Package ‘tripack’

May 30, 2020

Version 1.3-9.1
Title Triangulation of Irregularly Spaced Data
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Description A constrained two-dimensional Delaunay triangulation package
providing both triangulation and generation of voronoi mosaics of
irregular spaced data.
License ACM | file LICENSE
Date 2020-03-06
NeedsCompilation yes
License_restricts_use yes
Repository CRAN
Date/Publication 2020-05-30 09:50:58 UTC

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Add a constraint to an triangulaion object

Description

This subroutine provides for creation of a constrained Delaunay triangulation which, in some sense, covers an arbitrary connected region R rather than the convex hull of the nodes. This is achieved simply by forcing the presence of certain adjacencies (triangulation arcs) corresponding to constraint curves. The union of triangles coincides with the convex hull of the nodes, but triangles in R can be distinguished from those outside of R. The only modification required to generalize the definition of the Delaunay triangulation is replacement of property 5 (refer to tri.mesh by the following:

5') If a node is contained in the interior of the circumcircle of a triangle, then every interior point of the triangle is separated from the node by a constraint arc.

In order to be explicit, we make the following definitions. A constraint region is the open interior of a simple closed positively oriented polygonal curve defined by an ordered sequence of three or more distinct nodes (constraint nodes) P(1),P(2),...,P(K), such that P(I) is adjacent to P(I+1) for I = 1,...,K with P(K+1) = P(1). Thus, the constraint region is on the left (and may have nonfinite area) as the sequence of constraint nodes is traversed in the specified order. The constraint regions must not contain nodes and must not overlap. The region R is the convex hull of the nodes with constraint regions excluded.
Note that the terms boundary node and boundary arc are reserved for nodes and arcs on the boundary of the convex hull of the nodes.

The algorithm is as follows: given a triangulation which includes one or more sets of constraint nodes, the corresponding adjacencies (constraint arcs) are forced to be present (Fortran subroutine EDGE). Any additional new arcs required are chosen to be locally optimal (satisfy the modified circumcircle property).

**Usage**

```r
add.constraint(tri.obj, cstx, csty, reverse = FALSE)
```

**Arguments**

- `tri.obj`: object of class "tri"
- `cstx`: vector containing x coordinates of the constraint curve.
- `csty`: vector containing y coordinates of the constraint curve.
- `reverse`: if TRUE the orientation of the constraint curve is reversed.

**Value**

An new object of class "tri".

**References**


**See Also**

- `tri`
- `print.tri`
- `plot.tri`
- `summary.tri`
- `triangles`
- `convex.hull`

**Examples**

```r
# we will use the simple test data from TRIPACK:
data(tritest)
tritest.tr <- tri.mesh(tritest)
opar <- par(mfrow = c(2, 2))
plot(tritest.tr)

# include all points in a big triangle:
tritest.tr <- add.constraint(tritest.tr, c(-0.1, 2, -0.1),
                             c(-3, 0.5, 3), reverse = TRUE)

# insert a small cube:
tritest.tr <- add.constraint(tritest.tr, c(0.4, 0.4, 0.6, 0.6),
                             c(0.6, 0.4, 0.4, 0.6),
                             reverse = FALSE)

par(opar)
```
cells  

extract info about voronoi cells

Description

This function returns some info about the cells of a voronoi mosaic, including the coordinates of the vertices and the cell area.

Usage

cells(voronoi.obj)

Arguments

voronoi.obj  object of class voronoi

Details

The function calculates the neighbourhood relations between the underlying triangulation and translates it into the neighbourhood relations between the voronoi cells.

Value

returns a list of lists, one entry for each voronoi cell which contains

<table>
<thead>
<tr>
<th>cell</th>
<th>cell index</th>
</tr>
</thead>
<tbody>
<tr>
<td>center</td>
<td>cell 'center'</td>
</tr>
<tr>
<td>neighbours</td>
<td>neighbour cell indices</td>
</tr>
<tr>
<td>nodes</td>
<td>2 times nnb matrix with vertice coordinates</td>
</tr>
<tr>
<td>area</td>
<td>cell area</td>
</tr>
</tbody>
</table>

Note

outer cells have area=NA, currently also nodes=NA which is not really useful – to be done later

Author(s)

A. Gebhardt

See Also

voronoi.mosaic, voronoi.area
circles

Examples

data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x, tritest$y)
tritest.cells <- cells(tritest.vm)
# highlight cell 12:
plot(tritest.vm)
polygon(t(tritest.cells[[12]]$nodes), col = "green")
# put cell area into cell center:
text(tritest.cells[[12]]$center[1],
     tritest.cells[[12]]$center[2],
     tritest.cells[[12]]$area)

Description

This function plots circles at given locations with given radii.

