Package ‘wqspt’

March 6, 2023

Title Permutation Test for Weighted Quantile Sum Regression

Version 1.0.1

Author Drew Day [aut, cre],
     James Peng [aut],
     Adam Szpiro [aut]

Maintainer Drew Day <Drew.Day@seattlechildrens.org>

Description Implements a permutation test method for the weighted quantile sum (WQS) regression, building off the ‘gWQS’ package (Renzetti et al. (2021) <https://CRAN.R-project.org/package=gWQS>). Weighted quantile sum regression is a statistical technique to evaluate the effect of complex exposure mixtures on an outcome (Carrico et al. (2015) <doi:10.1007/s13253-014-0180-3>). The model features a statistical power and Type I error (i.e., false positive) rate trade-off, as there is a machine learning step to determine the weights that optimize the linear model fit. This package provides an alternative method based on a permutation test that should reliably allow for both high power and low false positive rate when utilizing WQS regression (Day et al. (2022) <doi:10.1289/EHP10570>).

License GPL-3

Encoding UTF-8

RoxygenNote 7.2.1

Imports rlang, gWQS, pbapply, ggplot2, mvtnorm, viridis, extraDistr,
cowplot, methods

Suggests rmarkdown, knitr, testthat (>= 3.0.0)

VignetteBuilder knitr

Config/testthat/edition  3

NeedsCompilation no

Depends R (>= 3.5.0)

Repository CRAN

Date/Publication 2023-03-06 14:00:02 UTC
R topics documented:

- `wqspt_plot` .................................................. 2
- `wqs_full_perm` ............................................. 3
- `wqs_pt` .......................................................... 5
- `wqs_sim` ....................................................... 8

Index 11

---

**wqspt_plot**  
*Plotting method for wqspt object*

**Description**
Generates plots to help visualize and summarize WQS permutation test results.

**Usage**

```r
wqspt_plot(
  wqsptresults,
  FixedPalette = FALSE,
  InclKey = FALSE,
  AltMixName = NULL,
  AltOutcomeName = NULL,
  ViridisPalette = "D",
  StripTextSize = 14,
  AxisTextSize.Y = 12,
  AxisTextSize.X = 12,
  LegendTextSize = 14,
  PvalLabelSize = 5,
  HeatMapTextSize = 5
)
```

**Arguments**

- `wqsptresults`  
  An object of class `wqs_pt`.
- `FixedPalette`  
  If TRUE, the heatmap color key for the mixture weights has categorical cutoffs with the following categories: <0.1, 0.1 - <0.2, 0.2 - <0.3, and >= 0.3. If false, the heatmap color key is continuous and dependent on the weight values.
- `InclKey`  
  If TRUE, a horizontal heatmap legend is included at the bottom of the full plot.
- `AltMixName`  
  Defaults to NULL. If not NULL, these are alternative names for the mixture components to be displayed on the heatmap y axis.
- `AltOutcomeName`  
  Defaults to NULL. If not NULL, this is an alternative name for the outcome to be displayed on the heatmap x axis.
- `ViridisPalette`  
  Color palette to be used for the viridisLite package-based coloring of the heatmap, with possible values from 'A' to 'E'. Defaults to 'D'.
StripTextSize  Text size for the plot strip labels. Defaults to 14.
AxisTextSize.Y  Text size for the y axis text. Defaults to 12.
AxisTextSize.X  Text size for the x axis text. Defaults to 12.
LegendTextSize  Text text size for the legend text. Defaults to 14.
PValLabelSize  The geom_text size for the permutation test p-value label. Defaults to 5.
HeatMapTextSize  The geom_text size for the mixture weight heatmap labels. Defaults to 5.

**Value**

Returns a list with 4 objects.

- **FullPlot** Two plots stacked vertically: (1) Forest plot of the beta WQS coefficient with the naive confidence intervals as well as the permutation test p-value (2) A heatmap of the WQS weights for each mixture component.
- **CoeffPlot** Forest plot of the beta WQS coefficient with the naive confidence intervals as well as the permutation test p-value.
- **WtPlot** A heatmap of the WQS weights for each mixture component.
- **WtLegend** A legend for the weights in the WtPlot heatmap.

