRUE, samples which fail to reach convergence (subject to this cap) are masked out with self$dtype$min or nan depending on self$dtype$is_integer. Default value: 100.
- **validate_args**: Logical, default FALSE. When TRUE distribution parameters are checked for validity despite possibly degrading runtime performance. When FALSE invalid inputs may silently render incorrect outputs. Default value: FALSE.
- **allow_nan_stats**: Default value: FALSE.
- **name**: name prefixed to Ops created by this class.

Details

Mathematical Details The probability mass function (pmf) is,

\[
\text{pmf}(k; \alpha, k \geq 0) = \frac{k^{-\alpha}}{Z} \\
Z = \zeta(\alpha).
\]

where \(\alpha = \text{power}\) and \(Z\) is the normalization constant. \(\zeta\) is the Riemann zeta function. Note that gradients with respect to the power parameter are not supported in the current implementation.

Value

a distribution instance.

See Also

For usage examples see e.g. tfd_sample(), tfd_log_prob(), tfd_mean().
tfp_version

Description

TensorFlow Probability Version

Usage

tfp_version()
The Amari-alpha Csiszar-function in log-space

Description

A Csiszar-function is a member of $F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex} \}$.

Usage

\[
\text{vi_amari_alpha}(\logu, \alpha = 1, \text{self\_normalized} = \text{FALSE}, \text{name} = \text{NULL})
\]

Arguments

- \(\logu\) float-like Tensor representing \(\log(u)\) from above.
- \(\alpha\) float-like scalar.
- \(\text{self\_normalized}\) logical indicating whether \(f'(u=1)=0\). When \(f'(u=1)=0\) the implied Csiszar f-Divergence remains non-negative even when \(p, q\) are unnormalized measures.
- \(\text{name}\) name prefixed to Ops created by this function.

Details

When \(\text{self\_normalized} = \text{TRUE}\), the Amari-alpha Csiszar-function is:

\[
\begin{align*}
  f(u) &= \begin{cases} 
  -\log(u) + (u - 1), & \alpha = 0 \\
  u \log(u) - (u - 1), & \alpha = 1 \\
  \frac{(u^{\alpha} - 1) - \alpha (u - 1)}{(\alpha (\alpha - 1))}, & \text{otherwise}
  \end{cases}
\end{align*}
\]

When \(\text{self\_normalized} = \text{FALSE}\) the \((u - 1)\) terms are omitted.

Warning: when \(\alpha \neq 0\) and/or \(\text{self\_normalized} = \text{True}\) this function makes non-log-space calculations and may therefore be numerically unstable for \(\logu \gg 0\).

Value

\(\text{amari\_alpha\_of\_u}\) float-like Tensor of the Csiszar-function evaluated at \(u = \exp(\logu)\).

References

The Arithmetic-Geometric Csiszar-function in log-space

Description

A Csiszar-function is a member of \( F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex } \} \).

Usage

\[
\text{vi_arithmetic_geometric}(\log u, \text{self_normalized} = \text{FALSE}, \text{name} = \text{NULL})
\]

Arguments

- **logu**: float-like Tensor representing \( \log(u) \) from above.
- **self_normalized**: logical indicating whether \( f(u=1)=0 \). When \( f(u=1)=0 \) the implied Csiszar f-Divergence remains non-negative even when \( p, q \) are unnormalized measures.
- **name**: name prefixed to Ops created by this function.

Details

When \( \text{self_normalized} = \text{True} \) the Arithmetic-Geometric Csiszar-function is:

\[
f(u) = (1 + u) \log\left( \frac{1 + u}{\sqrt{u}} \right) - (1 + u) \log(2)
\]

When \( \text{self_normalized} = \text{False} \) the \( (1 + u) \log(2) \) term is omitted.

Observe that as an f-Divergence, this Csiszar-function implies:

\[
D_f[p, q] = KL[m, p] + KL[m, q]
\]

\[
m(x) = 0.5 \ p(x) + 0.5 \ q(x)
\]

In a sense, this divergence is the "reverse" of the Jensen-Shannon f-Divergence. This Csiszar-function induces a symmetric f-Divergence, i.e., \( D_f[p,q] = D_f[q,p] \).

Warning: when \( \text{self_normalized} = \text{True} \) this function makes non-log-space calculations and may therefore be numerically unstable for \( |\log u| \to 0^+ \).

Value

\text{arithmetic_geometric_of_u}: \text{float-like Tensor of the Csiszar-function evaluated at } u = \exp(\log u).
**vi_chi_square**

The chi-square Csiszar-function in log-space

**Description**

A Csiszar-function is a member of \( F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex} \} \).

**Usage**

\[
\text{vi_chi_square}(\log u, \text{name} = \text{NULL})
\]

**Arguments**

- \( \log u \): float-like Tensor representing \( \log(u) \) from above.
- \( \text{name} \): name prefixed to Ops created by this function.