Usage

circles(x, y, r, ...)

Arguments

x vector of x coordinates
y vector of y coordinates
r vector of radii
... additional graphic parameters will be passed through

Note

This function needs a previous plot where it adds the circles.

Author(s)

A. Gebhardt

See Also

lines, points

Examples

x <- rnorm(10)
y <- rnorm(10)
r <- runif(10, 0, 0.5)
plot(x, y, xlim = c(-3, 3), ylim = c(-3, 3), pch = "+")
circles(x, y, r)
Description
Sample data for the link{circumcircle} function.
circtest are points sampled from a circle with some jitter added, i.e. they represent the most complicated case for the link{circumcircle} function.

circtest  circtest / sample data

Description
This function returns the circumcircle of a triangle.

Usage
cicum(x, y)

Arguments
x Vector of three elements, giving the x coordinates of the triangle nodes.
y Vector of three elements, giving the y coordinates of the triangle nodes.

Details
This is an interface to the Fortran function CIRCUM found in TRIPACK.

Value
x 'x' coordinate of center
y 'y' coordinate of center
radius circumcircle radius
signed.area signed area of triangle (positive iff nodes are numbered counter clock wise)
aspect.ratio ratio "radius of inscribed circle"/"radius of circumcircle", varies between 0 and 0.5
0 means collinear points, 0.5 equilateral triangle.

Note
This function is mainly intended to be used by circumcircle.
**circumcircle**

**Author(s)**

Fortran code: R. J. Renka, R code: A. Gebhardt

**References**


**See Also**

circumcircle

**Examples**

```r
circum(c(0,1,0),c(0,0,1))
```

**Description**

This function returns the (smallest) circumcircle of a set of n points

**Usage**

```r
circumcircle(x, y = NULL, num.touch=2, plot = FALSE, debug = FALSE)
```

**Arguments**

- `x`: vector containing x coordinates of the data. If `y` is missing `x` should contain two elements $x$ and $y$.
- `y`: vector containing y coordinates of the data.
- `num.touch`: How often should the resulting circle touch the convex hull of the given points? default: 2
  possible values: 2 or 3
  Note: The circumcircle of a triangle is usually defined to touch at 3 points, this function searches by default the minimum circle, which may be only touching at 2 points. Set parameter `num.touch` accordingly if you dont want the default behaviour!
- `plot`: Logical, produce a simple plot of the result.
  default: FALSE
- `debug`: Logical, more plots, only needed for debugging.
  default: FALSE
Details

This is a (naive implemented) algorithm which determines the smallest circumcircle of n points:
First step: Take the convex hull.
Second step: Determine two points on the convex hull with maximum distance for the diameter of
the set.
Third step: Check if the circumcircle of these two points already contains all other points (of the
convex hull and hence all other points).
If not or if 3 or more touching points are desired (num.touch=3), search a point with minimum
enclosing circumcircle among the remaining points of the convex hull.
If such a point cannot be found (e.g. for data(circtest2)), search the remaining triangle combi-
nations of points from the convex hull until an enclosing circle with minimum radius is found.
The last search uses an upper and lower bound for the desired minimum radius:
Any enclosing rectangle and its circumcircle gives an upper bound (the axis-parallel rectangle is
used).
Half the diameter of the set from step 1 is a lower bound.

Value

x 'x' coordinate of circumcircle center
y 'y' coordinate of circumcircle center
radius radius of circumcircle

Author(s)

Albrecht Gebhardt

See Also

convex.hull

Examples

data(circtest)
# smallest circle:
circumcircle(circtest,num.touch=2,plot=TRUE)

# smallest circle with maximum touching points (3):
circumcircle(circtest,num.touch=3,plot=TRUE)

# some stress test for this function,
data(circtest2)
# circtest2 was generated by:
# 100 random points almost one a circle:
# alpha <- runif(100,0,2*pi)
# x <- cos(alpha)
# y <- sin(alpha)
# circtest2<-list(x=cos(alpha)+runif(100,0,0.1),
convex.hull

# y=sin(alpha)+runif(100,0,0.1))
#
circumcircle(circtest2,plot=TRUE)

---

convex.hull  
*Return the convex hull of a triangulation object*

---

**Description**

Given a triangulation tri.obj of *n* points in the plane, this subroutine returns two vectors containing the coordinates of the nodes on the boundary of the convex hull.