---

**wqs_full_perm**

Full wrapper WQS permutation test

**Description**

`wqs_full_perm` is a full wrapper function that is a full implementation of the Weighted Quantile Sum (WQS) regression method followed by the permutation test to determine the significance of the WQS coefficient.

**Usage**

```r
wqs_full_perm(
  formula,
  data,
  mix_name,
  q = 10,
  b_main = 1000,
  b_perm = 200,
  b1_pos = TRUE,
  b1_constr = FALSE,
  rs = FALSE,
  niter = 200,
  seed = NULL,
  family = "gaussian",
  plan_strategy = "multicore",
)```
```
stop_if_nonsig = FALSE,
stop_thresh = 0.05,
...
```

**Arguments**

- **formula**: An object of class formula. The wqs term must be included in the formula (e.g., `y ~ wqs + ...`).
- **data**: The `data.frame` to be used in the WQS regression run.
- **mix_name**: A vector with the mixture column names.
- **q**: An integer to indicate the number of quantiles to split the mixture variables.
- **b_main**: The number of bootstraps for the main WQS regression run.
- **b_perm**: The number of bootstraps for the iterated permutation test WQS regression runs and the reference WQS regression run (only for linear WQS regression and only when `b_mean != b_perm`).
- **b1_pos**: A logical value that indicates whether beta values should be positive or negative.
- **b1_constr**: Logical value that determines whether to apply positive or negative constraints in the optimization function for the weight optimization.
- **rs**: A logical value indicating whether random subset implementation should be performed.
- **niter**: Number of permutation test iterations.
- **seed**: An integer to fix the seed. This will only impact the initial WQS regression run and not the permutation test iterations. The default setting is `NULL`, which means no seed is used for the initial WQS regression. The seed will be saved in the "gwqs_main" object as "gwqs_main$seed".
- **family**: A description of the error distribution and link function to be used in the model. This can be a character string naming a family function (e.g., "binomial") or a family object (e.g., `binomial(link="logit")`). Currently validated families include `gaussian(link="identity")` for linear regression, `binomial()` with any accepted link function (e.g., "logit" or "probit"), `poisson(link = "log")`, `quasipoisson(link = "log")`, or "negbin" for negative binomial. The "multinomial" family is not yet supported.
- **plan_strategy**: Evaluation strategy for the plan function. You can choose among "sequential", "transparent", "multisession", "multicore", "multiprocess", "cluster" and "remote." See future::plan documentation for full details.
- **stop_if_nonsig**: if TRUE, the function will not proceed with the permutation test if the main WQS regression run produces nonsignificant p-value.
- **stop_thresh**: numeric p-value threshold required in order to proceed with the permutation test, if `stop_if_nonsig = TRUE`.
- **...**: Other parameters to put into the gwqs function call.
wqs_pt

Value

wqs_full_perm returns an object of class wqs_perm, which contains three sublists:

- **perm_test**
  - List containing: (1) pval: permutation test p-value, (2) (linear regression only) testbeta1: reference WQS regression coefficient beta1 value, (3) (linear regression only) betas: Vector of beta values from each permutation test run, (4) (logistic regression only) testpval: test reference p-value, (5) (logistic regression only) permypvals: p-values from the null models.

- **gwqs_main**
  - Main gWQS object (same as model input). This will now include an additional object "seed" that returns the seed used for this main WQS regression.

- **gwqs_perm**
  - Permutation test reference gWQS object (NULL if model family != "gaussian" or if same number of bootstraps are used in permutation test WQS regression runs as in the main run).

Examples

```
library(gWQS)

# mixture names
PCBs <- names(wqs_data)[1:17]  # half of the original 34 for quick computation

perm_test_res <- wqs_full_perm(formula = yLBX ~ wqs, data = wqs_data,
    mix_name = PCBs, q = 10, b_main = 5, b_perm = 5, b1_pos = TRUE, b1_constr = FALSE,
    niter = 3, seed = 16, plan_strategy = "multicore", stop_if_nonsig = FALSE)

# Note: The default values of b_main = 1000, b_perm = 200, and niter = 200
# are the recommended parameter values. This example has a lower b_main,
# b_perm, and niter in order to serve as a shorter test run.
```

---

wqs_pt  WQS permutation test

Description

wqs_pt takes a gwqs object as an input and runs the permutation test (Day et al. 2022) to obtain an estimate for the p-value significance for the WQS coefficient.

Usage