**Details**

The Chi-square Csiszar-function is:

\[
f(u) = u^2 - 1
\]

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( \log u \gg 0 \).

**Value**

\( \text{chi_square_of_u} \): float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\log u) \).

**See Also**

Other vi-functions: `vi_amari_alpha()`, `vi_arithmetic_geometric()`, `vi_csiszar_vimco()`, `vi_dual_csiszar_function()`, `vi_fit_surrogate_posterior()`, `vi_jeffreys()`, `vi_jensen_shannon()`, `vi_kl_forward()`, `vi_kl_reverse()`, `vi_log1p_abs()`, `vi_modified_gan()`, `vi_monte_carlo_variational_loss()`, `vi_pearson()`, `vi_squared_hellinger()`, `vi_symmetrized_csiszar_function()`
vi_csiszar_vimco

Use VIMCO to lower the variance of the gradient of
\texttt{csiszar\_function(Avg(logu))}

Description

This function generalizes VIMCO (Mnih and Rezende, 2016) to Csiszar f-Divergences.

Usage

\begin{verbatim}
vi_csiszar_vimco(
  f,
  p_log_prob,
  q,
  num_draws,
  num_batch_draws = 1,
  seed = NULL,
  name = NULL
)
\end{verbatim}

Arguments

- **f**
  function representing a Csiszar-function in log-space.
- **p_log_prob**
  function representing the natural-log of the probability under distribution p. (In variational inference p is the joint distribution.)
- **q**
  tfd\_Distribution-like instance; must implement \texttt{sample(n,seed)} and \texttt{log\_prob(x)}. (In variational inference q is the approximate posterior distribution.)
- **num_draws**
  Integer scalar number of draws used to approximate the f-Divergence expectation.
- **num_batch_draws**
  Integer scalar number of draws used to approximate the f-Divergence expectation.
- **seed**
  integer seed for \texttt{q\$sample}.
- **name**
  String prefixed to Ops created by this function.

Details

Note: if \texttt{q.reparameterization\_type = tfd.FULLY\_REPARAMETERIZED}, consider using \texttt{monte\_carlo\_csiszar\_f\_divergence}.

The VIMCO loss is:

\begin{align*}
\text{vimco} &= f(\text{Avg}(\log u[i] \mid i = 0, \ldots, m-1)) \\
\text{where,} \\
\log u[i] &= \log( p(x, h[i]) / q(h[i] \mid x) ) \\
h[i] &\sim q(H \mid x)
\end{align*}

Interestingly, the VIMCO gradient is not the naive gradient of \texttt{vimco}. Rather, it is characterized by:
grad[vimco] - variance_reducing_term

where,

\[
\text{variance}_\text{reducing}_\text{term} = \sum_i \frac{\text{grad}[\log q(h[i] | x)] \times (\text{vimco} - f(\log \text{Avg}[h[j;i] : j=0,...,m-1])))}{\text{Var}_i} \\
h[j;i] = u[j] \quad \text{for } j=i, \quad \text{GeometricAverage}\{ u[k] : k!=i \} \quad \text{for } j\neq i
\]

(We omitted stop\_gradient for brevity. See implementation for more details.) The Avg[h[j;i]:j] term is a kind of "swap-out average" where the i-th element has been replaced by the leave-i-out Geometric-average.

This implementation prefers numerical precision over efficiency, i.e., \(O(\text{num}\_\text{draws} \times \text{num}\_\text{batch}\_\text{draws} \times \text{prod}(\text{batch\_shape}) \times \text{prod}(\text{event\_shape}))\). (The constant may be fairly large, perhaps around 12.)

**Value**

vimco The Csiszar f-Divergence generalized VIMCO objective

**References**


**See Also**

Other vi-functions: `vi_amari_alpha()`, `vi_arithmetic_geometric()`, `vi_chi_square()`, `vi_dual_csiszar_function()`, `vi_fit_surrogate_posterior()`, `vi_jeffreys()`, `vi_jensen_shannon()`, `vi_kl_forward()`, `vi_kl_reverse()`, `vi_log1p_abs()`, `vi_modified_gan()`, `vi_monte_carlo_variational_loss()`, `vi_pearson()`, `vi_squared_hellinger()`, `vi_symmetrized_csiszar_function()`

---

**Description**

A Csiszar-function is a member of \(F = \{ f:R_+ \to R : f \text{ convex} \} \).

**Usage**

\[ \text{vi_dual_csiszar_function}(\text{logu}, \text{csiszar}\_\text{function}, \text{name} = \text{NULL}) \]

**Arguments**

- **logu** float-like Tensor representing \(\log(u)\) from above.
- **csiszar\_function** function representing a Csiszar-function over log-domain.
- **name** name prefixed to Ops created by this function.
Details

The Csiszar-dual is defined as:

\[ f^*(u) = u f(1 / u) \]

where \( f \) is some other Csiszar-function. For example, the dual of \( \text{kl}_\text{reverse} \) is \( \text{kl}_\text{forward} \), i.e.,

\[ f(u) = -\log(u) \]
\[ f^*(u) = u f(1 / u) = -u \log(1 / u) = u \log(u) \]

The dual of the dual is the original function:

\[ f^{**}(u) = \{u f(1/u)\}^*(u) = u (1/u) f(1/(1/u)) = f(u) \]

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( \log u \gg 0 \).