**Usage**

```r
convex.hull(tri.obj, plot.it=FALSE, add=FALSE,...)
```

**Arguments**

- `tri.obj`: object of class ”tri”
- `plot.it`: logical, if TRUE the convex hull of *tri.obj* will be plotted.
- `add`: logical. if TRUE (and `plot.it`=TRUE), add to a current plot.
- `...`: additional plot arguments

**Value**

- `x`: x coordinates of boundary nodes.
- `y`: y coordinates of boundary nodes.

**Author(s)**

A. Gebhardt

**References**


**See Also**

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `add.constraint`. 

---

```r
# y=sin(alpha)+runif(100,0,0.1))
#
circumcircle(circtest2,plot=TRUE)
```
**Examples**

```r
# rather simple example from TRIPACK:
data(tritest)
tr<-tri.mesh(tritest$x, tritest$y)
convex.hull(tr, plot.it=TRUE)
# random points:
rand.tr<-tri.mesh(runif(10), runif(10))
plot(rand.tr)
rand.ch<-convex.hull(rand.tr, plot.it=TRUE, add=TRUE, col="red")
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 &
quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
plot(quakes.tri)
convex.hull(quakes.tri, plot.it=TRUE, add=TRUE, col="red")
```

---

**identify.tri**

*Identify points in a triangulation plot*

**Description**

Identify points in a plot of "x" with its coordinates. The plot of "x" must be generated with `plot.tri`.

**Usage**

```r
## S3 method for class 'tri'
identify(x,...)
```

**Arguments**

- `x` object of class "tri"
- `...` additional parameters for `identify`

**Value**

an integer vector containing the indexes of the identified points.

**Author(s)**

A. Gebhardt

**See Also**

`tri.print.tri, plot.tri, summary.tri`
in.convex.hull

Examples

data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
plot(tritest.tr)
identify.tri(tritest.tr)

in.convex.hull

Determines if points are in the convex hull of a triangulation object

Description

Given a triangulation tri.obj of \( n \) points in the plane, this subroutine returns a logical vector indicating if the points \((x_i, y_i)\) are contained within the convex hull of tri.obj.

Usage

in.convex.hull(tri.obj, x, y)

Arguments

- **tri.obj**: object of class "tri"
- **x**: vector of x-coordinates of points to locate
- **y**: vector of y-coordinates of points to locate

Value

Logical vector.

Author(s)

A. Gebhardt

References


See Also

tri, print.tri, plot.tri, summary.tri, triangles, add.constraint, convex.hull.
Examples

# example from TRIPACK:
data(tritest)
tr<-tri.mesh(tritest$x, tritest$y)
in.convex.hull(tr, 0.5, 0.5)
in.convex.hull(tr, c(0.5, -1, 1), c(0.5, 1, 1))
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 &
                quakes[,2]<=182.29 & quakes[,2]>=165.77),]
q.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
in.convex.hull(q.tri, quakes$lon[990:1000], quakes$lat[990:1000])

left

Determines whether given points are left of a directed edge.

Description

This function returns a logical vector indicating which elements of the given points P0 are left of the directed edge P1->P2.

Usage

left(x0, y0, x1, y1, x2, y2)

Arguments

x0 Numeric vector, 'x' coordinates of points P0 to check
y0 Numeric vector, 'y' coordinates of points P0 to check, same length as 'x'.
x1 'x' coordinate of point P1
y1 'y' coordinate of point P1
x2 'x' coordinate of point P2
y2 'y' coordinate of point P2

Value

Logical vector.

Note

This is an interface to the Fortran function VLEFT, which is modeled after TRIPACK's LEFT function but accepts more than one point P0.

Author(s)

A. Gebhardt
neighbours

See Also

in.convex.hull

Examples

left(c(0,0,1,1),c(0,1,0,1),0,0,1,1)

neighbours List of neighbours from a triangulation object

Description

Extract a list of neighbours from a triangulation object

Usage

neighbours(tri.obj)

Arguments

tri.obj object of class "tri"

Value

nested list of neighbours per point

Author(s)

A. Gebhardt

References


See Also

tri,print.tri,plot.tri,summary.tri,triangles

Examples

data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
tritest.nb<-neighbours(tritest.tr)
on.convex.hull

Determines if points are on the convex hull of a triangulation object

Description

Given a triangulation tri.obj of \( n \) points in the plane, this subroutine returns a logical vector indicating if the points \((x_i, y_i)\) lay on the convex hull of tri.obj.