```
wqs_pt(
    model,
    niter = 200,
    boots = NULL,
    b1_pos = TRUE,
```
Arguments

- **model**: A gwqs object as generated from the gWQS package.
- **niter**: Number of permutation test iterations.
- **boots**: Number of bootstrap samples for each permutation test WQS regression iteration. If boots is not specified, then we will use the same bootstrap count for each permutation test WQS regression iteration as that specified in the main WQS regression run.
- **b1_pos**: A logical value that indicates whether beta values should be positive or negative.
- **b1_constr**: Logical value that determines whether to apply positive or negative constraints in the optimization function for the weight optimization.
- **rs**: A logical value indicating whether random subset implementation should be performed.
- **plan_strategy**: Evaluation strategy for the plan function. You can choose among "sequential", "transparent", "multisession", "multicore", "multiprocess", "cluster" and "remote." See future::plan documentation for full details.
- **seed**: (optional) Random seed for the permutation test WQS reference run. This should be the same random seed as used for the main WQS regression run. This seed will be saved in the "gwqs_perm" object as "gwqs_perm$seed".

Details

To use wqs_pt, we first need to run an initial WQS regression run while setting validation = 0. We will use this gwqs object as the model argument for the wqs_pt function. Note that permutation test has so far only been validated for linear WQS regression (i.e., family = "gaussian") or logistic WQS regression (i.e., family = binomial(link = "logit")), though the permutation test algorithm should also work for all WQS GLMs. Therefore, this function accepts gwqs objects made with the following families: "gaussian" or gaussian(link = "identity"), "binomial" or binomial() with any accepted link function (e.g., "logit" or "probit"), "poisson" or poisson(link="log"), "negbin" for negative binomial, and "quasipoisson" or quasipoisson(link="log"). This function cannot currently accommodate gwqs objects made with the "multinomial" family, and it is not currently able to accommodate stratified weights or WQS interaction terms (e.g., y ~ wqs * sex).

The argument boots is the number of bootstraps for the WQS regression run in each permutation test iteration. Note that we may elect a bootstrap count boots lower than that specified in the model object for the sake of efficiency. If boots is not specified, then we will use the same bootstrap count in the permutation test WQS regression runs as that specified in the model argument.

The arguments b1_pos and rs should be consistent with the inputs chosen in the model object. The seed should ideally be consistent with the seed set in the model object for consistency, though this is not required.
**Value**

`wqs_pt` returns an object of class `wqs_pt`, which contains:

- `perm_test`: List containing: (1) `pval`: permutation test p-value, (2) (linear WQS regression only) `testbeta1`: reference WQS coefficient beta1 value, (3) (linear WQS regression only) `betas`: Vector of beta values from each permutation test run, (4) (WQS GLM only) `testpval`: test reference p-value, (5) (WQS GLM only) `permpvals`: p-values from the null models.
- `gwqs_main`: Main gWQS object (same as model input).
- `gwqs_perm`: Permutation test reference gWQS object (NULL if model family != "gaussian" or if same number of bootstraps are used in permutation test WQS regression runs as in the main run).

**References**


**Examples**

```r
library(gWQS)

# mixture names
PCBs <- names(wqs_data)[1:17] #half of the original 34 for quick computation

# create reference wqs object with 5 bootstraps
wqs_main <- gwqs(yLBX ~ wqs, mix_name = PCBs, data = wqs_data, q = 10,
                 validation = 0, b = 5, b1_pos = TRUE, b1_constr = FALSE,
                 plan_strategy = "multicore", family = "gaussian", seed = 16)

# Note: We recommend niter = 1000 for the main WQS regression. This example
# has a lower number of bootstraps to serve as a shorter test run.

