Package ‘vs gof test’

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Type  Package
Title  Goodness-of-Fit Tests Based on Kullback-Leibler Divergence
Version  0.3-2
Date  2018-06-21
Author  Justine Lequesne [aut], Philippe Regnault [aut, cre]
Maintainer  Philippe Regnault <philipperegnault@hotmail.com>
Description  An implementation of Vasicek and Song goodness-of-fit tests. Several functions are provided to estimate differential Shannon entropy, i.e., estimate Shannon entropy of real random variables with density, and test the goodness-of-fit of some family of distributions, including uniform, Gaussian, log-normal, exponential, gamma, Weibull, Pareto, Fisher, Laplace and beta distributions; see Lequesne and Regnault (2018) <arXiv:1806.07244>.

Depends  stats, fitdistrplus
Imports  Rcpp (>= 0.12.1)
Suggests  knitr
VignetteBuilder  knitr
LinkingTo  Rcpp
Encoding  UTF-8
License  GPL (>= 2)
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Goodness-of-Fit Tests Based on Kullback-Leibler Divergence

Description

An implementation of Vasicek and Song goodness-of-fit tests. Several functions are provided to estimate differential Shannon entropy, i.e., estimate Shannon entropy of real random variables with density, and test the goodness-of-fit of some family of distributions, including uniform, Gaussian, log-normal, exponential, gamma, Weibull, Pareto, Fisher, Laplace and beta distributions; see Lequesne and Regnault (2018) <arXiv:1806.07244>.

Details

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Further information is available in the following vignettes:
contaminants

vsgoftest_tutorial  Tutorial (source, pdf)

Author(s)

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References


Examples

```r
set.seed(1)
samp <- rnorm(50, mean = 2, s = 3)

# Estimating entropy
entropy.estimate(x = samp, window = 8)
log(2*pi*exp(1))/2  # true value of entropy of normal distribution

# Testing normality
vs.test(x = samp, densfun = 'dnorm', param = c(2, 3), B = 500)  # Simple null hypothesis
vs.test(x = samp, densfun='dnorm', B = 500)  # Composite null hypothesis
```

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Description

Organic and inorganic contaminant concentration data from Superfund sites; see Singh *et al.* (1997).

Usage

data(contaminants)
Format

Four numeric vectors of respective lengths 17, 17, 23 and 23.

Details

aluminium1 and manganese are groundwater concentration measurements of aluminium and manganese from seventeen wells at the Naval Construction Battalion Center Superfound Site in Rhode Island.

aluminium2 and toluene are concentration measurements of aluminium and toluene compiled from two waste piles at Elmara School Superfound site in Washington County, PA.

Source


dlaplace

The Laplace distribution

Description

Density, cumulative distribution function, quantile function and random generation for the laplace distribution.

Usage

\[
\text{dlaplace}(x, \mu, b, \text{log} = \text{FALSE})
\]
\[
\text{plaplace}(q, \mu, b, \text{lower.tail} = \text{TRUE}, \text{log.p} = \text{FALSE})
\]
\[
\text{qlaplace}(p, \mu, b, \text{lower.tail} = \text{TRUE}, \text{log.p} = \text{FALSE})
\]
\[
\text{rlaplace}(n, \mu, b)
\]

Arguments

- \(x, q\) (numeric, vector) a vector of quantiles.
- \(p\) (numeric, vector) a vector of probabilities.
- \(n\) (numeric, vector) sample size to be generated.
- \(\mu\) (numeric, single value) the location parameter.
- \(b\) (numeric, single value) the scale parameter.
- \(\text{log, log.p}\) (logical, single value) if TRUE, probabilities are given as \(\log(p)\). Default is FALSE.
- \(\text{lower.tail}\) (logical, single value) if TRUE (default), probabilities are \(P(X \leq x)\); otherwise \(P(X > x)\).
Details

The laplace distribution with shape parameter $\mu > 0$ and scale parameter $b > 0$ has density

$$f(x) = \frac{1}{2b} \exp\left(-\frac{|x - \mu|}{b}\right), \quad x \in \mathbb{R}.$$  

Value

dlaplace gives the density, plaplace gives the distribution function, qlaplace gives the quantile function, and rlaplace generates random deviates.

The length of the result is determined by n for rnorm, and is the maximum of the lengths of the numerical arguments for the other functions.

Author(s)

J. Lequesne <justine.lequesne@unicaen.fr>

Examples

```r
set.seed(1)
rlaplace(100, mu=10, b=1)
```

---

The Pareto distribution

Description

Density, cumulative distribution function, quantile function and random generation for the Pareto distribution.

Usage

```r
dpareto(x, mu, c, log = FALSE)
ppareto(q, mu, c, lower.tail = TRUE, log.p = FALSE)
qpareto(p, mu, c, lower.tail = TRUE, log.p = FALSE)
rpareto(n, mu, c)
```

Arguments

- `x, q` (numeric, vector) a vector of quantiles.
- `p` (numeric, vector) a vector of probabilities.
- `n` (numeric, vector) sample size to be generated.
- `mu` (numeric, single value) the shape parameter.
- `c` (numeric, single value) the scale parameter.
- `log, log.p` (logical, single value) if TRUE, probabilities are given as log(p). Default is FALSE.
- `lower.tail` (logical, single value) if TRUE (default), probabilities are $P(X \leq x)$; otherwise $P(X > x)$.
Details

The pareto distribution with shape parameter $\mu > 0$ and scale parameter $c > 0$ has density

$$f(x) = \frac{\mu c^\mu}{x^{1+\mu}},$$

for $x \geq 0$.