Usage

on.convex.hull(tri.obj, x, y)

Arguments

- **tri.obj**: object of class "tri"
- **x**: vector of x-coordinates of points to locate
- **y**: vector of y-coordinates of points to locate

Value

Logical vector.

Author(s)

A. Gebhardt

References


See Also

tri, print.tri, plot.tri, summary.tri, triangles, add.constraint, convex.hull, in.convex.hull.

Examples

# example from TRIPACK:
data(tritest)tr<-tri.mesh(tritest$x, tritest$y)on.convex.hull(tr, 0.5, 0.5)on.convex.hull(tr, c(0.5, -1, 1), c(0.5, 1, 1))# use a part of the quakes data set:
data(quakes)quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 & quakes[,2]<=182.29 & quakes[,2]>=165.77),]q.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")on.convex.hull(q.tri, quakes.part$lon[1:20], quakes.part$lat[1:20])
outer.convhull

Version of outer which operates only in a convex hull

Description

This version of outer evaluates FUN only on that part of the grid $cx cy$ that is enclosed within the convex hull of the points ($px, py$).
This can be useful for spatial estimation if no extrapolation is wanted.

Usage

outer.convhull(cx, cy, px, py, FUN, duplicate="remove", ...)

Arguments

cx x coordinates of grid
cy y coordinates of grid
px vector of x coordinates of points
py vector of y coordinates of points
FUN function to be evaluated over the grid
duplicate indicates what to do with duplicate ($px_i, py_i$) points, default "remove".
... additional arguments for FUN

Value

Matrix with values of FUN (NAs if outside the convex hull).

Author(s)

A. Gebhardt

See Also

in.convex.hull

Examples

x <- runif(20)
y <- runif(20)
z <- runif(20)
z.lm <- lm(z ~ x + y)
f.pred <- function(x, y)
  (predict(z.lm, data.frame(x=as.vector(x), y=as.vector(y))))
xg <- seq(0, 1, 0.05)
yg <- seq(0, 1, 0.05)
image(xg, yg, outer.convhull(xg, yg, x, y, f.pred))
points(x, y)
plot.tri  

**Plot a triangulation object**

Description

plots the triangulation "x"

Usage

```r
## S3 method for class 'tri'
plot(x, add=FALSE, xlim=range(x$x), ylim=range(x$y),
     do.points=TRUE, do.labels = FALSE, isometric=FALSE,...)
```

Arguments

- `x`: object of class "tri"
- `add`: logical, if TRUE, add to a current plot.
- `do.points`: logical, indicates if points should be plotted.
- `do.labels`: logical, indicates if points should be labelled
- `xlim`, `ylim`: x/y ranges for plot
- `isometric`: generate an isometric plot (default FALSE)
- `...`: additional plot parameters

Value

None

Author(s)

A. Gebhardt

References


See Also

`tri`, `print.tri`, `summary.tri`
Examples

# random points
plot(tri.mesh(rpois(100, lambda=20), rpois(100, lambda=20), duplicate="remove"))
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 &
                     quakes[,2]<=182.29 & quakes[,2]>=165.77),]
quakes.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
plot(quakes.tri)
# use the whole quakes data set
# (will not work with standard memory settings, hence commented out)
#plot(tri.mesh(quakes$lon, quakes$lat, duplicate="remove"), do.points=F)

plot.voronoi

Plot a voronoi object

Description

Plots the mosaic "x".
Dashed lines are used for outer tiles of the mosaic.

Usage

## S3 method for class 'voronoi'
plot(x, add=FALSE,
     xlim=c(min(x$tri$x) -
     0.1*diff(range(x$tri$x)),
     max(x$tri$x) +
     0.1*diff(range(x$tri$x))),
     ylim=c(min(x$tri$y) -
     0.1*diff(range(x$tri$y)),
     max(x$tri$y) +
     0.1*diff(range(x$tri$y))),
     all=FALSE,
     do.points=TRUE,
     main="Voronoi mosaic",
     sub=deparse(substitute(x)),
     isometric=FALSE,
     ...)
all  show all (including dummy points in the plot
do.points logical, indicates if points should be plotted.
main  plot title
sub   plot subtitle
isometric generate an isometric plot (default FALSE)
...   additional plot parameters

Value

None

Author(s)