# run permutation test
perm_test_res <- wqs_pt(wqs_main, niter = 3, b1_pos = TRUE)

# Note: The default value of niter = 200 is the recommended parameter value.
# This example has a lower niter in order to serve as a shorter test run.
```
wqs_sim generates a simulated dataset of mixture components, covariates, and outcomes based on an initial set of specifications.

Usage

```r
wqs_sim(
  nmix = 10,
  ncovrt = 10,
  nobs = 500,
  ntruewts = 10,
  ntruecovrt = 5,
  vcov = 0,
  eps = 1,
  truewqsbeta = NULL,
  truebeta0 = NULL,
  truewts = NULL,
  truegamma = NULL,
  rnd_wqsbeta_dir = "none",
  seed = 101,
  q = 10,
  family = "gaussian"
)
```

Arguments

- **nmix**: Number of mixture components in simulated dataset.
- **ncovrt**: Number of covariates in simulated dataset.
- **nobs**: Number of observations in simulated dataset.
- **ntruewts**: Number of mixture components that have a non-zero association with the outcome (i.e., are not noise).
- **ntruecovrt**: Number of covariates that have a non-zero association with the outcome (i.e., are not noise).
- **vcov**: This parameter relates to the variance-covariance matrix of the simulated independent variables (i.e., the m exposure mixture components and z covariates). This is either a variance-covariance matrix of dimensions (m + z) x (m + z) or a single value. If this is a single value, the variance-covariance matrix will have ones on the diagonal and that single value will be all the off-diagonal values. For example, if this input were 0.4 and there were two mixture components and no covariates, the variance-covariance matrix would be matrix(c(1, 0.4, 0.4, 1), nrow = 2, ncol = 2). The default value is 0, giving a variance-covariance matrix with variances of 1 and covariances of 0.
eps Dispersion parameter. If the family is "gaussian", this corresponds to the residual standard deviation. If the family is "binomial" or "poisson", this parameter is ignored. If the family is "negbin", this represents the "size" parameter of the negative binomial distribution (see the documentation for the mbinom function for more details).

truewqsbeta Simulated WQS beta_1 value. If NULL, then this value will be randomly sampled depending on the parameter rnd_wqsbeta_dir.

truebeta0 Simulated beta_0 value. If NULL, then this value will be randomly sampled from a standard normal distribution.

truewts Simulated vector of mixture weights. If NULL, then this value will be randomly sampled from a Dirichlet distribution with a vector of alpha values all equal to 1 (see the documentation for the extraDistr::rdichlet function documentation for more details).

truegamma Simulated gamma vector. If NULL, then this value will be randomly sampled from a standard normal distribution.

rnd_wqsbeta_dir Direction of randomly sampled truewqsbeta (if truewqsbeta = NULL). The options are "positive", "negative", or NULL. If "positive" or "negative", the truewqsbeta will be sampled from a standard half normal distribution in either of those respective directions. If NULL, then truewqsbeta will be sampled from a standard normal distribution.

seed Random seed.

q Number of quantiles.

family Family for the generative model creating the outcome vector. Options include "gaussian" or gaussian(link = "identity") for a continuous outcome, "binomial" or binomial() with any accepted link function for a binary outcome, and finally for count outcomes this can be "poisson" or poisson(link="log") for the Poisson distributed outcome values, or "negbin" for negative binomial distributed outcome values.

Value

wqs_perm returns a list of:

weights Simulated weights.

coef Simulated beta coefficients.

Data Simulated dataset.

etahat predicted linear predictor (eta) values from the data generating model.

wqs Weighted quantile sum vector (quantile-transformed mixture components multiplied by weights).

modmat Model matrix.

Xq Quantile-transformed mixture components.
Examples

# For these examples, we only run a GLM using the simulated dataset
# including the simulated WQS vector just to show that the user-specified
# coefficients for beta_1 and beta_0 are returned. An example of running
# the full permutation test WQS regression for the simulated dataset
# (for which the WQS vector would be determined by the model)
# with the "gaussian" family is shown as well.

wqsform<-formula(paste("y~wqs+","C",1:10,collapse="+"))

testsim_gaussian<-wqs_sim(truewqsbeta=0.2,truebeta0=-2,
truewts=c(rep(0.15,5),rep(0.05,5)),family="gaussian")
Dat<-testsim_gaussian$Data
Dat$wqs<-testsim_gaussian$wqs
summary(glm(wqsform,data=Dat,family="gaussian"))$coef[1:2,]

testsim_logit<-wqs_sim(truewqsbeta=0.2,truebeta0=-2,
truewts=c(rep(0.15,5),rep(0.05,5)),family="binomial")
Dat<-testsim_logit$Data
Dat$wqs<-testsim_logit$wqs
summary(glm(wqsform,data=Dat,family="binomial"))$coef[1:2,]
Index

wqs_full_perm, 3
wqs_pt, 5
wqs_sim, 8
wqspt_plot, 2