Value

dual_f_of_u float-like Tensor of the result of calculating the dual of \( f \) at \( u = \exp(\log u) \).

See Also

Other vi-functions: \( \text{vi}_\text{amari}_\alpha() \), \( \text{vi}_\text{arithmetic}_\text{geometric}() \), \( \text{vi}_\text{chi}_\text{square}() \), \( \text{vi}_\text{csiszar}_\text{vimco}() \), \( \text{vi}_\text{fit}_\text{surrogate}_\text{posterior}() \), \( \text{vi}_\text{jeffreys}() \), \( \text{vi}_\text{jensen}_\text{shannon}() \), \( \text{vi}_\text{kl}_\text{forward}() \), \( \text{vi}_\text{kl}_\text{reverse}() \), \( \text{vi}_\text{log1p}_\text{abs}() \), \( \text{vi}_\text{modified}_\text{gan}() \), \( \text{vi}_\text{monte}_\text{carlo}_\text{variational}_\text{loss}() \), \( \text{vi}_\text{pearson}() \), \( \text{vi}_\text{symmetrized}_\text{csiszar}_\text{function}() \)

---

vi_fit_surrogate_posterior

* Fit a surrogate posterior to a target (unnormalized) log density *

Description

The default behavior constructs and minimizes the negative variational evidence lower bound (ELBO),
given by

\[
\text{q_samples} \leftarrow \text{surrogate_posterior}\$\text{sample}(\text{num_draws}) \quad \text{elbo_loss} \leftarrow -\text{tf}\$\text{reduce_mean}(\text{target_log_prob_fn}(\text{q_samples}) - \text{surrogate_posterior}\$\text{log_prob}(\text{q_samples}))
\]