A. Gebhardt

References


See Also

voronoi, print.voronoi, summary.voronoi

Examples

# plot a random mosaic
plot(voronoi.mosaic(runif(100),runif(100),duplicate="remove"))
# use isometric=TRUE and all=TRUE to see the complete mosaic
# including extreme outlier points:
plot(voronoi.mosaic(runif(100),runif(100),duplicate="remove"),
    all=TRUE, isometric=TRUE)
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 &
    quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.vm<-voronoi.mosaic(quakes.part$lon, quakes.part$lat,
    duplicate="remove")
plot(quakes.vm, isometric=TRUE)
# use the whole quakes data set
# (will not work with standard memory settings, hence commented out here)
#plot(voronoi.mosaic(quakes$lon, quakes$lat, duplicate="remove"), isometric=TRUE)
plot.voronoi.polygons  plots an voronoi.polygons object

Description

plots an voronoi.polygons object

Usage

## S3 method for class 'voronoi.polygons'
plot(x, which, color=TRUE, ...)

Arguments

x  object of class voronoi.polygons
which  index vector selecting which polygons to plot
color  logical, determines if plot should be colored, default: TRUE
...  additional plot arguments

Author(s)

A. Gebhardt

See Also

voronoi.polygons

Examples

##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##-- or do help(data=index) for the standard data sets.
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)
tritest.vp <- voronoi.polygons(tritest.vm)
plot(tritest.vp)
plot(tritest.vp,which=c(1,3,5))
print.summary.tri  
Print a summary of a triangulation object

Description
Prints some information about tri.obj

Usage
## S3 method for class 'summary.tri'
print(x, ...)

Arguments
x  object of class "summary.tri", generated by summary.tri.
...  additional parameters for print

Value
None

Author(s)
A. Gebhardt

References

See Also
tri,tri.mesh,print.tri,plot.tri,summary.tri.

print.summary.voronoi  
Print a summary of a voronoi object

Description
Prints some information about x

Usage
## S3 method for class 'summary.voronoi'
print(x, ...)


print.tri

Arguments

x          object of class "summary.voronoi", generated by summary.voronoi.
...         additional parameters for print

Value

None

Author(s)

A. Gebhardt

References


See Also

voronoi, voronoi.mosaic, print.voronoi, plot.voronoi, summary.voronoi.

print.tri  Print a triangulation object

Description

prints a adjacency list of "x"

Usage

## S3 method for class 'tri'
print(x,...)

Arguments

x          object of class "tri"
...         additional parameters for print

Value

None

Author(s)

A. Gebhardt
References


See Also

tri, plot.tri, summary.tri

---

**print.voronoi** *Print a voronoi object*

**Description**

prints a summary of "x"

**Usage**

```r
## S3 method for class 'voronoi'
print(x,...)
```

**Arguments**

- `x` object of class "voronoi"
- `...` additional parameters for print

**Value**

None

**Author(s)**

A. Gebhardt

**References**


**See Also**

voronoi, plot.voronoi, summary.voronoi
summary.tri

Return a summary of a triangulation object

Description

Returns some information (number of nodes, triangles, arcs, boundary nodes and constraints) about object.

Usage

```r
## S3 method for class 'tri'
summary(object,...)
```

Arguments

- `object` object of class "tri"
- `...` additional parameters for `summary`

Value

An object of class "summary.tri", to be printed by `print.summary.tri`.

It contains the number of nodes (n), of arcs (na), of boundary nodes (nb), of triangles (nt) and constraints (nc).

Author(s)

A. Gebhardt

References


See Also

`tri`, `print.tri`, `plot.tri`, `print.summary.tri`. 
summary.voronoi

Return a summary of a voronoi object

Description

Returns some information about object

Usage

```r
# S3 method for class 'voronoi'
summary(object, ...)
```

Arguments

- `object`: object of class "voronoi"
- `...`: additional parameters for summary

Value

Object of class "summary.voronoi".

It contains the number of nodes (nn) and dummy nodes (nd).

Author(s)

A. Gebhardt

References


See Also

`voronoi`, `voronoi.mosaic`, `print.voronoi`, `plot.voronoi`, `print.summary.voronoi`
tri

A triangulation object

Description

R object that represents the triangulation of a set of 2D points, generated by tri.mesh or add.constraint.