Value

dpareto gives the density, ppareto gives the distribution function, qpareto gives the quantile function, and rpareto generates random deviates.

The length of the result is determined by n for rnorm, and is the maximum of the lengths of the numerical arguments for the other functions.

Author(s)

J. Lequesne <justine.lequesne@unicaen.fr>

References


Examples

```r
n <- 100
rpareto(n, mu=2, c=1)
```

### entropy.estimate

**Vasicek estimate of differential Shannon Entropy**

Description

Computes Vasicek estimate of differential Shannon entropy from a numeric sample.

Usage

```r
entropy.estimate(x, window)
```

Arguments

- **x**: (numeric, vector) the numeric sample.
- **window**: (numeric, single value) an integer between 1 and half on the sample size specifying the window size for computing Vasicek estimate. See Details for additional information.
Details

Vasicek estimator of Shannon entropy is defined, for a random sample $X_1, \ldots, X_n$, by

$$\frac{1}{n} \sum_{i=1}^{n} \log \left( \frac{n}{2m} \left[ X_{(i+m)} - X_{(i-m)} \right] \right),$$

where $X_{(i)}$ is the order statistic, $m < (n/2)$ is the window size, and $X_{(i)} = X_{(1)}$ for $i < 1$ and $X_{(i)} = X_{(n)}$ for $i > n$.

Value

A single numeric value representing the Vasicek estimate of entropy of the sample

Author(s)

J. Lequesne <justine.lequesne@unicaen.fr>

References


See Also

*vs.test* which performs Vasicek-Song goodness-of-fit tests to the specified maximum entropy distribution family.

Examples

```r
set.seed(2)
samp <- rnorm(100, mean = 0, sd = 1)
entropy.estimate(x = samp, window = 8)
log(2*pi*exp(1))/2 #true value of entropy of normal distribution
```
Arguments

x (numeric, vector) the numeric sample.

densfun A character string specifying the fitted distribution. Possible values are "dunif", "dnorm", "dlnorm", "dexp", "dgamma", "dweibull", "dpareto", "df", "dlaplace" and "dbeta".

param (numeric, vector) specifies the parameter(s) of the fitted distribution. If NULL (default), a GOF test to the parametric family of distributions specified by densfun is performed.

simulate.p.value (logical, single value) if TRUE, the p-value of the sample is estimated by means of Monte Carlo methods. If NULL (the default), the p-value is simulated if the sample size is smaller than 80; otherwise, an asymptotic p-value is computed.

B (numeric, single value) a numeric value specifying the number of simulations to perform in Monte-Carlo estimation of the p-value.

delta (numeric, single value) a numeric value smaller than $1/3$ specifying the upper bound $n^{1/3} - \delta$ for window size, where $n$ is the sample size. The default depends on densfun; see Vignettes for details.

extend (logical, single value). If FALSE (the default), the bound for the window is $n^{1/3} - \delta$; if TRUE, the bound is $n/2$.

relax (logical, single value) avoids the constraint $V_{mn} \leq -\frac{1}{n} \sum_{i=1}^{n} \log p_0(X_i, \hat{\theta}_n)$ when computing the optimal window; see details. Default is FALSE.

Details

The test statistic is

$$I_{mn} = -V_{mn} - \frac{1}{n} \sum_{i=1}^{n} \log p_0(X_i, \theta),$$

where $V_{mn}$ is the Vasicek estimator of Shannon entropy computed from the numeric sample x with window size m and $p_0(x, \theta)$ is the density function of the specified distribution densfun to be tested, with $\theta$ the parameter of the null for a simple hypothesis or its maximum likelihood estimate for a composite null hypothesis (param=NULL); See Song (2002), Girardin and Lequesne (2017) and Lequesne and Regnault (2018).

An optimal window size $m$ is automatically computed; see Song (2002).

An exact p-value is computed if the sample size is less than 100. Otherwise, asymptotic distribution is used whose approximation may be inaccurate for small samples; see Lequesne and Regnault (2018).

Value

A list with class "htest" containing the following components:

observed The sample under study.

data.name The name (as an R object) of the sample.

null.value A character string specifying the name of the fitted distribution.
method The character string "Vasicek GOF test to" followed by the name of the fitted distribution.
statistic Vasicek test statistic; see Details below.
parameter The optimal window for Vasicek test statistic
estimate Parameter(s) of the fitted distribution. If param is NULL, parameters are estimated. If param is suitably filled out by the user, it is returned.
p.value The p-value of the test.

Author(s)
J. Lequesne <justine.lequesne@unicaen.fr>

References

See Also
entropy.estimate which computes the Vasicek estimator of Shannon entropy.

Examples
set.seed(1)
samp <- rnorm(500, 2, 3)
vs.test(x = samp, densfun = 'dnorm', param = c(2, 3), B = 500) # Simple null hypothesis
vs.test(x = samp, densfun='dnorm', B = 500) # Composite null hypothesis
## Using asymptotic distribution to compute the p-value
vs.test(x = samp, densfun='dnorm', simulate.p.value = FALSE) # Composite null hypothesis
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