Usage

```r
vi_fit_surrogate_posterior(
  target_log_prob_fn,
  surrogate_posterior,
  optimizer,
  num_steps,
  convergence_criterion = NULL,
  trace_fn = tf$p$optimization$'\_trace_loss',
)```

variational_loss_fn = NULL,
discrepancy_fn = tfp$vi$kl_reverse,
sample_size = 1,
importance_sample_size = 1,
trainable_variables = NULL,
jit_compile = NULL,
seed = NULL,
name = "fit_surrogate_posterior"
)

Arguments

target_log_prob_fn

function that takes a set of Tensor arguments and returns a Tensor log-density. Given q_sample <- surrogate_posterior$sample(sample_size), this will be (in Python) called as target_log_prob_fn(q_sample) if q_sample is a list or a tuple, target_log_prob_fn(**q_sample) if q_sample is a dictionary, or target_log_prob_fn(q_sample) if q_sample is a Tensor. It should support batched evaluation, i.e., should return a result of shape [sample_size].

surrogate_posterior

A tfp$distributions$Distribution instance defining a variational posterior (could be a tfp$distributions$JointDistribution). Crucially, the distribution’s log_prob and (if reparameterized) sample methods must directly invoke all ops that generate gradients to the underlying variables. One way to ensure this is to use tfp$util$DeferredTensor to represent any parameters defined as transformations of unconstrained variables, so that the transformations execute at runtime instead of at distribution creation.

optimizer

Optimizer instance to use. This may be a TF1-style tf$train$Optimizer, TF2-style tf$optimizers$Optimizer, or any Python-compatible object that implements optimizer$apply_gradients(grads_and_vars).

num_steps

integer number of steps to run the optimizer.

convergence_criterion

Optional instance of tfp$optimizer$convergence_criteria$ConvergenceCriterion representing a criterion for detecting convergence. If NULL, the optimization will run for num_steps steps, otherwise, it will run for at most num_steps steps, as determined by the provided criterion. Default value: NULL.

trace_fn

function with signature state = trace_fn(loss,grads,variables), where state may be a Tensor or nested structure of Tensors. The state values are accumulated (by tf$scan) and returned. The default trace_fn simply returns the loss, but in general can depend on the gradients and variables (if trainable_variables is not NULL then variables==trainable_variables; otherwise it is the list of all variables accessed during execution of loss_fn()), as well as any other quantities captured in the closure of trace_fn, for example, statistics of a variational distribution. Default value: function(loss,grads,variables) loss.

variational_loss_fn

function with signature loss <- variational_loss_fn(target_log_prob_fn,surrogate_posterior,...) defining a variational loss function. The default is a Monte Carlo approximation
to the standard evidence lower bound (ELBO), equivalent to minimizing the 'reverse' KL[q||p] divergence between the surrogate q and true posterior p. Default value: `functools.partial(tfp.vi.monte_carlo_variational_loss, discrepancy_fn=tpf.vi.kl_reverse, use_reparameterization=True)`.

**discrepancy_fn**
A function of Python callable representing a Csiszar f function in log-space. See the docs for `tfp.vi.monte_carlo_variational_loss` for examples. This argument is ignored if a `variational_loss_fn` is explicitly specified. Default value: `tfp$vi$kl_reverse`.

**sample_size**
Integer number of Monte Carlo samples to use in estimating the variational divergence. Larger values may stabilize the optimization, but at higher cost per step in time and memory. Default value: 1.

**importance_sample_size**
An integer number of terms used to define an importance-weighted divergence. If `importance_sample_size > 1`, then the surrogate posterior is optimized to function as an importance-sampling proposal distribution. In this case, posterior expectations should be approximated by importance sampling, as demonstrated in the example below. This argument is ignored if a `variational_loss_fn` is explicitly specified. Default value: 1.

**trainable_variables**
Optional list of `tf$Variable` instances to optimize with respect to. If NULL, defaults to the set of all variables accessed during the computation of the variational bound, i.e., those defining `surrogate_posterior` and the model `target_log_prob_fn`. Default value: NULL.

**jit_compile**
If TRUE, compiles the loss function and gradient update using XLA. XLA performs compiler optimizations, such as fusion, and attempts to emit more efficient code. This may drastically improve the performance. See the docs for `tf.function`. Default value: NULL.

**seed**
Integer to seed the random number generator.

**name**
Name prefixed to ops created by this function. Default value: 'fit_surrogate_posterior'.