Arguments

- **n** Number of nodes
- **x** x coordinates of the triangulation nodes
- **y** y coordinates of the triangulation nodes
- **tlist** Set of nodal indexes which, along with tlptr, tlend, and tlnew, define the triangulation as a set of n adjacency lists – counterclockwise-ordered sequences of neighboring nodes such that the first and last neighbors of a boundary node are boundary nodes (the first neighbor of an interior node is arbitrary). In order to distinguish between interior and boundary nodes, the last neighbor of each boundary node is represented by the negative of its index.
- **tlptr** Set of pointers in one-to-one correspondence with the elements of tlist. tlist[tlptr[i]] indexes the node which follows tlist[i] in cyclical counterclockwise order (the first neighbor follows the last neighbor).
- **tlend** Set of pointers to adjacency lists. tlend[k] points to the last neighbor of node k for k = 1,...,n. Thus, tlist[tlend[k]]<0 if and only if k is a boundary node.
- **tlnew** Pointer to the first empty location in tlist and tlptr (list length plus one).
- **nc** number of constraints
- **lc** starting indices of constraints in x and y
- **call** call, which generated this object

Note

The elements tlist, tlptr, tlend and tlnew are mainly intended for internal use in the appropriate Fortran routines.

Author(s)

A. Gebhardt

References


See Also

tri.mesh, print.tri, plot.tri, summary.tri
tri.dellens  

Compute the Delaunay segment lengths

Description

Return a vector of Delaunay segment lengths for the voronoi object. The Delaunay triangles connected to sites contained in exceptions vector are ignored (unless inverse is TRUE, when only those Delaunay triangles are accepted).

The exceptions vector is provided so that sites at the border of a region can be removed, as these tend to bias the distribution of Delaunay segment lengths. exceptions can be created by voronoi.findrejsetsites.

Usage

tri.dellens(voronoi.obj, exceptions = NULL, inverse = FALSE)

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>voronoi.obj</td>
<td>object of class &quot;voronoi&quot;</td>
</tr>
<tr>
<td>exceptions</td>
<td>a numerical vector</td>
</tr>
<tr>
<td>inverse</td>
<td>Logical</td>
</tr>
</tbody>
</table>

Value

A vector of Delaunay segment lengths.

Author(s)

S. J. Eglen

See Also

voronoi.findrejsetsites, voronoi.mosaic,

Examples

data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x, tritest$y)

tritest.vm.rejects <- voronoi.findrejsetsites(tritest.vm, 0, 1, 0, 1)
trilens.all <- tri.dellens(tritest.vm)
trilens.acc <- tri.dellens(tritest.vm, tritest.vm.rejects)
trilens.rej <- tri.dellens(tritest.vm, tritest.vm.rejects, inverse=TRUE)

par(mfrow=c(3,1))
dotchart(trilens.all, main="all Delaunay segment lengths")
dotchart(trilens.acc, main="excluding border sites")
dotchart(trilens.rej, main="only border sites")
**tri.find**

---

**Locate a point in a triangulation**

**Description**

This subroutine locates a point \( P=(x,y) \) relative to a triangulation created by \texttt{tri.mesh}. If \( P \) is contained in a triangle, the three vertex indexes are returned. Otherwise, the indexes of the rightmost and leftmost visible boundary nodes are returned.

**Usage**

\[
\text{tri.find}(\text{tri.obj}, x, y)
\]

**Arguments**

- \( \text{tri.obj} \): an triangulation object
- \( x \): x-coordinate of the point
- \( y \): y-coordinate of the point

**Value**

A list with elements \( i1,i2,i3 \) containing nodal indexes, in counterclockwise order, of the vertices of a triangle containing \( P=(x,y) \), or, if \( P \) is not contained in the convex hull of the nodes, \( i1 \) indexes the rightmost visible boundary node, \( i2 \) indexes the leftmost visible boundary node, and \( i3 = 0 \). Rightmost and leftmost are defined from the perspective of \( P \), and a pair of points are visible from each other if and only if the line segment joining them intersects no triangulation arc. If \( P \) and all of the nodes lie on a common line, then \( i1=i2=i3 = 0 \) on output.

**Author(s)**

A. Gebhardt

**References**


**See Also**

\texttt{tri.print.tri, plot.tri, summary.tri, triangles, convex.hull}
**Examples**

```r
data(tritest)
tritest.tr<-tri.mesh(tritest$x, tritest$y)
plot(tritest.tr)
pnt<-list(x=0.3, y=0.4)
triangle.with.pnt<-tri.find(tritest.tr, pnt$x, pnt$y)
attach(triangle.with.pnt)
lines(tritest$x[c(i1, i2, i3, i1)], tritest$y[c(i1, i2, i3, i1)], col="red")
points(pnt$x, pnt$y)
```

---

**tri.mesh**

*Create a delaunay triangulation*

**Description**

This subroutine creates a Delaunay triangulation of a set of N arbitrarily distributed points in the plane referred to as nodes. The Delaunay triangulation is defined as a set of triangles with the following five properties:

1) The triangle vertices are nodes.