### Details
This corresponds to minimizing the 'reverse' Kullback-Liebler divergence (KL[q||p]) between the variational distribution and the unnormalized `target_log_prob_fn`, and defines a lower bound on the marginal log likelihood, log p(x) >= -elbo_loss.

More generally, this function supports fitting variational distributions that minimize any Csiszar f-divergence.

### Value
`results` Tensor or nested structure of Tensors, according to the return type of `result_fn`. Each Tensor has an added leading dimension of size `num_steps`, packing the trajectory of the result over the course of the optimization.

### See Also
The Jeffreys Csiszar-function in log-space

Description

A Csiszar-function is a member of $F = \{ f: R_+ \to R : f \text{ convex} \}$.

Usage

vi_jeffreys(logu, name = NULL)

Arguments

- logu: float-like Tensor representing $\log(u)$ from above.
- name: name prefixed to Ops created by this function.

Details

The Jeffreys Csiszar-function is:

$$ f(u) = 0.5 \left( u \log(u) - \log(u) \right) $$
$$ = 0.5 \text{kl.forward} + 0.5 \text{kl.reverse} $$
$$ = \text{symmetrized_csiszar_function}(\text{kl.reverse}) $$
$$ = \text{symmetrized_csiszar_function}(\text{kl.forward}) $$

This Csiszar-function induces a symmetric f-Divergence, i.e., $D_f[p, q] = D_f[q, p]$.

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for $\log u \gg 0$.

Value

jeffreys_of_u: float-like Tensor of the Csiszar-function evaluated at $u = \exp(\logu)$.

See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jensen_shannon(), vi_kl_forward(), vi_kl_reverse(), vi_log1p_abs(), vi_modified_gan(), vi_monte_carlo_variational_loss(), vi_pearson(), vi_squared_hellinger(), vi_symmetrized_csiszar_function()
The Jensen-Shannon Csiszar-function in log-space

Description

A Csiszar-function is a member of $F = \{ f:R_+ \to R : f \text{ convex} \}$.

Usage

\[
\text{vi\_jensen\_shannon}(\log u, \text{self\_normalized} = \text{FALSE}, \text{name} = \text{NULL})
\]

Arguments

- \( \log u \): float-like Tensor representing \( \log(u) \) from above.
- \( \text{self\_normalized} \): logical indicating whether \( f'(u=1)=0 \). When \( f'(u=1)=0 \) the implied Csiszar f-Divergence remains non-negative even when \( p, q \) are unnormalized measures.
- \( \text{name} \): name prefixed to Ops created by this function.

Details

When \( \text{self\_normalized} = \text{True} \), the Jensen-Shannon Csiszar-function is:

\[
f(u) = u \log(u) - (1 + u) \log(1 + u) + (u + 1) \log(2)
\]

When \( \text{self\_normalized} = \text{False} \) the \( (u + 1) \log(2) \) term is omitted.

Observe that as an f-Divergence, this Csiszar-function implies:

\[
D_f[p, q] = KL[p, m] + KL[q, m]
\]

\[
m(x) = 0.5 \ p(x) + 0.5 \ q(x)
\]

In a sense, this divergence is the "reverse" of the Arithmetic-Geometric f-Divergence.

This Csiszar-function induces a symmetric f-Divergence, i.e., \( D_f[p, q] = D_f[q, p] \).

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( \log u \gg 0 \).

Value

\( \text{jensen\_shannon\_of\_u} \), float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\log u) \).

References

vi_kl_forward

The forward Kullback-Leibler Csiszar-function in log-space

Description

A Csiszar-function is a member of \( F = \{ f:R_+ \to R : f \text{ convex} \}. \)

Usage

vi_kl_forward(logu, self_normalized = FALSE, name = NULL)

Arguments

- `logu`: float-like Tensor representing \( \log(u) \) from above.
- `self_normalized`: logical indicating whether \( f'(u=1)=0. \) When \( f'(u=1)=0 \) the implied Csiszar f-Divergence remains non-negative even when \( p, q \) are unnormalized measures.
- `name`: name prefixed to Ops created by this function.

Details

When `self_normalized = TRUE`, the KL-reverse Csiszar-function is \( f(u) = u \log(u) - (u - 1) \). When `self_normalized = FALSE` the \( (u - 1) \) term is omitted. Observe that as an f-Divergence, this Csiszar-function implies: \( D_f[p,q] = KL[p,q] \)

The KL is "forward" because in maximum likelihood we think of minimizing \( q \) as in \( KL[p,q] \).

Warning: when `self_normalized = True` this function makes non-log-space calculations and may therefore be numerically unstable for \( \loglogu > 0 \).

Value

`kl_forward_of_u`: float-like Tensor of the Csiszar-function evaluated at \( u = \exp(logu) \).

See Also

Other vi-functions: `vi_amari_alpha()`, `vi_arithmetic_geometric()`, `vi_chi_square()`, `vi_csiszar_vimco()`, `vi_dual_csiszar_function()`, `vi_fit_surrogate_posterior()`, `vi_jeffreys()`, `vi_kl_forward()`, `vi_kl_reverse()`, `vi_log1p_abs()`, `vi_modified_gan()`, `vi_monte_carlo_variational_loss()`, `vi_pearson()`, `vi_squared_hellinger()`, `vi_symmetrized_csiszar_function()`
vi_kl_reverse

The reverse Kullback-Leibler Csiszar-function in log-space

Description

A Csiszar-function is a member of \( F = \{ f:R_+ \to R : f \text{ convex} \} \).

Usage

vi_kl_reverse(logu, self_normalized = FALSE, name = NULL)

Arguments

- logu: float-like Tensor representing \( \log(u) \) from above.
- self_normalized: logical indicating whether \( f(u=1)=0 \). When \( f(u=1)=0 \) the implied Csiszar f-Divergence remains non-negative even when \( p, q \) are unnormalized measures.
- name: name prefixed to Ops created by this function.

Details

When \( \text{self_normalized} = \text{TRUE} \), the KL-reverse Csiszar-function is \( f(u) = -\log(u) + (u - 1) \). When \( \text{self_normalized} = \text{FALSE} \) the \( (u - 1) \) term is omitted. Observe that as an f-Divergence, this Csiszar-function implies: \( D_f[p,q] = \text{KL}[q,p] \)

The KL is "reverse" because in maximum likelihood we think of minimizing \( q \) as in \( \text{KL}[p,q] \).

Warning: when \( \text{self_normalized} = \text{True} \) this function makes non-log-space calculations and may therefore be numerically unstable for \( \log(u) \approx 0 \).

Value

kl_reverse_of_u float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\logu) \).

See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jeffreys(), vi_jensen_shannon(), vi_kl_forward(), vi_log1p_abs(), vi_modified_gan(), vi_monte_carlo_variational_loss(), vi_pearson(), vi_squared_hellinger(), vi_symmetrized_csiszar_function()
The log1p-abs Csiszar-function in log-space

Description

A Csiszar-function is a member of $F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex} \}$.

Usage

vi_log1p_abs(logu, name = NULL)

Arguments

- logu: float-like Tensor representing $\log(u)$ from above.
- name: name prefixed to Ops created by this function.

Details

The Log1p-Abs Csiszar-function is:

$$f(u) = u^{\operatorname{sign}(u-1)} - 1$$

This function is so-named because it was invented from the following recipe. Choose a convex function $g$ such that $g(0) = 0$ and solve for $f$:

$$\log(1 + f(u)) = g(\log(u)).$$

$$\iff$$

$$f(u) = \exp(g(\log(u))) - 1$$

That is, the graph is identically $g$ when $y$-axis is log1p-domain and $x$-axis is log-domain.

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for $\lvert \logu \rvert \gg 0$.

Value

log1p_abs_of_u: float-like Tensor of the Csiszar-function evaluated at $u = \exp(\logu)$.

See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jeffreys(), vi_jensen_shannon(), vi_kl_forward(), vi_kl_reverse(), vi_modified_gan(), vi_monte_carlo_variational_loss(), vi_pearson(), vi_squared_hellinger(), vi_symmetrized_csiszar_function()
vi_modified_gan

**The Modified-GAN Csiszar-function in log-space**

**Description**

A Csiszar-function is a member of \( F = \{ f:R_+ \text{ to } R : f \text{ convex} \} \).

**Usage**

\[
\text{vi_modified_gan}(\text{logu}, \text{self\_normalized = FALSE, name = NULL})
\]

**Arguments**

- **logu**: float-like Tensor representing \( \log(u) \) from above.
- **self\_normalized**: logical indicating whether \( f(u=1)=0 \). When \( f(u=1)=0 \) the implied Csiszar f-Divergence remains non-negative even when \( p, q \) are unnormalized measures.
- **name**: name prefixed to Ops created by this function.

**Details**

When \( \text{self\_normalized = True} \) the modified-GAN (Generative/Adversarial Network) Csiszar-function is:

\[
f(u) = \log(1 + u) - \log(u) + 0.5 (u - 1)
\]

When \( \text{self\_normalized = False} \) the \( 0.5 (u -1) \) is omitted.

The unmodified GAN Csiszar-function is identical to Jensen-Shannon (with \( \text{self\_normalized = False} \)).

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( |\log u| >> 0 \).

**Value**

\( \text{jensen\_shannon\_of\_u} \), float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\text{logu}) \).

**See Also**

Other vi-functions: \text{vi\_amari\_alpha()}, \text{vi\_arithmetic\_geometric()}, \text{vi\_chi\_square()}, \text{vi\_csiszar\_vimco()}, \text{vi\_dual\_csiszar\_function()}, \text{vi\_fit\_surrogate\_posterior()}, \text{vi\_jeffreys()}, \text{vi\_jensen\_shannon()}, \text{vi\_kl\_forward()}, \text{vi\_kl\_reverse()}, \text{vi\_log1p\_abs()}, \text{vi\_monte\_carlo\_variational\_loss()}, \text{vi\_pearson()}, \text{vi\_squared\_hellinger()}, \text{vi\_symmetrized\_csiszar\_function()}
Monte-Carlo approximation of an f-Divergence variational loss

**Description**

Variational losses measure the divergence between an unnormalized target distribution $p$ (provided via `target_log_prob_fn`) and a surrogate distribution $q$ (provided as `surrogate_posterior`). When the target distribution is an unnormalized posterior from conditioning a model on data, minimizing the loss with respect to the parameters of `surrogate_posterior` performs approximate posterior inference.

**Usage**