2) No triangle contains a node other than its vertices.

3) The interiors of the triangles are pairwise disjoint.

4) The union of triangles is the convex hull of the set of nodes (the smallest convex set which contains the nodes).

5) The interior of the circumcircle of each triangle contains no node.

The first four properties define a triangulation, and the last property results in a triangulation which is as close as possible to equiangular in a certain sense and which is uniquely defined unless four or more nodes lie on a common circle. This property makes the triangulation well-suited for solving closest point problems and for triangle-based interpolation.

The triangulation can be generalized to a constrained Delaunay triangulation by a call to `add.constraint`. This allows for user-specified boundaries defining a nonconvex and/or multiply connected region.

The operation count for constructing the triangulation is close to $O(N)$ if the nodes are presorted on X or Y components. Also, since the algorithm proceeds by adding nodes incrementally, the triangulation may be updated with the addition (or deletion) of a node very efficiently. The adjacency information representing the triangulation is stored as a linked list requiring approximately $13N$ storage locations.

**Usage**

```r
tri.mesh(x, y = NULL, duplicate = "error",
         jitter = 10^-12, jitter.iter = 6, jitter.random = FALSE)
```
triangles

Arguments

- **x**: vector containing x coordinates of the data. If y is missing x should contain two elements x and y.
- **y**: vector containing y coordinates of the data.
- **duplicate**: flag indicating how to handle duplicate elements. Possible values are: "error" – default, "strip" – remove all duplicate points, "remove" – leave one point of duplicate points.
- **jitter**: Jitter of amount of \( \text{diff}(\text{range}(\text{XX})) \times \text{jitter} \) (XX=x or y) will be added to coordinates if collinear points are detected. Afterwards interpolation will be tried once again.
- **jitter.iter**: number of iterations to retry with jitter, amount will be increased in each iteration by \( \text{iter}^1.5 \)
- **jitter.random**: logical, see jitter, defaults to FALSE

Value

An object of class "tri"

References


See Also

tri, print.tri, plot.tri, summary.tri, triangles, convex.hull, neighbours, add.constraint.

Examples

data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
tritest.tr

triangles  Extract a list of triangles from a triangulation object
Description

This function extracts a triangulation data structure from an triangulation object created by \texttt{tri.mesh}.

The vertices in the returned matrix (let’s denote it with \texttt{retval}) are ordered counterclockwise with the first vertex taken to be the one with smallest index. Thus, \texttt{retval[i,"node2"]} and \texttt{retval[i,"node3"]} are larger than \texttt{retval[i,"node3"]} and index adjacent neighbors of node \texttt{retval[i,"node1"]}. The columns \texttt{trx} and \texttt{arcx}, \texttt{x=1,2,3} index the triangle and arc, respectively, which are opposite (not shared by) node \texttt{nodex}, with \texttt{trix}=0 if \texttt{arcx} indexes a boundary arc. Vertex indexes range from 1 to \text{N}, triangle indexes from 0 to \text{NT}, and, if included, arc indexes from 1 to \text{NA} = \text{NT+}N-1. The triangles are ordered on first (smallest) vertex indexes, except that the sets of constraint triangles (triangles contained in the closure of a constraint region) follow the non-constraint triangles.

Usage

\texttt{triangles(tri.obj)}

Arguments

\texttt{tri.obj} \hspace{1em} \text{object of class "tri"}

Value

A matrix with columns \texttt{node1},\texttt{node2},\texttt{node3}, representing the vertex nodal indexes, \texttt{tr1},\texttt{tr2},\texttt{tr3}, representing neighboring triangle indexes and \texttt{arc1},\texttt{arc2},\texttt{arc3} representing arc indexes.

Each row represents one triangle.

Author(s)

A. Gebhardt

References


See Also

\texttt{tri}, \texttt{print.tri}, \texttt{plot.tri}, \texttt{summary.tri}, \texttt{triangles}

Examples

\# use a slightly modified version of data(tritest)
data(tritest2)
tritest2.tr<-\texttt{tri.mesh(tritest2$x, tritest2$y)}
\texttt{triangles(tritest2.tr)}
**tripack-internal Internal functions**

**Description**
Internal tripack functions

**Details**
These functions are not intended to be called by the user.

---

**tritest tritest / sample data**

**Description**
A very simply set set of points to test the tripack functions, taken from the FORTRAN original. tritest2 is a slight modification by adding \( \text{runif}(-0.1,0.1) \) random numbers to the coordinates.