```r
vi_monte_carlo_variational_loss(
  target_log_prob_fn,
  surrogate_posterior,
  sample_size = 1L,
  importance_sample_size = 1L,
  discrepancy_fn = vi_kl_reverse,
  use_reparametrization = NULL,
  seed = NULL,
  name = NULL
)
```

**Arguments**

- `target_log_prob_fn` function that takes a set of Tensor arguments and returns a Tensor log-density. Given `q_sample <- surrogate_posterior$sample(sample_size)`, this will be (in Python) called as `target_log_prob_fn(q_sample)` if `q_sample` is a list or a tuple, `target_log_prob_fn(**q_sample)` if `q_sample` is a dictionary, or `target_log_prob_fn(q_sample)` if `q_sample` is a Tensor. It should support batched evaluation, i.e., should return a result of shape `[sample_size]`.

- `surrogate_posterior` A `tfp$distributions$Distribution` instance defining a variational posterior (could be a `tfp$distributions$JointDistribution`). Crucially, the distribution’s `log_prob` and (if reparameterized) `sample` methods must directly invoke all ops that generate gradients to the underlying variables. One way to ensure this is to use `tfp$util$DeferredTensor` to represent any parameters defined as transformations of unconstrained variables, so that the transformations execute at runtime instead of at distribution creation.

- `sample_size` integer number of Monte Carlo samples to use in estimating the variational divergence. Larger values may stabilize the optimization, but at higher cost per step in time and memory. Default value: 1.
importance_sample_size
integer number of terms used to define an importance-weighted divergence. If
importance_sample_size > 1, then the surrogate_posterior is optimized to func-
tion as an importance-sampling proposal distribution. In this case it often makes
sense to use importance sampling to approximate posterior expectations (see
tfp.vi.fit_surrogate_posterior for an example). Default value: 1.

discrepancy_fn
function representing a Csiszar function in log-space. That is, discrepancy_fn(log(u))
= f(u), where f is convex in u. Default value: vi_kl_reverse.

use_reparameterization
logical. When NULL (the default), automatically set to: surrogate_posterior.reparameterization_'
== tfp$distributions$FULLY_REPARAMETERIZED. When TRUE uses the stan-
dard Monte-Carlo average. When FALSE uses the score-gradient trick. (See
above for details.) When FALSE, consider using csiszar_vimco.

seed
integer seed for surrogate_posterior$sample.

name
name prefixed to Ops created by this function.

Details
This function defines divergences of the form E_q[discrepancy_fn(log p(z) - log q(z))], sometimes
known as f-divergences.

In the special case discrepancy_fn(logu) == -logu (the default vi_kl_reverse), this is the reverse
Kullback-Liebler divergence KL[q||p], whose negation applied to an unnormalized p is the
widely-used evidence lower bound (ELBO). Other cases of interest available under tfp$vi include
the forward KL[p||q] (given by vi_kl_forward(logu) == exp(logu) * logu), total variation dis-
tance, Amari alpha-divergences, and more.

Csiszar f-divergences
A Csiszar function f is a convex function from \( \mathbb{R}^+ \) (the positive reals) to \( \mathbb{R} \). The Csiszar f-Divergence
is given by:

\[
\text{D}_f[p(X), q(X)] := E_{q(X)}[ f( p(X) / q(X) ) ] = \frac{1}{m} \sum_{j=1}^{m} f( p(x_j) / q(x_j) )
\]

where \( x_j \sim \text{iid} q(X) \)

For example, \( f = \lambda u: -\log(u) \) recovers KL[q||p], while \( f = \lambda u: u \log(u) \) recovers the
forward KL[p||q]. These and other functions are available in tfp$vi.

Tricks: Reparameterization and Score-Gradient
When q is "reparameterized", i.e., a diffeomorphic transformation of a parameterless distribution
(e.g., Normal(Y; m, s) \( \Leftrightarrow \) Y = sX + m, X ~ Normal(0,1)), we can swap gradient and ex-
petation, i.e., grad[Avg{ s_i : i=1...n }] = Avg{ grad[s_i] : i=1...n } where S_n=Avg{s_i} and
s_i = f(x_i), x_i ~iid q(X).

However, if q is not reparameterized, TensorFlow’s gradient will be incorrect since the chain-rule
stops at samples of unreparameterized distributions. In this circumstance using the Score-Gradient
trick results in an unbiased gradient, i.e.,

\[
\text{grad}[ E_q[f(X)] ] = \text{grad}[ \int dx \ q(x) \ f(x) ]
\]
\[
\begin{align*}
= \int dx \ \text{grad}\[ q(x) f(x) \] \\
= \int dx \ [ q'(x) f(x) + q(x) f'(x) ] \\
= \int dx \ q(x) \ [ q'(x) / q(x) f(x) + f'(x) ] \\
= \int dx \ q(x) \ \text{grad}\[ f(x) q(x) / \text{stop_grad}[q(x)] \] \\
= E_q[ \text{grad}\[ f(x) q(x) / \text{stop_grad}[q(x)] \] ] 
\end{align*}
\]

Unless \(q\).reparameterization_type != tfd.FULLY_REPARAMETERIZED it is usually preferable to set use_reparametrization = True.

Example Application: The Csiszar f-Divergence is a useful framework for variational inference. I.e., observe that,

\[
f(p(x)) = f( E_{q(Z | x)}[ p(x, Z) / q(Z | x) ] ) \\
\leq E_{q(Z | x)}[ f( p(x, Z) / q(Z | x) ) ] \\
:= D_f[p(x, Z), q(Z | x)]
\]

The inequality follows from the fact that the "perspective" of \(f\), i.e., \((s, t) \mapsto t f(s / t))\), is convex in \((s, t)\) when \(s / t\) in domain(f) and \(t\) is a real. Since the above framework includes the popular Evidence Lower BOund (ELBO) as a special case, i.e., \(f(u) = -\log(u)\), we call this framework "Evidence Divergence Bound Optimization" (EDBO).

Value

\[
\text{monte_carlo_variational_loss} \ \text{float-like Tensor} \ \text{Monte Carlo approximation of the Csiszar f-Divergence.}
\]

References


See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jeffreys(), vi_jensen_shannon(), vi_kl_forward(), vi_kl_reverse(), vi_log1p_abs(), vi_modified_gan(), vi_pearson(), vi_squared_hellinger(), vi_symmetrized_csiszar_function()

---

vi_pearson

The Pearson Csiszar-function in log-space

Description

A Csiszar-function is a member of \(F = \{ f:R_{+} \to R : f \text{ convex } \} \).

Usage

\[
\text{vi_pearson}(\logu, \ \text{name} = \text{\texttt{NULL}})
\]
Arguments

logu float-like Tensor representing log(u) from above.
name name prefixed to Ops created by this function.

Details

The Pearson Csiszar-function is:

\[ f(u) = (u - 1)^2 \]

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( \log u \gg 0 \).

Value

pearson_of_u: float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\log u) \).

See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jeffreys(), vi_jensen_shannon(), vi_kl_forward(), vi_kl_reverse(), vi_loglp_abs(), vi_modified_gan(), vi_monte_carlo_variational_loss(), vi_squared_hellinger(), vi_symmetrized_csiszar_function()

vi_squared_hellinger The Squared-Hellinger Csiszar-function in log-space

Description

A Csiszar-function is a member of \( F = \{ f:R_+ \to R : f \text{ convex} \} \).

Usage

vi_squared_hellinger(logu, name = NULL)

Arguments

logu float-like Tensor representing log(u) from above.
name name prefixed to Ops created by this function.

Details

The Squared-Hellinger Csiszar-function is:

\[ f(u) = (\sqrt{u} - 1)^2 \]

This Csiszar-function induces a symmetric f-Divergence, i.e., \( D_f[p,q] = D_f[q,p] \).

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( \log u \gg 0 \).
vi_symmetrized_csiszar_function

Value

Squared-Hellinger_of_u: float-like Tensor of the Csiszar-function evaluated at \( u = \exp(\log u) \).

See Also

Other vi-functions: vi_amari_alpha(), vi_arithmetic_geometric(), vi_chi_square(), vi_csiszar_vimco(), vi_dual_csiszar_function(), vi_fit_surrogate_posterior(), vi_jeffreys(), vi_jensen_shannon(), vi_kl_forward(), vi_kl_reverse(), vi_log1p_abs(), vi_modified_gan(), vi_monte_carlo_variational_loss(), vi_pearson(), vi_symmetrized_csiszar_function()

vi_symmetrized_csiszar_function

Symmetrizes a Csiszar-function in log-space

Description

A Csiszar-function is a member of \( F = \{ f:R_+ \to R : f \text{ convex} \} \).

Usage

vi_symmetrized_csiszar_function(logu, csiszar_function, name = NULL)

Arguments

- logu: float-like Tensor representing \( \log(u) \) from above.
- csiszar_function: function representing a Csiszar-function over log-domain.
- name: name prefixed to Ops created by this function.

Details

The symmetrized Csiszar-function is defined as:

\[ f_g(u) = 0.5 \cdot g(u) + 0.5 \cdot u \cdot g\left(\frac{1}{u}\right) \]

where \( g \) is some other Csiszar-function. We say the function is "symmetrized" because:

\[ D_{\log}\{f_g\}(p, q) = D_{\log}\{f_g\}(q, p) \]

for all \( p \gg q \) (i.e., support\((p) = \text{support}\((q)\)).

There exists alternatives for symmetrizing a Csiszar-function. For example,

\[ f_g(u) = \max\{f(u), f^*(u)\}, \]

where \( f^* \) is the dual Csiszar-function, also implies a symmetric f-Divergence.

Example: When either of the following functions are symmetrized, we obtain the Jensen-Shannon Csiszar-function, i.e.,
The Total Variation Csiszar-function in log-space

A Csiszar-function is a member of \( F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex} \} \).

Usage

\[
\text{vi_total_variation}(\log u, \text{name} = \text{NULL})
\]

Arguments

- \( \log u \) : float-like Tensor representing \( \log(u) \) from above.
- \( \text{name} \) : name prefixed to Ops created by this function.

Details

The Total-Variation Csiszar-function is:

\[
f(u) = 0.5 \, |u - 1|
\]

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( |\log u| \gg 0 \).
**Description**

The Triangular Csiszar-function is:

\[ f(u) = \frac{(u - 1)^2}{1 + u} \]

Warning: this function makes non-log-space calculations and may therefore be numerically unstable for \( |\log u| >> 0 \).

**Value**

\[ \text{total\_variation\_of\_u}: \text{float-like Tensor of the Csiszar-function evaluated at } u = \exp(\log u). \]

**See Also**

Other vi-functions#': `vi_t_power()`, `vi_triangular()`
The T-Power Csiszar-function in log-space

Description

A Csiszar-function is a member of $F = \{ f: \mathbb{R}_+ \to \mathbb{R} : f \text{ convex} \}$.

Usage

```r
vi_t_power(logu, t, self_normalized = FALSE, name = NULL)
```

Arguments

- `logu` float-like Tensor representing log(u) from above.
- `t` Tensor of same dtype as `logu` and broadcastable shape.
- `self_normalized` logical indicating whether $f'(u=1)=0$. When $f'(u=1)=0$ the implied Csiszar f-Divergence remains non-negative even when p, q are unnormalized measures.
- `name` name prefixed to Ops created by this function.

Details

When `self_normalized = True` the T-Power Csiszar-function is:

$$f(u) = s \left[ u^t - 1 - t(u - 1) \right]$$

$s = \begin{cases} -1 & 0 < t < 1 \\ +1 & \text{otherwise} \end{cases}$

When `self_normalized = False` the $-t(u -1)$ term is omitted.

This is similar to the amari_alpha Csiszar-function, with the associated divergence being the same up to factors depending only on $t$.

Warning: when `self_normalized = True` this function makes non-log-space calculations and may therefore be numerically unstable for $\log u \gg 0$.

Value

- `t_power_of_u`: float-like Tensor of the Csiszar-function evaluated at $u = \exp(\log u)$.

See Also

Other vi-functions: `vi_total_variation()`, `vi_triangular()`
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