**References**

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**voronoi Voronoi object**

**Description**
An voronoi object is created with `voronoi.mosaic`

**Arguments**

- \( x,y \) x and y coordinates of nodes of the voronoi mosaic. Each node is a circumcircle center of some triangle from the Delaunay triangulation.
- \( \text{node} \) logical vector, indicating real nodes of the voronoi mosaic. These nodes are the centers of circumspheres of triangles with positive area of the delaunay triangulation.
  - If \( \text{node}[i]=\text{FALSE} \), \((c[i],x[i])\) belongs to a triangle with area 0.
- \( n1,n2,n3 \) indices of neighbour nodes. Negative indices indicate dummy points as neighbours.
tri  triangulation object, see tri.
area area of triangle i. area[i]=-1 indicates a removed triangle with area 0 at the border of the triangulation.
ratio aspect ratio (inscribed radius/circumradius) of triangle i.
radius circumradius of triangle i.
dummy.x, dummy.y x and y coordinates of dummy points. They are used for plotting of unbounded tiles.

Author(s)
A. Gebhardt

See Also
voronoi.mosaic, plot.voronoi

Describe area
Calculate area of Voronoi polygons

Computes the area of each Voronoi polygon. For some sites at the edge of the region, the Voronoi polygon is not bounded, and so the area of those sites cannot be calculated, and hence will be NA.

Usage
voronoi.area(voronoi.obj)

Arguments
voronoi.obj object of class "voronoi"

Value
A vector of polygon areas.

Author(s)
S. J. Eglen

See Also
voronoi,
Examples

```r
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x, tritest$y)
tritest.vm.areas <- voronoi.area(tritest.vm)
plot(tritest.vm)
text(tritest$x, tritest$y, tritest.vm.areas)
```

---

test

Description

Find the sites in the Voronoi tessellation that lie at the edge of the region. A site is at the edge if any of the vertices of its Voronoi polygon lie outside the rectangle with corners \((x_{\text{min}}, y_{\text{min}})\) and \((x_{\text{max}}, y_{\text{max}})\).

Usage

```r
voronoi.findrejectsites(voronoi.obj, xmin, xmax, ymin, ymax)
```

Arguments

- **voronoi.obj**: object of class "voronoi"
- **xmin**: minimum x-coordinate of sites in the region
- **xmax**: maximum x-coordinate of sites in the region
- **ymin**: minimum y-coordinate of sites in the region
- **ymax**: maximum y-coordinate of sites in the region

Value

A logical vector of the same length as the number of sites. If the site is a reject, the corresponding element of the vector is set to TRUE.

Author(s)

S. J. Eglen

See Also

`tri.dellens`
Description
This function creates a Voronoi mosaic.

It creates first a Delaunay triangulation, determines the circumcircle centers of its triangles, and connects these points according to the neighbourhood relations between the triangles.

Usage
voronoi.mosaic(x,y=NULL,duplicate="error")

Arguments
x vector containing x coordinates of the data. If y is missing x should contain two elements $x$ and $y$.
y vector containing y coordinates of the data.
duplicate flag indicating how to handle duplicate elements. Possible values are: "error" – default, "strip" – remove all duplicate points, "remove" – leave one point of duplicate points.

Value
An object of class voronoi.

Author(s)
A. Gebhardt

See Also
voronoi, voronoi.mosaic, print.voronoi, plot.voronoi

Examples
# example from TRIPACK:
data(tritest)
tritest.vm<-voronoi.mosaic(tritest$x, tritest$y)
tritest.vm
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 & quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.vm<-voronoi.mosaic(quakes.part$lon, quakes.part$lat, duplicate="remove")
quakes.vm
**Description**

This function extracts polygons from a `voronoi.mosaic` object.

**Usage**

```r
voronoi.polygons(voronoi.obj)
```

**Arguments**

- `voronoi.obj` object of class `voronoi.mosaic`

**Value**

Returns an object of class `voronoi.polygons` with unnamed list elements for each polygon. These list elements are matrices with columns `x` and `y`.

**Author(s)**

Denis White

**See Also**

- `plot.voronoi.polygons`
- `voronoi.mosaic`

**Examples**

```r
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,  
##-- or do help(data=index) for the standard data sets.

data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x, tritest$y)
tritest.vp <- voronoi.polygons(tritest.vm)
tritest.vp
```
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